

Appendix

1 Ecosystem model

The implementation of the ecosystem model is a modification of previous work [1, 2]. The main difference is the introduction of an additional detritus compartment which allows to simulate differing decay time scales of phosphorous and nitrogen. The seven prognostic variables are: nitrate, phosphate, (non-nitrogen-fixing) phytoplankton, zooplankton, two detritus compartments describing nitrogen and phosphorus content and dissolved oxygen. Each prognostic variable C is determined following:

$$\frac{\partial C}{\partial t} = T + sms, \quad (1)$$

where T represents all diffusive and advective transport terms. sms denote the source minus sink terms, which describe the biogeochemical interactions as follows:

Phytoplankton (P) equation:

$$sms(P) = \bar{J}P - G(P)Z - \mu_P P \quad (2)$$

Zooplanton (Z) equation:

$$sms(Z) = \gamma_1 G(P)Z - \gamma_2 Z - \mu_Z Z^2 \quad (3)$$

Nitrogen detritus (D_N) equation:

$$sms(D_N) = (1 - \gamma_1) G(P)Z + \mu_P P + \mu_Z Z^2 - \mu_{D_N} D_N - w_s \frac{\partial D_N}{\partial z} \quad (4)$$

Phosphorus detritus (D_P) equation:

$$sms(D) = (1 - \gamma_1) G(P)Z + \mu_P P + \mu_Z Z^2 - \mu_{D_P} D_P - w_s \frac{\partial D_P}{\partial z} \quad (5)$$

Nitrate (NO_3) equation:

$$sms(NO_3) = (\mu_D D + \gamma_2 Z) \left(1 - 0.8 R_{O:N} r_{sox}^{NO_3}\right) - \bar{J}P \quad (6)$$

Phosphate (PO_4) equation:

$$sms(PO_4) = \mu_D D + \gamma_2 Z - \bar{J}P \quad (7)$$

1.1 Phytoplankton growth

The function $\bar{J} = \bar{J}(I, NO_3, PO_4)$ provides the growth rate of non-diazotrophic phytoplankton determined from irradiance (I), NO_3 , PO_4 ,

$$\bar{J}(I, NO_3, PO_4) = \min(J_I, J_{max} u_{NO_3}, J_{max} u_{PO_4}), \quad (8)$$

The maximum growth rate J_{max} is a function of temperature (T):

$$J_{max}(T) = a \cdot \exp\left(\frac{T}{T_b}\right) \quad (9)$$

such that growth rates increase by a factor of ten over the temperature range of -2 to 34 °C. We use $a = 0.6 \text{ d}^{-1}$ for the maximum growth rate at 0 °C. Under nutrient-replete conditions, the light-limited growth rate J_I is calculated according to:

$$J_I = \frac{J_{max}\alpha I}{[J_{max}^2 + (\alpha I)^2]^{1/2}} \quad (10)$$

where α is the initial slope of the photosynthesis vs. irradiance (P-I) curve.

Nutrient limitation is represented by the product of J_{max} and the nutrient uptake rates $u_{\text{NO}_3} = \text{NO}_3 / (k_{\text{NO}_3} + \text{NO}_3)$ and $u_{\text{PO}_4} = \text{PO}_4 / (k_{\text{PO}_4} + \text{PO}_4)$, with $k_{\text{PO}_4} = k_{\text{NO}_3} R_{\text{PO}_4:\text{NO}_3}$ providing the respective nutrient uptake rates.

1.2 Grazing

Zooplankton grazing of (non-nitrogen-fixing) phytoplankton $G(P)$ is parameterized using a Holling type III function:

$$G(P) = \frac{g\epsilon P^2}{g + \epsilon P^2} \quad (11)$$

1.3 Sinking of Detritus

The rate of sinking of Detritus w_s is a linear function of depth z but can not exceed a maximum value of w_{Dmax} :

$$w_s = w_s(z) = \min(w_{\text{D0}} + m_w z, w_{\text{Dmax}}). \quad (12)$$

1.4 Ecosystem model parameters

Parameter	Symbol	Value	Units
Phytoplankton (P) Coefficients			
Initial slope of P-I curve	α	0.025	$\text{day}^{-1}/(\text{W m}^{-2})$
Maximum growth rate	a	0.6	day^{-1}
E-folding temperature of biotic rates	T_b	15.65	$^{\circ}\text{C}$
Half-saturation constant for N uptake	k_{NO_3}	0.5	mmol m^{-3}
Specific mortality rate of (non nitrogen-fixing) phytoplankton	μ_P	0.03	day^{-1}
Zooplankton (Z) Coefficients			
Assimilation efficiency	γ_1	0.75	
Maximum grazing rate	g	2.0	day^{-1}
Prey capture rate	ϵ	1.0	$(\text{mmol m}^{-3})^{-2} \text{day}^{-1}$
(Quadratic) mortality	μ_Z	0.2	$(\text{mmol m}^{-3})^{-2} \text{day}^{-1}$
Excretion	γ_2	0.03	day^{-1}
Detrital (D) Coefficients			
Detrital nitrogen remineralization rate	μ_{DN}	0.05	day^{-1}
Euphotic layer detrital phosphorus remineralization rate	μ_{DPS}	0.1	day^{-1}
Detrital phosphorus remineralization rate	μ_{DP}	0.05	day^{-1}
Sinking speed at surface	w_{D0}	7	m day^{-1}
Increase of sinking speed with depth	m_w	0.04	day^{-1}
Maximum sinking speed in water column	w_{Dmax}	40	m day^{-1}

References

- [1] A. Oschlies and V. Garçon, 1999: An eddy-permitting coupled physical-biological model of the North Atlantic. Part I: Sensitivity to advection numerics and mixed layer physics. *Global Biogeochem. Cycles*, **13**.
- [2] A. Schmittner, A. Oschlies, X. Giraud, M. Eby, and H.L. Simmons, 2005: A global model of the marine ecosystem for long term simulations: sensitivity to ocean mixing, buoyancy forcing, particle sinking and dissolved organic matter cycling. *Global Biogeochem. Cycles*, **19**.