



*Supplement of*

## **Assessing global-scale organic matter reactivity patterns in marine sediments using a lognormal reactive continuum model**

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1 **1. Details of investigated sites.**

2 **Table S1. Supplementary sources of data for Fig. 3 in the main text.**

<b>longitude</b>	<b>latitude</b>	<b>Sea area</b>	<b>Water depth</b>	$\omega$	$G_{max}$	<b>Ref.</b>
(°)	(°)	(Ocean)	(m)	(cm/a)	(wt%)	
72°45' W	42°15' N	Long Island Sound	10	0.2	1.7	(1)
131°75' E	43°11' N	Amur Bay	1	0.3	2.9	(29)
130°72' E	42°61' N	Ekspeditsii Bight	1.5	0.4	2.1	(29)
131°83' E	42°96' N	Voevoda bight	2.1	0.3	6.2	(29)
09°08' E	56°53.10' N	Livø Strait	7	0.1	6.2	(27)
04°18' E	51°77' N	Haringvliet Lake	7.5	1.01	4.73	(26)
123°29' W	48°36' N	NorthCarolina,USA	8	0.15	4.5	(9)
09°09' E	56°50.32' N	Bjørnsholm Bay	10	0.1	12	(27)
70°63' W	41°73.8' N	Buzzards Bay	15	0.2	1.9	(14)
70°62' W	41°74.4' N	Buzzards Bay	16	0.2	2.1	(14)
71°41' W	41°43.9' N	Rhode Island	17	0.2	16	(14)
89°44' W	29°07' N	Mississippi River	20	0.8	0.9	(22)
89°35' W	29°06' N	Mississippi River	20	0.8	0.52	(22)
73°42' W	43°81' S	Southern Chilean	20	0.29	1.4	(23)
73°51' W	43°47' S	Southern Chilean	20	0.29	3.2	(23)
73°63' W	44°62' S	Southern Chilean	20	0.29	3.1	(23)
73°18' W	45°31' S	Southern Chilean	20	0.29	1.6	(23)
74°46' W	44°51' S	Southern Chilean	20	0.29	2.4	(23)
74°53' W	45°68' S	Southern Chilean	20	0.29	1.5	(23)
13°86' E	54°74' N	Arkona Bassin	35	0.048	3.8	(21)
13°79' E	54°80' N	Arkona Bassin	44	0.074	4.1	(21)
13°66' E	54°94' N	Arkona Bassin	44	0.19	5.2	(21)
13°61' E	54°91' N	Arkona Bassin	44	0.215	4.9	(21)
136°78' W	34°29' N	Ago Bay	50	0.2	2.5	(18)
136°72' W	34°30' N	Ago Bay	50	0.2	2.4	(18)
136°70' W	34°25' N	Ago Bay	50	0.2	2.48	(18)
14°18' E	23°46.52' S	Namibian shelf	110	0.34	12	(16)
86°13' W	09°37' N	Costa Rica	160	0.01	2.4	(20)
86°11' W	09°39' N	Costa Rica	160	0.01	1.75	(20)
86°15' W	09°42' N	Costa Rica	160	0.01	1.6	(20)
123°25' W	48°32' N	Saanich Inlet	170	0.69	4.8	(7)
05°12' W	78°93' N	East Greenland shelf	189	0.37	0.72	(24)
12°77' W	74°99' N	East Greenland shelf	320	0.46	0.48	(24)
04°59' W	75°06' N	Central Greenland	272	0.09	0.62	(24)
123°30' W	48°37' N	Saanich Inlet	210	1.04	3.8	(11)
77°39' W	12°0.5' S	Peru continental	186	0.23	14	(2)
77°40' W	12°0.5' S	Peru continental	255	0.23	7.9	(2)
76°50' W	13°37.3' S	Peru continental	370	0.14	20	(5)
76°51' W	13°37.3' S	Peru continental	370	0.04	20	(5)
77°57' W	11°15.1' S	Peru continental	186	0.15	14	(5)

78°07' W	11°20.6' S	Peru continental	411	0.15	20	(4)
77°24' W	12°23' S	Peruvian margin	297	0.06	17.2	(33)
77°10' W	12°13' S	Peruvian margin	306	0.3	3.1	(33)
77°15' W	12°17' S	Peruvian margin	409	0.5	14.8	(33)
24°59' W	71°21' N	Weddell Sea	422	0.58	0.28	(25)
120°14' W	34°19.3' N	Santa Barbara Basin	430	0.2	2.8	(13)
120°01' W	34°14.3' N	Santa Barbara Basin	578	0.2	3.2	(13)
120°02' W	34°16.0' N	Santa Barbara Basin	585	0.2	2.6	(13)
12°85' E	38°13' N	Castellammare	550	0.2	1.1	(28)
12°91' E	38°14' N	Castellammare	550	0.2	0.85	(28)
146°00' E	49°44.88' N	Sea of Okhotsk	613	0.093	2.1	(30)
144°04' E	54°26.52' N	Sea of Okhotsk	685	0.022	1.7	(30)
144°42' E	52°43.88' N	Sea of Okhotsk	713	0.115	1.8	(30)
144°14' E	53°50.00' N	Sea of Okhotsk	771	0.092	1.7	(30)
146°02' E	48°22.73' N	Sea of Okhotsk	1256	0.013	1.6	(30)
146°08' E	48°11.83' N	Sea of Okhotsk	1602	0.01	0.83	(30)
77°11' W	12°14' S	Peruvian margin	695	0.3	6.1	(33)
77°35' W	12°31' S	Peruvian margin	756	0.08	2.9	(33)
77°40' W	12°35' S	Peruvian margin	770	0.052	4.6	(33)
02°45' W	62°79' N	Shetland Faeroe	777	0.68	1.2	(24)
119°42' E	22°29' N	South China Sea	1004	0.08	0.78	(32)
38°51' W	77°39' N	Weddell Sea	1097	0.21	0.42	(25)
31°24' W	74°24' N	Weddell Sea	1178	0.14	0.36	(25)
09°67' W	68°71' N	Weddell Sea	1185	0.08	0.32	(25)
27°64' W	73°17' N	Weddell Sea	1566	0.24	0.35	(25)
22°36' W	73°36' N	Weddell Sea	1598	0.24	0.25	(25)
27°16' W	73°48' N	Weddell Sea	444	0.74	0.21	(25)
118°83' W	32°85' N	Southern California	1500	0.06	6.5	(23)
65°35' E	20°00' N	Arabian Sea	3000	0.0024	0.56	(31)
68°33' E	15°36' N	Arabian Sea	3500	0.0025	0.95	(31)
64°33' E	14°24' N	Arabian Sea	3500	0.0024	0.63	(31)
65°02' E	10°03' N	Arabian Sea	3500	0.0012	0.53	(31)
60°31' E	16°10' N	Arabian Sea	4000	0.0034	3.8	(31)
71°24' W	36°10' N	NW Atlantic	4215	0.01	1.2	(8)
70°50' W	32°59.3' N	NW Atlantic	4595	0.003	0.28	(8)
60°50' W	35°19.8' N	NW Atlantic	5341	0.01	0.34	(8)
136°03' E	28°59.00' N	Philippine Sea	2972	0.00006	0.34	(6)
135°93' E	29°08.00' N	Shikoku Basin	2972	0.00006	0.5	(6)
135°99' E	29°10.00' N	Shikoku Basin	2972	0.00006	0.42	(6)
134°93' E	28°59.00' N	Shikoku Basin	2972	0.00002	0.27	(6)
151°39' W	13°41.7' N	the North Pacific	5686	0.00015	0.4	(10)
148°57' W	6°13.2' N	the North Pacific	5718	0.00019	0.23	(10)
146°09' W	9°30.5' N	the North Pacific	5004	0.00023	0.36	(10)
146°01' W	9°19.3' N	the North Pacific	5205	0.00032	0.45	(10)

145°59' W	9°31.5' N	the North Pacific	5164	0.00036	0.26	(10)
144°49' W	3°59.5' N	the North Pacific	5214	0.00036	0.22	(10)
145°01' W	3°50.2' N	the North Pacific	4599	0.00041	0.23	(10)
148°44' W	9°15.0' N	the North Pacific	4619	0.00043	0.35	(10)
148°46' W	9°06.5' N	the North Pacific	5144	0.00058	0.32	(10)
151°39' W	14°41.7' N	the North Pacific	5686	0.0002	0.2	(10)
148°47' W	9°06.5' N	the North Pacific	5189	0.0012	0.25	(10)
168°46' W	65°01.7' S	South flank Pacific	2930	0.00258	0.5	(12)
174°14' W	66°49.7' S	South flank Pacific	3260	0.0018	0.32	(12)
174°44' W	62°54.2' S	North flank Pacific	4139	0.00588	0.6	(12)
63°27' W	22°54.9' N	Nares Abyssal Plain	5868	0.0005	0.3	(15)
63°26' W	22°54.9' N	Nares Abyssal Plain	5868	0.0005	0.14	(15)
63°00' W	23°22.3' N	Nares Abyssal Plain	5878	0.0005	0.12	(15)
63°01' W	23°22.3' N	Nares Abyssal Plain	5878	0.0005	0.008	(15)
169°04' E	08°13' N	Equatorial Pacific	4239	<0.002	0.25	(17)
177°58' E	07°27' N	Equatorial Pacific	5269	<0.002	0.42	(17)
175°52' W	05°03' N	Equatorial Pacific	5867	<0.002	0.6	(17)
174°54' W	03°04' N	Equatorial Pacific	3572	<0.002	0.54	(17)
171°04' W	00°02' S	Equatorial Pacific	5352	<0.002	0.7	(17)
168°04' W	02°26' S	Equatorial Pacific	5361	<0.002	0.52	(17)
166°37' W	03°39' S	Equatorial Pacific	5469	<0.002	0.53	(17)
166°32' W	09°10' S	Equatorial Pacific	5283	<0.002	0.15	(17)
85°22' W	05°30' S	Peru Basin	4082	0.002	1.7	(19)
85°11' W	06°34' S	Peru Basin	4165	0.0006	0.72	(19)
88°27' W	07°40' S	Peru Basin	4127	0.0004	0.8	(19)
3.07 W	51.5 N	Severn estuary	8	0.43	2.9	(34)
4.85 E	43.31 N	Rhone zone	19	0.1	1.9	(35)
4.77 E	43.27 N	Rhone shelf	74	0.5	1.5	(36)
10.34 E	56.11 N	Aarhus Bay	15	0.32	3.8	(37)
13.78 E	54.8 N	Arkona Basin	43	0.0074	3.9	(38)
7.97 E	54.08 N	Helgoland Mud	29	1.3	1.1	(39)
9.75 E	57.92 N	Skagerrak S10	86	0.5	1.4	(40)
9.7 E	57.95 N	Skagerrak S11	150	0.5	0.7	(41)
9.6 E	58.05 N	Skagerrak S13	386	0.5	2.1	(42)
63.02 E	24.88 N	Arabian Sea	645	0.05	1.1	(43)
62.99 E	24.81 N	Arabian Sea	957	0.05	0.95	(44)
62.99 E	24.71 N	Arabian Sea	1586	0.05	0.92	(45)
168.8 W	54.57 N	Bering Sea	1476	0.0016	1.6	(46)
53.59 W	39.31 S	Argentine Basin	3687	0.008	1.2	(47)

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4 **Reference for supplementary Table 4**

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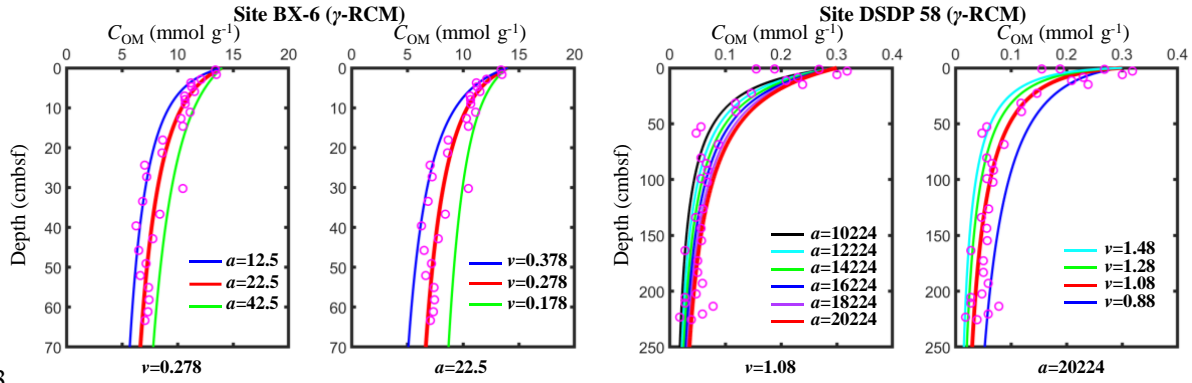
## 135 **2. Parameter sensitivity analysis for the *l*-RCM and the $\gamma$ -RCM**

136 We did parameter sensitivity analysis for  $\gamma$ -RCM and *l*-RCM, respectively. The results shown that  
137 when  $\nu$  is fixed value, the parameter  $a$  can vary over a wide range (from 10000 to 20000) while  
138 maintaining a relatively good fit ( $R^2 > 0.9$ ). However, when  $a$  is a fixed value, the variation of  
139 parameter  $\nu$  can cause a large fitting error. The results were shown in the Table S2 and Fig. S1.

140 Besides, we found when both  $a$  and  $v$  had a huge change,  $\gamma$ -RCM can also obtain a good fit result,  
 141 as shown in the Fig. S3.

142 **Table S2. Fitting results of parametric sensitivity analysis of  $\gamma$ -RCM**

Sensitivity analysis of $\gamma$ -RCM							
<b>BX-6</b>	<b><math>v=0.278</math></b>	$a=12.5$	$R^2=0.82$	<b>DSDP 58</b>	<b><math>v=1.08</math></b>	$a=10224$	$R^2=0.91$
		$a=22.5$	$R^2=0.93$			$a=12224$	$R^2=0.92$
		$a=32.5$	$R^2=0.86$			$a=14224$	$R^2=0.93$
		$a=42.5$	$R^2=0.74$			$a=16224$	$R^2=0.92$
		$a=52.5$	$R^2=0.61$			$a=18224$	$R^2=0.92$
						$a=20224$	$R^2=0.92$
	<b><math>a=22.5</math></b>	$v=0.178$	$R^2=0.56$		<b><math>a=20224</math></b>	$v=0.68$	$R^2=0.63$
		$v=0.278$	$R^2=0.93$			$v=0.88$	$R^2=0.84$
		$v=0.378$	$R^2=0.76$			$v=1.08$	$R^2=0.92$
						$v=1.28$	$R^2=0.93$
						$v=1.48$	$R^2=0.91$



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**Fig. S1. Parameter sensitivity analysis of  $\gamma$ -RCM.**

145 The  $l$ -RCM best-fit parameters are well fixed. According to the parametric sensitivity analysis, we  
 146 found that very small changes in parameters  $\mu$  and  $\sigma$  can cause large errors in the fitting results. The  
 147 results were shown in the Table S3 and Fig. S2.

148 **Table S3. Fitting results of parametric sensitivity analysis of  $l$ -RCM.**

Sensitivity analysis of $l$ -RCM							
<b>BX-6</b>	<b><math>\mu=2.24</math></b> <b><math>\times 10^{-3}</math></b>	$\sigma=1.031$	$R^2=0.71$	<b>DSDP</b>	<b><math>\mu=6.11</math></b> <b><math>\times 10^{-5}</math></b>	$\sigma=0.663$	$R^2=0.87$
		$\sigma=2.031$	$R^2=0.93$			$\sigma=1.663$	$R^2=0.92$
		$\sigma=3.031$	$R^2=0.88$			$\sigma=2.663$	$R^2=0.88$
		$\sigma=4.031$	$R^2=0.83$			$\sigma=3.663$	$R^2=0.81$
	<b><math>\sigma=2.031</math></b>	$\mu=1.24 \times 10^{-3}$	$R^2=0.62$		<b><math>\sigma=1.663</math></b>	$\mu=3.11 \times 10^{-5}$	$R^2=0.86$
		$\mu=2.24 \times 10^{-3}$	$R^2=0.93$			$\mu=6.11 \times 10^{-5}$	$R^2=0.92$
		$\mu=3.24 \times 10^{-3}$	$R^2=0.89$			$\mu=9.11 \times 10^{-5}$	$R^2=0.87$
		$\mu=4.24 \times 10^{-3}$	$R^2=0.82$			$\mu=12.11 \times 10^{-5}$	$R^2=0.82$

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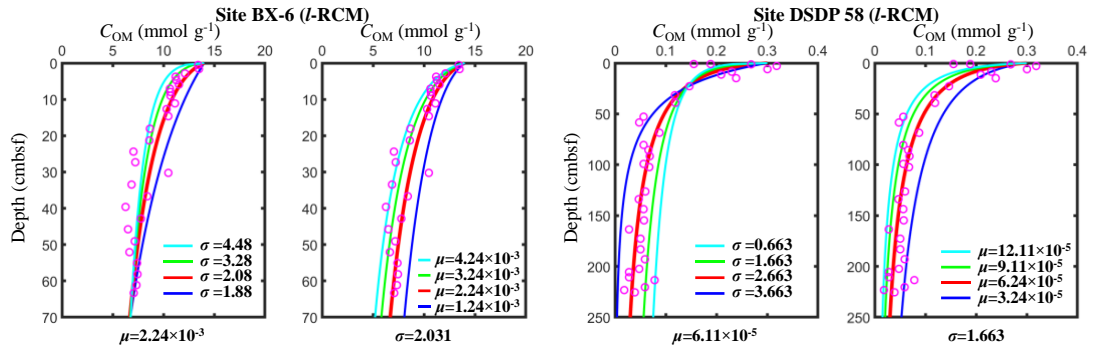


Fig. S2. Parameter sensitivity analysis of *l*-RCM.

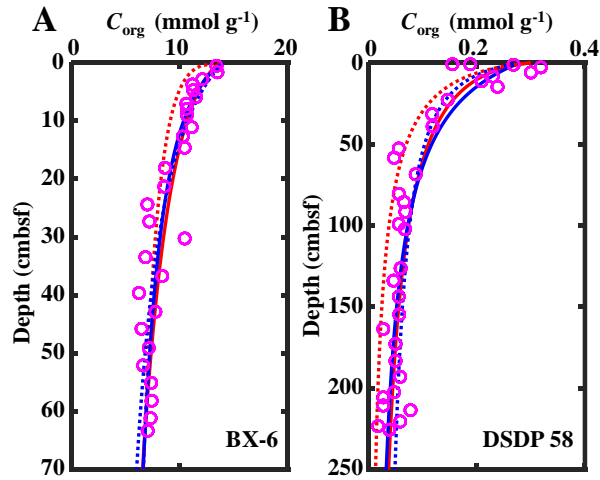


Fig. S3. A: pink circles are measured OM data. The red solid ( $\mu=2.23 \times 10^{-3}$ ,  $\sigma=2.03$ ,  $R^2=0.93$ ) and dotted lines ( $\mu=2.23 \times 10^{-3}$ ,  $\sigma=1.03$ ,  $R^2=0.82$ ) are the results of *l*-RCM, the blue solid ( $\nu=0.278$ ,  $a=22.5$ ,  $R^2=0.93$ ) and dotted lines ( $\nu=0.5$ ,  $a=53$ ,  $R^2=0.91$ ) are the results of  $\gamma$ -RCM. B: pink circles are measured OM data. The red solid ( $\mu=6.11 \times 10^{-5}$ ,  $\sigma=1.66$ ,  $R^2=0.92$ ) and dotted lines ( $\mu=8.8 \times 10^{-5}$ ,  $\sigma=1.36$ ,  $R^2=0.78$ ) are the results of *l*-RCM, the blue solid ( $\nu=1.08$ ,  $a=20225$ ,  $R^2=0.92$ ) and dotted lines ( $\nu=0.5$ ,  $a=4024$ ,  $R^2=0.89$ ) are the results of  $\gamma$ -RCM.