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*Supplement of*

## **Coupled eco-hydrology and biogeochemistry algorithms enable the simulation of water table depth effects on boreal peatland net CO<sub>2</sub> exchange**

**Mohammad Mezbahuddin et al.**

*Correspondence to:* Mohammad Mezbahuddin ([symon.mezbahuddin@gov.ab.ca](mailto:symon.mezbahuddin@gov.ab.ca), [mezbahud@ualberta.ca](mailto:mezbahud@ualberta.ca))

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### Appendix A: Soil carbon (C), nitrogen (N) and phosphorus (P) transformations

#### Decomposition

$D_{S_{i,j,l,C}} = D'_{S_{i,j,l,C}} M_{i,d,l,C} f_{igl}(S_{i,l,C} / G_{i,l,C})$	decomposition of litter, POC, humus	[SA1a]
$D_{Z_{i,j,l,C}} = D'_{Z_{i,j,l,C}} M_{i,d,l,C} f_{igl}(Z_{i,l,C} / G_{i,l,C})$	decomposition of microbial residues	[SA1b]
$D_{A_{i,l,C}} = D'_{A_{i,l,C}} M_{i,d,l,C} f_{igl}(A_{i,l,C} / G_{i,l,C})$	decomposition of adsorbed SOC	[SA1c]
$S_{i,l,C} = \sum_j S_{i,j,l,C}$	total C in all kinetic components of litter, POC, humus	[SA2a]
$Z_{i,l,C} = \sum_j Z_{i,j,l,C}$	total C in all kinetic components of microbial residues	[SA2b]
$G_{i,l,C} = S_{i,l,C} + Z_{i,l,C} + A_{i,l,C}$	total C in substrate-microbe complexes	[SA2c]
$M_{i,d,l,C} = M_{i,a,l,C} + q_m (M_{i,a,l,C} G_{ix,l,C} - M_{ix,a,l,C} G_{i,l,C}) / (G_{ix,l,C} + G_{i,l,C})$	redistribution of active microbial biomass from each substrate-microbe complex $i$ to other substrate-microbe complexes $ix$	[SA3a]
$M_{i,a,l,C} = \sum_n M_{i,n,a,l,C}$	according to concentration differences (priming)	[SA3b]
$D'_{S_{i,j,l,C}} = \{D_{S_j,C}[S_{i,j,l,C}]\} / \{[S_{i,j,l,C}] + K_{mD}(1.0 + [\sum M_{i,d,l,C}] / K_{iD})\}$	substrate and water constraint on $D$ from colonized litter, POC and humus, microbial residues and adsorbed SOC	[SA4a]
$D'_{Z_{i,j,l,C}} = \{D_{Z_j,C}[Z_{i,j,l,C}]\} / \{[Z_{i,j,l,C}] + K_{mD}(1.0 + [M_{i,d,l,C}] / K_{iD})\}$		[SA4b]
$D'_{A_{i,l,C}} = \{D_{A,C}[A_{i,l,C}]\} / \{[A_{i,l,C}] + K_{mD}(1.0 + [M_{i,d,l,C}] / K_{iD})\}$		[SA4c]
$\delta S_{i,j,k,l,C} / \delta t = \beta \sum_n (U_{i,n,l,C} - R_{h,i,n,l,C}) (S'_{i,j,k,l,C} / S'_{i,j,l,C}) \{ (S'_{i,j,l,C} / S_{i,j,l,C}) / (S'_{i,j,l,C} / S_{i,j,l,C} + K_{is}) \}$	colonized litter determined by microbial growth into uncolonized litter	[SA5]
$f_{igl} = T_{sl} \{ e^{[B - H_a / (RT_s)]} \} / \{ 1 + e^{[(H_{dl} - ST_s) / (RT_s)]} + e^{[(ST_{sl} - H_{dh}) / (RT_s)]} \}$	Arrhenius function for $D$ and $R_h$	[SA6]

$D_{S_{i,j,l,N,P}} = D_{S_{i,j,l,C}}(S_{i,j,l,N,P}/S_{i,j,l,C})$	N and P coupled with C during $D$	[SA7a]
$D_{Z_{i,j,l,N,P}} = D_{Z_{i,j,l,C}}(Z_{i,j,l,N,P}/Z_{i,j,l,C})$		[SA7b]
$D_{A_{i,l,N,P}} = D_{A_{i,l,C}}(A_{i,l,N,P}/A_{i,l,C})$		[SA7c]
$Y_{i,l,C} = k_{ts}(G_{i,l,C} F_s[Q_{i,l,C}]^b - X_{i,l,C})$	Freundlich sorption of DOC	[SA8]
$Y_{i,l,N,P} = Y_{i,l,C}(Q_{i,l,N,P}/Q_{i,l,C})$	$(Y_{i,l,C} > 0)$ adsorption of DON, DOP	[SA9]
$Y_{i,l,N,P} = Y_{i,l,C}(X_{i,l,N,P}/X_{i,l,C})$	$(Y_{i,l,C} < 0)$ desorption of DON, DOP	[SA10]
<b>Microbial growth</b>		
$R_h = \sum_i \sum_n \sum_l R_{hi,n,l}$		[SA11]
$R_{hi,n,l} = R'_{hn} \min\{C_{Ni,n,l,a}/C_{Nj}, C_{Pi,n,l,a}/C_{Pj}\}$	$R_h$ constrained by microbial N, P	[SA12]
$R'_{hi,n,l} = M_{i,n,a,l,C} \{R_{hi,n,l} [Q_{i,l,C}]\} / \{K_{mqC} + [Q_{i,l,C}]\} f_{igl} f_{\psi gl}$	$R_h$ constrained by substrate DOC	[SA13]
$R_{hi,n,l} = R'_{hi,n,l} (U_{O2i,n,l} / U'_{O2i,n,l})$	$R_h$ constrained by $O_2$	[SA14]
$f_{\psi gl} = 1.0 - 6.67(1.0 - e^{(M\psi_s/(RT_s d))})$	$\psi_s$ constraints on microbial growth	[SA15]
$U'_{O2i,n,l} = 2.67 R'_{hi,n,l}$	$O_2$ demand driven by potential $R_h$	[SA16]
$U_{O2i,n,l} = U'_{O2i,n,l} [O_{2mi,n,l}] / ([O_{2mi,n,l}] + K_{O2})$	active uptake coupled with radial diffusion of $O_2$	[SA17a]
$= 4\pi n M_{i,n,a,l,C} D_{sO2} [r_m r_{wl} / (r_{wl} - r_m)] ([O_{2s}] - [O_{2mi,n,l}])$		[SA17b]
$R_{mi,n,j,l} = R_m M_{i,n,j,l,N} f_{tml}$		[SA18]
$f_{tml} = e^{[y(T_s) - 298.16]}$		[SA19]
$R_{gi,n,l} = R_{hi,n,l} - \sum_j R_{mi,n,j,l}$		[SA20]
$U_{i,n,l,C} = \min(R_{hi,n,l}, \sum_j R_{mi,n,j,l}) + R_{gi,n,l} (1 + \Delta G_x / E_m)$	DOC uptake driven by $R_g$	[SA21]
$U_{i,n,l,N,P} = U_{i,n,l} Q_{i,l,N,P} / Q_{i,l,C}$	DON, DOP uptake driven by $U_{i,n,l,C}$	[SA22]
$D_{Mi,n,j,l,C} = D_{Mi,j} M_{i,n,j,C} f_{tg}$	first-order decay of microbial C,	[SA23]

$$D_{M_{i,n,j},N,P} = D_{M_{i,j}} M_{i,n,j,l,N,P} f_{\text{igl}} f_{\text{di},n,N,P}$$

$$\delta M_{i,n,j,l,C} / \delta t = F_j U_{i,n,l,C} - F_j R_{hi,n,l} - D_{M_{i,n,j,l,C}}$$

$$\delta M_{i,n,j,l,C} / \delta t = F_j U_{i,n,l,C} - R_{mi,n,j,l} - D_{M_{i,n,j,l,C}}$$

### Microbial nutrient exchange

$$U_{\text{NH}_4,i,n,j,l} = (M_{i,n,j,l,C} C_{Nj} - M_{i,n,j,l,N})$$

$$U_{\text{NH}_4,i,n,j,l} = \min \{ (M_{i,n,j,l,C} C_{Nj} - M_{i,n,j,l,N}), \\ U'_{\text{NH}_4} a_{i,n,j,l} ([\text{NH}_4^+_{i,n,j,l}] - [\text{NH}_4^+_{\text{mn}}]) / ([\text{NH}_4^+_{i,n,j,l}] - [\text{NH}_4^+_{\text{mn}}] + K_{\text{NH}_4}) \}$$

$$U_{\text{NO}_3,i,n,j,l} = \min \{ (M_{i,n,j,l,C} C_{Nj} - (M_{i,n,j,l,N} + U_{\text{NH}_4,i,n,j,l})), \\ U'_{\text{NO}_3} a_{i,n,j,l} ([\text{NO}_3^-_{i,n,j,l}] - [\text{NO}_3^-_{\text{mn}}]) / ([\text{NO}_3^-_{i,n,j,l}] - [\text{NO}_3^-_{\text{mn}}] + K_{\text{NO}_3}) \}$$

$$U_{\text{PO}_4,i,n,j,l} = (M_{i,n,j,l,C} C_{Pj} - M_{i,n,j,l,P})$$

$$U_{\text{PO}_4,i,n,j,l} = \min \{ (M_{i,n,j,l,C} C_{Pj} - M_{i,n,j,l,P}), \\ U'_{\text{PO}_4} A_{i,n,j,l} ([\text{H}_2\text{PO}_4^-_{i,n,j,l}] - [\text{H}_2\text{PO}_4^-_{\text{mn}}]) / ([\text{H}_2\text{PO}_4^-_{i,n,j,l}] - [\text{H}_2\text{PO}_4^-_{\text{mn}}] + K_{\text{PO}_4}) \}$$

$$\Phi_{i,n=f,j,l} = \max \{ 0, M_{i,n=f,j,l,C} C_{Nj} - M_{i,n=f,j,l,N} - \max \{ 0, U_{i,n=f,j,l,N} \} \}$$

$$R_{\Phi_{i,n=f,j,l}} = E_{\Phi} \Phi_{i,n=f,j,l}$$

$$\delta M_{i,n,j,l,N} / \delta t = F_j U_{i,n,l,N} + U_{\text{NH}_4,i,n,j,l} + U_{\text{NO}_3,i,n,j,l} + \Phi_{i,n=f,j,l} - D_{M_{i,n,j,l,N}}$$

$$\delta M_{i,n,j,l,P} / \delta t = F_j U_{i,n,l,P} + U_{\text{PO}_4,i,n,j,l} - D_{M_{i,n,j,l,P}}$$

$$M_{i,n,a,l,C} = M_{i,n,j=\text{labile},l,C} + M_{i,n,j=\text{resistant},l,C} F_r / F_1$$

### Humification

$$H_{S_{i,j}=\text{lignin},l,C} = D_{S_{i,j}=\text{lignin},l,C}$$

$$H_{S_{i,j}=\text{lignin},l,N,P} = D_{S_{i,j}=\text{lignin},l,N,P}$$

$$H_{S_{i,j} \neq \text{lignin},l,C} = H_{S_{i,j}=\text{lignin},l,C} L_{hj}$$

$$H_{S_{i,j} \neq \text{lignin},l,N,P} = H_{S_{i,j} \neq \text{lignin},l,C} S_{i,l,N,P} / S_{i,l,C}$$

partial release of microbial N, P [SA24]

$[R_{hi,n,l} > R_{mi,n,j,l}]$  growth [SA25a]

$[R_{hi,n,l} < R_{mi,n,j,l}]$  senescence [SA25b]

$U_{\text{NH}_4} < 0$  mineralization [SA26a]

$U_{\text{NH}_4} > 0$  immobilization [SA26b]

$U_{\text{NO}_3} > 0$  immobilization [SA26c]

$U_{\text{PO}_4} < 0$  mineralization [SA26d]

$U_{\text{PO}_4} > 0$  immobilization [SA26e]

$\text{N}_2$  fixation driven by N deficit of [SA27]

diazotrophic population [SA28]

growth vs. losses of microbial N, P [SA29a]

[SA29b]

[SA30]

decomposition products of litter [SA31]

added to POC depending on lignin [SA32]

[SA33]

[SA34]

$H_{M_i,n,j,l,C} = D_{M_i,n,j,l,C} F_h$	decomposition products of	[SA35]
$H_{M_i,n,j,l,N,P} = H_{M_i,n,j,l,C} M_{i,n,j,l,N,P} / M_{i,n,j,l,C}$	microbes added to humus depending on clay	[SA36]

### Definition of variables in Appendix A

Variable	Definition	Unit	Value	Reference
<i>Subscripts</i>				
<i>i</i>	substrate-microbe complex: coarse woody litter, fine non-woody litter, POC, humus			
<i>j</i>	kinetic component: labile <i>l</i> , resistant <i>r</i> , active <i>a</i>			
<i>l</i>	soil or litter layer			
<i>n</i>	microbial functional type: heterotrophic (bacteria, fungi), autotrophic (nitrifiers, methanotrophs), diazotrophic, obligate aerobe, facultative anaerobes (denitrifiers), obligate anaerobes (methanogens)			
<i>Variables</i>				
$A_{i,l,C}$	mass of adsorbed SOC	g C m <sup>-2</sup>		
$[A_{i,l,C}]$	concentration of adsorbed SOC in soil	g C Mg <sup>-1</sup>		
<i>a</i>	microbial surface area	m <sup>2</sup> m <sup>-2</sup>		
<b><i>B</i></b>	parameter such that $f_{ig} = 1.0$ at $T_l = 298.15$ K		26.230	
<b><i>b</i></b>	Freundlich exponent for sorption isotherm		0.85	(Grant et al., 1993a, b)
<b><math>\beta</math></b>	specific colonization rate of uncolonized substrate	-	2.5	(Grant et al., 2010)
$C_{N,Pi,n,a,l}$	ratio of $M_{i,n,a,N,P}$ to $M_{i,n,a,C}$	g N or P g C <sup>-1</sup>		
$C_{N,Pj}$	maximum ratio of $M_{i,n,j,N,P}$ to $M_{i,n,j,C}$ maintained by $M_{i,n,j,C}$	g N or P g C <sup>-1</sup>	0.22 and 0.13 (N), 0.022 and 0.013 (P) for <i>j</i> = labile and resistant, respectively	(Grant et al., 1993a, b)

$D_{M_i,j}$	specific decomposition rate of $M_{i,n,j}$ at 30°C	$\text{g C g C}^{-1} \text{h}^{-1}$	0.0125 and 0.00035 for $j =$ labile and resistant, respectively	(Grant et al., 1993a, b)
$D_{M_i,n,j,l,C}$	decomposition rate of $M_{i,n,j,l,C}$	$\text{g C m}^{-2} \text{h}^{-1}$		
$D_{M_i,n,j,l,N,P}$	decomposition rate of $M_{i,n,j,l,N,P}$	$\text{g N or P m}^{-2} \text{h}^{-1}$		
$D_{sO_2l}$	aqueous dispersivity–diffusivity of $O_2$ during microbial uptake in soil	$\text{m}^2 \text{h}^{-1}$		
$D_{A_i,l,C}$	decomposition rate of $A_{i,l,C}$ by $M_{i,d,t,C}$ producing $Q$ [SA13]	$\text{g C m}^{-2} \text{h}^{-1}$		
$D_{A_j,C}$	specific decomposition rate of $A_{i,l,C}$ by $M_{i,d,t,C}$ at 25°C and saturating[ $A_{i,l,C}$ ]	$\text{g C g C}^{-1} \text{h}^{-1}$	0.025	(Grant et al., 1993a, b)
$D_{A_{i,j},l,N,P}$	decomposition rate of $A_{i,l,N,P}$ by $M_{i,d,t,C}$	$\text{g N or P m}^{-2} \text{h}^{-1}$		
$D'_{A_{i,j},l,C}$	specific decomposition rate of $S_{i,j,l,C}$ by $\Sigma_n M_{i,n,a,l}$ at 25°C	$\text{g C g C}^{-1} \text{h}^{-1}$		
$D_{S_{i,j,l,C}}$	decomposition rate of $S_{i,j,l,C}$ by $\Sigma_n M_{i,n,a,l}$ producing $Q$ [SA13]	$\text{g C m}^{-2} \text{h}^{-1}$		
$D_{S_j,C}$	specific decomposition rate of $S_{i,j,l,C}$ by $\Sigma_n M_{i,n,a,l}$ at 25°C and saturating[ $S_{i,l,C}$ ]	$\text{g C g C}^{-1} \text{h}^{-1}$	1.0, 1.0, 0.15, and 0.025 for $j =$ = protein, carbohydrate, cellulose, and lignin	(Grant et al., 1993a, b)
$D_{S_{i,j},l,N,P}$	decomposition rate of $S_{i,j,l,N,P}$ by $\Sigma_n M_{i,n,a,l}$	$\text{g N or P m}^{-2} \text{h}^{-1}$		
$D'_{S_{i,j},l,C}$	specific decomposition rate of $S_{i,j,l,C}$ by $\Sigma_n M_{i,n,a,l}$ at 25°C	$\text{g C g C}^{-1} \text{h}^{-1}$		
$D_{Z_{i,j,l,C}}$	decomposition rate of $Z_{i,j,l,C}$ by $\Sigma_n M_{i,n,a,l}$ producing $Q$ in [SA13]	$\text{g C m}^{-2} \text{h}^{-1}$		
$D_{Z_{i,j,l,N,P}}$	decomposition rate of $Z_{i,j,l,N,P}$ by $\Sigma_n M_{i,n,a,l}$	$\text{g N or P m}^{-2} \text{h}^{-1}$		
$D_{Z_j,C}$	specific decomposition rate of $Z_{i,j,l,C}$ by $\Sigma_n M_{i,n,a,l}$ at 25°C and saturating[ $Z_{i,l,C}$ ]	$\text{g C g C}^{-1} \text{h}^{-1}$	0.25 and 0.05 for $j =$ labile and resistant biomass	(Grant et al., 1993a, b)
$D'_{Z_{i,j,l,C}}$	specific decomposition rate of $Z_{i,j,l,C}$ by $\Sigma_n M_{i,n,a,l}$ at 25°C	$\text{g C g C}^{-1} \text{h}^{-1}$		

$\Delta G_x$	energy yield of C oxidation with different reductants $x$	$\text{kJ g C}^{-1}$	37.5 ( $x = \text{O}_2$ ); 4.43 ( $x = \text{DOC}$ )	
$E_m$	energy requirement for growth of $M_{i,n,a,l}$	$\text{kJ g C}^{-1}$	25	
$E_\phi$	energy requirement for non-symbiotic $\text{N}_2$ fixation by heterotrophic diazotrophs ( $n = f$ )	$\text{g C g N}^{-1}$	5	(Waring and Running, 1998)
$F_h$	fraction of products from microbial decomposition that are humified (function of clay content)		$0.167 + 0.167 \cdot \text{clay}$	
$F_l$	fraction of microbial growth allocated to labile component $M_{i,n,l}$		0.55	(Grant et al., 1993a, b)
$F_r$	fraction of microbial growth allocated to resistant component $M_{i,n,r}$		0.45	(Grant et al., 1993a, b)
$F_s$	equilibrium ratio between $Q_{i,l,C}$ and $H_{i,l,C}$			
$f_{\text{ai},n,\text{N,P}}$	fraction of N or P released with $D_{M_{i,n,j,l},C}$ during decomposition	dimensionless	0.33 $U_{\text{NH}_4} > 0$ 1.00 $U_{\text{NH}_4} < 0$ 0.33 $U_{\text{PO}_4} > 0$ 1.00 $U_{\text{PO}_4} < 0$	
$f_{\text{tg}l}$	temperature function for microbial growth respiration	dimensionless		
$f_{\text{tm}l}$	temperature function for maintenance respiration	dimensionless		
$f_{\text{wgl}}$	soil water potential function for microbial, root or mycorrhizal growth respiration	dimensionless		(Pirt, 1975)
$\Phi_{i,n=f,j,l}$	non-symbiotic $\text{N}_2$ fixation by heterotrophic diazotrophs ( $n = f$ )	$\text{g N m}^{-2} \text{h}^{-1}$		
$G_{i,l,C}$	total C in substrate-microbe complex	$\text{g C Mg}^{-1}$		
$[\text{H}_2\text{PO}_4^-]$	concentration of $\text{H}_2\text{PO}_4^-$ in soil solution	$\text{g P m}^{-3}$		

$H_a$	energy of activation	J mol <sup>-1</sup>	65 x 10 <sup>3</sup>	(Addiscott, 1983)
$H_{ah}$	energy of high temperature deactivation	J mol <sup>-1</sup>	225 x 10 <sup>3</sup>	
$H_{al}$	energy of low temperature deactivation	J mol <sup>-1</sup>	198 x 10 <sup>3</sup>	
$H_{Mi,n,j,l,C}$	transfer of microbial C decomposition products to humus	g C m <sup>-2</sup> h <sup>-1</sup>		
$H_{Mi,n,j,l,N,P}$	transfer of microbial N or P decomposition products to humus	g N or P m <sup>-2</sup> h <sup>-1</sup>		
$H_{Si,j,l,C}$	transfer of C hydrolysis products to particulate OM	g C m <sup>-2</sup> h <sup>-1</sup>		
$H_{Si,j,l,N,P}$	transfer of N or P hydrolysis products to particulate OM	g N or P m <sup>-2</sup> h <sup>-1</sup>		
$K_{iS}$	inhibition constant for microbial colonization of substrate	-	0.5	(Grant et al., 2010)
$K_{NH_4}$	M-M constant for NH <sub>4</sub> <sup>+</sup> uptake at microbial surfaces	g N m <sup>-3</sup>	0.40	
$K_{NO_3}$	M-M constant for NO <sub>3</sub> <sup>-</sup> uptake at microbial surfaces	g N m <sup>-3</sup>	0.35	
$K_{PO_4}$	M-M constant for H <sub>2</sub> PO <sub>4</sub> <sup>-</sup> uptake at microbial surfaces	g P m <sup>-3</sup>	0.125	
$K_{iD}$	inhibition constant for $[M_{i,n,a}]$ on $S_{i,C}$ , $Z_{i,C}$	g C m <sup>-3</sup>	25	(Lizama and Suzuki, 1991 ; Grant et al., 1993a, b)
$K_{mD}$	Michaelis–Menten constant for $D_{Si,j,C}$	g C Mg <sup>-1</sup>	75	
$K_{mQ_C}$	Michaelis–Menten constant for $R'_{hi,n}$ on $[Q_{i,C}]$	g C m <sup>-3</sup>	36	
$K_{O_2}$	Michaelis–Menten constant for reduction of O <sub>2s</sub> by microbes, roots and mycorrhizae	g O <sub>2</sub> m <sup>-3</sup>	0.064	(Griffin, 1972)
$k_{ts}$	equilibrium rate constant for sorption	h <sup>-1</sup>	0.01	(Grant et al., 1993a, b)
$L_{hj}$	ratio of nonlignin to lignin components in humified hydrolysis products		0.10, 0.05, and 0.05 for $j$ = protein, carbohydrate, and cellulose, respectively	(Schulten and Schnitzer, 1997)
$M$	molecular mass of water	g mol <sup>-1</sup>	18	



$M_{i,d,l,C}$	heterotrophic microbial C used for decomposition	$\text{g C m}^{-2}$	
$M_{i,n,j,l,C}$	microbial C	$\text{g C m}^{-2}$	
$M_{i,n,j,l,N}$	microbial N	$\text{g N m}^{-2}$	
$M_{i,n,j,l,P}$	microbial P	$\text{g P m}^{-2}$	
$M_{i,n,a,l,C}$	active microbial C from heterotrophic population $n$ associated with $G_{i,l,C}$	$\text{g C m}^{-2}$	
$[M_{i,n,a,l,C}]$	concentration of $M_{i,n,a}$ in soil water = $M_{i,n,a,l,C} / \theta_l$	$\text{g C m}^{-3}$	
$[\text{NH}_4^+_{i,n,j,l}]$	concentration of $\text{NH}_4^+$ at microbial surfaces	$\text{g N m}^{-3}$	
$[\text{NH}_4^+_{mn}]$	concentration of $\text{NH}_4^+$ at microbial surfaces below which $U_{\text{NH}_4} = 0$	$\text{g N m}^{-3}$	0.0125
$[\text{NO}_3^-_{i,n,j,l}]$	concentration of $\text{NO}_3^-$ at microbial surfaces	$\text{g N m}^{-3}$	
$[\text{NO}_3^-_{mn}]$	concentration of $\text{NO}_3^-$ at microbial surfaces below which $U_{\text{NO}_3} = 0$	$\text{g N m}^{-3}$	0.03
$[\text{H}_2\text{PO}_4^-_{i,n,j,l}]$	concentration of $\text{H}_2\text{PO}_4^-$ at microbial surfaces	$\text{g N m}^{-3}$	
$[\text{H}_2\text{PO}_4^-_{mn}]$	concentration of $\text{H}_2\text{PO}_4^-$ at microbial surfaces below which $U_{\text{PO}_4} = 0$	$\text{g N m}^{-3}$	0.002
$[\text{O}_{2mi,n,l}]$	$\text{O}_2$ concentration at heterotrophic microsites	$\text{g O}_2 \text{ m}^{-3}$	
$[\text{O}_{2sl}]$	$\text{O}_2$ concentration in soil solution	$\text{g O}_2 \text{ m}^{-3}$	
$Q_{i,l,C}$	$\text{DOC}$ from products of $D_{Si,j,l,C}$ [SA3] and $D_{Zi,j,l,C}$ [SA5]	$\text{g C m}^{-2}$	
$[Q_{i,l,C}]$	solution concentration of $Q_{i,l,C}$	$\text{g C Mg}^{-1}$	
$Q_{i,l,N,P}$	$\text{DON}$ and $\text{DOP}$ from products of $(D_{Si,j,l,N,P} + D_{Zi,j,l,N,P})$	$\text{g N or P m}^{-2}$	
$q_m$	constant for reallocating $M_{i,a,l,C}$ to $M_{i,d,l,C}$	-	0.5

<b>R</b>	gas constant	J mol <sup>-1</sup> K <sup>-1</sup>	8.3143	
$R_{\phi_i, n=f, j, l}$	respiration for non-symbiotic N <sub>2</sub> fixation by heterotrophic diazotrophs ( $n = f$ )	g C m <sup>-2</sup> h <sup>-1</sup>		
$R_{g_i, n, l}$	growth respiration of $M_{i, n, a, l}$ on $Q_{i, l, C}$ under nonlimiting O <sub>2</sub> and nutrients	g C g C <sup>-1</sup> h <sup>-1</sup>		
$R_h$	total heterotrophic respiration of all $M_{i, n, a, l}$ under ambient DOC, O <sub>2</sub> , nutrients, $\theta$ and temperature	g C m <sup>-2</sup> h <sup>-1</sup>		
$R_{h_i, n, l}$	heterotrophic respiration of $M_{i, n, a, l}$ under ambient DOC, O <sub>2</sub> , nutrients, $\theta$ and temperature	g C m <sup>-2</sup> h <sup>-1</sup>		
$R_{h_i, n, l}$	specific heterotrophic respiration of $M_{i, n, a, l}$ under nonlimiting O <sub>2</sub> , DOC, $\theta$ and 25°C	g C g C <sup>-1</sup> h <sup>-1</sup>		
$R_{h' n}$	specific heterotrophic respiration of $M_{i, n, a, l}$ under nonlimiting DOC, O <sub>2</sub> , nutrients, $\theta$ and 25°C	g C g C <sup>-1</sup> h <sup>-1</sup>	0.125	(Shields et al., 1973)
$R_{h' i, n, l}$	heterotrophic respiration of $M_{i, n, a, l}$ under nonlimiting O <sub>2</sub> and ambient DOC, nutrients, $\theta$ and temperature	g C m <sup>-2</sup> h <sup>-1</sup>		
$R_m$	specific maintenance respiration at 25°C	g C g N <sup>-1</sup> h <sup>-1</sup>	0.0115	(Barnes et al., 1997)
$R_{m_i, n, j, l}$	maintenance respiration by $M_{i, n, j, l}$	g C m <sup>-2</sup> h <sup>-1</sup>		
$r_{wl}$	radius of $r_m$ + water film at current water content	m		
$r_m$	radius of heterotrophic microsite	m	$2.5 \times 10^{-6}$	
$r_{wl}$	thickness of water films	m		
<b>S</b>	change in entropy	J mol <sup>-1</sup> K <sup>-1</sup>	710	(Sharpe and DeMichele, 1977)
$[S_{i, j, l, C}]$	concentration of $S_{i, j, l, C}$ in soil	g C Mg <sup>-1</sup>		
$S_{i, j, l, C}$	mass of colonized litter, POC or humus C	g C m <sup>-2</sup>		
$S'_{i, j, l, C}$	mass of uncolonized litter, POC or humus C	g C m <sup>-2</sup>		

$S_{i,j,l,N,P}$	mass of litter, POC or humus N or P	g N or P m <sup>-2</sup>	
$T_{sl}$	soil temperature	K	
$U_{i,n,C}$	uptake of $Q_{i,l,C}$ by $\sum_n M_{i,n,a,l}$ under limiting nutrient availability	g C m <sup>-2</sup> h <sup>-1</sup>	
$U_{i,n,N,P}$	uptake of $Q_{i,l,N,P}$ by $\sum_n M_{i,n,a,l}$ under limiting nutrient availability	g N or P m <sup>-2</sup> h <sup>-1</sup>	
$U_{NH_4i,n,j,l}$	NH <sub>4</sub> <sup>+</sup> uptake by microbes	g N m <sup>-2</sup> h <sup>-1</sup>	
$U'_{NH_4}$	maximum $U_{NH_4}$ at 25 °C and non-limiting NH <sub>4</sub> <sup>+</sup>	g N m <sup>-2</sup> h <sup>-1</sup>	5.0 x 10 <sup>-3</sup>
$U_{NO_3i,n,j,l}$	NO <sub>3</sub> <sup>-</sup> uptake by microbes	g N m <sup>-2</sup> h <sup>-1</sup>	
$U'_{NO_3}$	maximum $U_{NO_3}$ at 25 °C and non-limiting NO <sub>3</sub> <sup>-</sup>	g N m <sup>-2</sup> h <sup>-1</sup>	5.0 x 10 <sup>-3</sup>
$U_{O_2i,n}$	O <sub>2</sub> uptake by $M_{i,n,a,l}$ under ambient O <sub>2</sub>	g m <sup>-2</sup> h <sup>-1</sup>	
$U'_{O_2i,n}$	O <sub>2</sub> uptake by $M_{i,n,a,l}$ under nonlimiting O <sub>2</sub>	g m <sup>-2</sup> h <sup>-1</sup>	
$U_{PO_4i,n,j,l}$	H <sub>2</sub> PO <sub>4</sub> <sup>-</sup> uptake by microbes	g N m <sup>-2</sup> h <sup>-1</sup>	
$U'_{PO_4}$	maximum $U_{PO_4}$ at 25 °C and non-limiting H <sub>2</sub> PO <sub>4</sub> <sup>-</sup>	g N m <sup>-2</sup> h <sup>-1</sup>	5.0 x 10 <sup>-3</sup>
$X_{i,l,C}$	adsorbed C hydrolysis products	g C Mg <sup>-1</sup>	
$X_{i,l,N,P}$	adsorbed N or P hydrolysis products	g P Mg <sup>-1</sup>	
$y$	selected to give a $Q_{10}$ for $f_{tm}$ of 2.25		0.081
$\psi_s$	soil or residue water potential	MPa	
$Y_{i,l,C}$	sorption of C hydrolysis products	g C m <sup>-2</sup> h <sup>-1</sup>	
$Y_{i,l,N,P}$	sorption of N or P hydrolysis products	g P m <sup>-2</sup> h <sup>-1</sup>	
$[Z_{i,j,l,C}]$	concentration of $Z_{i,j,l,C}$ in soil	g C Mg <sup>-1</sup>	

$Z_{i,j,l,C}$  mass of microbial residue C in soil g C m<sup>-2</sup>

$Z_{i,j,l,N,P}$  mass of microbial residue N or P in soil g P m<sup>-2</sup>

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## Appendix B: Soil-plant water relations

### Canopy transpiration

$$Rn_{ci} + LE_{ci} + H_{ci} + G_{ci} = 0$$

$$LE_{ci} = L (e_a - e_{ci(T_{ci}, \psi_{ci}))} / r_{ai}$$

$$LE_{ci} = L (e_a - e_{ci(T_{ci}, \psi_{ci}))} / (r_{ai} + r_{ci}) - LE_{ci} \text{ [SB1b]}$$

$$H_{ci} = \rho C_p (T_a - T_{ci}) / r_{ai}$$

$$r_{cmini} = 0.64 (C_b - C_i') / V_{c'i}$$

$$r_{ci} = r_{cmini} + (r_{cmaxi} - r_{cmini}) e^{-\beta \psi_{ci}}$$

$$r_{ai} = \{ \ln((z_u - z_{di}) / z_{ti})^2 / (K^2 u_a) \} / (1 - 10 Ri)$$

$$Ri = \{ g (z_u - z_{ti}) / (u_a^2 T_a) \} (T_a - T_c)$$

$$\psi_{ci} = \psi_{ci} - \psi_{pi}$$

canopy energy balance [SB1a]

LE from canopy evaporation [SB1b]

LE from canopy transpiration [SB1c]

H from canopy energy balance [SB1d]

$r_c$  driven by rates of carboxylation [SB2a]

vs. diffusion [SB2b]

$r_c$  constrained by water status

$r_a$  driven by windspeed, surface [SB3a]

$r_a$  adjusted for stability vs. [SB3b]

buoyancy

[SB4]

### Root/moss/mycorrhizal water uptake

$$U_{wi} = \sum_l \sum_r U_{wi,r,l}$$

[SB5]

$$U_{wi,r,l} = (\psi_{c'i} - \psi_{s'l}) / (\Omega_{si,r,l} + \Omega_{ti,r,l} + \sum_x \Omega_{ai,r,l,x})$$

$U_w$  along hydraulic gradient

[SB6]

$$\psi_{c'i} = \psi_{ci} + 0.01 z_{bi}$$

[SB7]

$$\psi_{s'l} = \psi_{sl} - 0.01 z_l$$

[SB8]

$$\Omega_{si,r,l} = \ln \{ (d_{i,r,l} / r_{i,r,l}) / (2\pi L_{i,r,l} \kappa_{i,r,l}) \} \theta_{wl} / \theta_{pl}$$

[SB9]

$$\Omega_{ti,r,l} = \Omega_{vi,r,l} / L_{i,r,l}$$

[SB10]

$$\Omega_{ai,r,l,x=1} = \Omega_{ai,r} z_l / \{ n_{i,r,l,1} (r_{i,r,l,1} / r'_{i,r})^4 \} + \gamma \Omega_{ai,r} z_{bi} / \{ n_{i,r,l,1} (r_{bi} / r_{b'i})^4 \} \sum_{i,r,l} (M_{i,r,l}) / M_{i,r,l}$$

[SB11]

$$\Omega_{ai,r,l,x=2} = \Omega_{ai,r} (L_{i,r,l,2} / n_{i,r,l,2}) / \{ n_{i,r,l,2} (r_{i,r,l,2} / r'_{i,r})^4 \}$$

[SB12]

$$\delta L_{i,r,l,1} / \delta t = \delta M_{i,r,l,1} / \delta t v_r / \{ \rho_r (1 - \theta_{p,i,r}) (\pi r_{i,r,l,1}^2) \}$$

[SB13]

### Canopy water potential

$$(e_a - e_{i(T_{ci}))} / (r_{ai} + r_{ci}) \text{ [SB1]} = \sum_l \sum_r (\psi_{c'i} - \psi_{s'l}) / (\Omega_{si,r,l} + \Omega_{ti,r,l} + \sum_x \Omega_{ai,r,l,x}) + X_{ci} \delta \psi_{ci} / \delta t$$

$\psi_{ci}$  solved when transpiration from

[SB14]

[SB1-SB4] equals uptake from

[SB5-SB13] + change in storage

## Definition of variables in Appendix B

Variable	Definition	Unit	Equation	Value	Reference
<i>Subscripts</i>					
<i>I</i>	plant species or functional type: coniferous, deciduous, annual, perennial, C <sub>3</sub> , C <sub>4</sub> , monocot, dicot etc.				
<i>J</i>	branch or tiller				
<i>K</i>	Node				
<i>L</i>	soil or canopy layer				
<i>M</i>	leaf azimuth				
<i>n</i>	leaf inclination				
<i>o</i>	leaf exposure (sunlit vs. shaded)				
<i>r</i>	root/moss/mycorrhizae				
<i>Variables</i>					
$\beta$	stomatal resistance shape parameter	MPa <sup>-1</sup>	-5.0		(Grant and Flanagan, 2007)
<i>C<sub>b</sub></i>	[CO <sub>2</sub> ] in canopy air	μmol mol <sup>-1</sup>			
<i>C'<sub>i</sub></i>	[CO <sub>2</sub> ] in canopy leaves at $\psi_{c_i} = 0$ MPa	μmol mol <sup>-1</sup>	0.70 <i>C<sub>b</sub></i>		(Larcher, 2003)
<i>d<sub>i,r,l</sub></i>	half distance between adjacent roots/mosses	m			
<i>E<sub>ci</sub></i>	canopy transpiration	m <sup>3</sup> m <sup>-2</sup> h <sup>-1</sup>			
<i>e<sub>a</sub></i>	atmospheric vapor density at <i>T<sub>a</sub></i> and ambient humidity	g m <sup>-3</sup>			
<i>e<sub>ci(T<sub>ci</sub>, ψ<sub>ci</sub>)</sub></i>	canopy vapor density at <i>T<sub>ci</sub></i> and $\psi_{c_i}$	g m <sup>-3</sup>			

$G_{ci}$	canopy storage heat flux	$W m^{-2}$		
$H_{ci}$	canopy sensible heat flux	$W m^{-2}$		
$K$	von Karman's constant		0.41	
$\kappa_{i,r,l}$	hydraulic conductivity between soil and root/moss surface	$m^2 MPa^{-1} h^{-1}$		
$\gamma$	scaling factor for bole axial resistance from primary root/moss axial resistance	-	$1.6 \times 10^4$	(Grant et al., 2007)
$L$	latent heat of evaporation	$J g^{-1}$	2460	
$LE_{ci}$	latent heat flux between canopy and atmosphere	$W m^{-2}$		
$L_{i,r,l}$	length of roots/mosses/mycorrhizae	$m m^{-2}$		
$M_{i,r,l}$	mass of roots/mosses/mycorrhizae	$g m^{-2}$		
$n_{i,r,l,x}$	number of primary ( $x = 1$ ) or secondary ( $x = 2$ ) axes	$m^{-2}$		
$\Omega_{ai,r}$	axial resistivity to water transport along root/moss/mycorrhizal axes	$MPa h m^{-4}$	$4.0 \times 10^9$ deciduous $1.0 \times 10^{10}$ coniferous	(Larcher, 2003)
$\Omega_{ai,r,l,x}$	axial resistance to water transport along axes of primary ( $x = 1$ ) or secondary ( $x = 2$ ) roots/mosses/mycorrhizae	$MPa h m^{-1}$		
$\Omega_{vi,r}$	radial resistivity to water transport from surface to axis of roots/mosses/mycorrhizae	$MPa h m^{-2}$	$1.0 \times 10^4$	(Doussan et al., 1998)
$\Omega_{ii,r,l}$	radial resistance to water transport from surface to axis of roots/mosses/mycorrhizae	$MPa h m^{-1}$		
$\Omega_{si,r,l}$	radial resistance to water transport from soil to surface of roots/mosses/mycorrhizae	$MPa h m^{-1}$		
$\theta_{wl}$	soil water content	$m^3 m^{-3}$		

$\theta_{bl}$	soil porosity	$m^3 m^{-3}$		
$\theta_{p_{i,r}}$	root porosity	$m^3 m^{-3}$		
$Ri$	Richarson number			(van Bavel and Hillel, 1976)
$Rn_{ci}$	canopy net radiation	$W m^{-2}$		
$r_{ai}$	aerodynamic resistance to vapor flux from canopy	$s m^{-1}$		
$r_{bi}$	radius of bole at ambient $\psi_{c_i}$	m		
$r_{b'_i}$	radius of bole at $\psi_{c_i} = 0$ MPa	m		
$r_{ci}$	canopy stomatal resistance to vapor flux	$s m^{-1}$		
$r_{cmaxi}$	canopy cuticular resistance to vapor flux	$s m^{-1}$	$5.0 \times 10^3$	(Larcher, 2003)
$r_{cmini}$	minimum $r_{c_i}$ at $\psi_{c_i} = 0$ MPa	$s m^{-1}$		
$r_{i,r,l,x}$	radius of primary ( $x=1$ ) or secondary ( $x=2$ ) roots/mosses/mycorrhizae at ambient $\psi_{r_i l,z}$	m		
$r'_{i,r}$	radius of secondary roots/mosses/mycorrhizae at $\psi_{r_i l,z} = 0$ MPa	m	$2.0 \times 10^{-4}$ tree $1.0 \times 10^{-4}$ bush $0.05 \times 10^{-4}$ mycorrhizae	
$\rho_r$	root specific density	$g C g FW^{-1}$	0.05	(Grant, 1998)
$T_a$	air temperature	K		
$T_c$	canopy temperature	K		
$U_{wi}$	total water uptake from all rooted soil layers	$m^3 m^{-2} h^{-1}$		
$U_{wi,r,l}$	water uptake by root/moss/mycorrhizal surfaces in each soil layer	$m^3 m^{-2} h^{-1}$		



$u_a$	wind speed measured at $z_u$	$\text{m s}^{-1}$		
$V_c' i$	potential canopy $\text{CO}_2$ fixation rate at $\psi_{ci} = 0$ MPa	$\mu\text{mol m}^{-2} \text{s}^{-1}$		
$v_r$	root specific volume	$\text{m}^3 \text{g FW}^{-1}$	$10^{-6}$	(Grant, 1998)
$X_{ci}$	canopy capacitance	$\text{m}^3 \text{m}^{-2} \text{MPa}^{-1}$		
$\psi_{ci}$	canopy water potential	MPa		
$\psi_{c'i}$	$\psi_{ci} +$ canopy gravitational potential	MPa		
$\psi_{\pi i}$	canopy osmotic potential	MPa		
$\psi_{sl}$	soil water potential	MPa		
$\psi_{s'l}$	$\psi_{sl} +$ soil gravitational potential	MPa		
$\psi_{ti}$	canopy turgor potential	MPa	1.25 at $\psi_c = 0$	
$z_{bi}$	length of bole from soil surface to top of canopy	m		
$z_{di}$	canopy zero-plane displacement height	m		(Perrier, 1982)
$z_l$	depth of soil layer below surface	m		
$z_r$	canopy surface roughness	m		(Perrier, 1982)
$z_u$	height of wind speed measurement	m		

## Appendix C: Gross primary productivity and autotrophic respiration

### C<sub>3</sub> gross primary productivity

$$GPP = \sum_{i,j,k,l,m,n,o} (V_{ci,j,k,l,m,n,o} - V_{gi,j,k,l,m,n,o}) A_{i,j,k,l,m,n,o}$$

$$V_{gi,j,k,l,m,n,o} = (C_b - C_{ii,j,k,l,m,n,o}) / r_{ii,j,k,l,m,n,o}$$

$$V_{ci,j,k,l,m,n,o} = \min\{V_{bi,j,k,l,m,n,o}, V_{ji,j,k,l,m,n,o}\}$$

$$r_{ii,j,k,l,m,n,o} = r_{i\min i,j,k,l,m,n,o} + (r_{i\max i} - r_{i\min i,j,k,l,m,n,o}) e^{(-\beta\psi/t_i)}$$

$$r_{i\min i,j,k,l,m,n,o} = (C_b - C_i') / V_{ci,j,k,l,m,n,o}'$$

$$V_{bi,j,k,l,m,n,o} = V_{b\max i,j,k} (C_{ci,j,k,l,m,n,o} - \Gamma_{i,j,k}) / (C_{ci,j,k,l,m,n,o} + K_{c_i}) f_{\psi i,j,k,l,m,n,o} f_{ci}$$

$$V_{b\max i,j,k} = V_{b'} F_{rubisco_i} M_{i,j,k,prot} / A_{i,j,k} f_{tbi}$$

$$\Gamma_{i,j,k} = 0.5 O_c V_{o\max i,j,k} K_{c_i} / (V_{b\max i,j,k} K_{o_i})$$

$$V_{o\max i,j,k} = V_{o'} F_{rubisco_i} M_{i,j,k,prot} / A_{i,j,k} f_{toi}$$

$$K_{c_i} = K_{c_i} f_{tkci} (1 + O_c / (K_{o_i} f_{tkoi}))$$

$$V_{ji,j,k,l,m,n,o} = J_{i,j,k,l,m,n,o} Y_{i,j,k,l,m,n,o} f_{\psi i,j,k,l,m,n,o} f_{ci}$$

$$J_{i,j,k,l,m,n,o} = (\varepsilon I_{i,l,m,n,o} + J_{\max i,j,k} - ((\varepsilon I_{i,l,m,n,o} + J_{\max i,j,k})^2 - 4\alpha\varepsilon I_{i,l,m,n,o} J_{\max i,j,k})^{0.5}) / (2\alpha)$$

$$J_{\max i,j,k} = V_{j'} F_{chlorophyll_i} M_{i,j,k,prot} / A_{i,j,k} f_{tji}$$

$$f_{\psi i,j,k,l,m,n,o} = (r_{i\min i,j,k,l,m,n,o} / r_{ii,j,k,l,m,n,o})^{0.5}$$

solve for  $C_{ii,j,k,l,m,n,o}$  at which [SC1]

$V_{ci,j,k,l,m,n,o} = V_{gi,j,k,l,m,n,o}$   
diffusion [SC2]

carboxylation [SC3]

$r_i$  is leaf-level equivalent of  $r_c$  [SC4]

minimum  $r_i$  is driven by [SC5]

carboxylation

CO<sub>2</sub>, water, temperature and  
nutrient constraints on  $V_b$  [SC6a]

[SC6b]

[SC6c]

[SC6d]

[SC6e]

water, temperature and nutrient [SC7]

constraints on  $V_j$

[SC8a]

[SC8b]

non-stomatal effect related to [SC9]

stomatal effect

$$f_{tbi} = \exp[\mathbf{B}_v - \mathbf{H}_{av}/(RT_{ci})] / \{1 + \exp[(\mathbf{H}_{ai} - ST_{ci})/(RT_{ci})] + \exp[(ST_{ci} - \mathbf{H}_{ah})/(RT_{ci})]\}$$

Arrhenius functions for [SC10a]

$$f_{toi} = \exp[\mathbf{B}_o - \mathbf{H}_{ao}/(RT_{ci})] / \{1 + \exp[(\mathbf{H}_{ai} - ST_{ci})/(RT_{ci})] + \exp[(ST_{ci} - \mathbf{H}_{ah})/(RT_{ci})]\}$$

carboxylation, oxygenation and [SC10b]

$$f_{tji} = \exp[\mathbf{B}_j - \mathbf{H}_{aj}/(RT_{ci})] / \{1 + \exp[(\mathbf{H}_{ai} - ST_{ci})/(RT_{ci})] + \exp[(ST_{ci} - \mathbf{H}_{ah})/(RT_{ci})]\}$$

electron transport [SC10c]

$$f_{tkci} = \exp[\mathbf{B}_{kc} - \mathbf{H}_{ake}/(RT_{ci})]$$

temperature sensitivity of  $\mathbf{K}_{c_p}$ ,  $\mathbf{K}_o$ , [SC10d]

$$f_{tkoi} = \exp[\mathbf{B}_{ko} - \mathbf{H}_{ako}/(RT_{ci})]$$

[SC10e]

$$f_{iCi} = \min\{\sigma_{Ni,j}/(\sigma_{Ni,j} + \sigma_{Ci,j}/\mathbf{K}_{iC_N}), \sigma_{Pi,j}/(\sigma_{Pi,j} + \sigma_{Ci,j}/\mathbf{K}_{iC_P})\}$$

product inhibition of  $V_b$ ,  $V_j$  from [SC11]

$$\delta M_{L_{Rij,k}} / \delta t = \delta M_{L_{ij,k}} / \delta t \min\{[N'_{leaf} + (N_{leaf} - N'_{leaf})f_{iCi}]/N_{prot}, [P'_{leaf} + (P_{leaf} - P'_{leaf})f_{iCi}]/P_{prot}\}$$

$\sigma_N$  and  $\sigma_P$  vs.  $\sigma_C$  in shoots [SC12]

leaf structural protein growth [SC12]

### Autotrophic respiration

$$R_a = \sum_i \sum_j (R_{ci,j} + R_{si,j}) + \sum_i \sum_l \sum_z (R_{ci,r,l} + R_{si,r,l}) + \mathbf{E}_{N,P} (U_{NH4i,r,l} + U_{NO3i,r,l} + U_{PO4i,r,l})$$

total autotrophic respiration [SC13]

$$R_{ci,j} = \mathbf{R}_c' \sigma_{Ci,j} f_{tai}$$

$O_2$  constraint on root respiration [SC14a]

$$R_{ci,r,l} = \mathbf{R}_c' \sigma_{Ci,r,l} f_{tai,l} (U_{O2i,r,l} / U'_{O2i,r,l})$$

from active uptake coupled with [SC14b]

$$U_{O2i,r,l} = U'_{O2i,r,l} [O_{2ri,r,l}] / ([O_{2ri,r,l}] + \mathbf{K}_{O_2})$$

diffusion of  $O_2$  from soil as for [SC14c]

$$= U_{w_{i,r,l}} [O_{2sl}] + 2\pi L_{i,r,l} D_{sO_2} ([O_{2sl}] - [O_{2ri,r,l}]) \ln\{(r_{sl} + r_{ri,r,l}) / r_{ri,r,l}\}$$

and from active uptake coupled [SC14d]

$$+ 2\pi L_{i,r,l} D_{rO_2} ([O_{2qi,r,l}] - [O_{2ri,r,l}]) \ln(r_{qi,r,l} / r_{ri,r,l})$$

with diffusion of  $O_2$  from roots [SC14d]

$$U'_{O2i,r,l} = 2.67 R_{a'i,r,l}$$

[SC14e]

$$R_{si,j} = -\min\{0.0, R_{ci,j} - R_{mi,j}\}$$

remobilization when  $R_m > R_c$  [SC15]

$$R_{mi,j} = \sum_z (N_{i,j,z} \mathbf{R}_m' f_{tmi})$$

maintenance respiration [SC16]

$$R_{gi,j} = \max\{0.0, \min\{(R_{ci,j} - R_{mi,j}) \min\{1.0, \max\{0.0, \psi_{ti} - \psi_t'\}\}\}$$

growth when  $R_m < R_c$  [SC17]

### Growth and senescence

$$l_{i,j,z,C} = R_{si,j} M_{L_{N^{ij}}} / M_{L_{R^{ij}}}$$

senescence drives litterfall of non- [SC18]

remobilizable material [SC18]

$$l_{i,j,z,N} = l_{i,j,z,C} \mathbf{N}_{\text{prot}} (1.0 - \mathbf{X}_{\text{mx}} f_{\text{XNi},j})$$

$$l_{i,j,z,P} = l_{i,j,z,C} \mathbf{P}_{\text{prot}} (1.0 - \mathbf{X}_{\text{mx}} f_{\text{XPi},j})$$

$$f_{\text{XNi},j} = \sigma_{\text{Ci},j} / (\sigma_{\text{Ci},j} + \sigma_{\text{Ni},j} / \mathbf{K}_{\text{XN}})$$

litterfall of N and P is driven by [SC19a]

that of C but reduced by [SC19b]

translocation to  $\sigma_{\text{N}}$  and  $\sigma_{\text{P}}$  [SC19c]

according to ratios of  $\sigma_{\text{N}}$  and  $\sigma_{\text{P}}$  with  $\sigma_{\text{C}}$  [SC19d]

$$f_{\text{XPi},j} = \sigma_{\text{Ci},j} / (\sigma_{\text{Ci},j} + \sigma_{\text{Pi},j} / \mathbf{K}_{\text{XP}})$$

$$\delta M_{\text{Bi},j} / \delta t = \sum_z [R_{\text{gi},j} (1 - \mathbf{Y}_{\text{gi},z}) / \mathbf{Y}_{\text{gi},z}] - R_{\text{si},j} - l_{i,j,C}$$

branch growth driven by  $R_{\text{g}}$  [SC20a]

$$\delta M_{\text{Ri},r,l} / \delta t = [R_{\text{gi},r,l} (1 - \mathbf{Y}_{\text{gi},r}) / \mathbf{Y}_{\text{gi},r}] - R_{\text{si},r,l} - l_{i,r,l,C}$$

root growth driven by  $R_{\text{g}}$  [SC20b]

$$\delta A_{\text{Li},j,k,l} / \delta t = \chi (M_{\text{Li},j,k,l} / y_i)^{-0.33} \delta M_{\text{Li},j,k,l} / \delta t \min\{1, \max\{0, \psi_{\text{ti}} - \psi_{\text{t}}\}\}$$

leaf expansion driven by leaf mass growth [SC21a]

$$\delta L_{i,r,l,1} / \delta t = (\delta M_{\text{Ri},r,l,1} / \delta t) v_r / \{\rho_r (1 - \theta_{\text{P},r}) (\pi r_{\text{ti},r,l,1}^2)\}$$

root extension of primary and secondary axes driven by root mass growth [SC21b]

$$\delta L_{i,r,l,2} / \delta t = (\delta M_{\text{Ri},r,l,2} / \delta t) v_r / \{\rho_r (1 - \theta_{\text{P},r}) (\pi r_{\text{ti},r,l,2}^2)\}$$

[SC21c]

$$f_{\text{tai}} = T_{\text{ci}} \{\exp[\mathbf{B}_v - \mathbf{H}_{\text{av}} / (\mathbf{RT}_{\text{ci}})]\} / \{1 + \exp[(\mathbf{H}_{\text{al}} - \mathbf{ST}_{\text{ci}}) / (\mathbf{RT}_{\text{ci}})] + \exp[(\mathbf{ST}_{\text{ci}} - \mathbf{H}_{\text{ah}}) / (\mathbf{RT}_{\text{ci}})]\}$$

Arrhenius function for  $R_{\text{a}}$  [SC22a]

$$f_{\text{tmi}} = e^{(0.0811 * (T_{\text{ci}} - 298.15))}$$

temperature function for  $R_{\text{m}}$  [SC22b]

### Root/moss/mycorrhizal nutrient uptake

$$U_{\text{NH}_4,i,r,l} = \{U_{\text{wi},r,l} [\text{NH}_4^+] + 2\pi L_{i,r,l} D_{\text{eNH}_4} ([\text{NH}_4^+] - [\text{NH}_4^+]_{i,r,l}) / \ln(d_{i,r,l} / r_{\text{ti},r,l})\}$$

$$= U'_{\text{NH}_4} (U_{\text{O}_2,i,r,l} / U'_{\text{O}_2,i,r,l}) A_{i,r,l} ([\text{NH}_4^+]_{i,r,l} - [\text{NH}_4^+]_{\text{mn}}) / ([\text{NH}_4^+]_{i,r,l} - [\text{NH}_4^+]_{\text{mn}} + \mathbf{K}_{\text{NH}_4}) f_{\text{ti}} f_{\text{ini},r,l}$$

Root/moss/mycorrhizal N and P uptake from mass flow + diffusion coupled with active [SC23a]

$$U_{\text{NO}_3,i,r,l} = \{U_{\text{wi},r,l} [\text{NO}_3^-] + 2\pi L_{i,r,l} D_{\text{eNO}_3} ([\text{NO}_3^-] - [\text{NO}_3^-]_{i,r,l}) / \ln(d_{i,r,l} / r_{\text{ti},r,l})\}$$

[SC23b]

$$= U'_{\text{NO}_3} (U_{\text{O}_2,i,r,l} / U'_{\text{O}_2,i,r,l}) A_{i,r,l} ([\text{NO}_3^-]_{i,r,l} - [\text{NO}_3^-]_{\text{mn}}) / ([\text{NO}_3^-]_{i,r,l} - [\text{NO}_3^-]_{\text{mn}} + \mathbf{K}_{\text{NO}_3}) f_{\text{ti}} f_{\text{ini},r,l}$$

uptake of  $\text{NH}_4^+$ ,  $\text{NO}_3^-$  and  $\text{H}_2\text{PO}_4^-$  [SC23c]

constrained by  $\text{O}_2$  uptake, as for microbial N and P uptake [SA26] [SC23d]

$$U_{\text{PO}_4,i,r,l} = \{U_{\text{wi},r,l} [\text{H}_2\text{PO}_4^-] + 2\pi L_{i,r,l} D_{\text{ePO}_4} ([\text{H}_2\text{PO}_4^-] - [\text{H}_2\text{PO}_4^-]_{i,r,l}) / \ln(d_{i,r,l} / r_{\text{ti},r,l})\}$$

$$= U'_{\text{PO}_4} (U_{\text{O}_2,i,r,l} / U'_{\text{O}_2,i,r,l}) A_{i,r,l} ([\text{H}_2\text{PO}_4^-]_{i,r,l} - [\text{H}_2\text{PO}_4^-]_{\text{mn}}) / ([\text{H}_2\text{PO}_4^-]_{i,r,l} - [\text{H}_2\text{PO}_4^-]_{\text{mn}} + \mathbf{K}_{\text{PO}_4}) f_{\text{ti}} f_{\text{gl}}$$

product inhibition of  $U_{\text{NH}_4}$ ,  $U_{\text{NO}_3}$  and  $U_{\text{PO}_4}$  determined by  $\sigma_{\text{N}}$  and [SC23f]

$\sigma_{\text{P}}$  vs.  $\sigma_{\text{C}}$  in roots [SC23g]

[SC23h]

$$f_{\text{ip},r,l}$$

$$f_{\text{ini},r,l} = \sigma_{\text{Ci},r,l} / (\sigma_{\text{Ci},r,l} + \sigma_{\text{Ni},r,l} / \mathbf{K}_{\text{IN}_C})$$

$$f_{\text{ip},r,l} = \sigma_{\text{Ci},r,l} / (\sigma_{\text{Ci},r,l} + \sigma_{\text{Pi},r,l} / \mathbf{K}_{\text{IP}_C})$$

## Definition of variables in Appendix C

Variable	Definition	Unit	Value	Reference
<i>Subscripts</i>				
<i>i</i>	species or functional type: evergreen, coniferous, deciduous, annual, perennial, C <sub>3</sub> , C <sub>4</sub> , monocot, dicot, legume etc.			
<i>j</i>	branch or tiller			
<i>k</i>	Node			
<i>l</i>	soil or canopy layer			
<i>m</i>	leaf azimuth			
<i>n</i>	leaf inclination			
<i>o</i>	leaf exposure (sunlit vs. shaded)			
<i>z</i>	organ including leaf, stem, root, moss mycorrhizae			
<i>Variables</i>				
<i>A</i>	leaf, root/moss/mycorrhizal surface area	m <sup>2</sup> m <sup>-2</sup>		
<i>β</i>	shape parameter for stomatal effects on CO <sub>2</sub> diffusion and non-stomatal effects on carboxylation	MPa <sup>-1</sup>	-5.0	(Grant and Flanagan, 2007)
<i>B</i>	parameter such that $f_l = 1.0$ at $T_c = 298.15$ K		17.533	
<i>B<sub>j</sub></i>	parameter such that $f_{ijl} = 1.0$ at $T_c = 298.15$ K		17.363	
<i>B<sub>kc</sub></i>	parameter such that $f_{ikci} = 1.0$ at $T_c = 298.15$ K		22.187	
<i>B<sub>ko</sub></i>	parameter such that $f_{tkoi} = 1.0$ at $T_c = 298.15$ K		8.067	
<i>B<sub>o</sub></i>	parameter such that $f_{toi} = 1.0$ at $T_c = 298.15$ K		24.221	

$B_v$	parameter such that $f_{ivi} = 1.0$ at $T_c = 298.15$ K		26.238	
$C_b$	[CO <sub>2</sub> ] in canopy air	$\mu\text{mol mol}^{-1}$		
$C_{c(b4)}$	[CO <sub>2</sub> ] in C <sub>4</sub> bundle sheath	$\mu\text{M}$		
$C_{c(m4)}$	[CO <sub>2</sub> ] in C <sub>4</sub> mesophyll in equilibrium with $C_{i,j,k,l,m,n,o}$	$\mu\text{M}$		
$C_c$	[CO <sub>2</sub> ] in canopy chloroplasts in equilibrium with $C_{i,j,k,l,m,n,o}$	$\mu\text{M}$		
$C_{i(m4)}'$	[CO <sub>2</sub> ] in C <sub>4</sub> mesophyll air when $\psi_{ci} = 0$	$\mu\text{mol mol}^{-1}$	$0.45 \times C_b$	
$C_{i(m4)}$	[CO <sub>2</sub> ] in C <sub>4</sub> mesophyll air	$\mu\text{mol mol}^{-1}$		
$C_{i,j,z=l}$	C content of leaf ( $z = l$ )	$\text{g C m}^{-2}$		
$C_i'$	[CO <sub>2</sub> ] in canopy leaves when $\psi_{ci} = 0$	$\mu\text{mol mol}^{-1}$	$0.70 \times C_b$	(Larcher, 2003)
$C_i$	[CO <sub>2</sub> ] in canopy leaves	$\mu\text{mol mol}^{-1}$		
$D_{e \text{ NH}_4 l}$	effective dispersivity-diffusivity of NH <sub>4</sub> <sup>+</sup> during root/moss/mycorrhizal uptake	$\text{m}^2 \text{ h}^{-1}$		
$D_{e \text{ NO}_3 l}$	effective dispersivity-diffusivity of NO <sub>3</sub> <sup>-</sup> during root/moss/mycorrhizal uptake	$\text{m}^2 \text{ h}^{-1}$		
$D_{e \text{ PO}_4 l}$	effective dispersivity-diffusivity of H <sub>2</sub> PO <sub>4</sub> <sup>-</sup> during root/moss/mycorrhizal uptake	$\text{m}^2 \text{ h}^{-1}$		
$D_{rO_2}$	aqueous diffusivity of O <sub>2</sub> from root aerenchyma to root or mycorrhizal surfaces	$\text{m}^2 \text{ h}^{-1}$		
$D_{sO_2}$	aqueous diffusivity of O <sub>2</sub> from soil to root or mycorrhizal surfaces	$\text{m}^2 \text{ h}^{-1}$		
$d_{i,r,l}$	half distance between adjacent roots assumed equal to uptake path length	m	$(\pi L_{s,z} / \Delta Z)^{-1/2}$	(Grant, 1998)

$E_{N,P}$	energy cost of nutrient uptake	g C g N <sup>-1</sup> or P <sup>-1</sup>	2.15	(Veen, 1981)
$f_{C(c3)}$	C <sub>3</sub> product inhibition of RuBP carboxylation activity in C <sub>4</sub> bundle sheath or C <sub>3</sub> mesophyll	–		
$f_{C(m4)}$	C <sub>4</sub> product inhibition of PEP carboxylation activity in C <sub>4</sub> mesophyll	–		
$F_{chl}$	fraction of leaf protein in chlorophyll	-	0.025	
$f_{iC}$	N,P inhibition on carboxylation, leaf structural N,P growth	–		
$f_{iN}$	N inhibition on root/moss/mycorrhizal N uptake	–		
$f_{iP}$	P inhibition on root/moss/mycorrhizal P uptake	–		
$F_{rubisco}$	fraction of leaf protein in rubisco	-	0.125	
$f_{ta}$	temperature effect on $R_{ai,j}$	–		
$f_{tb}$	temperature effect on carboxylation	–		
$f_{tg}$	temperature function for root/moss/mycorrhizal growth respiration	dimensionless		
$f_{tj}$	temperature effect on electron transport			
$f_{tkc}$	temperature effect on $K_{c_i}$			(Bernacchi et al., 2001, 2003)
$f_{tko}$	temperature effect on $K_{o_i}$			(Bernacchi et al., 2001, 2003)
$f_{tm}$	temperature effect on $R_{mi,j}$	–	Q <sub>10</sub> = 2.25	
$f_{to}$	temperature effect on oxygenation			
$f_{tv}$	temperature effect on carboxylation	–		

$f_{xN}$	fraction of $X_{mx}$ N translocated out of leaf or root/moss during senescence	–		
$f_{xP}$	fraction of $X_{mx}$ P translocated out of leaf or root/moss during senescence	–		
$f_{\psi i}$	non-stomatal water effect on carboxylation	–		(Medrano et al., 2002)
$f_{\psi i}$	non-stomatal water effect on carboxylation	–		
$H_a$	energy of activation	J mol <sup>-1</sup>	57.5 x 10 <sup>3</sup>	
$H_{aj}$	energy of activation for electron transport	J mol <sup>-1</sup>	43 x 10 <sup>3</sup>	(Bernacchi et al., 2001, 2003)
$H_{akc}$	parameter for temperature sensitivity of $K_c$	J mol <sup>-1</sup>	55 x 10 <sup>3</sup>	(Bernacchi et al., 2001, 2003)
$H_{ako}$	parameter for temperature sensitivity of $K_o$	J mol <sup>-1</sup>	20 x 10 <sup>3</sup>	(Bernacchi et al., 2001, 2003)
$H_{ao}$	energy of activation for oxygenation	J mol <sup>-1</sup>	60 x 10 <sup>3</sup>	(Bernacchi et al., 2001, 2003)
$H_{av}$	energy of activation for carboxylation	J mol <sup>-1</sup>	65 x 10 <sup>3</sup>	(Bernacchi et al., 2001, 2003)
$H_{dh}$	energy of high temperature deactivation	J mol <sup>-1</sup>	222.5 x 10 <sup>3</sup>	
$H_{dh}$	energy of high temperature deactivation	J mol <sup>-1</sup>	220 x 10 <sup>3</sup>	
$H_{dl}$	energy of low temperature deactivation	J mol <sup>-1</sup>	198.0 x 10 <sup>3</sup>	
$H_{dl}$	energy of low temperature deactivation	J mol <sup>-1</sup>	190 x 10 <sup>3</sup>	
$I$	Irradiance	μmol m <sup>-2</sup> s <sup>-1</sup>		



$J_{(b4)}$	electron transport rate in C <sub>4</sub> bundle sheath	$\mu\text{mol m}^{-2} \text{s}^{-1}$		
$J_{(m4)}$	electron transport rate in C <sub>4</sub> mesophyll	$\mu\text{mol m}^{-2} \text{s}^{-1}$		
$J$	electron transport rate in C <sub>3</sub> mesophyll	$\mu\text{mol m}^{-2} \text{s}^{-1}$		
$J_{\text{max}}'$	specific electron transport rate at non-limiting $I$ and 25°C when $\psi_{ci} = 0$ and nutrients are nonlimiting	$\mu\text{mol g}^{-1} \text{s}^{-1}$	400	
$J_{\text{max}(b4)}$	electron transport rate in C <sub>4</sub> bundle sheath at non-limiting $I$	$\mu\text{mol m}^{-2} \text{s}^{-1}$		
$J_{\text{max}(m4)}$	electron transport rate in C <sub>4</sub> mesophyll at non-limiting $I$	$\mu\text{mol m}^{-2} \text{s}^{-1}$		
$J_{\text{max}}$	electron transport rate at non-limiting $I$ , $\psi_{ci}$ , temperature and N,P	$\mu\text{mol m}^{-2} \text{s}^{-1}$		
$K_{c(b4)}$	Michaelis-Menten constant for carboxylation in C <sub>4</sub> bundle sheath	$\mu\text{M}$	30.0 at 25°C and zero O <sub>2</sub>	(Lawlor, 1993)
$K_{c(m4)}$	Michaelis-Menten constant for carboxylation in C <sub>4</sub> mesophyll	$\mu\text{M}$	3.0 at 25°C	(Lawlor, 1993)
$K_c$	Michaelis-Menten constant for carboxylation at zero O <sub>2</sub>	$\mu\text{M}$	12.5 at 25 °C	(Farquhar et al., 1980)
$K_c$	Michaelis-Menten constant for carboxylation at ambient O <sub>2</sub>	$\mu\text{M}$		
$K_{icN}$	inhibition constant for growth in shoots from $\sigma_C$ vs. $\sigma_N$	$\text{g C g N}^{-1}$	100	(Grant, 1998)
$K_{icP}$	inhibition constant for growth in shoots from $\sigma_C$ vs. $\sigma_P$	$\text{g C g P}^{-1}$	1000	(Grant, 1998)
$K_{I/C4(b4)}$	constant for CO <sub>2</sub> product inhibition of C <sub>4</sub> decarboxylation in C <sub>4</sub> bundle sheath	$\mu\text{M}$	1000.0	

$K_{I\%C4(m4)}$	constant for C <sub>4</sub> product inhibition of PEP carboxylation activity in C <sub>4</sub> mesophyll	$\mu\text{M}$	$5 \times 10^6$	
$K_{I\nu_{lf}}$	constant for C <sub>3</sub> product inhibition of RuBP carboxylation activity in C <sub>4</sub> bundle sheath or C <sub>3</sub> mesophyll caused by $[\nu_{fi,j}]$	$\text{g C g N}^{-1}$	100	
$K_{I\pi_{lf}}$	constant for C <sub>3</sub> product inhibition of RuBP carboxylation activity in C <sub>4</sub> bundle sheath or C <sub>3</sub> mesophyll caused by $[\pi_{fi,j}]$	$\text{g C g P}^{-1}$	1000	
$K_{iN_C}$	inhibition constant for N uptake in roots/mosses from $\sigma_{C_{i,j}}$ vs. $\sigma_{N_j}$	$\text{g N g C}^{-1}$	0.1	(Grant, 1998)
$K_{iP_C}$	inhibition constant for P uptake in roots/mosses from $\sigma_{C_{i,j}}$ vs. $\sigma_{P_{i,j}}$ roots	$\text{g P g C}^{-1}$	0.01	(Grant, 1998)
$K_{NH_4}$	M-M constant for NH <sub>4</sub> <sup>+</sup> uptake at root/moss/mycorrhizal surfaces	$\text{g N m}^{-3}$	0.40	(Barber and Silberbush, 1984)
$K_{NO_3}$	M-M constant for NO <sub>3</sub> <sup>-</sup> uptake at root/moss/mycorrhizal surfaces	$\text{g N m}^{-3}$	0.35	(Barber and Silberbush, 1984)
$K_{PO_4}$	M-M constant for H <sub>2</sub> PO <sub>4</sub> <sup>-</sup> uptake root/moss/mycorrhizal surfaces	$\text{g P m}^{-3}$	0.125	(Barber and Silberbush, 1984)
$K_{O_2}$	Michaelis-Menten constant for root or mycorrhizal O <sub>2</sub> uptake	$\text{g m}^{-3}$	0.064	(Griffin, 1972)
$K_o$	inhibition constant for O <sub>2</sub> in carboxylation	$\mu\text{M}$	500 at 25 °C	(Farquhar et al., 1980)
$K_{xN}$	inhibition constant for remobilization of leaf or root/moss N during senescence	$\text{g N g C}^{-1}$	0.1	
$K_{xP}$	inhibition constant for remobilization of leaf or root/moss P during senescence	$\text{g P g C}^{-1}$	0.01	
$L$	root length	$\text{m m}^{-2}$		

$l_c$	C litterfall from leaf or root/moss	$\text{g C m}^{-2} \text{ h}^{-1}$		
$l_{N,P}$	N or P litterfall from leaf or root/moss	$\text{g C m}^{-2} \text{ h}^{-1}$		
$M_B$	branch C phytomass	$\text{g C m}^{-2}$		
$M_L$	leaf C phytomass	$\text{g C m}^{-2}$		
$M_{L_N}, M_{L_R}$	non-remobilizable, remobilizable leaf C phytomass	$\text{g C m}^{-2}$		
$M_R$	root C phytomass	$\text{g C m}^{-2}$		
$M_{iprot}$	leaf protein phytomass calculated from leaf N, P contents	$\text{g N m}^{-2}$		
N,P	N or P content of organ $z$	$\text{g N m}^{-2}$		
$N_{prot}$	N content of protein remobilized from leaf or root	$\text{g N C}^{-1}$	0.4	
$[\text{NH}_4^+_{i,r,l}]$	concentration of $\text{NH}_4^+$ at root/moss/mycorrhizal surfaces	$\text{g N m}^{-3}$		
$[\text{NH}_4^+_{mn}]$	concentration of $\text{NH}_4^+$ at root/moss/mycorrhizal surfaces below which $U_{\text{NH}_4} = 0$	$\text{g N m}^{-3}$	0.0125	(Barber and Silberbush, 1984)
$[\text{NO}_3^-_{i,r,l}]$	concentration of $\text{NO}_3^-$ at root/moss/mycorrhizal surfaces	$\text{g N m}^{-3}$		
$[\text{NO}_3^-_{mn}]$	concentration of $\text{NO}_3^-$ at root/moss/mycorrhizal surfaces below which $U_{\text{NO}_3} = 0$	$\text{g N m}^{-3}$	0.03	(Barber and Silberbush, 1984)
$[\text{H}_2\text{PO}_4^-_{i,r,l}]$	concentration of $\text{H}_2\text{PO}_4^-$ at root/moss/mycorrhizal surfaces	$\text{g N m}^{-3}$		
$[\text{H}_2\text{PO}_4^-_{mn}]$	concentration of $\text{H}_2\text{PO}_4^-$ at root/moss/mycorrhizal surfaces below which $U_{\text{PO}_4} = 0$	$\text{g N m}^{-3}$	0.002	(Barber and Silberbush, 1984)
$N_{leaf}$	maximum leaf structural N content	$\text{g N g C}^{-1}$	0.10	
$N'_{leaf}$	minimum leaf structural N content	$\text{g N g C}^{-1}$	$0.33 \times N_{leaf}$	
$N_{lf}$	total leaf N	$\text{g N m}^{-2} \text{ leaf}$		

$[N_{\text{chl}(b4)}]'$	ratio of chlorophyll N in C <sub>4</sub> bundle sheath to total leaf N	g N g N <sup>-1</sup>	0.05
$[N_{\text{chl}(m4)}]'$	ratio of chlorophyll N in C <sub>4</sub> mesophyll to total leaf N	g N g N <sup>-1</sup>	0.05
$[N_{\text{pep}(m4)}]'$	ratio of PEP carboxylase N in C <sub>4</sub> mesophyll to total leaf N	g N g N <sup>-1</sup>	0.025
$[N_{\text{rub}(b4)}]'$	ratio of RuBP carboxylase N in C <sub>4</sub> bundle sheath to total leaf N	g N g N <sup>-1</sup>	0.025
$O_{2q}$	aqueous O <sub>2</sub> concentration in root or mycorrhizal aerenchyma	g m <sup>-3</sup>	
$O_{2r}$	aqueous O <sub>2</sub> concentration at root or mycorrhizal surfaces	g m <sup>-3</sup>	
$O_{2s}$	aqueous O <sub>2</sub> concentration in soil solution	g m <sup>-3</sup>	
$O_c$	[O <sub>2</sub> ] in canopy chloroplasts in equilibrium with O <sub>2</sub> in atm.	μM	
$P_{\text{leaf}}$	maximum leaf structural P content	g P g C <sup>-1</sup>	0.10
$P'_{\text{leaf}}$	minimum leaf structural P content	g P g C <sup>-1</sup>	0.33 x $P_{\text{leaf}}$
$P_{\text{prot}}$	P content of protein remobilized from leaf or root	g P C <sup>-1</sup>	0.04
$[\pi_f]$	concentration of nonstructural root P uptake product in leaf	g P g C <sup>-1</sup>	
$\theta_P$	root or mycorrhizal porosity	m <sup>3</sup> m <sup>-3</sup>	0.1 – 0.5
$R$	gas constant	J mol <sup>-1</sup> K <sup>-1</sup>	8.3143
$R$	gas constant	J mol <sup>-1</sup> K <sup>-1</sup>	8.3143
$R_a$	total autotrophic respiration	g C m <sup>-2</sup> h <sup>-1</sup>	
$R_a'$	$R_a$ under nonlimiting O <sub>2</sub>	g C m <sup>-2</sup> h <sup>-1</sup>	
$R_c'$	specific autotrophic respiration of $\sigma_{C_i,j}$ at $T_{C_i} = 25$ °C	g C g C <sup>-1</sup> h <sup>-1</sup>	0.015

$R_c$	autotrophic respiration of $\sigma_{C_{i,j}}$ or $\sigma_{C_{i,r,l}}$	$g C m^{-2} h^{-1}$		
$R_g$	growth respiration	$g C m^{-2} h^{-1}$		
$r_{lf}$	leaf stomatal resistance	$s m^{-1}$		
$r_{lfmaxi}$	leaf cuticular resistance	$s m^{-1}$		
$r_{lfmini,j,k,l,m,n,o}$	leaf stomatal resistance when $\psi_{ci} = 0$	$s m^{-1}$		
$r_{li,j,k,l,m,n,o}$	leaf stomatal resistance	$s m^{-1}$		
$r_{lmaxi}$	leaf cuticular resistance	$s m^{-1}$		
$r_{lmini,j,k,l,m,n,o}$	leaf stomatal resistance when $\psi_{ci} = 0$	$s m^{-1}$		
$R_m'$	specific maintenance respiration of $\sigma_{C_{i,j}}$ at $T_{ci} = 25$ °C	$g C g N^{-1} h^{-1}$	0.0115	(Barnes et al., 1997)
$R_{mi,j}$	above-ground maintenance respiration	$g C m^{-2} h^{-1}$		
$r_{qi,r,l}$	radius of root aerenchyma	m		
$r_{ri,r,l}$	root/moss/mycorrhizal radius	m	$1.0 \times 10^{-4}$ or $5.0 \times 10^{-6}$	
$R_{si,j}$	respiration from remobilization of leaf C	$g C m^{-2} h^{-1}$		
$r_{sl}$	thickness of soil water films	m		
$\rho_r$	dry matter content of root/moss biomass	$g g^{-1}$	0.125	
$S$	change in entropy	$J mol^{-1} K^{-1}$	710	(Sharpe and DeMichele, 1977)
$S$	change in entropy	$J mol^{-1} K^{-1}$	710	
$\sigma_C$	nonstructural C product of CO <sub>2</sub> fixation	$g C g C^{-1}$		

$\sigma_N$	nonstructural N product of root/moss/mycorrhizal uptake	g N g C <sup>-1</sup>		
$\sigma_P$	nonstructural P product of root/moss/mycorrhizal uptake	g P g C <sup>-1</sup>		
$T_c$	canopy temperature	K		
$T_c$	canopy temperature	°C		
$U_{NH_4i,r,l}$	NH <sub>4</sub> <sup>+</sup> uptake by roots/mosses/mycorrhizae	g N m <sup>-2</sup> h <sup>-1</sup>		
$U'_{NH_4}$	maximum $U_{NH_4}$ at 25 °C and non-limiting NH <sub>4</sub> <sup>+</sup>	g N m <sup>-2</sup> h <sup>-1</sup>	5.0 x 10 <sup>-3</sup>	(Barber and Silberbush, 1984)
$U_{NO_3i,r,l}$	NO <sub>3</sub> <sup>-</sup> uptake by roots/mosses/mycorrhizae	g N m <sup>-2</sup> h <sup>-1</sup>		
$U'_{NO_3}$	maximum $U_{NO_3}$ at 25 °C and non-limiting NO <sub>3</sub> <sup>-</sup>	g N m <sup>-2</sup> h <sup>-1</sup>	5.0 x 10 <sup>-3</sup>	(Barber and Silberbush, 1984)
$U_{PO_4i,r,l}$	H <sub>2</sub> PO <sub>4</sub> <sup>-</sup> uptake by roots/mosses/mycorrhizae	g N m <sup>-2</sup> h <sup>-1</sup>		
$U'_{PO_4}$	maximum $U_{PO_4}$ at 25 °C and non-limiting H <sub>2</sub> PO <sub>4</sub> <sup>-</sup>	g N m <sup>-2</sup> h <sup>-1</sup>	5.0 x 10 <sup>-3</sup>	(Barber and Silberbush, 1984)
$U_{O_2i,r,l}$	O <sub>2</sub> uptake by roots and mycorrhizae under ambient O <sub>2</sub>	g O m <sup>-2</sup> h <sup>-1</sup>		
$U'_{O_2i,l,r}$	O <sub>2</sub> uptake by roots and mycorrhizae under nonlimiting O <sub>2</sub>	g O m <sup>-2</sup> h <sup>-1</sup>		
$U_{w_i,r,l}$	root/moss/mycorrhizal water uptake	m <sup>3</sup> m <sup>-2</sup> h <sup>-1</sup>		
$V_{\phi(b4)ij,k}$	CO <sub>2</sub> leakage from C <sub>4</sub> bundle sheath to C <sub>4</sub> mesophyll	g C m <sup>-2</sup> h <sup>-1</sup>		
$V_b'$	specific rubisco carboxylation at 25 °C	μmol g <sup>-1</sup> rubisco s <sup>-1</sup>	45	(Farquhar et al., 1980)
$V_{b(b4)ij,k}$	CO <sub>2</sub> -limited carboxylation rate in C <sub>4</sub> bundle sheath	μmol m <sup>-2</sup> s <sup>-1</sup>		
$V_{b(m4)ij,k,l,m,n,o}$	CO <sub>2</sub> -limited carboxylation rate in C <sub>4</sub> mesophyll	μmol m <sup>-2</sup> s <sup>-1</sup>		

$V_{bi,j,k,l,m,n,o}$	CO <sub>2</sub> -limited leaf carboxylation rate	$\mu\text{mol m}^{-2} \text{s}^{-1}$		
$V_{\text{bmax}(b4)'}'$	RuBP carboxylase specific activity in C <sub>4</sub> bundle sheath at 25°C when $\psi_{ci} = 0$ and nutrients are nonlimiting	$\mu\text{mol g}^{-1} \text{s}^{-1}$	75	
$V_{\text{bmax}(b4)i,j,k}$	CO <sub>2</sub> -nonlimited carboxylation rate in C <sub>4</sub> bundle sheath	$\mu\text{mol m}^{-2} \text{s}^{-1}$		
$V_{\text{bmax}(m4)'}'$	PEP carboxylase specific activity in C <sub>4</sub> mesophyll at 25°C when $\psi_{ci} = 0$ and nutrients are nonlimiting	$\mu\text{mol g}^{-1} \text{s}^{-1}$	150	
$V_{\text{bmax}(m4)i,j,k}$	CO <sub>2</sub> -nonlimited carboxylation rate in C <sub>4</sub> mesophyll	$\mu\text{mol m}^{-2} \text{s}^{-1}$		
$V_{\text{bmax}i,j,k}$	leaf carboxylation rate at non-limiting CO <sub>2</sub> , $\psi_{ci}$ , $T_c$ and N,P	$\mu\text{mol m}^{-2} \text{s}^{-1}$		
$V_{c(b4)i,j,k,l,m,n,o}$	CO <sub>2</sub> fixation rate in C <sub>4</sub> bundle sheath	$\mu\text{mol m}^{-2} \text{s}^{-1}$		
$V_{c(m4)i,j,k,l,m,n,o}$	CO <sub>2</sub> fixation rate in C <sub>4</sub> mesophyll	$\mu\text{mol m}^{-2} \text{s}^{-1}$		
$V_{c0(m4)}$ $i,j,k,l,m,n,o$	CO <sub>2</sub> fixation rate in C <sub>4</sub> mesophyll when $\psi_{ci} = 0$ MPa	$\mu\text{mol m}^{-2} \text{s}^{-1}$		
$V_{ci,j,k,l,m,n,o}$	leaf CO <sub>2</sub> fixation rate	$\mu\text{mol m}^{-2} \text{s}^{-1}$		
$V_{c'i,j,k,l,m,n,o}$	leaf CO <sub>2</sub> fixation rate when $\psi_{ci} = 0$	$\mu\text{mol m}^{-2} \text{s}^{-1}$		
$V_{g(m4)i,j,k,l,m,n,o}$	CO <sub>2</sub> diffusion rate into C <sub>4</sub> mesophyll	$\mu\text{mol m}^{-2} \text{s}^{-1}$		
$V_{gi,j,k,l,m,n,o}$	leaf CO <sub>2</sub> diffusion rate	$\mu\text{mol m}^{-2} \text{s}^{-1}$		
$V_j'$	specific chlorophyll e <sup>-</sup> transfer at 25 °C	$\mu\text{mol g}^{-1} \text{chlorophyll}$ $\text{s}^{-1}$	450	(Farquhar et al., 1980)
$V_{j(b4)i,j,k,l,m,n,o}$	irradiance-limited carboxylation rate in C <sub>4</sub> bundle sheath	$\mu\text{mol m}^{-2} \text{s}^{-1}$		

$V_{j(m4)ij,k,l,m,n,o}$	irradiance-limited carboxylation rate in C <sub>4</sub> mesophyll	$\mu\text{mol m}^{-2} \text{s}^{-1}$		
$V_{ij,k,l,m,n,o}$	irradiance-limited leaf carboxylation rate	$\mu\text{mol m}^{-2} \text{s}^{-1}$		
$V_o'$	specific rubisco oxygenation at 25 °C	$\mu\text{mol g}^{-1} \text{ rubisco s}^{-1}$	9.5	(Farquhar et al., 1980)
$V_{\text{max}ij,k}$	leaf oxygenation rate at non-limiting O <sub>2</sub> , $\psi_{ci}$ , $T_c$ and N,P	$\mu\text{mol m}^{-2} \text{s}^{-1}$		
$V_{\chi\text{C4}(b4)ij,k}$	decarboxylation of C <sub>4</sub> fixation product in C <sub>4</sub> bundle sheath	$\text{g C m}^{-2} \text{ h}^{-1}$		
$V_{\chi\text{C4}(m4)}$	transfer of C <sub>4</sub> fixation product between C <sub>4</sub> mesophyll and bundle sheath	$\text{g C m}^{-2} \text{ h}^{-1}$		
[ $V_{lf}$ ]	concentration of nonstructural root/moss/mycorrhizal N uptake product in leaf	$\text{g N g C}^{-1}$		
$v_r$	specific volume of root biomass	$\text{m}^3 \text{ g}^{-1}$		
$W_{lf(b4)}$	C <sub>4</sub> bundle sheath water content	$\text{g m}^{-2}$		
$W_{lf(m4)}$	C <sub>4</sub> mesophyll water content	$\text{g m}^{-2}$		
$X_{\text{mx}}$	maximum fraction of remobilizable N or P translocated out of leaf or root during senescence	-	0.6	(Kimmins, 2004)
$Y_{(b4)}$	carboxylation yield from electron transport in C <sub>4</sub> bundle sheath	$\mu\text{mol CO}_2 \mu\text{mol e}^{-1}$		
$Y_{(m4)}$	carboxylation yield from electron transport in C <sub>4</sub> mesophyll	$\mu\text{mol CO}_2 \mu\text{mol e}^{-1}$		
$Y_g$	fraction of $\sigma_{C_{i,j}}$ used for growth expended as $R_{g_{i,j,z}}$ by organ $z$	$\text{g C g C}^{-1}$	0.28 ( $z = \text{leaf}$ ), 0.24 ( $z = \text{root and other non-foliar}$ ), 0.20 ( $z = \text{wood}$ )	(Waring and Running, 1998)



$y$	plant population	$\text{m}^2$		
$Y$	carboxylation yield	$\mu\text{mol CO}_2 \mu\text{mol e}^{-1}$		
$\Gamma$	CO <sub>2</sub> compensation point	$\mu\text{M}$		
$\Gamma_{(b4)}$	CO <sub>2</sub> compensation point in C <sub>4</sub> bundle sheath	$\mu\text{M}$		
$\Gamma_{(m4)}$	CO <sub>2</sub> compensation point in C <sub>4</sub> mesophyll	$\mu\text{M}$		
$\alpha$	shape parameter for response of $J$ to $I$	-	0.7	
$\alpha$	shape parameter for response of $J$ to $I$	-	0.75	
$\chi$	area:mass ratio of leaf growth	$\text{m g}^{-3}$	0.0125	(Grant and Hesketh, 1992)
$\chi_{C4(b4)}$	non-structural C <sub>4</sub> fixation product in C <sub>4</sub> bundle sheath	$\text{g C m}^{-2}$		
$\chi_{C4(m4)}$	non-structural C <sub>4</sub> fixation product in C <sub>4</sub> mesophyll	$\text{g C m}^{-2}$		
$[\chi_{c3(b4)}]$	concentration of non-structural C <sub>3</sub> fixation product in C <sub>4</sub> bundle sheath	$\text{g g}^{-1}$		
$[\chi_{C4(m4)}]$	concentration of non-structural C <sub>4</sub> fixation product in C <sub>4</sub> mesophyll	$\mu\text{M}$		
$\epsilon$	quantum yield	$\mu\text{mol e}^- \mu\text{mol quanta}^{-1}$	0.45	(Farquhar et al., 1980)
$\epsilon$	quantum yield	$\mu\text{mol e}^- \mu\text{mol quanta}^{-1}$	0.45	(Farquhar et al., 1980)
$\kappa_{C4(b4)}$	conductance to CO <sub>2</sub> leakage from C <sub>4</sub> bundle sheath	$\text{h}^{-1}$	20	
$\psi_t$	canopy turgor potential	MPa	1.25 at $\psi_c = 0$	

## Appendix D: Soil water, heat and gas fluxes

5

### 6 Surface water flux

7 
$$\frac{\Delta(d_w A)}{\Delta t} = \sum_i Q_{w,in_i} + \sum_i Q_{w,out_i} + P - E_{res} - E_{surf}; \text{ kinematic wave theory of overland flow} \quad [\text{SD1}]$$

8 
$$Q_{w_i} = v_i (d_w - d_{sw}) L_i \quad [\text{SD2}]$$

9 
$$v_i = \frac{R^{0.67} S_i^{0.5}}{z_r} \quad [\text{SD3}]$$

10 
$$R = \frac{s_r d_{mw}}{s_r^2 + 1} \quad [\text{SD4}]$$

11 
$$S_i = \frac{2 \text{abs}[(Z + d_{sw} + d_{mw})_{s_i} - (Z + d_{sw} + d_{mw})_{d_i}]}{L_{s_i} + L_{d_i}} \quad [\text{SD5}]$$

12 
$$E_{res} = \frac{e_{air} - e_{res}(\psi_{res} T_{res})}{r_{a_{res}} + r_{s_{res}}} \quad [\text{SD6}]$$

13 
$$E_{surf} = \frac{e_{air} - e_{surf}(\psi_{surf} T_{surf})}{r_{a_{surf}} + r_{s_{surf}}} \quad [\text{SD7}]$$

14 Where, subscripts  $i$ =dimensions ( $i=x, y$ ),  $s$ =source cell,  $d$ =destination cell,  $in$ =flow into the grid cells, and  $out$ =flow out of the grid cells;  $d_w$ =depth of surface  
 15 water (m);  $A$ =area of landscape position ( $\text{m}^2$ );  $t$ =time (h);  $Q_w$ =surface water flux ( $\text{m}^3 \text{m}^{-2} \text{h}^{-1}$ );  $P$ =precipitation flux ( $\text{m}^3 \text{m}^{-2} \text{h}^{-1}$ );  $E_{res}$ =evaporation flux from  
 16 surface residue ( $\text{m}^3 \text{m}^{-2} \text{h}^{-1}$ );  $E_{surf}$ =evaporation flux from soil surface ( $\text{m}^3 \text{m}^{-2} \text{h}^{-1}$ );  $v$ =velocity of surface water flow ( $\text{m h}^{-1}$ );  $d_{sw}$ = maximum depth of surface  
 17 water storage (m);  $L$ =length of grid cells (m);  $R$ =ratio of cross-sectional area to perimeter of surface flow (m);  $S$ =slope ( $\text{m m}^{-1}$ );  $z_r$ =Manning's roughness  
 18 coefficient ( $=0.01 \text{ m}^{-1/3} \text{ h}$ );  $s_r$ =slope of channel sides during surface flow ( $\text{m m}^{-1}$ );  $Z$ =surface elevation (m);  $d_{sw}$ = maximum depth of surface water storage (m);  
 19  $d_{mw}$ =depth of mobile surface water (m);  $e_{air}$ =atmospheric vapour density ( $\text{g m}^{-3}$ );  $e_{res}$ =vapour density at surface residue ( $\text{g m}^{-3}$ ) at current residue water potential  
 20 ( $\psi_{res}$ ) and temperature ( $T_{res}$ );  $r_{a_{res}}$ =boundary layer resistance to evaporation from surface residue ( $\text{h m}^{-1}$ );  $r_{s_{res}}$ =surface resistance to evaporation from surface

21 residue ( $\text{h m}^{-1}$ );  $e_{\text{surf}}$ =vapour density at soil surface ( $\text{g m}^{-3}$ ) at current soil surface water potential ( $\psi_{\text{surf}}$ ) and temperature ( $T_{\text{surf}}$ );  $r_{\text{a,surf}}$  =boundary layer resistance to  
 22 evaporation from soil surface ( $\text{h m}^{-1}$ ); and  $r_{\text{s,surf}}$  =surface resistance to evaporation from soil surface ( $\text{h m}^{-1}$ ).

23 **Sub-surface water flux**

24 
$$\frac{\Delta\theta_w}{\Delta t} = \sum_i (Q_{w_{\text{mat},\text{in}_i}} + Q_{w_{\text{mac},\text{in}_i}} - Q_{w_{\text{mat},\text{out}_i}} - Q_{w_{\text{mac},\text{out}_i}}) + \sum_j (Q_{w_{b,\text{mat},\text{in}_j}} + Q_{w_{b,\text{mac},\text{in}_j}} - Q_{w_{b,\text{mat},\text{out}_j}} - Q_{w_{b,\text{mac},\text{out}_j}}) + Q_f - U_w$$
 ; 3D continuity equation for water balance of each soil layer [SD8]

25 
$$Q_{w_{\text{mat}_i}} = K'_{\text{mat}_i} (\psi_{s_s} - \psi_{s_d});$$
 soil matrix water flow [SD9]

26 
$$K'_{\text{mat}_i} = \frac{2K_{\text{mat}_{s_i}} K_{\text{mat}_{d_i}}}{K_{\text{mat}_{s_i}} L_{d_i} + K_{\text{mat}_{d_i}} L_{s_i}};$$
 when both the source and destination grid cells are either saturated or unsaturated (Richard's equation) [SD10]

27 
$$K'_{\text{mat}_i} = \frac{2K_{\text{mat}_{s_i}}}{L_{s_i} + L_{d_i}};$$
 when the source cell is saturated and the destination cell is unsaturated (Green-Ampt equation) [SD11]

28 
$$K'_{\text{mat}_i} = \frac{2K_{\text{mat}_{d_i}}}{L_{s_i} + L_{d_i}};$$
 when the source cell is unsaturated and the destination cell is saturated (Green-Ampt equation) [SD12]

29 
$$K_{\text{mat}_i} = K_{s,\text{mat}} \left( \frac{q-p+1}{q} \right)^{1.33} \left[ \frac{\sum_{p=1}^{p=q} \frac{2p-1}{\psi_p^2}}{\sum_{r=p}^{r=q} \frac{2r+1-2p}{\psi_r^2}} \right];$$
 Green and Corey (1971) model used in MCM simulation of *ecosys* [SD13]

30 
$$p = \text{Int} \left[ q \frac{(\theta_s - \theta_p)}{\theta_s} \right] + 1$$
 [SD14]

$$31 \quad n(k) = 1 + 0.001k \quad [\text{SD15}]$$

$$32 \quad m(k) = 1 - \frac{1}{n(k)} \quad [\text{SD16}]$$

$$33 \quad \alpha(k) = \frac{m(k)^{1-m(k)}}{\psi_{in}} \quad (\text{van Genuchten 1978}) \quad [\text{SD17}]$$

$$34 \quad S_{e_{fc,sim}}(k) = \left[ 1 + (\alpha(k)\psi_{fc})^{n(k)} \right]^{-m(k)} \quad (\text{van Genuchten 1980}) \quad [\text{SD18}]$$

$$35 \quad S_{e_{wp,sim}}(k) = \left[ 1 + (\alpha(k)\psi_{wp})^{n(k)} \right]^{-m(k)} \quad (\text{van Genuchten 1980}) \quad [\text{SD19}]$$

$$36 \quad \theta_r(k) = \max \left[ 0, \frac{\theta_s - \theta_{v,fc} + \theta_{v,wp}}{S_{e_{fc,sim}}(k) - S_{e_{wp,sim}}(k)} \right] \quad [\text{SD20}]$$

$$37 \quad \theta_{v,fc,sim}(k) = \theta_r(k) + [\theta_s - \theta_r(k)] S_{e_{fc,sim}}(k) \quad (\text{van Genuchten 1980}) \quad [\text{SD21}]$$

$$38 \quad \theta_{v,fc,sim}(k) = \theta_r(k) + [\theta_s - \theta_r(k)] S_{e_{fc,sim}}(k) \quad (\text{van Genuchten 1980}) \quad [\text{SD22}]$$

$$39 \quad K_{mat_i} = K_{s,mat} S_e^{0.5} \left[ 1 - \left( 1 - S_e^{\frac{1}{m}} \right)^m \right]^2; \text{ where } S_e = \frac{\theta - \theta_r}{\theta_s - \theta_r} = \left[ 1 + (\alpha\psi_m)^n \right]^{-m}; \text{ Mualem-van Genuchten model (Mualem, 1976; van Genuchten, 1980)}$$

40 used in VGM simulation of *ecosys* (Mezbahuddin et al., 2016) [SD23]

$$41 \quad K_{mat_i} = K_{s,mat} S_e^{0.5} \left[ \frac{1 - \left( 1 - (S_e S_c)^{\frac{1}{m}} \right)^m}{1 - \left( 1 - S_c^{\frac{1}{m}} \right)^m} \right]^2; \text{ where } S_e = \frac{1}{S_c} [1 + (\alpha\psi_m)^n]^{-m} \text{ and } S_c = [1 + (\alpha\psi_e)^n]^{-m}; \text{ modified Mualem-van Genuchten model (Ippisch}$$

42 et al., 2006) used in VGM simulation of *ecosys* (Mezbahuddin et al., 2016) [SD24]

43  $Q_{w_{mac_i}} = K'_{mac_i} (\psi_{g_s} - \psi_{g_d})$ ; soil macropore water flow [SD25]

44  $K'_{mac} = \frac{2K_{mac_s} K_{mac_d}}{K_{mac_s} L_{d_i} + K_{mac_d} L_{s_i}}$  [SD26]

45  $K_{mac} = N_{mac} K_{mac}^*$  [SD27]

46  $K_{mac}^* = \frac{\pi R^4}{8\eta}$ ; Hagen-Poiseuille's theory of laminar flow in tubes [SD28]

47  $N_{mac} = \theta_{mac} \pi R^2$  [SD29]

48  $Q_{w_{b,mat_j}} = \frac{K_{b,mat_j} [\psi'_b - \psi_{s_b} + 0.01(d_{z_b} - WTD_x)]}{L_{t_j}}$ ; lateral discharge occurs when  $d_{z_b} < WTD_x$  and  $\psi_{s_b} > \psi'_b + 0.01(d_{z_b} - WTD_x)$  and lateral

49 recharge occurs when  $d_{z_b} > WTD_x$  [SD30]

50  $Q_{w_{b,mac_j}} = \frac{K_{b,mac_j} 0.01[d_{z_b} - L_{z_b} (\theta_{w,mac} - 0.5) - WTD_x]}{L_{t_j}}$ ; lateral discharge occurs when  $d_{z_b} < WTD_x$  and lateral recharge occurs when  $d_{z_b} > WTD_x$

51 [SD31]

52 Where, subscripts  $i$ =dimensions ( $i=x, y, z$ ),  $j$ =dimensions ( $j=x, y$ ),  $s$ =source cell,  $d$ =destination cell,  $in$ =flow into the grid cells, and  $out$ =flow out of the grid cells;  
53  $b$ =boundary grid cell;  $mat$ =soil matrix/micropore;  $mac$ =soil macropore;  $\theta_w$ =soil water content ( $m^3 m^{-3}$ );  $Q_w$ =sub-surface water flux ( $m^3 m^{-2} h^{-1}$ );  $Q_f$ =freeze-thaw  
54 flux (a positive flux represents thaw and a negative flux represents freeze) ( $m^3 m^{-2} h^{-1}$ );  $U_w$ =total root water uptake flux ( $m^3 m^{-2} h^{-1}$ );  $K$ =hydraulic conductance  
55 ( $m MPa^{-1} h^{-1}$ );  $\psi_s$ =total soil water potential (MPa);  $K$ =hydraulic conductivity ( $m^2 MPa^{-1} h^{-1}$ );  $L$ =length of the grid cells (m);  $K_{s,mat}$ =saturated soil matrix hydraulic  
56 conductivity ( $m^2 MPa^{-1} h^{-1}$ );  $p$ =individual pore class [1,2,3,... $q$ ; where  $q$ =total number of pore classes (=100)];  $\psi_p$ =matric potential of pore class  $p$ ;  $\psi_r$ =matric  
57 potential of pore class  $r$  ( $r=p \rightarrow q$ );  $n$ =van Genuchten parameter that describes the mean slope of the desorption curve or the range of pore size distribution;  $\alpha$ =  
58 the inverse of the pressure head at the air-entry value (i.e.  $\alpha \approx 1/\text{air entry potential}$ ) that governs the shape of van Genuchten desorption curve ( $-MPa^{-1}$ );  $k$ =number  
59 of iteration (1,2,3.....19000);  $\psi_{in}$ =matric potential at inflection point ( $-MPa$ );  $S_{e_{fc,sim}}$  = simulated relative degree of saturation at field capacity;  $\psi_{fc}$ =matric  
60 potential at field capacity ( $-MPa$ );  $S_{e_{wp,sim}}$  = simulated relative degree of saturation at wilting point;  $\psi_{wp}$ =matric potential at wilting point ( $-MPa$ );  $\theta_r$ =residual soil  
61 water content ( $m^3 m^{-3}$ );  $\theta_s$ =soil water content at saturation ( $m^3 m^{-3}$ );  $\theta_{v,fc}$ =observed input for soil water content at field capacity ( $m^3 m^{-3}$ );  $\theta_{v,wp}$ =observed input

62 for soil water content at wilting point ( $\text{m}^3 \text{m}^{-3}$ );  $\theta_{v,fc_{sim}}$ =simulated soil water content at field capacity ( $\text{m}^3 \text{m}^{-3}$ );  $\theta_{v,wp_{sim}}$ =simulated soil water content at wilting  
63 point ( $\text{m}^3 \text{m}^{-3}$ );  $\theta$ =ambient soil water content ( $\text{m}^3 \text{m}^{-3}$ );  $\psi_m$ =matric potential as a function of  $\theta$  (-MPa);  $\psi_c$ =matric potential very close to saturation (= -0.0001  
64 MPa);  $\psi_g$ =gravitational soil water potential (MPa);  $N_{mac}$ =number of macropore channels ( $\text{m}^{-2}$ );  $K_{mac}^*$ =individual macropore hydraulic conductivity ( $\text{m}^4 \text{MPa}^{-1} \text{h}^{-1}$   
65 macropore channel $^{-1}$ );  $\eta$ =dynamic viscosity of water (MPa h);  $\theta_{mac}$ =volumetric macropore fraction ( $\text{m}^3 \text{m}^{-3}$ );  $R$ =radius of a macropore channel (m);  $\psi'$ =soil water  
66 potential at saturation (MPa) (=0 and -0.0005 MPa for van Genuchten and modified Campbell model respectively);  $d_z$ =depth of the mid-point of a grid cell from  
67 the surface (m);  $L_z$ =vertical thickness of a grid cell (m);  $WTD_x$ =depth of the water table depth at the adjacent watershed with which modeled grid cells exchange  
68 water laterally (m); and  $L_t$ =lateral distance over which lateral discharge/recharge occurs (m), MCM = modified Campbell model, VGM = van Genuchten model.

## 69 Water table depth

$$70 \quad WTD = -[d_{z,sat} - L_{z,sat} (1 - \frac{\theta_g}{\theta_g^*})]; \text{ negative sign represents depth below the surface of the a particular grid cell} \quad [SD32]$$

71 Where, WTD=water table depth (m);  $d_{z,sat}$ =depth to the bottom of the layer immediately above the uppermost saturated layer (m);  $L_{z,sat}$ =vertical thickness of the  
72 layer immediately above the uppermost saturated layer (m);  $\theta_g$ =current air-filled porosity of the layer immediately above the uppermost saturated layer ( $\text{m}^3 \text{m}^{-3}$ );  
73 and  $\theta_g^*$ =air-filled porosity at air-entry potential of the layer immediately above the uppermost saturated layer ( $\text{m}^3 \text{m}^{-3}$ ).

## 74 Heat flux

$$75 \quad R_n + LE + H + G = 0; \text{ energy balance for each of the canopy, snow, residue and soil surface} \quad [SD33]$$

$$76 \quad \sum G_{c,in_i} - \sum G_{c,out_i} + L_v Q_f + c(T - T_{fz}) = 0; \text{ 3D general heat flux equation in snowpack, surface residue and soil layers} \quad [SD34]$$

$$77 \quad T_{fz} = \frac{-9.095895 \times 10^4}{\psi_m - 333} \text{ (for residue layer)} = \frac{-9.095895 \times 10^4}{\psi_m + \psi_o - 333} \text{ (for soil layers)} \quad [SD35]$$

$$= T'_{fz} \text{ (for snowpack)}$$

$$78 \quad G_{c_i} = \frac{2\kappa_{s,d_i} (T_s - T_d)}{L_{s_i} + L_{d_i}} + c_{w_s} T_s Q_{w_i} \quad [SD36]$$

$$79 \quad D_{snowpack} = \frac{V_{sweq} \frac{\rho_w}{\rho_{oldsnow}} + V_{ice} + V_{water}}{A_{snowpack}} \quad [SD37]$$

$$80 \quad \rho_{oldsnow} = \min(0.5, \rho_{freshsnow} + 0.25 \frac{V_{snow}}{A_{snowpack}}) \quad [SD38]$$

81

82 Where, subscripts  $i$ =dimensions ( $i=x, y, z$ ),  $s$ =source cell,  $d$ =destination cell,  $in$ =flow into the grid cells, and  $out$ =flow out of the grid cells;  $R_n$ =net radiation ( $Wm^{-2}$ );  $LE$ =latent heat flux ( $Wm^{-2}$ );  $H$ =sensible heat flux ( $Wm^{-2}$ ); and  $G$ =ground heat flux ( $Wm^{-2}$ );  $G_c$ =conductive heat flux ( $MJ m^{-2} h^{-1}$ );  $L_v$ =latent heat of  
83 evaporation ( $=2460 MJ m^{-3}$ );  $Q_f$ =freeze-thaw flux (a positive flux represents thaw and a negative flux represents freeze) ( $m^3 m^{-2} h^{-1}$ );  $c$ =heat capacity of  
84 residue/soil layers (solid + liquid + void) or the snowpack (snow + ice + water) ( $MJ m^{-2} K^{-1}$ );  $T$ =ambient temperature of soil/residue layers or the snowpack (K);  
85  $T_{frz}$ =freezing temperature of soil/residue layers or the snowpack (K);  $\psi_m$ =matric water potential of residue/soil layers (-MPa);  $\psi_o$ =osmotic potential of soil layers  
86 (-MPa);  $T'_{frz}$ =freezing temperature of free water ( $=273.15 K$ );  $\kappa$ =thermal conductivity ( $MJ m^{-1} h^{-1} K^{-1}$ );  $L$ =length of the residue layer/ a soil layer/ the snowpack  
87 (m);  $c_w$ =heat capacity of water ( $=4.19 MJ m^{-2} K^{-1}$ );  $Q_w$ =water flux ( $m^3 m^{-2} h^{-1}$ );  $D_{snowpack}$ =depth of snowpack (m);  $V_{sweq}$ =volume of snow water equivalent ( $m^3$ );  
88  $\rho_w$ =density of water ( $=1 Mg m^{-3}$ );  $\rho_{oldsnow}$ =density of settled snow ( $Mg m^{-3}$ );  $V_{ice}$ =volume of ice in snowpack ( $m^3 m^{-3}$ );  $V_{water}$ =volume of water in snowpack ( $m^3 m^{-3}$ );  
89  $A_{snowpack}$ =snowpack basal area ( $m^2$ );  $\rho_{freshsnow}$ =density of freshly fallen snow ( $=0.083 Mg m^{-3}$ );  $V_{snow}$ =volume of snow in the snowpack ( $m^3$ )  
90

## 91 Gas flux

$$92 \quad Q_{ds\gamma_s} = \alpha_{gs_s} D_{d\gamma} \left( S'_{\gamma} f_{T_{d\gamma_s}} [\gamma_{gs}]_s - [\gamma_{ss}]_s \right); \text{ volatilization-dissolution between aqueous and gaseous phases in soil} \quad [SD39]$$

$$93 \quad Q_{dr\gamma_s} = \alpha_{gr_s} D_{d\gamma} \left( S'_{\gamma} f_{T_{d\gamma_s}} [\gamma_{gr}]_s - [\gamma_{sr}]_s \right); \text{ volatilization-dissolution between aqueous and gaseous phases in roots} \quad [SD40]$$

$$94 \quad Q_{gs\gamma_{surf}} = g_{a,surf} \left\{ [\gamma_a] - \left\{ 2[\gamma_{gs}]_{surf} D_{gs\gamma_{surf}} / L_{surf} + g_{a,surf} [\gamma_a] \right\} / \left\{ 2D_{gs\gamma_{surf}} / L_{surf} + g_{a,surf} \right\} \right\}; \text{ convective-conductive gas flux between soil surface} \\ 95 \text{ and the atmosphere} \quad [SD41]$$

$$96 \quad Q_{gs\gamma_i} = -Q_{wi} [\gamma_{gs}]_s + \frac{2D_{gs\gamma_i} \left( [\gamma_{gs}]_s - [\gamma_{gs}]_d \right)}{L_{s_i} + L_{d_i}}; \text{ 3D convective-conductive gas flux between two adjacent grid cells} \quad [SD42]$$

97 
$$Q_{gr\gamma_{i=z}} = \frac{D_{gr\gamma_{i=z}} \left( [\gamma_{gr}]_d - [\gamma_a] \right)}{\sum_{l,i=z} L_{d_{i=z}}};$$
 convective-conductive gas flux between root and the atmosphere [SD43]

98 
$$D_{gs\gamma_i} = \frac{D'_{g\gamma} f_{T_{g_s}} \left[ 0.5 \left( \theta_{g_s} + \theta_{g_d} \right) \right]^2}{\theta_{p_s}^{0.67}};$$
 3D gaseous diffusivity between two adjacent grid cells as functions of air-filled porosities in those cells [SD44]

99 
$$D_{gr\gamma_{i=z}} = \frac{D'_{g\gamma} f_{T_{g_s}} \theta_{pr_s}^{1.33} A_{r_s}}{A_{i=x,y}};$$
 gaseous diffusivity as a function of air-filled porosity in the roots/mycorrhizae [SD45]

100 Where, subscripts  $i$ =dimensions ( $i=x, y, z$ ),  $s$ =source cell,  $d$ =destination cell,  $surf$ =soil surface layer;  $Q_{ds\gamma}$ =volatilization – dissolution of gas  $\gamma$  between aqueous  
101 and gaseous phases in soil ( $\text{g m}^{-2} \text{h}^{-1}$ );  $\alpha_{gs}$ =air-water interfacial area in soil ( $\text{m}^2 \text{m}^{-2}$ );  $D_{dr}$ = volatilization - dissolution transfer coefficient for gas  $\gamma$  ( $\text{m}^2 \text{h}^{-1}$ );  $S'_\gamma$   
102 =Ostwald solubility coefficient of gas  $\gamma$  at 30°C (0.0293 for  $\gamma = \text{O}_2$ ) (Wilhelm et al., 1977);  $f_{T_{d,\gamma}}$ =temperature dependence of  $S'_\gamma$  (Wilhelm et al., 1977);  
103  $[\gamma_{gs}]$ =gaseous concentration of gas  $\gamma$  in soil ( $\text{g m}^{-3}$ );  $[\gamma_{ss}]$ = aqueous concentration of gas  $\gamma$  in soil ( $\text{g m}^{-3}$ );  $Q_{dr}$ = volatilization – dissolution of gas  $\gamma$  between  
104 aqueous and gaseous phases in root/moss ( $\text{g m}^{-2} \text{h}^{-1}$ );  $\alpha_{gr}$ = air-water interfacial area in root/mycorrhizae ( $\text{m}^2 \text{m}^{-2}$ ) (Skopp, 1985);  $[\gamma_{gr}]$ = gaseous concentration of  
105 gas  $\gamma$  in root/mycorrhizae ( $\text{g m}^{-3}$ );  $[\gamma_{sr}]$ = aqueous concentration of gas  $\gamma$  in root/moss/mycorrhizae ( $\text{g m}^{-3}$ );  $Q_{gs\gamma}$ = gaseous flux of gas  $\gamma$  in soil ( $\text{g m}^{-2} \text{h}^{-1}$ );  $Q_w$ =sub-  
106 surface water flux ( $\text{m}^3 \text{m}^{-2} \text{h}^{-1}$ );  $D_{gs\gamma}$ =gaseous diffusivity of gas  $\gamma$  in soil ( $\text{m}^2 \text{h}^{-1}$ ) (Millington and Quirk, 1960);  $L$ =thickness of grid cells (m);  $Q_{gr\gamma}$ =gaseous flux of  
107 gas  $\gamma$  between root/mycorrhizae and the atmosphere ( $\text{m}^2 \text{h}^{-1}$ );  $D_{gr}$ =gaseous diffusivity of gas  $\gamma$  in root/mycorrhizae ( $\text{m}^2 \text{h}^{-1}$ ) (Luxmoore et al., 1970a,b);  $g_a$ =  
108 boundary layer conductance ( $\text{m h}^{-1}$ );  $[\gamma_a]$ =atmospheric concentration of gas  $\gamma$  ( $\text{g m}^{-3}$ );  $D'_{g\gamma}$ =diffusivity of gas  $\gamma$  in air at 0°C ( $\text{m}^2 \text{h}^{-1}$ ) ( $6.43 \times 10^{-2} \text{m}^2 \text{h}^{-1}$  for  $\gamma = \text{O}_2$ )  
109 (Campbell, 1985);  $f_{T_g}$ =temperature dependence of  $D'_{g\gamma}$  (Campbell, 1985);  $\theta_g$ =air-filled porosity ( $\text{m}^3 \text{m}^{-3}$ );  $\theta_p$ =total porosity of soil ( $\text{m}^3 \text{m}^{-3}$ );  $\theta_{pr}$ =  
110 root/mycorrhizal porosity representing aerenchyma fraction ( $\text{m}^3 \text{m}^{-3}$ );  $A_r$ = root cross-sectional area ( $\text{m}^2$ ); and  $A$ =area of landscape position ( $\text{m}^2$ ).



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202 **Table S1.** Statistics from regressions between hourly modelled and gap-filled CO<sub>2</sub> fluxes from  
 203 2004-2009 at a Western Canadian fen peatland

<b>(a)</b> Regressions of modelled vs. gap-filled net ecosystem CO <sub>2</sub> fluxes over whole years of 2004-2008 <sup>a</sup>						
Year	Total annual precipitation (mm)	<i>n</i>	<i>a</i>	<i>b</i>	<i>R</i> <sup>2</sup>	RMSE (μmol m <sup>-2</sup> s <sup>-1</sup> )
2004	553	3750	-0.13	1.20	0.89	0.64
2005	387	2807	-0.49	1.03	0.76	0.82
2006	465	2748	-0.48	1.15	0.81	0.58
2007	431	3375	-0.36	0.97	0.74	1.23
2008	494	2941	-0.54	1.05	0.79	0.95
<b>(b)</b> Regressions of modelled vs. gap-filled net ecosystem CO <sub>2</sub> fluxes over growing seasons (May-August) of 2004-2009						
Year	Total growing season precipitation (mm)	<i>n</i>	<i>a</i>	<i>b</i>	<i>R</i> <sup>2</sup>	RMSE (μmol m <sup>-2</sup> s <sup>-1</sup> )
2004	287	837	-0.01	1.21	0.87	1.22
2005	276	680	-0.57	1.07	0.75	1.26
2006	253	773	-1.70	0.95	0.73	0.78
2007	237	1058	-0.51	0.98	0.76	1.88
2008	276	810	-1.04	1.02	0.79	1.62
2009	138	1010	-0.02	0.98	0.87	1.20

204 (*a*, *b*) from simple linear regressions of modelled on gap-filled, and *R*<sup>2</sup> = coefficient of  
 205 determination; RMSE = root mean square for errors from simple linear regressions of gap-  
 206 filled on simulated; <sup>a</sup> whole year modelled vs. gap-filled CO<sub>2</sub> flux regression for 2009  
 207 could not be done due to the lack of gap-filling (arose from long gap in measurements)  
 208 from September to December in that year.