

# 1 Large eddy simulations of surface roughness parameter 2 sensitivity to canopy-structure characteristics

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## 10 11 **Abstract**

12 Surface roughness parameters, namely the roughness length and displacement height, are  
13 an integral input used to model surface fluxes. However, most models assume these  
14 parameters to be a fixed property of plant functional type and disregard the governing  
15 structural heterogeneity and dynamics. In this study, we use large-eddy simulations to  
16 explore, *in silico*, the effects of canopy structure characteristics on surface roughness  
17 parameters. We performed a virtual experiment to test the sensitivity of resolved surface  
18 roughness to four axes of canopy structure: (1) leaf area index, (2) the vertical profile of  
19 leaf density, (3) canopy height, and (4) canopy gap fraction. We found roughness  
20 parameters to be highly variable, but uncovered positive relationships between  
21 displacement height and maximum canopy height, aerodynamic canopy height and  
22 maximum canopy height and leaf area index, and eddy-penetration depth and gap  
23 fraction. We also found negative relationships between aerodynamic canopy height and  
24 gap fraction, and between eddy-penetration depth and maximum canopy height and leaf  
25 area index. We generalized our model results into a virtual 'Biometric' parameterization  
26 that relates roughness length and displacement height to canopy height, leaf area index  
27 and gap fraction. Using a decade of wind and canopy structure observations in a site in  
28 Michigan, we tested the effectiveness of our model-driven 'Biometric' parameterization  
29 approach in predicting the friction velocity over heterogeneous and disturbed canopies.

1 We compared the accuracy of these predictions with the friction-velocity predictions  
2 obtained from the common simple approximation related to canopy height, the values  
3 calculated with large eddy simulations of the explicit canopy structure as measured by  
4 airborne and ground-based lidar, two other parameterization approaches that utilize  
5 varying canopy-structure inputs, and the annual and decadal means of the surface  
6 roughness parameters at the site from meteorological observations. We found that the  
7 classical representation of constant roughness parameters (in space and time) as a fraction  
8 of canopy height performed relatively well. Nonetheless, of the approaches we tested,  
9 most of the empirical approaches that incorporate seasonal and inter-annual variation of  
10 roughness length and displacement height as a function of the dynamics of canopy  
11 structure produced more precise and less biased estimates for friction velocity than  
12 models with temporally invariable parameters.

## 13 **1 Introduction**

14 Our ability to accurately predict mass and energy fluxes from the land surface to the  
15 atmosphere at any time scale depends on the accuracy of the surface drag parameterization  
16 (Finnigan, 2000;Mahrt, 2010). Over forested environments, vertical mixing of canopy air with  
17 the free atmosphere above, which is the process responsible for the exchange of energy, water  
18 vapor, and CO<sub>2</sub> between the land surface and the atmosphere, is a function of the turbulent  
19 eddies created through interactions between vegetative structure (e.g., trees, tree-stems,  
20 leaves) and the wind (Thomas and Foken, 2007a). In many regional models, estimation of  
21 surface drag, and thus surface fluxes, is typically dependent upon parameterization of the  
22 friction velocity,  $u_*$ , based on Monin-Obukhov similarity theory (MOST) (Monin and  
23 Obukhov, 1954) using parameters that describe the effects of drag generated by the surface on  
24 the shape of the curve describing the vertical distribution of wind speed. These parameters are  
25 displacement height,  $d$ , and roughness length,  $z_0$ . Though they represent different physical  
26 properties of the surface effects on the velocity profile, we will refer to them throughout the  
27 manuscript using the combined term 'roughness parameters'. In many land surface, vegetation,  
28 ecosystem, and hydrology models, such as the Community Earth System Model (CESM)  
29 (Gent et al., 2011), Mapping Evapotranspiration with Internalized Calibration (METRIC)  
30 (Allen et al., 2007), and Surface Energy Balance Algorithm for Land (SEBAL) (Bastiaanssen  
31 et al., 1998), the surface sensible and latent heat fluxes are functions of the aerodynamic  
32 resistance for heat transfer,  $r_{ah}$ .  $r_{ah}$  is a function of the turbulence at the surface layer, defined

1 through the friction velocity,  $u_*$ . In models which cannot directly resolve  $u_*$ ,  $r_{ah}$  is  
2 parameterized as a function of  $d$  and  $z_0$ . In these models  $d$  and  $z_0$  may be derived from  
3 different canopy structure characteristics. By the simplest approach,  $d$  and  $z_0$  are linear  
4 functions of site-level canopy height ( $h$ ) – typically:  $d \approx 0.66h$  (Cowan, 1968) and  $z_0 \approx 0.10h$   
5 (Tanner and Pelton, 1960). The accuracy of these estimates may be limited, however, by the  
6 dynamic nature (space and time) of canopy structural characteristics. First, the canopy is a  
7 complex structure that is hard to describe using simple low-variable-number formulations.  
8 Second, estimates of the canopy structural characteristics are limited by the typical absence of  
9 data about the vertical distribution of leaf area (Massman and Weil, 1999; Shaw and Pereira,  
10 1982) and tree-top heights, and the difference between coarse model grid-cell resolution and  
11 the finer scale at which canopy structure characteristics vary and affect roughness and  
12 momentum and flux transfer.

13 One common approach to incorporate canopy structure in the parameterization of roughness  
14 length into models in a more realistic way utilizes satellite imagery products to estimate  
15 vegetation structure and relate it to canopy-roughness relationships. For example, the SEBAL  
16 model (Moran, 1990) utilizes a function based on the Normalized Difference Vegetation  
17 Index (NDVI) while the METRIC model employs Perrier Function (Perrier, 1982). These  
18 canopy-roughness relationships have been shown to improve evapotranspiration estimates  
19 (Santos et al., 2012), but are specific to sparse or short vegetative environments, such as  
20 agricultural systems, and are not typically recommended for forest environments  
21 (Bastiaanssen et al., 1998).

22 To incorporate the effects of canopy structure in denser and taller vegetative environments  
23 such as forests, empirical functions have been proposed using coarse canopy metrics such as  
24 canopy area index (the total, single-sided area of all canopy elements within a  $1 \times 1 \text{ m}^2$   
25 ground area) (Raupach, 1994), stand density (stems per area), or leaf area index ( $LAI$ , the total  
26 surface area of leaves found within a  $1 \times 1 \text{ m}^2$  vertical column of vegetation) (Nakai et al.,  
27 2008a). However, the data required to use these functions are typically not available at most  
28 sites and, with the exception of  $LAI$ , are not yet obtainable through large-scale satellite remote  
29 sensing. In many climate models, surface-layer grid cells are prescribed with biome-specific  
30 qualities, i.e., sets of parameters describing constant vegetation structure and flux-driving  
31 characteristics for all model cells containing a specific biome or plant functional type (PFT).  
32 For example, the Ecosystem Demography model version 2 (ED2, Medvigy et al., 2009)

1 provides twenty different vegetation functional types, seven of which are representative of  
2 forested environments, to describe all land surfaces across the globe. Each such vegetation  
3 functional type is characterized by fixed, canopy-height driven roughness parameters.  
4 Similarly, aerodynamic resistance to surface flux in the advanced hydrological model  
5 tRIBS+VEGGIE (Ivanov et al., 2008) is only driven by vegetation height, with is either  
6 prescribed, or set as a default per PFT.

7 Roughness parameters have been shown to scale with structural characteristics, such as the  
8 influence of area-index (vegetation area per ground area) terms on  $d$  and  $z_0$ , through numerical  
9 studies (Shaw and Pereira, 1982;Choudhury and Monteith, 1988) and wind-tunnel  
10 experiments (Raupach, 1994). Above-canopy meteorology data has shown estimates of  
11 roughness parameters to be highly variable both spatially and temporally (Maurer et al.,  
12 2013;Harman, 2012;Zhou et al., 2012). As evidence for canopy-roughness relationships has  
13 risen, various studies have attempted to generalize small-scale interactions between roughness  
14 parameters and canopy structure by deriving  $d$  and  $z_0$  from above-canopy meteorological  
15 measurements (Braam et al., 2012;Maurer et al., 2013;Raupach et al., 1996;Nakai et al.,  
16 2008a), remote-sensing (Schaudt and Dickinson, 2000;Weligepolage et al., 2012), numerical  
17 experiments (Grimmond and Oke, 1999;Wouters et al., 2012), and large-eddy simulations  
18 (LES) (Aumond et al., 2013;Bohrer et al., 2009;Bou-Zeid et al., 2007;Bou-Zeid et al., 2009).  
19 Although the understanding of these small-scale canopy-roughness interactions has grown,  
20 accounting for fine-scale canopy structure effects on roughness parameters in larger-scale  
21 climate models requires further development.

22 In this study, we use the Regional Atmospheric Modeling System (RAMS)-based Forest  
23 Large-Eddy Simulation (RAFLES) (Bohrer et al., 2008;Bohrer et al., 2009) to conduct a  
24 virtual experiment to estimate the sensitivity of surface roughness parameters to specific  
25 characteristics of fine-scale canopy structure. RAFLES incorporates a prescribed 3-D domain  
26 that includes the vegetation leaf density and stem diameters, and dynamically calculates the  
27 change to wind velocity as a function of leaf and stem surface drag in each voxel  
28 (Chatziefstratiou et al., 2014). The level of detail at which vegetation is represented in  
29 RAFLES makes it particularly suitable for conducting this series of virtual experiments that  
30 simulate the drag parameters over a simplistic set of virtual canopy structures that vary by  
31 structural component, including stand density and patch fraction, canopy height, leaf area  
32 index and vertical profile of leaf density. The approach of prescribing drag in LES to resolve

1 site-level roughness was previously tested and shown to provide higher accuracy than the  
 2 traditional roughness parameterization (Aumond et al., 2013). Finally, we use 10 years of  
 3 direct observations of canopy structure and roughness parameters (Maurer et al., 2013) to  
 4 estimate the sensitivity of modelled friction velocity to temporal variation in canopy structure  
 5 and its effects on roughness length. We compare these results with other approaches that may  
 6 be used to represent canopy structure when modelling roughness parameters.

## 7 **2 Materials and methods**

### 8 **2.1 Theory**

9 Monin-Obukhov similarity theory (MOST) describes the relationships between the mean  
 10 horizontal wind speed and the friction velocity in the inertial sublayer (Monin and Obukhov,  
 11 1954). Further details on the formulation of MOST used in this work are described in Maurer  
 12 et al., (2013). In brief, MOST describes the functional relationship between surface stress and  
 13 the parameters  $d$  and  $z_0$  and wind speed using a logarithmic function. The original MOST  
 14 formulation was expanded to include the effects of thermal instability and the flow regime in  
 15 the roughness sub-layer (RSL), as follows:

$$16 \frac{\kappa \bar{u}_z}{u_*} = \ln\left(\frac{z-d}{z_0}\right) - \psi_m\left(\frac{z-d}{L}\right) + \psi_m\left(\frac{z_0}{L}\right) + I\psi_u\left(\frac{z-d}{L}, \frac{z-d}{z_*-d}\right) \quad (1)$$

17 where  $\bar{u}_z$  is the mean horizontal wind speed at height  $z$ , above the ground. When the data is  
 18 derived from meteorological observations, an over-bar over a variable represents the 30-  
 19 minute mean of the 10 Hz time series of that variable. Given the mean eastward and  
 20 northward wind velocities,  $\bar{u}$  and  $\bar{v}$ ,  $\bar{u}_z$  is rotated toward the wind direction such that:

$$21 \bar{u}_z = \left(\bar{u}^2 + \bar{v}^2\right)^{1/2} \quad (2)$$

22 where  $\kappa$  is the von Kármán constant,  $\sim 0.4$ ,  $z_*$  is the upper limit of the RSL estimated as  $2h$   
 23 (Mölder et al., 1999; Raupach et al., 1996),  $h$  is the canopy height.  $I$  is an indicator function  
 24 defined as ( $I = 1$  for  $z \leq z_*$ ; or  $I = 0$  for  $z > z_*$ ).  $u_*$  is the friction velocity defined as:

$$25 u_* = \left(\overline{u'w'^2} + \overline{v'w'^2}\right)^{1/4} \quad (3)$$

1 where each prime term (e.g.,  $w'$ ) is the perturbation of the specific variable from its mean  
 2 (e.g.,  $w - \bar{w}$ ). The atmospheric-stability correction function,  $\psi_m(x)$ , was described by Paulson  
 3 (1970) for unstable atmospheric conditions ( $z/L < 0$ ) as:

$$4 \quad \psi_m(x) = 2 \ln \left[ \frac{1 + (1 - 16x)^{1/4}}{2} \right] + \ln \left[ \frac{1 + (1 - 16x)^{1/2}}{2} \right] - 2 \tan^{-1} \left[ (1 - 16x)^{1/4} \right] + \frac{\pi}{2} \quad (4)$$

5 where  $x$  is either  $(z - d)/L$  or  $z_0/L$ .

6 Current understanding of aerodynamic properties near forest canopies within the roughness  
 7 sub-layer (RSL) has led to empirical corrections to the MOST model (Harman and Finnigan,  
 8 2007; De Ridder, 2010; Cellier and Brunet, 1992; Garratt, 1980; Mölder et al., 1999; Physick and  
 9 Garratt, 1995; Raupach, 1992). These corrections allow us to utilize MOST with  
 10 meteorological observation within the RSL, which typically includes the height range where  
 11 eddy-covariance measurements of forest flux dynamics are conducted across the globe. The  
 12 RSL correction we used,  $\psi_u(x_1, x_2)$ , was described by De Ridder (2010) as:

$$13 \quad \psi_u(x_1, x_2) = (1 - 16x_1)^{-1/4} \left[ \left( 1 + \frac{\nu}{\mu \cdot x_2} \right) x_1 \right] \frac{1}{\gamma} \ln \left( 1 + \frac{\gamma}{\mu x_2} \right) \exp(-\mu x_2) \quad (5)$$

14 where  $x_1 = (z - d)/L$ ,  $x_2 = (z - d)/(z_* - d)$ , and  $\nu$ ,  $\mu$ , and  $\gamma$  are empirical constants  
 15 provided by De Ridder (2010) as 0.5, 2.59, and 1.5, respectively. The inclusion of the RSL  
 16 correction ( $\psi_u \neq 0$ ) occurs when the calculation is performed within the RSL ( $z \leq z_*$ ,  $I = 1$ ).  
 17 Flux data is typically observed within the RSL at one point in space, requiring the  
 18 implementation of the RSL correction. When boundary layer conditions are near neutral,  
 19  $(z - d)/L$  and  $z_0/L$  approach zero, and thus,  $\psi_m(x)$  becomes negligible (Eq. 4).

20 Contrary to the classic estimate of  $z_0$  (function of  $h$ ), Thom (1971) suggested a relationship  
 21 between  $z_0$  and  $(h - d)$ , as opposed to a relationship between  $z_0$  and  $h$  alone, where the ratio of  
 22  $z_0/(h - d)$  was defined as  $\lambda$ , a dimensionless, stand-specific parameter. This allows  $z_0$  to be  
 23 dependent on the spacing of the surface roughness elements and not only their height. For  
 24 example,  $(h - d)$  will theoretically be smaller for more densely packed surfaces, providing a  
 25 smoother surface and smaller roughness length. This relationship can be written as:

$$26 \quad z_0 = \lambda(h - d) \quad (6)$$

1 Nakai et al. (2008b) substituted the aerodynamic height,  $h_a$ , for the canopy height,  $h$ , into this  
2 relationship and rearranged the equation to read:

$$3 \quad h_a = d + \frac{z_0}{\lambda} \quad (7)$$

4 In simulation results, where the detailed 3-D wind field is known, we use Eq. 7 to calculate  $\lambda$   
5 for each simulation using  $h_a$ , which can be calculated from the vertical profile of horizontal  
6 wind speed and the empirically fitted  $d$  and  $z_0$ .

7 We investigated the eddy penetration depth ( $\delta_e$ ), which is the length scale describing the  
8 vertical distance from the top of the canopy that is influenced by turbulent mixing from  
9 above. It is defined as the distance between  $h_a$  and the height where the momentum flux value  
10 is 10% of its value at  $h_a$  (Nepf et al., 2007).

## 11 **2.2 Site description**

12 The data used to test the effectivity of our LES-driven, and other modeling approaches  
13 originates from a mixed, deciduous forest site at the University of Michigan Biological  
14 Station (UMBS) in northern, lower Michigan, USA (45° 33' 35" N, 84° 42' 48" W, elev. 236  
15 m above sea level). The forest is dominated (~30% of leaf area index) by early-successional  
16 bigtooth aspen (*Populus grandidentata*) and paper birch (*Betula papyrifera*), with a mean age  
17 of 85-90 years (Gough et al., 2013). The remaining leaf area is mostly represented by red oak  
18 (*Quercus rubra*), red maple (*Acer rubrum*) and white pine (*Pinus strobus*). Mean canopy  
19 height is roughly 20-25 m with an average stem density of  $\approx 750$  stems  $\text{ha}^{-1}$  (including only  
20 trees with DBH > 8 cm). Eddy covariance flux measurements have been ongoing at the site  
21 since 1999 and data is available through AmeriFlux (<http://ameriflux.lbl.gov/>), site code: US-  
22 UMB. Empirical allometric equations, fitted to measurements in this site (Garrity et al., 2012)  
23 are used to determine canopy height from a tree census and measurements of diameter at  
24 breast height (DBH). Full censuses were conducted in 2001 and 2010, and partial censuses of  
25 DBH for 993 are measured annually. Leaf area index is measured weekly using an optical  
26 sensor (LAI2000, Licor Biosciences, Lincoln, NE, USA). Additional details on the calculation  
27 of roughness length parameter from wind observations in the site and the determination of  
28 canopy structure are described in Maurer et al., (2013). Portable canopy lidar measurements  
29 (Hardiman et al., 2013) were used to determine the mean leaf area density profile that was  
30 used as the 'natural' leaf area density case. Airborne lidar measurements were conducted by

1 the National Center for Airborne Lidar Mapping (NCALM) in summer 2009. The lidar data  
2 and processing for our site are described in Garrity et al., (2012). This dataset was used to  
3 determine the mean and variation of canopy top height and gap fraction, and to prescribe the  
4 explicit canopy structure in the 'Realistic' LES test case (see section 2.4).

### 5 **2.3 Large eddy simulations**

6 We used wind fields and heat fluxes from RAFLES simulations results to calculate surface  
7 roughness parameters of simplified virtual forests. RAFLES (Bohrer et al., 2009) uses a 3-D  
8 heterogeneous canopy domain where leaf and stem areas are prescribed within each voxel.  
9 The leaf area density and the instantaneous wind speed within the voxel determine the drag  
10 force that is applied to wind flow through that grid cell within each time step. Common to the  
11 approach used in most LES, it assumes the leaf area is composed of flat surfaces oriented  
12 downstream and neglects higher-order effects of leaf and stem shapes and sub-grid-scale  
13 wake generation (shown to be a small effect, Shaw and Patton, 2003). It is combined with  
14 radiation attenuation (given the leaf densities in the grid cells above) to determine the sensible  
15 and latent heat fluxes emitted from each grid cell. The model uses the finite volume approach  
16 for discretization of the simulation domain. It resolves the effects of volume restriction due to  
17 the volume of the vegetation (stems, branches) by reducing the aperture areas available for  
18 flux exchange between each pair of neighboring grid cells and by reducing the volume that is  
19 available for flow within each grid cell according to the volume of the vegetation present  
20 (Chatziefstratiou et al., 2014). It resolves sub-grid-scale turbulence using the Deardorff (1978)  
21 scheme, and includes a parameterization for sub-grid-scale turbulence dissipation due to leaf  
22 drag (Shaw and Patton, 2003).

23 Simulations consisted of three hours of simulation time at a time step of 0.02 s. RAFLES uses  
24 a nested time stepping scheme with higher frequency calculations for turbulence and still  
25 higher frequency calculations for pressure perturbations. Eight pressure and four turbulence  
26 time steps were nested in one model time step. Output data snapshots of all grid cells in the  
27 simulation domain were recorded every 2 seconds. The initial 2.5 hours of simulation time  
28 were used as a 'spin-up' period to ensure satisfactory turbulent mixing and semi-stability of  
29 the vertical profiles of turbulence and potential temperature. The latter half hour of simulation  
30 time was used for analysis, consisting of 300 2-sec snapshots.



1 Synthetic virtual domains covered  $1.25 \times 1.25 \times 1.4 \text{ km}^3$  (length x width x height) at a  
2 horizontal grid spacing of  $5 \times 5 \text{ m}^2$ , which approximately corresponds to the mean size of  
3 individual tree-crowns. Vertical grid spacing was 3 m in the lower sub-domain, from the  
4 ground to 100 m above ground level. Above that region, vertical grid spacing was gradually  
5 increased by 12% per each subsequent horizontal layer up to a maximal grid spacing of 30 m.  
6 The vertical grid spacing then remained constant above that height up to the model top at 1.4  
7 km. The model has periodic boundary conditions at the lateral boundaries, no-slip boundary  
8 conditions at the bottom boundary and a no-flux top boundary with Rayleigh friction to  
9 dampen vertical perturbations at the top 6 model layers (180 m). Initial conditions were  
10 horizontally homogeneous and followed a prescribed vertical profile for potential  
11 temperature, humidity, and wind speed. The prescribed initial vertical profile of the potential  
12 temperature described a well-mixed atmospheric boundary layer and was constant from 50 m  
13 to the height of the capping inversion, and increased with height above that level. Latent and  
14 sensible heat fluxes were prescribed based on observed mean noontime observations for  
15 August 2011 above the canopy at US-UMB. For each column of the horizontal simulation  
16 domain, the sum of the fluxes and Bowen ratio were distributed around the prescribed mean  
17 as an empirical function of *LAI*. Fluxes were further distributed vertically following a leaf-  
18 area dependent empirical exponential profile. More details on the numerical setup of the  
19 model and the approach for flux forcing are provided in Bohrer et al. (2009).

#### 20 **2.4 Virtual experiment setup: Sensitivity analysis to quantify the** 21 **effects of specific canopy-structure characteristics on roughness** 22 **parameters**

23 Forest canopies are a complex array of 3-D structures. Many structural characteristics, such as  
24 tree height, *LAI*, vertical leaf area density (*LAD*) profile, and gap fraction, among others,  
25 affect the airflow inside and above the canopy and, consequently, affect the resulting  
26 roughness parameters and aerodynamic properties of the surface that describe such canopy  
27 structure. Using synthetic cases representing different aspects of canopy structure, we  
28 conducted a virtual experiment to test the sensitivity of roughness parameters to four axes of  
29 canopy structure: (1) mean site-level *LAI*, ranging from observed leaf-off conditions ( $LAI =$   
30  $1.0 \text{ m}^2 \text{ m}^{-2}$ ) to typical, mid-growing season leaf-on conditions ( $LAI > 1.0 \text{ m}^2 \text{ m}^{-2}$ ); (2) *LAD*  
31 ( $\text{m}^2\text{m}^{-3}$ ) profile, defined through the vertical bias of the vertical leaf density distribution (See  
32 *Appendix Figure 1*); (3) canopy height ranging from 9 to 27 m; and (4) canopy patch-level

1 continuity (gap fraction) ranging from 0 to 50% (see *Appendix Figure 2*). Based on the  
 2 available computing resources, we selected twenty combinations of the structural  
 3 characteristics listed above. A list of all simulation cases and the canopy-structure  
 4 characteristics is presented in Table 1.

5 In the gap fraction cases, canopy gaps were randomly created across the domain ranging from  
 6 a single-pixel (25 m<sup>2</sup>, tree-crown scale) to multi-pixel blocks (tens to hundreds m<sup>2</sup>). A gap  
 7 was described by shorter vegetation ( $h = 9$  m) and a non-gap (closed canopy) was described  
 8 by taller vegetation ( $h = 27$  m). It should be noted that we introduced gaps in our horizontally  
 9 homogenous canopy using holes of varying sizes and shapes, which was done to minimize the  
 10 complexity of the prescribed “heterogeneity” treatment (*Appendix Figure 2*). The resulting  
 11 gap-size distribution was arbitrary and may not have been well-representative of an actual,  
 12 heterogeneous canopy environment with tree-fall gaps.

## 13 **2.5 Empirical determination of roughness parameters from simulations** 14 **results**

15 To calculate flux and wind statistics, we first calculated the mean value of each model  
 16 variable at each vertical model level over the entire horizontal domain at that height level, and  
 17 over all 300 time snapshots. We then rotated the horizontal wind coordinates of each vertical  
 18 level toward the downstream direction, such that the resulting mean rotated downstream  
 19 velocity is:

$$20 \quad \langle u_r \rangle_{xyt} = \left( \langle u \rangle_{xyt}^2 + \langle v \rangle_{xyt}^2 \right)^{1/2} \quad (8)$$

21 where  $\langle \rangle_{xyt}$  marks an average of the simulation results over all voxels in the x (eastward) y  
 22 (northward) and t (temporal, 300 snapshots) dimensions. Although the wind forcing aloft is  
 23 eastward, a rotation develops following the Ekman spiral and is further amplified by random  
 24 x-y asymmetries in the simulation domain. The rotation for the horizontal coordinate system  
 25 of each horizontal layer is necessary to maintain a consistent downstream axis required for  
 26 data analysis. After this rotation, we calculated the instantaneous perturbation of the velocity  
 27 components from the  $\langle \rangle_{xyt}$  average for each voxel in space and time along each horizontal  
 28 layer, such that:

$$29 \quad u_r' = u_r - \langle u_r \rangle_{xyt} \quad (9)$$

1 where the prime indicates an instantaneous perturbation from the mean value, in this example  
 2 of the  $u_r$  (downstream) velocity component. Similar formulation applies to the vertical ( $w$ )  
 3 and cross-stream ( $v_r$ ) velocity components. Momentum flux at the down-stream direction was  
 4 calculated as:

$$5 \quad \langle u_r' w' \rangle_{xyt} = \left\langle \left( u_r - \langle u_r \rangle_{xyt} \right) \left( w - \langle w \rangle_{xyt} \right) \right\rangle_{xyt} \quad (10)$$

6 See Bohrer et al. (2009) for additional details on the calculation of wind statistics and  
 7 momentum fluxes from RAFLES output.

8 We determined the effective aerodynamic canopy height,  $h_a$ , by identifying the height of the  
 9 inflection point in the vertical wind-speed profile. This height marks the transition between  
 10 the sub-canopy and above-canopy flow regimes (Thomas and Foken, 2007b). To find this  
 11 point, we compiled a domain-averaged wind-speed profile using Eq. 8. Then, we determined  
 12  $h_a$  as the location where the second derivative of the horizontal wind profile crosses zero. We  
 13 approximated this location within the vertical grid resolution using linear interpolation. We  
 14 calculated the characteristic domain-averaged  $u_*$  for each simulation case by calculating the  
 15 horizontal-temporal average  $u_*$  for each for each horizontal plane of grid cells within the 3-D  
 16 virtual domain and further averaging these vertically over the range from  $3.5-4.5h$  ( $u_*$  values  
 17 are nearly invariable with height in that range). Obukhov length was calculated for each  
 18 horizontal plane of grid cells within the 3-D virtual domain as a function of the characteristic  
 19  $u_*$ , surface heat flux (prescribed) and the mean potential virtual temperature at each  
 20 horizontal plane of grid cells. Next, the vertical profile of horizontal mean wind speed from  
 21 all grid layers above  $1.5h_a$  and below  $4.5h$  (95 m) above ground was fitted to Eq. 1 to  
 22 determine  $d$  and  $z_0$  using the characteristic friction velocity and the Obukhov length. The  
 23 empirical fit was calculated using MATLAB's (version R2013b, The MathWorks, Inc.,  
 24 Natick, MA, USA) nonlinear, least-squares fit function:  $fit()$ . We constrained the solution for  
 25 the surface roughness parameters to a physically meaningful range by constraining  $d$  to be  
 26 between 0 and  $h_a$  of the simulated forest and  $z_0$  to be larger than 0.

## 1 3 Results

### 2 3.1 Virtual experiment to explore canopy-roughness relationships

3 We found that  $d$  was significantly affected by maximum canopy height ( $h_{\max}$ ) (3-way  
4 ANOVA, Table 2). We also found that  $h_a$  and  $\delta_e$  were significantly affected by  $h_{\max}$ ,  $LAI$ , and  
5 gap fraction ( $GF$ ) (Table 2).  $z_0$  was not found to be significantly affected by any single aspect  
6 of canopy structure investigated within this study. As suggested by Thom (1971) and Nakai et  
7 al. (2008b) we checked the relationship between  $z_0$  and  $(h_a - d)$  and found a significant  
8 relationship ( $r^2 = 0.72$ ,  $P < 0.001$ ). We found a positive relationship between  $d$  and  $h_{\max}$  (fit  
9 forced through [0,0], Figure 1).

$$10 \quad d = 0.69h_{\max} \quad (11)$$

11 Surprisingly, canopy gaps showed little effect on  $d$ . A higher correlation existed between  $d$   
12 and  $h_{\max}$  ( $r^2 = 0.78$ ) than between  $d$  and mean canopy height ( $r^2 = 0.48$ ) across the gap  
13 fraction sensitivity analysis. There was little change to  $d$  with increasing gap fraction, except  
14 for the scenario with 50% gap fraction in the leaf-on simulations, which was significantly  
15 lower. Therefore, the relationship with  $h_{\max}$  (which was constant as the number of gaps  
16 increased) was selected instead of mean canopy height (which decreased as the number of  
17 gaps increased). Seasonality (leaf-on vs. leaf-off) also showed surprisingly small differences  
18 in  $d$  as height was varied, which had previously been observed at US-UMB (Maurer et al.,  
19 2013).

20 We found positive  $h_a$ - $h_{\max}$  and  $h_a$ - $LAI$  relationships and a negative  $h_a$ -gap fraction ( $GF$ )  
21 relationship (Figure 2). We note that a positive  $h_a$ - $h$  relationship was previously observed at  
22 US-UMB using 12 years of meteorological data and tree-growth censuses (Maurer et al.,  
23 2013). By utilizing the suite of RAFLES simulations we empirically calculated a single  
24 canopy- $h_a$  relationship as:

$$25 \quad h_a = h_{\max} + aLAI + bGF + c \quad (12)$$

26 where  $a = 0.06$  m,  $b = (-)0.69$  m, and  $c = (-)0.11$  m.

27 We found a negative  $\delta_e$ - $LAI$  relationship and positive  $\delta_e$ - $h_{\max}$  and  $\delta_e$ - $GF$  relationships (Figure  
28 3). As expected, we found  $\delta_e$  to be consistently higher during leaf-off periods compared to  
29 leaf-on periods at corresponding heights and gap fractions as wind was better able to penetrate

1 the sub-canopy. Increased  $LAI$  intensified the effect of gap fraction on  $\delta_e$  as the slope of the  
2 leaf-on fit-line was larger than that of leaf-off periods.

3 Relationships were empirically determined using roughness parameters from each RAFLES  
4 simulation, except for those with ‘unnatural’ vertical LAD profiles (i.e., the ‘Upper’,  
5 ‘Middle’, and ‘Lower’ LAD cases) as no patterns were observed between any roughness  
6 parameters and vertical LAD profile. Maximum canopy height was used instead of mean  
7 canopy height because maximum canopy height was more tightly correlated with each  
8 roughness parameter than mean canopy height. The resulting roughness parameters for each  
9 simulation are listed in Table 1.

10 We calculated a ‘Biometric’  $h_a$  using the relationship we found in the virtual experiment  
11 between  $h_a$  and  $LAI$ , gap fraction and  $h_{max}$  (Eq. 12). To simulate the conditions in our site at  
12 US-UMB, we assumed a gap fraction of 5%, which was found by calculating the percent area  
13 within the NCALM lidar scan domain with vegetation height less than 2 m. We used the peak  
14 growing season site-level mean  $LAI$  of 4.2 as measured from 2000-2011 (Maurer et al., 2013).  
15 A ‘Biometric’  $d$  was then calculated using Eq. 10. Finally, a ‘Biometric’  $z_0$  was calculated as:

$$16 \quad z_0 = \lambda(h_a - d) \quad (13)$$

17 where  $\lambda = 0.34$  was determined from Eq. 7 given the set of  $h_a$ ,  $d$  and  $z_0$  values from our  
18 simulations through the virtual sensitivity experiment.

### 19 **3.2 Testing empirical approaches that link roughness parameters to biometric** 20 **measurements**

21 The ‘Biometric’ approach, derived from our simulation results, provides relationships between  
22 easily measurable characteristics of the canopy (i.e.,  $LAI$  and maximum canopy height) and  $d$   
23 and  $z_0$ . In order to evaluate the potential improvement to estimates of  $u_*$  using this approach,  
24 we compared the accuracy and precision of modeled  $u_*$  values using the ‘Biometric’ approach  
25 with those of 5 alternative approaches. We evaluate the resulting friction velocities predicted  
26 by each of these six (‘Biometric’ and 5 alternatives) structure-driven parameterization  
27 approaches using 30-min observed values of  $u_*$ , canopy height and  $LAI$  over multiple years  
28 at US-UMB (2000-2011, at 34 m a.g.l). The 5 alternative approaches employed are:

29 (1) ‘Classical’ – fixed  $d = 0.66h$  and  $z_0 = 0.10h$ , where we use  $h = 22$  m;

1 (2) 'Explicit-LES' – fixed  $d = 0.67h$  and  $z_0 = 0.094h$  as determined from the simulation results  
2 of the 'realistic' LES case;

3 (3) 'Yearly Observed' – a purely empirical approach, using the values of  $d$  and  $z_0$  calculated  
4 from meteorological observations during each growing season at US-UMB from 2000-  
5 2011 (Maurer et al., 2013). In this approach, the values of  $d$  and  $z_0$  vary each year  
6 according to observations.  $d$  and  $z_0$  were calculated by fitting Eq. 1 to a seasonal set of  
7 half-hourly mean observations of wind speed and friction velocity at twice the canopy  
8 height (46 m a.g.l.) and only during neutral to slightly unstable atmospheric conditions  
9 during daytime. We also tested applicability of shorter-term observations of  $d$  and  $z_0$  to  
10 long-term predictions of friction velocity. This test was motivated by the fact that there  
11 are only few sites around the world with more than a decade of data, while short  
12 observation campaigns are more common. We used the observed  $d$  and  $z_0$  from each year  
13 to simulate the entire decadal time series of friction velocity. This resulted in 12 different  
14 'Yearly' models. Anecdotally, the most accurate model was associate with observed  $d$  and  
15  $z_0$  from 2008, and the least accurate model with the yearly values from 2005.

16 Numerous past studies have attempted to derive relationships between roughness parameters  
17 and other canopy-structure statistics. We chose two in this study:

18 (4) Raupach (1994) calculated  $d$  and  $z_0$  as functions of canopy area index ( $\Lambda$ ), drag coefficient  
19 ( $c_d$ ), and canopy height ( $h$ ):

$$20 \quad d = \left[ 1 - \frac{1 - \exp(-\sqrt{2c_d\Lambda})}{\sqrt{2c_d\Lambda}} \right] h \quad (14)$$

21 and

$$22 \quad z_0 = \left[ \left( 1 - \frac{d}{h} \right) \exp\left( -\frac{\kappa \bar{u}}{u_*} - \eta_h \right) \right] h \quad (15)$$

23 where  $c_d = 7.5$ ,  $\eta_h = 0.193$ , and  $\Lambda = 2nbh/A$ , where  $n$  is the number of stems in a sample  
24 plot,  $b$  is the mean diameter at breast height,  $h$  is the mean tree height, and  $A$  is the total  
25 ground area within the canopy sampling area. Full plot censuses provided the data to  
26 calculate  $\Lambda$ . These were conducted in 2001 and 2010, and  $\Lambda$  values where linearly  
27 interpolated for the years between the censuses and extrapolated to 2011;

28 (5) Nakai et al. (2008a) calculated  $d$  and  $z_0$  as functions of stand density ( $\rho_s$ ),  $LAI$ , and  $h$ :

$$d = \left[ 1 - \left( \frac{1 - \exp(-\alpha\rho_s)}{\alpha\rho_s} \right) \left( \frac{1 - \exp(-\beta LAI)}{\beta LAI} \right) \right] h \quad (16)$$

and

$$z_0 = 0.264 \left( 1 - \frac{d}{h} \right) h \quad (17)$$

where  $\alpha$  and  $\beta$  are  $7.24 \times 10^{-4}$  ha stems<sup>-1</sup> and 0.273, respectively, and we used the US-UMB mean stand density of 750 stems ha<sup>-1</sup>.

The values of  $d$  and  $z_0$  as determined by each of the parameterization approaches are listed in Table 3. The range for yearly observed mean  $d$  values was 18.3-26.0 m and for  $z_0$  0.99-1.99 m. The 'Classical' approximation based on  $h$  resulted in a significantly lower  $d = 14.0$  m (outside the range of the inter-annual variability over 12 years), and a slightly above-range  $z_0 = 2.10$  m. The 'Explicit-LES' resulted in a very similar  $d$  to the 'Classical' approach. The 'Biometric' approach predicted high but within-range  $d$  values (24.0-25.0 m) but extreme  $z_0$  values (3.64-3.82 m). There was nearly no overlap between the values of  $z_0$  from each of the approaches, indicating poor agreement between approaches for this parameter.

### 3.3 Improvements to estimates of friction velocity using canopy-structure-roughness relationships

Modeled  $u_*$  from all six approaches was regressed against observed  $u_*$ . The slope and intercept of the fit-line (estimates of accuracy), coefficient of determination ( $r^2$ ), and root mean square error (estimates of precision) are reported in Table 3. Surprisingly, all parameterization approaches produced similar results, with coefficient of determinations between 0.56 and 0.61, near zero, but significantly negative intercepts between (-)0.052 and (-)0.072 (significant margin  $\pm 0.004$ ). The most significant difference between the approaches was in their bias. All approaches (except the 'Yearly Observed' 2008 which was the only one that was not significantly biased) produced a significant positive bias, but the bias varied from near zero to 43% (slope of observed vs. modeled fit-line between 1.01 and 1.431, significant margin  $\pm 0.01$ ). The results of all parameterization approaches are listed in Table 3. We found that the precision of the results obtained by using each of the 12 'Yearly Observed' models over the entire 12-years period to be higher than the combined results of using the observation for each specific year during that year only. The bias of the prediction obtained with the

1 observed  $d$  and  $z_0$ , applied to the entire 12-year period varied from no significant bias (using  
2 the 2008 parameters) to 1.38 (with the 2005 parameters). The combined (each year with its  
3 own parameters) produced an intermediate bias for the friction velocity estimates.

4 The 'Yearly Observed' method is dependent on long term observations of wind, temperature,  
5 heat flux and friction velocity, which are rarely available in forest sites. The other methods we  
6 tested do not require directly observed roughness parameters. Of these methods, the 'Raupach  
7 94' approach had the highest precision and lowest bias (slope = 1.24,  $r^2 = 0.604$ ), the 'Explicit  
8 LES approach ranked second and our 'Biometric' approach ranked third, although it  
9 performed similarly to the very simple 'Classical' approach. The 'Nakai 08' approach proved  
10 to be the least compatible with our site.

## 11 **4 Discussion**

### 12 **4.1 Response of roughness parameters to canopy structure change**

13 To date, despite a strong need by the modeling community, there is no single consensus  
14 approach that relates roughness length and displacement height to observable properties of  
15 canopy structure, such as LAI, height, leaf density and gap fraction. Furthermore,  
16 observations in our field site (Maurer et al 2013) and by others (Nakai et al., 2008a) have  
17 shown that the roughness parameters in forests are not easily constrained by leaf area or  
18 canopy height. Our underlying assumption in setting up this model-based experiment was that  
19 the lack of clear empirical relationship between roughness parameter and canopy structure  
20 was due to the complexity of canopy structure. We assumed that different characteristics of  
21 the canopy drive different effects on roughness length and displacement height. In real  
22 forests, many of the structural characteristics vary in time in different ways, resulting in  
23 interacting and sometimes conflicting effects on roughness length and displacement height.  
24 We set up a numerical experiment that was designed to separate the effects of different  
25 observable characteristics of canopy structure. We also hypothesized that, to some degree, the  
26 difficulty in identifying a clear effect of canopy structure on each of the roughness parameters  
27 is because roughness length and displacement height values may trade-off, such that similar  
28 solutions can be fitted either with low  $d$  and high  $z_0$ , or *vice versa* (Nakai et al., 2008a; Nakai  
29 et al., 2008b; Maurer et al., 2013).

30 By testing the independent effects of different characteristics of canopy structure through a set  
31 of controlled virtual experiments, we indeed found that different roughness parameters where



1 sensitive to different structural characteristics. The aerodynamic canopy height ( $h_a$ ) and eddy  
2 penetration depth ( $\delta_e$ ) were both sensitive to leaf area, canopy height and gap fraction (figure  
3 2,3). In contrast,  $d$  was only significantly sensitive to canopy height, while  $z_0$  did not show  
4 any significant relationships with any single canopy structure characteristic.

5 We found positive  $d$ - $h_{\max}$  and  $h_a$ - $h_{\max}$  relationships independent of  $LAI$ . A strong correlation  
6 had previously been reported between  $h_a$  and  $h$  (Nakai et al., 2008b;Bohrer et al.,  
7 2009;Maurer et al., 2013;Thomas and Foken, 2007b). As canopy height was the only canopy  
8 characteristic that varied among the 'canopy height variation' simulations (Table 1.c.), it is  
9 reasonable to assume that  $\delta_e$  would be relatively constant, regardless of canopy height.  
10 However, as canopy height increased within our virtual domain, the constant mean site-level  
11  $LAI$  was stretched further in the vertical direction. Therefore, the mean leaf density in the  
12 upper canopy was smaller for taller canopies resulting in an increased  $\delta_e$  with canopy height  
13 (Figure 3b). In spite of increased  $\delta_e$ , we also observed a positive  $d$ - $h_{\max}$  relationship.  
14 Indicating that the increased  $\delta_e$  only partially compensated for the increase in canopy height,  
15 allowing for  $d$  to increase linearly with canopy height, but with a slope smaller than 1.

16 We found a linear relationship between  $h_a$  and gap fraction. Eddy-penetration depth scaled  
17 with gap fraction as well. It was consistently larger during leaf-off periods compared to leaf-  
18 on periods, and the presence of higher  $LAI$  during the leaf-on periods resulted in a steeper  
19 linear slope of the relationship between  $\delta_e$  and gap fraction (Figure 3c). Intuitively, increased  
20 gap fraction should lead to increased  $\delta_e$ , as more canopy openings allow eddies to penetrate  
21 deeper into the canopy. These findings are not surprising, as Shaw et al. (1988) found deeper  
22  $\delta_e$  at lower  $LAI$ . For example, we found that increased gap fraction corresponded to increased  
23 momentum flux, turbulence, and horizontal wind speed inside the canopy (below  $1h$ ) (Figures  
24 5, 6). This was likely due to the extension of turbulent eddy penetration deep into canopy  
25 gaps, indicated by elevated standard deviation of the vertical velocity,  $\sigma_w$  (a component of the  
26 turbulence kinetic energy) in canopy gaps (Figure 6a). Such locations of increased turbulent  
27 eddy penetration are less likely to occur in horizontally homogenous canopies (Figure 6b).  
28 However, the lack of any relationships between roughness length and gap fraction at all levels  
29 below 50% gap (Table 1) was surprising, as Bohrer et al., (2009) found increases to  $d$ ,  $z_0$ , and  
30  $h_a$  in patchier canopies (more gaps) during leaf-on conditions. The major difference between  
31 these two studies was that the scale of the gaps prescribed here – corresponding with 1-2  
32 crown sizes – was typically smaller than those in the Bohrer et al., (2009) experiments.

1 We found no consistent correlations between roughness parameters and the mode of the  
2 vertical LAD profile, as the variability in roughness parameters over the range of LAD  
3 scenarios was extremely high (Table 1). Although the shape of the vertical profile of wind  
4 speed is apparently different between the 'Lower' and the 'Upper' LAD profiles (Figure 7)  
5 there was no consistent canopy-wind or canopy-turbulence relationships that could be  
6 predicted by the bias of the vertical LAD curve (Figure 7). LAD profiles may change in  
7 complex ways across the landscape and over many time scales (seasons, years, decades) due  
8 to disturbance or senescence. As our virtual experiment has shown, the effects of the vertical  
9 LAD profile are inconsistent with a simple representation of the vertical distribution of LAD  
10 using its vertical bias as a single descriptive characteristic. Our results indicate that site-level  
11 mean  $LAI$  and canopy height are easier to obtain and, in general, provide more reliable  
12 characteristics of canopy structure than the vertical profile of LAD.

13 Our simulations did not detect a continuous increase to  $d$  or  $z_0$  with  $LAI$ , which was  
14 inconsistent with several previous wind tunnel or model studies (Choudhury and Monteith,  
15 1988; Grimmond and Oke, 1999; Raupach, 1994; Shaw and Pereira, 1982). We also did not  
16 find significant relationships with any single property of canopy structure, except between  
17 displacement height and canopy height. To a limited degree, this was the result of tradeoffs  
18 between the two, as indicated by the fact that  $h_a$ , which combines  $d$  and  $z_0$  through the slope  
19 of their tradeoff curve,  $\lambda$ , was better constrained than  $d$  or  $z_0$  alone. However, this tradeoff  
20 cannot fully explain the lack of relationship, as we did not find a significant and consistent  
21 relationship between  $z_0$  and different canopy structural characteristics even when we assumed  
22 a fixed displacement height and fitted only for  $z_0$  (results not shown). Combined, our results  
23 indicate that both of our underlying hypotheses were at least partially false, and neither the  
24 structural complexity of the canopy, nor the tradeoffs between  $z_0$  and  $d$  can fully explain the  
25 lack of clear relationship between canopy structure and  $d$  and  $z_0$ .

26 The lack of canopy structure effects on  $z_0$  within the virtual sensitivity experiment, and in  
27 particular, the lack of consistent seasonal differences between leaf-on and leaf-off periods,  
28 may suggest that leaf area is not the primary driver of  $z_0$ . To further understand the drivers of  
29  $z_0$ , we calculated the sensitivity of  $z_0$  to changes in wind speed at a measurement height  $z$   
30 above the canopy,  $\delta_{z_0 u}$ . This can be done by solving Eq. 1 for  $z_0$  assuming neutral conditions,  
31 and calculating the sensitivity as the partial derivative of  $z_0$  with respect to  $\bar{u}_z$ :

$$\delta_{z_0 u} = \frac{\partial z_0}{\partial \bar{u}_z} = \frac{-\kappa(z-d)}{u_*} \exp\left(\frac{-\kappa \bar{u}_z}{u_*}\right) \quad (17)$$

2 We determine that at low to intermediate mean wind speeds (below 3 m/s),  $z_0$  is extremely  
 3 sensitive to variation in  $\bar{u}$ , with the derivative being between 5 and 30 (Figure 8). This  
 4 indicates that, for an observed variation of 0.1 m/s measured at twice the canopy height the  
 5 resulting  $z_0$  will change by 0.5-3 m, which is a full range of the expected  $z_0$  values for a 20 m  
 6 tall canopy. At our site in Michigan, 3 m/s was approximately the median wind speed and was  
 7 therefore selected to drive the simulations. In reality, variations in half-hourly mean wind  
 8 speed at the order of 0.1 m/s can be a result of local variations in the flow field due to  
 9 topography, or measurement errors due to instrument placement and calibration. In both reality  
 10 and LES, such variations in wind speed at a given measurement point could also be the result  
 11 of effects of local modification to the flow field due to specific heterogeneous canopy-surface  
 12 structures (which were determined to extend up to  $5h$ , Raupach and Thom, 1981;Bohrer et al.,  
 13 2009), and could also be driven by random large eddies that may affect the 30 minute average  
 14 at a specific half hour. We hypothesize that this high sensitivity of  $z_0$  may be inhibiting the  
 15 attempts to empirically estimate its relationships with the canopy structural characteristic.

## 16 **4.2 Integrating canopy-structure characteristics into models**

17 Typically, surface roughness parameterization is used in models to directly or indirectly  
 18 predict the friction velocity, which is further used in the surface flux calculations. To test the  
 19 performance of different parameterization approaches, we used data from 12 years of wind,  
 20 friction velocity, Obukhov length, and canopy structure observations in a forest site in  
 21 Michigan. We compared six approaches that differ in whether they do (or do not) incorporate  
 22 temporal variation to canopy structure, and in the source of data they require to determine  $z_0$   
 23 and  $d$ . Surprisingly, but optimistically for the purpose of accurate modeling, all the surface  
 24 roughness parameterization approaches we tested resulted in relatively high precision ( $r^2 =$   
 25 0.58-0.61) in predicting the half-hourly friction velocity over 12 years. This is surprising  
 26 because each of the approaches used a different set of values for  $z_0$  and  $d$ , which in some  
 27 cases, were very far from each other. For example The 'Biometric' and the 'Classical' approach  
 28 performed rather similarly, but the 'Biometric' approach  $z_0$  values were about 80% larger than  
 29 the 'Classical'. To understand this discrepancy, we calculated the sensitivity of the friction  
 30 velocity to variation in  $z_0$ ,  $\delta_{u^*z_0}$ .

$$1 \quad \delta_{u^*z_0} = \frac{\partial u^*}{\partial z_0} = \frac{\bar{\kappa} u^*}{z_0} \left[ \ln \left( \frac{(z-d)}{z_0} \right) \right]^2 \quad (18)$$

2 For a case similar to the one we simulated, with a canopy at 22 m and mean wind speed of 3  
3 m/s, we found that the friction velocity is not sensitive to changes in roughness length when  
4 roughness length is higher than 0.6 m (Figure 8). As a general approximation (following the  
5 'Classical' approach), for a forest canopy higher than 10 m, roughness length is expected to be  
6 larger than  $0.1h = 1$  m. Therefore, while the value of the roughness length parameter is highly  
7 sensitive to changes in the half-hourly mean wind speed (Equation 17, Figure 8, Table 1), the  
8 resulting friction velocity may not be greatly affected from this variation in the parameter's  
9 value.

10 The best performing approach for parameterization of roughness length and displacement  
11 height, was obtained using the annually observed values of these parameters. The 'Yearly  
12 Observed' model demonstrated ~7% less error than the fixed-in-time 'Classical' canopy-  
13 roughness relationships. The combined 'Yearly Observed' approach used the  $z_0$  and  $d$  values  
14 for each year to predict friction velocity values in the same years. This method performed  
15 better than when applying the data observed during a single year to the entire time period.  
16 However, the roughness parameters observed during 2011 provided a more accurate and  
17 precise model for the entire 12-year time series, than the combined approach. The  $z_0$  and  $d$   
18 values observed during 2005 provided the worst model, but still performed better than the  
19 'Classical' approach. It is rather intuitive that when observations of  $z_0$  and  $d$  exist, they will  
20 provide the best approach for modeling of friction velocity (Table 3). Our results indicate that  
21 the inter-annual variability of canopy structure that affects roughness length has only a very  
22 small effect on the resulting friction velocity. Annual growing-season averages of  $z_0$  and  $d$   
23 from any single year can provide a suitable approximation to the decadal time series of  
24 roughness length parameter values. However, the low spatial coverage by flux networks over  
25 the globe limits the use of this method across large spatial domains.

26 LES with an explicit, prescribed canopy structure based on lidar observations of the canopy at  
27 a site can generate a surrogate virtual observations from which to evaluate the roughness  
28 parameters. However, these type of simulations are limited in their temporal domain (just a  
29 few hours as a representative of an entire decade). They are also dependent on high resolution  
30 canopy lidar observations that, to date, are not common. Parameterization approaches which  
31 rely on biometric observations, rather than on wind observations, may be the most reliable

1 and broadly available method to estimate long-term roughness parameters. Our ability to  
2 estimate canopy structure characteristics such as *LAI*, canopy height, and gap fraction over a  
3 broad range of spatial and temporal scales is continuously improving through the use of on-  
4 site biometric measurements, and airborne and satellite remote sensing observations (Chen et  
5 al., 2002;Jonckheere et al., 2004;Zheng and Moskal, 2009).

6 As an indication for the potential of biometric approaches, the approach suggested by  
7 Raupach (1994) performed even better than the combined 'Yearly Observed' approach (Table  
8 3). However, this approach relies on stem census observations. While such records are more  
9 common than flux sites, there is still no broad global coverage for this type of observation.  
10 We tested two biometric approaches that only required more commonly observable canopy  
11 characteristics. The approach by Nakai et al (2008a) and the approach derived by the virtual  
12 experiments in this study (the 'Biometric' approach) require *LAI*, canopy height and gap  
13 fraction or stand density to determine  $z_0$  and  $d$ . Of the two, our 'Biometric' approach  
14 performed relatively well, and provided slightly better estimates than the 'Classical' approach.  
15 Variable success by the three biometric methods may not be surprising – a study by  
16 Grimmond and Oke (1999) determined that careful consideration must be given to higher-  
17 order structural features of the surface than the ones represented in this study and include in  
18 the biometric approaches. Examples of such higher-order structural characteristics include the  
19 complexity of organization, and density of roughness elements. Similar reasoning could  
20 provide insight towards the poor performance of the method of Nakai et al. (2008a) at US-  
21 UMB, which is less dense, taller, and has higher *LAI* than those sites used to parameterize the  
22 'Nakai 08' method.

23 The 'Biometric' method presented in this study is essentially a variant of the 'Classical'  
24 method, with the major difference being the use of maximum canopy height as opposed to  
25 mean canopy height, and adding small perturbations to displacement height based on *LAI* and  
26 gap fraction. The limited success of this method can be attributed to some degree to the  
27 limited effect of inter-annual variability of canopy structure. However, a decade of  
28 observations in a site represents only a very narrow range of potential canopy structures. We  
29 predict that this method will significantly improve the prediction of friction velocity when  
30 applied to situations where canopy structural variability is larger, such as after significant  
31 disturbance events.

## 1 5 Conclusions

2 In this study we used an LES, long-term meteorological observations, and remote sensing of  
3 the canopy to explore the effects of canopy structure on surface roughness parameters in a  
4 forest site. We performed a virtual experiment to test the sensitivity of roughness parameters  
5 with respect to four axes of variation in canopy structure: (1) leaf area index, (2) the mode of  
6 the vertical profile of LAD, (3) canopy height, and (4) gap fraction. We found consistent  
7 relationships between the aerodynamic canopy height and *LAI*, maximum height, and gap  
8 fraction and between *d* and maximal canopy height. We found that the predicted values of  
9 friction velocity are not sensitive to roughness length. As a result, most of the roughness-  
10 based approaches we tested for simulating friction velocity performed similarly well. This is  
11 despite having very different approaches for determining the values of  $z_0$  and  $d$ , and having  
12 large differences in the range of  $z_0$  and  $d$  values. This is good news for modelers, because it  
13 limits the error from using the current approaches that do not vary in time and do not  
14 incorporate canopy structure.

15 Nonetheless, most of the approaches we tested which used annually variable  $z_0$  and  $d$  and that  
16 incorporated canopy structure provided better approximation for friction velocity than the  
17 'Classical', time-invariable method. Many easily obtainable metrics of canopy-structure  
18 characteristics are available through a suite of measurements, such as on-site meteorological  
19 and biometric observations or satellite-derived site characteristics. Additionally, many  
20 ecosystem models and ecosystem modules within earth system models resolve the growth of  
21 the forest and accurately predict canopy height and *LAI*. Some models, such as the Ecosystem  
22 Demography model (Medvigy et al., 2009) even resolve the distribution of stem sizes. Such  
23 demographic models could readily incorporate the approach by Raupach (1994) for a  
24 significant improvement in surface roughness parameterization. For other models that resolve,  
25 or are forced by observed leaf area and vegetation height, our LES-derived 'Biometric'  
26 approach could offer an easy way to dynamically affect the roughness-length  
27 parameterization. This could provide an improvement of surface flux modeling, especially  
28 when canopy structure variations are large. Due to limited spatial coverage by direct  
29 meteorological measurements, remote sensed structure statistics, and stand inventories, we  
30 suggest utilizing site- and time-specific biometric measurements of canopy structure to  
31 estimate site-level  $d$  and  $z_0$ . The effectivity of these model improvements will, of course, be

1 dependent upon the quality, quantity, and resolution of the datasets available at the forest of  
2 interest.

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19

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**Table 1:** Description of simulation cases used for sensitivity analysis of roughness parameters derived from an LES over variable canopy layouts, and the resulting roughness parameters for each simulation case. Canopy structure was varied along four axes: (a) *LAI*, (b) vertical LAD profile, (c) canopy height, (d) gap fraction and (e) realistic.

Experiment	LAI (m <sup>2</sup> m <sup>-2</sup> )	LAD (m <sup>2</sup> m <sup>-3</sup> )	Height (m)	Gap Fraction	<i>d</i> (m)	<i>z</i> <sub>0</sub> (m)	<i>d</i> / <i>h</i>	<i>z</i> <sub>0</sub> / <i>h</i>	$\lambda$	<i>h</i> <sub>a</sub> (m)	$\delta_e$ (m)
<b>(a)</b> <b>LAI</b> <b>variation</b>	1.0	Natural	21	0%	14.2	2.6	0.67	0.12	0.38	20.9	13.1
	2.6				13.7	3.1	0.65	0.15	0.41	21.1	11.0
	3.2				16.5	1.3	0.79	0.06	0.27	21.1	10.7
	3.7				7.6	4.0	0.36	0.19	0.29	21.2	9.9
	4.2				16.0	1.2	0.76	0.06	0.24	21.1	10.2
<b>(b)</b> <b>LAD</b> <b>profile</b> <b>variation</b>	4.2	Lower	21	0%	13.6	1.7	0.65	0.08	0.24	20.7	12.6
		Middle			8.8	5.7	0.42	0.27	0.55	19.1	8.2
		Natural			16.0	1.2	0.76	0.06	0.24	21.1	10.2
		Upper			13.8	2.8	0.66	0.14	0.38	21.2	10.2
<b>(c)</b> <b>Canopy</b> <b>height</b> <b>variation</b>	1.0	Natural	9	0%	4.4	0.8	0.49	0.09	0.17	9.3	7.1
			15		3.6	3.5	0.24	0.23	0.31	15.0	10.1
			21		14.2	2.6	0.67	0.12	0.38	20.9	13.1
			27		20.1	2.5	0.74	0.09	0.36	26.9	15.8
	4.2	Natural	9	0%	3.7	2.0	0.41	0.22	0.35	9.4	6.3
			15		8.7	2.5	0.58	0.17	0.38	15.2	7.9
			21		16.0	1.2	0.76	0.06	0.24	21.1	10.2
			27		20.1	2.9	0.75	0.11	0.41	27.1	11.9
<b>(d)</b> <b>Gap</b> <b>fraction</b> <b>variation</b>	1.0	Natural	27	0%	20.1	2.5	0.74	0.09	0.36	26.9	15.8
				10%	19.8	2.2	0.73	0.08	0.31	26.8	17.5
				25%	18.5	3.2	0.69	0.12	0.39	26.8	18.2
				35%	17.9	2.4	0.66	0.09	0.27	26.7	19.2
				50%	18.7	1.8	0.69	0.07	0.23	26.7	20.2
	4.2	Natural	27	0%	20.1	2.9	0.75	0.11	0.41	27.1	11.9
				10%	20.4	2.7	0.76	0.10	0.42	27.0	13.0
				25%	18.7	2.8	0.69	0.11	0.34	27.0	14.4
				35%	19.1	2.4	0.71	0.09	0.30	26.9	15.8
				50%	14.4	4.0	0.53	0.15	0.32	26.9	17.3
<b>(e)</b> <b>Realistic</b>	4.2	Natural	27	5%	14.2	0.9	0.67	0.05	0.43	16.7	10.3

7

1 **Table 2.** Results of a 3-way ANOVA to test any significance maximum canopy height ( $h_{max}$ ),  
 2 leaf area index ( $LAI$ ), and gap fraction ( $GF$ ) have on displacement height ( $d$ ), roughness  
 3 length ( $z_0$ ), aerodynamic canopy height ( $h_a$ ), or eddy-penetration depth ( $\delta_e$ ).  $P$ -values listed in  
 4 **bold** font indicate a significant effect.

5

Variable	3-way ANOVA $p$ -value		
	$h_{max}$	$LAI$	$GF$
$D$	<b>&lt;0.001</b>	0.065	0.370
$z_0$	0.290	0.227	0.918
$h_a$	<b>&lt;0.001</b>	<b>&lt;0.001</b>	<b>0.007</b>
$\delta_e$	<b>&lt;0.001</b>	<b>0.001</b>	<b>0.004</b>

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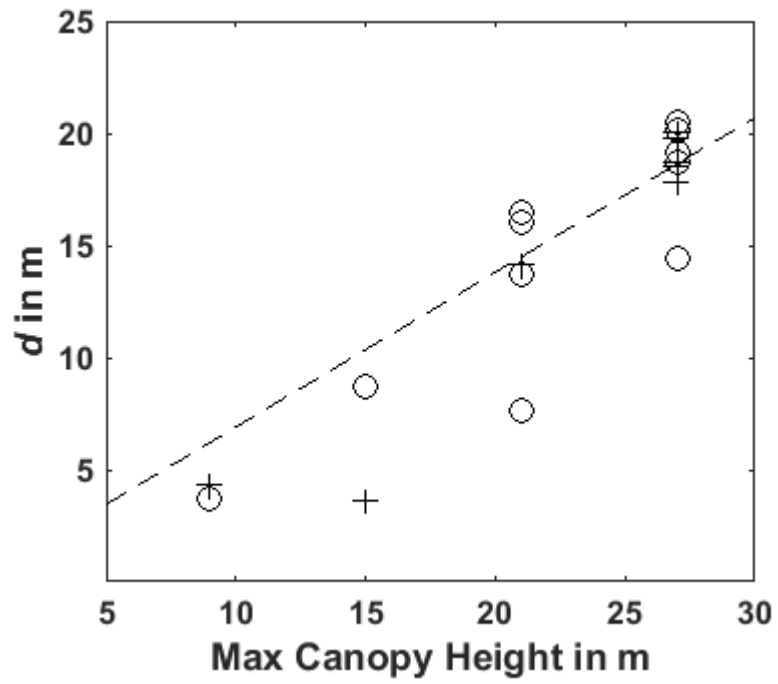
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**Table 3.** 30-min block-averaged friction velocity ( $u_*$ ) model evaluation against measured  $u_*$  for displacement height ( $d$ ) and roughness length ( $z_0$ ) calculated from various methods – 'Classical', 'Yearly Observed', 'Biometric', 'Raupach 94', and 'Nakai 08' - at US-UMB spanning the 2000-2011 growing seasons. We show the slope and intercept of the linear fit, which are measures of the accuracy of the models, the coefficient of determination ( $r^2$ ), which is a measure of precision, and the root mean square error (RMSE) between modeled and observed  $u_*$ , which is indicative of both precision and accuracy.

<b>Method</b>		<b><math>d</math> (m)</b>	<b><math>z_0</math> (m)</b>	<b>Slope</b>	<b>Intercept</b>	<b><math>r^2</math></b>	<b>RMSE</b>
<b>Classical</b>		14.0	2.10	1.41	-0.05	0.584	0.212
<b>Explicit-LES</b>		14.2	0.94	1.31	-0.06	0.597	0.194
<b>Yearly Obs.</b>	Combined (2000-2011)	23.1 (18.3-26.0)	1.40 (0.99-1.99)	1.11	-0.04	0.564	0.187
	2008 (lowest bias)	26.0	0.99	1.01	-0.06	0.593	0.188
	2011 (highest $r^2$ )	25.0	1.17	1.19	-0.07	0.607	0.179
	2005 (worst)	18.3	1.99	1.38	-0.06	0.588	0.207
<b>Biometric</b>		24.5 (24.0-25.0)	3.74 (3.67-3.82)	1.41	-0.05	0.585	0.212
<b>Raupach 94</b>		17.2 (16.6-17.9)	0.89 (0.88-0.91)	1.24	-0.07	0.604	0.183
<b>Nakai 08</b>		11.5 (11.1-12.0)	2.59 (2.40-2.86)	1.43	-0.05	0.582	0.216

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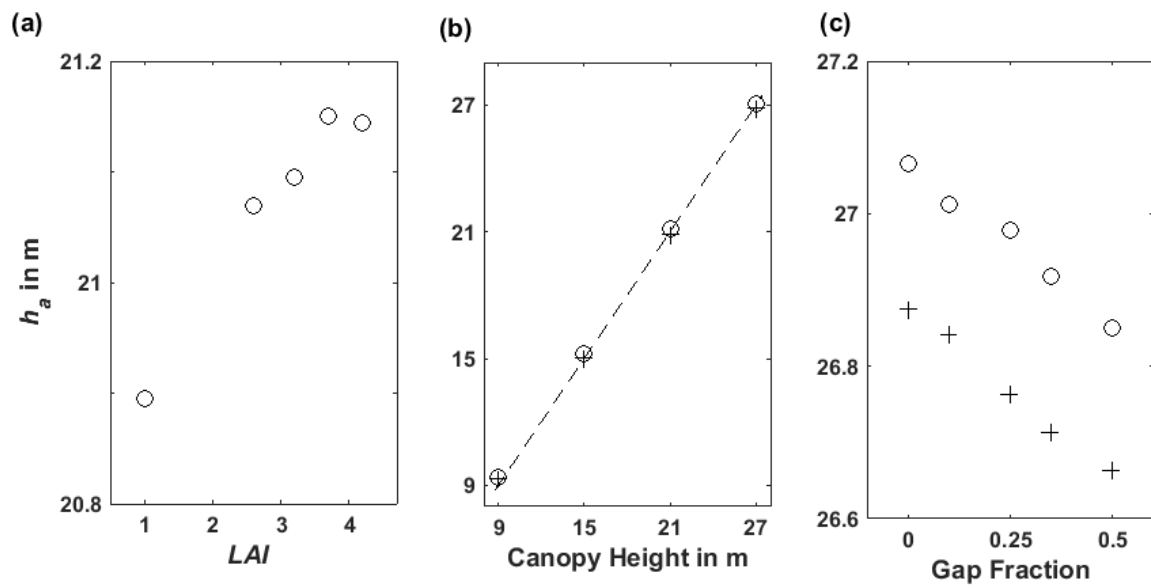


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**Figure 1.** LES domain-averaged  $d$  vs. maximum canopy height. Crosses and circles correspond to leaf-off ( $LAI = 1.0 \text{ m}^2 \text{ m}^{-2}$ ) and leaf-on ( $LAI > 1.0 \text{ m}^2 \text{ m}^{-2}$ ) conditions, respectively. Best-fit line (forced through  $[0,0]$ ) shown as dashed line ( $d = 0.69h_{\max}$ ).

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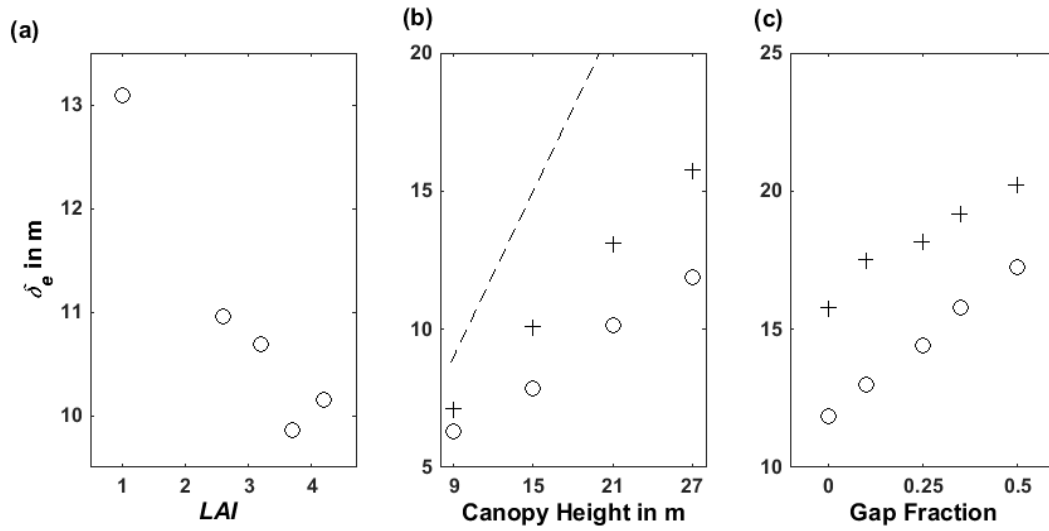
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4 **Figure 2.** LES domain-averaged aerodynamic canopy height ( $h_a$ ) vs. (a) leaf area index (LAI),  
5 (b) canopy height ( $h_{max}$ ), and (c) gap fraction (GF). For (b) and (c), crosses and circles  
6 correspond to leaf-off and peak-LAI conditions, respectively.

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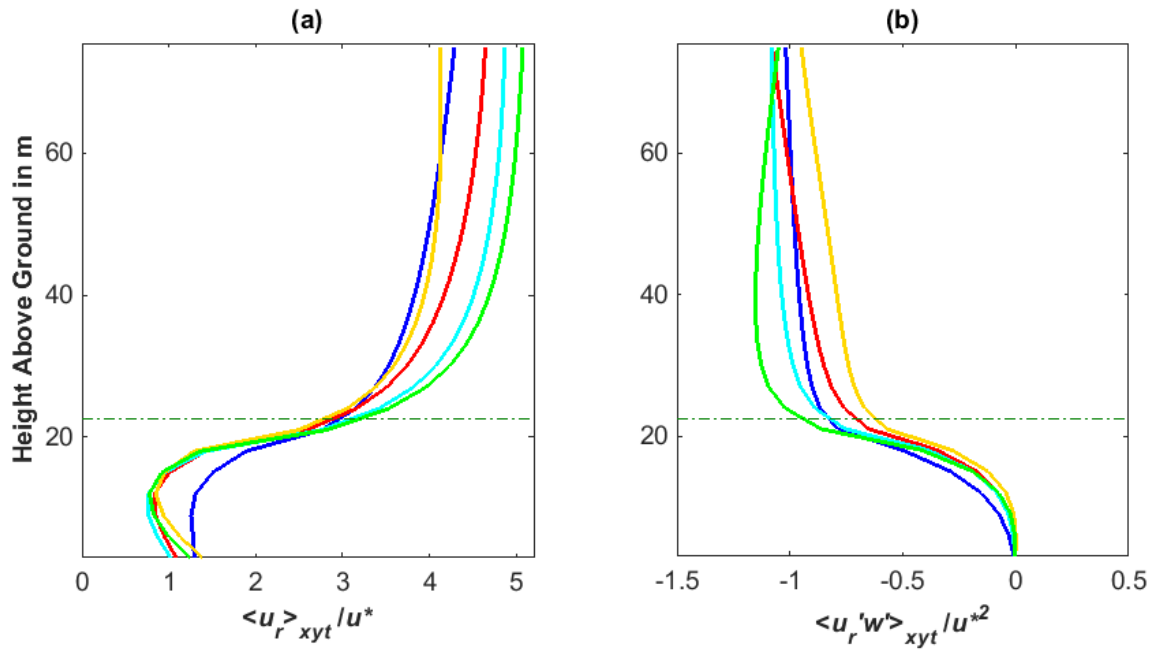
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**Figure 3.** LES domain-averaged eddy-penetration depth ( $\delta_e$ ) vs. (a) leaf area index ( $LAI$ ), (b) canopy height ( $h_{max}$ ) and (c) gap fraction ( $GF$ ). For (b) and (c), crosses and circles correspond to leaf-off and peak- $LAI$  conditions, respectively. The dashed line in panel (b) represents the 1:1 line.

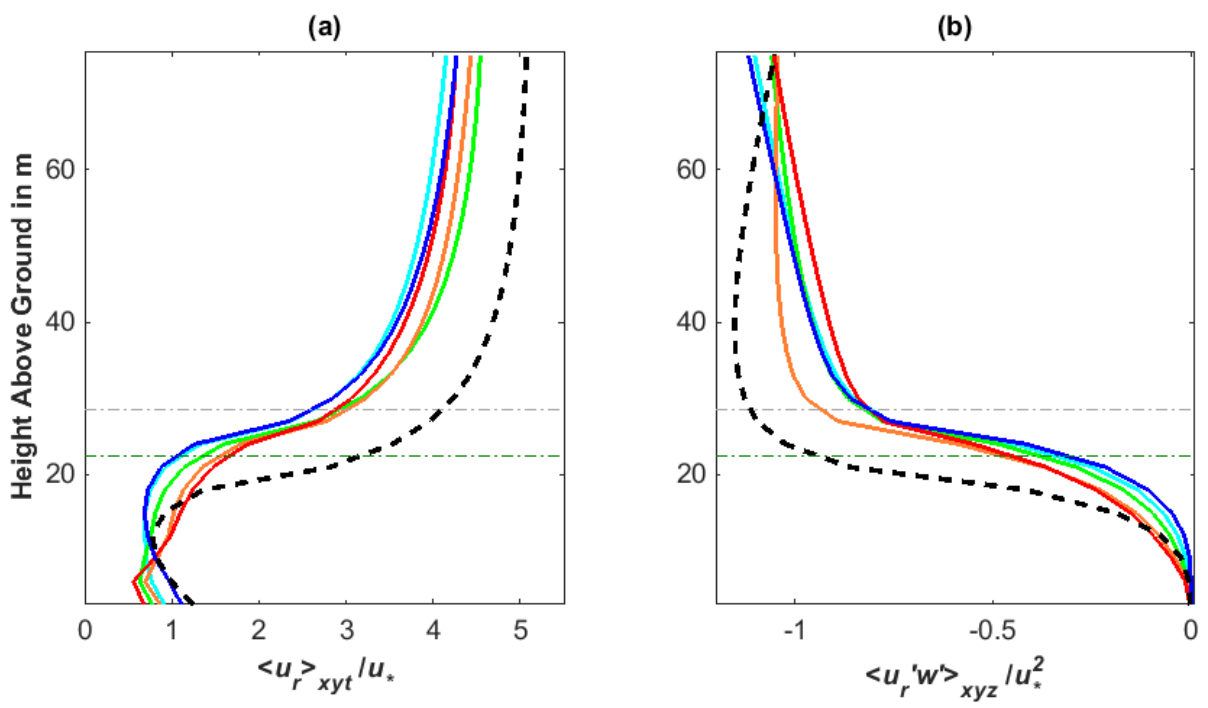
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**Figure 4.** Vertical profiles of (a) Horizontal wind normalized by friction velocity, and (b) momentum flux normalized by the square of friction velocity for  $LAI = 1.0 \text{ m}^2 \text{ m}^{-2}$  (blue),  $LAI = 2.6 \text{ m}^2 \text{ m}^{-2}$  (cyan),  $LAI = 3.2 \text{ m}^2 \text{ m}^{-2}$  (green),  $LAI = 3.7 \text{ m}^2 \text{ m}^{-2}$  (orange), and  $LAI = 4.2 \text{ m}^2 \text{ m}^{-2}$  (red). Canopy height shown as horizontal dashed green line.

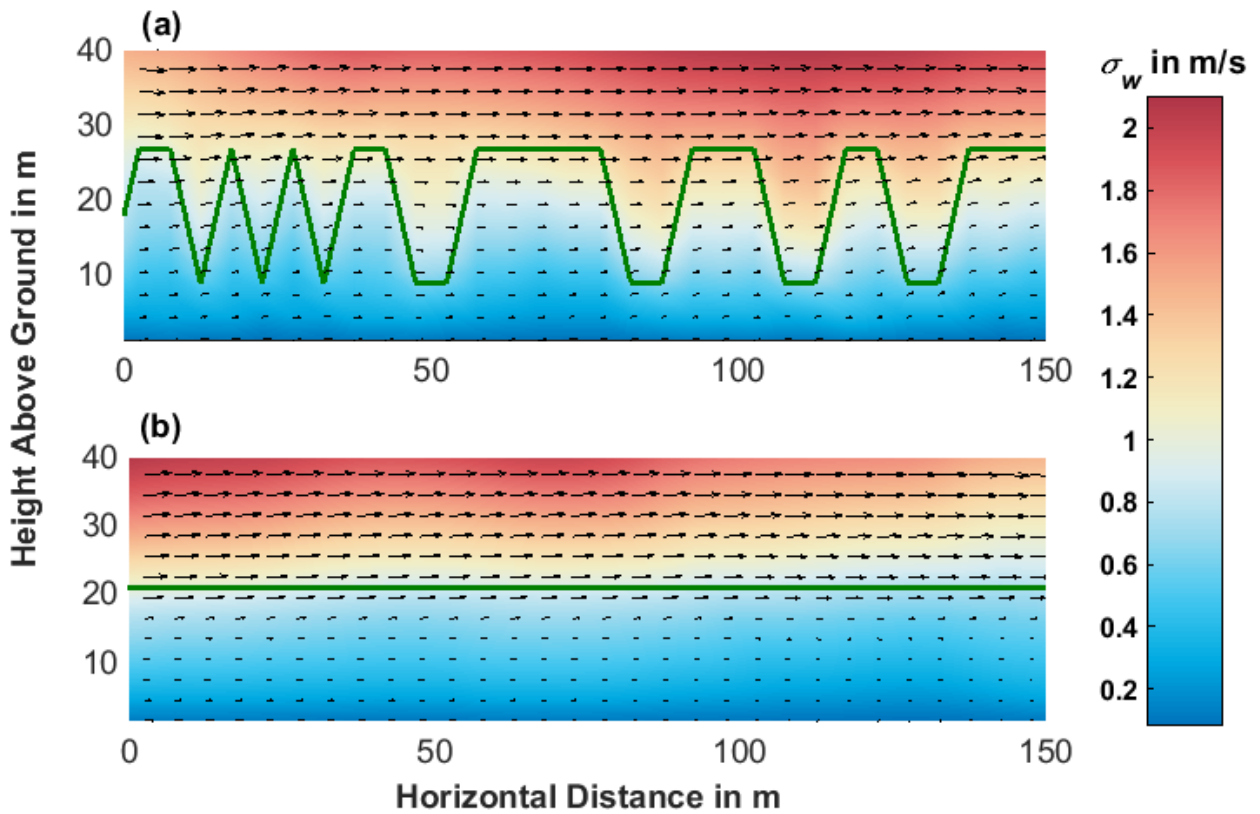
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**Figure 5.** Vertical profiles of (a) Horizontal wind normalized by friction velocity, and (b) momentum flux normalized by the square of friction velocity in a 27 m tall canopy with gap fractions of 0% (blue), 10% (cyan), 25% (green), 35% (orange), and 50% (red); and in a continuous 21 m tall canopy (dashed back). Canopy height for the tall and short canopies is shown as dashed horizontal gray and green lines, respectively.

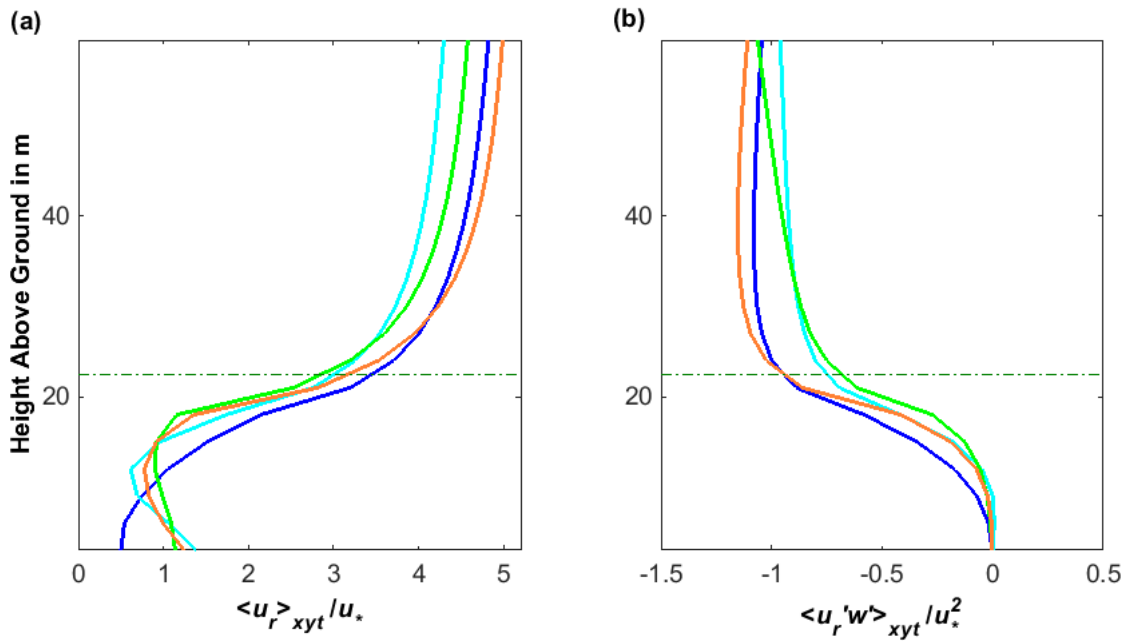
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3 **Figure 6.** Vertical cross-section through the simulation results of (a) a 27 m tall canopy with  
4 25% gap fraction and (b) homogeneous 21 m tall canopy. 30-minutes mean wind speed and  
5 direction are illustrated using black arrows, the standard deviation of vertical velocity (an  
6 indication of turbulence intensity) is plotted using a colormap. Canopy top in each simulation  
7 is illustrated by a solid green line.

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2 **Figure 7.** Vertical profiles of (a) Horizontal wind normalized by friction velocity, and (b)  
 3 momentum flux normalized by the square of friction velocity for 'Lower' (blue), 'Middle'  
 4 ('cyan), 'Upper' (green), and 'Natural' (orange) LAD profiles. Canopy height shown as  
 5 dashed horizontal green line.

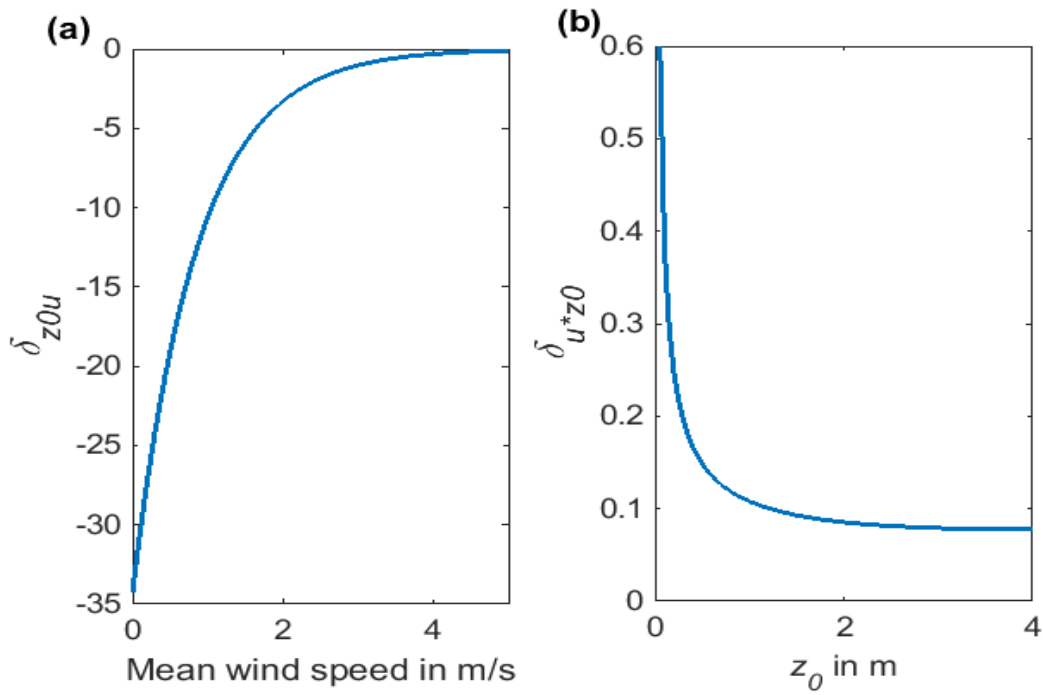
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2 **Figure 8.** (a) Sensitivity analysis of  $z_0$  as a function of variation of the mean wind speed  
3 ( $\delta_{z_0 u}$ ). We illustrate it here is a particular range of parameters, choosing a canopy height  $h=22$   
4 m (roughly the height we used in the simulation and observation site), displacement height  
5  $d=0.67h$ , observation height of  $2h$  (the recommended observation height for a flux tower) and  
6  $u_*$  of 0.35 m/s. The results are similar for other canopy heights and  $u_*$  values. (b) Sensitivity  
7 of  $u_*$  to variation in  $z_0$  ( $\delta_{u^* z_0}$ ). We plotted the response curve over the same parametric range  
8 expected for  $z_0$  values, wind speed at the center range of 3 m/s.  $u_*$  is relatively insensitive  
9 ( $\delta_{u^* z_0} < 0.15$ ) for any  $z_0$  above 0.5 m.

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