



Supplement of

Validation of demographic equilibrium theory against tree-size distributions and biomass density in Amazonia

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1 Tables

Table S1: Coefficients for Allometry Equation from Feldpausch 2012

Region	a_h	b_h	c_h
All S.America	42.574	0.0482	0.8307
Western Regions	46.263	0.0876	0.6072
Brazilian Shield	227.35	0.0139	0.555
Guyana Shield	42.845	0.0433	0.9372
Eastern-Central	48.131	0.0375	0.8228

Table S2: Principal Investigators of Data Collection Teams for Each Forest Plot Used

Plot Code	Principal Investigators
ALF_01	Jon Lloyd, Ted Feldpausch
ALF_02	Jon Lloyd, Ted Feldpausch
ALM_01	John Terborgh, Oliver Phillips, Roel Brienen
ALP_01	Abel Monteagudo-Mendoza, Javier Silva Espejo, Oliver Phillips, Rodolfo Vasquez Martinez, Roel Brienen, Yadvinder Malhi
ALP_02	Abel Monteagudo-Mendoza, Oliver Phillips, Rodolfo Vasquez Martinez, Roel Brienen
ALP_30	Abel Monteagudo-Mendoza, Javier Silva Espejo, Oliver Phillips, Rodolfo Vasquez Martinez, Roel Brienen, Yadvinder Malhi
ALP_40	Abel Monteagudo-Mendoza, Freddy Ramirez Arevalo, Oliver Phillips, Roel Brienen
AMA_02	Esteban Álvarez Dávila, Irina Mendoza Polo, Oliver Phillips
BAC_01	Emilio Vilanova Torre, Geertje van der Heijden, Hirma Ramírez-Angulo, Oliver Phillips
BAC_02	Emilio Vilanova Torre, Geertje van der Heijden, Hirma Ramírez-Angulo, Oliver Phillips
BAC_03	Emilio Vilanova Torre, Geertje van der Heijden, Hirma Ramírez-Angulo, Oliver Phillips
BAC_04	Emilio Vilanova Torre, Geertje van der Heijden, Hirma Ramírez-Angulo, Oliver Phillips
BAC_05	Emilio Vilanova Torre, Geertje van der Heijden, Hirma Ramírez-Angulo, Oliver Phillips
BAC_06	Emilio Vilanova Torre, Geertje van der Heijden, Hirma Ramírez-Angulo, Oliver Phillips
BEE_01	Alexander Parada Gutierrez, Luzmila Arroyo, Oliver Phillips
BEE_05	Alexander Parada Gutierrez, Luzmila Arroyo, Oliver Phillips
BES_01	Esteban Álvarez Dávila, Irina Mendoza Polo, Oliver Phillips
BET_01	Esteban Álvarez Dávila, Irina Mendoza Polo, Oliver Phillips
BET_02	Esteban Álvarez Dávila, Irina Mendoza Polo, Oliver Phillips
BOG_01	Abel Monteagudo-Mendoza, David Neill, Oliver Phillips
BOG_02	David Neill, Oliver Phillips
CAI_04	Emilio Vilanova Torre, Geertje van der Heijden, Hirma Ramírez-Angulo, Oliver Phillips
CAX_01	Oliver Phillips, Samuel Almeida
CAX_02	Oliver Phillips, Samuel Almeida
CAX_06	Luiz Aragão, Oliver Phillips, Samuel Almeida, Yadvinder Malhi
CAX_08	Luiz Aragão, Oliver Phillips, Samuel Almeida, Yadvinder Malhi
CLA_03	Emilio Vilanova Torre, Geertje van der Heijden, Hirma Ramírez-Angulo, Oliver Phillips
CLA_04	Emilio Vilanova Torre, Geertje van der Heijden, Hirma Ramírez-Angulo, Oliver Phillips
CRP_02	Alejandro Araujo-Murakami, Luzmila Arroyo, Oliver Phillips, Roel Brienen
CUZ_01	Abel Monteagudo-Mendoza, Oliver Phillips
CUZ_02	Abel Monteagudo-Mendoza, Oliver Phillips
CUZ_03	Abel Monteagudo-Mendoza, Oliver Phillips
CUZ_04	Abel Monteagudo-Mendoza, Oliver Phillips
DIV_01	Esteban Álvarez Dávila, Irina Mendoza Polo, Oliver Phillips
DOI_01	Marcos Silveira, Oliver Phillips, Ted Feldpausch
ECE_01	Esteban Álvarez Dávila, Irina Mendoza Polo, Oliver Phillips
ECE_02	Esteban Álvarez Dávila, Irina Mendoza Polo
ELD_01	Emilio Vilanova Torre, Geertje van der Heijden, Hirma Ramírez-Angulo, Oliver Phillips
ELD_02	Emilio Vilanova Torre, Geertje van der Heijden, Hirma Ramírez-Angulo, Oliver Phillips
ELD_03	Emilio Vilanova Torre, Geertje van der Heijden, Hirma Ramírez-Angulo, Oliver Phillips
ELD_04	Emilio Vilanova Torre, Geertje van der Heijden, Hirma Ramírez-Angulo, Oliver Phillips
ESP_01	Miles Silman, William Farfan-Rios
HCC_21	Luzmila Arroyo, Oliver Phillips, Roel Brienen
HCC_22	Alejandro Araujo-Murakami, Luzmila Arroyo, Oliver Phillips, Roel Brienen
HCC_24	Alejandro Araujo-Murakami, Luzmila Arroyo, Oliver Phillips, Roel Brienen
JAS_02	David Neill, Oliver Phillips, Roel Brienen
JAS_03	David Neill, Roel Brienen
JAS_04	David Neill, Oliver Phillips, Roel Brienen
JEN_11	Abel Monteagudo-Mendoza, Eurídice Honorio Coronado, Oliver Phillips, Roel Brienen

Plot Code	Principal Investigators
JEN_12	Eurídice Honorio Coronado, Oliver Phillips, Roel Brienen
JFR_01	Ted Feldpausch
JFR_02	Ted Feldpausch
JFR_03	Ted Feldpausch
JFR_04	Ted Feldpausch
JFR_05	Ted Feldpausch
JFR_06	Ted Feldpausch
JFR_07	Ted Feldpausch
JFR_08	Ted Feldpausch
JFR_09	Ted Feldpausch
KAL_01	Esteban Álvarez Dávila, Irina Mendoza Polo, Oliver Phillips
LAS_02	Fernando Cornejo Valverde, Nigel Pitman, Oliver Phillips
LFB_01	Alejandro Araujo-Murakami, Luzmila Arroyo, Oliver Phillips, Roel Brienen, Timothy Killeen
LFB_02	Alejandro Araujo-Murakami, Luzmila Arroyo, Oliver Phillips, Roel Brienen
LSL_01	Alejandro Araujo-Murakami, Luzmila Arroyo, Oliver Phillips, Roel Brienen
LSL_02	Alejandro Araujo-Murakami, Luzmila Arroyo, Oliver Phillips, Roel Brienen
MIN_01	Marcos Silveira, Oliver Phillips, Ted Feldpausch
MNU_05	John Terborgh, Oliver Phillips, Roel Brienen
MNU_06	Fernando Cornejo Valverde, John Terborgh, Oliver Phillips, Roel Brienen
MTH_01	Marcos Silveira, Oliver Phillips, Ted Feldpausch
PNY_01	Abel Monteagudo-Mendoza, Oliver Phillips, Rodolfo Vasquez Martinez
PNY_02	Abel Monteagudo-Mendoza, Oliver Phillips, Rodolfo Vasquez Martinez
PNY_03	Abel Monteagudo-Mendoza, Oliver Phillips, Rodolfo Vasquez Martinez
PNY_04	Abel Monteagudo-Mendoza, Oliver Phillips, Rodolfo Vasquez Martinez
PNY_05	Abel Monteagudo-Mendoza, Oliver Phillips, Rodolfo Vasquez Martinez
PNY_06	Abel Monteagudo-Mendoza, Nadir Pallqui Camacho, Oliver Phillips, Rodolfo Vasquez Martinez
PNY_07	Abel Monteagudo-Mendoza, Oliver Phillips, Rodolfo Vasquez Martinez
POR_01	Marcos Silveira, Oliver Phillips, Ted Feldpausch
POR_02	Oliver Phillips, Ted Feldpausch
PTN_01	Esteban Álvarez Dávila, Oliver Phillips, Zorayda Restrepo Correa
RAS_01	Esteban Álvarez Dávila, Irina Mendoza Polo, Oliver Phillips
RCS_01	Abel Monteagudo-Mendoza, Luis Valenzuela Gamarra, Oliver Phillips
RCS_02	Abel Monteagudo-Mendoza, Luis Valenzuela Gamarra, Oliver Phillips
RCS_03	Abel Monteagudo-Mendoza, Luis Valenzuela Gamarra, Oliver Phillips
RET_05	Alejandro Araujo-Murakami, Guido Pardo, Oliver Phillips, Roel Brienen, Vincent Vos
RET_06	Alejandro Araujo-Murakami, Guido Pardo, Oliver Phillips, Roel Brienen, Vincent Vos
RET_08	Alejandro Araujo-Murakami, Guido Pardo, Oliver Phillips, Roel Brienen, Vincent Vos
RET_09	Alejandro Araujo-Murakami, Guido Pardo, Oliver Phillips, Roel Brienen, Vincent Vos
RFH_01	Marcos Silveira, Oliver Phillips, Ted Feldpausch
RIO_01	Emilio Vilanova Torre, Geertje van der Heijden, Hirma Ramírez-Angulo, Oliver Phillips
RIO_02	Emilio Vilanova Torre, Geertje van der Heijden, Hirma Ramírez-Angulo, Oliver Phillips
RST_01	Jorcely Barroso, Marcos Silveira, Oliver Phillips, Ted Feldpausch
SCT_01	Alexander Parada Gutierrez, Casimiro Mendoza, Luzmila Arroyo, Oliver Phillips
SCT_06	Alexander Parada Gutierrez, Casimiro Mendoza, Luzmila Arroyo, Oliver Phillips
SEU_01	Emilio Vilanova Torre, Geertje van der Heijden, Hirma Ramírez-Angulo, Oliver Phillips
SEU_02	Emilio Vilanova Torre, Geertje van der Heijden, Hirma Ramírez-Angulo, Oliver Phillips
SEU_03	Emilio Vilanova Torre, Geertje van der Heijden, Hirma Ramírez-Angulo, Oliver Phillips
SEU_04	Geertje van der Heijden, Hirma Ramírez-Angulo, Oliver Phillips
SEU_05	Emilio Vilanova Torre, Geertje van der Heijden, Hirma Ramírez-Angulo, Oliver Phillips
SEU_06	Emilio Vilanova Torre, Geertje van der Heijden, Hirma Ramírez-Angulo, Oliver Phillips
SUC_01	Abel Monteagudo-Mendoza, Oliver Phillips, Rodolfo Vasquez Martinez, Roel Brienen
SUC_02	Abel Monteagudo-Mendoza, Oliver Phillips, Rodolfo Vasquez Martinez, Roel Brienen
SUC_03	Abel Monteagudo-Mendoza, Roel Brienen
SUC_04	Abel Monteagudo-Mendoza, Oliver Phillips, Rodolfo Vasquez Martinez, Roel Brienen
SUC_05	Abel Monteagudo-Mendoza, Oliver Phillips, Rodolfo Vasquez Martinez, Roel Brienen
TAM_01	Abel Monteagudo-Mendoza, Oliver Phillips, Rodolfo Vasquez Martinez, Ted Feldpausch, Timothy Baker
TAM_02	Abel Monteagudo-Mendoza, Oliver Phillips, Rodolfo Vasquez Martinez, Ted Feldpausch
TAM_03	Abel Monteagudo-Mendoza, Oliver Phillips, Rodolfo Vasquez Martinez, Ted Feldpausch
TAM_04	Abel Monteagudo-Mendoza, Oliver Phillips, Rodolfo Vasquez Martinez, Ted Feldpausch
TAM_05	Abel Monteagudo-Mendoza, Oliver Phillips, Rodolfo Vasquez Martinez
TAM_06	Abel Monteagudo-Mendoza, Oliver Phillips, Rodolfo Vasquez Martinez
TAM_07	Abel Monteagudo-Mendoza, Oliver Phillips, Rodolfo Vasquez Martinez, Ted Feldpausch
TAM_08	Abel Monteagudo-Mendoza, Oliver Phillips, Rodolfo Vasquez Martinez
TAM_09	Javier Silva Espejo, Oliver Phillips, Yadivinder Malhi
TAN_03	Beatriz Marimon, Ben Hur Marimon Junior, Oliver Phillips, Ted Feldpausch
TAN_04	Beatriz Marimon, Ben Hur Marimon Junior, Jon Lloyd, Ted Feldpausch
TIP_01	Abel Monteagudo-Mendoza, Oliver Phillips
TIP_02	David Neill, Oliver Phillips
TIP_03	Abel Monteagudo-Mendoza, Oliver Phillips
YAN_01	Abel Monteagudo-Mendoza, Oliver Phillips, Rodolfo Vasquez Martinez, Roel Brienen
YAN_02	Abel Monteagudo-Mendoza, Oliver Phillips, Rodolfo Vasquez Martinez, Roel Brienen
ZAR_02	Eliana Jimenez-Rojas, Maria Cristina Peñuela-Mora , Oliver Phillips
ZAR_03	Eliana Jimenez-Rojas, Maria Cristina Peñuela-Mora , Oliver Phillips
ZAR_04	Eliana Jimenez-Rojas, Maria Cristina Peñuela-Mora , Oliver Phillips

Plot	Log Likelihood			AIC			BIC		
	MST	1 Param	2 Param	MST	1 Param	2 Param	MST	1 Param	2 Param
PNY_02	-2,136	-2,071	-2,064	139.0	10.4	0.0	130.0	5.98	0.0
PNY_03	-2,339	-2,271	-2,271	133.0	0.0	1.81	128.0	0.0	6.41
PNY_04	-1,774	-1,739	-1,739	67.5	0.0	1.92	63.3	0.0	6.18
PNY_05	-2,082	-2,035	-2,033	95.1	2.3	0.0	88.4	0.0	2.13
PNY_06	-1,624	-1,608	-1,608	29.6	0.0	1.81	25.5	0.0	5.95
PNY_07	-1,711	-1,697	-1,695	28.7	1.3	0.0	23.2	0.0	2.93
POR_01	-1,929	-1,912	-1,910	33.7	1.53	0.0	27.9	0.0	2.78
POR_02	-1,764	-1,730	-1,728	66.9	0.519	0.0	62.1	0.0	3.74
PTN_01	-1,741	-1,710	-1,708	62.0	1.83	0.0	55.8	0.0	2.48
RAS_01	-2,277	-2,221	-2,219	112.0	1.11	0.0	106.0	0.0	3.37
RCS_01	-2,128	-2,118	-2,114	23.4	5.65	0.0	14.5	1.2	0.0
RCS_02	-2,403	-2,403	-2,398	6.32	7.88	0.0	0.0	6.19	2.94
RCS_03	-2,565	-2,506	-2,495	137.0	20.7	0.0	128.0	16.1	0.0
RET_05	-2,012	-1,953	-1,953	115.0	0.0	1.81	111.0	0.0	6.2
RET_06	-1,776	-1,735	-1,732	85.4	4.91	0.0	76.9	0.653	0.0
RET_08	-1,717	-1,676	-1,673	84.3	4.59	0.0	75.9	0.365	0.0
RET_09	-1,652	-1,623	-1,622	56.2	0.0	0.711	52.1	0.0	4.87
RFH_01	-1,325	-1,310	-1,309	29.6	1.51	0.0	24.2	0.0	2.43
RIO_01	-493	-497	-495	0.0	9.85	8.01	0.0	12.8	13.9
RIO_02	-467	-470	-469	0.0	7.84	7.99	0.0	10.7	13.7
RST_01	-1,928	-1,892	-1,884	84.6	13.9	0.0	76.0	9.6	0.0
SCT_01	-1,899	-1,885	-1,885	26.1	0.0	1.97	21.8	0.0	6.33
SCT_06	-1,965	-1,938	-1,938	52.1	0.0	1.91	47.7	0.0	6.31
SEU_01	-801	-790	-790	19.3	0.0	1.77	15.8	0.0	5.27
SEU_02	-882	-865	-865	31.7	0.0	1.88	28.1	0.0	5.54
SEU_03	-551	-550	-549	0.124	0.0	0.48	0.0	2.93	6.47
SEU_04	-625	-621	-620	6.33	0.497	0.0	2.63	0.0	2.71
SEU_05	-701	-683	-682	33.5	0.0	0.987	30.1	0.0	4.36
SEU_06	-568	-558	-557	17.9	0.0	1.03	14.8	0.0	4.15
SUC_01	-2,068	-2,037	-2,036	59.9	0.0793	0.0	55.4	0.0	4.33
SUC_02	-2,015	-2,000	-2,000	27.8	0.0	1.53	23.4	0.0	5.92
SUC_03	-1,944	-1,927	-1,927	32.1	0.0	1.97	27.8	0.0	6.31
SUC_04	-2,078	-2,054	-2,054	45.4	0.0	1.09	40.9	0.0	5.5
SUC_05	-1,969	-1,957	-1,957	21.3	0.0	1.99	17.0	0.0	6.33
TAM_01	-2,152	-2,105	-2,102	94.7	3.81	0.0	86.5	0.0	0.62
TAM_02	-2,319	-2,251	-2,250	134.0	0.223	0.0	129.0	0.0	4.3
TAM_03	-1,405	-1,399	-1,356	94.2	85.4	0.0	86.3	81.5	0.0
TAM_04	-1,017	-989	-989	54.7	0.0	1.98	51.0	0.0	5.69
TAM_05	-1,830	-1,800	-1,799	57.0	0.0	0.149	52.7	0.0	4.43
TAM_06	-2,331	-2,268	-2,267	124.0	0.0	0.746	119.0	0.0	5.24
TAM_07	-1,728	-1,687	-1,686	81.1	0.0	1.66	76.9	0.0	5.9
TAM_08	-1,718	-1,677	-1,677	81.0	0.0	1.55	76.8	0.0	5.78
TAM_09	-1,908	-1,870	-1,870	74.1	0.0	1.99	69.8	0.0	6.31
TAN_03	-1,878	-1,838	-1,837	78.5	0.0	1.53	74.1	0.0	5.91
TAN_04	-1,855	-1,804	-1,804	98.6	0.0	1.39	94.3	0.0	5.75
TIP_01	-1,879	-1,835	-1,831	91.3	4.88	0.0	82.7	0.565	0.0
TIP_02	-1,836	-1,795	-1,794	80.9	0.0	1.59	76.6	0.0	5.89
TIP_03	-1,619	-1,623	-1,618	0.0	11.3	3.5	0.0	15.5	11.8
YAN_01	-2,065	-2,048	-2,047	32.5	0.329	0.0	27.8	0.0	4.08
YAN_02	-2,054	-2,036	-2,035	34.1	0.0	0.811	29.7	0.0	5.19
ZAR_02	-1,894	-1,899	-1,892	0.0	12.4	0.691	0.0	16.8	9.49
ZAR_03	-2,181	-2,110	-2,107	144.0	3.13	0.0	137.0	0.0	1.36
ZAR_04	-2,086	-2,043	-2,036	95.1	10.7	0.0	86.3	6.27	0.0

Plot	Log Likelihood			AIC			BIC		
	MST	1 Param	2 Param	MST	1 Param	2 Param	MST	1 Param	2 Param
PNY_02	-3,588	-3,511	-3,509	154.0	2.92	0.0	147.0	0.0	1.53
PNY_03	-4,085	-4,045	-4,037	90.9	12.6	0.0	81.6	7.96	0.0
PNY_04	-3,108	-3,067	-3,066	79.7	0.922	0.0	74.5	0.0	3.34
PNY_05	-3,298	-3,250	-3,249	94.7	0.0	0.441	90.3	0.0	4.87
PNY_06	-2,749	-2,735	-2,733	28.7	1.69	0.0	22.9	0.0	2.45
PNY_07	-2,913	-2,898	-2,893	35.6	8.48	0.0	27.2	4.25	0.0
POR_01	-3,513	-3,488	-3,487	47.8	0.0	0.793	43.5	0.0	5.1
POR_02	-2,987	-2,947	-2,946	78.7	0.0	1.52	74.5	0.0	5.78
PTN_01	-3,123	-3,108	-3,099	44.1	16.7	0.0	35.4	12.4	0.0
RAS_01	-4,013	-3,950	-3,946	130.0	6.91	0.0	121.0	2.42	0.0
RCS_01	-3,978	-3,984	-3,971	9.93	23.3	0.0	1.03	18.9	0.0
RCS_02	-4,208	-4,198	-4,190	31.3	12.6	0.0	22.0	7.99	0.0
RCS_03	-4,156	-4,045	-4,040	229.0	8.98	0.0	220.0	4.37	0.0
RET_05	-3,447	-3,391	-3,390	110.0	0.0	1.06	106.0	0.0	5.45
RET_06	-3,090	-3,046	-3,044	88.5	1.35	0.0	82.9	0.0	2.91
RET_08	-2,897	-2,853	-2,852	86.0	0.375	0.0	81.4	0.0	3.85
RET_09	-2,872	-2,837	-2,837	66.3	0.0	0.676	62.2	0.0	4.84
RFH_01	-2,317	-2,298	-2,298	35.9	0.0	1.25	32.0	0.0	5.19
RIO_01	-940	-947	-944	0.0	15.5	12.9	0.0	18.5	18.7
RIO_02	-870	-873	-870	0.0	7.59	2.99	0.0	10.5	8.72
RST_01	-3,334	-3,307	-3,304	55.9	3.36	0.0	48.3	0.0	0.926
SCT_01	-3,194	-3,174	-3,174	38.5	0.0	1.9	34.2	0.0	6.26
SCT_06	-3,431	-3,390	-3,390	79.6	0.0	1.93	75.2	0.0	6.33
SEU_01	-1,199	-1,196	-1,196	2.39	0.0	1.51	0.0	1.11	6.12
SEU_02	-1,460	-1,455	-1,453	9.83	1.46	0.0	4.72	0.0	2.19
SEU_03	-988	-986	-986	2.05	0.0	1.8	0.0	1.01	5.87
SEU_04	-1,087	-1,081	-1,080	10.4	0.0	1.03	7.23	0.0	4.24
SEU_05	-1,333	-1,314	-1,314	35.0	0.0	1.23	31.6	0.0	4.61
SEU_06	-909	-896	-895	24.3	0.0	1.37	21.1	0.0	4.49
SUC_01	-3,473	-3,442	-3,442	60.3	0.0	1.8	55.8	0.0	6.22
SUC_02	-3,358	-3,344	-3,344	24.4	0.0	1.28	20.0	0.0	5.66
SUC_03	-3,450	-3,453	-3,452	0.0	8.39	8.33	0.0	12.7	17.0
SUC_04	-3,550	-3,524	-3,524	49.8	0.0	1.95	45.3	0.0	6.35
SUC_05	-3,214	-3,197	-3,197	32.0	0.0	0.645	27.6	0.0	4.98
TAM_01	-3,682	-3,632	-3,632	98.2	0.0	0.989	93.7	0.0	5.42
TAM_02	-3,969	-3,885	-3,885	168.0	0.0	2.0	163.0	0.0	6.52
TAM_03	-2,492	-2,503	-2,460	60.0	83.9	0.0	52.2	80.0	0.0
TAM_04	-1,624	-1,594	-1,594	57.7	0.0	0.862	54.0	0.0	4.57
TAM_05	-3,319	-3,284	-3,283	68.1	0.0	1.32	63.9	0.0	5.6
TAM_06	-3,838	-3,774	-3,773	128.0	0.0	1.94	123.0	0.0	6.43
TAM_07	-2,842	-2,798	-2,798	87.1	0.0	1.65	82.9	0.0	5.88
TAM_08	-3,007	-2,949	-2,949	114.0	0.0	0.918	110.0	0.0	5.15
TAM_09	-3,222	-3,188	-3,188	66.7	0.0	1.78	62.4	0.0	6.1
TAN_03	-3,376	-3,348	-3,347	53.9	0.0743	0.0	49.5	0.0	4.3
TAN_04	-3,213	-3,169	-3,167	88.5	1.04	0.0	83.1	0.0	3.32
TIP_01	-3,279	-3,232	-3,232	90.6	0.0	2.0	86.3	0.0	6.31
TIP_02	-2,943	-2,891	-2,891	102.0	0.0	1.96	97.3	0.0	6.26
TIP_03	-2,944	-2,949	-2,948	0.0	12.9	12.9	0.0	17.0	21.2
YAN_01	-3,328	-3,305	-3,305	45.1	0.0	1.88	40.7	0.0	6.28
YAN_02	-3,488	-3,460	-3,460	54.2	0.0	1.64	49.8	0.0	6.02
ZAR_02	-3,344	-3,346	-3,339	5.24	11.0	0.0	0.0	10.1	3.56
ZAR_03	-3,975	-3,913	-3,904	138.0	17.2	0.0	129.0	12.7	0.0
ZAR_04	-3,776	-3,737	-3,729	88.8	13.7	0.0	80.0	9.34	0.0

2 Derivation of relationship between μ_1 and ϕ

If we have a forest size-distribution which has power law growth, with scaling power ϕ_t and a constant mortality rate γ_t what happens if we fit the size-distribution with a fixed growth scaling power ϕ that is not necessarily equal to ϕ_t ?

The pdf of the actual true distribution is: -

$$f(D) = \mu_{t1} D^{-\phi_t} \frac{\exp(x_t \mu_{t1} D_L^{1-\phi_t})}{\exp(x_t \mu_{t1} D^{1-\phi_t})} \quad (1)$$

where $x_t = 1/(1 - \phi_t)$ and D_L is the left-truncation point of the dataset.

The log-Likelihood L is

$$L = \sum_i \ln(f(D_i)) \quad (2)$$

where D_i is the trunk diameter of the i th tree in the dataset.

Solving for $\frac{\partial L}{\partial \mu_{t1}} = 0$ gives the result of fitting the dataset with MLE with fixed ϕ , giving a fitted μ_1

$$\mu_1 = \frac{1 - \phi}{\left(\frac{1}{n} \sum_i D_i^{1-\phi} - D_L^{1-\phi} \right)} \quad (3)$$

where n is the number of trees in the dataset.

Can remove the dependence on the data by noting

$$\frac{1}{n} \sum_i D_i^{1-\phi} = \overline{D^{1-\phi}} = \int_{D_L}^{\infty} f(D) D^{1-\phi} dD \quad (4)$$

If we say

$$v(D) = x_t \mu_{t1} D^{1-\phi_t} \quad (5)$$

and

$$y = \frac{1 - \phi}{1 - \phi_t} \quad (6)$$

then

$$\overline{D^{1-\phi}} = \frac{\exp(v_L)}{(x\mu_{t1})^y} \int_{v_L}^{\infty} v^y \exp(-v) dv = \frac{\exp(v_L)}{(x_t\mu_{t1})^y} \Gamma(y+1, v_L) \quad (7)$$

So the final result is

$$\boxed{\mu_1 = \frac{1 - \phi}{\left(\frac{\exp(v_L)}{(x_t\mu_{t1})^y} \Gamma(y+1, v_L) - D_L^{1-\phi} \right)}} \quad (8)$$

If $\phi = \phi_t$ then $y = 1$ so $\exp(v_L)\Gamma(y+1, v_L) = 1 + v_L$ and we correctly get $\mu_1 = \mu_{t1}$.

3 Region and Country DBH Size-Distributions

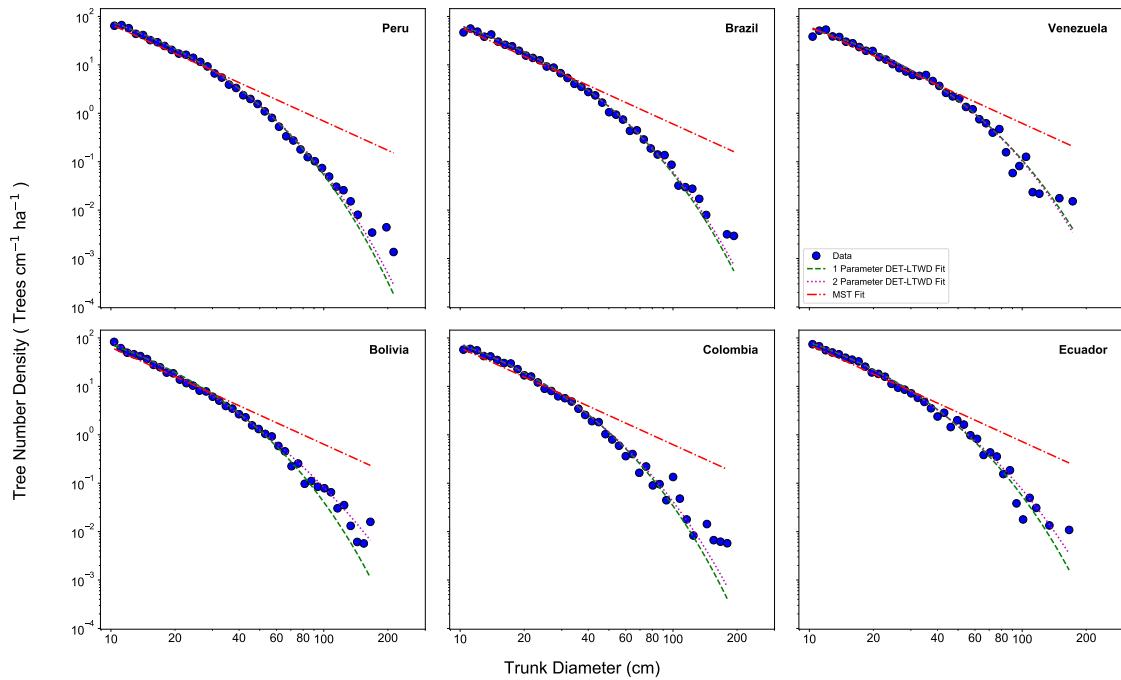


Figure S1: Shows the fit of the three models to the trunk diameter data for each country.

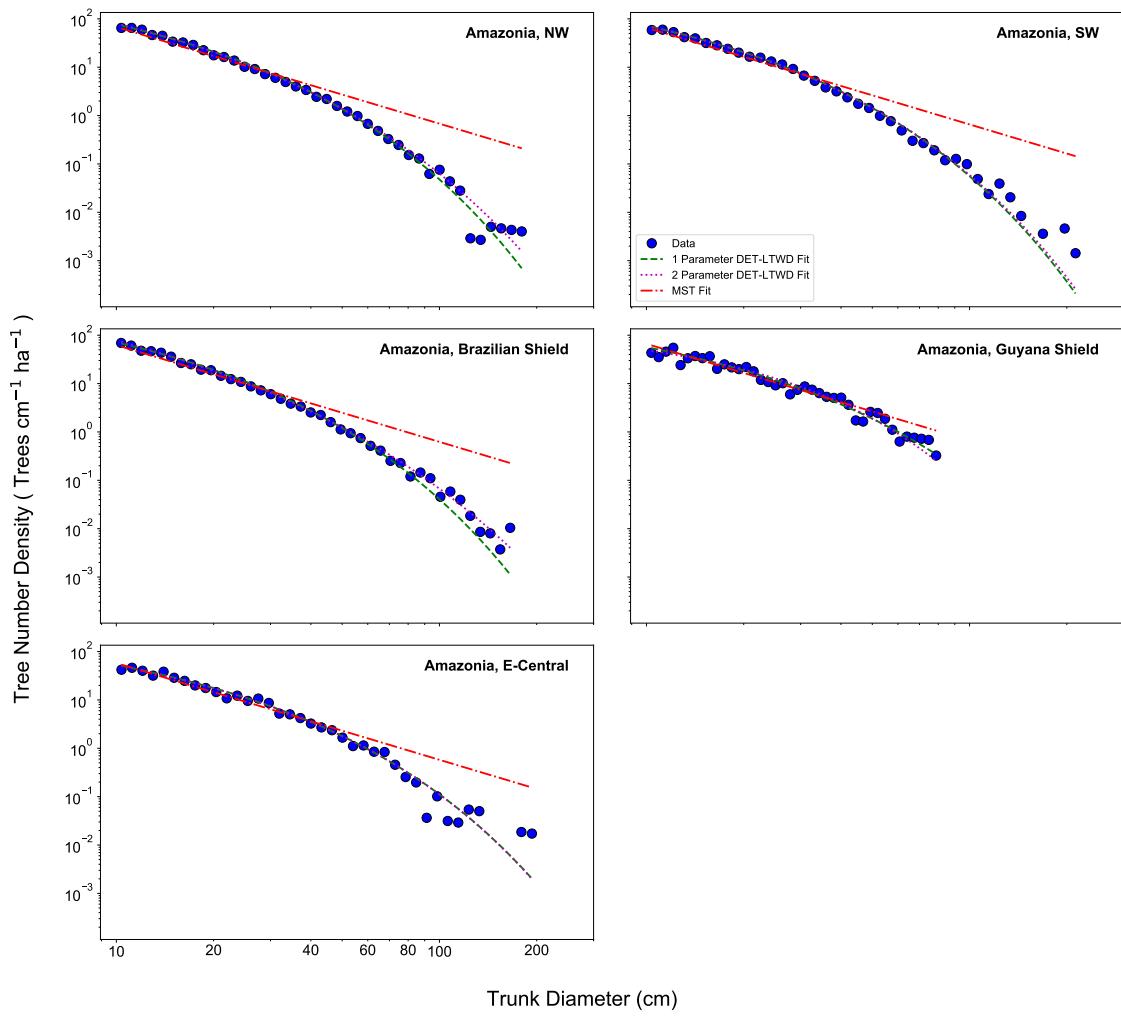


Figure S2: Shows the fit of the three models to the trunk diameter data for each allometric region.

4 Region and Country Mass Size-Distributions

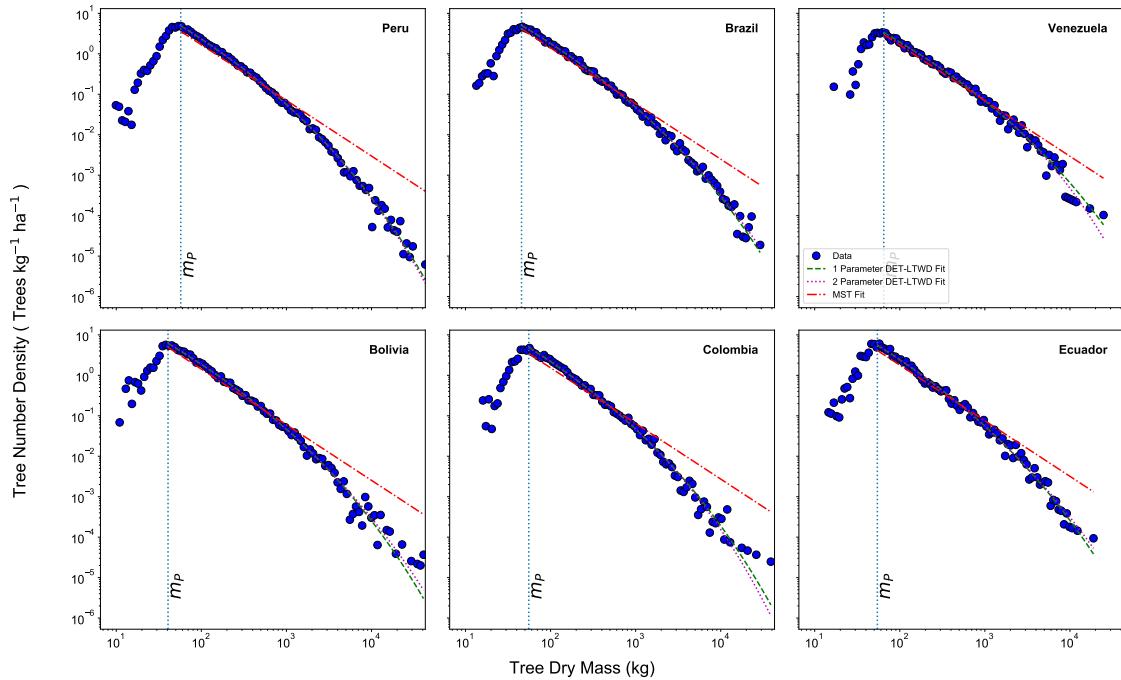


Figure S3: Shows the fit of the three models to the mass data for each country.

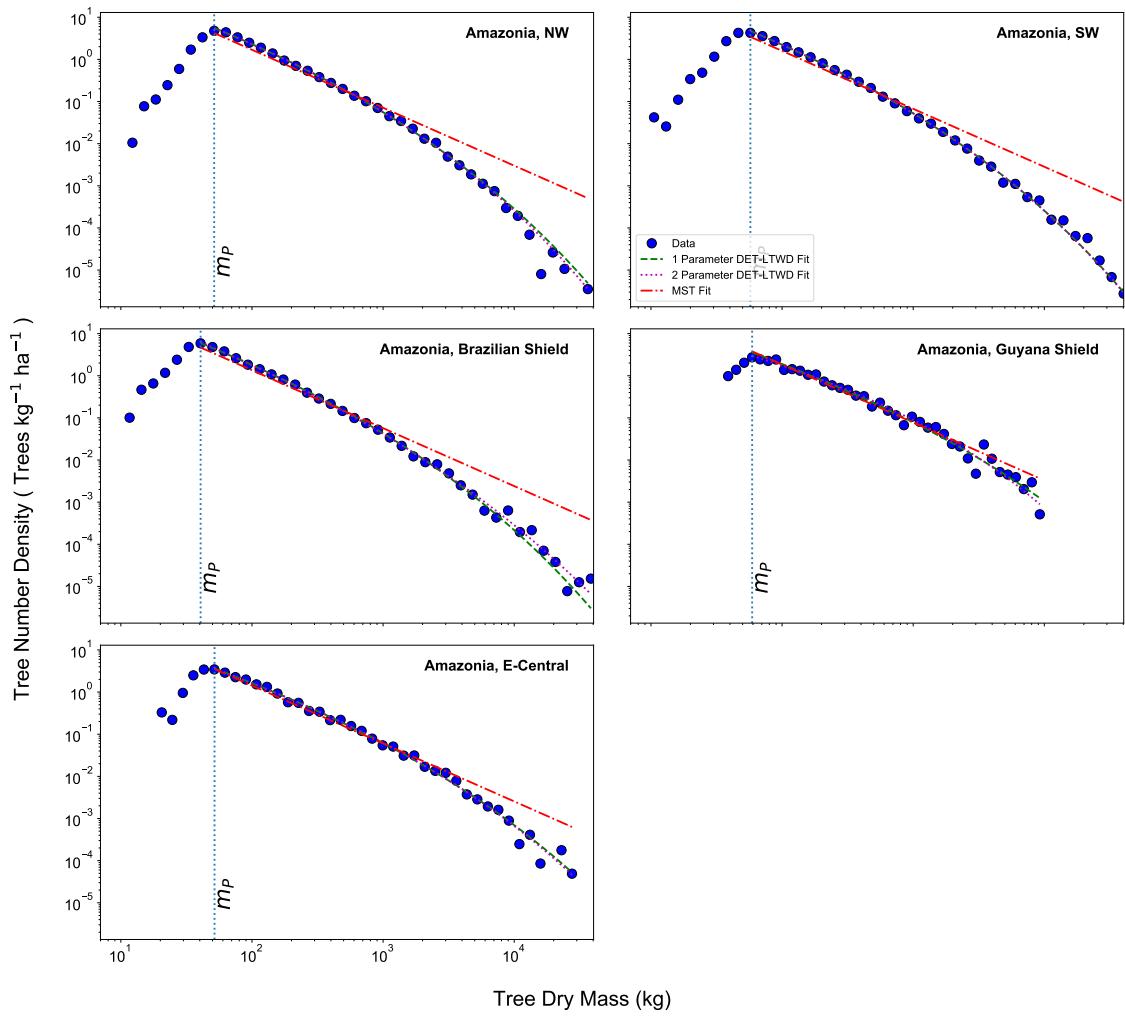


Figure S4: Shows the fit of the three models to the mass data for each allometric region.

5 Forest Plot DBH Size-Distributions

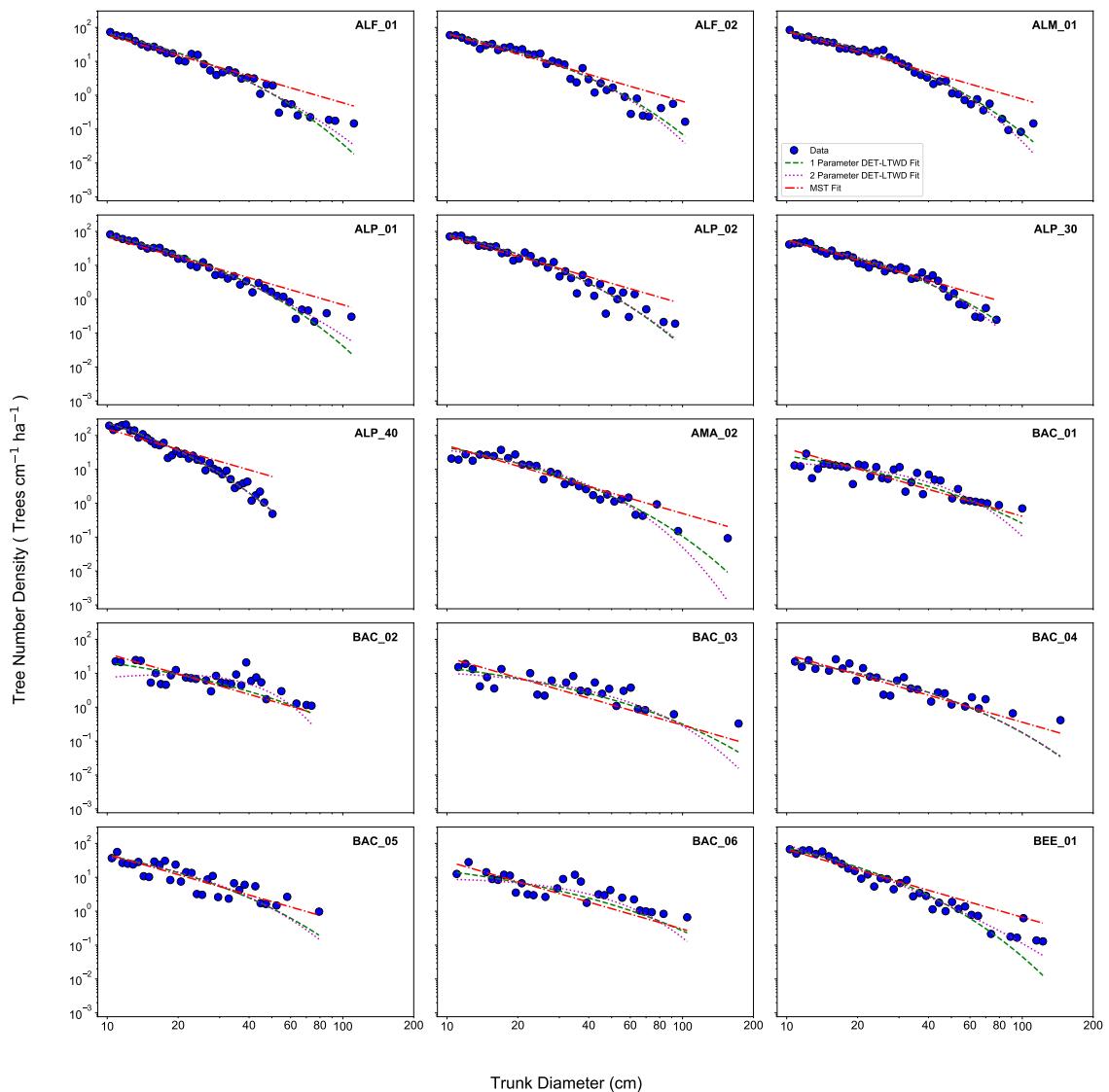


Figure S5: Diameter Size Distributions of Individual Forest Plots.

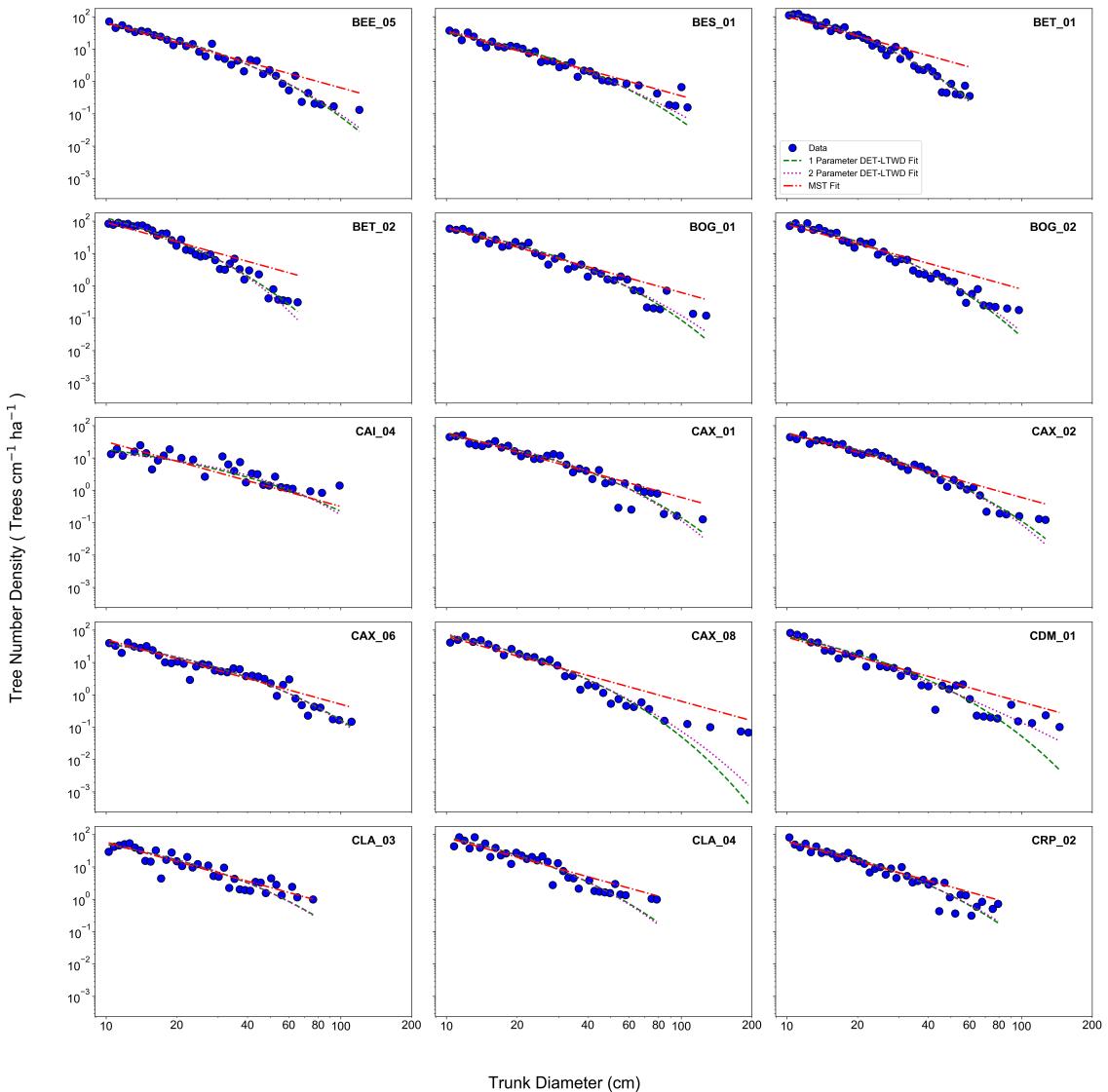


Figure S6: Diameter Size Distributions of Individual Forest Plots.

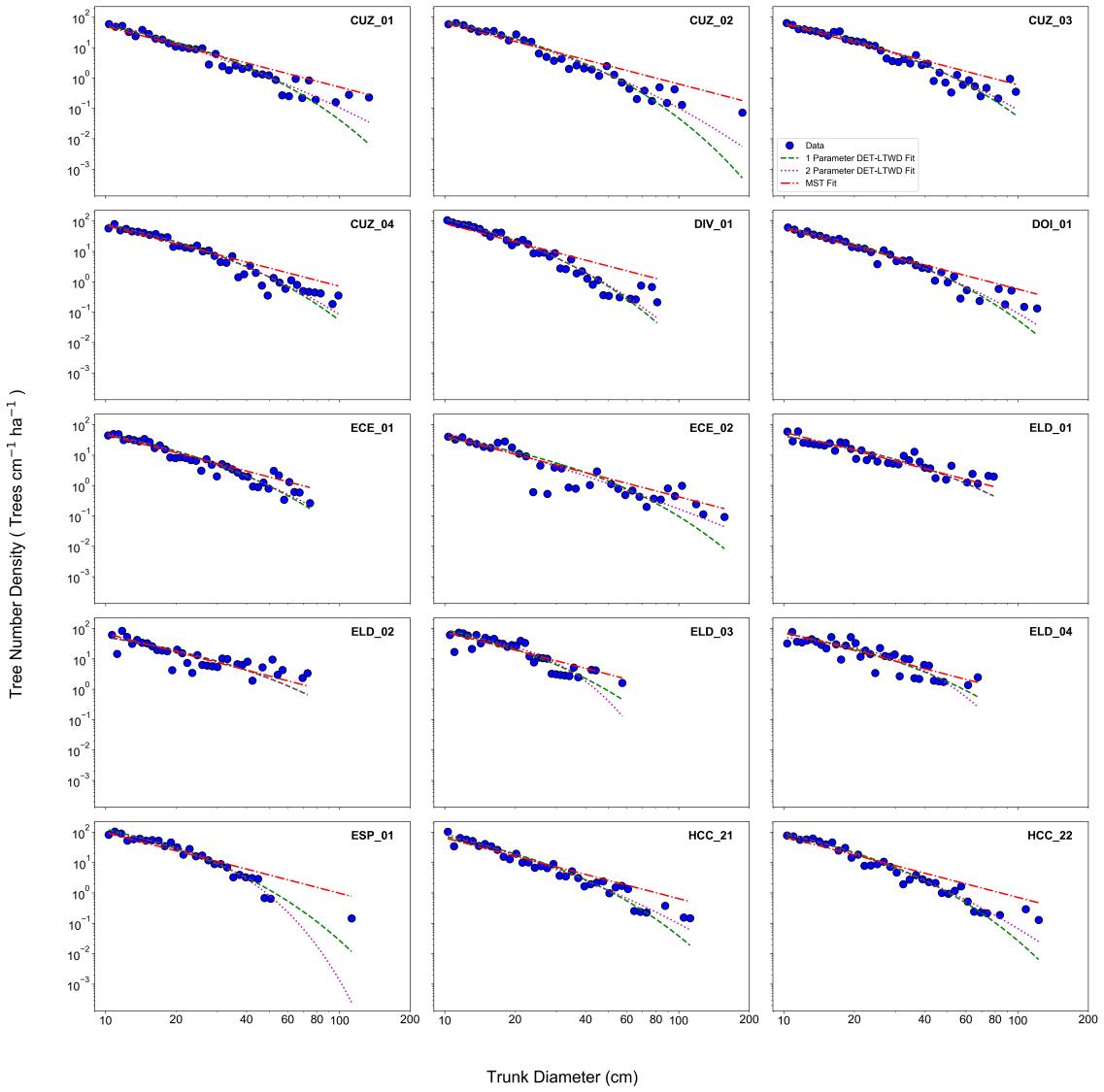


Figure S7: Diameter Size Distributions of Individual Forest Plots.

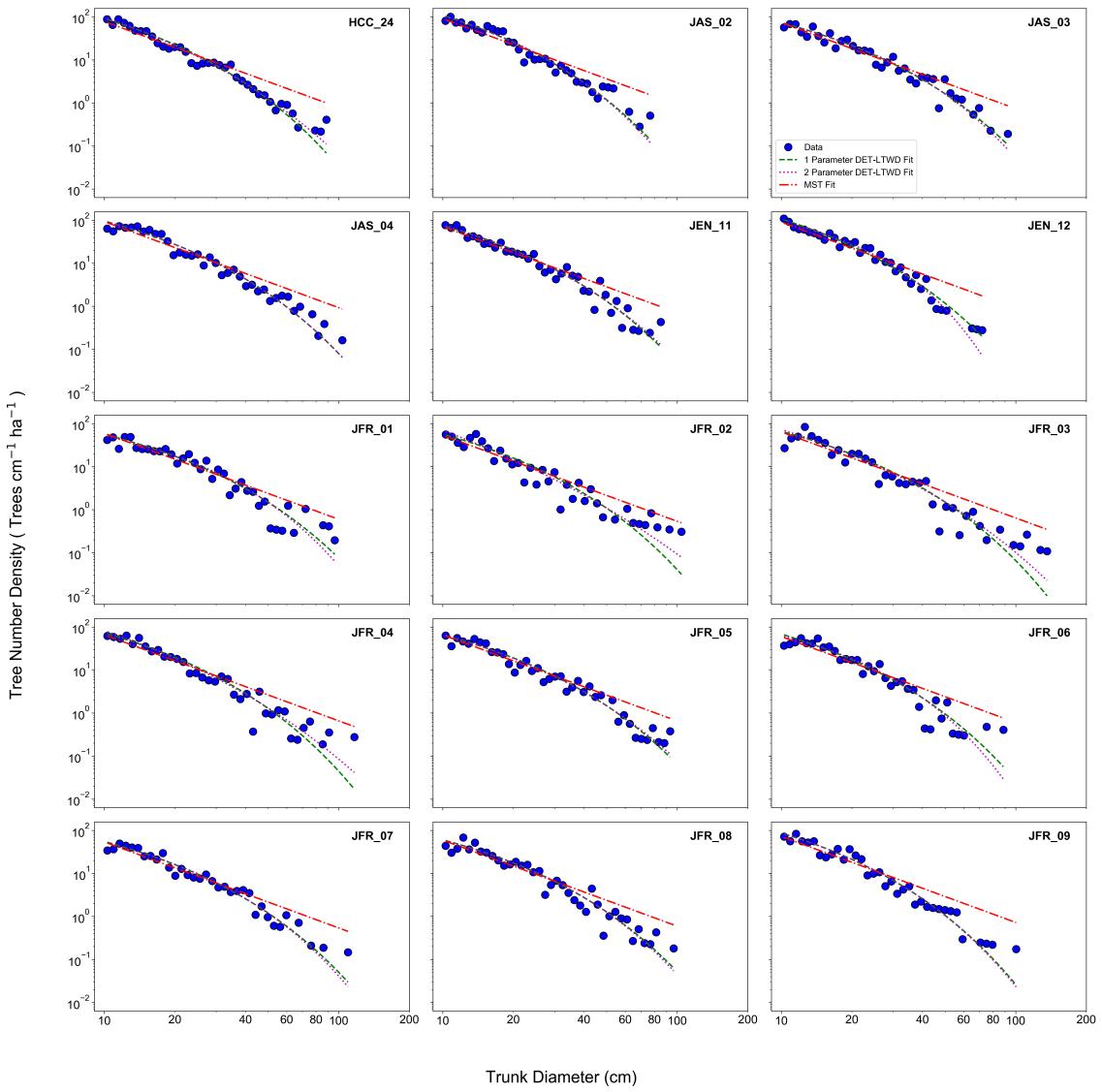


Figure S8: Diameter Size Distributions of Individual Forest Plots.

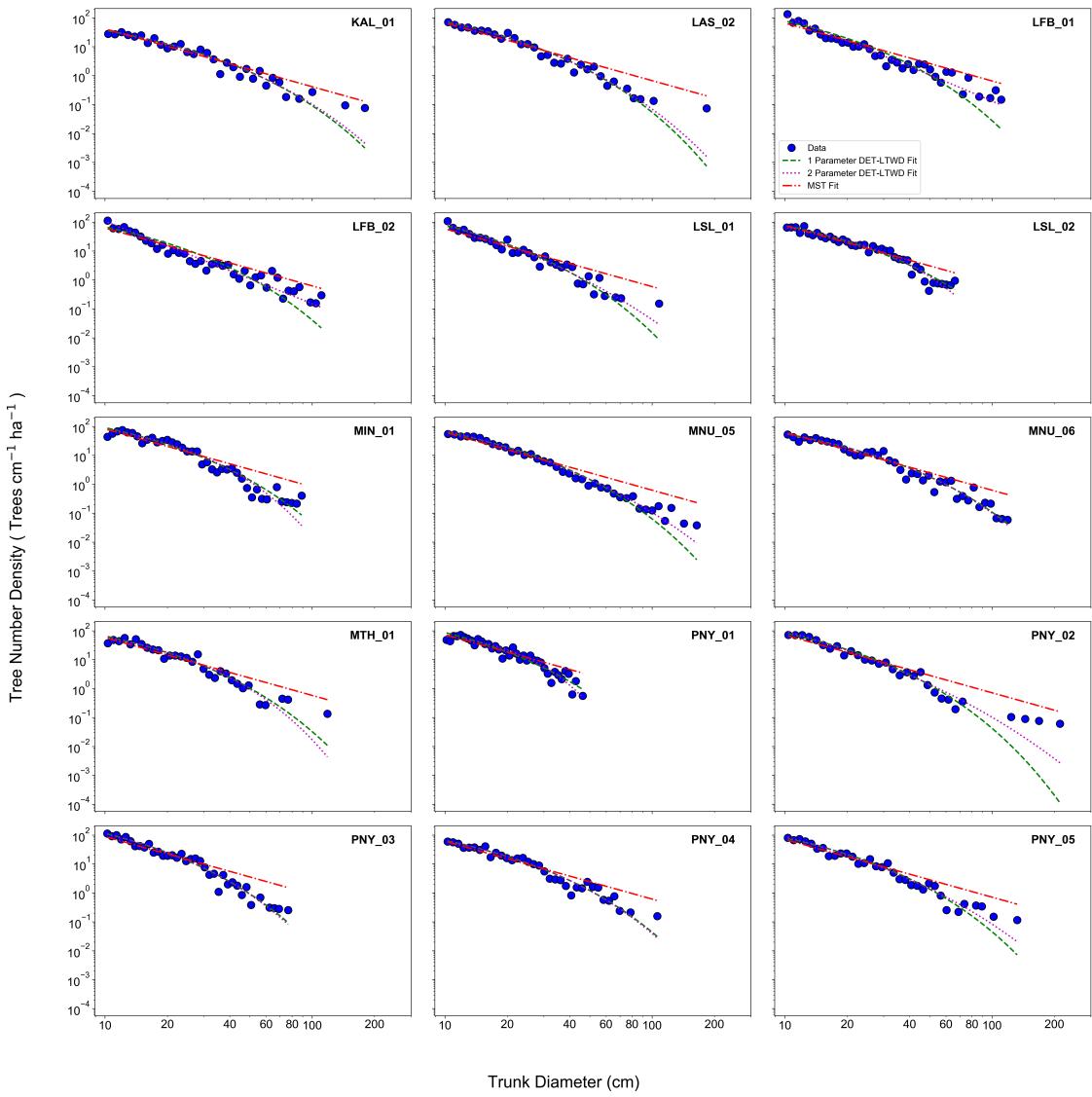


Figure S9: Diameter Size Distributions of Individual Forest Plots.

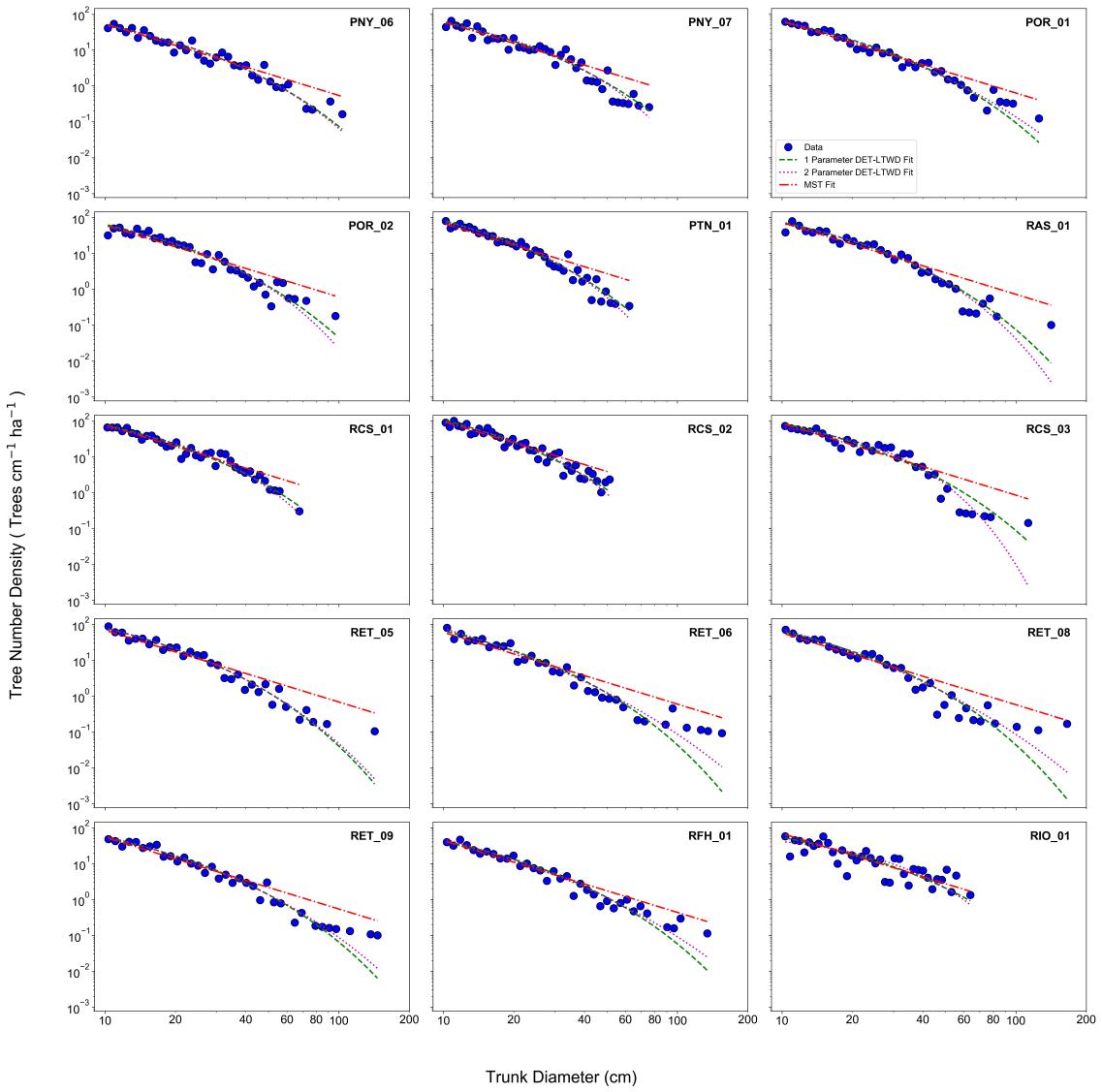


Figure S10: Diameter Size Distributions of Individual Forest Plots.

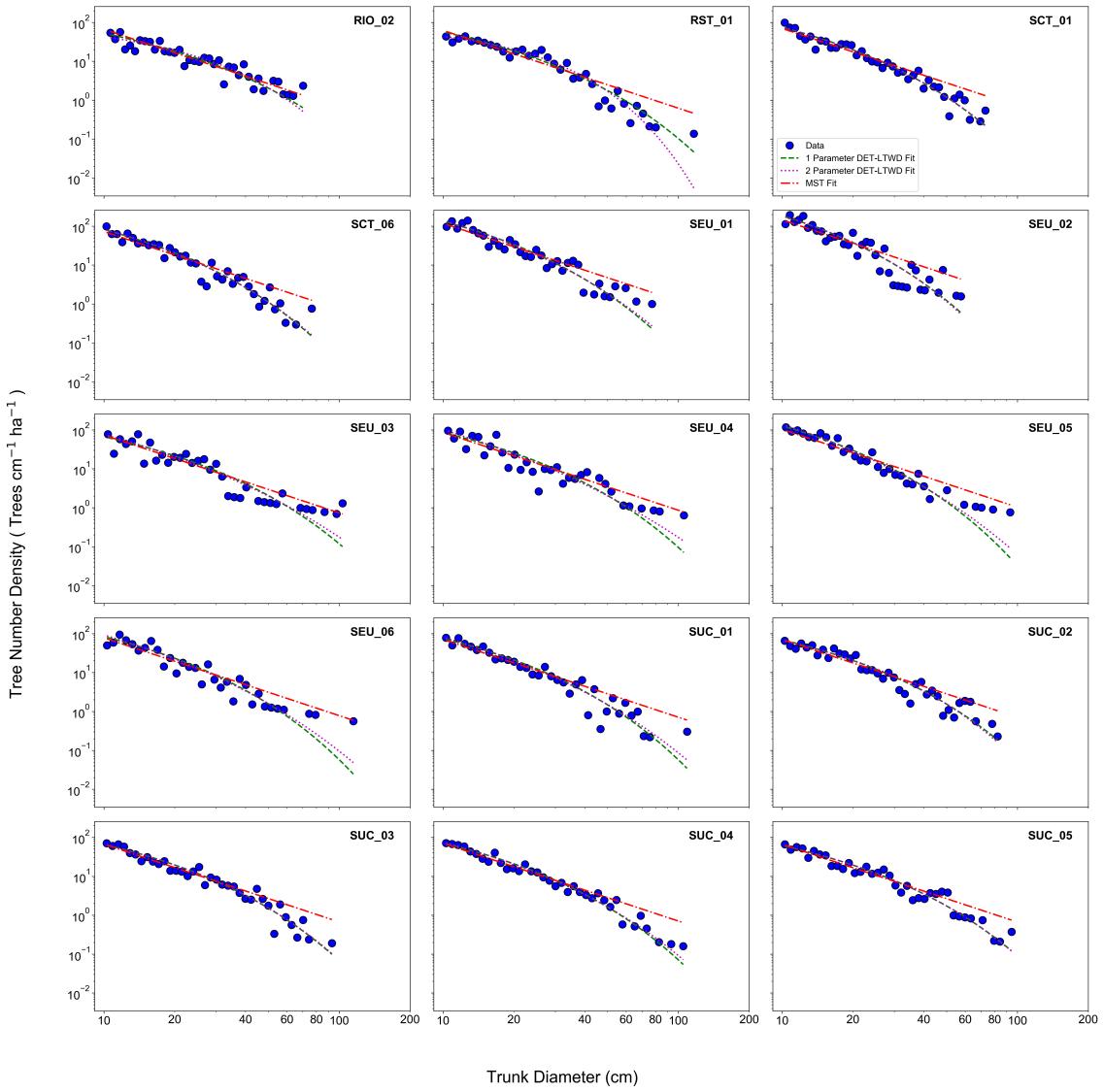


Figure S11: Diameter Size Distributions of Individual Forest Plots.

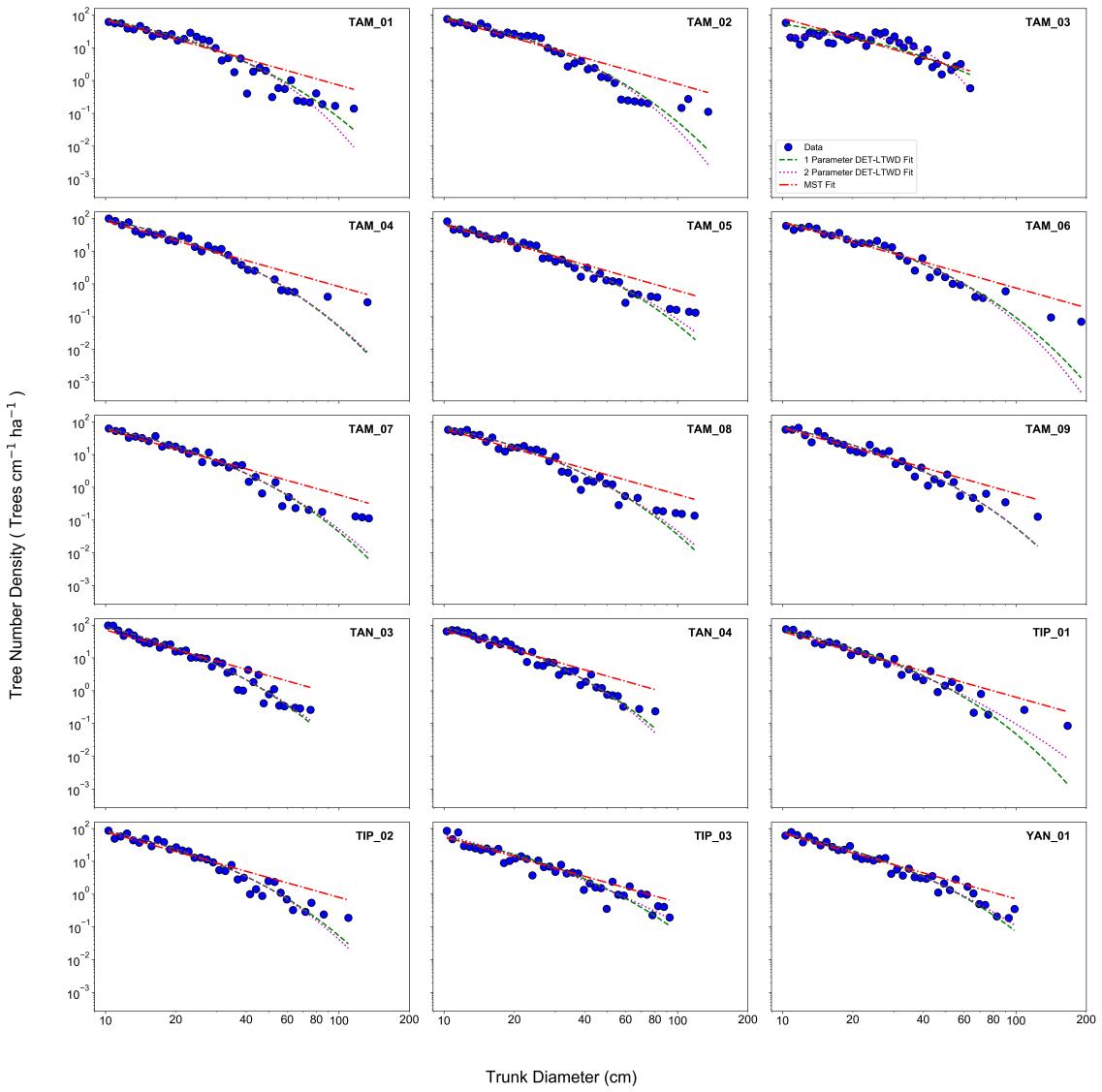


Figure S12: Diameter Size Distributions of Individual Forest Plots.

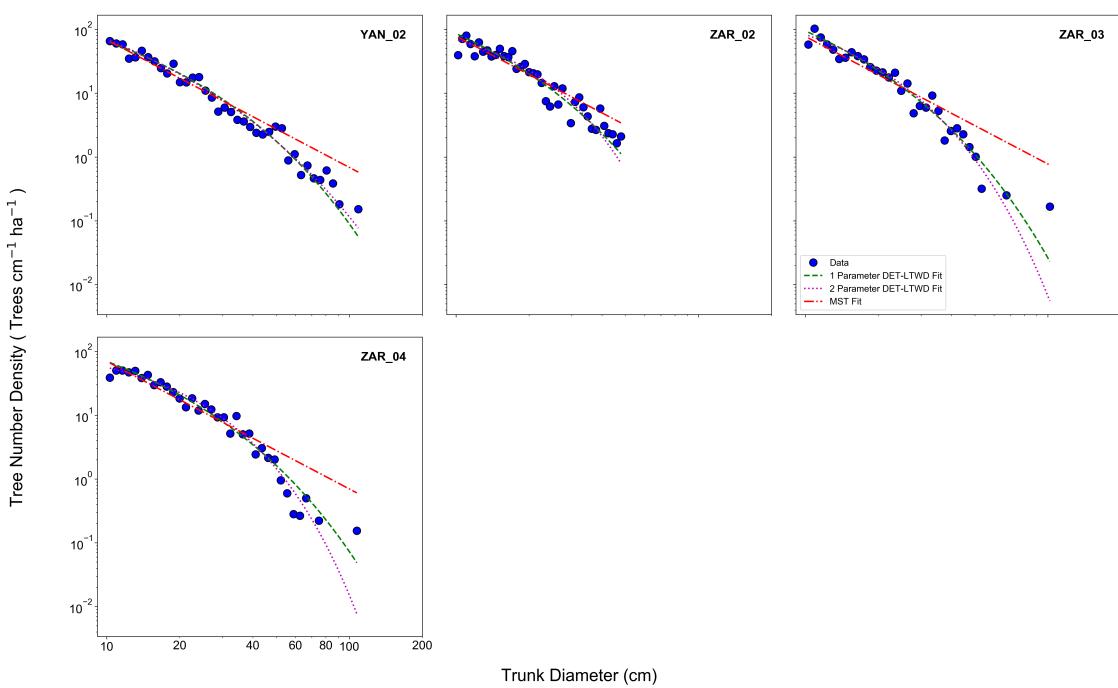


Figure S13: Diameter Size Distributions of Individual Forest Plots.

6 Forest Plot Mass Size-Distributions

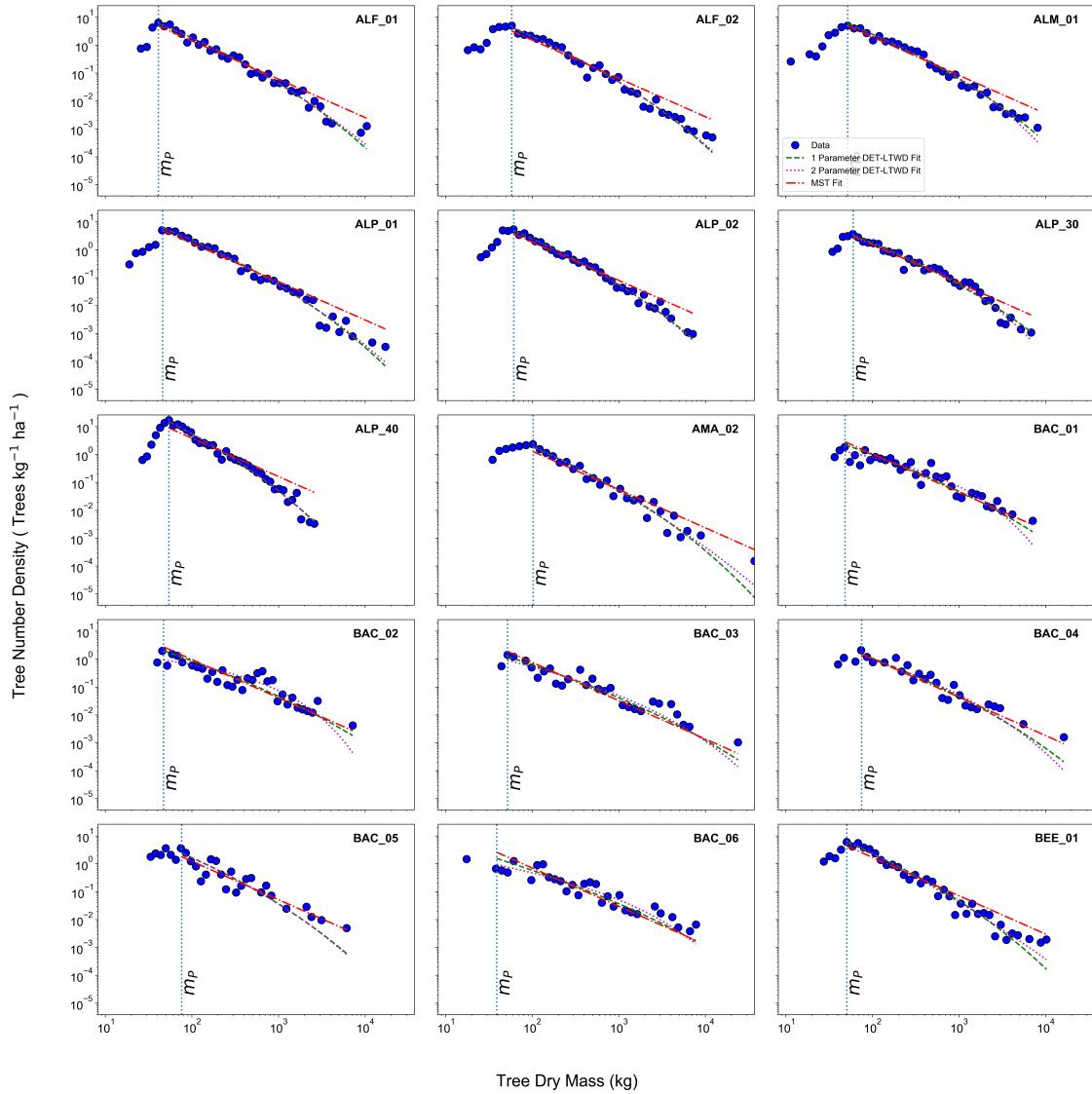


Figure S14: Mass Size Distributions of Individual Forest Plots.

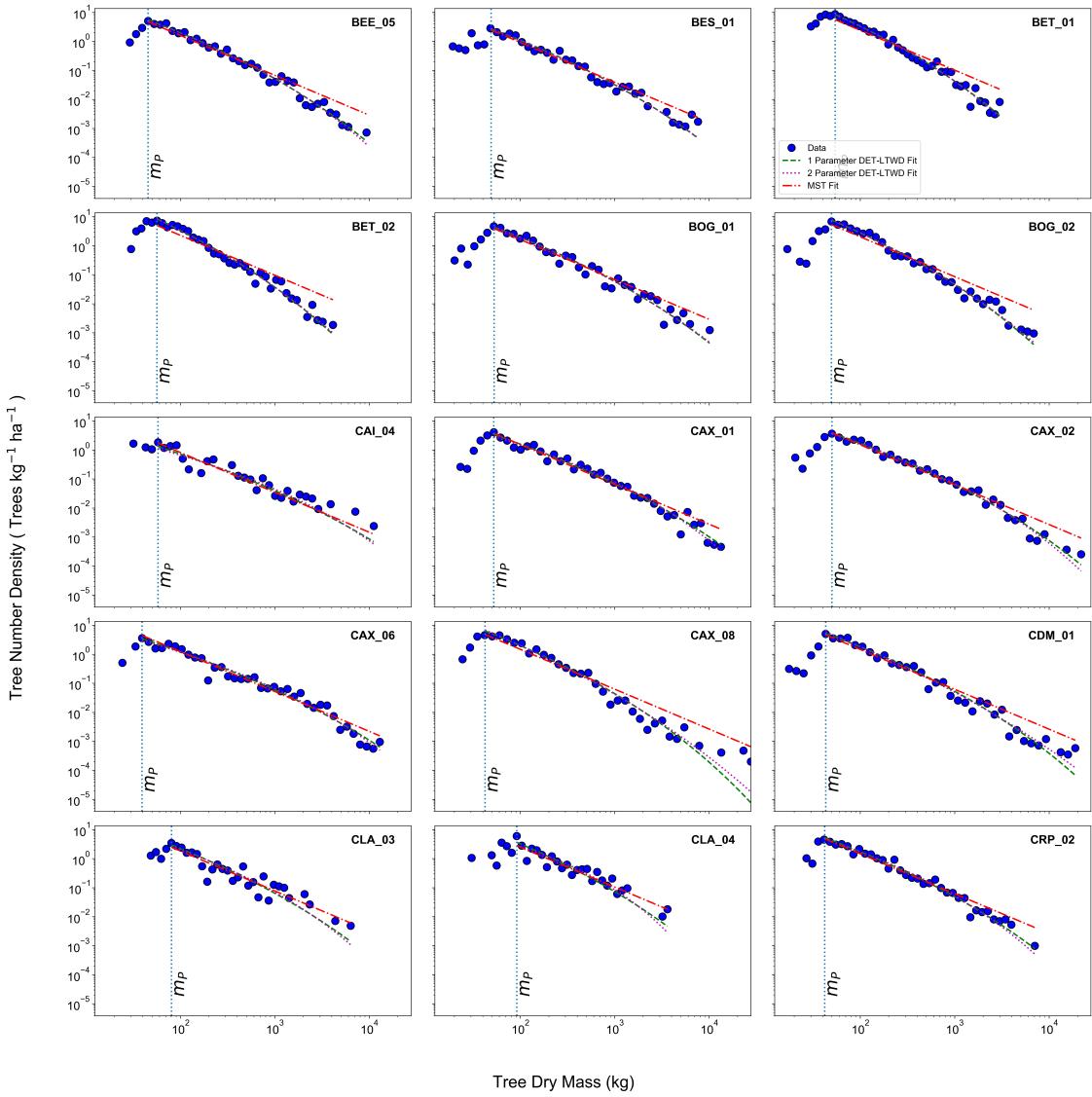


Figure S15: Mass Size Distributions of Individual Forest Plots.

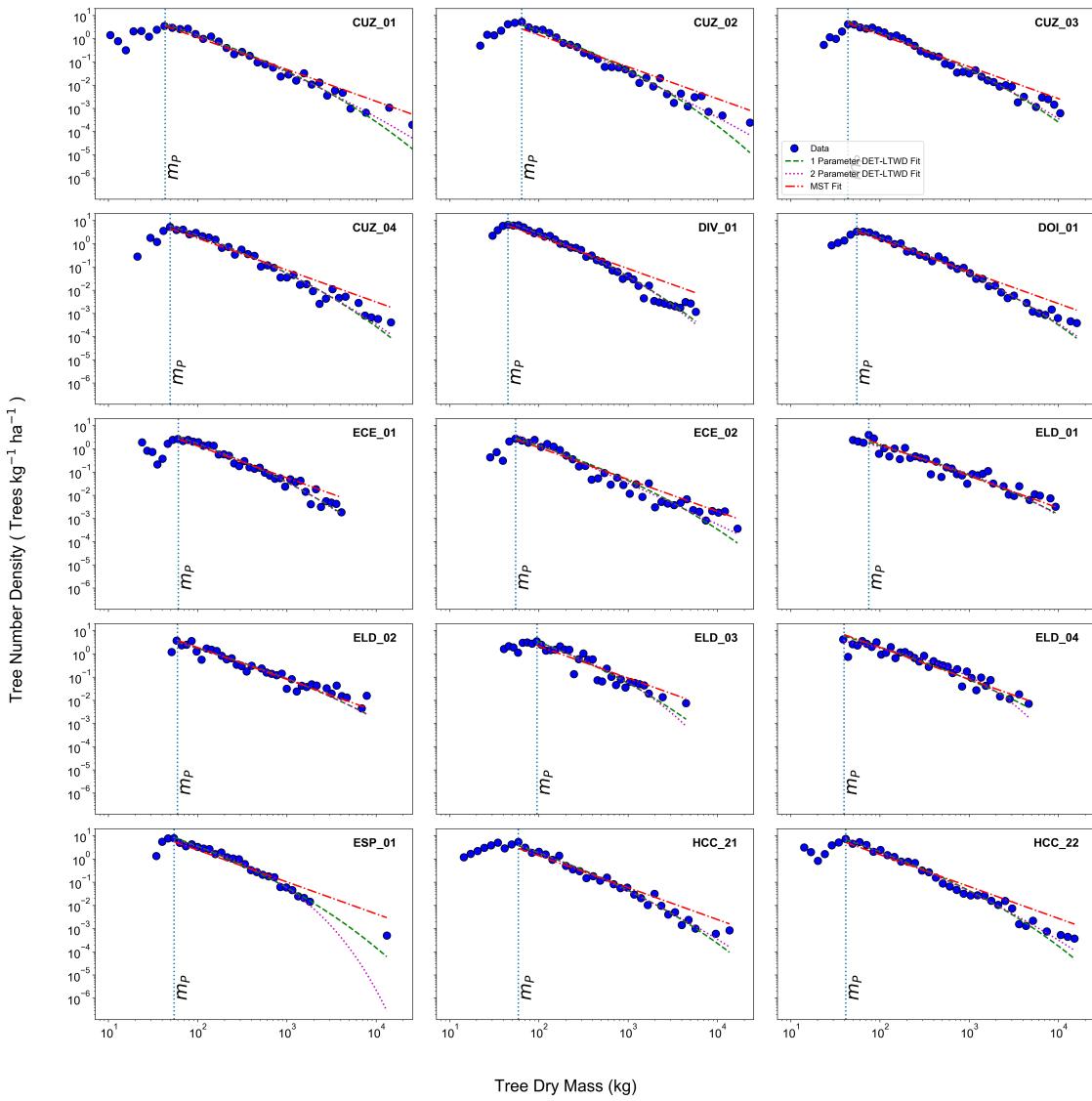


Figure S16: Mass Size Distributions of Individual Forest Plots.

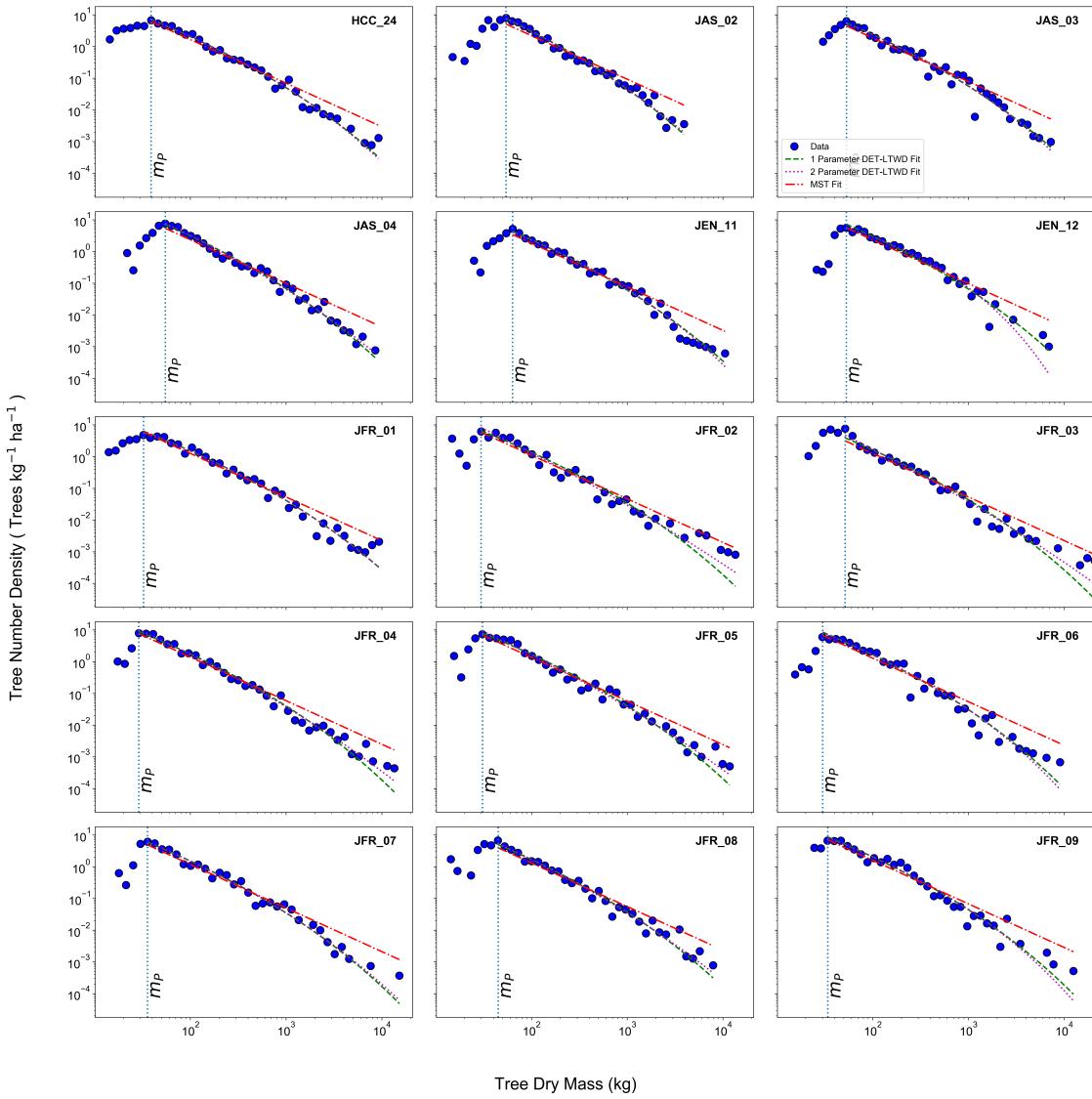


Figure S17: Mass Size Distributions of Individual Forest Plots.

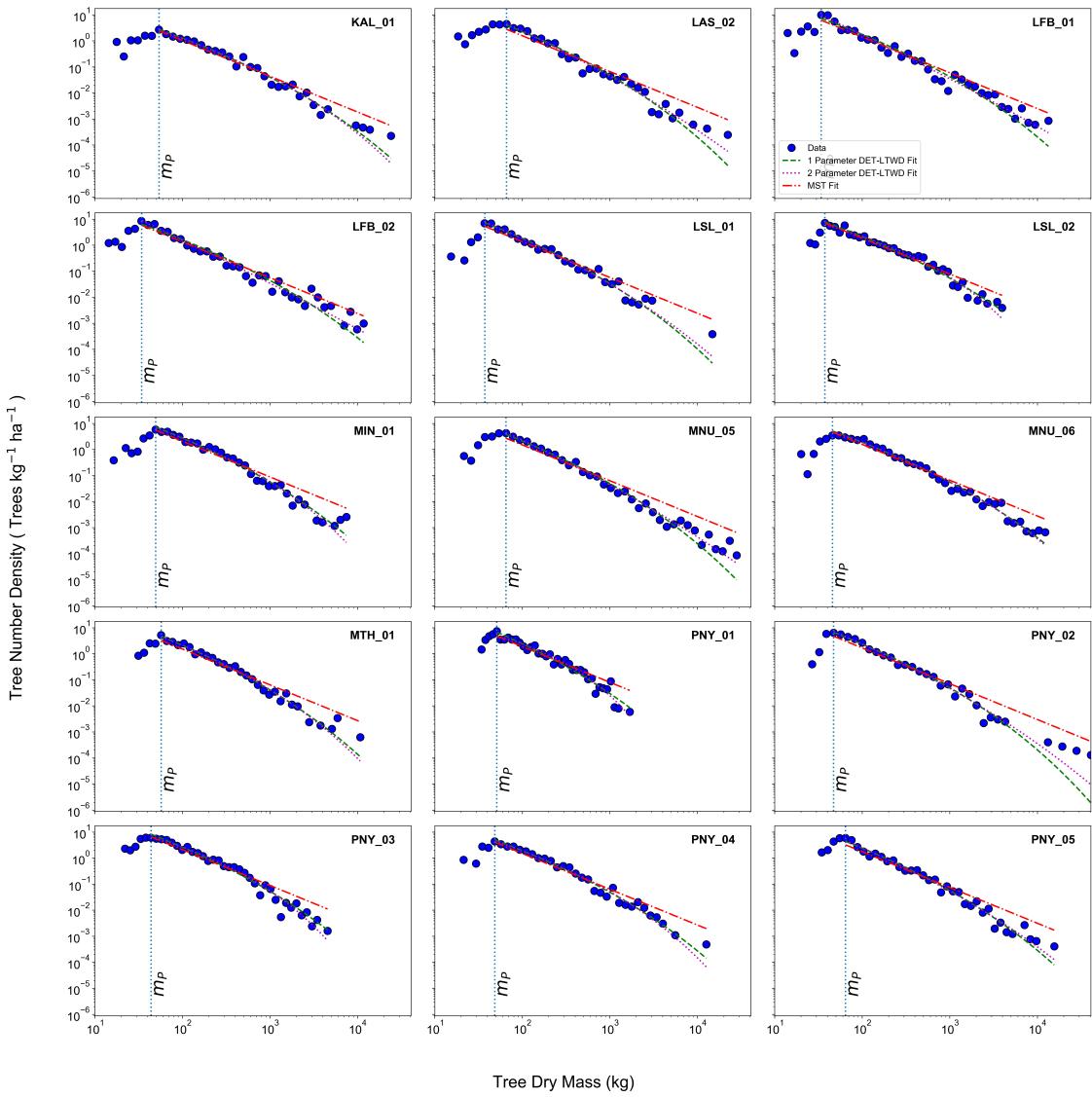


Figure S18: Mass Size Distributions of Individual Forest Plots.

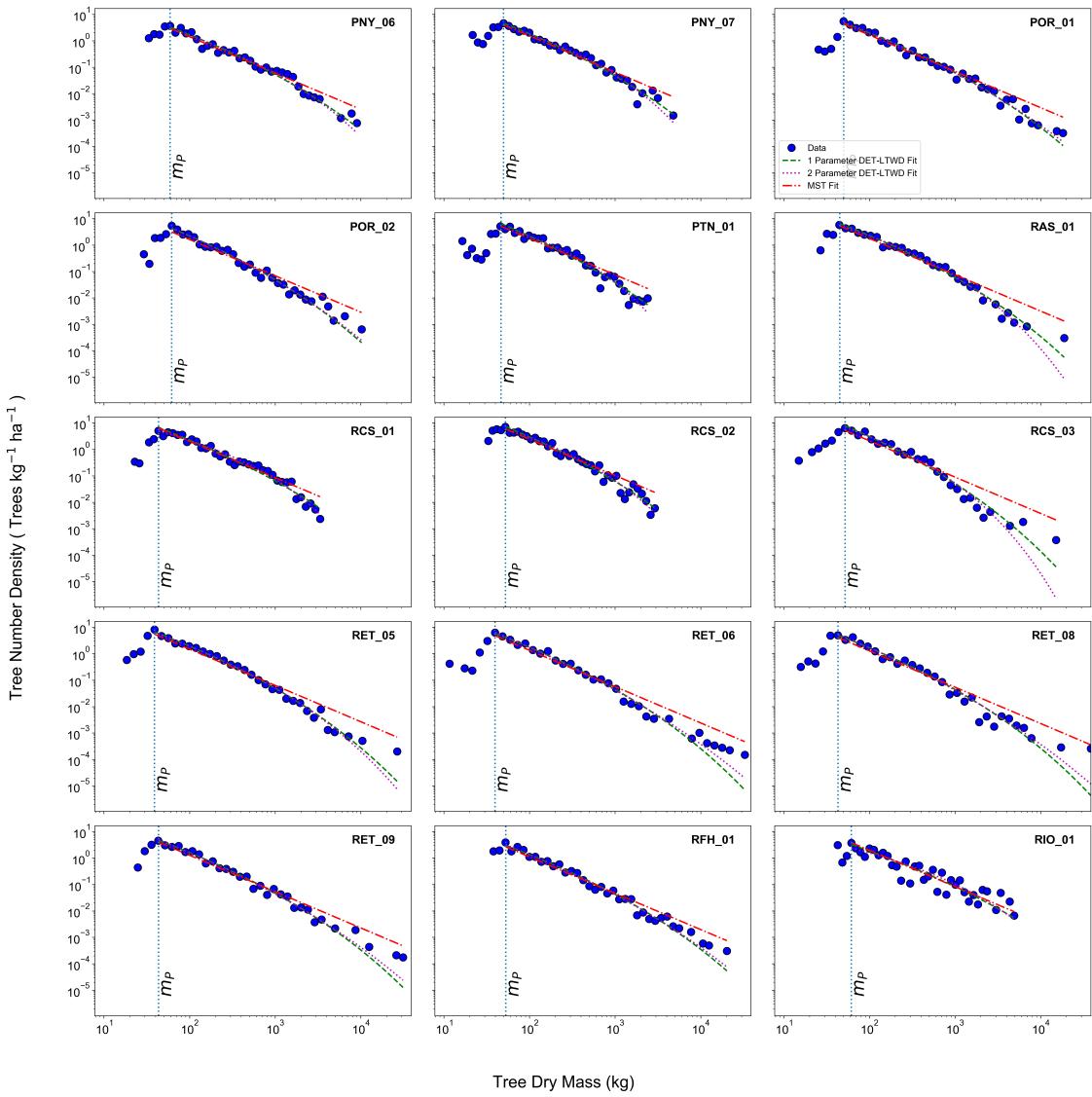


Figure S19: Mass Size Distributions of Individual Forest Plots.

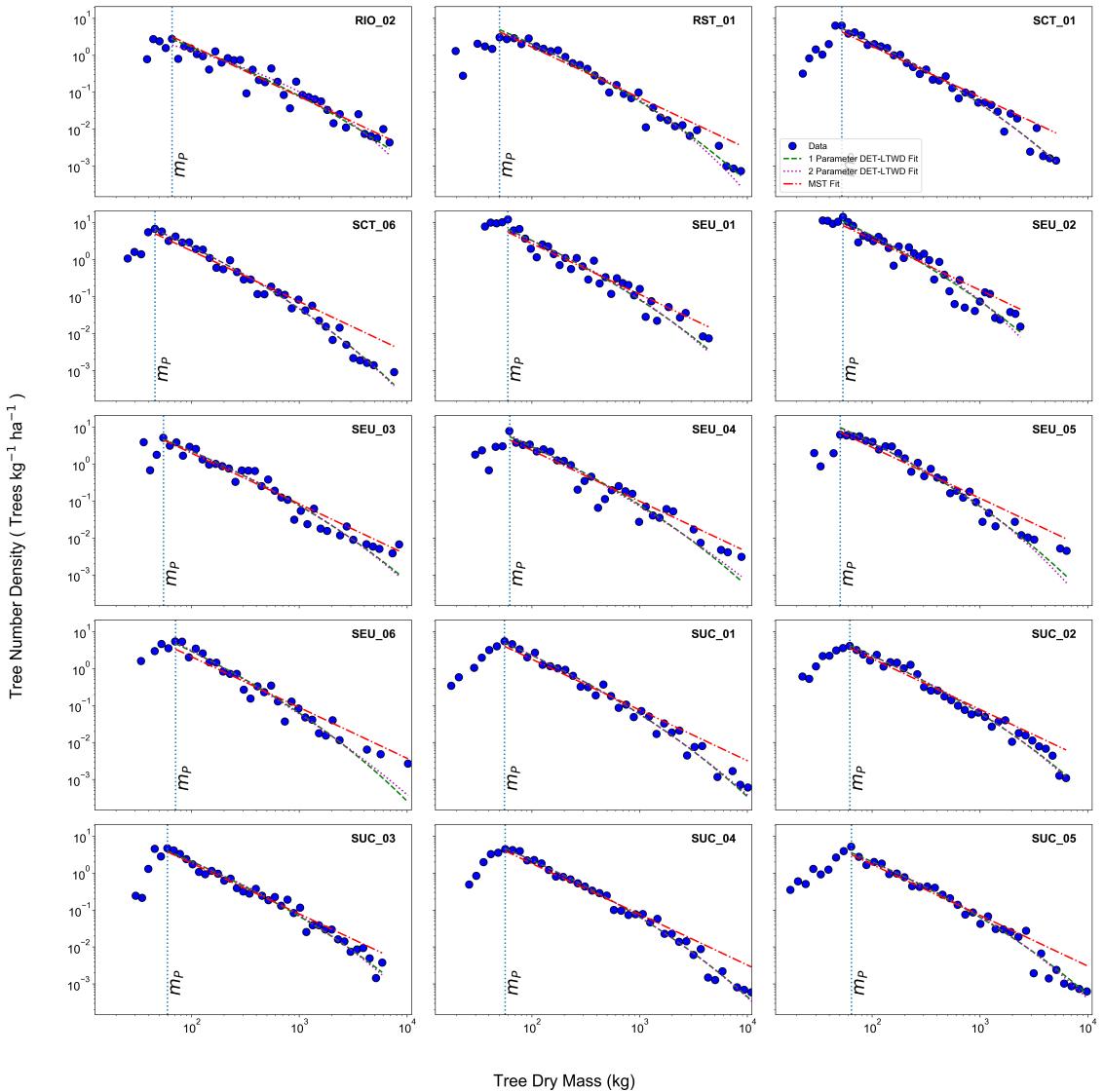


Figure S20: Mass Size Distributions of Individual Forest Plots.

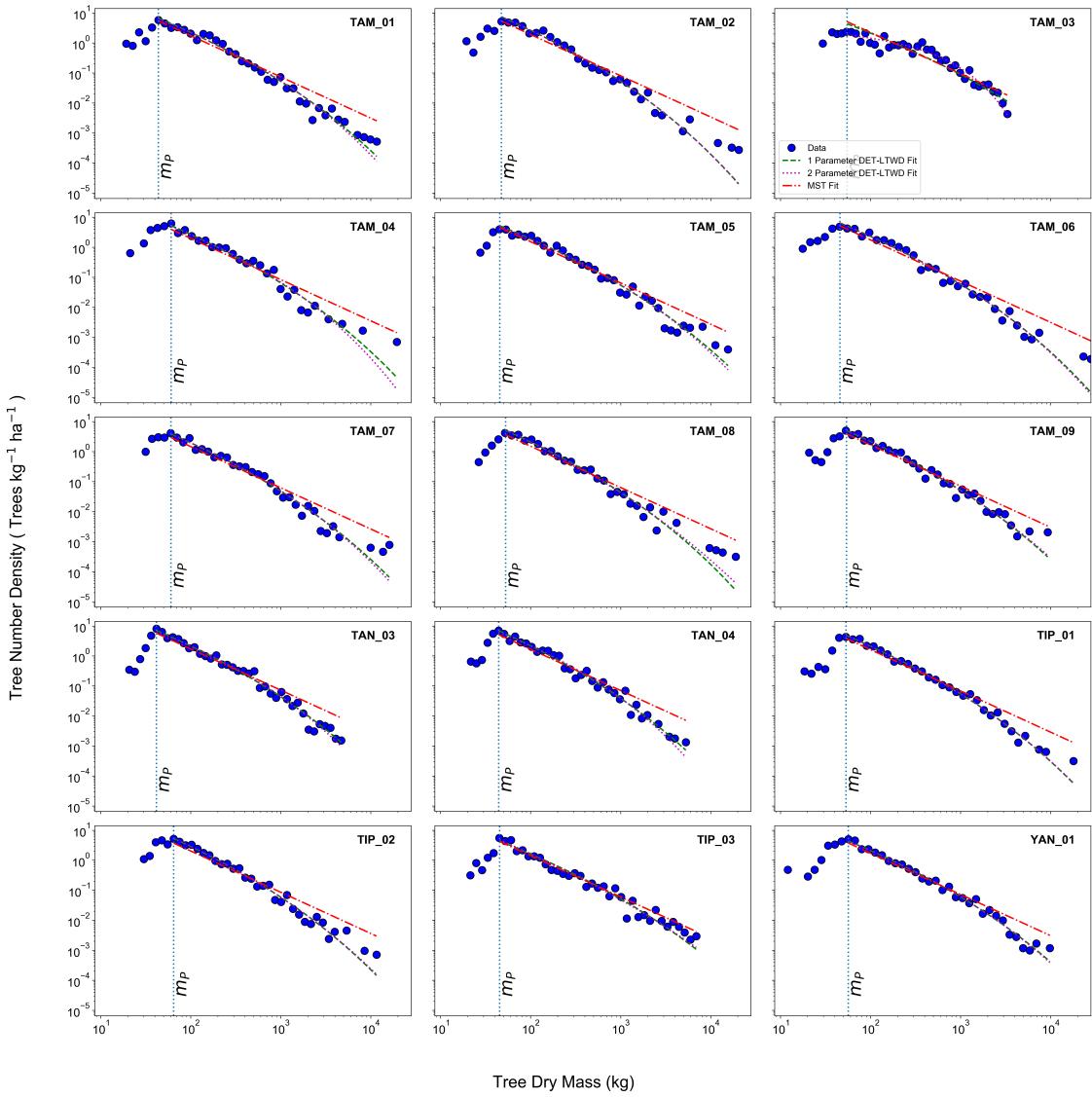


Figure S21: Mass Size Distributions of Individual Forest Plots.

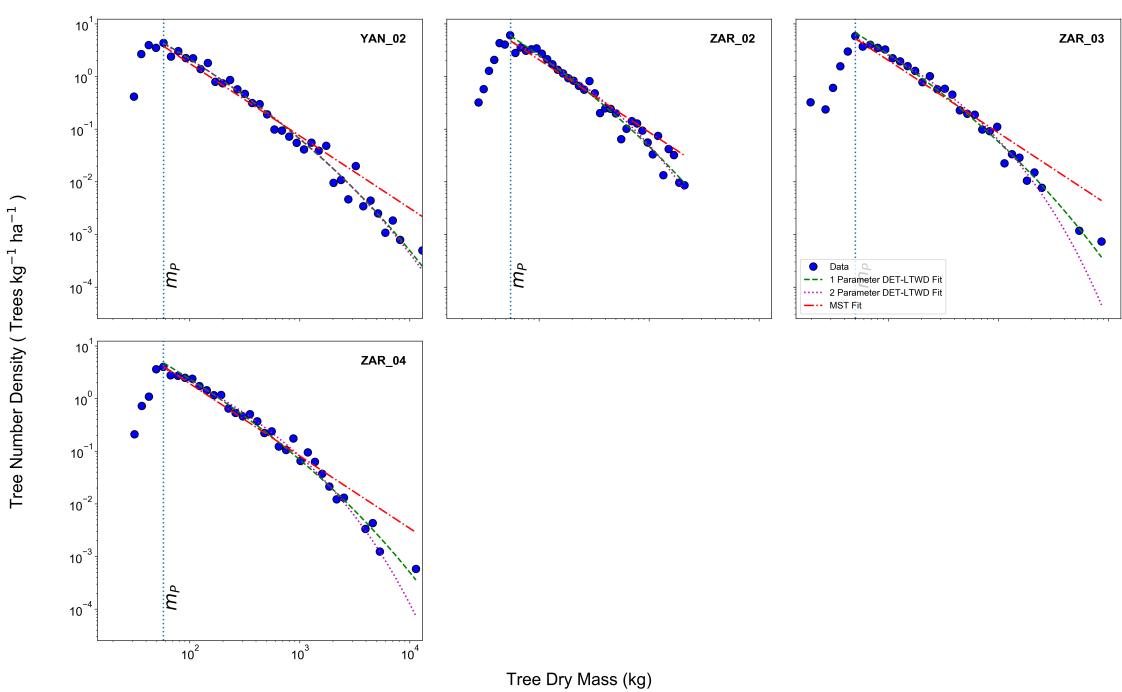


Figure S22: Mass Size Distributions of Individual Forest Plots.

7 Cumulative Biomass v Tree Mass

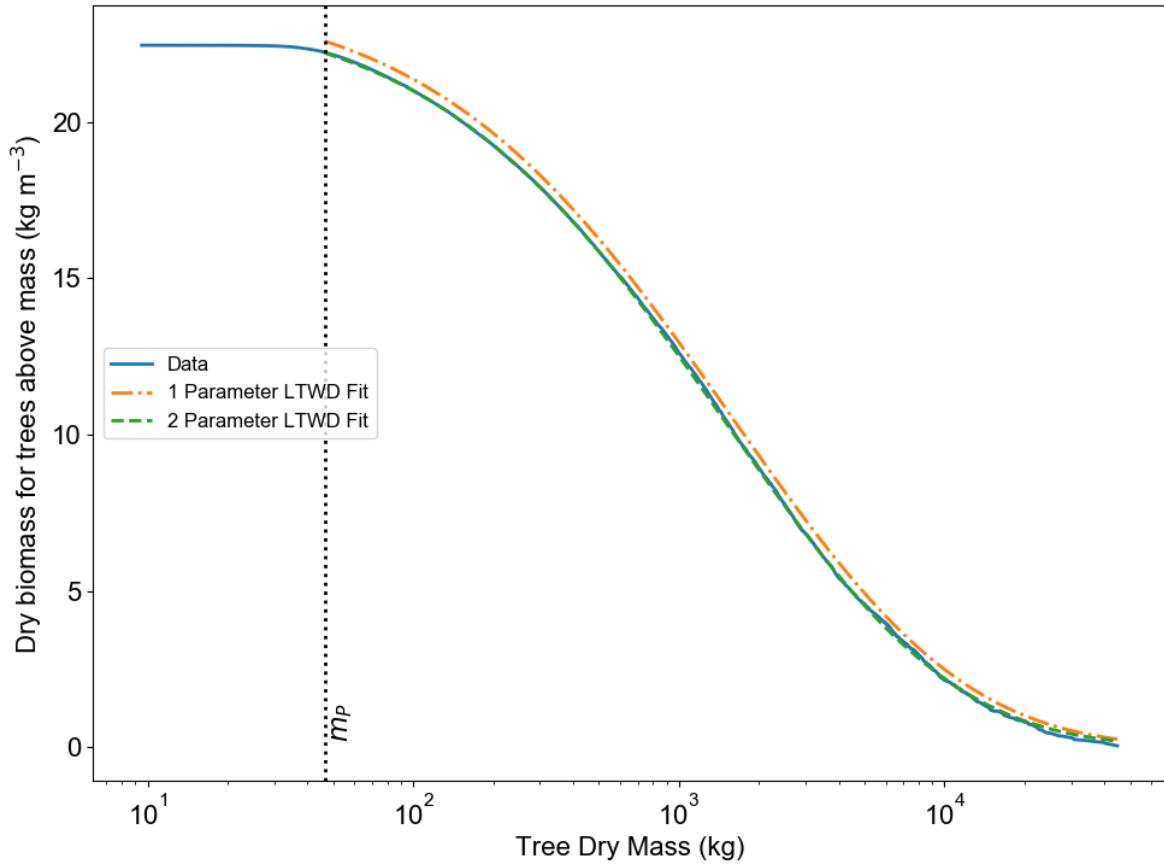


Figure S23: Shows the amount of biomass for all S.America consisting of trees equal or greater than a given tree mass, infinite maximum tree size assumption.

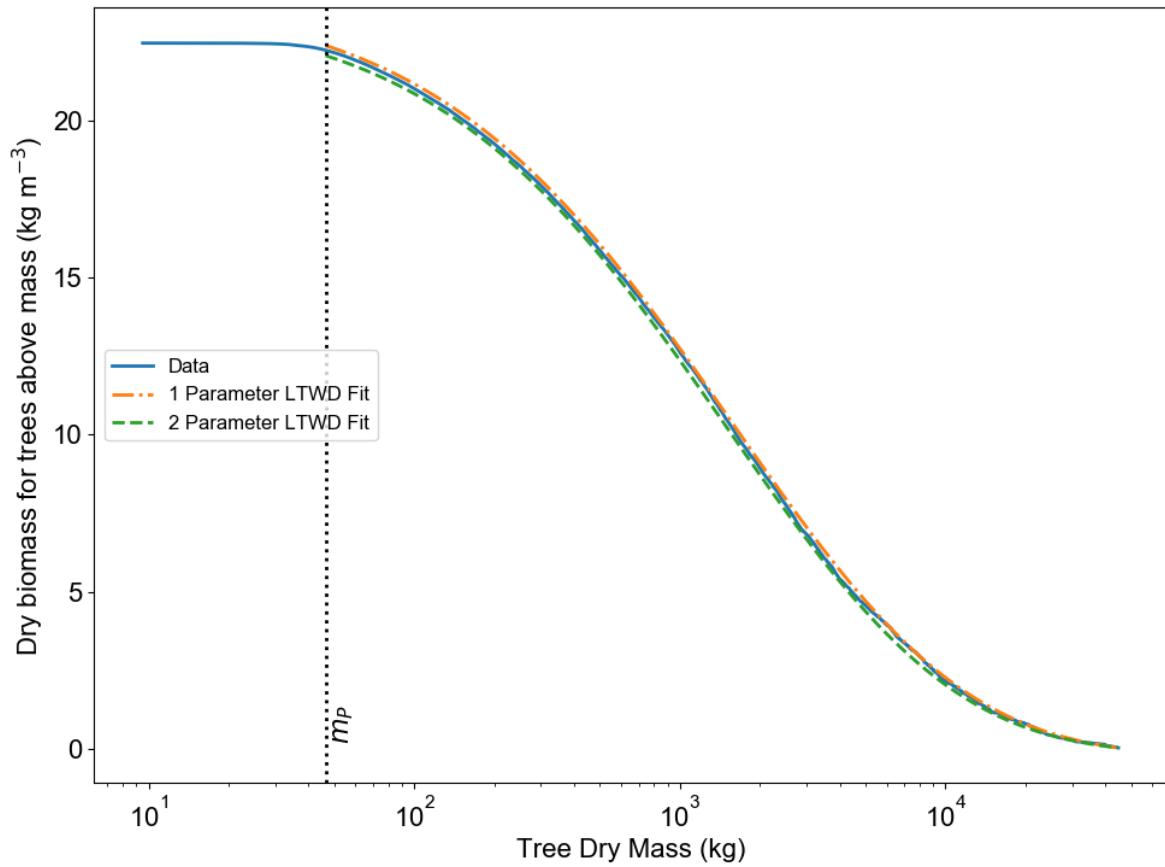


Figure S24: Shows the amount of biomass for all S.America consisting of trees equal or greater than a given tree mass, finite maximum tree size assumption (theory corrected by largest tree in the dataset).

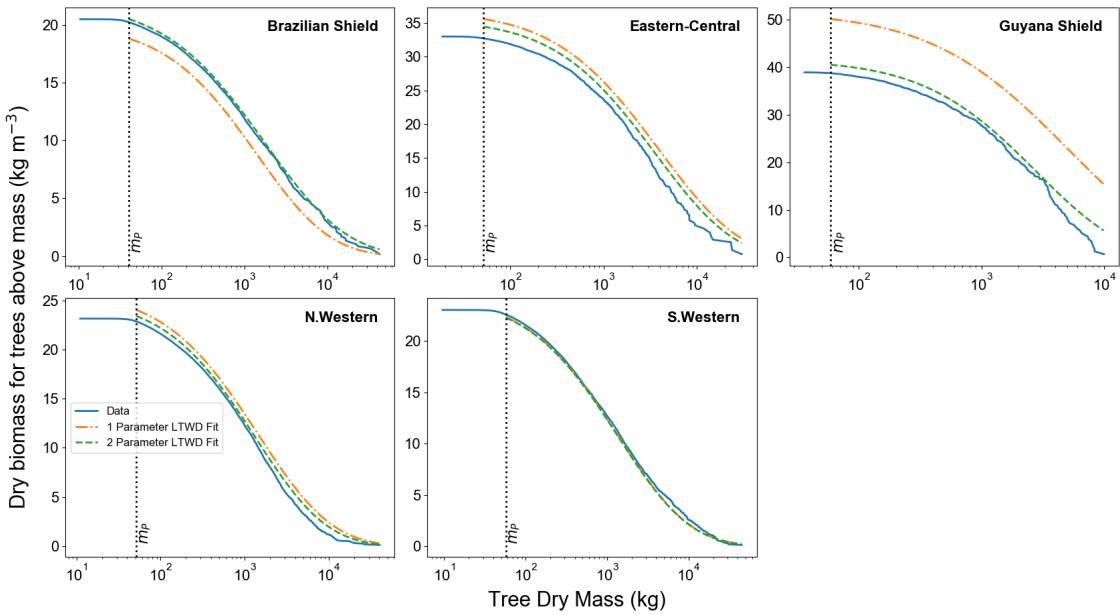


Figure S25: Shows the amount of biomass for each allometric region consisting of trees equal or greater than a given tree mass, infinite maximum tree size assumption.

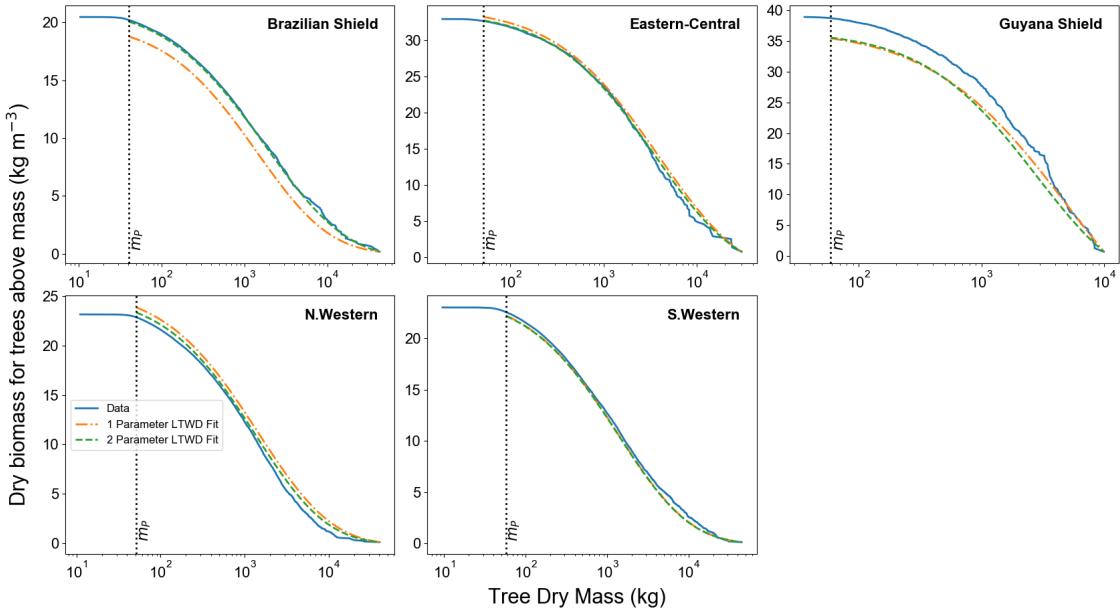


Figure S26: Shows the amount of biomass for each allometric region consisting of trees equal or greater than a given tree mass, finite maximum tree size assumption (theory corrected by largest tree in the dataset).

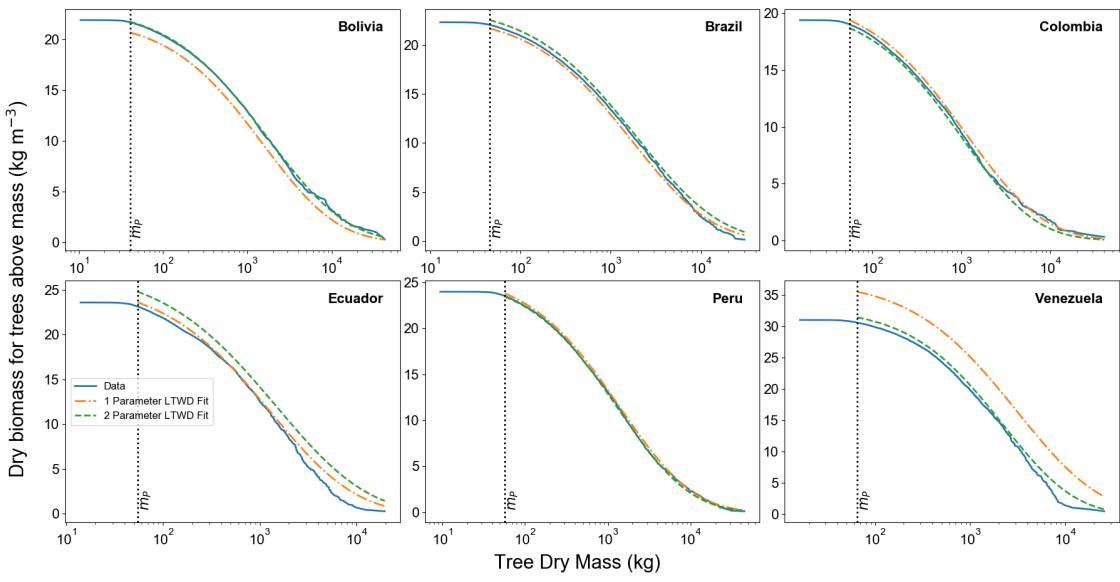


Figure S27: Shows the amount of biomass for each country consisting of trees equal or greater than a given tree mass, infinite maximum tree size assumption.

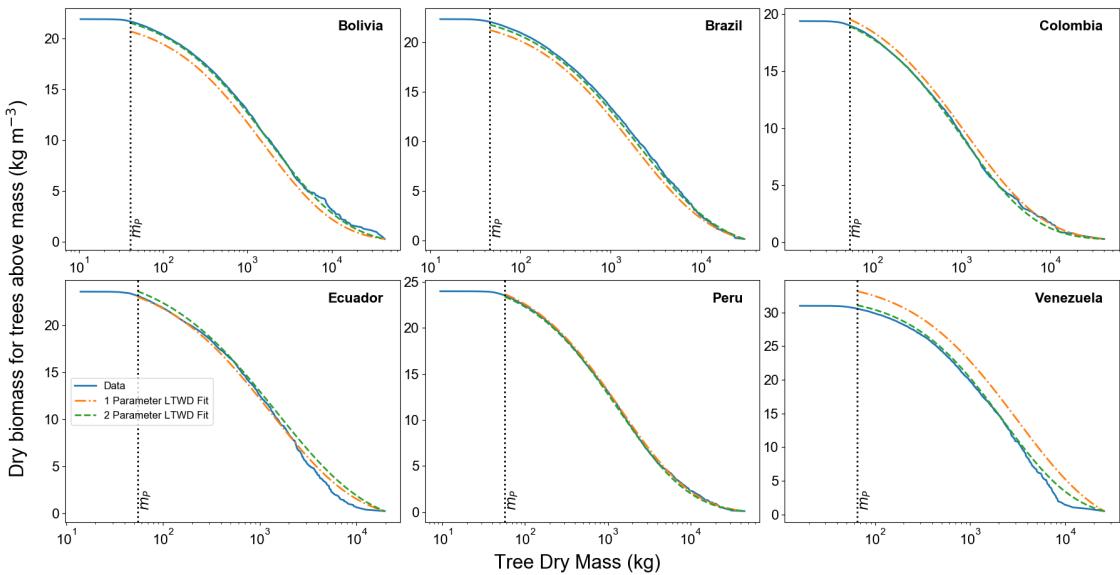


Figure S28: Shows the amount of biomass for each country consisting of trees equal or greater than a given tree mass, finite maximum tree size assumption (theory corrected by largest tree in the dataset).

8 Cumulative Biomass v Height and Trunk Diameter

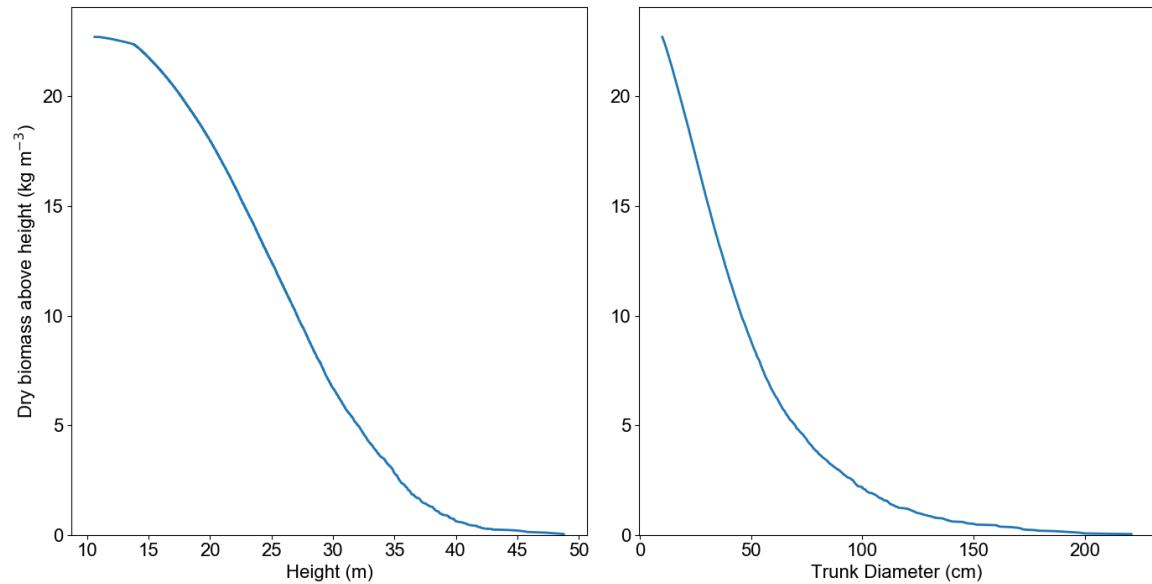


Figure S29: Shows the amount of biomass for all S.America consisting of trees equal or greater than a) a given height and b) a given diameter.

9 Effect of Sample Size on MST AIC Scores

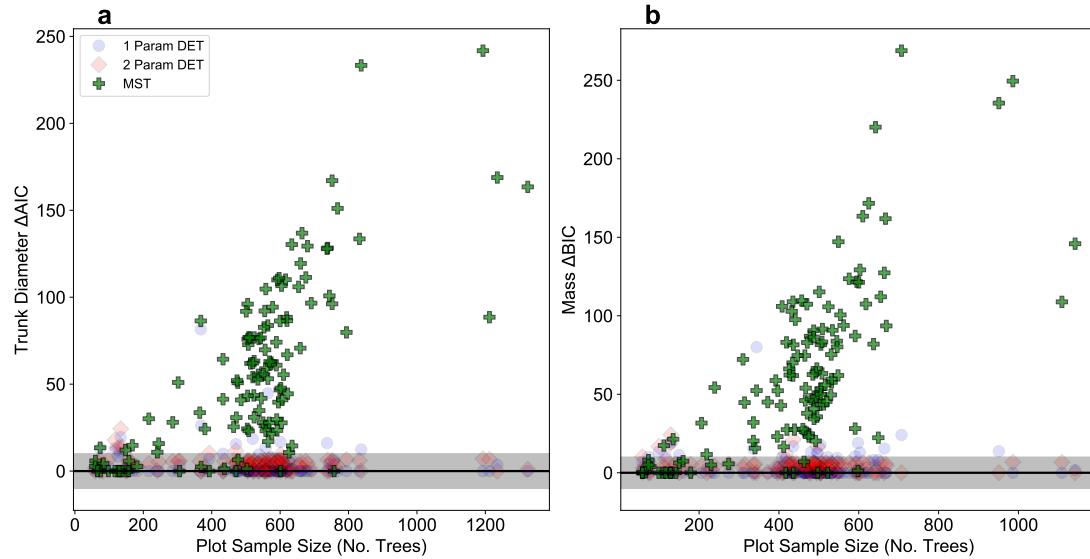


Figure S30: Shows the effect of forest plot sample size on the difference between MST AIC score and that of the best fitting model. Both DET models also shown for comparison. As the sample size increases the MST AIC scores increase (ie MST worsens). a) Trunk Diameter b) Mass.

10 Log Likelihood for Fitting DBH Distributions

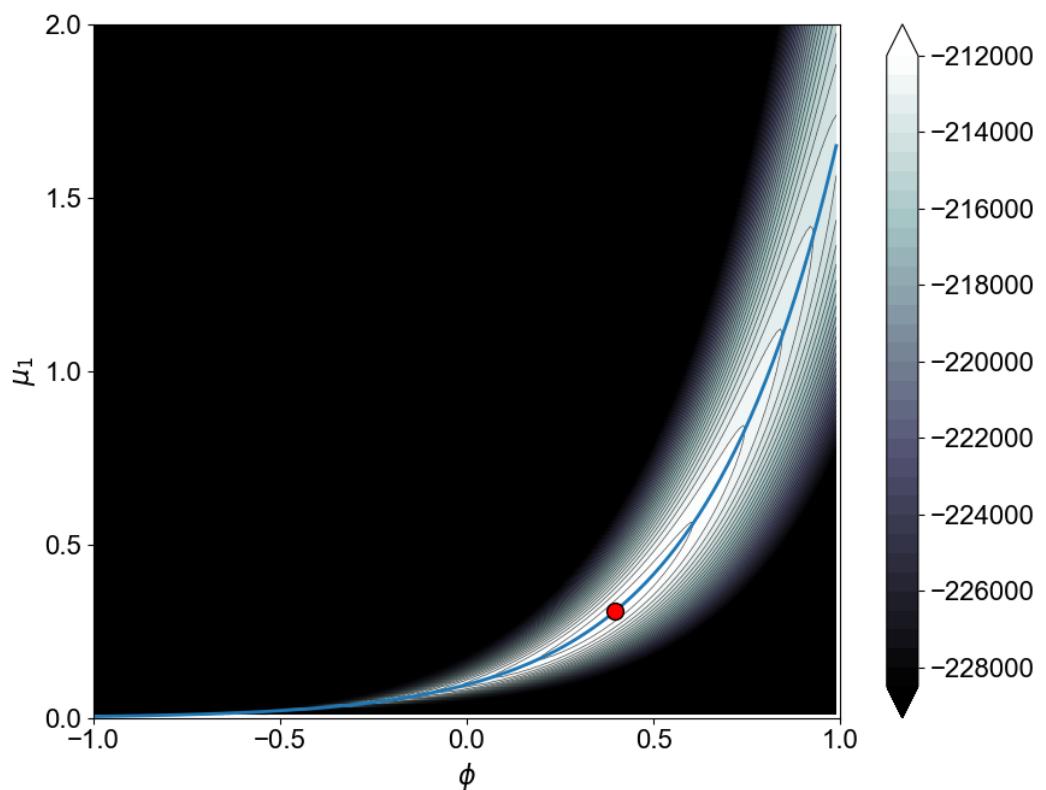


Figure S31: Shows the Log Likelihood (contours) for various choices of parameters ϕ and μ_1 for the whole dataset (all forest plots together). The line shows the best fit for a given ϕ and the red circle is the best fit found by MLE.

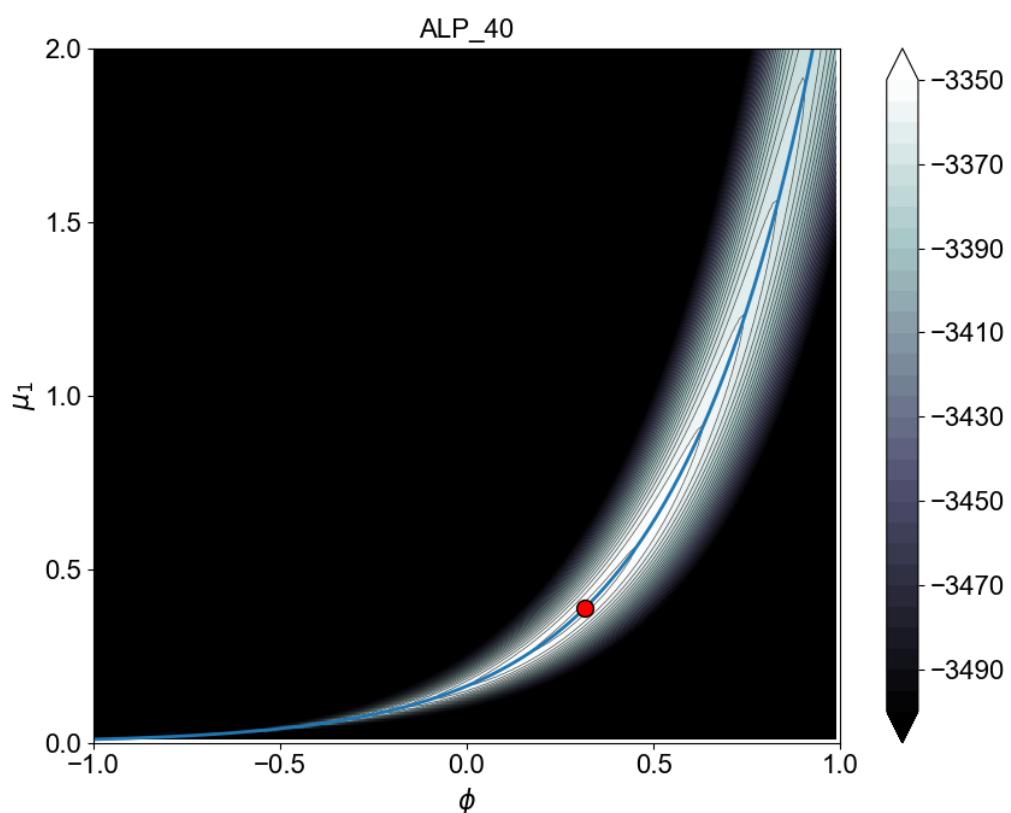


Figure S32: Shows the Log Likelihood (contours) for various choices of parameters ϕ and μ_1 for forest plot ALP_40. The line shows the best fit for a given ϕ and the red circle is the best fit found by MLE.