

1 **A model of the methane cycle, permafrost, and hydrology of the Siberian**
2 **continental margin**

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5
6 **Abstract**

7 A two-dimensional model of a passive continental margin was adapted to
8 the simulation of the methane cycle on Siberian continental shelf and
9 slope, attempting to account for the impacts of glacial / interglacial
10 cycles in sea level, alternately exposing the continental shelf to freezing
11 conditions with deep permafrost formation during glacial times, and
12 immersion in the ocean in interglacial times. The model is then subjected
13 to a potential future climate warming scenario.

14 Pore fluid salinity plays a central role in the model geochemical dynamics.
15 In the permafrost zone, pure water ice tolerates a higher fluid salinity
16 than methane hydrate can, eliminating hydrate as an equilibrium phase.
17 An analogous region in the ice - hydrate - brine phase diagram excludes
18 ice in favor of hydrate, but the two phases can coexist at a sub-saturated
19 methane concentration. In the permafrost zone (cold and low pressure),
20 in contrast, the dissolved methane concentration cannot be higher than
21 equilibrium with gas, so the hydrate exclusion from this zone is
22 inescapable. This thermodynamic constraint restricts methane hydrate to
23 at least 300 meters depth below the sediment surface, precluding a fast
24 hydrate dissolution response to sea-floor warming.

25 The initial salinity of the sediment column may have been affected by
26 previous hydrological forcing, because freshwater invasion driven by a
27 pressure head is probably much faster than salinity invasion due to
28 convective-diffusive processes. This has a ratcheting effect, leaving relict
29 fresh water lenses below sea level in many parts of the world. The pore
30 fluid salinity determines the relative volumes of the ice, brine, and
31 hydrate phases in the sediment column, and therefore the timing of ice
32 formation and melting, but the chemical composition, in particular the
33 salinity of the brine phase, is fixed, in equilibrium, by the local

34 temperature. The model hydrate inventory on the shelf is however
35 sensitive to the initial salinity of the sediment column.

36 Through the glacial / interglacial cycles, the atmospheric methane flux is
37 affected most strongly by changes in sea level, because bubbles dissolve
38 in the ocean when sea level is high. Methane emissions to the
39 atmosphere are highest during the sea-level fall part of the cycle (as soil
40 is freezing), rather than during the warming deglaciations. Timings of the
41 atmospheric methane flux changes are sensitive to assumptions made
42 about bubble transport inhibition by permafrost. The atmospheric flux is
43 sensitive to biogenic and thermogenic methane production rates, but the
44 hydrate inventory is only sensitive to thermogenic methane production.
45 The geothermal heat flux affects the thickness of the hydrate stability
46 zone (primarily the depth of its base), but not the inventory of hydrate in
47 the model until a low-gradient threshold is passed. The model produces
48 methane inventory changes of 50 Gton C as bubbles, and as much as
49 hundreds of Gton C as hydrate, but these reservoir changes interact
50 mostly with pore water dissolved methane rather than driving immediate
51 methane loss from the sediment column.

52 The model-predicted methane flux to the atmosphere in response to a
53 warming climate is small, relative to the global methane production rate,
54 because of the ongoing flooding of the continental shelf. The
55 atmospheric methane flux response to sudden warming takes thousands
56 of years, because of the slow thermal diffusion time to the hydrate
57 stability zone, and because a warming perturbation beginning now would
58 follow a much larger warming perturbation that started thousands of
59 years ago, when the sediment surface flooded. On time scales of
60 thousands of years in the future, the increased methane flux increase due
61 to warming could be completely counteracted by sea level rise, which
62 decreases the efficiency of bubble transit through the water column.

63 **1. Introduction**

64 ***1.1 The Siberian Continental Shelf System***

65 The Siberian Arctic continental shelf has been the focus of attention from
66 scientists and the public at large for its potential to release methane, a
67 greenhouse gas, in response to climate warming, a potential amplifying
68 positive feedback to climate change [*Shakhova, 2010; Westbrook,*
69 *2009*]. The goal of this paper is to simulate the geophysical and carbon

70 cycle dynamics of the Siberian continental margin within the context of a
71 basin- and geologic time-scale mechanistic model of the coastal margin
72 carbon cycle called SpongeBOB [Archer *et al.*, 2012]. An initial condition
73 for the glacial cycle simulations was generated by spinning the up at low
74 resolution over 62 million simulated years. Then the model at higher
75 resolution is driven by cyclic changes in sea level and air temperature
76 resulting from glacial cycles, to simulate the impact of the hydrological
77 pressure head and permafrost formation on the fluid flow and methane
78 cycle on the shelf. Finally, an 100,000-year interglacial interval in the
79 simulation is subjected to anthropogenic warming of the overlying water
80 and potential 60-meter changes sea level. Sensitivity studies are
81 presented for the biogenic and thermogenic methane production rates,
82 initial salinity, geothermal temperature gradient, rates of hydrological
83 flow, and permafrost impact on gas mobility.

84

1.1.1 Permafrost

85 One component of the simulation is a wedge of frozen sediment
86 (permafrost) submerged beneath the ocean on the continental shelf of
87 Siberia, left behind from glacial time when the shelves were exposed to
88 the frigid atmosphere by lowered sea level [Romanovskii and Hubberten,
89 2001]. The ice is thought to provide a seal to upward migration of
90 methane gas [Shakhova *et al.*, 2009], especially where ancient fresh
91 groundwater flow produced a layer of very high saturation ice infill, a
92 formation called the Ice Complex in Siberia [Romanovskii *et al.*, 2000],
93 although there are high ice saturations found in the Alaskan Arctic as well
94 [Zimov *et al.*, 2006].

95 With inundation by the natural sea level rise over the last 10+ thousand
96 years, the permafrost is transiently melting, although the time constant
97 for this is generally long enough that significant frozen volume remains,
98 especially in shallower waters which were flooded more recently
99 [Khvorostyanov *et al.*, 2008a; Nicol'sky and Shakhova, 2010; Romanovskii
100 and Hubberten, 2001; Romanovskii *et al.*, 2004; Shakhova *et al.*, 2009;
101 Taylor *et al.*, 1996]. Even overlying water at the freezing temperature
102 can provoke subsurface melting by providing a warmer boundary
103 condition against which geothermal heat establishes the subsurface
104 temperature profile, but with climate warming, the waters could surpass
105 the freezing temperature, allowing heat to flow from above as well as
106 below [Khvorostyanov *et al.*, 2008b].

107 Elevated methane concentrations have been measured in the water
108 column over the Siberian shelf, even in areas of shallow water where the
109 permafrost should still be strongly intact [*Shakhova, 2010; Shakhova et*
110 *al., 2005*]. Chemical and isotopic signatures of hydrocarbons adsorbed
111 onto surface sediments indicate a thermal origin [*Cramer and Franke,*
112 *2005*], suggesting that the methane is produced many kilometers deep in
113 the sediment column. The apparent ability for this methane to transverse
114 the barrier of the Ice Complex has been attributed to hypothesized
115 openings in the ice (called “taliks”), resulting from lakes or rivers on the
116 exposed shelf, or geologic faults [*Nicol'sky and Shakhova, 2010;*
117 *Romanovskii et al., 2004; Shakhova et al., 2009*].

118 **1.1.2 Salt**

119 Dissolved salt in the pore waters can have a strong impact on the timing
120 of thawing permafrost [*Nicol'sky and Shakhova, 2010; Shakhova et al.,*
121 *2009*]. When sea level drops and exposes the top of the sediment
122 column to the atmosphere and fresh water, the salinity of the subsurface
123 pore waters can be flushed out by hydrological groundwater flow, driven
124 by the pressure head from the elevated terrestrial water table above sea
125 level. The boundary between fresh and salty pore water tends to
126 intersect the sediment surface at the water's edge [*Moore et al., 2011*].
127 From there, the boundary tends to dip landward, to a depth of
128 approximately 40 meters below sea level for every 1 meter of elevation
129 of the table water. The ratio of water table elevation to freshwater lens
130 depth is driven by the relative densities of fresh and salt water, as the
131 fluid seeks an isostatic balance in which the fresh water displaces an
132 equal mass of salt water [*Verrjuit, 1968*].

133 The SpongeBOB model has been modified to simulate the processes
134 responsible for these observations. We do not attempt to simulate a
135 detailed outcropping history over 62 million-year spinup time of the
136 sediment column, but rather demonstrate the general process by
137 subjecting the nearly complete sediment column to a one-time sea level
138 lowering, exposing the continental shelf to groundwater forcing. After a
139 few million years, the sediment column subsides, due to compaction and
140 absence of sediment deposition, resulting in a sediment column that has
141 been considerably freshened by the atmospheric exposure. This
142 freshening persists in the model for millions of years, because there is no
143 corresponding “salt-water pump” during high sea-level stands. This
144 behavior is consistent with the discovery of vast nearly fresh aquifers in

145 currently submerged continental shelf regions around the world [*Post et*
146 *al.*, 2013], left over from groundwater forcing during glacial time.

147 **1.1.3 Carbon**

148 Another component of the simulation is the Yedoma, deposits of wind-
149 blown dust and organic carbon that accumulated on the coastal plains of
150 exposed continental shelves during glacial times [*Zimov et al.*, 2006].
151 The deposits contain a substantial fraction of organic carbon, consisting
152 of grass roots and remains, preserved by the freezing conditions. When
153 they thaw, they begin to release CO₂ and methane to the atmosphere
154 [*Dutta et al.*, 2006; *Schuur et al.*, 2008; *Zimov et al.*, 2006]. Oxidation
155 of the carbon can give off enough heat to accelerate the melting driven
156 by primary climate forcing [*Khvorostyanov et al.*, 2008b].

157 **2. Model Description**

158 ***2.1 Previously Published Model Formulation***

159 SpongeBOB is a two-dimensional basin spatial-scale and geological time-
160 scale model for the methane cycle in continental margin sediments. The
161 model, configured for a passive margin basin, was described by Archer et
162 al [2012], as applied to the Atlantic coast of the United States. The
163 model attempts to “grow” a sediment column based on first principles or
164 parameterizations of sediment and pore water physical and chemical
165 dynamics. The approach integrates processes of the carbon and methane
166 cycles within the evolving sediment column matrix, providing constraints
167 to the rates and processes that may inform the response of the system
168 to future changes in climate. Where model parameterizations or
169 parameters are poorly constrained, sensitivity studies are used to assess
170 which of the uncertainties are the most significant.

171 Sediment is delivered from the coast of the model as riverine material,
172 and it settles according to a parameterization of grain size, with finer
173 material advecting further offshore before deposition. The organic
174 carbon concentration of the depositing material is determined in the
175 model as a function of water depth at the time of sedimentation. Rather
176 than attempt to simulate the complex biogeochemical dynamics of the
177 ocean and surficial sediments (early diagenesis), the POC fraction and the
178 H/C ratio of the organic matter are specified by a parameterization based
179 on water depth to reproduce the observed patterns of sediment surface
180 POC deposition, as a driver to the subsurface model.

181 The H/C ratio of the depositing organic matter limits the potential extent
182 of methane production from the organic matter. The degradation rate of
183 organic carbon is estimated based on its age, a relationship that captures
184 many orders of magnitude of variability in the natural world [*Middelburg*
185 *et al.*, 1997]. The reaction pathways presume a reactive intermediate H_2 ,
186 which either reduces SO_4^{2-} if it is available or it reacts with DIC to produce
187 methane. Isotopic fractionation of CO_2 , CH_4 , and radioiodine are
188 simulated by maintaining parallel concentration fields of different
189 isotopologs, and applying fractionation factors to the chemical kinetic
190 rate constants or equilibrium conditions. Dissolved methane in the pore
191 water has the potential to freeze into methane hydrate or degas into
192 bubbles, depending on the temperature, pressure, salinity, and CH_4
193 concentration.

194 Sediment compaction drives pore fluid advection through the sediment
195 column, but the fluid flow is also focused in some simulations by ad hoc
196 vertical channels of enhanced permeability, to simulate in at least a
197 qualitative way the impact of heterogeneity in the fluid flow on the
198 characteristics of the tracer field. Methane hydrate is concentrated in
199 these channels by focused upward flow, and the pore-water tracers in the
200 channels resembles that of hydrate-bearing regions (in SO_4^{2-}
201 concentration and 129-Iodine ages).

202 Most of the model configuration and formulation was described by Archer
203 et al. [2012]. The new modifications required to simulate groundwater
204 hydrological flow and permafrost formation are described in detail below.

205 **2.2 Groundwater Hydrology**

206 **2.2.1 Pressure Head**

207 When the sediment column is exposed to the atmosphere, the pressure
208 field from the variable elevation of the water table (the pressure head)
209 begins to affect the fluid flow. The pressure head for a fluid particle at
210 the depth of the water table varies as

$$211 P_{\text{head}}(z) = g \int_z^{z_{\text{wt}}} \rho_{\text{seawater}} dz$$

212 where z_{wt} is the elevation of the water table. The pressure head at each
213 depth in the domain is a function of the physical water table height above
214 it and the density anomalies integrated from the water table to the depth
215 of the point in question. The pressure head resulting from a varying

216 water table can therefore be altered at depth by variations in pore fluid
217 density driven by salinity or temperature.

218 **2.2.2 Fluid Flow**

219 The pressure head acts in concert with the excess pressure P_{excess} to drive
220 horizontal Darcy flow through the sediment, as

$$221 \quad u_{\text{Darcy},i \rightarrow i+1} = \frac{k_{h,i} + k_{h,i+1}}{2\mu} \frac{(P_{\text{excess},i} - P_{\text{excess},i+1}) + (P_{\text{head},i} - P_{\text{head},i+1})}{(\Delta x_i + \Delta x_{i+1})/2}$$

222 while the vertical flow in the model is driven only by compaction pressure

$$223 \quad w_{\text{Darcy},j \rightarrow j+1} = \frac{k_{v,j} P_{\text{excess},j} - P_{\text{excess},j+1}}{\mu (\Delta z_j + \Delta z_{j+1})/2}$$

224 The value of P_{excess} is determined from the porosity and sediment load of
225 the sediment in each grid box, as described in Archer et al [2012]. An
226 assumed sediment rheology is used to calculate the load-bearing capacity
227 of the solid matrix within a given grid cell. P_{excess} is calculated by assuming
228 that the load of the solid phase overlying the grid cell that is not carried
229 by the solid matrix must be carried by the P_{excess} in the fluid phase. When
230 ice forms (described below), it leaves P_{excess} unchanged, but the flow is
231 inhibited by scaling the permeability k by the decrease in fluid porosity.

232 In previous versions of the SpongeBOB model, the fluid flow was
233 calculated explicitly, each time step, as a function of P_{excess} at the
234 beginning of the time step. Numerical stability motivated a modification
235 of the vertical flow to an implicit numerical scheme, which finds by
236 iteration an internally consistent array of vertical flow velocities and
237 resulting P_{excess} values from a time point at the end of the time step.
238 Ocean and atmosphere models often use this methodology for vertical
239 flow. A benefit to this change is stability in the vertical flow field,
240 reducing numerical noise that can cause trouble with other aspects of the
241 model such as ice formation. Implicit schemes can be more efficient
242 computationally, but in this case the execution time is not improved by
243 the implicit method, just the stability.

244 Note that the flow scheme in its formulation is entirely elastic, whereas in
245 reality, pore fluid excluded by the pressure of a sediment column above
246 sea level, for example, where it is uncompensated by buoyancy in

247 seawater, should remain excluded when sea level rises again, like
248 toothpaste from the tube. However, my attempts to embed this plastic
249 behavior into an implicit solver failed to converge.

250 **2.2.3 Water Table Depth**

251 The model maintains z_{wt} , the elevation of the water table within the
252 sediment column, as a continuous variable that ranges through the
253 discreet vertical grid of the model. The formulation allows boxes to be
254 empty of water or partially “saturated” at the top of the fluid column. In
255 these simulations, however, the water table remained very close to the
256 sediment surface, as unsaturated soil produced by subsurface flow is
257 quickly replenished by hydrological recharge.

258 **2.2.4 Canyons**

259 The model as described so far represents a laterally homogeneous slab, a
260 poor approximation for hydrology above sea level because of the
261 formation of canyons and river networks in a real drained plateau. The
262 depth of the water table in a river canyon is depressed, relative to the
263 surroundings, to the depth of the canyon. The water table is higher in
264 between the canyons because of recharge, and the difference in head
265 drives lateral flow, the canyons acting to drain the sediment column.

266 The model formulation has been altered to represent this mechanics in a
267 simplified way. Rather than expand the model into the full third
268 dimension, the 2-D field of the model is held to represent the sediment
269 column at a hypothetical ridge crest, as altered by an adjacent canyon.
270 The canyon elevation is represented by z_{canyon} , and its width by a scale
271 Δy_{canyon} . A cross-column flow velocity $v_{Darcy,j}$ is calculated as

$$272 \quad v_{Darcy,j} = \frac{k_{h,j} (P_{head,canyon} - P_{head})}{\mu \Delta y_{canyon}}$$

273 where $P_{head,canyon}$ is the pressure head as a function of depth in the
274 hypothetical canyon, calculated assuming that the water table outcrops
275 at z_{canyon} , and that the temperatures in the sediment column have
276 adjusted to the formation of the canyon, such that the near-surface
277 geothermal gradient is the same between the hypothetical canyon and
278 the bulk sediment column. The lateral “drainage” flow ($v_{Darcy,j}$) drives
279 vertical velocities by continuity.

280 The horizontal distance scale Δy_{canyon} is somewhat arbitrary and difficult to
281 constrain, given that in the reality of river networks the distance to the
282 nearest canyon from any point in the domain is likely to be a function of
283 altitude, distance from the coast, and time. Another poorly resolved
284 factor is the depth of the canyon. In reality, canyons cut into a plateau
285 following a dynamic that erosion is proportional to slope, but stops at sea
286 level. As a simplification the model is set to hold the canyon depth at
287 current sea level.

288 The canyon mechanism accelerates the freshening of the sediment
289 column by providing a pathway for the escape of the salt water, although
290 it was found that the net effect in the model is not dramatic (results
291 shown below), in part because the canyon drainage mechanism only acts
292 on pore fluids above sea level, while the hydrological freshwater pumping
293 mechanism reaches much deeper than sea level. In the real fractal
294 geometry of canyons, the spacing between canyons across a plain is
295 similar to the width of the plain (length of the canyons), so the Base
296 simulation assumes a canyon width of 100 km, based on the 100+ km
297 width scale of the continental shelf.

298 **2.3 Permafrost**

299 The ice model is based on an assumption of thermodynamic equilibrium, in
300 which the heat content of the cell is distributed between the pure ice,
301 hydrate, and brine phases, and the salinity of the brine drives a freezing
302 point depression to match the local temperature. The ice content in a grid
303 cell relaxes toward equilibrium, quickly enough to approximate an
304 equilibrium state through the slow temperature evolution in the model
305 (which neglects a seasonal cycle at the surface), but slowly enough to
306 avoid instabilities with other components of the model such as fluid flow
307 and methane hydrate formation. A limiter in the code prevents more
308 than 99% of the fluid in a grid cell from freezing, but the thermodynamic
309 equilibrium salinity is used to calculate, for example, the stability of
310 methane hydrate, to prevent the numerical limiter from affecting the
311 thermodynamic availability of water to drive chemical reactions.

312 This model formulation implies that the salinity of pore fluid in subfreezing
313 conditions (the permafrost zone) is independent of the original salinity of
314 the bulk sediment column, but is rather determined only by the freezing-
315 point depression implied by the temperature. If the original column is
316 relatively fresh, there will be a smaller volume of pore fluid at a

317 subfreezing temperature than if it is originally salty (see for example
318 Figure 4 in [Nicolisky and Shakhova, 2010]), but the activity of the water
319 (a correlate of the salinity) is set by the temperature and the
320 thermodynamics of pure ice, which are the same in the two cases. Layers
321 of high-salinity unfrozen brines called cryopegs [Gilichinsky et al., 2005;
322 Nicolisky et al., 2012] are consistent with this formulation.

323 **2.4 Thermodynamic competition between ice and hydrate**

324 The high salinity (low activity of water) in the permafrost zone has the
325 practical impact of excluding methane hydrate from permafrost soils that
326 are significantly colder than freezing. The thermodynamics are illustrated
327 in Figure 1. When the system consists only of ice and fluid phases, the
328 equilibrium salinity S_{eq} increases with decreasing temperature below
329 freezing (Figure 1a, left). Above the melting temperature, ice is unstable,
330 as indicated by the nonzero values of the disequilibrium temperature,
331 $\Delta T_{eq, ice} = T - T_{eq, ice}$, in contours, even in zero-salinity water (right). For a
332 system consisting of only the hydrate and fluid phases (assuming that ice
333 formation is disallowed, and also gas saturation for methane) (Figure 1b),
334 the behavior is similar but with an added pressure dependence due to the
335 compressibility of the gas phase. When both solid phases are allowed,
336 the overall equilibrium salinity will whichever is higher between $S_{eq, ice}$ and
337 $S_{eq, hydrate}$. Whichever phase can seize water at its lowest activity (highest
338 salinity) will be the stable phase. The salinity of the brine excluded from
339 that phase will be too high to permit the existence of the other solid
340 phase at that temperature. The contours show ΔT_{eq} for hydrate (solid)
341 and ice (dashed), which are also plotted in color in Figures 1d and e. This
342 is illustrated in Figure 1d, in colors of $\Delta T_{eq, hydrate}$ and contours of the
343 excess salinity relative to hydrate equilibrium, $S_{max} - S_{eq, hydrate}$. Hydrate is
344 only stable when $\Delta T_{eq, hydrate}$ is zero (purple color). Under permafrost
345 conditions of low pressure and low temperature (upper left corner), $\Delta T_{eq, hydrate}$
346 is greater than zero, indicating that hydrate is unstable, coinciding
347 with the salinity forcing from the ice, in overlain contours. A similar
348 exclusion of ice in part of the hydrate stability zone is seen Figure 1e, but
349 this would only happen in nature in conditions of unlimited methane. The
350 resulting phase diagram for ice and methane hydrate is shown in Figure
351 1f. Hydrate stability is suppressed in the permafrost zone by this
352 thermodynamic mechanism.

353 Permafrost formation has several impacts on the methane cycle in the
354 model. Biogenic methanogenesis is assumed stopped in the ice fraction

355 of a grid cell (which approaches unity but never reaches it in the model,
356 due to exclusion of salt into brine). Bubble transport in the model
357 balances bubble production, driven by a small and not very well
358 constrained standing bubble concentration within the pore space. It is
359 generally assumed [*Shakhova et al.*, 2010b] that permafrost inhibits gas
360 transport through the sediment column, both based on sediment column
361 carbon and hydrogen budgets [*Hunt*, 1995] and on the tight seal
362 provided by the ice complex. The seal provided to Arctic lakes, which can
363 drain overnight if the seal is breached, also lends credence to this idea. In
364 the model, this effect was simulated by stopping gas transport
365 completely when a grid cell exceeds 50% ice fraction (with sensitivity
366 runs assuming 10%, 30%, 70%, and 90%).

367 **2.5 Atmospheric Methane Fluxes**

368 Bubbles emerging from the sediment column into the water column of the
369 ocean may dissolve in the water column, or they may reach the sea
370 surface, a direct methane flux to the atmosphere [*Westbrook et al.*,
371 2009]. In the model, bubble dissolution in the water column is assumed
372 to attenuate the bubble flux according to the water depth with an e-
373 folding attenuation scale of 30 meters [*Gentz et al.*, 2014; *Portnov et al.*,
374 2013; *Westbrook et al.*, 2009]. In reality, a low-flux gas seep, producing
375 small bubbles, will probably not reach as far into the water column as a
376 30-meter scale height, while a faster seep can reach further. Methane
377 dissolved in the water column, in reality, may survive oxidation (time
378 constant of about a year), and degas to the atmosphere, but this
379 possibility is not included in the model. For land grid points (exposed to
380 the atmosphere by lowered sea level), any upward bubble flux at the
381 sediment surface is assumed 100% released to the atmosphere. The
382 model neglects methane oxidation in soils, as well as many other
383 terrestrial processes such as thaw bulbs beneath bodies of water [*Walter*
384 *et al.*, 2006], and the seasonal cycle of melting and thawing in the
385 surface active layer. In short, the methane fluxes to the atmosphere
386 computed from the model runs are crude, and underlain by a sedimentary
387 methane cycle with large uncertainties, intended to capture the main
388 sensitivities to various processes rather than to provide strong
389 quantitative constraint to the fluxes in the real world.

390 **2.6 Comparison with Previous Models**

391 The dynamics of the permafrost layer, and its present state, have been
392 extensively modeled within detailed maps of the crust and sediment
393 structure [Gavrilov *et al.*, 2003; Nicolovsky and Shakhova, 2010; Nicolovsky *et*
394 *al.*, 2012; Romanovskii and Hubberten, 2001; Romanovskii *et al.*, 2005].
395 The crust underlying the continental shelf area has been alternately rising
396 and subsiding in blocks called horsts and grabens [Nicolovsky *et al.*, 2012].
397 The sediment cover on the grabens is much thicker than it is in the
398 horsts. SpongeBOB, an idealized two-dimensional model, does not
399 address this complexity, but the thickness of the sediment cover on the
400 shelf ranges from 5 – 10 kilometers, reminiscent of the grabens
401 (subsiding blocks). A thin sediment column would not reach the
402 temperature required for thermogenic methane production. The rates of
403 thermogenic methane production are not predicted or constrained by the
404 model, because of the different depositional histories of the sediment
405 columns. However, we can gauge the sensitivity of the methane cycle in
406 the near-surface sediments to thermogenic methane production by
407 scaling the model-predicted rate (by factors of 10 and 100).

408 Methane hydrate modeling has been done in the Arctic applied to the
409 Siberian continental slope [Reagan, 2008; Reagan and Moridis, 2009;
410 Reagan *et al.*, 2011], but only one calculation has been done in the
411 context of permafrost formation [Romanovskii *et al.*, 2005], as found on
412 the shelf. Romanovski [2005] modeled the extent of the methane
413 hydrate stability zone through glacial cycles, but based the calculations
414 on marine salinity values when calculating the stability of hydrate, while I
415 argue that in sub-freezing conditions (in the permafrost zone) the only
416 water available for hydrate formation will be in a saline brine that would
417 be in equilibrium with ice at the local temperature. This formulation
418 restricts hydrate stability from the permafrost zone to greater depth
419 below the sea floor than predicted by Romanovski [2005]. In the
420 Mackenzie Delta, hydrate was detected in a core drilled into onshore
421 permafrost soils [Dallimore and Collett, 1995], but only at depths greater
422 than 300 meters, near the base of the permafrost zone.

423 **3. Results**

424 **3.1 Initial Spinup**

425 The point of the spinup phase is to generate an initial condition for the
426 glacial cycle simulations. The more usual approach in modeling hydrates

427 is to start with an ad-hoc initial condition [Reagan, 2008; Reagan and
428 Mordis, 2009; Reagan et al., 2011]. For SpongeBOB the model state at
429 any time is the result of the time-history of sedimentation, which is driven
430 by the time-evolving depth of the sea floor, and interacting with isostatic
431 adjustment of the crust. The simplest way to generate an initial condition
432 in the model without a startup transient is to spin the model up from
433 bedrock at low resolution. Because of the over-simplicity of the tectonic,
434 sea level, and sedimentation forcing of the spinup phase, its POC
435 concentrations and methane production rates do not constrain those of
436 the real Siberian shelf. The sensitivity of the glacial methane cycles to
437 methane production rates will be evaluated by scaling the model
438 methanogenesis rates from the spinup result. The model setting was
439 grown for 62 million years of model time. The initial spinup used a
440 relatively coarse resolution as shown in Figure 2a.

441 For the glacial / interglacial experiments, the initial condition was
442 interpolated to a higher resolution grid in the vertical, as shown in Figure
443 2b. Particulate organic carbon (POC) concentrations are highest just off
444 the shelf break (Figure 3), because this is where most of the sediment is
445 deposited, and because the sedimentary material is richest in POC in
446 shallow ocean water depths [Archer et al., 2012]. The unchanging sea
447 level in the spinup period kept the sediment surface from outcropping,
448 resulting in nearly uniform marine salinity throughout the model domain
449 (Figure 4a). Methane concentration (Figure 5a) closely mirrors the
450 solubility of dissolved methane, resulting in near saturation
451 concentrations through most of the model domain (Figure 5b). As in the
452 previous model simulations [Archer et al., 2012], the imposition of
453 permeable channels has a strong effect on the chemistry of the
454 permeable grid cells (Figure 5d), although the impact on the integrated
455 model behavior, such as the methane flux to the atmosphere, was small in
456 these simulations.

457 **3.2 Impact of Freshwater Hydrology**

458 When sea level drops such that the surface of the sediment column
459 outcrops to the atmosphere, the pore fluid becomes subject to the
460 pressure head driving it seaward, and to fresh water recharge from
461 precipitation. The pressure head forcing and the buoyancy of the
462 sediment fluid column combine to create a mechanism to excavate
463 salinity from the upper sediment column. Initially after sea level fall, there
464 is a pressure head gradient extending throughout the sediment column,

465 provoking lateral flow at all depths. As the pore fluid at the surface is
466 replaced by fresh runoff, the lighter density of that fluid tends to diminish
467 the pressure head gradient in the deeper sediment column. The deeper
468 pressure gradient and flow approach zero as the fresh water lens in the
469 outcropping region approaches an isostatic equilibrium condition known as
470 the Ghyben-Herzberg relation [Moore *et al.*, 2011], in which each meter
471 elevation of the water table is compensated for by about 40 meters of
472 fresh water below sea level, determined by the difference in densities of
473 fresh and salt water.

474 To create this condition within the model, two simulations are presented
475 in which sea level was decreased by 30 and 120 meters, respectively, and
476 held there for millions of years (Figure 6). The 30-meter drop experiment
477 produced land outcrop in about 1/4 of the model domain, with the
478 predicted equilibrium Ghyben-Herzberg halocline reaching about 1200
479 meters maximum depth. The model salinity relaxes into close agreement
480 with the predicted halocline, lending support to the model formulation for
481 density, pressure head, and fluid flow. As time progresses further, the
482 outcropping land surface subsides (there is no land deposition in this
483 scenario), until it drops below the new lowered sea level value after about
484 2.5 Myr.

485 Variants of this experiment were done with differing values of the lateral
486 distance to drainage canyons in the model, which provide a pathway for
487 fluid loss in sediments above sea level. When a hypothetical canyon is
488 located 10 km from the SpongeBOB slab, the model salinity approaches
489 equilibrium on an e-folding time scale of about 400 kyr (Figure 7). When
490 the canyon is 100 km distant or nonexistent, the equilibration time scale
491 is about 600 kyr. Based on the idea that canyons of order 100 km long
492 should be about 100 km apart, the Base simulation in this paper assumes
493 canyon spacing of 100 km.

494 When sea level is lowered by 120 m, the sequence of events is similar,
495 except that the pressure head is so high that to satisfy the Ghyben-
496 Herzberg relation would require fresh pore waters at many kilometers
497 depth, even deeper than bedrock on the “continental” side of the model
498 domain. Because of the low permeability of the deepest sediment
499 column, the freshwater pumping groundwater mechanism is unable to
500 reach these deepest pore waters, which therefore remain salty. The time
501 scale for establishing a significant freshening of the upper kilometer of
502 the sediment column is still on the order of 100-500 kyr, and the

503 subsequent subsidence time of the sediment column in the model, until it
504 drops below the new lowered sea level, takes about 10 Myr. In both
505 cases, subsidence of the exposed sediment column prevents the
506 sediment surface in the model from remaining above sea level indefinitely
507 (without land deposition).

508 The sequence of events leaves behind a fresh water lens below sea level
509 that persists in the model for millions of years (Figure 6). Groundwater
510 flow, driven by the pressure head, provides an advective means of
511 pumping fresh water into the subsurface sediment column that has no
512 counterpart for salty ocean water. The model lacks the mechanism of salt
513 fingering, which can enhance the diffusion of salt from above into a fresh
514 water aquifer [Kooi *et al.*, 2000]. However, higher-resolution models of
515 smaller domains that accounted for salt fingering also show a time
516 asymmetry, with faster fresh water invasion on sea level drop than salt
517 invasion on sea level rise [Lu and Werner, 2013; Watson *et al.*, 2010].
518 As the size of the domain increases with increasing sea level change,
519 advective processes such as hydrological flow should become even more
520 dominant over diffusive processes such as salt fingering. The recent
521 discovery of vast freshwater aquifers on global continental shelves [Post
522 *et al.*, 2013], persisting since the time of lowered sea level 20,000 years
523 ago, and the lower-than-marine salinities of the pore waters measured in
524 submerged surface Arctic sediments (summarized by [Nicolisky *et al.*,
525 2012]) are also consistent with the existence of a fresh-water
526 hydrological pump which has a significant impact on sediment column
527 salinities. The hydrological pumping generates a low-methane plume that
528 also persists for millions of years in the model (Figure 8). Two states,
529 called “prefreshened” and “pure marine”, serve as end-member initial
530 conditions for glacial / interglacial simulations (Figure 4b), to evaluate the
531 sensitivity of the model glacial cycles to the initial salinity of the sediment
532 column.

533 **3.3 Glacial Cycles**

534 **3.3.1 Setup and Forcing**

535 Beginning from an entirely submerged initial condition, the model is
536 subjected to 100-kyr sawtooth cycles of sea level ranging between -120
537 to +20 meters from the initial sea level (starting at -120 for
538 prefreshened, 0 for pure marine) (Figure 9a).

539 The model scenarios and sensitivity studies are summarized in [Table 1](#).
540 The simplest scenario (SL) varies the sea level while keeping the air and
541 water temperatures time-invariant. The sea-level air temperature is
542 maintained at 0 °C. This simulation is nearly permafrost-free, with a small
543 exception where the altitude of the sediment surface is much higher than
544 sea level (due to the lapse rate in the atmosphere). There is no
545 deposition of sediment above sea level in this simulation. Permafrost
546 formation is added in simulation GL, in which the air temperature ramps
547 down to -16 °C at sea level, linearly with the glacial sea level fall ([Figure
548 9b](#)). In the ocean, shelf waters are always -1.8 °C, but an interglacial
549 subsurface temperature maximum of 1 °C at 200 meters decreases to
550 -1.8 °C during glacial times. Deposition of organic-rich sediments when
551 the surface is exposed to the atmosphere (Yedoma: represented as
552 accumulation of 10 meters in 100 kyr, with 30% POC) is added in
553 scenarios SL+LD and GL+LD (LD for land deposition). The atmospheric
554 temperature impact of a global warming scenario (GW) is also shown in
555 [Figure 9b](#), beginning at 400 kyr, and compared with an extended-
556 interglacial control forcing (Ctl). The potential impact of geologic-time
557 scale sea level rise is added to the global warming scenario in simulation
558 GL+SL.

559 Other model sensitivity runs used varying values of the thermogenic and
560 biogenic methane production rates, the geothermal temperature gradient.
561 Several altered-physics runs were done, one adding vertical permeable
562 channels, one disabling horizontal flow, and several to evaluate the impact
563 of ice formation on methane hydrate stability.

564 **3.3.2 Salinity and Ice**

565 In the “prefreshened” initial condition (Fr), millions of years have elapsed
566 since the previous exposure of the sediment to hydrological forcing, but a
567 core of fresh water remains. Salinities near the sediment surface have
568 grown saltier due to diffusive contact with seawater ([Figure 10, left](#)). A
569 fully marine initial condition (Mar) ([Figure 10, right](#)) was initialized from
570 the unfreshened case, in which sea level was held at a fixed value
571 throughout the 65 Myr spinup of the sediment column. The salinities are
572 nearly uniform in this case.

573 When the sediment surface is re-exposed to the atmosphere during an
574 interval of sea level, in the absence of ice formation (simulation SL), the

575 surface layer tends to freshen relatively quickly due to the hydrological
576 forcing, but a subsurface salinity maximum persists (Figure 10c and d).
577 However, if the air temperatures are cold enough to form ice (simulation
578 GL), surface salinities in the model increase to up to nearly 190 psu, in
579 both prefreshened and pure marine cases (Figure 10e and f). By the next
580 interglacial time (Figure 10g and h), ice near the sediment surface has
581 melted enough for near-surface pore waters to reach relatively low
582 salinities.

583

3.3.3 Pressure and Flow

584 The effect of the sea level and permafrost forcing on the pressures and
585 flow velocities are shown in Figure 11. On a spatial scale of the entire
586 model domain (Figure 11, left), the highest driving pressures are found at
587 the base of the sediment column, underneath the region of maximum
588 sediment accumulation (the depocenter just off the shelf break).
589 Changes in sea level drive large fluctuations in the pressure head
590 (contours) extending to bedrock. In the near-surface continental shelf
591 (Figure 11, right), the driving pressure variations are dominated by the
592 pressure head driven by sea level changes. The formation of permafrost
593 (GL, Figure 11 e and f) seals the upper sediment column to fluid flow.
594 When sea level rises again, in the model configuration including
595 permafrost, there is a strong pulse of downward flow following partial
596 melting of the permafrost (Figure 11 h). It is possible that this flow,
597 which lasts a few thousand years, is an artifact of the elastic model
598 configuration, in which the release of a load (by submergence of the
599 upper sediment column into the ocean) provokes the expansion of pore
600 spaces in the sediment. The anomalous flow, integrated over its duration,
601 could displace the pore fluid by about 40 meters, which is less than one
602 grid cell. The model configuration without the sealing effect of permafrost
603 (SL) does not show this pulse of invasive flow on sea level rise.

604

3.3.4 Methane Cycle

605 There are multiple ways in which the glacial cycles of sea level and air and
606 water temperature might impact the flux of methane to the atmosphere.
607 Submergence in the ocean is one modulating factor, because the
608 emerging bubbles dissolve in the ocean rather than reaching the
609 atmosphere. Another factor is the deposition of high-POC surface soils
610 during low sea level stands, and its exposure to degradation later when
611 the permafrost soils melt. A third factor is permafrost, impeding gas and

612 fluid flow and excluding dissolved methane and salt from ice formation.
613 The impacts of these processes are assessed by comparing the results
614 from model configurations with and without each process in question.

615 The impact of phase competition between ice and hydrate is shown in
616 **Figure 12**. In the Base scenario (**Figure 12a and c**) hydrate stability is
617 excluded from the permafrost zone as described above and in **Figure 1**.
618 Preventing ice from forming in an altered-physics simulation (+ No Ice)
619 decreases the fluid-phase salinity relative to the Base simulation, and
620 allows the methane hydrate stability zone to nearly reach the sea floor
621 (**Figure 12b and d**), during strongest glacial conditions. Another altered-
622 physics simulation was done in which ice is allowed to form, but not
623 affect the salinity as it drives methane hydrate stability (which was hard-
624 wired to marine salinity). Methane hydrate is still unstable in the
625 permafrost zone through most of the simulation (see movie files in
626 supplemental material), indicating that thermal interaction must also have
627 a strong impact on methane hydrate stability in the permafrost zone.

628 The evolution of the dissolved methane disequilibrium condition ($\text{CH}_4 /$
629 CH_4_{sat}) is shown in **Figure 13**. At the initiation of the glacial cycles,
630 methane is undersaturated in near-surface sediments on the continental
631 shelf, by diffusive contact with the methane-free ocean upper boundary
632 condition. In the prefreshened sediment column scenario (Fr), methane
633 concentrations in the depth range of 100-1000 meters are lower than in
634 the marine case (Mar, **Figure 13b**), due to the ventilation by the
635 hydrological pump (**Figure 13a**). Further freshening of the pore waters in
636 the ice-free case (SL+LD) tends to deplete methane in the upper
637 sediment column (**Figure 13c-e**), while methane exclusion from the
638 permafrost ice leads to supersaturation in simulation GL+LD (**Figure 13 f-**
639 **h**). The hydrate stability zone is somewhat expanded in the prefreshened
640 sediment column relative to the marine case (**Figure 13 g vs. h, heavy**
641 **black contour**).

642 **Figure 14** shows snapshots of various aspects of the shelf carbon cycle,
643 beginning from a prefreshened initial condition. Sections of POC
644 concentration in **Figure 14, left** show the accumulation of POC-rich
645 Yedoma deposits on land (**Figure 14 g and j**). The rate of methane
646 production in the model (**Figure 14, right**) depends on temperature and
647 organic carbon age, but it is also attenuated by permafrost formation in
648 the model, scaling to zero in the completely frozen case. Methanogenesis
649 rates are near zero in the permafrost zone during glacial time (**Figure**

650 14h), but partially recover during interglacial time (Figure 14k) even
651 though permafrost is still present.

652 A zone of methane hydrate stability exists below the permafrost zone
653 when permafrost is present, and some methane hydrate accumulates in
654 that zone. The highest pore-fraction values are found near the
655 continental slope, where the shelf stability field outcrops within the slope
656 depocenter. Dissolved methane concentrations exceed saturation within
657 the stability zone in the model (Figure 13), but the accumulation of
658 methane hydrate (Figure 14, right) is limited by the rate of methane
659 production.

660 Time series plots of the inventory of methane as hydrate on the shelf are
661 shown in Figure 15. The integration cuts off at $x=560$ km to exclude the
662 sediment depocenter on the continental slope. Hydrate inventories reach
663 maximum values during deglaciations. There is more hydrate when the
664 pore water is fresher, and there would be more if ice were excluded from
665 forming (Figure 15a). The hydrate inventory is much more sensitive to
666 thermogenic methane production, deep in the sediment column, than
667 Yedoma deposition (Figure 15b). The impact of the geothermal heat flux
668 is to change the depth of the bottom of the hydrate stability zone
669 (Figure 12 e and f), but the impact is small on the hydrate inventory,
670 unless the temperature gradient is so low that hydrate persists through
671 the entire glacial cycle (Figure 15c). The hydrate forms from the
672 dissolved methane pool, which exceeds 1000 Gton C in shelf porewaters
673 of the model.

674 The impact of the glacial cycles on the methane pathway to the
675 atmosphere in the model is shown in Figure 16. When sea level is high,
676 the efficiency of bubble transport across the sediment-water interface
677 reaching the atmosphere ranges from about 75% near the coast to about
678 10% at the shelf break (Figure 16a). Most of the methane flux from the
679 sediment is located just off the shelf break (Figure 16e), where the
680 escape efficiency is low, so not much methane makes it to the
681 atmosphere during the interglacial. During glacial times, the sediment
682 column is exposed to the atmosphere, and the escape efficiency in the
683 model is 100% (Figure 16b). Permafrost inhibits the terrestrial methane
684 flux (Figure 16i) relative to the case without permafrost (Figure 16f).
685 During some deglaciations, the release of pent-up gas by permafrost
686 degradation leads to a spike of excess methane flux to the atmosphere
687 (Figure 16j-k relative to 16g-h).

688 Time series plots of the major fluxes of the methane cycle on the
689 continental margin are shown in [Figure 17](#). The methanogenesis rates in
690 the model output are in units of moles per meter of coastline, since it is a
691 2-D model. We scale this up to the Siberian continental margin by
692 assuming a width of 1,000 km. The area of the shelf is then $5 \cdot 10^{11} \text{ m}^2$,
693 roughly comparable to the real shelf area of 460,000 km² [*Stein and Fahl,*
694 2000]. The biological rate of methane production on the continental shelf
695 evolves through time in [Figure 17b](#). Yedoma deposition (case SL+LD)
696 tends to slowly increase the total shelf respiration rate in the model,
697 relative to a case with no land deposition (case SL). The formation of
698 permafrost, during glacial periods of case GL+LD, attenuates
699 methaneogenesis by inhibiting biological activity in the frozen soil.

700 The solid regions in [Figure 17 c-h](#) are cumulative methane sinks for six
701 different model scenarios, plotted underneath red lines showing biogenic
702 methane production. In time average, where sinks balance sources, the
703 colored areas should fill up the region below the red line.

704 Trapping of methane by impermeable permafrost leads to a spike of
705 methane fluxes at the ends of deglaciations in simulations with
706 permafrost ([Figure 17 c and e](#)). The spikes happen as sea level
707 approaches its highest extent, stifling the offshore groundwater flow by
708 decreasing the pressure head, but early in the interglacial time while
709 permafrost is the most intact. The spikes are stronger for the first glacial
710 cycles than the last, apparently due to long-term adjustment of the
711 methane cycle on the shelf (a growing together of the production rate
712 (red lines in [Figure 17 c-f](#)) and the various methane sinks (colored areas).

713 Permafrost formation blocks methane emission during times of low sea
714 level. This can be seen in the collapse of the blue regions in [Figure 17 c](#)
715 [vs. d and e vs. f](#) during times of low sea level. Blocking horizontal flow
716 disrupts offshore flow, the only significant methane sink on the shelf
717 during glacial periods ([Figure 17h](#)), resulting in somewhat higher deglacial
718 spikes of methane emission than predicted by the models including
719 transport. There is no direct link between ice fraction and methane
720 oxidation in the model, which is driven only by coexisting concentrations
721 of sulfate and methane, but the rate of methane oxidation also drops to
722 negligible during glacial times in the simulations with permafrost (grey in
723 [Figure 17 c and e](#)). The absolute rates of methane loss differ between
724 the Prefreshened vs. Marine initial conditions, but this is in part due to
725 differences in the width of the continental shelf between the two

726 simulations. The patterns of the methane cycle are very similar, however,
727 between the two cases, and also not much affected by the imposition of
728 permeable vertical channels (Figure 17g).

729 atmospheric fluxes

730 Fluxes of methane to the atmosphere are shown in Figure 18. In the
731 absence of permafrost (Figure 18 a and b), or assuming that bubble
732 migration is blocked only if the ice fraction exceeds 90%, a condition
733 rarely attained in the model (Figure 18e), the highest methane fluxes to
734 the atmosphere are found during glacial (cold) times, rather than warm
735 interglacials. This is due to dissolution of methane gas into the ocean
736 when the sediment column is submerged. When permafrost blocks
737 methane gas fluxes in the sediment column, the highest atmospheric
738 fluxes are generally found during the time of early sea level fall, when
739 unfrozen sediment is exposed to the atmosphere before it has a chance
740 to freeze. The timing of the variations in atmospheric flux through the
741 glacial cycles is very sensitive to the critical ice fraction for blocking gas
742 transport (Figure 18e).

743 The impacts of the pore water salt inventory are most apparent during
744 the time of sea level fall, with permafrost formation (red lines). The
745 saltier sediment column takes about 20 kyr to choke off the methane flux
746 to the atmosphere (Figure 18a), while the pre-freshened sediment
747 column stops the methane flux more abruptly, in just a few thousand
748 years (Figure 18b).

749 Atmospheric emissions also scale with methane production rates,
750 generally maintaining the temporal patterns of emission as set by
751 permafrost and submergence in the ocean.

752 **3.4 Anthropogenic Global Warming**

758 The global warming (GW) scenario begins from a high sea-level interglacial
759 state, and raising the temperature following the climate impact of the
760 “spike and long tail” time distribution of a slug of new CO₂ added to the

761 atmosphere [Archer et al., 2009] (Figure 8). There is a stage of fast
762 atmospheric drawdown as CO₂ invades the ocean, but once the ocean,
763 atmosphere, and land surface reach equilibrium (after a few hundred
764 years), the CO₂ content of the entire biosphere begins to relax toward an
765 initial “natural” value, on time scales of hundreds of thousands of years,
766 by weathering reactions with carbonate and siliceous solid rocks. The net
767 result is a CO₂ drawdown that can be expressed as the sum of several
768 exponential functions in time, with time scales ranging from 10² – 10⁶
769 years.

770 Changes in water column temperature are assumed equal to those of the
771 atmosphere, following paleoceanographic reconstructions [Martin et al.,
772 2002] and long-term coupled ocean / atmosphere circulation model
773 experiments [Stouffer and Manabe, 2003]. The GW scenario imposes this
774 temperature change on the water column, relaxing toward equilibrium
775 with the atmospheric CO₂ trajectory with a time constant of 100 years.

776 The effect of sea level rise is added to create a second global warming
777 scenario GW+SL. On time scales of thousands of years the sea level
778 response to changing global temperature is much stronger than the sea
779 level response over the coming century, as prominently forecast by the
780 IPCC. Reconstruction of sea level and global temperature covariation in
781 the geologic past (glacial time to Eocene hothouse) reveals a covariation
782 of 10-20 meters per °C [Archer and Brovkin, 2008]. The global warming
783 with sea level scenario assumes an equilibrium sea level response of 15
784 meters / °C, which it relaxes toward with a time constant of 1000 years.

785 The atmospheric methane fluxes, shown in Figure 19, increase in the
786 global warming (GW) model run, as they also do in the control (Ctl)
787 simulation, which is essentially an extended but unwarmed interglacial
788 period. The permafrost melts on a time scale of about 10,000 years for
789 the GW simulation, and about 50,000 for the Ctl. The rates of methane
790 production, and flux to the atmosphere, both increase with the loss of the
791 permafrost, if there is no change in sea level. However, the new methane
792 flux comes not as a sudden burst, but rather as a slow transition toward a
793 new, higher, chronic release rate. When sea level is also changed
794 (GW+SL), bubbles dissolve in the water column, which more than
795 counteracts the increase in methane flux due to the extended interglacial
796 (Ctl) or warming (GW) scenarios.

797 **3.5 Summary of Model Sensitivity Studies**

798 **Sediment Porewater Salinity.** Ice freezes until the salinity of the
799 residual brine brings about a freezing point depression equal to the in situ
800 temperature. A saltier initial sediment column will reach this condition
801 with a lower ice fraction, its melting is accelerated, and its hydrate
802 inventory is lower (Figure 18). The equilibrium salinity in the permafrost
803 zone is not affected by the salt inventory of the column, only the relative
804 volumes of the solid and fluid phases.

805 **Methane Production Rates.** The atmospheric flux increases with
806 increases in either shallow, biogenic methane production, driven by
807 deposition of Yedoma, and thermogenic methane production in the deep
808 sediment column (Figure 19). Biogenic methane is produced too shallow
809 in the sediment column to impact the inventory of methane hydrate
810 (Figure 15). The timing through the glacial cycles of atmospheric
811 methane emissions from these scenarios parallel each other, because they
812 are controlled in common by the transport-blocking effects of permafrost
813 and sediment submergence in the ocean.

814 **Geothermal Temperature Gradient.** When the heat flux is higher, the
815 temperature gradient is steeper, pivoting about the sediment surface
816 temperature, which is set by the ocean. The base of the methane
817 hydrate stability boundary gets shallower, while the top remains at about
818 the same depth, resulting in a thinning of the stability zone (Figure 12).
819 The hydrate inventory through the glacial cycles however is not much
820 affected, unless the heat flux gets small enough for hydrate to persist
821 through the glaciations (Figure 15).

822 **Ice vs. hydrate thermodynamic competition.** When ice is included
823 as a competing phase, it excludes methane hydrate from the low-
824 pressure, very cold permafrost zone. The hydrate stability zone thins
825 (from above and below in the model: Figure 12), and the hydrate
826 inventory decreases (Figure 15). When ice formation is disallowed, the
827 hydrate stability zone approaches the sediment surface during coldest
828 glacial time, but by the time of an interglacial-based global warming
829 climate perturbation, the stability zone boundary has retreated to several
830 hundred meters below the sea floor, precluding a sudden hydrate
831 dissolution response to a suddenly warming ocean.

832 **Permafrost inhibition of gas migration.** When the ice fraction of
833 the model exceeds a critical threshold, gas migration is blocked.
834 Changing the value of this threshold has a strong impact on the rates of
835 methane emission during glacial versus interglacial times. This process is
836 therefore a high priority for future model refinement.

837 **Vertical flow heterogeneity.** The chemistry of continental margin
838 sediments in this model [Archer *et al.*, 2012] showed a strong sensitivity
839 to flow heterogeneity, achieved by increasing the vertical permeability of
840 every fifth grid cell. In the configuration presented here, the impact of
841 the channels is much smaller. The dynamics of this simulation are
842 thermally driven, rather than by sediment deposition driving fluid flow in
843 the continental margin case. Atmospheric methane fluxes are spikier when
844 the channels are included, but the mean rate is not much changed.

845 **Ground water flow.** Groundwater flow carries enough methane to be a
846 significant sink during times of low sea level. However, disabling that flow
847 has only subtle impacts on the other aspects of the methane cycle on the
848 shelf. Spikes of methane emission during late deglaciation get somewhat
849 more intense.

850 **4. Implications of the Model Results for the Real Siberian Continental** 851 **Margin**

851 This is the first simulation of the full methane cycle on the Siberian
852 continental margin, or any other location with embedded permafrost soils,
853 including hydrate formation and transient fluxes. It is internally
854 consistent, linking processes from the ocean, the sea floor, and the deep
855 Earth, within constraints of sediment accommodation and conservation of
856 carbon, through geologic time. As such it has some lessons to teach us
857 about the real Siberian continental margin. However, many of the model
858 variables are not well known, such as the methaneogenesis rates or soil
859 permeabilities, meaning that in some aspects the model results are not a
860 strong constraint on reality.

861 The absolute values of the methane inventories in the system, as hydrate
862 and bubbles, are not well constrained theoretically. The rate of methane
863 production in shallow sediments is not well characterized. In reality there
864 might be some flux of methane from the crust, but this is not included in
865 the simulation. The transport of bubbles through the sediment column is
866 mechanistically poorly understood, therefore not well represented in the
867 code, which affects the inventories of bubbles in the sediment.

868 Ultimately the bubble concentration in the model reaches a rough steady
869 state where production of methane gas balances its escape through the
870 sediment column, but the steady state value from the model could be
871 wrong. The model lacks faults, permeable layers, or the ability to “blow
872 out”, producing the sedimentary wipe-out zones observed seismically in
873 the subsurface [Riedel *et al.*, 2002], and the pockmarks at the sediment
874 surface [Hill *et al.*, 2004]. On land, the model lacks seasonal melting of
875 surface permafrost (to form the active layer) and the thaw bulbs
876 underneath lakes and rivers. In the ocean, the intensity of water column
877 dissolution of rising bubbles depends on the bubble sizes, which depend
878 on the gas emission rate, ultimately driven by details of gas transport in
879 the sediment, which are neglected in the model.

880 These uncertainties all affect the flux of methane to the atmosphere,
881 which is therefore not well constrained by the model. However, the
882 model is consistent with observations [Kort *et al.*, 2012], that the total
883 atmospheric methane flux from the Siberian margin is a small fraction of
884 the global flux of methane to the atmosphere, and thus represents only a
885 minor climate forcing. The model would have to be pushed very hard (as
886 would the measurements) to fundamentally change this conclusion.

887 The model bubble flux to the atmosphere in the base case in analog
888 present-day conditions is only 0.02 Tg CH₄ per year, which is an order of
889 magnitude lower than an estimate of the total methane emission rate
890 from aircraft [Kort *et al.*, 2012] of 0.3 Tg CH₄ / yr. However, the model
891 only accounts (crudely) for the bubble flux to the atmosphere, and does
892 not include gas exchange evasion of methane from the water column,
893 which could be significant. Concentrations of methane in the water
894 column of 50 nM are common [Shakhova *et al.*, 2010a], which, if they
895 were unimpeded by sea ice, could lead to a flux from the region of 0.4 Tg
896 CH₄ / yr (assuming a typical gas exchange piston velocity of 3 m/day).
897 Methane fluxes into the water column range up to 0.4 Tg CH₄ / yr during
898 times of relatively high sea level. Once released to the water column, the
899 fate of a methane molecule will depend on its lifetime with respect to
900 oxidation, which could be up to a year in the open water column
901 [Valentine *et al.*, 2001], versus its lifetime with respect to gas exchange,
902 which for ice-unimpeded conditions would be just a few months for a 50-
903 meter deep water column. Thus the methane in bubbles dissolving in the
904 water column has some chance of making it to the atmosphere anyway,
905 depending on stratification in the water column and the extent of ice, and

906 the gas exchange flux has the potential to be significant in the regional
907 total flux.

908 Shakhova et al [2010b] proposed that 50 Gton C as methane could erupt
909 from the Arctic on a time scale of a few years. As has been
910 acknowledged, the model provides poor constraint on the standing stock
911 of bubbles or methane hydrate in the sediment column, and neglects
912 many of the mechanisms that could come into play in transporting
913 methane quickly to the atmosphere, such as faults, channels, and
914 blowouts of the sediment column. However, one seemingly robust model
915 result is the thermodynamic exclusion of methane hydrate from the
916 permafrost zone, by competition for water between ice and hydrate.
917 Thermodynamics does not control everything, especially at low
918 temperature, but kinetic inhibitions are more often found for nucleation
919 steps rather than decomposition. To find an accumulation of
920 “metastable” hydrate would also require some sort of transport
921 mechanism of hydrate into the region where it is unstable, which does not
922 exist. There is no reason to imagine that hydrate could form in situ when
923 thermodynamic conditions are wrong for it. A kinetic inhibition of water-
924 ice formation would work, but ice does not tend to super-cool in a dirty,
925 nucleation-site-rich environment like sediments. Therefore it seems as
926 though methane hydrate should not be expected in sediment depths
927 shallower than about 300 meters. A warming perturbation at the sea
928 floor today will not reach this depth for hundreds or thousands of years.

929 Could an abrupt methane release arise from release of trapped bubbles
930 from melting ice? The model actually does produce a glacial cycle in
931 bubble inventory, with changes exceeding 50 Gton over a cycle,
932 apparently driven by methane exclusion from ice formation (Figure 15).
933 But the model does not deliver an abrupt release in response to
934 anthropogenic warming for any of its sensitivity studies (Figure 18).
935 Permafrost melting driven by deglacial sea level rise has already been
936 going on for thousands of years. In this span of time a temperature
937 anomaly has diffused quite deep into the sediment column. In order for
938 the abrupt temperature anomaly of global warming to further accelerate
939 the ongoing ice or hydrate melting, it will have to diffuse down in the
940 sediment column to where the ice still is. We would get a faster initial
941 response to global warming if the transition from glacial to global warming
942 sediment surface temperatures hadn’t mostly happened thousands of
943 years ago.

944 In the real world, geological features such as faults and permeable layers
945 dominate the methane cycle in the sediments. A continuum model such
946 as this one predicts a smooth methane release response to a warming,
947 growing in on some e-folding time-scale. A world dominated by features
948 that each represent a small fraction of the total methane reservoir will
949 release methane more episodically, but the statistical distribution of the
950 response in time should still show the e-folding time scale of the
951 underlying driving mechanism, the diffusion of heat into the sediment
952 column. The way to deliver 50 Gton of methane to the atmosphere is for
953 it all to be released from a single geologic feature pent up by ice. But 50
954 Gton of C represents a large fraction of all the traditional natural gas
955 deposits on Earth (about 100 Gton C). The place to look for such a large
956 unstable gas reservoir is in the field, not in this model, but until such a
957 thing is found it remains conjecture.

958 Another probably robust feature of the model is the dominant impact of
959 sea level inundation of the sediment column on the atmospheric methane
960 flux. The methane flux is highest during cold times, because sea level is
961 low, rather than providing a positive climate feedback of releasing
962 methane during warm (high sea level) intervals. There is a warming
963 positive feedback in the simulated future from climate warming, but it is
964 much smaller than the impact of sea level changes in the past. The
965 potential for future sea level change is much higher for the deep future,
966 thousands of years from now, than the forecast for the year 2100,
967 because it takes longer than a century for ice sheets to respond to
968 changes in climate. The model finds that for the future, if sea level
969 changes by tens of meters, as guided by paleoclimate reconstructions
970 [Archer and Brovkin, 2008], the impact of sea level rise could overwhelm
971 the impact of warming. The dominance of sea level over temperature in
972 the model of this area is due to dissolution of methane in the water
973 column, rather than a pressure effect on hydrate stability, which is
974 generally a weaker driver than ocean temperature in deeper-water
975 settings [Mienert et al., 2005].

976 **5. Bibliography**

977 Archer, D., and V. Brovkin, The millennial lifetime of fossil fuel CO₂,
978 *Climatic Change*, 90, 283-297, 2008.

- 979 Archer, D.E., B.A. Buffett, and P.C. McGuire, A two-dimensional model of
980 the passive coastal margin deep sedimentary carbon and methane cycles,
981 *Biogeosciences*, 9, 1-20, 2012.
- 982 Archer, D.E., M. Eby, V. Brovkin, A.J. Ridgwell, L. Cao, U. Mikolajewicz, K.
983 Caldeira, H. Matsueda, G. Munhoven, A. Montenegro, and K. Tokos,
984 Atmospheric lifetime of fossil fuel carbon dioxide, *Ann. Reviews Earth*
985 *Planet Sci.*, 37, 117-34, 2009.
- 986 Cramer, B., and D. Franke, Indications for an active petroleum system in
987 the Laptev Sea, NE Siberia, *Journal of Petroleum Geology*, 28 (4), 369-
988 383, 2005.
- 989 Dallimore, S.R., and T.S. Collett, Intrapermafrost Gas Hydrates from a
990 Deep Core-Hole in the Mackenzie Delta, Northwest-Territories, Canada,
991 *Geology*, 23 (6), 527-530, 1995.
- 992 Dutta, K., E.A.G. Schuur, J.C. Neff, and S.A. Zimov, Potential carbon
993 release from permafrost soils of Northeastern Siberia, *Global Change*
994 *Biology*, 12 (12), 2336-2351, 2006.
- 995 Gavrilov, A.V., X.N. Romanovskii, V.E. Romanovsky, H.W. Hubberten, and
996 V.E. Tumskoy, Reconstruction of ice complex remnants on the eastern
997 Siberian Arctic Shelf, *Permafrost and Periglacial Processes*, 14 (2), 187-
998 198, 2003.
- 999 Gentz, T., E. Damm, J.S. von Deimling, S. Mau, D.F. McGinnis, and M.
1000 Schluter, A water column study of methane around gas flares located at
1001 the West Spitsbergen continental margin, *Continental Shelf Research*, 72,
1002 107-118, 2014.
- 1003 Gilichinsky, D., E. Rivkina, C. Bakermans, V. Shcherbakova, L. Petrovskaya,
1004 S. Ozerskaya, N. Ivanushkina, G. Kochkina, K. Laurinavichuis, S.
1005 Pecheritsina, R. Fattakhova, and J.M. Tiedje, Biodiversity of cryopegs in
1006 permafrost, *Fems Microbiology Ecology*, 53 (1), 117-128, 2005.
- 1007 Hill, J.C., N.W. Driscoll, J.K. Weissel, and J.A. Goff, Large-scale elongated
1008 gas blowouts along the US Atlantic margin, *Journal of Geophysical*
1009 *Research-Solid Earth*, 109 (B9), 2004.
- 1010 Hunt, J.M., *Petroleum Geochemistry and Geology*, 743 pp., Freeman, New
1011 York, 1995.

- 1012 Khvorostyanov, D.V., P. Ciais, G. Krinner, S.A. Zimov, C. Corradi, and G.
1013 Guggenberger, Vulnerability of permafrost carbon to global warming. Part
1014 II: sensitivity of permafrost carbon stock to global warming, *Tellus Series*
1015 *B-Chemical and Physical Meteorology*, 60 (2), 265-275, 2008a.
- 1016 Khvorostyanov, D.V., G. Krinner, P. Ciais, M. Heimann, and S.A. Zimov,
1017 Vulnerability of permafrost carbon to global warming. Part I: model
1018 description and role of heat generated by organic matter decomposition,
1019 *Tellus Series B-Chemical and Physical Meteorology*, 60 (2), 250-264,
1020 2008b.
- 1021 Kooi, H., J. Groen, and A. Leijnse, Modes of seawater intrusion during
1022 transgressions, *Water Resources Res.*, 36 (12), 3581-3589, 2000.
- 1023 Kort, E.A., S.C. Wofsy, B.C. Daube, M. Diao, J.W. Elkins, R.S. Gao, E.J.
1024 Hints, D.F. Hurst, R. Jimenez, F.L. Moore, J.R. Spackman, and M.A.
1025 Zondlo, Atmospheric observations of Arctic Ocean methane emissions up
1026 to 82 degrees north, *Nature Geoscience*, 5 (5), 318-321, 2012.
- 1027 Lu, C., and A.D. Werner, Timescales of seawater intrusion and retreat,
1028 *Advances in Water Resources*, 59, 39-51, 2013.
- 1029 Martin, P.A., D.W. Lea, Y. Rosenthal, N.J. Shackleton, M. Sarnthein, and T.
1030 Papenfuss, Quaternary deep sea temperature histories derived from
1031 benthic foraminiferal Mg/Ca, *Earth and Planetary Science Letters*, 198 (1-
1032 2), 193-209, 2002.
- 1033 Middelburg, J.J., K. Soetaert, and P.M.J. Herman, Empirical relations for
1034 use in global diagenetic models, *Deep-Sea Research I*, 44, 327-344,
1035 1997.
- 1036 Mienert, J., M. Vanneste, S. Bunz, K. Andreassen, H. Haflidason, and H.P.
1037 Sejrup, Ocean warming and gas hydrate stability on the mid-Norwegian
1038 margin at the Storegga Slide, *Marine and Petroleum Geology*, 22 (1-2),
1039 233-244, 2005.
- 1040 Moore, W.S., C.A. Carlson, and S.J. Giovannoni, The Effect of Submarine
1041 Groundwater Discharge on the Ocean, *Annual Review of Marine Science*, 2,
1042 59-88, 2011.

- 1043 Nicolsky, D., and N. Shakhova, Modeling sub-sea permafrost in the East
1044 Siberian Arctic Shelf: the Dmitry Laptev Strait, *Environmental Research*
1045 *Letters*, 5 (1), 2010.
- 1046 Nicolsky, D.J., V.E. Romanovsky, N.N. Romanovskii, A.L. Kholodov, N.E.
1047 Shakhova, and I.P. Semiletov, Modeling sub-sea permafrost in the East
1048 Siberian Arctic Shelf: The Laptev Sea region, *Journal of Geophysical*
1049 *Research-Earth Surface*, 117, 2012.
- 1050 Portnov, A., A.J. Smith, J. Mienert, G. Cherkashov, P. Rekant, P. Semenov,
1051 P. Serov, and B. Vanshtein, Offshore permafrost decay and massive
1052 seabed methane escape in water depths > 20m at the South Kara Sea
1053 shelf, *Geophysical Research Letters*, 40 (15), 3962-3967, 2013.
- 1054 Post, V.E.A., J. Groen, H. Kooi, M. Person, S.M. Ge, and W.M. Edmunds,
1055 Offshore fresh groundwater reserves as a global phenomenon, *Nature*,
1056 504 (7478), 71-78, 2013.
- 1057 Reagan, M.T., Dynamic response of oceanic hydrate deposits to ocean
1058 temperature change, *Journal of Geophysical Research-Oceans*, 113 (C12),
1059 2008.
- 1060 Reagan, M.T., and G.J. Moridis, Large-scale simulation of methane hydrate
1061 dissociation along the West Spitsbergen Margin, *Geophysical Research*
1062 *Letters*, 36, 2009.
- 1063 Reagan, M.T., G.J. Moridis, S.M. Elliott, and M. Maltrud, Contribution of
1064 oceanic gas hydrate dissociation to the formation of Arctic Ocean
1065 methane plumes, *Journal of Geophysical Research-Oceans*, 116, 2011.
- 1066 Riedel, M., G.D. Spence, N.R. Chapman, and R.D. Hyndman, Seismic
1067 investigations of a vent field associated with gas hydrates, offshore
1068 Vancouver Island, *Journal of Geophysical Research-Solid Earth*, 107 (B9),
1069 2002.
- 1070 Romanovskii, N.N., and H.W. Hubberten, Results of permafrost modelling
1071 of the lowlands and shelf of the Laptev Sea region, Russia, *Permafrost*
1072 *and Periglacial Processes*, 12 (2), 191-202, 2001.
- 1073 Romanovskii, N.N., H.W. Hubberten, A. Gavrilov, V.E. Tumskey, and A.L.
1074 Kholodov, Permafrost of the east Siberian Arctic shelf and coastal
1075 lowlands, *Quaternary Science Reviews*, 23 (11-13), 1359-1369, 2004.

- 1076 Romanovskii, N.N., H.W. Hubberten, A.V. Gavrilov, A.A. Eliseeva, and G.S.
1077 Tipenko, Offshore permafrost and gas hydrate stability zone on the shelf
1078 of East Siberian Seas, *Geo-Marine Letters*, 25 (2-3), 167-182, 2005.
- 1079 Romanovskii, N.N., H.W. Hubberten, A.V. Gavrilov, V.E. Tumskey, G.S.
1080 Tipenko, M.N. Grigoriev, and C. Siegert, Thermokarst and land-ocean
1081 interactions, Laptev Sea Region, Russia, *Permafrost and Periglacial*
1082 *Processes*, 11 (2), 137-152, 2000.
- 1083 Schuur, E.A.G., J. Bockheim, J.G. Canadell, E. Euskirchen, C.B. Field, S.V.
1084 Goryachkin, S. Hagemann, P. Kuhry, P.M. Lafleur, H. Lee, G. Mazhitova, F.E.
1085 Nelson, A. Rinke, V.E. Romanovsky, N. Shiklomanov, C. Tarnocai, S.
1086 Venevsky, J.G. Vogel, and S.A. Zimov, Vulnerability of permafrost carbon
1087 to climate change: Implications for the global carbon cycle, *Bioscience*, 58
1088 (8), 701-714, 2008.
- 1089 Shakhova, N., Geochemical and geophysical evidence of methane release
1090 over the East Siberian Arctic Shelf, *Journal of Geophysical Research-*
1091 *Oceans*, 115, 10.1029/2009JC005602, 2010.
- 1092 Shakhova, N., I. Semiletov, and G. Panteleev, The distribution of methane
1093 on the Siberian Arctic shelves: Implications for the marine methane cycle,
1094 *Geophysical Research Letters*, 32 (9), 2005.
- 1095 Shakhova, N., I. Semiletov, A. Salyuk, V. Yusupov, D. Kosmach, and O.
1096 Gustafsson, Extensive Methane Venting to the Atmosphere from
1097 Sediments of the East Siberian Arctic Shelf, *Science*, 327 (5970), 1246-
1098 1250, 2010a.
- 1099 Shakhova, N.E., V.A. Alekseev, and I.P. Semiletov, Predicted methane
1100 emission on the East Siberian shelf, *Doklady Earth Sciences*, 430 (2),
1101 190-193, 2010b.
- 1102 Shakhova, N.E., D.Y. Nicolsky, and I.P. Semiletov, Current state of subsea
1103 permafrost on the East Siberian Shelf: Tests of modeling results based on
1104 field observations, *Doklady Earth Sciences*, 429 (2), 1518-1521, 2009.
- 1105 Stein, R., and K. Fahl, Holocene accumulation of organic carbon at the
1106 Laptev Sea continental margin (Arctic Ocean): sources, pathways, and
1107 sinks, *Geo-Marine Letters*, 20 (1), 27-36, 2000.

- 1108 Stouffer, R.J., and S. Manabe, Equilibrium response of thermohaline
1109 circulation to large changes in atmospheric CO₂ concentration, *Clim.*
1110 *Dynamics*, 20, 759-773, 2003.
- 1111 Taylor, A.E., S.R. Dallimore, and S.I. Outcalt, Late quaternary history of
1112 the Mackenzie-Beaufort region, Arctic Canada, from modelling of
1113 permafrost temperatures .1. The onshore offshore transition, *Canadian*
1114 *Journal of Earth Sciences*, 33 (1), 52-61, 1996.
- 1115 Valentine, D.L., D.C. Blanton, W.S. Reeburgh, and M. Kastner, Water
1116 column methane oxidation adjacent to an area of active hydrate
1117 dissociation, Eel River Basin, *Geochimica Et Cosmochimica Acta*, 65 (16),
1118 2633-2640, 2001.
- 1119 Verrjuit, A., A note on the Ghyben-Herzberg formula, *Bull. Int. Assoc. Sci.*
1120 *Hydrology*, 13 (4), 43-46, 1968.
- 1121 Walter, K.M., S.A. Zimov, J.P. Chanton, D. Verbyla, and F.S. Chapin,
1122 Methane bubbling from Siberian thaw lakes as a positive feedback to
1123 climate warming, *Nature*, 443 (7107), 71-75, 2006.
- 1124 Watson, T.A., A.D. Werner, and C.T. Simmons, Transience of seawater
1125 intrusion in response to sea level rise, *Water Resources Res.*, 40
1126 (W12533), doi:10.1029/2010WR009564, 2010.
- 1127 Westbrook, G.K., Escape of methane gas from the seabed along the West
1128 Spitsbergen, *Geophysical Research Letters*, 36, 2009.
- 1129 Westbrook, G.K., K.E. Thatcher, E.J. Rohling, A.M. Piotrowski, H. Paelike,
1130 A.H. Osborne, E.G. Nisbet, T.A. Minshull, M. Lanoiselle, R.H. James, V.
1131 Huehnerbach, D. Green, R.E. Fisher, A.J. Crocker, A. Chabert, C. Bolton, A.
1132 Beszczynska-Moeller, C. Berndt, and A. Aquilina, Escape of methane gas
1133 from the seabed along the West Spitsbergen continental margin,
1134 *Geophysical Research Letters*, 36, 2009.
- 1135 Zimov, S.A., S.P. Davydov, G.M. Zimova, A.I. Davydova, E.A.G. Schuur, K.
1136 Dutta, and F.S. Chapin, III, Permafrost carbon: Stock and decomposability
1137 of a globally significant carbon pool, *Geophysical Research Letters*, 33
1138 (20), 2006.
- 1139

1140 **6. Figure Captions**

1141 Figure 1. Thermodynamics of hydrate and ice. Top) Colors are salinities,
1142 which range from fresh if there is no solid phase, to saltier as the freezing
1143 point depression of the solid phase follows the in situ temperature.
1144 Contours indicate the extent of thermal disequilibrium, $\Delta T_{eq} = T - T_{eq}$. a)
1145 For the system of ice and fluid. b) Considering hydrate and fluid phases,
1146 excluding ice formation and assuming equilibrium with methane gas. c)
1147 Combined ice + hydrate + fluid system, where the salinity is controlled by
1148 the most stable solid phase. Solid contours are $\Delta T_{eq, hydrate}$, dashed $\Delta T_{eq, ice}$.
1149 d and e) Colors are ΔT_{eq} , where 0 (purple) indicates stability, and contours
1150 are the excess salinity relative to a solid phase, e.g. $S_{max} - S_{eq, hydrate}$ in (d),
1151 for hydrate, and e) ice. f) Phase diagram for the ice + hydrate + brine
1152 system. Hydrate is excluded from the ice phase space by the high salinity
1153 of the brine. Ice is ideally also excluded from part of the hydrate stability
1154 zone by a similar mechanism, but this would only happen in nature under
1155 conditions of unlimited methane availability. Thus it is easier to envision
1156 coexistence of hydrate and ice within the hydrate stability zone, under
1157 conditions of limited methane availability, than it is to imagine hydrate in
1158 the permafrost zone, where ice has no impediment for formation.

1159 Figure 2. Domain of the model as applied to the Laptev Sea continental
1160 shelf and slope. This is the result of 62 million years of sediment
1161 accumulation on the crust, isostatic subsidence, pore fluid flow, and
1162 thermal diffusion, used as the initial condition for glacial / interglacial
1163 cycle and climate change simulations. Color indicates temperature. a)
1164 Full view. Black line shows the bottom of the crust, which grades
1165 smoothly from continental on the left into ocean crust through most of
1166 the domain on the right. b) Zoom in to see increased model resolution in
1167 the upper kilometer of the sediment column.

1168 Figure 3. Particulate Organic Carbon (POC) concentration. Highest values
1169 are found in the sediment depocenter just off the continental shelf break.

1171 Figure 4. Pore water salinity a) The fully marine case, in which the
1172 sediment column has always been submerged underneath a time-invariant
1173 sea level. b) Result of sediment column freshening by hydrological
1174 groundwater flow, driven by the pressure head resulting from a water
1175 table higher than sea level. A movie of the transition from marine to

1176 freshened (the origin of b) can be seen at
1177 http://geosci.uchicago.edu/~archer/spongebob_arctic/fig4.movie.gif

1178 Figure 5. Initial distribution of dissolved methane. a) Concentration in
1179 moles/m³. b-d) $\Omega = \text{CH}_4 / \text{CH}_{4(\text{sat})}$ deviation from equilibrium, b) of the
1180 Marine (salty) initial condition; c) of the pre-freshened initial condition
1181 (note depletion in near-surface near-shore sediments in the upper left);
1182 d) including permeable channels every five grid points, plus pre-
1183 freshening.

1184 Figure 6. Freshening the sediment column by hydrological groundwater
1185 flushing. Color indicates salinity. Solid black line represents sea level in
1186 the ocean (white space), and the equilibrium fresh-salty boundary given a
1187 snapshot of the pressure head (the Ghyben-Herzberg relation). Left side:
1188 results of dropping sea level 30 meters and holding it there. A freshwater
1189 lens forms and strives to reach Ghyben Herzberg equilibrium as the
1190 sediment column subsides, where atmospheric exposure decreases its
1191 buoyancy and stops sediment accumulation. After the sediment column
1192 subsides beneath the still-lowered sea level, the fresh water lens remains
1193 for millions of years. A movie can be seen at
1194 http://geosci.uchicago.edu/~archer/spongebob_arctic/fig6a.movie.gif .
1195 Right side: Result of dropping sea level 120 meters and holding it there
1196 forever. Movie at
1197 http://geosci.uchicago.edu/~archer/spongebob_arctic/fig6b.movie.gif

1198 Figure 7. Time scale of depleting the salinity of the continental shelf
1199 sediment column after an instantaneous sea level drop of 30 meters. The
1200 effect of lateral canyons is to provide a pathway for saline fluid to be
1201 replaced by fresh groundwater in sediments above sea level. If the lateral
1202 canyon spacing is 10 km, they can have a significant impact on the time
1203 constant for ground water flushing. A more conservative 100-km canyon
1204 is adopted for the rest of the simulations.

1205 Figure 8. Dissolved methane impact by hydrological freshening of the
1206 sediment column as described in Figure 5. $\Omega = \text{CH}_4 / \text{CH}_{4(\text{sat})}$. Movies can
1207 be seen at
1208 http://geosci.uchicago.edu/~archer/spongebob_arctic/fig8a.movie.gif
1209 and
1210 http://geosci.uchicago.edu/~archer/spongebob_arctic/fig8b.movie.gif

1211 Figure 9. Time-dependent forcing for the glacial / interglacial simulations
1212 and the global warming scenarios. a) Sea level is imposed as a sawtooth
1213 100-kyr cycle, with interglacial intervals shaded. The GW+S simulation
1214 tracks potential changes in sea level on long time scales due to fossil fuel
1215 CO₂ release, following a covariation from the geologic past of 15 meters /
1216 °C. The GW and Control simulations hold sea level at interglacial levels.
1217 b) Ocean temperature forcings.

1218 Figure 10. Colors indicate salinity in the unfrozen pore fluid of the
1219 sediment column. Thin solid black contours show the frozen fraction of
1220 the pore space. Heavy black stippled contour shows the stability
1221 boundary of methane hydrate as a function of temperature, pressure, and
1222 unfrozen pore fluid salinity. Left side: previously pre-freshened initial
1223 condition. Right side: Pure marine initial condition. c-d) Lowered sea level
1224 (from 70 kyr in Figure 8) but warm air temperatures prevent permafrost
1225 formation. e-f) Glacial conditions of lowered sea level (70 kyr) and
1226 atmospheric temperature of -17 °C driving permafrost formation. The
1227 pre-freshened and the marine initial conditions differ in the frozen fraction
1228 of sediment, but the salinity of the unfrozen fluid, a correlate of the
1229 activity of water, depends only the temperature. g-h) Rising sea level (at
1230 90 kyr in Figure 8) into an interglacial interval. Movies of the glacial
1231 cycles (GL) with the prefreshened initial condition can be seen at
1232 http://geosci.uchicago.edu/~archer/spongebob_arctic/fig10a.movie.gif ,
1233 and the marine initial condition at
1234 http://geosci.uchicago.edu/~archer/spongebob_arctic/fig10b.movie.gif.

1235 Figure 11. Pore fluid pressure forcing and flow through the glacial cycles.
1236 Left) Colors indicate $P_{\text{excess}} + P_{\text{head}}$, solid contours are ice fraction, dashed
1237 contours are P_{head} . Right) Colors indicate $P_{\text{excess}} + P_{\text{head}}$, note different color
1238 scale from Left. Initial refers to the prefreshened initial condition. “Low
1239 Sea Level” refers to simulation SL. “Glacial” and “Interglacial” refer to
1240 simulation GL. Dashed contours indicate ice fraction, vectors fluid
1241 velocity. Movies of the prefreshened initial condition and glacial cycles
1242 (GL) can be seen at
1243 http://geosci.uchicago.edu/~archer/spongebob_arctic/press_uw.65e6.nc.ld2.gl.pf_eq.gw.comp.movie.gif and
1244 http://geosci.uchicago.edu/~archer/spongebob_arctic/pressure_flow.65e6.nc.ld2.gl.pf_eq.gw.comp.movie.gif.

1247 Figure 12. Sensitivities of the hydrate stability zone. Impact of the
1248 competition between ice and hydrate phases (a-d), and the geothermal

1249 temperature gradient (e-f). When ice is included as a potential solid
1250 phase, the pore waters are salty in the permafrost zone (a), restricting
1251 hydrate stability to at least 300 meters below sea level throughout the
1252 simulation (c). When ice is forbidden to form, hydrate can be stable
1253 nearly to the sediment surface during the height of the glaciation (b and
1254 d). The base of the stability zone is sensitive to the geothermal
1255 temperature gradient, while the shallowest reach of the stability zone
1256 does not respond to changing heat fluxes, because the temperatures are
1257 “anchored” at the ocean value at the top of the sediment column.

1258 Figure 13. Dissolved methane concentration relative to equilibrium ($\Omega =$
1259 $\text{CH}_4 / \text{CH}_{4(\text{sat})}$). Solid contours indicate ice fraction, dashed contours show
1260 the methane hydrate stability boundary. Movies for the left, center, and
1261 right columns, respectively can be seen at
1262 http://geosci.uchicago.edu/~archer/spongebob_arctic/fig13a.movie.gif ,
1263 http://geosci.uchicago.edu/~archer/spongebob_arctic/fig13b.movie.gif ,
1264 and
1265 http://geosci.uchicago.edu/~archer/spongebob_arctic/fig13c.movie.gif.

1266 Figure 14. Carbon cycle through glacial cycles from a prefreshened initial
1267 condition. Solid contours: Ice Fraction. Dashed contours: Methane
1268 hydrate stability zone. Left) Particulate organic carbon (POC)
1269 concentration. Movie at
1270 http://geosci.uchicago.edu/~archer/spongebob_arctic/fig14a.movie.gif.
1271 Center) Biological methane production rate. Movie at
1272 http://geosci.uchicago.edu/~archer/spongebob_arctic/fig14b.movie.gif
1273 Right) Methane hydrate concentration. Movie at
1274 http://geosci.uchicago.edu/~archer/spongebob_arctic/fig14c.movie.gif.
1275 Movies of methane hydrate stability and concentration are given for the
1276 sensitivity studies, in the supplemental material and at
1277 <http://geosci.uchicago.edu/~archer/spongebob/>.

1278 Figure 15. Glacial cycle of methane hydrate inventory on the continental
1279 shelf. a) Effects of salt and ice. b) Sensitivity to methaneogenesis rates.
1280 c) Sensitivity to the column temperature gradient. d) Glacial cycles of
1281 shelf bubble inventories, effects of salt and ice.

1283 Figure 16. Spatial distribution and sea level impact of methane fluxes to
1284 the atmosphere. a-d) Solid line shows the elevation of the sediment
1285 surface relative to the sea level at the time. Grey lines (scale to right)

1286 show the efficiency of bubble transport through the water column,
1287 assuming a flux attenuation length scale of 30 meters. e-k) Dashed line:
1288 Methane bubble flux across the sediment surface. Solid line: Methane
1289 bubble flux to the atmosphere (dashed line multiplied by transport
1290 efficiency). Most of the methane flux in the model occurs near the shelf
1291 break, and submergence in the ocean has a strong impact on the flux to
1292 the atmosphere. A related movie can be seen at
1293 http://geosci.uchicago.edu/~archer/spongebob_arctic/fig16.movie.gif .

1294 Figure 17. Glacial / interglacial cycle of methane fluxes on the
1295 continental margin of the model. Sea level at top, grey regions indicate
1296 interglacial intervals, pink the Anthropocene. a-e) Cumulative methane
1297 fluxes. Red lines show production rate. Brown regions show lateral
1298 transport of dissolved methane. Grey shows oxidation by SO_4^{2-} in the
1299 sediment column. Blue shows bubble flux to the water column. During
1300 interglacial times (e.g. far left) there is a small onshore transport of
1301 methane, which is represented by a negative starting point for the
1302 oxidation (grey) region. In equilibrium, the colored areas should fill in the
1303 region under the red curve.

1307 Figure 18. Methane fluxes to the atmosphere. Sea level at the top,
1308 interglacial intervals in vertical grey bars, the Anthropocene in pink. a)
1309 From a pre-freshened initial condition, with and without permafrost
1310 formation. b) From a pure marine initial condition. c and d) Sensitivity to
1311 terrestrial organic carbon deposition during low sea-level stands, and to
1312 thermogenic methane flux. e) Sensitivity to the impact of ice fraction on
1313 bubble mobility.

1314 Figure 19. Impact of anthropogenic warming on the methane cycle in the
1315 model. a) Base cases, a warming scenario (GW), without and with a
1316 geological time-scale sea level rise scenario (+SLR), and extended
1317 interglacial control (Ctl). Warming plus increasing sea level decreases the
1318 methane flux overall, due to bubble dissolution in a deeper water column.
1319 b) Altered model physics impacts. c and d) Altered methanogenesis
1320 rates. e) Sensitivity to the ice fraction at which bubble mobility is
1321 assumed stopped.

1322 Tables

1323 Table 1. Summary of model runs.

SL	Sea level changes with constant air and water temperatures
GL	SL + glacial cycles in air and water temperature
GW	A long-term global warming scenario, a peak and long tail temperature perturbation consistent with CO ₂ release and cessation of the glacial sawtooth forcing.
+SLR	Adds geologic-timescale sea level rise due to anthropogenic climate change, based on correlation between temperature and sea level in the geologic past (10 meters / °C).
Ctl	An extended interglacial with no CO ₂ release forcing.
+ LD	Land deposition of carbon-rich Yedoma. Base case is 10 m / 100 kyr, with sensitivity runs using 30 and 100 m / 100 kyr accumulation of 30% POC material. Movies in the supplemental material are identified by the tags Land30 and Land100.
+ TG	Thermogenic methane production rate sensitivity runs, scaling the rate from the spinup result by factors of 10 and 100. Movies in the supplemental material are identified by the tags TGenX10 and TGenX100.
+ Geotherm	Sensitivity of ice and hydrate cycles on the geothermal temperature gradient. Temperatures from the Base simulation were adjusted when calculating the stability of ice and hydrate, to simulate the impact of

	geothermal heat fluxes on hydrate stability. Note that other aspects of the sediment column, including the solubility of methane, retained the original temperatures. Heat fluxes simulated include 25 mW/m ² , 37.5, 50 (Base), 62.5, and 75. Movies of the non-base runs are identified by tags HF050, HF075, HF125, and HF150.
Ice and Bubble Transport	When the ice fraction exceeds a threshold value methane gas flow is disabled. Base case is 50%, variants 10%, 30%, 70%, and 90%, identified with tags Ice10, Ice30, Ice70, and Ice90.
No Ice	The ice phase is disallowed in the thermodynamic calculation. Movies in the supplemental material include salinity. The files are tagged as NoIce
No Salt from Ice	Ice is allowed to form, but it does not affect the salinity as it determines methane hydrate stability. Movie files are tagged as NoSalFromIce.
Permeable Channels	Increasing vertical permeability by a factor of 10 every 5 th grid cell, to generate heterogeneity in the flow. Tagged as PermChan
No Horizontal Flow	Horizontal flow is disabled. Tagged as NoHFlow.

1324 Movies comparing altered scenario runs with the Base scenario are given
1325 in the supplemental material, and at
1326 <http://geosci.uchicago.edu/~archer/spongebob/>. Movies named
1327 hydrate* and bubbles* show methane hydrate and bubble inventories and
1328 stability zone changes. Files entitled salinity* show salinities, and
1329 bubb_atm* show bubble fluxes through and out of the sediment column,
1330 into the ocean, and into the atmosphere, through time.

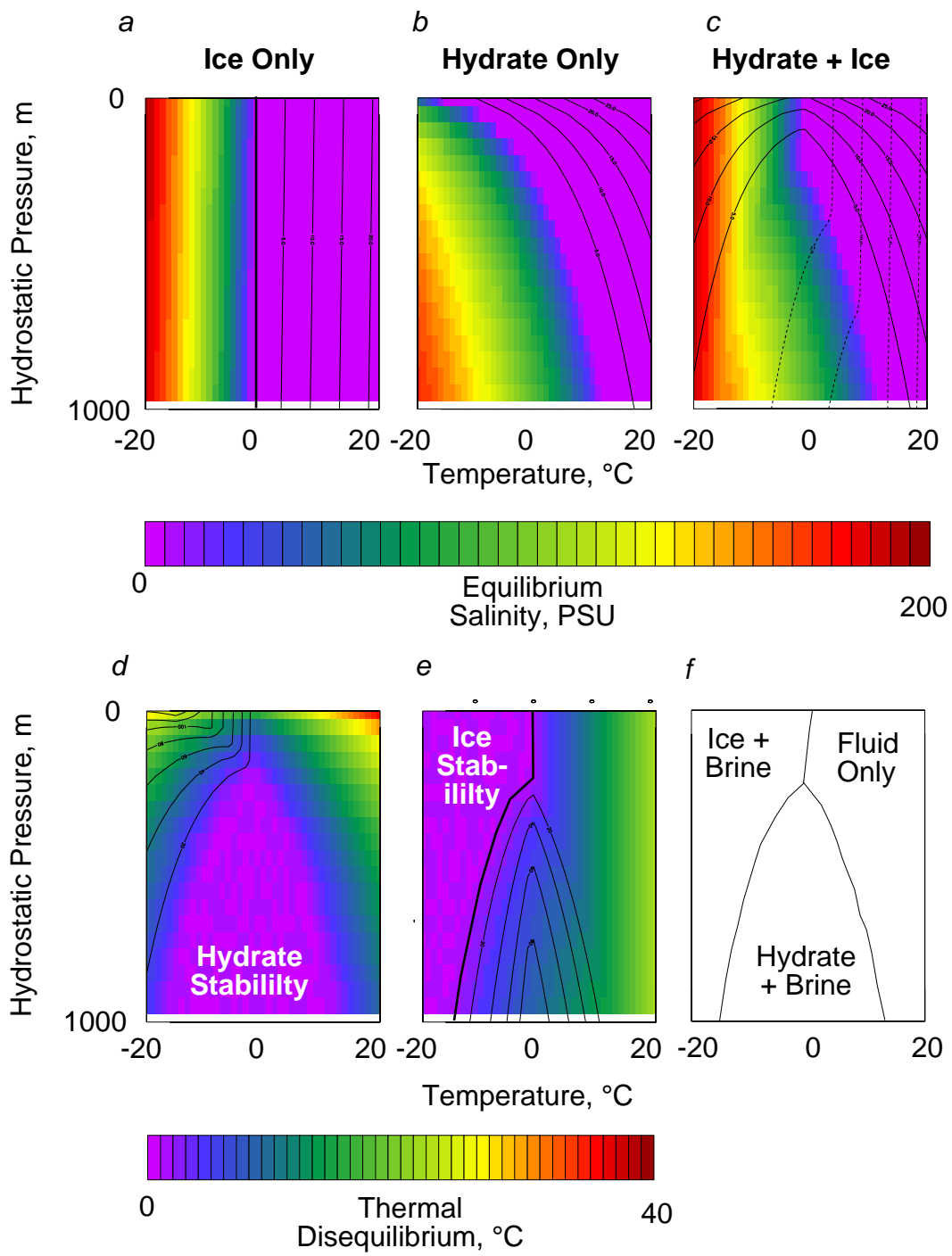


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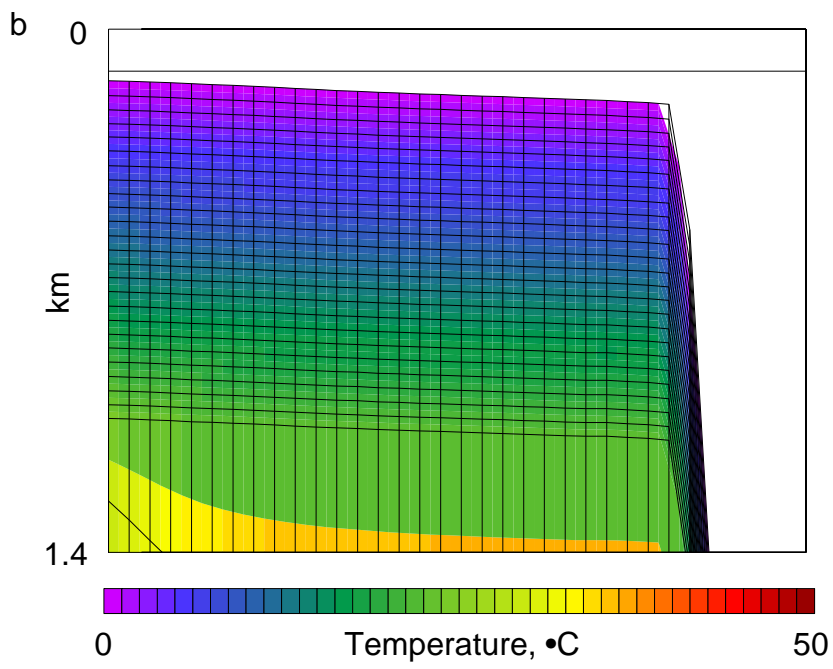
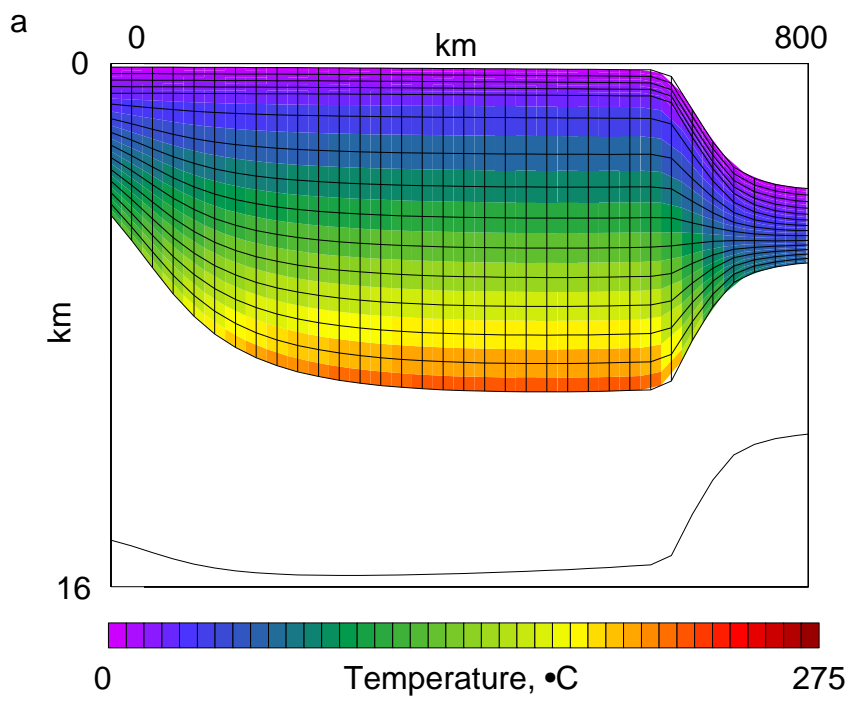


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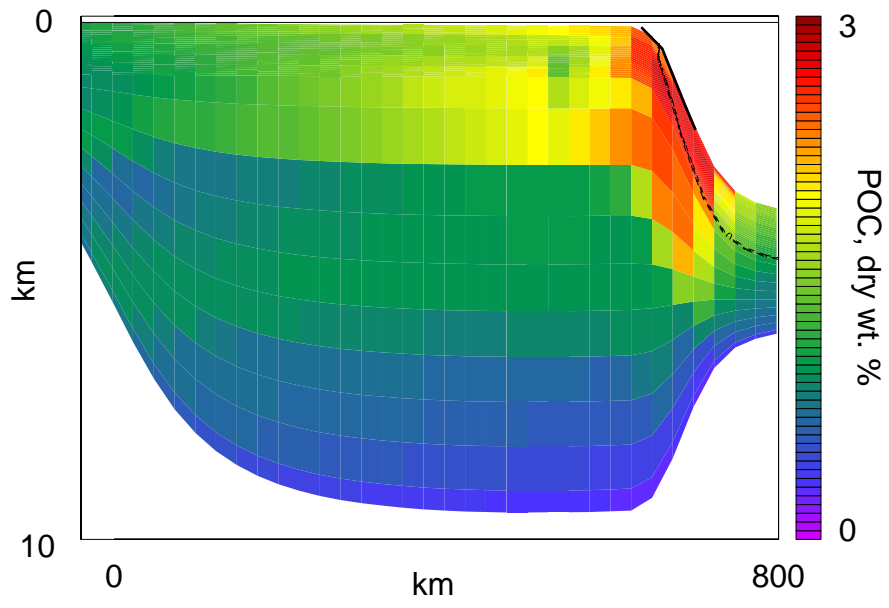


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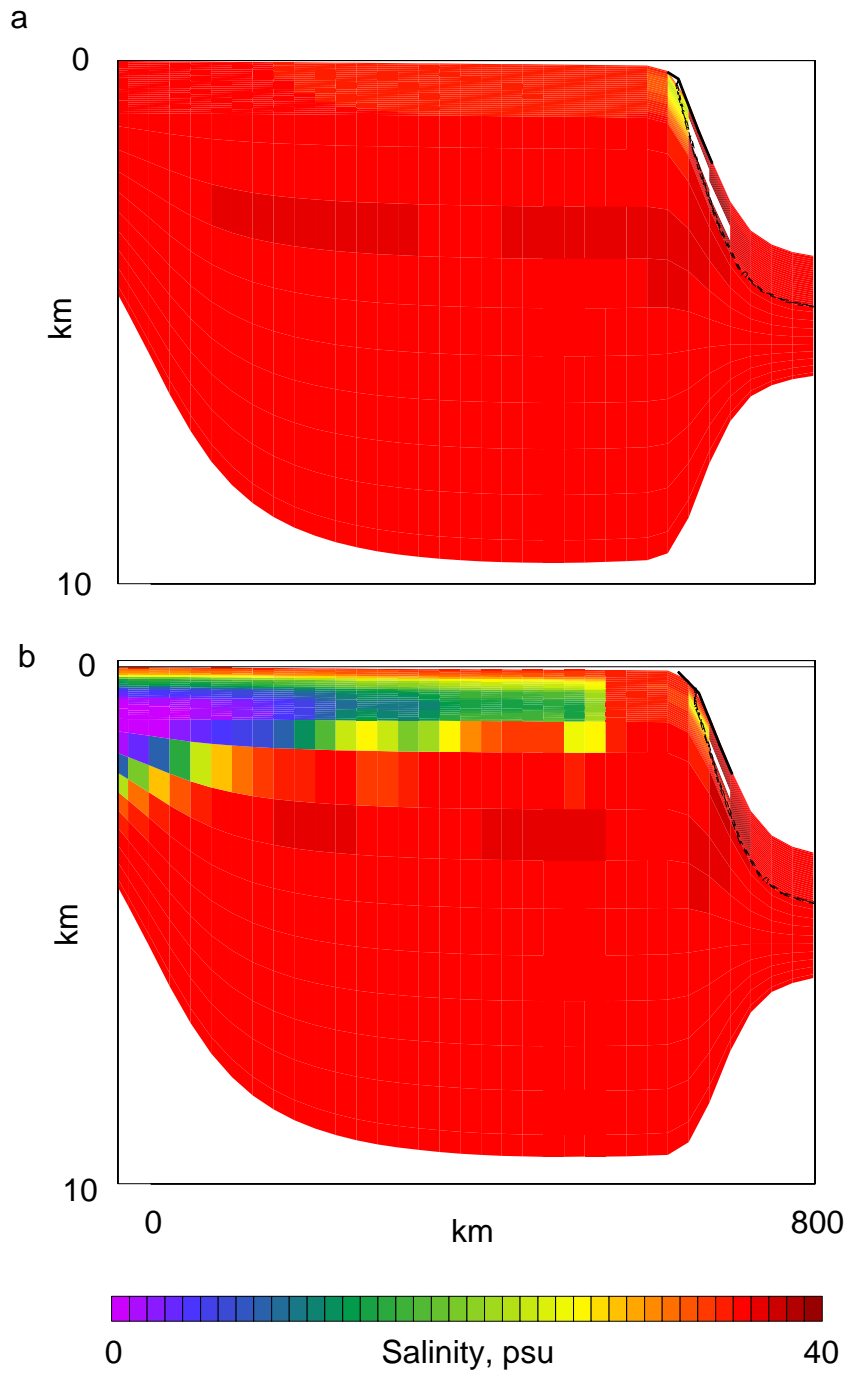


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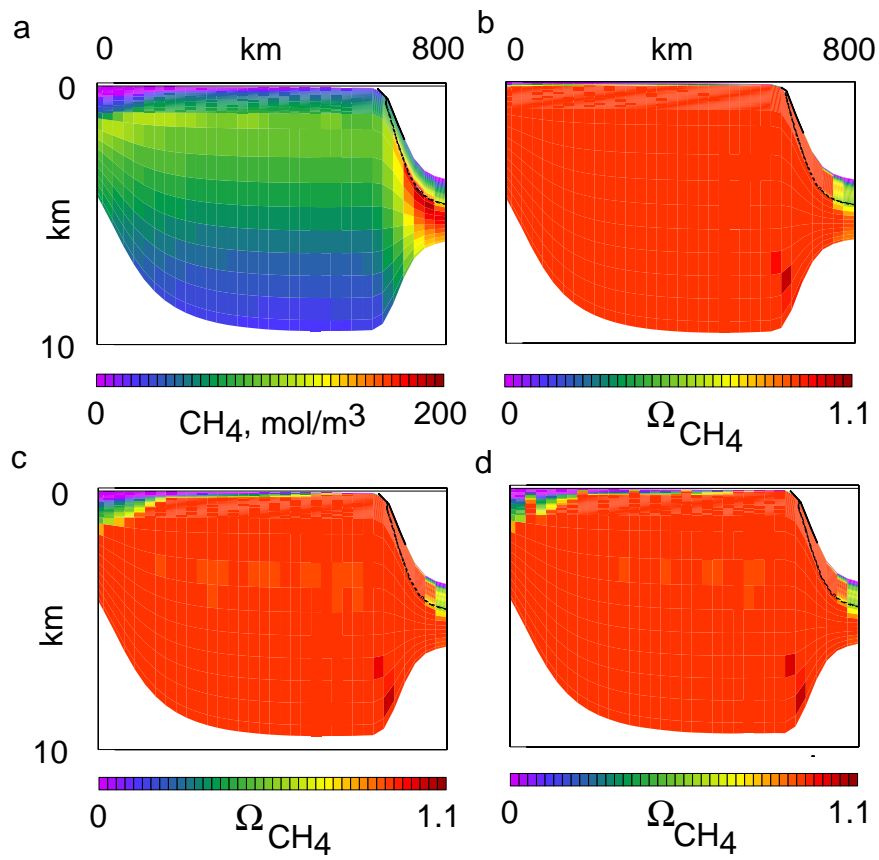


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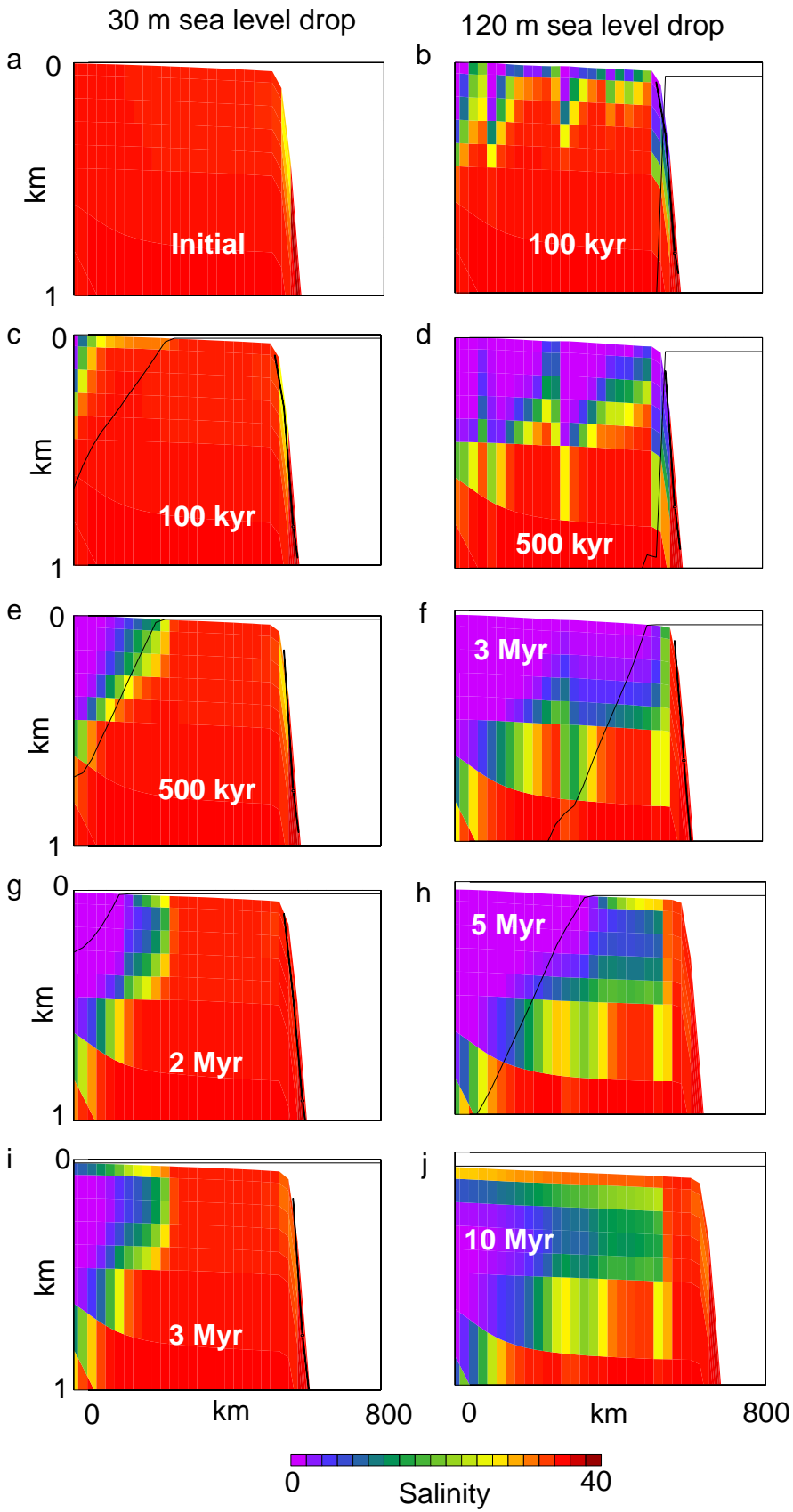


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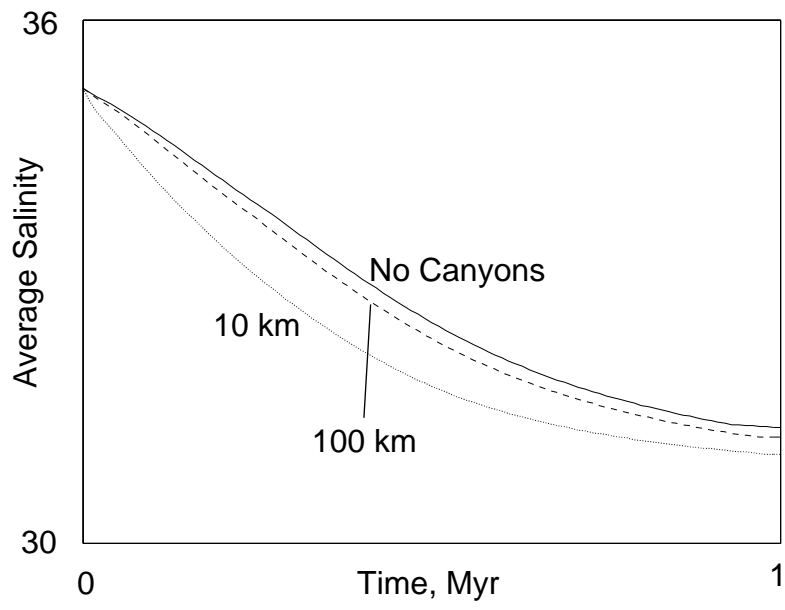


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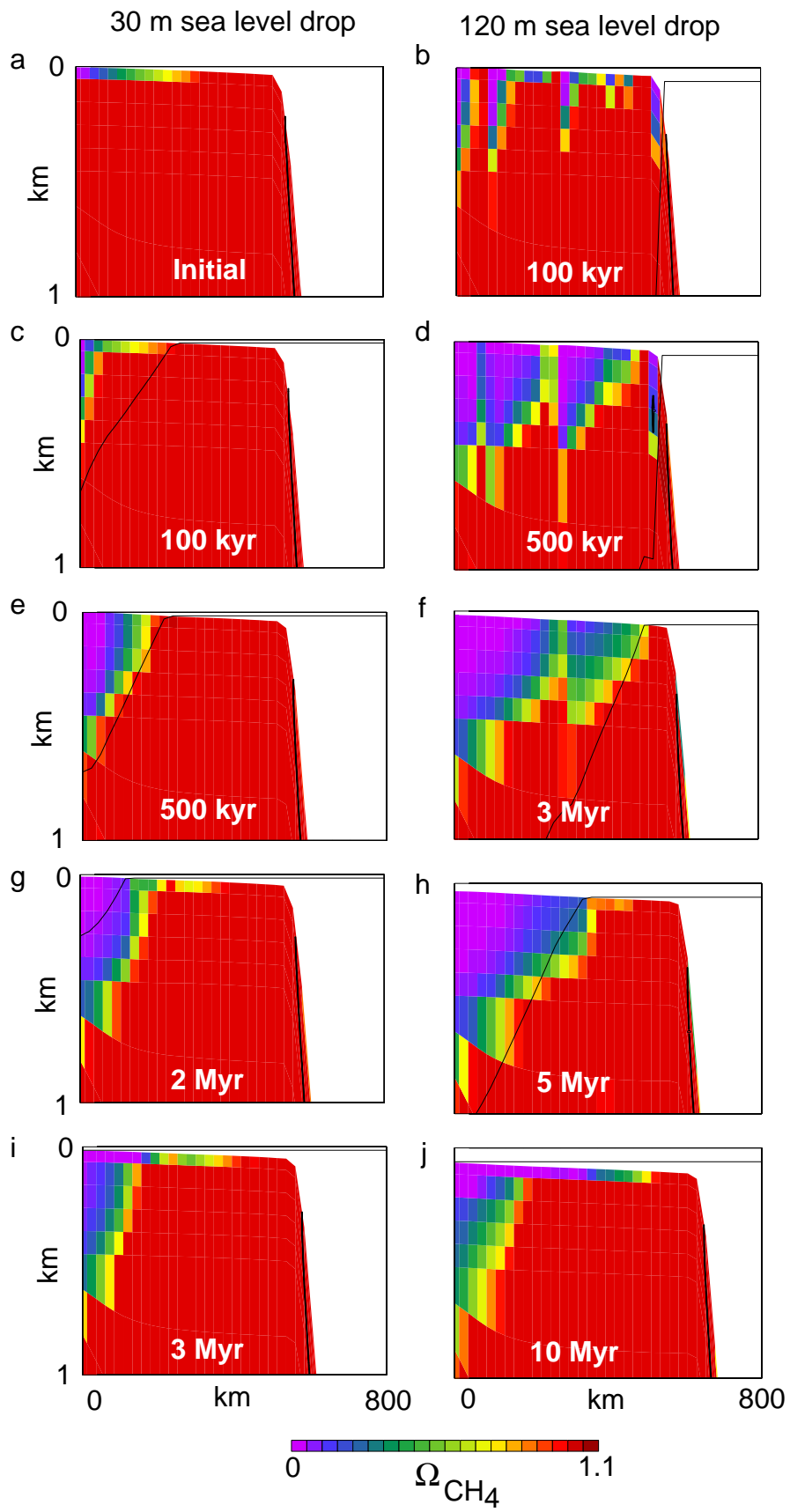


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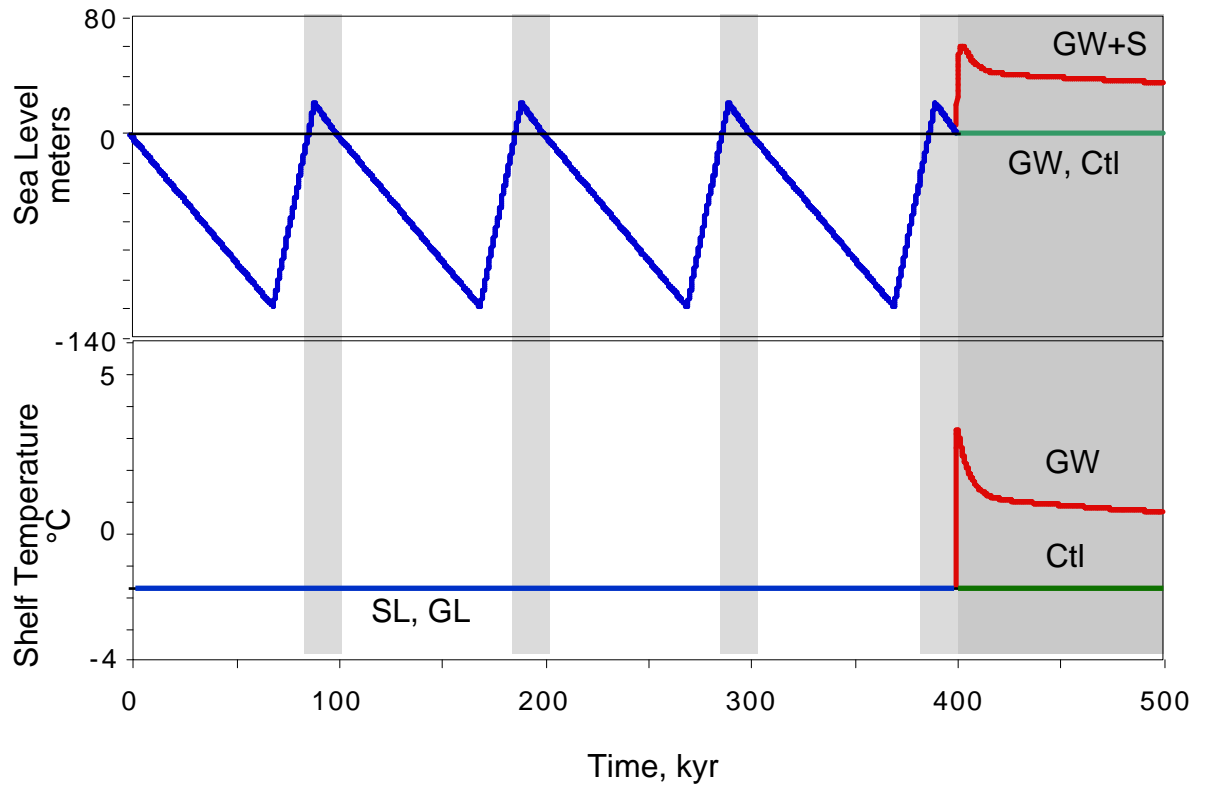


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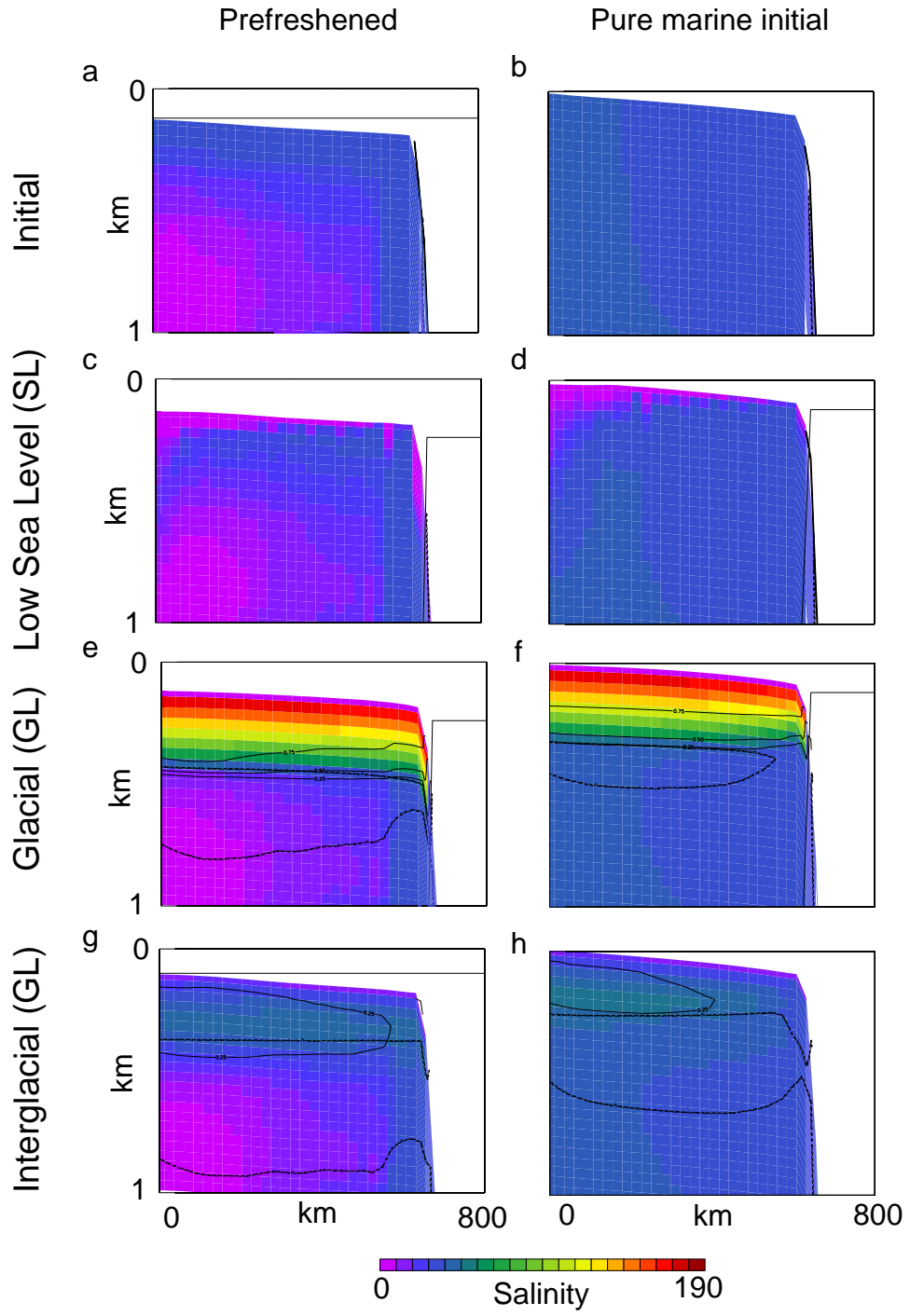


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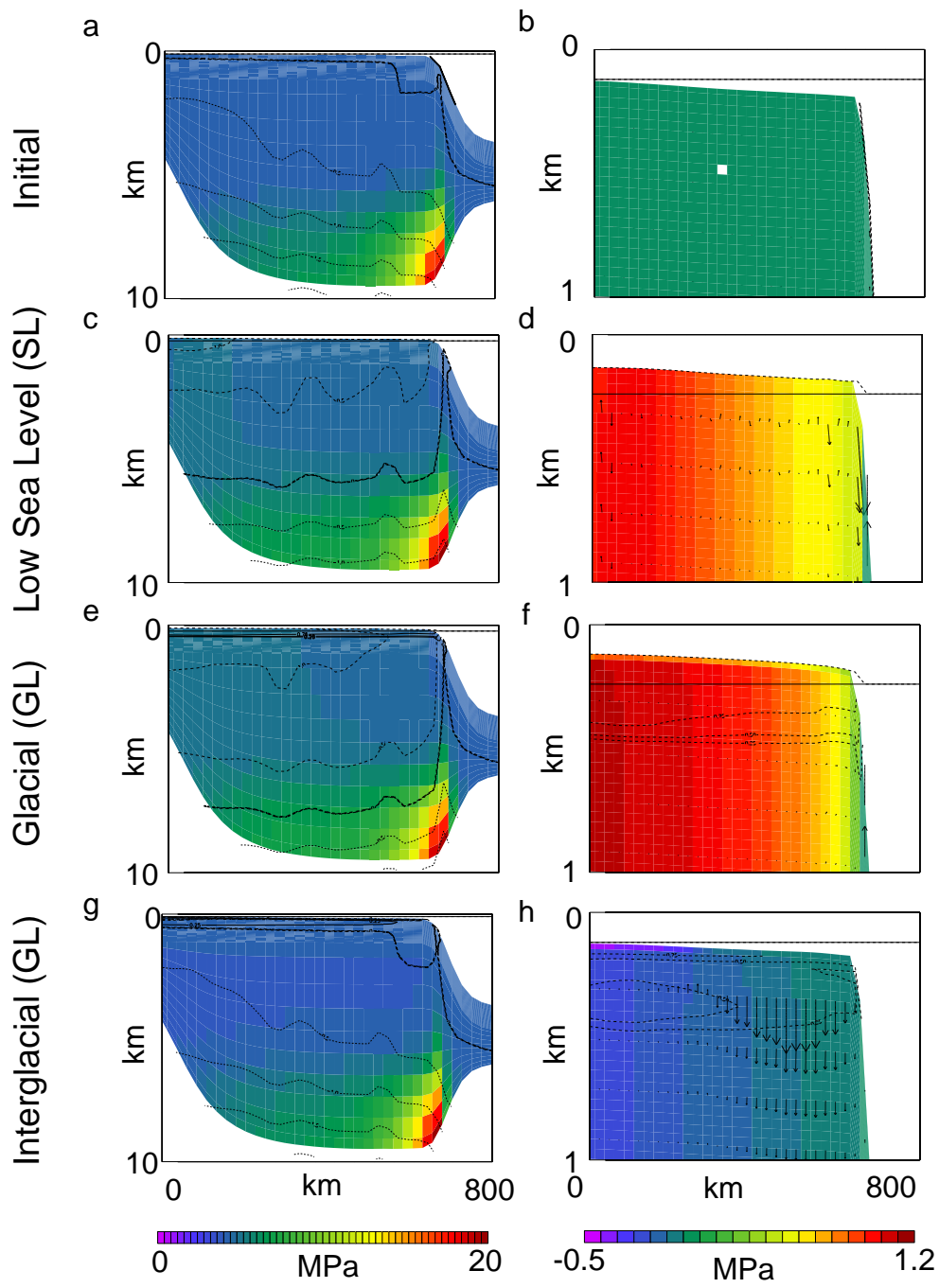


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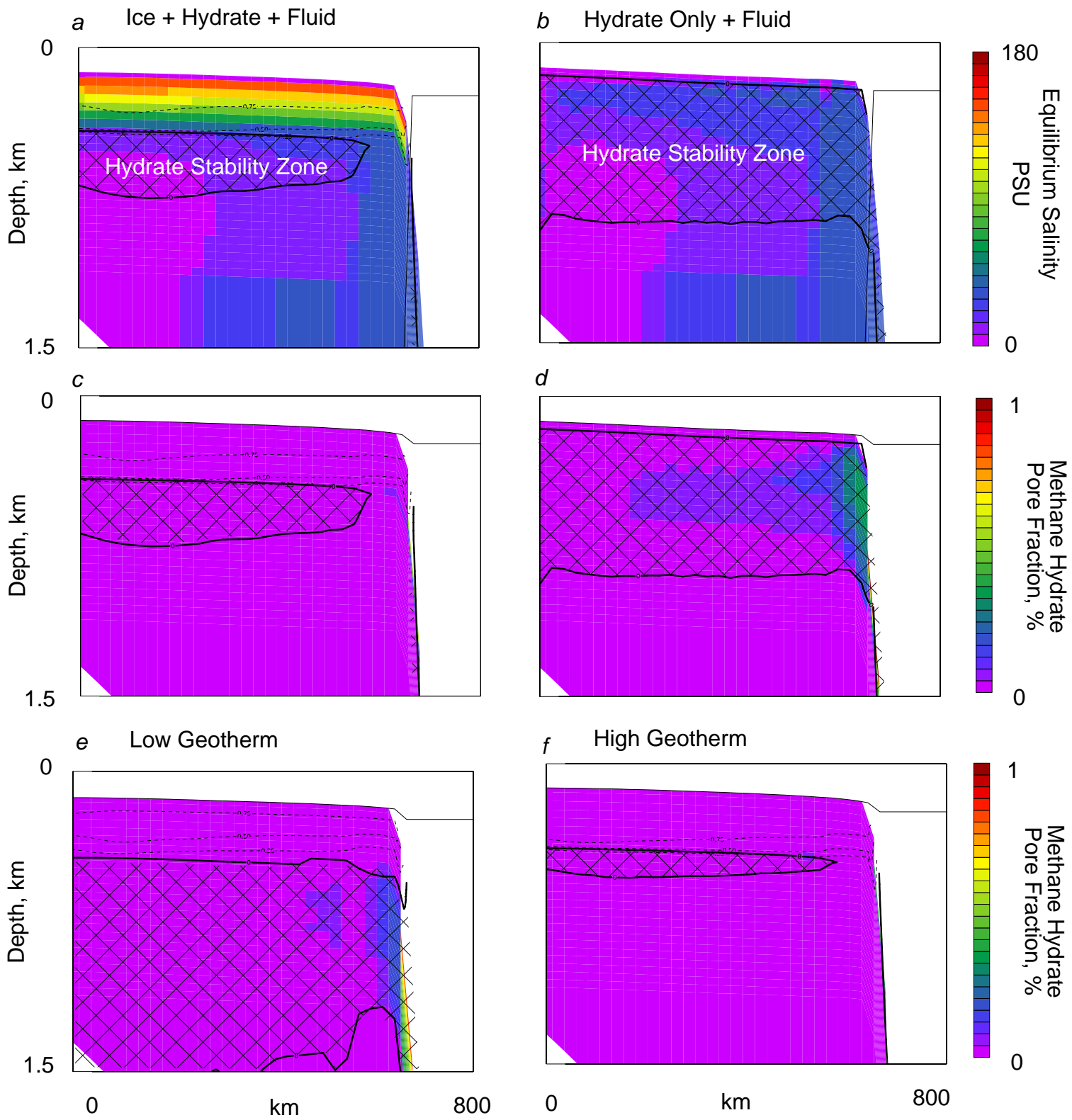


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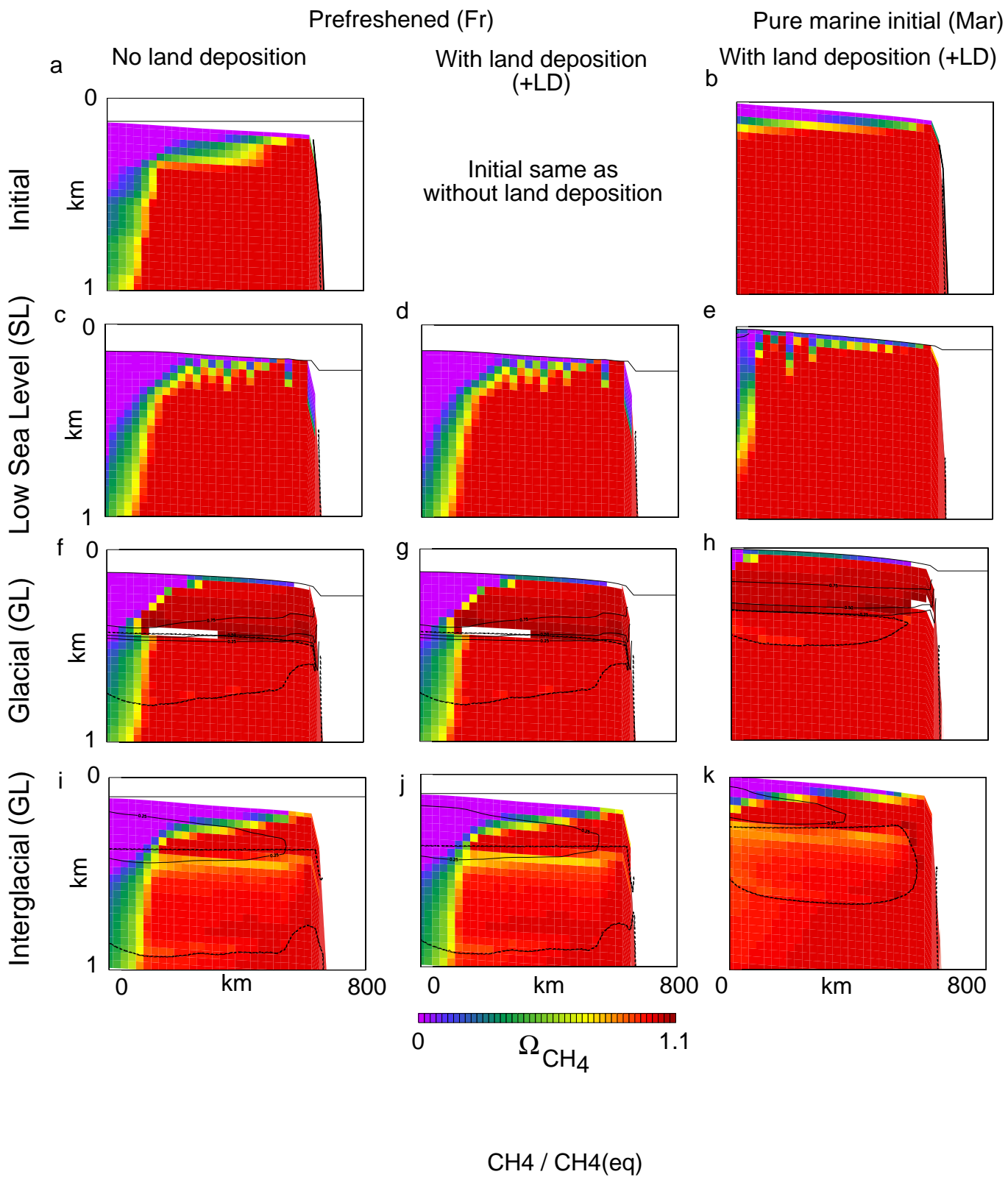


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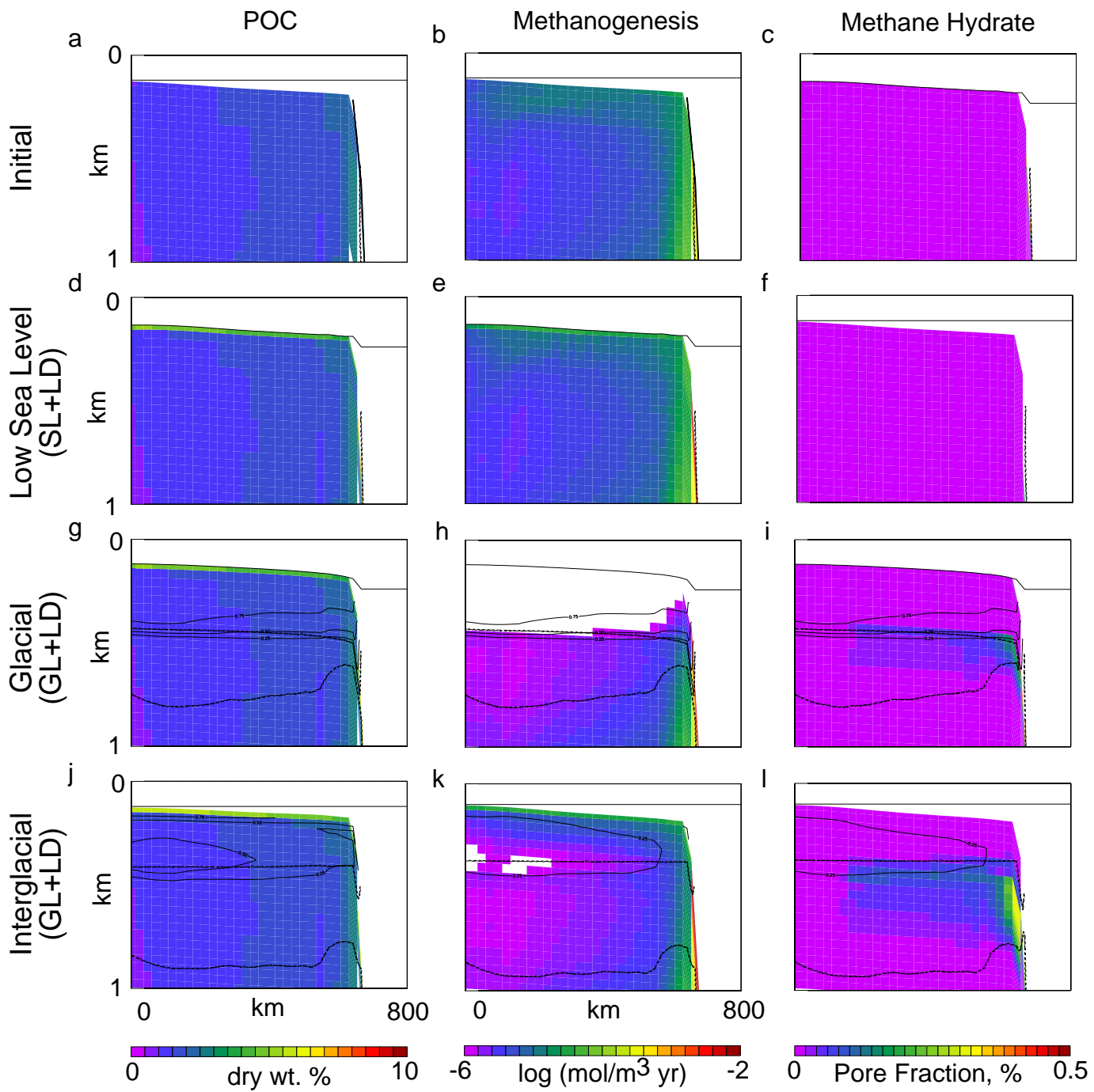


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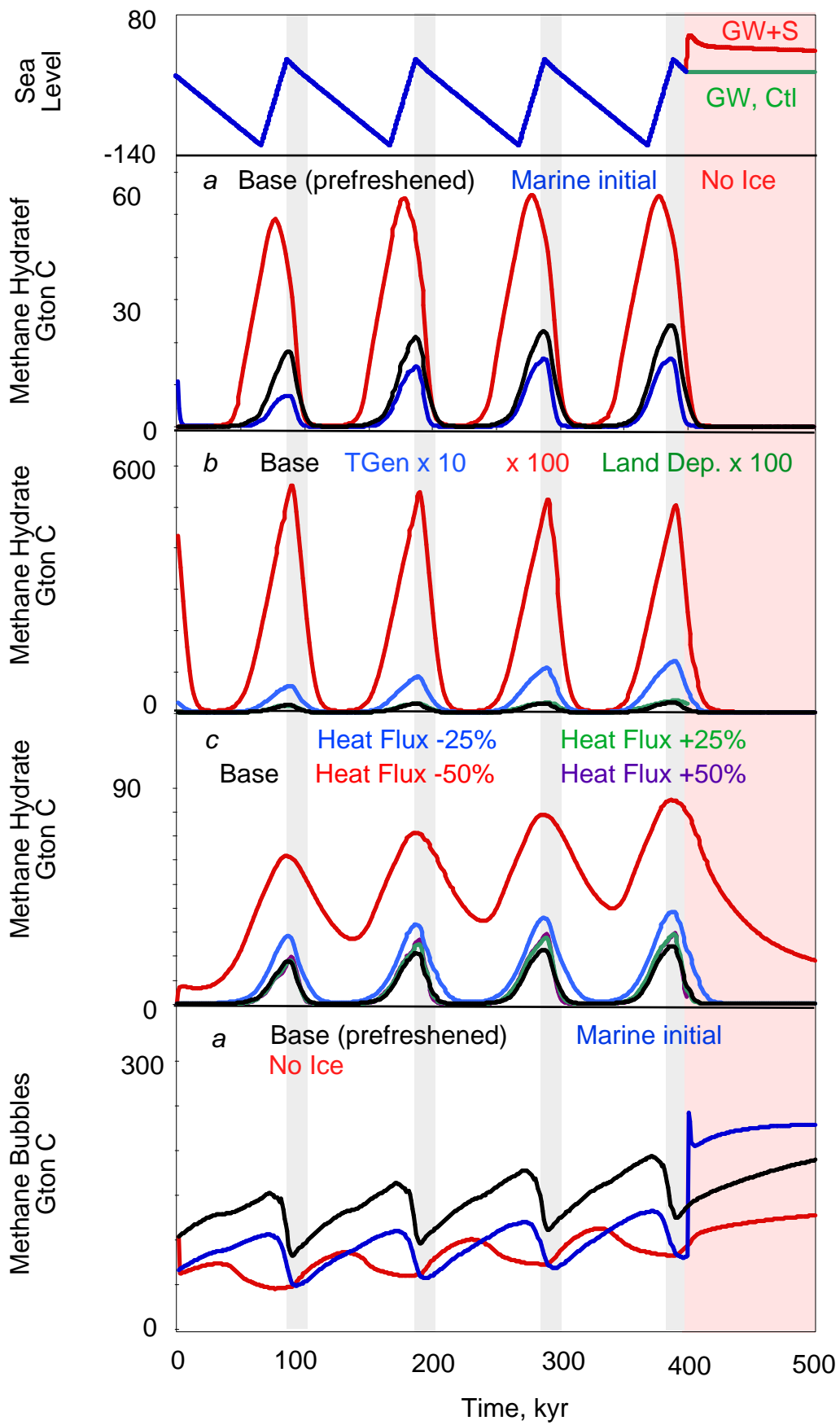


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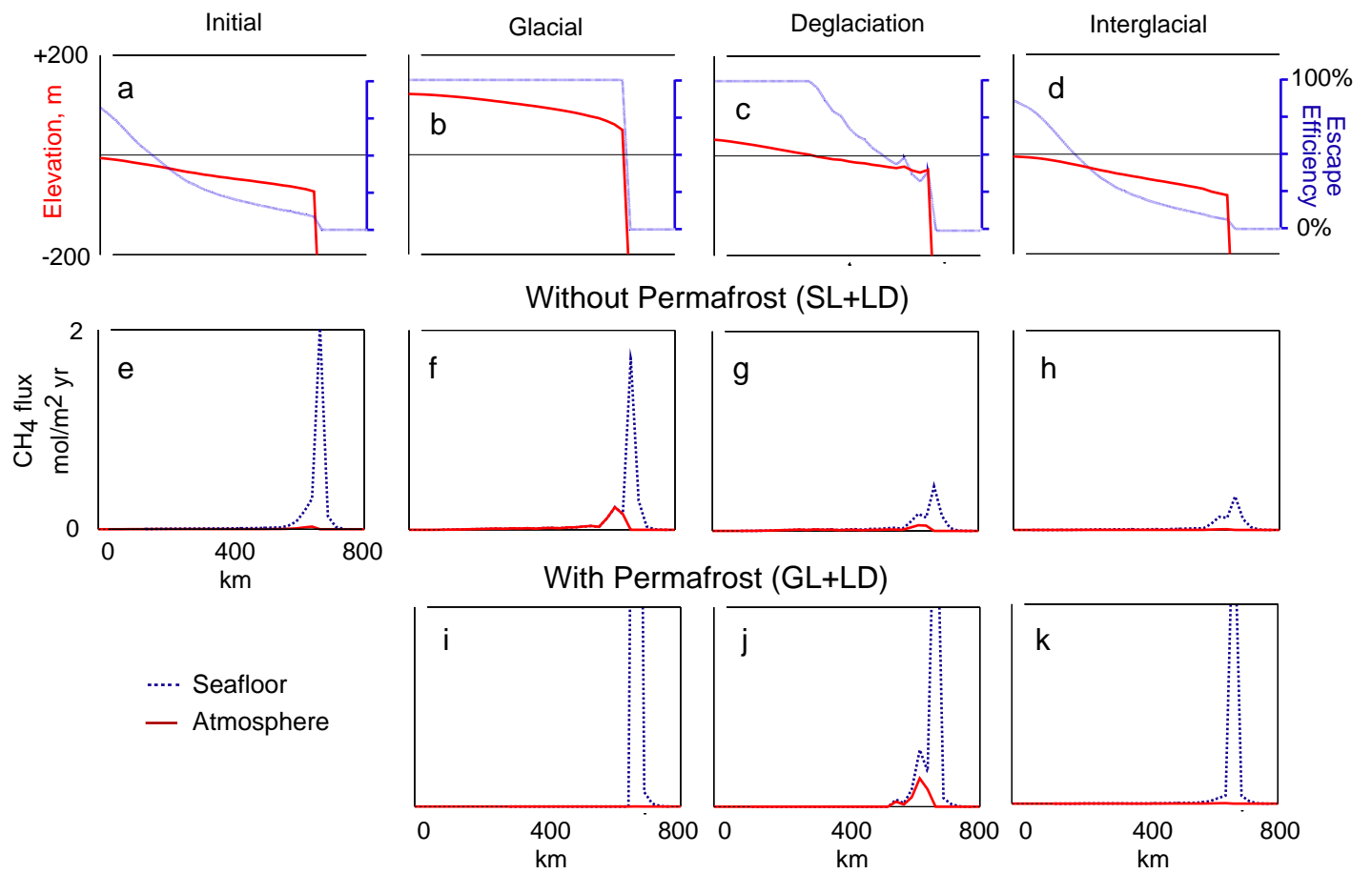


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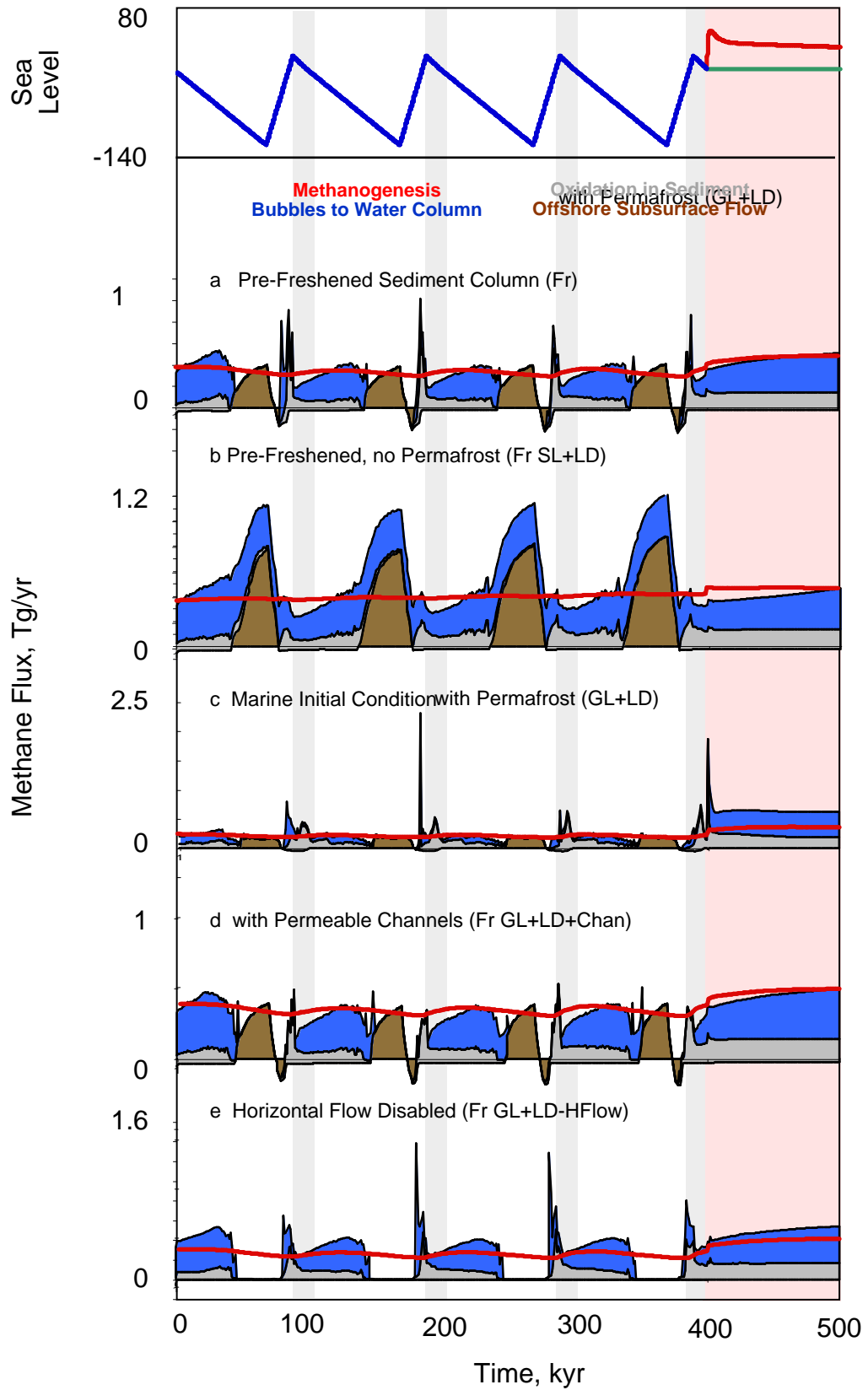


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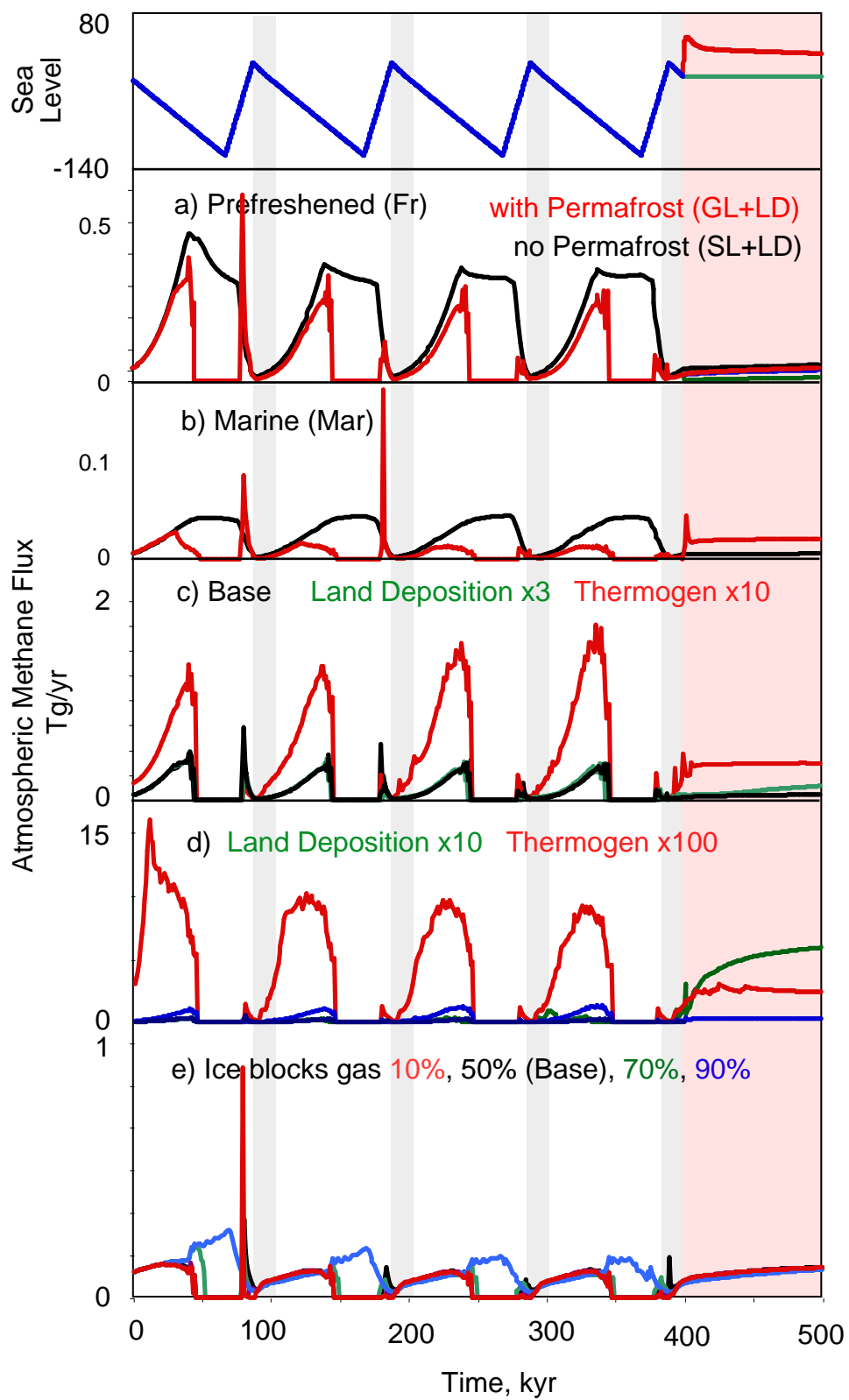


Figure 18

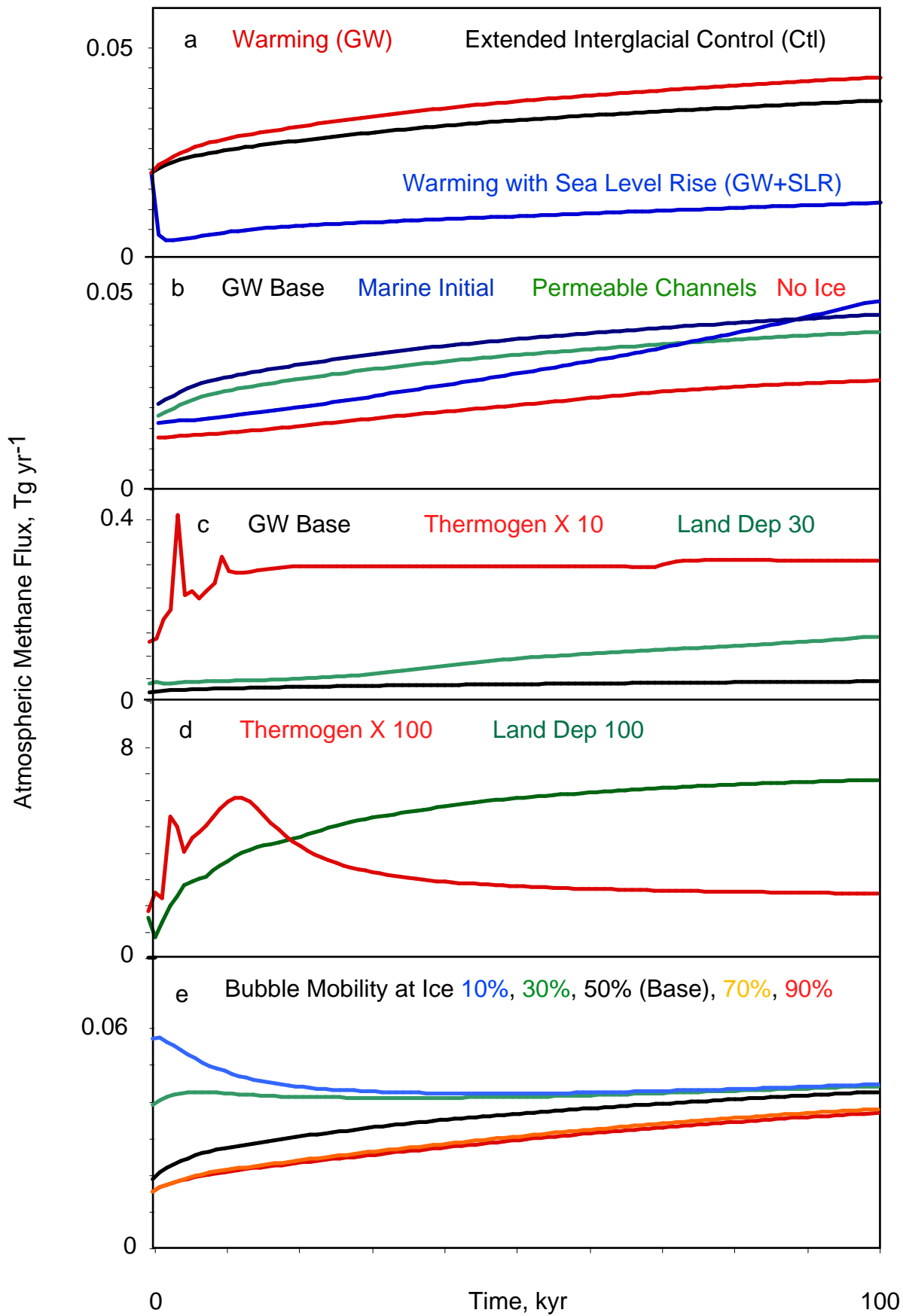


Figure 19