

Detecting Tropical Forest Biomass Dynamics from Repeated Lidar Measurements

Supplementary Material

(1) Lidar Data Acquisition

LVIS (Laser Vegetation Imaging Sensor) is a medium altitude waveform digitizing Lidar measuring canopy height, ground elevation, and the waveform representing the vertical profile or the distribution of intercepted surfaces within the Lidar footprint (Hofton et al., 2002), at scan angles of $\pm 12^\circ$. Its expanded spatial coverage allows large scale mapping of topography, forest structure, and AGB (Weishampel et al., 2000; Drake et al., 2002a; Drake et al., 2002b). LVIS Lidar data were collected by NASA over BCI in 1998 (Blair et al., 1999; Dubayah and Drake, 2000). This 1998 Panama LVIS survey consists of 215,984 individual LVIS shots, of which 108,184 are located over BCI and used for this study. 3077 of these shots are located over the 50ha plot, which corresponds to an average density of 60 shots per ha, or 0.0006 shots per square meter. LVIS is flown at 1000m altitude and its large footprint (~20 m) generally exceeds the average crown diameter of large trees (King, 1996; Drake et al., 2003). LVIS accuracy has been reported to be better than 1 m (Hofton et al, 2000). Here, we consider that LVIS accuracy is less than 2m for our uncertainty analysis.

The airborne discrete-return Lidar (DRL) that acquired data in 2009 was a small footprint instrument, ranging between 0.25m and 0.60m footprint. It is a proven technique in quantifying sub-canopy topography and providing accurate vertical forest structure (Dubayah and Drake, 2000; Hyypä et al., 2001; Lefsky et al., 2002). The DRL data was collected at very low altitude (between 500 and 1500m) and included repeated passes at

scan angles of $\pm 17^\circ$, resulting in multiple measurements per square meter (up to 10 points or echoes per square meter) for precise characterization of vegetation structure.

DRL data were collected by Blom Corporation and Northrop Grumman as part of an NSF funded project, using an Optech 3100 Lidar scanning at a rate of 70Khz. The data were collected over 11 individual flights yielding a total of over 233 million laser shots, and over 528 million individual points, resulting in an average point density of 5.6 points per square meter (ppm^2), and 8.1 returns per square meter (rpm^2). The DRL data was post-processed by BLOM Corporation using Bentley's MicroStation to calibrate and filter the data. In addition to the automated filtering process, additional manual editing of the sub-canopy DEM was performed to produce a bare-earth DEM product. To ensure accuracy and compliance with the precision requirements, the ground surface was tested using 36 ground surveyed points on flat, hard, well defined surfaces, free of obstacles. The results of the vertical accuracy assessment determined an average error in height of -0.069 m, an RMSE value of 0.076 m and a standard deviation of 0.032 m. Horizontal accuracy for similar types of DRL has been reported to be 0.1 m (Evans and Hudak, 2007).

Table S1 summarizes the characteristics of both sensors and highlights their differences. Differences in footprint size and density of points have to be taken into account when extracting and analyzing the data. In order to have a fairer comparison between the two datasets, the DRL data was first aggregated at 20m resolution to calculate the relative height metrics at 1ha. Some areas are not covered by any LVIS shots, which makes it hard to compare the two surveys in these areas. At the 0.04ha scale, 180 subplots are not covered by any LVIS shots, out of 1250. These subplots were not included in the 0.04ha scale analysis. Geolocation errors are small (less than 1m for LVIS, and 0.1m for DRL)

but they are hard to quantify. They are considered negligible at the 1ha scale. However, they can be a source of error at smaller spatial scales, especially at 0.04ha.

Table S1 : LVIS and DRL sensors characteristics

| | LVIS | DRL |
|--------------------------------|-----------------------------------|---------------------|
| Footprint size | ≈20m | 0.25-60cm |
| altitude of flight | 1000m | 457.2m |
| scan angles | ± 12° | ± 17° |
| GPS horizontal accuracy | <1m | 0.1m |
| Density of points | 0.006ppm ² (50ha plot) | 5.6ppm ² |

(2) LVIS Calibration

To compare LVIS and DRL Lidar data for changes in vegetation structure requires the data to be cross-calibrated. We performed the cross-calibration of the sensors such that both provide the same ground elevation under forest canopy (Fricker et al., 2012). LVIS, being a large footprint Lidar (20-25 m), has a limited ability to detect ground in dense canopy forests, particularly in complex topographies, thus affecting vegetation height metrics and potentially causing errors in AGB estimations (Dubayah et al., 2010). In contrast, the DRL sensor provides an accurate estimate of ground elevation (average error of 0.069m) and vegetation height. A shortened LVIS laser profile will result in a general underestimation of biomass and vertical stratification.

Average vertical difference between the LVIS last-return points and the DRL ground surface across BCI was of 28.7 cm. (Fricker et al, 2012). Although the majority (82.3%) of all LVIS points matched discrete return elevations to 2 meters or less, significant LVIS last-return outliers were identified, ranging from 16.4 m below the ground surface, to

last-return points over 35.7 m above the ground surface across the island. Also, areas of high terrain slope show consistently more error in large-footprint Lidar ground detection. Because our goal is to obtain optimal AGB estimations and to reduce errors due to the sensors, LVIS data had to be corrected before it was used in our AGB estimation algorithm.

LVIS data was corrected based on a method developed by Fricker et al (2012). It uses slope to correct LVIS semi-automatically. They use the LVIS sub-canopy Digital Elevation Model (DEM) alone to estimate slope and apply the effects of terrain slope on sub- canopy topography. However, for the present study we had high-resolution Lidar data (DRL) over the whole island, so we simply used the DRL DEM as a reference for sub-canopy topography. The elevation difference between DRL and LVIS subcanopy topography was calculated for each LVIS shot by comparing the LVIS ground elevation to the DRL ground elevation in a 20m diameter circle around the center location of each shot, representing its footprint, using a nearest neighbor approach.

This difference (positive or negative) was then added to each LVIS vertical height metrics. The average difference between LVIS ground and DRL ground in the 50ha plot was $1\text{m} \pm 2.2\text{m}$. The result is a more accurate LVIS digital elevation model and improved LVIS estimates of forest structure (Fig. S1), benefiting vegetation modeling applications (Evans and Hudak, 2007).

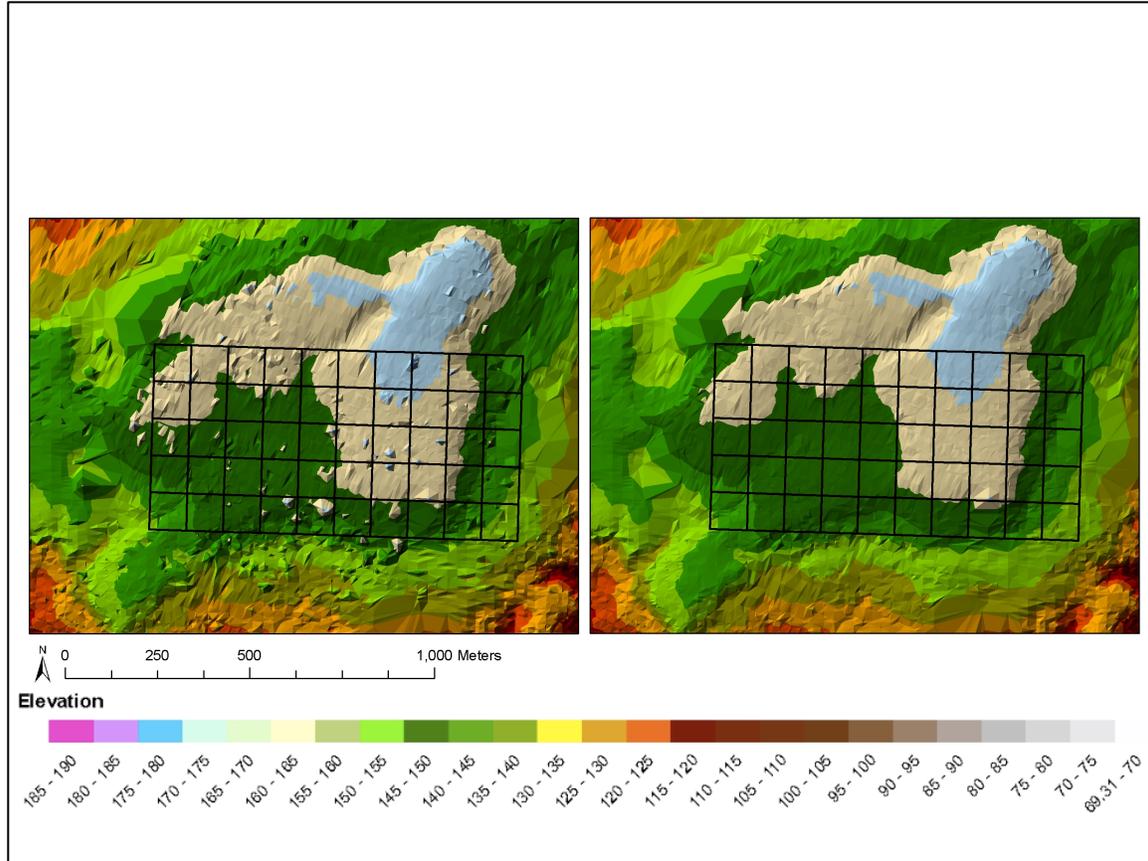


Figure S1 : LVIS ground correction. Raw LVIS ground returns (left) and corrected LVIS ground returns (right) using the DRL Digital Elevation Model.

Although the cross-calibration does not improve the relationships between LVIS and DRL intermediate metrics (RH25, RH50, RH75), it does improve RH100_{LVIS} relationship to RH100_{DRL} and to ground estimated AGB.

At the footprint level, correlation between RH100_{LVIS} and RH100_{DRL} went from $R^2 = 0.65$ to $R^2 = 0.73$ over the whole island.

At the subplot level, the relationship between RH100_{LVIS} and RH100_{DRL} is now closer to a one-to-one relationship, with an intercept of -1.68 and a coefficient of 1.02, versus an intercept of 4.46 and a coefficient of 0.88 without correction (1ha subplots).

As for the relationship between LVIS metrics and Ground AGB, correlation between

RH100_{LVIS} and AGB₂₀₀₀ went from $R^2=0.48$ without correction to $R^2 = 0.56$ with correction.

In spite of the above corrections, DRL and LVIS present too many differences to be used the same way to estimate AGB. They do not have the same footprint size, which makes it impossible to do a proper footprint to footprint comparison to estimate AGB as done in Dubayah et al. (2010). Furthermore, LVIS height metrics were directly calculated for each shot during post-processing, whereas we calculated the DRL height metrics using the vertical histogram of canopy height for a given pixel size (at 20m, 50m and 100m resolutions).

For these reasons, intermediate height metrics are different for DRL and LVIS. LVIS intermediate height metrics are systematically lower than DRL's. $RH25_{DRL} > RH25_{LVIS}$ by $9\text{m} \pm 2.8\text{m}$), $RH50_{DRL} > RH50_{LVIS}$ by $6.9\text{m} \pm 1.8\text{m}$), $RH75_{DRL} > RH75_{LVIS}$ by $5.1\text{m} \pm 1.3\text{m}$).

As a result, our different attempts to retrieve AGB change from Lidar by using ground estimated change (ΔAGB_{gnd}) and changes in RH (ΔRH) in our regression model did not show any relationship between these metrics.

Consequently, we used DRL and LVIS metrics independently in the determination of regression models for AGB estimations and proceeded in two steps : 1) estimation of AGB for both dates, 2) estimation of AGB change from these results.

(3) Lidar Height Metrics

To develop the relative height (RH) metrics at each scale, LVIS and DRL data were extracted using shape files partitioning the 50ha plot into respectively, 1250, 200 and 50

regions of interest representing the spatial scales of the analysis. From LVIS waveform data, relative height quartiles RH25, RH50, RH75 and RH100 were produced for each shot, where the RH100 metric represents the canopy top height or the maximum height of trees within the Lidar footprint.

We aggregated all the shots whose center coordinates fell into a given subplot to calculate the average of the LVIS the relative height metrics (and the maximum height for RH100), rather than having their whole footprint contained in the plot, as done previously (Dubayah et al., 2010). This choice was based on the sizes of the ground subplots used in this study. Because LVIS footprint is approximately 20m, very few shots fall entirely in a 20m*20m subplot. In addition to the four relative height metrics, mean canopy height (MCH) was also extracted.

A similar approach was used to convert the canopy height data from DRL at 1 m resolution to waveforms at the same spatial scales. The relative height metrics (RH25, RH50, RH75 and RH100) were produced from these waveforms, as well as MCH. This method is therefore slightly different than the one used to retrieve LVIS metrics at each spatial scale, since only the top canopy height at 1m resolution is known for DRL.

Although the RH metrics are individually correlated (Fig. S2), using the five of them improves the R^2 and the RMSE of the ground-based AGB vs. Lidar-based AGB, which confirms the results of the relative importance analysis. Unlike LVIS' metrics that are calculated from the percentiles of energy from LVIS shots, DRL's relative height metrics are directly calculated from RH100 distribution at each scale. Hence, the correlations between RH100 and the other RH metrics are higher for DRL than for LVIS (Fig. S2).

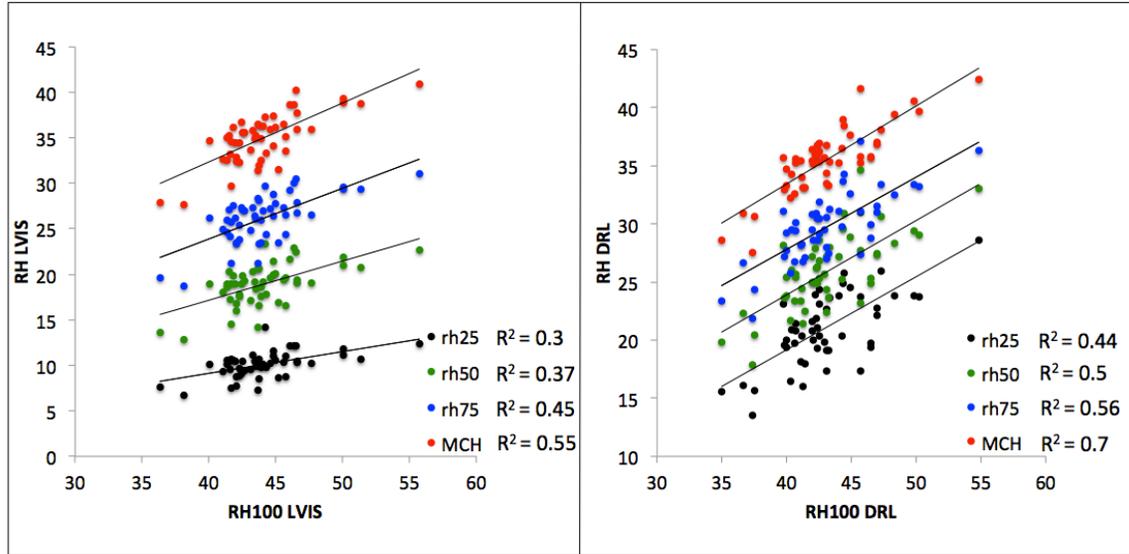


Figure S2: Relationship between the Lidar intermediate height metrics and the maximum height of the canopy derived at 1ha. Height metrics are correlated ($R^2 > 0.3$), but with significant variations that allow all five metrics to contribute to the biomass estimation.

(4) AGB estimation from ground measurements

Above-ground biomass density was estimated using an allometric regression model for moist tropical forests (Chave et al., 2005). The allometric method is based on the argument that the total aboveground biomass (AGB, in kg) of a tree with diameter D , measured at the breast height (DBH) 1.3m above ground must be proportional to the product of wood specific gravity (ρ) and tree stem volume. Stem volume, in turn, is proportional to the product of stem basal area and total tree height (H):

$$AGB = \exp[-2.977 + \ln(\rho D^2 H)] \cong 0.0509 \times \rho D^2 H \quad (\text{ES1})$$

Where \cong represents the mathematical identity meaning both formulas can be used in biomass estimation procedure. In the above equation, D (in cm) is measured during the inventory census periods, ρ (in g/cm^3) is provided from an available table of measurements for 123 species available in BCI, and tree height H (in m). Tree height measurements were not available for all the trees in the 50ha plot, so we developed a

relationship between DBH and height of 1835 trees among them 1604 trees with DBH > 10 cm, representing 154 species (Fig S3). The equation is provided in the log form for the entire range after testing different fits to the data with different DBH ranges:

$$H = -11.731 + 22.766 \log(D), D > 10 \text{ cm} \quad (\text{ES2})$$

We then used the height estimations as estimated from equation (ES2) into equation (ES1) for AGB estimation.

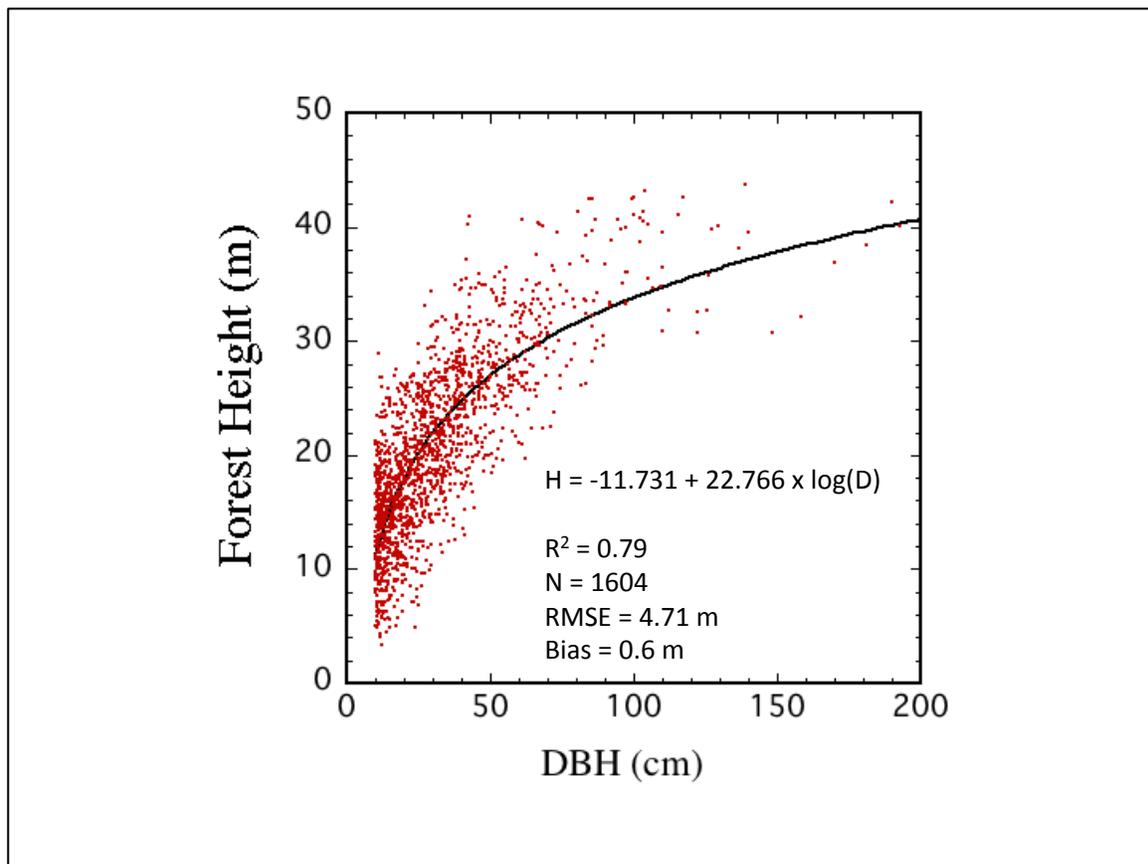


Figure S3 : Relationship between DBH (cm) and tree height H (in m).

The census data was filtered for anomalous and erroneous DBH measurements by first identifying all trees with growth larger than 45 mm/year and less than -5 mm/yr. The DBH of these trees were replaced using growth rates equal to mean growth rate of trees

in the same DBH class (Condit et al. 1993, 1999). The approach was extended to 2000, 2005, and 2010 when estimating biomass and biomass change from ground data. We calculated the errors associated with biomass estimation for each census at the scale of analysis and used these errors when analyzing the Lidar estimation of biomass and biomass change. See Chave et al., (2003) for more details on census data trimming procedures.

Table S2 : Ground Estimated AGB in 2000, 2005 and 2010 in 1ha subplots. The number of trees above 10cm DBH, basal area, and AGB are presented.

| plot id | 2000 | | | 2005 | | | 2010 | | |
|---------|------|-------|--------|------|-------|--------|------|-------|--------|
| | N00 | BA00 | AGB00 | N05 | BA05 | AGB05 | N10 | BA10 | AGB10 |
| 1 | 679 | 24.50 | 175.00 | 736 | 25.16 | 173.84 | 726 | 25.48 | 170.33 |
| 2 | 625 | 31.84 | 234.97 | 615 | 31.77 | 236.22 | 590 | 31.29 | 234.71 |
| 3 | 600 | 37.17 | 273.48 | 600 | 38.34 | 284.68 | 594 | 37.49 | 275.34 |
| 4 | 631 | 32.25 | 241.86 | 675 | 31.72 | 234.58 | 712 | 32.09 | 236.92 |
| 5 | 578 | 36.13 | 287.76 | 600 | 35.34 | 282.36 | 630 | 35.75 | 287.70 |
| 6 | 676 | 41.00 | 319.02 | 666 | 41.15 | 324.95 | 659 | 41.65 | 332.91 |
| 7 | 735 | 38.81 | 322.66 | 783 | 36.95 | 308.79 | 742 | 36.52 | 298.18 |
| 8 | 750 | 36.86 | 324.15 | 764 | 37.25 | 333.24 | 755 | 36.76 | 328.61 |
| 9 | 668 | 31.58 | 230.80 | 701 | 32.00 | 235.97 | 683 | 31.51 | 228.99 |
| 10 | 699 | 27.49 | 216.05 | 727 | 25.96 | 196.08 | 788 | 27.09 | 203.27 |
| 11 | 675 | 29.53 | 214.24 | 684 | 29.99 | 222.54 | 646 | 29.69 | 223.13 |
| 12 | 691 | 27.68 | 195.43 | 665 | 26.50 | 181.68 | 704 | 26.05 | 176.53 |
| 13 | 676 | 32.04 | 254.21 | 663 | 30.58 | 238.54 | 664 | 31.39 | 247.34 |
| 14 | 622 | 28.51 | 215.91 | 615 | 28.69 | 222.36 | 608 | 29.20 | 225.91 |
| 15 | 686 | 26.83 | 196.29 | 668 | 27.52 | 202.35 | 665 | 26.55 | 194.40 |
| 16 | 642 | 32.91 | 257.96 | 665 | 32.25 | 254.37 | 618 | 30.33 | 228.90 |
| 17 | 703 | 36.55 | 284.99 | 677 | 33.96 | 259.27 | 688 | 34.20 | 260.67 |
| 18 | 668 | 30.82 | 246.19 | 716 | 31.22 | 249.39 | 744 | 32.14 | 253.53 |
| 19 | 722 | 36.87 | 321.76 | 723 | 36.91 | 324.40 | 696 | 32.91 | 274.80 |
| 20 | 600 | 26.10 | 180.53 | 648 | 27.00 | 187.74 | 657 | 29.34 | 220.85 |
| 21 | 761 | 29.51 | 226.48 | 791 | 28.78 | 224.65 | 811 | 27.41 | 191.91 |
| 22 | 681 | 31.23 | 242.24 | 737 | 31.71 | 248.52 | 715 | 30.96 | 240.71 |
| 23 | 623 | 26.87 | 201.48 | 641 | 26.51 | 198.01 | 636 | 27.24 | 200.68 |
| 24 | 484 | 29.92 | 278.06 | 507 | 30.23 | 286.48 | 516 | 27.81 | 250.36 |
| 25 | 512 | 30.12 | 255.78 | 537 | 26.97 | 211.44 | 574 | 28.70 | 218.27 |
| 26 | 686 | 33.98 | 316.98 | 737 | 33.26 | 311.15 | 706 | 31.70 | 291.37 |
| 27 | 706 | 33.32 | 256.59 | 720 | 34.18 | 266.29 | 725 | 34.21 | 263.54 |

| | | | | | | | | | |
|----|-----|-------|--------|-----|-------|--------|-----|-------|--------|
| 28 | 643 | 31.45 | 245.74 | 656 | 30.58 | 232.94 | 674 | 31.53 | 248.54 |
| 29 | 737 | 37.01 | 342.30 | 769 | 36.92 | 347.25 | 764 | 35.96 | 341.34 |
| 30 | 732 | 31.69 | 255.71 | 725 | 32.55 | 264.64 | 735 | 30.97 | 246.13 |
| 31 | 837 | 22.40 | 129.86 | 776 | 22.22 | 129.11 | 773 | 20.67 | 116.14 |
| 32 | 681 | 29.10 | 235.44 | 665 | 27.87 | 222.85 | 619 | 27.62 | 222.12 |
| 33 | 693 | 25.59 | 182.73 | 703 | 25.89 | 183.52 | 722 | 24.82 | 171.58 |
| 34 | 679 | 24.10 | 172.68 | 686 | 23.78 | 169.53 | 693 | 23.25 | 160.55 |
| 35 | 641 | 30.42 | 241.19 | 633 | 29.48 | 238.33 | 651 | 27.97 | 219.34 |
| 36 | 578 | 36.69 | 302.60 | 592 | 36.87 | 309.28 | 606 | 37.64 | 314.00 |
| 37 | 717 | 27.94 | 203.51 | 754 | 27.93 | 203.64 | 748 | 27.13 | 188.36 |
| 38 | 634 | 32.53 | 268.01 | 641 | 32.49 | 272.43 | 656 | 30.02 | 237.33 |
| 39 | 776 | 33.67 | 255.18 | 821 | 33.62 | 259.47 | 827 | 33.36 | 254.91 |
| 40 | 805 | 31.69 | 231.88 | 845 | 31.25 | 229.13 | 859 | 30.79 | 224.54 |
| 41 | 802 | 30.61 | 205.98 | 767 | 28.81 | 189.41 | 793 | 27.42 | 176.61 |
| 42 | 834 | 30.43 | 222.48 | 788 | 29.03 | 213.28 | 763 | 29.04 | 212.33 |
| 43 | 863 | 27.27 | 178.60 | 841 | 27.04 | 177.22 | 896 | 26.40 | 173.06 |
| 44 | 752 | 26.26 | 187.53 | 781 | 25.41 | 178.99 | 805 | 29.26 | 224.67 |
| 45 | 714 | 31.33 | 251.18 | 721 | 29.82 | 245.84 | 727 | 29.24 | 238.80 |
| 46 | 716 | 29.76 | 212.86 | 745 | 28.00 | 198.99 | 733 | 27.12 | 192.87 |
| 47 | 860 | 27.86 | 172.76 | 892 | 28.64 | 181.41 | 830 | 29.27 | 189.26 |
| 48 | 749 | 30.76 | 249.56 | 734 | 31.32 | 255.26 | 761 | 32.27 | 264.93 |
| 49 | 735 | 42.38 | 404.06 | 726 | 41.53 | 398.79 | 712 | 39.71 | 369.13 |
| 50 | 687 | 30.45 | 251.54 | 696 | 30.58 | 255.36 | 696 | 28.87 | 236.20 |

(5) Ground estimated AGB and relative height metrics

The relationships between ground estimated AGB and the relative height metrics from both sensors have been carefully analyzed. Their correlation increases as the spatial scale becomes coarser (Fig. S4).

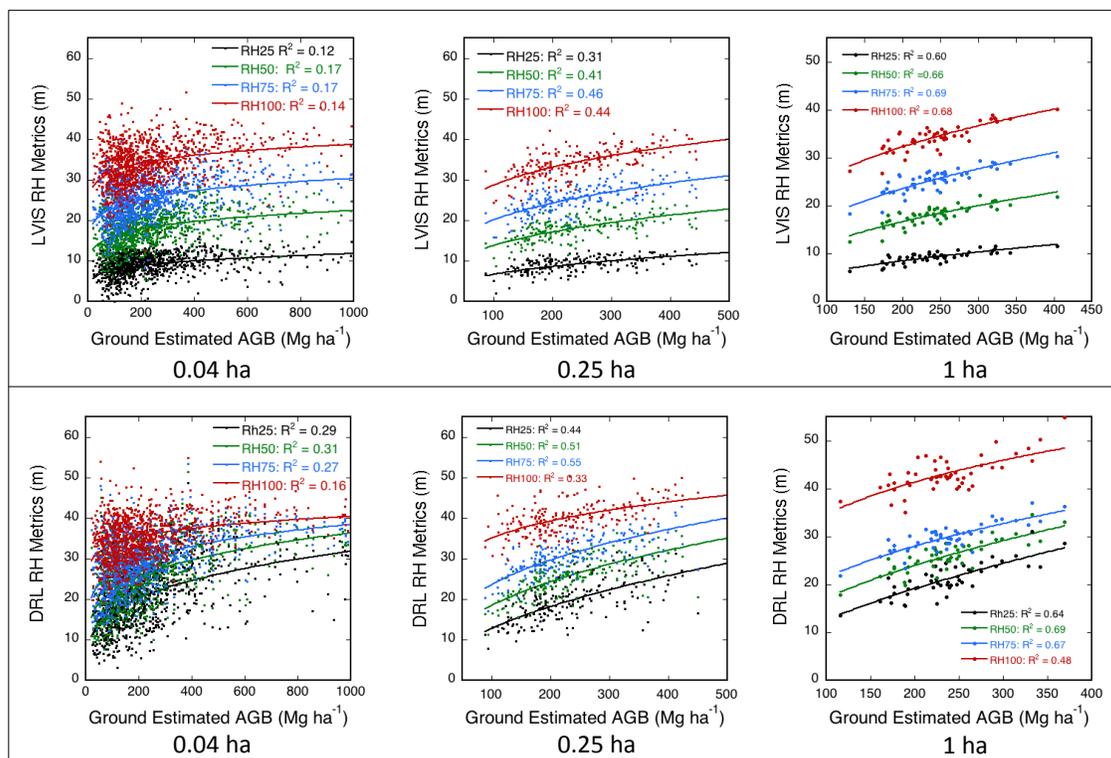


Figure S4 : Relationship between Ground Estimated AGB and RH metrics at three spatial scales (top : LVIS, bottom : DRL)

Table S3 : Coefficients of the Lidar derived AGB equation using five height metrics at 1ha.

$$AGB_{est} = a0 + a1RH25^{\alpha} + a2RH50^{\beta} + a3RH75^{\gamma} + a4MCH^{\delta} + a5RH100^{\epsilon}$$

| | a0 | a1 | a2 | a3 | a4 | a5 |
|-------------|-----------|-----------|-----------|-----------|-----------|-----------|
| LVIS | -53.91 | 3.82 | -1.03 | 0.46 | 0.05 | 0.02 |
| 100m | | | | | | |
| DRL | -23.8 | -1.94 | 4.5 | -1 | 0.08 | 0.05 |
| 100m | | | | | | |

| | α | β | γ | δ | ε |
|-------------|----------|----------|----------|----------|----------|
| LVIS | 1.08 | 1.31 | 1.63 | 2.14 | 2.2 |
| 100m | | | | | |
| DRL | 1.06 | 1.42 | 1.74 | 2.14 | 1.8 |
| 100m | | | | | |

(6) Ground-estimated AGB change

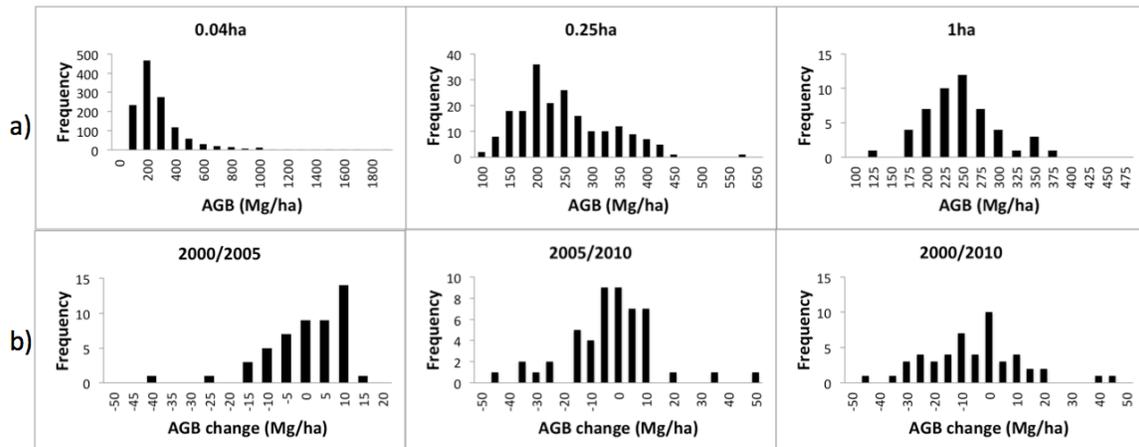


Figure S5 : a) Histograms of AGB distribution in the permanent plot at three spatial scales in 2010. AGB distribution is skewed to the left when using 0.04ha subplots. AGB distribution becomes normal when working with larger subplots, especially at 1ha. b) Histograms of AGB Change between 2000, 2005 and 2010 in the 50ha plot (1ha scale) . There are more extreme values (positive and negative) between 2005 and 2010, than between 2000 and 2005.

(7) Ground estimated AGB and MCH-derived AGB

Figure S6 shows the relationship between ground estimated AGB and Lidar estimated AGB, using MCH only (see Fig.5 in the main paper for the 5RH approach results). The coefficients of correlation are high at 1ha, but bias is higher than when using five relative height metrics in the model, especially as the spatial scale becomes finer.

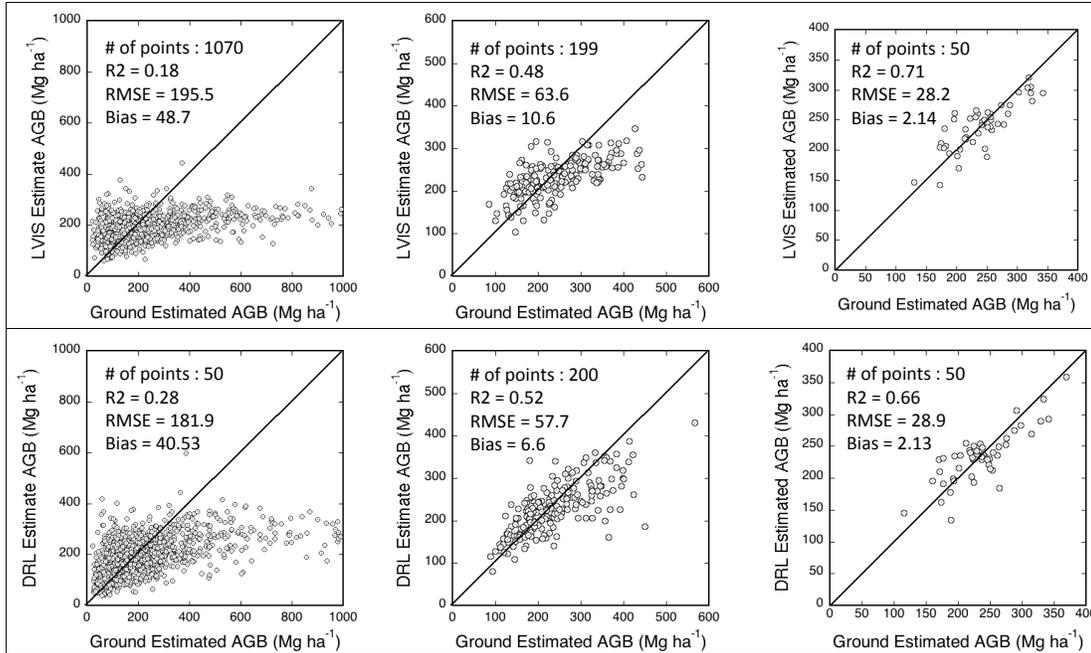


Figure S6 : Relationship between Ground estimated AGB and Lidar estimated AGB (top : LVIS, bottom : DRL).

(8) Spatial Scale

Figure S7 illustrates why using small plots for estimating AGB in tropical forests may result in an improper AGB estimation. Because tree crowns can reach over 20m in diameter, chances are that a tree crown will significantly overlap several adjacent 20m*20m subplots, thus contributing to the Lidar signal of more than one subplot. This yields to serious problems when attempting to correlate the Lidar signal and ground-based AGB estimations because the ground measurement of a tree (i.e., the physical location of the stem) only contributes to the AGB of a single subplot. This border effect declines as the subplot size increases to 50m*50m and 100m*100m subplots, although edge effects are still expected to be present. At 1ha, the contribution to canopy heights from trees rooted outside the plot boundary becomes small compared to those that do not transgress the plot boundaries.

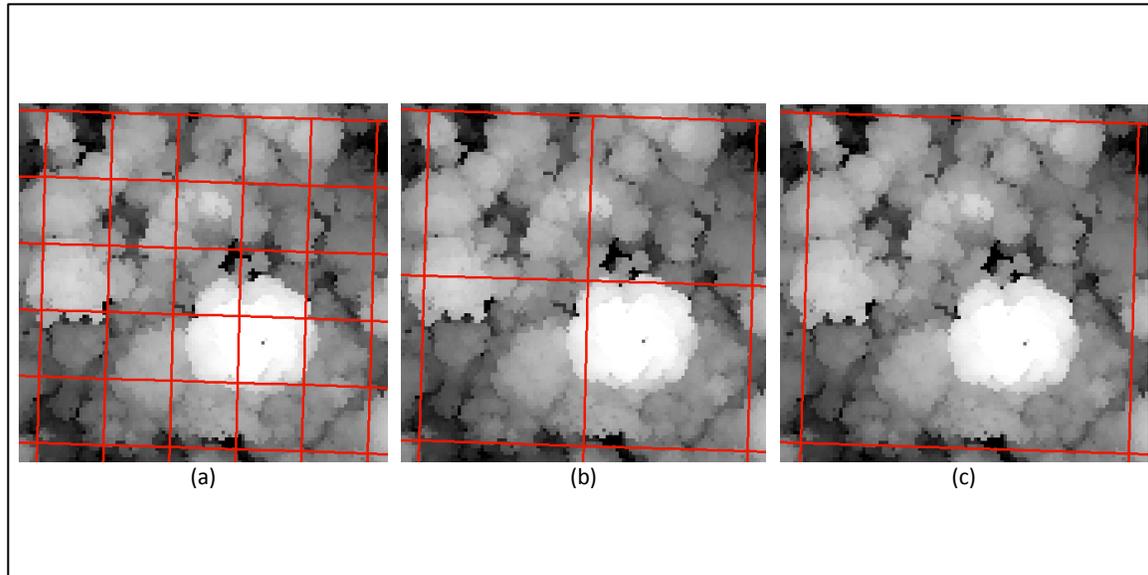


Figure S7 : Effects of plot size on DRL canopy height share. At 0.04ha (a), a big tree is predominant in two subplots and present in two others. At 0.25ha (b), the big tree is mainly present in one subplot, but other trees are split between subplots. At 1ha (c), the edge effect is still there but it becomes negligible compared to the number of trees that are fully contained in the subplot.

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