

1 **A model of the methane cycle, permafrost, and hydrology of the Siberian**
2 **continental margin**

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5
6 **Abstract**

7 A two-dimensional model of a sediment column, with Darcy fluid flow,
8 biological and thermal methane production, and permafrost and methane
9 hydrate formation, is subjected to glacial / interglacial cycles in sea level,
10 alternately exposing the continental shelf to the cold atmosphere during
11 glacial times, and immersing in the ocean in interglacial times. The glacial
12 cycles are followed by a “long tail” 100-kyr timescale warming due to
13 fossil fuel combustion.

14 The salinity of the sediment column in the interior of the shelf can be
15 decreased hydrological forcing, to depths well below sea level, when the
16 sediment is exposed to the atmosphere. There is no analogous advective
17 seawater-injecting mechanism upon resubmergence, only slower diffusive
18 mechanisms. This hydrological ratchet is consistent with the existence of
19 fresh water beneath the sea floor on continental shelves around the
20 world, left over from the last glacial time.

21 The salt content of the sediment column affects the relative proportions
22 of the solid and fluid H₂O-containing phases, but in the permafrost zone
23 the salinity in the pore fluid brine is a function of temperature only,
24 controlled by equilibrium with ice. Ice can tolerate a higher salinity in the
25 pore fluid than methane hydrate can at low pressure and temperature,
26 excluding methane hydrate from thermodynamic stability in the
27 permafrost zone. The implication is that any methane hydrate existing
28 today will be insulated from anthropogenic climate change by hundreds of
29 meters of sediment, resulting in a response time of thousands of years.

30 The strongest impact of the glacial / interglacial cycles on the
31 atmospheric methane flux is due to bubbles dissolving in the ocean when
32 sea level is high. When sea level is low and the sediment surface is
33 exposed to the atmosphere, the atmospheric flux is sensitive to whether
34 permafrost inhibits bubble migration in the model. If it does, the

35 atmospheric flux is highest during the glaciating, sea-level regression (soil
36 freezing) part of the cycle, rather than during deglacial transgression
37 (warming and thawing).

38 The atmospheric flux response to a warming climate is small, relative to
39 the rest of the methane sources to the atmosphere in the global budget,
40 because of the ongoing flooding of the continental shelf. The increased
41 methane flux due to ocean warming could be completely counteracted by
42 sea level rise of tens of meters on millennial time scales due to loss of ice
43 sheets, decreasing the efficiency of bubble transit through the water
44 column. The model results give no indication of a mechanism by which
45 methane emissions from the Siberian continental shelf could have a
46 significant impact on the near-term evolution of Earth's climate, but on
47 millennial timescales the release of carbon from hydrate and permafrost
48 could contribute significantly to the fossil fuel carbon burden in the
49 atmosphere / ocean / terrestrial carbon cycle.
50

51	1. Introduction.....	4
52	1.1 The Siberian Continental Shelf System	4
53	1.1.1 Permafrost	4
54	1.1.2 Salt	5
55	1.1.3 Carbon.....	6
56	1.2 Models of Methane Hydrate in the Permafrost Zone	6
57	1.3 Outline of This Work.....	7
58	2. Model Description.....	7
59	2.1 SpongeBOB Application to the Siberian Continental Margin	7
60	2.2 New Model Development: Groundwater Hydrology.....	8
61	2.2.1 Pressure Head	8
62	2.2.2 Pore Fluid Flow	9
63	2.2.3 Canyons.....	9
64	2.3 Permafrost.....	10
65	2.3.1 Thermodynamics of Ice and Hydrate.....	10
66	2.3.3 Other Impacts	11
67	2.4 Atmospheric Methane Fluxes	11
68	2.5 Initial Condition.....	12
69	2.5.1 Rational for Spinup.....	12
70	2.5.2 Sediment Column Salt Content.....	12
71	2.6 Glacial Cycle Forcing	13
72	2.6.1 Sea Level.....	13
73	2.6.2 Glacial Climate.....	13

74	2.6.3 Deposition of Carbon on Land	13
75	2.7 Anthropogenic Global Warming Forcing	14
76	2.7.1 Long-Term Climate Impact from CO ₂ Addition	14
77	2.7.2 Long-Term Behavior of Sea Level.....	14
78	2.8 Sensitivity Studies.....	14
79	3. Results.....	15
80	3.1 Glacial Cycles	15
81	3.1.1 Salinity.....	15
82	3.1.2 Pressure and Flow	15
83	3.1.3 Methane Cycle.....	16
84	3.2 Anthropogenic Global Warming.....	20
85	3.3 Sensitivity Studies.....	20
86	3.3.1 Sediment Salt Content.....	20
87	3.3.2 Methane Production Rates	21
88	3.3.3 Geothermal Temperature Gradient	21
89	3.3.4 Thermodynamic Competition Between Ice and Hydrate	21
90	3.3.5 Permafrost Inhibition of Gas Migration	21
91	3.3.6 Vertical flow heterogeneity	22
92	3.3.7 Ground water Flow	22
93	3.4 Comparison with Observations.....	22
94	4. Discussion	23
95	4.1 Limitations of the Model Results and Critical Issues for Future	
96	Development.....	23
97	4.1.1 Methane Production Rates	23
98	4.1.2 Gas Transport in the Sediment Column	23
99	4.1.3 Atmospheric Flux Efficiency.....	24
100	4.1.4 Uncertainty in Model Output.....	24
101	4.2 Robust Features of the Simulation.....	24
102	4.2.1 Arctic Ocean Methane Fluxes are Small in the Global Budget ..	24
103	4.2.1 The Hydrological Salinity Ratchet	24
104	4.2.2 Salinity (Water Activity) and Hydrate Stability in the Permafrost	
105	Zone	25
106	4.2.3 Sea Level Dominates the Glacial Cycle of Methane Flux.....	25
107	4.2.3 Methane Emission Response to Anthropogenic Climate Change	26
108	5. Acknowledgements.....	27
109	6. Bibliography.....	27
110	7. Figure Captions	29
111	8. Tables.....	33
112	9. Supplemental Text	35
113	S1. Vertical Flow	35

114	S2. Ice Formation	36
115	S3. Thermodynamics of Ice and Hydrate.....	36
116	S4. Construction of the Pre-Freshened Sediment Column	37
117	negligible impact of canyons	38
118	120 m same as 30	38
119	10. Supplemental Figure Captions	38
120		

121 **1. Introduction**

122 **1.1 The Siberian Continental Shelf System**

123 The Siberian Arctic continental shelf has been the focus of attention from
124 scientists and the public at large for its potential to release methane, a
125 greenhouse gas, in response to climate warming, a potential amplifying
126 positive feedback to climate change [*Shakhova, 2010; Westbrook,*
127 *2009*]. The goal of this paper is to simulate the geophysical and carbon
128 cycle dynamics of the Siberian continental margin within the context of a
129 basin- and geologic time-scale mechanistic model of the coastal margin
130 carbon cycle called SpongeBOB [*Archer et al., 2012*]. An initial condition
131 for the glacial cycle simulations was generated by spinning the up at low
132 resolution over 62 million simulated years. Then the model at higher
133 resolution is driven by cyclic changes in sea level and air temperature
134 resulting from glacial cycles, to simulate the impact of the hydrological
135 pressure head and permafrost formation on the fluid flow and methane
136 cycle on the shelf. Finally, an 100,000-year interglacial interval in the
137 simulation is subjected to anthropogenic warming of the overlying water
138 and potential 60-meter changes sea level. Sensitivity studies are
139 presented for the biogenic and thermogenic methane production rates,
140 initial salinity, geothermal temperature gradient, rates of hydrological
141 flow, and permafrost impact on gas mobility.

142 **1.1.1 Permafrost**

143 One component of the simulation is a wedge of frozen sediment
144 (permafrost) submerged beneath the ocean on the continental shelf of
145 Siberia, left behind from glacial time when the shelves were exposed to
146 the frigid atmosphere by lowered sea level [*Romanovskii and Hubberten,*
147 *2001*]. The ice is thought to provide a seal to upward migration of
148 methane gas [*Shakhova et al., 2009*], especially where ancient fresh
149 groundwater flow produced a layer of very high saturation ice infill, a
150 formation called the Ice Complex in Siberia [*Romanovskii et al., 2000*],

151 although there are high ice saturations found in the Alaskan Arctic as well
152 [*Zimov et al.*, 2006].

153 With inundation by the natural sea level rise over the last 10+ thousand
154 years, the permafrost is transiently melting, although the time constant
155 for this is generally long enough that significant frozen volume remains,
156 especially in shallower waters which were flooded more recently
157 [*Khvorostyanov et al.*, 2008a; *Nicolosky and Shakhova*, 2010; *Romanovskii*
158 *and Hubberten*, 2001; *Romanovskii et al.*, 2004; *Shakhova et al.*, 2009;
159 *Taylor et al.*, 1996]. Even overlying water at the freezing temperature
160 can provoke subsurface melting by providing a warmer boundary
161 condition against which geothermal heat establishes the subsurface
162 temperature profile, but with climate warming, the waters could surpass
163 the freezing temperature, allowing heat to flow from above as well as
164 below [*Khvorostyanov et al.*, 2008b].

165 Elevated methane concentrations have been measured in the water
166 column over the Siberian shelf, even in areas of shallow water where the
167 permafrost should still be strongly intact [*Shakhova*, 2010; *Shakhova et*
168 *al.*, 2005]. Chemical and isotopic signatures of hydrocarbons adsorbed
169 onto surface sediments indicate a thermal origin [*Cramer and Franke*,
170 2005], suggesting that the methane is produced many kilometers deep in
171 the sediment column. The apparent ability for this methane to transverse
172 the barrier of the Ice Complex has been attributed to hypothesized
173 openings in the ice (called “taliks”), resulting from lakes or rivers on the
174 exposed shelf, or geologic faults [*Nicolosky and Shakhova*, 2010;
175 *Romanovskii et al.*, 2004; *Shakhova et al.*, 2009].

176 **1.1.2 Salt**

177 Dissolved salt in the pore waters can impact the timing of thawing
178 permafrost [*Nicolosky and Shakhova*, 2010; *Shakhova et al.*, 2009]. When
179 sea level drops and exposes the top of the sediment column to the
180 atmosphere and fresh water, the salinity of the subsurface pore waters
181 can be flushed out by hydrological groundwater flow, driven by the
182 pressure head from the elevated terrestrial water table above sea level.
183 The boundary between fresh and salty pore water tends to intersect the
184 sediment surface at the water’s edge [*Moore et al.*, 2011]. From there,
185 the boundary tends to dip landward, to a depth of approximately 40
186 meters below sea level for every 1 meter of elevation of the table water.
187 The ratio of water table elevation to freshwater lens depth is driven by

188 the relative densities of fresh and salt water, as the fluid seeks an
189 isostatic balance in which the fresh water displaces an equal mass of salt
190 water [Verrjuit, 1968].

191 The SpongeBOB model has been modified to simulate the processes
192 responsible for these observations. We do not attempt to simulate a
193 detailed outcropping history over 62 million-year spinup time of the
194 sediment column, but rather demonstrate the general process by
195 subjecting the nearly complete sediment column to a one-time sea level
196 lowering, exposing the continental shelf to groundwater forcing (see
197 **Supplemental Text S4**). After a few million years, the sediment column
198 subsides, due to compaction and absence of sediment deposition,
199 resulting in a sediment column that has been considerably freshened by
200 the atmospheric exposure. This freshening persists in the model for
201 millions of years, because there is no corresponding “salt-water pump”
202 during high sea-level stands. This behavior is consistent with the
203 discovery of vast nearly fresh aquifers in currently submerged continental
204 shelf regions around the world [Post *et al.*, 2013], left over from
205 groundwater forcing during glacial time.

206

1.1.3 Carbon

207 Another component of the simulation is the Yedoma, deposits of wind-
208 blown dust and organic carbon that accumulated on the coastal plains of
209 exposed continental shelves during glacial times [Zimov *et al.*, 2006].
210 The deposits contain a substantial fraction of organic carbon, consisting
211 of grass roots and remains, preserved by the freezing conditions. When
212 they thaw, they begin to release CO₂ and methane to the atmosphere
213 [Dutta *et al.*, 2006; Schuur *et al.*, 2008; Zimov *et al.*, 2006]. Oxidation
214 of the carbon can give off enough heat to accelerate the melting driven
215 by primary climate forcing [Khvorostyanov *et al.*, 2008b].

216 **1.2 Models of Methane Hydrate in the Permafrost Zone**

217 The dynamics of the permafrost layer, and its present state, have been
218 extensively modeled within detailed maps of the crust and sediment
219 structure [Gavrilov *et al.*, 2003; Nicolsky and Shakhova, 2010; Nicolsky *et al.*,
220 2012; Romanovskii and Hubberten, 2001; Romanovskii *et al.*, 2005].
221 Methane hydrate modeling has been done in the Arctic applied to the
222 Siberian continental slope [Reagan, 2008; Reagan and Moridis, 2009;
223 Reagan *et al.*, 2011], but only one calculation has been done in the

224 context of permafrost formation [*Romanovskii et al.*, 2005], as found on
225 the shelf. Romanovski [2005] modeled the extent of the methane
226 hydrate stability zone through glacial cycles, but based the calculations
227 on marine salinity values when calculating the stability of hydrate. I will
228 argue that in sub-freezing conditions (in the permafrost zone) the only
229 water available for hydrate formation will be in a saline brine that would
230 be in equilibrium with ice at the local temperature. This formulation
231 restricts hydrate stability from the permafrost zone to greater depth
232 below the sea floor than if the salinity was unaffected by formation of ice.

233 **1.3 Outline of This Work**

234 The model description in Section 2 begins with a description of the
235 previously published aspects of the SpongeBOB model as it is applied to
236 the Siberian margin (2.1). New developments in the code include
237 pressure-head driven groundwater flow (2.2), permafrost formation and
238 its impacts on the thermodynamics of ice and hydrate (2.3), and the
239 calculation of the methane flux to the atmosphere (2.4). The procedure
240 for generating the initial condition sediment column for the glacial /
241 interglacial cycles (2.5) is presented along with a description of the
242 forcings imposed to generate the glacial / interglacial cycles (2.6), and
243 the subsequent anthropocene (2.7). The formulation and rationale for
244 the sensitivity studies is given in Section 2.8.

245 The Results in Section 3 include a discussion of the model behavior
246 through the glacial / interglacial cycles (3.1), and in response to
247 anthropogenic global warming scenarios (3.2). A summary of model
248 sensitivity study results is given in Section 3.3, and comparison with field
249 observations in Section 3.4.

250 The Discussion in Section 4 includes the model limitations and critical
251 issues for future development (4.1), followed by the robust features of
252 the model simulations (4.2).

253 **2. Model Description**

254 **2.1 *SpongeBOB Application to the Siberian Continental Margin***

255 SpongeBOB is a two-dimensional basin spatial-scale and geological time-
256 scale model for the methane cycle in continental margin sediments. The
257 model, configured for a passive margin basin, was described by Archer et
258 al [2012], applied to the Atlantic coast of the United States. The

259 bottom boundary is bedrock, and accumulation time scales are millions of
260 years, as sediment is introduced as coastal riverine material, and settles
261 on the sea floor. Isostatic adjustment and crustal subsidence make room
262 for the accumulation of 5-10 km of sediment, which progrades seaward in
263 sigmoidal packages, driven by a maximum sediment accumulation rates
264 just off the shelf break.

265 Here the model framework is used as a representation of the continental
266 shelf of Siberia, although the tectonic and depositional histories of the
267 region are heavily impacted by vertical tectonic motions not represented
268 in the model. The crust underlying the continental shelf area has been
269 alternately rising and subsiding in blocks called horsts and grabens
270 [Nicolisky *et al.*, 2012]. The sediment cover on the grabens is thick much
271 thicker than it is in the horsts, thick enough for thermal methane
272 production. The thickness of the sediment cover in the model ranges
273 from 5 – 10 kilometers throughout the domain, reminiscent of the
274 grabens (subsiding blocks), because thermogenic methane is an essential
275 part of the simulations.

276 The model maintains a concentration of particulate organic carbon, with
277 which it predicts rates of methanogenesis. However, because the
278 depositional histories and organic carbon concentrations in the Siberian
279 continental margin are not well constrained, the rates of biological and
280 thermal methane production predicted by the model are unreliable
281 predictors of reality. For this reason, methanogenesis rates in the model
282 are scaled arbitrarily as tunable model inputs. The depth distributions of
283 the sources depend mostly on temperature, an easier variable to predict
284 than organic carbon degradation activity.

285 **2.2 New Model Development: Groundwater Hydrology**

286 **2.2.1 Pressure Head**

287 When the sediment column is exposed to the atmosphere, the pressure
288 field from the variable elevation of the water table (the pressure head)
289 begins to affect the fluid flow. The pressure head for a fluid particle at
290 the depth of the water table varies as

$$291 \quad P_{\text{head}}(z) = g \int_z^{z_{\text{wt}}} \rho_{\text{fluid}} dz$$

292 where z_{wt} is the elevation of the water table, which affects the pressure
293 throughout the fluid column, and the integral of the fluid density allows

294 the pressure at depth to be affected by the salinity and temperature of
 295 the water above. The depth of the water table is a pronostic variable in
 296 the model. In these simulations, however, the water table remains very
 297 close to the sediment surface, as unsaturated soil produced by
 298 subsurface flow is quickly replenished by hydrological recharge.

299

2.2.2 Pore Fluid Flow

300 The pressure head acts in concert with the excess pressure P_{excess} , as
 301 defined by Archer et al. [2012], to drive horizontal Darcy flow through
 302 the sediment. The value of P_{excess} is determined from the porosity and
 303 sediment load of the sediment in each grid box. An assumed sediment
 304 rheology is used to calculate the load-bearing capacity of the solid matrix
 305 within a given grid cell. P_{excess} is calculated by assuming that the load of
 306 the solid phase overlying the grid cell that is not carried by the solid
 307 matrix must be carried by the P_{excess} in the fluid phase.

308 The horizontal flow is

309
$$u_{\text{Darcy},i \rightarrow i+1} = \frac{k_{h,i} + k_{h,i+1}}{2\mu} \frac{(P_{\text{excess},i} - P_{\text{excess},i+1}) + (P_{\text{head},i} - P_{\text{head},i+1})}{(\Delta x_i + \Delta x_{i+1})/2}$$

310 while the vertical flow in the model is driven only by compaction pressure

311
$$w_{\text{Darcy},j \rightarrow j+1} = \frac{k_{v,j}}{\mu} \frac{P_{\text{excess},j} - P_{\text{excess},j+1}}{(\Delta z_j + \Delta z_{j+1})/2}$$

312 where $k_{h,i}$ is the horizontal permeability at horizontal cell index j , $k_{v,j}$ is
 313 vertical permeability at vertical index j , μ is the viscosity, and Δx and Δz
 314 are cell dimensions. Notes on numerical issues are given in [Supplemental](#)
 315 [Text S1](#).

316

2.2.3 Canyons

317 The model as described so far represents a laterally homogeneous slab, a
 318 poor approximation for hydrology above sea level because of the
 319 formation of canyons and river networks in a real drained plateau. The
 320 depth of the water table in a river canyon is depressed, relative to the
 321 surroundings, to the depth of the canyon. The water table is higher in
 322 between the canyons because of recharge, and the difference in head
 323 drives lateral flow, the canyons acting to drain the sediment column.

324 The model formulation has been altered to represent this mechanics in a
325 simplified way. Rather than expand the model into the full third
326 dimension, the 2-D field of the model is held to represent the sediment
327 column at a hypothetical ridge crest, as altered by an adjacent canyon.
328 The canyon elevation is represented by z_{canyon} , and its width by a scale
329 Δy_{canyon} . A cross-column flow velocity $v_{\text{Darcy},j}$ is calculated as

$$330 \quad v_{\text{Darcy},j} = \frac{k_{h,j} (P_{\text{head,canyon}} - P_{\text{head}})}{\mu \Delta y_{\text{canyon}}}$$

331 where $P_{\text{head,canyon}}$ is the pressure head as a function of depth in the
332 hypothetical canyon, calculated assuming that the water table outcrops
333 at z_{canyon} , and that the temperatures in the sediment column have
334 adjusted to the formation of the canyon, such that the near-surface
335 geothermal gradient is the same between the hypothetical canyon and
336 the bulk sediment column. The lateral “drainage” flow ($v_{\text{Darcy},j}$) drives
337 vertical velocities by continuity.

338 The horizontal distance scale Δy_{canyon} is somewhat arbitrary and difficult to
339 constrain, given that in the reality of river networks the distance to the
340 nearest canyon from any point in the domain is likely to be a function of
341 altitude, distance from the coast, and time. Another poorly resolved
342 factor is the depth of the canyon. In reality, canyons cut into a plateau
343 following a dynamic that erosion is proportional to slope, stopping at sea
344 level. As a simplification the model is set to hold the canyon depth at
345 current sea level throughout the simulation.

346 In the real fractal geometry of canyons, the spacing between canyons
347 across a plain is similar to the width of the plain (length of the canyons),
348 so the Base simulation assumes a canyon width of 100 km, based on the
349 100+ km width scale of the continental shelf.

350 **2.3 Permafrost**

351 **2.3.1 Thermodynamics of Ice and Hydrate**

352 The ice model is based on an assumption of thermodynamic equilibrium, in
353 which the heat content of the cell is distributed between the pure ice,
354 hydrate, and brine phases, while the salt content is restricted to the
355 brine. Notes on numerical implementation are given in [Supplemental Text](#)
356 [S2](#).

357 In the permafrost zone where ice is present, the salinity of the brine
358 creates an ice-freezing point depression that matches the local
359 temperature. This equilibrium salinity is higher than methane hydrate can
360 tolerate, excluding hydrate from thermodynamic stability. For a more
361 detailed examination of the role of the brine salinity in determining the
362 relative stabilities of ice and hydrate, see [Supplemental Text S3](#).

363 **2.3.3 Other Impacts**

364 Permafrost formation has several impacts on the methane cycle in the
365 model. Biogenic methanogenesis is assumed stopped in the ice fraction
366 of a grid cell (which approaches unity but never reaches it in the model,
367 due to exclusion of salt into brine). Bubble transport in the model
368 balances bubble production, driven by a small and not very well
369 constrained standing bubble concentration within the pore space. It is
370 generally assumed [*Shakhova et al.*, 2010b] that permafrost inhibits gas
371 transport through the sediment column, both based on sediment column
372 carbon and hydrogen budgets [*Hunt*, 1995] and on the tight seal
373 provided by the ice complex. The seal provided to Arctic lakes, which can
374 drain overnight if the seal is breached, also lends credence to this idea. In
375 the model, this effect was simulated by stopping gas transport
376 completely when a grid cell exceeds 50% ice fraction (with sensitivity
377 runs assuming 10%, 30%, 70%, and 90%).

378 **2.4 Atmospheric Methane Fluxes**

379 Bubbles emerging from the sediment column into the water column of the
380 ocean may dissolve in the water column, or they may reach the sea
381 surface, a direct methane flux to the atmosphere [*Westbrook et al.*,
382 2009]. In the model, bubble dissolution in the water column is assumed
383 to attenuate the bubble flux according to the water depth with an e-
384 folding attenuation scale of 30 meters [*Gentz et al.*, 2014; *Portnov et al.*,
385 2013; *Westbrook et al.*, 2009]. In reality, a low-flux gas seep, producing
386 small bubbles, will probably not reach as far into the water column as a
387 30-meter scale height, while a faster seep can reach further. Methane
388 dissolved in the water column, in reality, may survive oxidation (time
389 constant of about a year), and degas to the atmosphere, but this
390 possibility is not included in the model. For land grid points (exposed to
391 the atmosphere by lowered sea level), any upward bubble flux at the
392 sediment surface is assumed 100% released to the atmosphere. The
393 model neglects methane oxidation in soils, as well as many other

394 terrestrial processes such as thaw bulbs beneath bodies of water [*Walter*
395 *et al.*, 2006], and the seasonal cycle of melting and thawing in the
396 surface active layer. See discussion in [Section 4.1](#).

397 **2.5 Initial Condition**

398 **2.5.1 Rational for Spinup**

399 The point of the spinup phase is to generate an initial condition for the
400 glacial cycle simulations. The more usual approach in modeling hydrates
401 is to start with an ad-hoc initial condition [*Reagan*, 2008; *Reagan and*
402 *Moridis*, 2009; *Reagan et al.*, 2011]. For SpongeBOB the model state at
403 any time is the result of the time-history of sedimentation, which is driven
404 by the time-evolving depth of the sea floor, and interacting with isostatic
405 adjustment of the crust. The simplest way to generate an initial condition
406 in the model without a startup transient is to spin the model up from
407 bedrock. The duration of the spinup phase is 62 million years, roughly
408 consistent with the time scale since the opening of the Laptev Rift. The
409 first 60 Myr used a relatively coarse resolution as shown in [Figure 1a](#). For
410 the glacial / interglacial experiments, the initial condition was interpolated
411 to a higher resolution grid in the vertical, as shown in [Figure 1b](#).

412 **2.5.2 Sediment Column Salt Content**

413 When sea level drops such that the surface of the sediment column
414 outcrops to the atmosphere, the pore fluid becomes subject to the
415 pressure head driving it seaward, and to fresh water recharge from
416 precipitation. The pressure head forcing and the buoyancy of the
417 sediment fluid column combine to create a mechanism to excavate
418 salinity from the upper sediment column, to depths well below sea level.
419 The salinity of the sediment column tends to be ratcheted down by
420 exposure to the atmosphere, because there is no comparable advective
421 pump for reinvasion of seawater when sea level rises.

422 A “pre-freshened” sediment column was constructed by dropping sea
423 level by 120 meters and holding it there for millions of years. The
424 sediment column subsides back into the ocean over a few million years,
425 but the fresh imprint of the hydrological flow persist for millions of years
426 ([Figure 2a](#) and [Supplemental Text S4](#)). If the sediment surface never
427 outcrops, the pore salinities remain nearly uniform and marine ([Figure 2b](#)).
428 Particulate organic carbon (POC) concentrations are highest just off the
429 shelf break ([Figure 3](#)), because this is where most of the sediment is

430 deposited, and because the sedimentary material is richest in POC in
431 shallow ocean water depths [*Archer et al.*, 2012]. Methane concentration
432 (Figure 4a) closely mirrors the solubility of dissolved methane, resulting in
433 near saturation concentrations through most of the model domain (Figure
434 4b). The pre-freshened (Fr) versus marine (Mr) initial conditions are
435 taken as end member salinity sensitivity runs (see Table 1).

436 **2.6 Glacial Cycle Forcing**

437 Beginning from an entirely submerged initial condition, the model is
438 subjected to 100-kyr sawtooth cycles of sea level ranging between -120
439 to +20 meters from the initial sea level (starting at -120 for
440 prefreshened, 0 for pure marine) (Figure 5a). The model forcing scenarios
441 are summarized in Table 1.

442 **2.6.1 Sea Level**

443 The simplest scenario (SL) varies the sea level while keeping the air and
444 water temperatures time-invariant. The sea-level air temperature is
445 maintained at 0 °C. This simulation is nearly permafrost-free, with a small
446 exception where the altitude of the sediment surface is much higher than
447 sea level (due to the lapse rate in the atmosphere). There is no
448 deposition of sediment above sea level in this simulation.

449 **2.6.2 Glacial Climate**

450 Permafrost formation is added in simulation GL, in which the air
451 temperature ramps down to -16 °C at sea level, linearly with the glacial
452 sea level fall (Figure 5b). In the ocean, shelf waters are always -1.8 °C,
453 but an interglacial subsurface temperature maximum of 1 °C at 200
454 meters decreases to -1.8 °C during glacial times.

455 **2.6.3 Deposition of Carbon on Land**

456 Deposition of organic-rich sediments when the surface is exposed to the
457 atmosphere (Yedoma: represented as accumulation of 10 meters in 100
458 kyr, with 30% POC) is added in scenarios SL+LD and GL+LD (LD for land
459 deposition).

460 **2.7 Anthropogenic Global Warming Forcing**

461 **2.7.1 Long-Term Climate Impact from CO₂ Addition**

462 The global warming (GW) scenario begins from a high sea-level interglacial
463 state, and raising the temperature following the climate impact of the
464 “spike and long tail” time distribution of a slug of new CO₂ added to the
465 atmosphere [Archer *et al.*, 2009] (Figure 8). There is a stage of fast
466 atmospheric drawdown as CO₂ invades the ocean, but once the ocean,
467 atmosphere, and land surface reach equilibrium (after a few hundred
468 years), the CO₂ content of the entire biosphere begins to relax toward an
469 initial “natural” value, on time scales of hundreds of thousands of years,
470 by weathering reactions with carbonate and siliceous solid rocks. The net
471 result is a CO₂ drawdown that can be expressed as the sum of several
472 exponential functions in time, with time scales ranging from 10² – 10⁶
473 years.

474 Changes in water column temperature are assumed equal to those of the
475 atmosphere, following paleoceanographic reconstructions [Martin *et al.*,
476 2002] and long-term coupled ocean / atmosphere circulation model
477 experiments [Stouffer and Manabe, 2003]. The GW scenario imposes this
478 temperature change on the water column, relaxing toward equilibrium
479 with the atmospheric CO₂ trajectory with a time constant of 100 years.

480 **2.7.2 Long-Term Behavior of Sea Level**

481 The effect of sea level rise is added to create a second global warming
482 scenario GW+SL. On time scales of thousands of years the sea level
483 response to changing global temperature is much stronger than the sea
484 level response over the coming century, as prominently forecast by the
485 IPCC. Reconstruction of sea level and global temperature covariation in
486 the geologic past (glacial time to Eocene hothouse) reveals a covariation
487 of 10-20 meters per °C [Archer and Brovkin, 2008]. The global warming
488 with sea level scenario assumes an equilibrium sea level response of 15
489 meters / °C, which it relaxes toward with a time constant of 1000 years.

490 **2.8 Sensitivity Studies**

491 A strategy for dealing with the many uncertainties in the model
492 formulation and parameterization is to do sensitivity studies, to
493 determine which of the unknowns are most significant. The model
494 sensitivity studies are summarized in Table 1. Sensitivity studies to the

495 rates of methane production have already been mentioned, as have the
496 pre-freshened versus marine initial conditions, representing uncertainty in
497 the salt content of the sediment column. Other model sensitivity runs
498 include the geothermal temperature gradient, and a parameterization of
499 permafrost inhibition of bubble migration. Several altered-physics runs
500 were done, one adding vertical permeable channels, one disabling
501 horizontal flow, and several to evaluate the impact of ice formation on
502 methane hydrate stability.

503 **3. Results**

504 **3.1 Glacial Cycles**

505 **3.1.1 Salinity**

506 In the “prefreshened” initial condition (Fr), millions of years have elapsed
507 since the previous exposure of the sediment to hydrological forcing, but a
508 core of fresh water remains. Salinities near the sediment surface have
509 grown saltier due to diffusive contact with seawater (Figure 6, left). A
510 fully marine initial condition (Mar) (Figure 6, right) was initialized from the
511 unfreshened case, in which sea level was held at a fixed value throughout
512 the 65 Myr spinup of the sediment column. The salinities are nearly
513 uniform in this case.

514 When the sediment surface is re-exposed to the atmosphere during an
515 interval of low sea level, in the absence of ice formation (simulation SL),
516 the surface layer tends to freshen relatively quickly due to the
517 hydrological forcing, although a subsurface salinity maximum persists
518 (Figure 6c and d). If the air temperatures are cold enough to form ice
519 (simulation GL), surface salinities in the model increase to up to nearly
520 190 psu, in both prefreshened and pure marine cases (Figure 6e and f).
521 By the next interglacial time (Figure 6g and h), ice near the sediment
522 surface has melted enough for near-surface pore waters to reach
523 relatively low salinities.

524 **3.1.2 Pressure and Flow**

525 The effect of the glacial / interglacial sea level and climate forcing on the
526 pressures and flow velocities are shown in Figure 7. On a spatial scale of
527 the entire model domain (Figure 7, left), the highest driving pressures are
528 found at the base of the sediment column, underneath the region of
529 maximum sediment accumulation (the depocenter just off the shelf

530 break). Changes in sea level drive large fluctuations in the pressure head
531 (contours) extending to bedrock. In the near-surface continental shelf
532 (Figure 7, right), the driving pressure variations are dominated by the
533 pressure head, driven by sea level changes. The formation of permafrost
534 (GL, Figure 7 e and f) seals the upper sediment column to fluid flow.

535 When sea level rises again, in the model configuration including
536 permafrost, there is a strong pulse of downward flow following partial
537 melting of the permafrost (Figure 7 h). It is possible that this flow, which
538 lasts a few thousand years, is an artifact of the elastic model
539 configuration, in which the release of a load (by submergence of the
540 upper sediment column into the ocean) provokes the expansion of pore
541 spaces in the sediment. The anomalous flow, integrated over its duration,
542 could displace the pore fluid by about 40 meters, which is less than one
543 grid cell. The model configuration without the sealing effect of permafrost
544 (SL) does not show this pulse of invasive flow on sea level rise.

545

3.1.3 Methane Cycle

546 There are multiple ways in which the glacial cycles of sea level and air and
547 water temperature might impact the flux of methane to the atmosphere.
548 Submergence in the ocean is one modulating factor, because the
549 emerging bubbles dissolve in the ocean rather than reaching the
550 atmosphere. Another factor is the deposition of high-POC surface soils
551 during low sea level stands, and its exposure to degradation later when
552 the permafrost soils melt. A third factor is permafrost, impeding gas and
553 fluid flow and excluding dissolved methane and salt from ice formation.
554 The impacts of these processes are assessed by comparing the results
555 from model configurations with and without each process in question.

556 **Ice vs. Hydrate.** The impact of phase competition between ice and
557 hydrate is shown in Figure 8. In the Base scenario (Figure 8a and c)
558 hydrate stability is excluded from the permafrost zone as described in
559 Supplemental Text S3. Preventing ice from forming in an altered-physics
560 simulation (+ No Ice) decreases the fluid-phase salinity relative to the
561 Base simulation, and allows the methane hydrate stability zone to nearly
562 reach the sea floor (Figure 8b and d), during strongest glacial conditions.
563 Another altered-physics simulation was done in which ice is allowed to
564 form, but not affect the salinity as it drives methane hydrate stability
565 (which was hard-wired to marine salinity). Methane hydrate is still
566 unstable in the permafrost zone through most of the simulation (see

567 movie files in supplemental material), indicating that thermal interaction
568 must also have a strong impact on methane hydrate stability in the
569 permafrost zone.

570 **Dissolved Methane.** The evolution of the dissolved methane
571 disequilibrium condition ($\text{CH}_4 / \text{CH}_{4 \text{ sat}}$) is shown in **Figure 9**. At the
572 initiation of the glacial cycles, methane is undersaturated in near-surface
573 sediments on the continental shelf, by diffusive contact with the
574 methane-free ocean upper boundary condition. In the prefreshened
575 sediment column scenario (Fr), methane concentrations in the depth
576 range of 100-1000 meters are lower than in the marine case (Mar, **Figure**
577 **9b**), due to the ventilation by the hydrological pump (**Figure 9a**). Further
578 freshening of the pore waters in the ice-free case (SL+LD) tends to
579 deplete methane in the upper sediment column (**Figure 9c-e**), while
580 methane exclusion from the permafrost ice leads to supersaturation in
581 simulation GL+LD (**Figure 9f-h**). The hydrate stability zone is somewhat
582 expanded in the prefreshened sediment column relative to the marine
583 case (**Figure 9 g vs. h, heavy black contour**).

584 **Methane Sources.** **Figure 10** shows snapshot sections of various
585 aspects of the shelf carbon cycle, beginning from a prefreshened initial
586 condition. Sections of POC concentration in **Figure 10, left** show the
587 accumulation of POC-rich Yedoma deposits on land (**Figure 10 g and j**).
588 The rate of methane production in the model (**Figure 10, right**) depends
589 on temperature and organic carbon age, but it is also attenuated by
590 permafrost formation in the model, scaling to zero in the completely
591 frozen case. Methanogenesis rates are near zero in the permafrost zone
592 during glacial time (**Figure 10h**), but partially recover during interglacial
593 time (**Figure 10k**) even though permafrost is still present.

594 **Hydrate.** A zone of methane hydrate stability exists below the
595 permafrost zone when permafrost is present, and some methane hydrate
596 accumulates in that zone. The highest pore-fraction values are found
597 near the continental slope, where the shelf stability field outcrops within
598 the slope depocenter. Dissolved methane concentrations exceed
599 saturation within the stability zone in the model (**Figure 9**), but the
600 accumulation of methane hydrate (**Figure 10, right**) is limited by the rate
601 of methane production.

602 Time series plots of the inventory of methane as hydrate on the shelf are
603 shown in **Figure 11**. The integration cuts off at $x=560$ km to exclude the

604 sediment depocenter on the continental slope. Hydrate inventories reach
605 maximum values during deglaciations. There is more hydrate when the
606 pore water is fresher, and there would be more if ice were excluded from
607 forming (Figure 11a). The hydrate inventory is much more sensitive to
608 thermogenic methane production, deep in the sediment column, than
609 Yedoma deposition (Figure 11b). The impact of the geothermal heat flux
610 is to change the depth of the bottom of the hydrate stability zone
611 (Figure 18 e and f), but the impact is small on the hydrate inventory,
612 unless the temperature gradient is so low that hydrate persists through
613 the entire glacial cycle (Figure 11c). The hydrate forms from the
614 dissolved methane pool, which exceeds 1000 Gton C in shelf porewaters
615 of the model.

616 **Permafrost, Ocean, and Atmospheric Methane Flux.** The impact
617 of the glacial cycles on the methane pathway to the atmosphere in the
618 model is shown in Figure 12. When sea level is high, the efficiency of
619 bubble transport across the sediment-water interface reaching the
620 atmosphere ranges from about 75% near the coast to about 10% at the
621 shelf break (Figure 12a). Most of the methane flux from the sediment is
622 located just off the shelf break (Figure 12e), where the escape efficiency
623 is low, so not much methane makes it to the atmosphere during the
624 interglacial. During glacial times, the sediment column is exposed to the
625 atmosphere, and the escape efficiency in the model is 100% (Figure
626 12b). Permafrost inhibits the terrestrial methane flux (Figure 12i)
627 relative to the case without permafrost (Figure 12f). During some
628 deglaciations, the release of pent-up gas by permafrost degradation leads
629 to a spike of excess methane flux to the atmosphere (Figure 12j-k
630 relative to 12g-h).

631 **Budget.** Time series plots of the major fluxes of the methane cycle on
632 the continental margin are shown in Figure 13. The methanogenesis rates
633 in the model output are in units of moles per meter of coastline, since it is
634 a 2-D model. We scale this up to the Siberian continental margin by
635 assuming a width of 1,000 km. The area of the shelf is then $5 \cdot 10^{11} \text{ m}^2$,
636 roughly comparable to the real shelf area of 460,000 km² [Stein and Fahl,
637 2000]. The biological rate of methane production on the continental shelf
638 evolves through time in Figure 13b. Yedoma deposition (case SL+LD)
639 tends to slowly increase the total shelf respiration rate in the model,
640 relative to a case with no land deposition (case SL). The formation of

641 permafrost, during glacial periods of case GL+LD, attenuates
642 methaneogenesis by inhibiting biological activity in the frozen soil.

643 The solid regions in **Figure 13 c-h** are cumulative methane sinks for six
644 different model scenarios, plotted underneath red lines showing biogenic
645 methane production. In time average, where sinks balance sources, the
646 colored areas should fill up the region below the red line.

647 Trapping of methane by impermeable permafrost leads to a spike of
648 methane fluxes at the ends of deglaciations in simulations with
649 permafrost (**Figure 13 c and e**). The spikes happen as sea level
650 approaches its highest extent, stifling the offshore groundwater flow by
651 decreasing the pressure head, but early in the interglacial time while
652 permafrost is the most intact. The spikes are stronger for the first glacial
653 cycles than the last, apparently due to long-term adjustment of the
654 methane cycle on the shelf (a growing together of the production rate
655 (red lines in **Figure 13 c-f**) and the various methane sinks (colored areas).

656 Permafrost formation blocks methane emission during times of low sea
657 level. This can be seen in the collapse of the blue regions in **Figure 13 c**
658 **vs. d and e vs. f** during times of low sea level. Blocking horizontal flow
659 disrupts offshore flow, the only significant methane sink on the shelf
660 during glacial periods (**Figure 13h**), resulting in somewhat higher deglacial
661 spikes of methane emission than predicted by the models including
662 transport. There is no direct link between ice fraction and methane
663 oxidation in the model, which is driven only by coexisting concentrations
664 of sulfate and methane, but the rate of methane oxidation also drops to
665 negligible during glacial times in the simulations with permafrost (grey in
666 **Figure 13 c and e**). The absolute rates of methane loss differ between
667 the Prefreshened vs. Marine initial conditions, but this is in part due to
668 differences in the width of the continental shelf between the two
669 simulations. The patterns of the methane cycle are very similar, however,
670 between the two cases, and also not much affected by the imposition of
671 permeable vertical channels (**Figure 13g**).

672 **Atmospheric Flux.** Fluxes of methane to the atmosphere are shown in
673 **Figure 14**. In the absence of permafrost (**Figure 14 a and b**), or assuming
674 that bubble migration is blocked only if the ice fraction exceeds 90%, a
675 condition rarely attained in the model (**Figure 14e**), the highest methane
676 fluxes to the atmosphere are found during glacial (cold) times, rather
677 than warm interglacials. This is due to dissolution of methane gas into

678 the ocean when the sediment column is submerged. When permafrost
679 blocks methane gas fluxes in the sediment column, the highest
680 atmospheric fluxes are generally found during the time of early sea level
681 fall, when unfrozen sediment is exposed to the atmosphere before it has
682 a chance to freeze. The timing of the variations in atmospheric flux
683 through the glacial cycles is very sensitive to the critical ice fraction for
684 blocking gas transport (Figure 14e).

685 The impacts of the pore water salt inventory are most apparent during
686 the time of sea level fall, with permafrost formation (red lines). The
687 saltier sediment column takes about 20 kyr to choke off the methane flux
688 to the atmosphere (Figure 14a), while the pre-freshened sediment
689 column stops the methane flux more abruptly, in just a few thousand
690 years (Figure 14b). Atmospheric emissions also scale with methane
691 production rates, generally maintaining the temporal patterns of emission
692 as set by permafrost and submergence in the ocean.

693 **3.2 Anthropogenic Global Warming**

694 The atmospheric methane fluxes, shown in Figure 15, increase in the
695 global warming (GW) model run, as they also do in the control (Ctl)
696 simulation, which is essentially an extended but unwarmed interglacial
697 period. The permafrost melts on a time scale of about 10,000 years for
698 the GW simulation, and about 50,000 for the Ctl. The rates of methane
699 production, and flux to the atmosphere, both increase with the loss of the
700 permafrost, if there is no change in sea level. However, the new methane
701 flux comes not as a sudden burst, but rather as a slow transition toward a
702 new, higher, chronic release rate.

703 When sea level is also changed (GW+SL), bubbles dissolve in the water
704 column, which more than counteracts the increase in methane flux due to
705 the extended interglacial (Ctl) or warming (GW) scenarios.

706 **3.3 Sensitivity Studies**

707 **3.3.1 Sediment Salt Content**

708 Ice freezes until the salinity of the residual brine brings about a freezing
709 point depression equal to the in situ temperature. A saltier initial
710 sediment column will reach this condition with a lower ice fraction, its
711 melting is accelerated, and its hydrate inventory is lower (Figure 14).
712 The equilibrium salinity in the permafrost zone is not affected by the salt

713 inventory of the column, only the relative volumes of the solid and fluid
714 phases.

715 **3.3.2 Methane Production Rates**

716 The atmospheric flux increases along with either shallow, biological
717 methane production, driven by deposition of Yedoma, or thermal methane
718 production in the deep sediment column (Figure 15). Biogenic methane
719 production is too shallow in the sediment column to impact the inventory
720 of methane hydrate (Figure 11). The timing through the glacial cycles of
721 atmospheric methane emissions from these scenarios parallel each other,
722 because they are controlled in common by the transport-blocking effects
723 of permafrost and sediment submergence in the ocean.

724 **3.3.3 Geothermal Temperature Gradient**

725 When the heat flux is higher, the temperature gradient is steeper,
726 pivoting about the sediment surface temperature, which is set by the
727 ocean. The base of the methane hydrate stability boundary gets
728 shallower, while the top remains at about the same depth, resulting in a
729 thinning of the stability zone (Figure 8). The hydrate inventory through
730 the glacial cycles however is not much affected, unless the heat flux gets
731 small enough for hydrate to persist through the glaciations (Figure 11).

732 **3.3.4 Thermodynamic Competition Between Ice and Hydrate**

733 When ice is included as a competing phase, it excludes methane hydrate
734 from the low-pressure, very cold permafrost zone. The hydrate stability
735 zone thins (from above and below in the model: Figure 8), and the
736 hydrate inventory decreases (Figure 11). When ice formation is
737 disallowed, the hydrate stability zone approaches the sediment surface
738 during coldest glacial time, but by the time of an interglacial-based global
739 warming climate perturbation, the stability zone boundary has retreated
740 to several hundred meters below the sea floor, precluding a sudden
741 hydrate dissolution response to a suddenly warming ocean.

742 **3.3.5 Permafrost Inhibition of Gas Migration**

743 When the ice fraction of the model exceeds a critical threshold, gas
744 migration is blocked. Changing the value of this threshold has a strong
745 impact on the rates of methane emission during glacial versus interglacial

746 times. This process is therefore a high priority for future model
747 refinement.

748 **3.3.6 Vertical flow heterogeneity**

749 The chemistry of continental margin sediments in this model [*Archer et*
750 *al.*, 2012] showed a strong sensitivity to flow heterogeneity, achieved by
751 increasing the vertical permeability of every fifth grid cell. In the
752 configuration presented here, the impact of the channels is much smaller.
753 The dynamics of this simulation are thermally driven, rather than by
754 sediment deposition driving fluid flow in the continental margin case.
755 Atmospheric methane fluxes are spikier when the channels are included,
756 but the mean rate is not much changed.

757 **3.3.7 Ground water Flow**

758 Groundwater flow carries enough methane to be a significant sink during
759 times of low sea level. However, disabling that flow has only subtle
760 impacts on the other aspects of the methane cycle on the shelf. Spikes
761 of methane emission during late deglaciation get somewhat more intense.

762 **3.4 Comparison with Observations**

763 The model bubble flux to the atmosphere in the base case in analog
764 present-day conditions is 0.02 Tg CH₄ per year, which is an order of
765 magnitude lower than an estimate of the total methane emission rate
766 from the sea surface (bubbles + gas exchange) [*Kort et al.*, 2012] of 0.3
767 Tg CH₄ / yr. The model does not include gas exchange evasion of
768 methane from the sea surface, which could be significant. Concentrations
769 of methane in the water column of 50 nM are common [*Shakhova et al.*,
770 2010a], which, if they were unimpeded by sea ice, could lead to a flux
771 from the region of 0.4 Tg CH₄ / yr (assuming a typical gas exchange
772 piston velocity of 3 m/day). Gas exchange is impeded by sea ice, but it
773 can be enhanced by storms [*Shakhova et al.*, 2013]. Once released to
774 the water column, the fate of a methane molecule will depend on its
775 lifetime with respect to oxidation, which could be up to a year in the open
776 water column [*Valentine et al.*, 2001], versus its lifetime with respect to
777 gas exchange, which for ice-unimpeded conditions would be just a few
778 months for a 50-meter deep water column. Thus the methane in bubbles
779 dissolving in the water column has some chance of making it to the
780 atmosphere anyway, depending on stratification in the water column and

781 the extent of ice, and the gas exchange flux has the potential to be
782 significant in the regional total flux.

783 Methane fluxes into the water column range up to 0.4 Tg CH₄ / yr during
784 times of relatively high sea level. This is much lower than the Shakhova
785 et al. [2013] estimate of 17 Tg CH₄ / yr from hot-spot ebullition fluxes
786 to the water column. The model fluxes are comparable to these
787 observations when the thermal methane flux is increased by a factor of
788 100 (see [Section 3.3.2](#)), but the model lacks the physical or mechanistic
789 detail required to focus the emissions into hot spots of concentrated
790 methane flux as observed ([Section 4.1](#)).

791 **4. Discussion**

792 ***4.1 Limitations of the Model Results and Critical Issues for Future*** 793 ***Development***

794 This is the first simulation of the full methane cycle on the Siberian
795 continental margin, or any other location with embedded permafrost soils,
796 including hydrate formation and transient fluxes. It is internally
797 consistent, linking processes from the ocean, the sea floor, and the deep
798 Earth, within constraints of sediment accommodation and conservation of
799 carbon, through geologic time. As such it has some lessons to teach
800 about the real Siberian continental margin. However, many of the model
801 variables are not well known, such as the methanogenesis rates or soil
802 permeabilities, meaning that in some aspects the model results are not a
803 strong constraint on reality. These uncertainties illuminate critical issues
804 for future model refinement.

805 **4.1.1 Methane Production Rates**

806 The rates of biological and thermal methane production on the Siberian
807 continental shelf are not well constrained by laboratory measurements or
808 field inferences. These rates are treated as tunable model parameters,
809 and the sensitivity studies show that they are important ones to
810 ultimately get right.

811 **4.1.2 Gas Transport in the Sediment Column**

812 Simulating the hot-spot behavior of bubble emission from the sea floor
813 will also require more detailed treatment of the mechanisms by which gas
814 moves around in the sediment column. The model lacks faults and

815 permeable layers that act as transport highways and hydrate
816 depocenters, and may concentrate the flow into a hot-spot ebullition
817 region. The model also lacks the ability to episodically “blow out”,
818 producing the sedimentary wipe-out zones observed seismically in the
819 subsurface [*Riedel et al.*, 2002], and the pockmarks at the sediment
820 surface [*Hill et al.*, 2004]. The steady-state hydrate inventory in the
821 model is extremely sensitive to the bubble vertical transport spatial scale
822 [*Archer et al.*, 2012], which determines how far a bubble can get through
823 unsaturated conditions before it redissolves. This result demonstrates
824 the importance of gas transport to predicting the methane hydrate or
825 bubble inventories.

826 **4.1.3 Atmospheric Flux Efficiency**

827 On land, the model lacks seasonal melting of surface permafrost, and the
828 thaw bulbs underneath lakes and rivers. In the ocean, the fraction of the
829 sea-floor gas flux which dissolves in the water column intensity of water
830 column dissolution of rising bubbles depends on the bubble sizes, which
831 depend on the gas emission rate, ultimately driven by details of gas
832 transport in the sediment.

833 **4.1.4 Uncertainty in Model Output**

834 These uncertainties affect the flux of methane to the atmosphere, and
835 model predictions of the standing stocks of methane as gas and hydrate
836 in the sediment column.

837 **4.2 Robust Features of the Simulation**

838 **4.2.1 Arctic Ocean Methane Fluxes are Small in the Global Budget**

839 The model is consistent with observations [*Kort et al.*, 2012], that the
840 total atmospheric methane flux from the Siberian margin is a small
841 fraction of the global flux of methane to the atmosphere, and thus
842 represents only a minor climate forcing. The model would have to be
843 pushed very hard (as would the measurements) to fundamentally change
844 this conclusion.

845 **4.2.1 The Hydrological Salinity Ratchet**

846 Groundwater flow, driven by the pressure head, provides an advective
847 means of pumping fresh water into the subsurface sediment column that
848 has no counterpart for salty ocean water. The model lacks the mechanism

849 of salt fingering, which can enhance the diffusion of salt from above into
850 a fresh water aquifer [*Kooi et al.*, 2000]. However, higher-resolution
851 models of smaller domains that accounted for salt fingering also show a
852 time asymmetry, with faster fresh water invasion on sea level drop than
853 salt invasion on sea level rise [*Lu and Werner*, 2013; *Watson et al.*,
854 2010]. As the size of the domain increases with increasing sea level
855 change, advective processes such as hydrological flow should become
856 even more dominant over diffusive processes such as salt fingering. The
857 recent discovery of vast freshwater aquifers on global continental shelves
858 [*Post et al.*, 2013], persisting since the time of lowered sea level 20,000
859 years ago, and the lower-than-marine salinities of the pore waters
860 measured in submerged surface Arctic sediments (summarized by
861 [*Nicolisky et al.*, 2012]) are also consistent with the existence of a fresh-
862 water hydrological pump which has a significant impact on sediment
863 column salinities.

864 **4.2.2 Salinity (Water Activity) and Hydrate Stability in the Permafrost Zone**

865 In the simulations the porewater salinities in the permafrost zone did not
866 depend on the total salt content of the sediment column, but only on the
867 temperature (and secondarily pressure) condition. A saltier sediment
868 column will end up with a larger volume of brine in equilibrium than a
869 fresher sediment column would have, but the salinities of the brines would
870 be the same.

871 In the permafrost zone (low temperature and pressure), ice can tolerate
872 higher salinity (lower water activity) than methane hydrate can. As long
873 as there is no kinetic impediment to ice formation, bubbles of methane
874 rising into this zone should encounter brine salinities too high to permit
875 formation of methane hydrate.

876 **4.2.3 Sea Level Dominates the Glacial Cycle of Methane Flux**

877 The methane flux to the atmosphere through the glacial / interglacial
878 cycles is highest during cold times, because sea level is low, rather than
879 providing a positive climate feedback by releasing methane during warm
880 (high sea level) intervals. Atmospheric methane concentrations were
881 lower during glacial times than interglacials, but since the Arctic Ocean is
882 a small fraction of the total methane budget (Section 4.1.2), the
883 atmospheric concentration does not necessarily reflect Arctic fluxes.

884 4.2.3 Methane Emission Response to Anthropogenic Climate Change

885 There is a warming positive feedback in the simulated future from climate
886 warming, with fluxes rising gradually on a time scale of thousands of
887 years. Shakhova et al [2010b] proposed that 50 Gton C as methane
888 could erupt from the Arctic on a time scale of a few years. However, the
889 thermodynamic exclusion of methane hydrate from the permafrost zone
890 (Section x.xx) ensures that methane hydrate will be isolated from
891 changes in ocean temperature by ~400 meters of mud and ice. A
892 warming perturbation at the sea floor today will not reach this depth for
893 hundreds or thousands of years. A complex model is not really required
894 to conclude that methane hydrate will probably not produce a methane
895 eruption of this scale so quickly.

896 Could an abrupt methane release arise from release of trapped bubbles
897 from melting ice? The model actually does produce a glacial cycle in
898 bubble inventory, with changes exceeding 50 Gton over a cycle,
899 apparently driven by methane exclusion from ice formation (Figure 11).
900 But the model does not deliver an abrupt release in response to
901 anthropogenic warming for any of its sensitivity studies (Figure 14). We
902 would get a faster initial response to global warming if the transition from
903 glacial to global warming sediment surface temperatures hadn't mostly
904 happened thousands of years ago.

905 The model provides poor constraint on the standing stock of bubbles or
906 methane hydrate in the sediment column, and neglects many of the
907 mechanisms that could come into play in transporting methane quickly to
908 the atmosphere, such as faults, channels, and blowouts of the sediment
909 column. A continuum model such as this one predicts a smooth methane
910 release response to a warming, growing in on some e-folding time-scale.
911 A world dominated by features that each represent a small fraction of the
912 total methane reservoir will release methane more episodically, but the
913 statistical distribution of the response in time should still show the e-
914 folding time scale of the underlying driving mechanism, the diffusion of
915 heat into the sediment column.

916 The way to deliver 50 Gton of methane to the atmosphere on a short
917 time scale is for it all to be released from a single geologic feature pent
918 up by ice. But 50 Gton of C represents a large fraction of all the
919 traditional natural gas deposits on Earth (about 100 Gton C). The place

920 to look for such a large unstable gas reservoir is in the field, not in this
921 model, but until such a thing is found it remains conjecture.

922 On time scales of thousands of years and longer, carbon from deep
923 methane hydrates and frozen organics on the Siberian continental shelf
924 could reach the atmosphere / ocean carbon cycle, potentially significantly
925 amplifying the “long tail” climate impact of anthropogenic carbon release.
926 Methane that is oxidized in the ocean would eventually equilibrate with
927 the atmosphere, so it is much easier for escaping methane to impact the
928 long tail as CO₂ than it is to affect the near future as methane.

929 The potential for future sea level change is much higher on millennial time
930 scales than the forecast for the year 2100, because it takes longer than
931 a century for ice sheets to respond to changes in climate. The model
932 finds that for the future, if sea level changes by tens of meters, as guided
933 by paleoclimate reconstructions [*Archer and Brovkin, 2008*], the impact
934 of sea level rise could overwhelm the impact of warming. The dominance
935 of sea level over temperature in the model of this area is due to
936 dissolution of methane in the water column, rather than a pressure effect
937 on hydrate stability, which is generally a weaker driver than ocean
938 temperature in deeper-water settings [*Mienert et al., 2005*].

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1010

1011 **7. Figure Captions**

1012 Figure 1. Domain of the model as applied to the Laptev Sea continental
1013 shelf and slope. This is the result of 62 million years of sediment
1014 accumulation on the crust, isostatic subsidence, pore fluid flow, and
1015 thermal diffusion, used as the initial condition for glacial / interglacial
1016 cycle and climate change simulations. Color indicates temperature. a)
1017 Full view. Black line shows the bottom of the crust, which grades
1018 smoothly from continental on the left into ocean crust through most of

1019 the domain on the right. b) Zoom in to see increased model resolution in
1020 the upper kilometer of the sediment column.

1021 Figure 2. Pore water salinity a) The fully marine case, in which the
1022 sediment column has always been submerged underneath a time-invariant
1023 sea level. b) Result of sediment column freshening by hydrological
1024 groundwater flow, driven by the pressure head resulting from a water
1025 table higher than sea level. A movie of the transition from marine to
1026 freshened (the origin of b) can be seen at
1027 http://geosci.uchicago.edu/~archer/spongebob_arctic/fig2.movie.gif

1028 Figure 3. Particulate Organic Carbon (POC) concentration. Highest values
1029 are found in the sediment depocenter just off the continental shelf break.

1030 Figure 4. Initial distribution of dissolved methane. a) Concentration in
1031 moles/m³. b-d) $\Omega = \text{CH}_4 / \text{CH}_{4(\text{sat})}$ deviation from equilibrium, b) of the
1032 Marine (salty) initial condition; c) of the pre-freshened initial condition
1033 (note depletion in near-surface near-shore sediments in the upper left);
1034 d) including permeable channels every five grid points, plus pre-
1035 freshening.

1036 Figure 5. Time-dependent forcing for the glacial / interglacial simulations
1037 and the global warming scenarios. a) Sea level is imposed as a sawtooth
1038 100-kyr cycle, with interglacial intervals shaded. The GW+S simulation
1039 tracks potential changes in sea level on long time scales due to fossil fuel
1040 CO₂ release, following a covariation from the geologic past of 15 meters /
1041 °C. The GW and Control simulations hold sea level at interglacial levels.
1042 b) Ocean temperature forcings.

1043 Figure 6. Colors indicate salinity in the unfrozen pore fluid of the sediment
1044 column. Thin solid black contours show the frozen fraction of the pore
1045 space. Heavy black stippled contour shows the stability boundary of
1046 methane hydrate as a function of temperature, pressure, and unfrozen
1047 pore fluid salinity. Left side: previously pre-freshened initial condition.
1048 Right side: Pure marine initial condition. c-d) Lowered sea level (from 70
1049 kyr in Figure 8) but warm air temperatures prevent permafrost formation.
1050 e-f) Glacial conditions of lowered sea level (70 kyr) and atmospheric
1051 temperature of -17 °C driving permafrost formation. The pre-freshened
1052 and the marine initial conditions differ in the frozen fraction of sediment,
1053 but the salinity of the unfrozen fluid, a correlate of the activity of water,
1054 depends only the temperature. g-h) Rising sea level (at 90 kyr in Figure

1055 8) into an interglacial interval. Movies of the glacial cycles (GL) with the
1056 prefreshened initial condition can be seen at
1057 http://geosci.uchicago.edu/~archer/spongebob_arctic/fig6a.movie.gif ,
1058 and the marine initial condition at
1059 http://geosci.uchicago.edu/~archer/spongebob_arctic/fig6b.movie.gif.

1060 Figure 7. Pore fluid pressure forcing and flow through the glacial cycles.
1061 Left) Colors indicate $P_{\text{excess}} + P_{\text{head}}$, solid contours are ice fraction, dashed
1062 contours are P_{head} . Right) Colors indicate $P_{\text{excess}} + P_{\text{head}}$, note different color
1063 scale from Left. Initial refers to the prefreshened initial condition. “Low
1064 Sea Level” refers to simulation SL. “Glacial” and “Interglacial” refer to
1065 simulation GL. Dashed contours indicate ice fraction, vectors fluid
1066 velocity. Movies can be seen at
1067 http://geosci.uchicago.edu/~archer/spongebob_arctic/fig7a.movie.gif
1068 and
1069 http://geosci.uchicago.edu/~archer/spongebob_arctic/fig7b.movie.gif.

1070 Figure 8. Sensitivities of the hydrate stability zone. Impact of the
1071 competition between ice and hydrate phases (a-d), and the geothermal
1072 temperature gradient (e-f). When ice is included as a potential solid
1073 phase, the pore waters are salty in the permafrost zone (a), restricting
1074 hydrate stability to at least 300 meters below sea level throughout the
1075 simulation (c). When ice is forbidden to form, hydrate can be stable
1076 nearly to the sediment surface during the height of the glaciation (b and
1077 d). The base of the stability zone is sensitive to the geothermal
1078 temperature gradient, while the shallowest reach of the stability zone
1079 does not respond to changing heat fluxes, because the temperatures are
1080 “anchored” at the ocean value at the top of the sediment column.

1081 Figure 9. Dissolved methane concentration relative to equilibrium ($\Omega =$
1082 $\text{CH}_4 / \text{CH}_{4(\text{sat})}$). Solid contours indicate ice fraction, dashed contours show
1083 the methane hydrate stability boundary. Movies for the left, center, and
1084 right columns, respectively can be seen at
1085 http://geosci.uchicago.edu/~archer/spongebob_arctic/fig9a.movie.gif ,
1086 http://geosci.uchicago.edu/~archer/spongebob_arctic/fig9b.movie.gif ,
1087 and
1088 http://geosci.uchicago.edu/~archer/spongebob_arctic/fig9c.movie.gif.

1089 Figure 10. Carbon cycle through glacial cycles from a prefreshened initial
1090 condition. Solid contours: Ice Fraction. Dashed contours: Methane
1091 hydrate stability zone. Left) Particulate organic carbon (POC)

1092 concentration. Movie at
1093 http://geosci.uchicago.edu/~archer/spongebob_arctic/fig10a.movie.gif.
1094 Center) Biological methane production rate. Movie at
1095 http://geosci.uchicago.edu/~archer/spongebob_arctic/fig10b.movie.gif
1096 Right) Methane hydrate concentration. Movie at
1097 http://geosci.uchicago.edu/~archer/spongebob_arctic/fig10c.movie.gif.
1098 Movies of methane hydrate stability and concentration are given for the
1099 sensitivity studies, in the supplemental material and at
1100 <http://geosci.uchicago.edu/~archer/spongebob/>.

1101 Figure 11. Glacial cycle of methane hydrate inventory on the continental
1102 shelf. a) Effects of salt and ice. b) Sensitivity to methaneogenesis rates.
1103 c) Sensitivity to the column temperature gradient. d) Glacial cycles of
1104 shelf bubble inventories, effects of salt and ice.

1105 Figure 12. Spatial distribution and sea level impact of methane fluxes to
1106 the atmosphere. a-d) Solid line shows the elevation of the sediment
1107 surface relative to the sea level at the time. Grey lines (scale to right)
1108 show the efficiency of bubble transport through the water column,
1109 assuming a flux attenuation length scale of 30 meters. e-k) Dashed line:
1110 Methane bubble flux across the sediment surface. Solid line: Methane
1111 bubble flux to the atmosphere (dashed line multiplied by transport
1112 efficiency). Most of the methane flux in the model occurs near the shelf
1113 break, and submergence in the ocean has a strong impact on the flux to
1114 the atmosphere. A related movie can be seen at
1115 http://geosci.uchicago.edu/~archer/spongebob_arctic/fig12.movie.gif .

1116 Figure 13. Glacial / interglacial cycle of methane fluxes on the
1117 continental margin of the model. Sea level at top, grey regions indicate
1118 interglacial intervals, pink the Anthropocene. a-e) Cumulative methane
1119 fluxes. Red lines show production rate. Brown regions show lateral
1120 transport of dissolved methane. Grey shows oxidation by SO_4^{2-} in the
1121 sediment column. Blue shows bubble flux to the water column. During
1122 interglacial times (e.g. far left) there is a small onshore transport of
1123 methane, which is represented by a negative starting point for the
1124 oxidation (grey) region. In equilibrium, the colored areas should fill in the
1125 region under the red curve.

1126 Figure 14. Methane fluxes to the atmosphere. Sea level at the top,
1127 interglacial intervals in vertical grey bars, the Anthropocene in pink. a)
1128 From a pre-freshened initial condition, with and without permafrost

1129 formation. b) From a pure marine initial condition. c and d) Sensitivity to
 1130 terrestrial organic carbon deposition during low sea-level stands, and to
 1131 thermogenic methane flux. e) Sensitivity to the impact of ice fraction on
 1132 bubble mobility.

1133 Figure 15. Impact of anthropogenic warming on the methane cycle in the
 1134 model. a) Base cases, a warming scenario (GW), without and with a
 1135 geological time-scale sea level rise scenario (+SLR), and extended
 1136 interglacial control (Ctl). Warming plus increasing sea level decreases the
 1137 methane flux overall, due to bubble dissolution in a deeper water column.
 1138 b) Altered model physics impacts. c and d) Altered methanogenesis
 1139 rates. e) Sensitivity to the ice fraction at which bubble mobility is
 1140 assumed stopped.

1141 **8. Tables**

1142 Table 1. Nomenclature describing the model scenarios and sensitivity
 1143 runs.

Fr	The sediment column has been pre-freshened by previous exposure to hydrological forcing.
Mr	Initial salinities are close to marine.
SL	Sea level changes with constant air and water temperatures
GL	SL + glacial cycles in air and water temperature
GW	A long-term global warming scenario, a peak and long tail temperature perturbation consistent with CO ₂ release and cessation of the glacial sawtooth forcing.
GW+SL	Adds geologic-timescale sea level rise due to anthropogenic climate change, based on correlation between temperature and sea level in the geologic past (10 meters / °C).
Ctl	An extended interglacial with no CO ₂ release forcing.

+ LD	Land deposition of carbon-rich Yedoma. Base case is 10 m / 100 kyr, with sensitivity runs using 30 and 100 m / 100 kyr accumulation of 30% POC material. Movies in the supplemental material are identified by the tags Land30 and Land100.
+ TG	Thermogenic methane production rate sensitivity runs, scaling the rate from the spinup result by factors of 10 and 100. Movies in the supplemental material are identified by the tags TGenX10 and TGenX100.
+ Geotherm	Sensitivity of ice and hydrate cycles on the geothermal temperature gradient. Temperatures from the Base simulation were adjusted when calculating the stability of ice and hydrate, to simulate the impact of geothermal heat fluxes on hydrate stability. Note that other aspects of the sediment column, including the solubility of methane, retained the original temperatures. Heat fluxes simulated include 25 mW/m ² , 37.5, 50 (Base), 62.5, and 75. Movies of the non-base runs are identified by tags HF050, HF075, HF125, and HF150.
Ice and Bubble Transport	When the ice fraction exceeds a threshold value methane gas flow is disabled. Base case is 50%, variants 10%, 30%, 70%, and 90%, identified with tags Ice10, Ice30, Ice70, and Ice90.
No Ice	The ice phase is disallowed in the thermodynamic calculation. Movies in the supplemental material include salinity. The files are tagged as Nolce

No Salt from Ice	Ice is allowed to form, but it does not affect the salinity as it determines methane hydrate stability. Movie files are tagged as NoSalFromIce.
Permeable Channels	Increasing vertical permeability by a factor of 10 every 5 th grid cell, to generate heterogeneity in the flow. Tagged as PermChan
No Horizontal Flow	Horizontal flow is disabled. Tagged as NoHFlow.

1144 Movies comparing altered scenario runs with the Base scenario are given
1145 in the supplemental material, and at
1146 <http://geosci.uchicago.edu/~archer/spongebob/>. Movies named
1147 hydrate* and bubbles* show methane hydrate and bubble inventories and
1148 stability zone changes. Files entitled salinity* show salinities, and
1149 bubb_atm* show bubble fluxes through and out of the sediment column,
1150 into the ocean, and into the atmosphere, through time.

1151

1152 **9. Supplemental Text**

1153 ***S1. Vertical Flow***

1154 In previous versions of the SpongeBOB model, the fluid flow was
1155 calculated explicitly, each time step, as a function of P_{excess} at the
1156 beginning of the time step. Numerical stability motivated a modification
1157 of the vertical flow to an implicit numerical scheme, which finds by
1158 iteration an internally consistent array of vertical flow velocities and
1159 resulting P_{excess} values from a time point at the end of the time step.
1160 Ocean and atmosphere models often use this methodology for vertical
1161 flow. A benefit to this change is stability in the vertical flow field,
1162 reducing numerical noise that can cause trouble with other aspects of the
1163 model such as ice formation. Implicit schemes can be more efficient
1164 computationally, but in this case the execution time is not improved by
1165 the implicit method, just the stability.

1166 Note that the flow scheme in its formulation is entirely elastic, whereas in
1167 reality, pore fluid excluded by the pressure of a sediment column above
1168 sea level, for example, where it is uncompensated by buoyancy in
1169 seawater, should remain excluded when sea level rises again, like
1170 toothpaste from the tube. However, my attempts to embed this plastic
1171 behavior into an implicit solver failed to converge.

1172 ***S2. Ice Formation***

1173 The ice content in a grid cell relaxes toward equilibrium, quickly enough to
1174 approximate an equilibrium state through the slow temperature evolution
1175 in the model (which neglects a seasonal cycle at the surface), but slowly
1176 enough to avoid instabilities with other components of the model such as
1177 fluid flow and methane hydrate formation. A limiter in the code prevents
1178 more than 99% of the fluid in a grid cell from freezing, but the
1179 thermodynamic equilibrium salinity is used to calculate, for example, the
1180 stability of methane hydrate, to prevent the numerical limiter from
1181 affecting the thermodynamic availability of water to drive chemical
1182 reactions.

1183 ***S3. Thermodynamics of Ice and Hydrate***

1184 When the system consists only of ice and fluid phases, the equilibrium
1185 salinity S_{eq} increases with decreasing temperature below freezing (Figure
1186 1a, left). Above the melting temperature, ice is unstable, as indicated by
1187 the nonzero values of the disequilibrium temperature, $\Delta T_{eq, ice} = T - T_{eq, ice}$,
1188 in contours, even in zero-salinity water (right). For a system consisting
1189 of only the hydrate and fluid phases (assuming that ice formation is
1190 disallowed, and also gas saturation for methane) (Figure 1b), the behavior
1191 is similar but with an added pressure dependence due to the
1192 compressibility of the gas phase.

1193 When both solid phases are allowed, the overall equilibrium salinity will
1194 whichever is higher between $S_{eq, ice}$ and $S_{eq, hydrate}$. Whichever phase can
1195 seize water at its lowest activity (highest salinity) will be the stable
1196 phase. The salinity of the brine excluded from that phase will be too high
1197 to permit the existence of the other solid phase at that temperature.
1198 The contours show ΔT_{eq} for hydrate (solid) and ice (dashed), which are
1199 also plotted in color in Figures 1d and e. This is illustrated in Figure 1d, in
1200 colors of $\Delta T_{eq, hydrate}$ and contours of the excess salinity relative to hydrate

1201 equilibrium, $S_{\max} - S_{\text{eq, hydrate}}$. Hydrate is only stable when $\Delta T_{\text{eq, hydrate}}$ is zero
1202 (purple color).

1203 Under permafrost conditions of low pressure and low temperature (upper
1204 left corner), $\Delta T_{\text{eq, hydrate}}$ is greater than zero, indicating that hydrate is
1205 unstable, coinciding with the salinity forcing from the ice, in overlain
1206 contours. A similar exclusion of ice in part of the hydrate stability zone is
1207 seen [Figure 1e](#), but this would only happen in nature in conditions of
1208 unlimited methane. The resulting phase diagram for ice and methane
1209 hydrate is shown in [Figure 1f](#). Hydrate stability is suppressed in the
1210 permafrost zone by this thermodynamic mechanism.

1211 There is an analogous exclusion of ice from part of the methane hydrate
1212 stability zone, but this assumes unlimited methane; if the dissolved
1213 methane concentration is less than gas saturation, both solid phases can
1214 coexist. In the permafrost zone, the dissolved methane concentration
1215 cannot exceed solubility with gas saturation, so the exclusion of methane
1216 hydrate from thermodynamic stability is inescapable.

1217 ***S4. Construction of the Pre-Freshened Sediment Column***

1218 If sea level falls, exposing the sediment column to the atmosphere for the
1219 first time, there is a pressure head gradient extending throughout the
1220 sediment column, provoking lateral flow at all depths. As the pore fluid at
1221 the surface is replaced by fresh runoff, the lighter density of that fluid
1222 tends to diminish the pressure head gradient in the deeper sediment
1223 column. The deeper pressure gradient and flow approach zero as the
1224 fresh water lens in the outcropping region approaches an isostatic
1225 equilibrium condition known as the Ghyben-Herzberg relation [*Moore et*
1226 *al.*, 2011], in which each meter elevation of the water table is
1227 compensated for by about 40 meters of fresh water below sea level,
1228 determined by the difference in densities of fresh and salt water.

1229 To create this condition within the model, two simulations are presented
1230 in which sea level was decreased by 30 and 120 meters, respectively, and
1231 held there for millions of years ([Supplemental Figure 2](#)). The 30-meter
1232 drop experiment produced land outcrop in about 1/4 of the model
1233 domain, with the predicted equilibrium Ghyben-Herzberg halocline
1234 reaching about 1200 meters maximum depth. The model salinity relaxes
1235 into close agreement with the predicted halocline, lending support to the
1236 model formulation for density, pressure head, and fluid flow. As time

1237 progresses further, the outcropping land surface subsides (there is no
1238 land deposition in this scenario), until it drops below the new lowered sea
1239 level value after about 2.5 Myr. The hydrological pumping generates a
1240 low-methane plume that also persists for millions of years in the model
1241 ([Supplemental Figure 3](#)).

1242 **negligible impact of canyons**

1243 Variants of this experiment were done with differing values of the lateral
1244 distance to drainage canyons in the model, which provide a pathway for
1245 fluid loss in sediments above sea level. When a hypothetical canyon is
1246 located 10 km from the SpongeBOB slab, the model salinity approaches
1247 equilibrium on an e-folding time scale of about 400 kyr ([Supplemental](#)
1248 [Figure 4](#)). When the canyon is 100 km distant or nonexistent, the
1249 equilibration time scale is about 600 kyr. Based on the idea that canyons
1250 of order 100 km long should be about 100 km apart, the Base simulation
1251 in this paper assumes canyon spacing of 100 km.

1252 **120 m same as 30**

1253 When sea level is lowered by 120 m, the sequence of events is similar,
1254 except that the pressure head is so high that to satisfy the Ghyben-
1255 Herzberg relation would require fresh pore waters at many kilometers
1256 depth, even deeper than bedrock on the “continental” side of the model
1257 domain. Because of the low permeability of the deepest sediment
1258 column, the freshwater pumping groundwater mechanism is unable to
1259 reach these deepest pore waters, which therefore remain salty. The time
1260 scale for establishing a significant freshening of the upper kilometer of
1261 the sediment column is still on the order of 100-500 kyr, and the
1262 subsequent subsidence time of the sediment column in the model, until it
1263 drops below the new lowered sea level, takes about 10 Myr. In both
1264 cases, subsidence of the exposed sediment column prevents the
1265 sediment surface in the model from remaining above sea level indefinitely
1266 (without land deposition).

1267 **10. Supplemental Figure Captions**

1268 Supplemental Figure 1. Thermodynamics of hydrate and ice. Top) Colors
1269 are salinities, which range from fresh if there is no solid phase, to saltier
1270 as the freezing point depression of the solid phase follows the in situ
1271 temperature. Contours indicate the extent of thermal disequilibrium, ΔT_{eq}
1272 = $T - T_{eq}$. a) For the system of ice and fluid. b) Considering hydrate and

1273 fluid phases, excluding ice formation and assuming equilibrium with
1274 methane gas. c) Combined ice + hydrate + fluid system, where the
1275 salinity is controlled by the most stable solid phase. Solid contours are
1276 $\Delta T_{\text{eq, hydrate}}$, dashed $\Delta T_{\text{eq, ice}}$. d and e) Colors are ΔT_{eq} , where 0 (purple)
1277 indicates stability, and contours are the excess salinity relative to a solid
1278 phase, e.g. $S_{\text{max}} - S_{\text{eq, hydrate}}$ in (d), for hydrate, and e) ice. f) Phase diagram
1279 for the ice + hydrate + brine system. Hydrate is excluded from the ice
1280 phase space by the high salinity of the brine. Ice is ideally also excluded
1281 from part of the hydrate stability zone by a similar mechanism, but this
1282 would only happen in nature under conditions of unlimited methane
1283 availability. Thus it is easier to envision coexistence of hydrate and ice
1284 within the hydrate stability zone, under conditions of limited methane
1285 availability, than it is to imagine hydrate in the permafrost zone, where
1286 ice has no impediment for formation.

1287 Supplemental Figure 2. Freshening the sediment column by hydrological
1288 groundwater flushing. Color indicates salinity. Solid black line represents
1289 sea level in the ocean (white space), and the equilibrium fresh-salty
1290 boundary given a snapshot of the pressure head (the Ghyben-Herzberg
1291 relation). Left side: results of dropping sea level 30 meters and holding it
1292 there. A freshwater lens forms and strives to reach Ghyben Herzberg
1293 equilibrium as the sediment column subsides, where atmospheric
1294 exposure decreases its buoyancy and stops sediment accumulation.
1295 After the sediment column subsides beneath the still-lowered sea level,
1296 the fresh water lens remains for millions of years. A movie can be seen at
1297 [http://geosci.uchicago.edu/~archer/spongebob_arctic/supp_fig2a.movie](http://geosci.uchicago.edu/~archer/spongebob_arctic/supp_fig2a.movie.gif)
1298 [.gif](http://geosci.uchicago.edu/~archer/spongebob_arctic/supp_fig2a.movie.gif) . Right side: Result of dropping sea level 120 meters and holding it
1299 there forever. Movie at
1300 [http://geosci.uchicago.edu/~archer/spongebob_arctic/supp_fig2b.movie](http://geosci.uchicago.edu/~archer/spongebob_arctic/supp_fig2b.movie.gif)
1301 [.gif](http://geosci.uchicago.edu/~archer/spongebob_arctic/supp_fig2b.movie.gif)

1302 Supplemental Figure 3. Dissolved methane impact by hydrological
1303 freshening of the sediment column as described in **Supplemental Figure 2**.
1304 $\Omega = \text{CH}_4 / \text{CH}_{4(\text{sat})}$. Movies can be seen at
1305 [http://geosci.uchicago.edu/~archer/spongebob_arctic/supp_fig3a.movie](http://geosci.uchicago.edu/~archer/spongebob_arctic/supp_fig3a.movie.gif)
1306 [.gif](http://geosci.uchicago.edu/~archer/spongebob_arctic/supp_fig3a.movie.gif) and
1307 [http://geosci.uchicago.edu/~archer/spongebob_arctic/supp_fig3b.movie](http://geosci.uchicago.edu/~archer/spongebob_arctic/supp_fig3b.movie.gif)
1308 [.gif](http://geosci.uchicago.edu/~archer/spongebob_arctic/supp_fig3b.movie.gif)

1309 Supplemental Figure 4. Time scale of depleting the salinity of the
1310 continental shelf sediment column after an instantaneous sea level drop

1311 of 30 meters. The effect of lateral canyons is to provide a pathway for
1312 saline fluid to be replaced by fresh groundwater in sediments above sea
1313 level. If the lateral canyon spacing is 10 km, they can have a significant
1314 impact on the time constant for ground water flushing. A more
1315 conservative 100-km canyon is adopted for the rest of the simulations.

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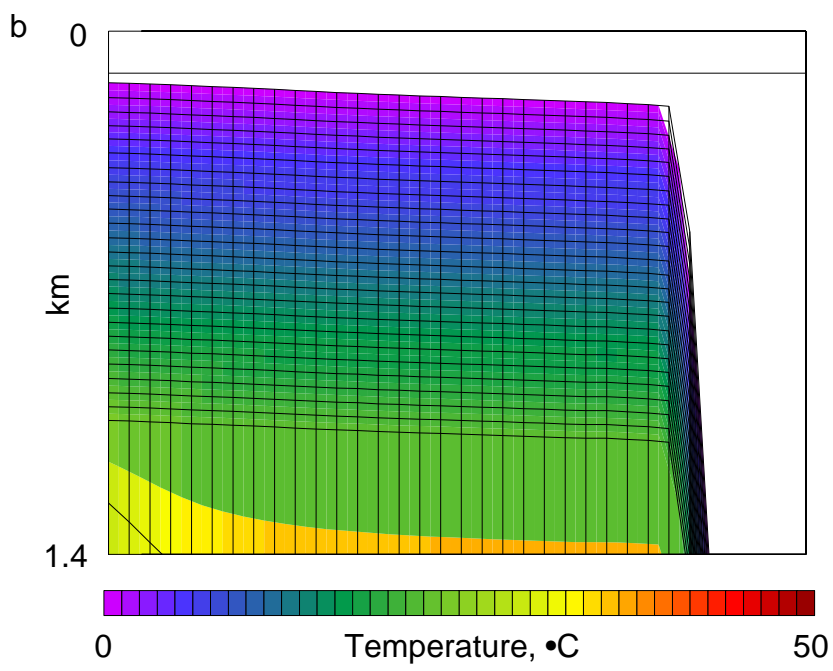
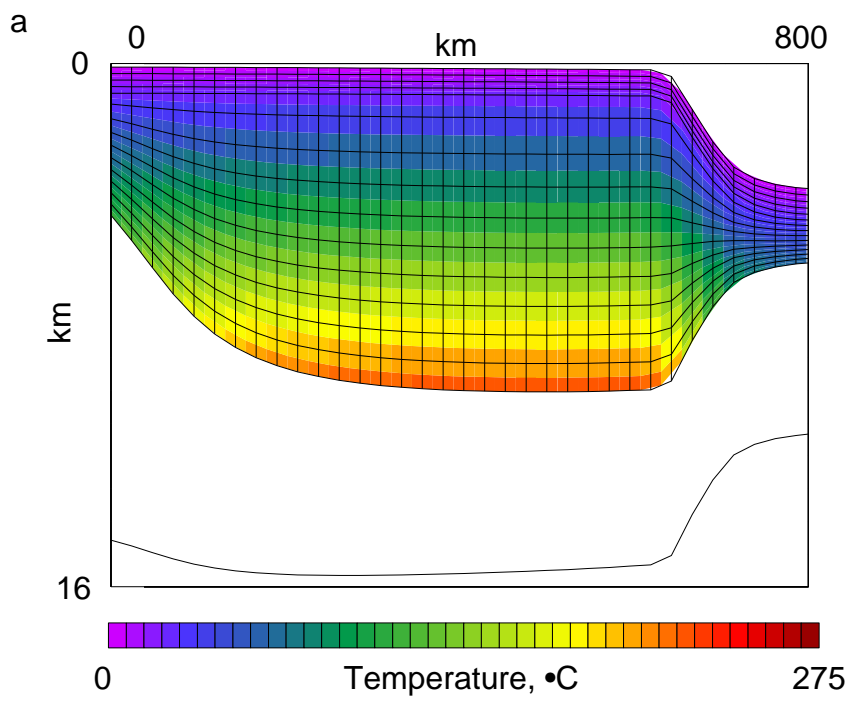


Figure 1

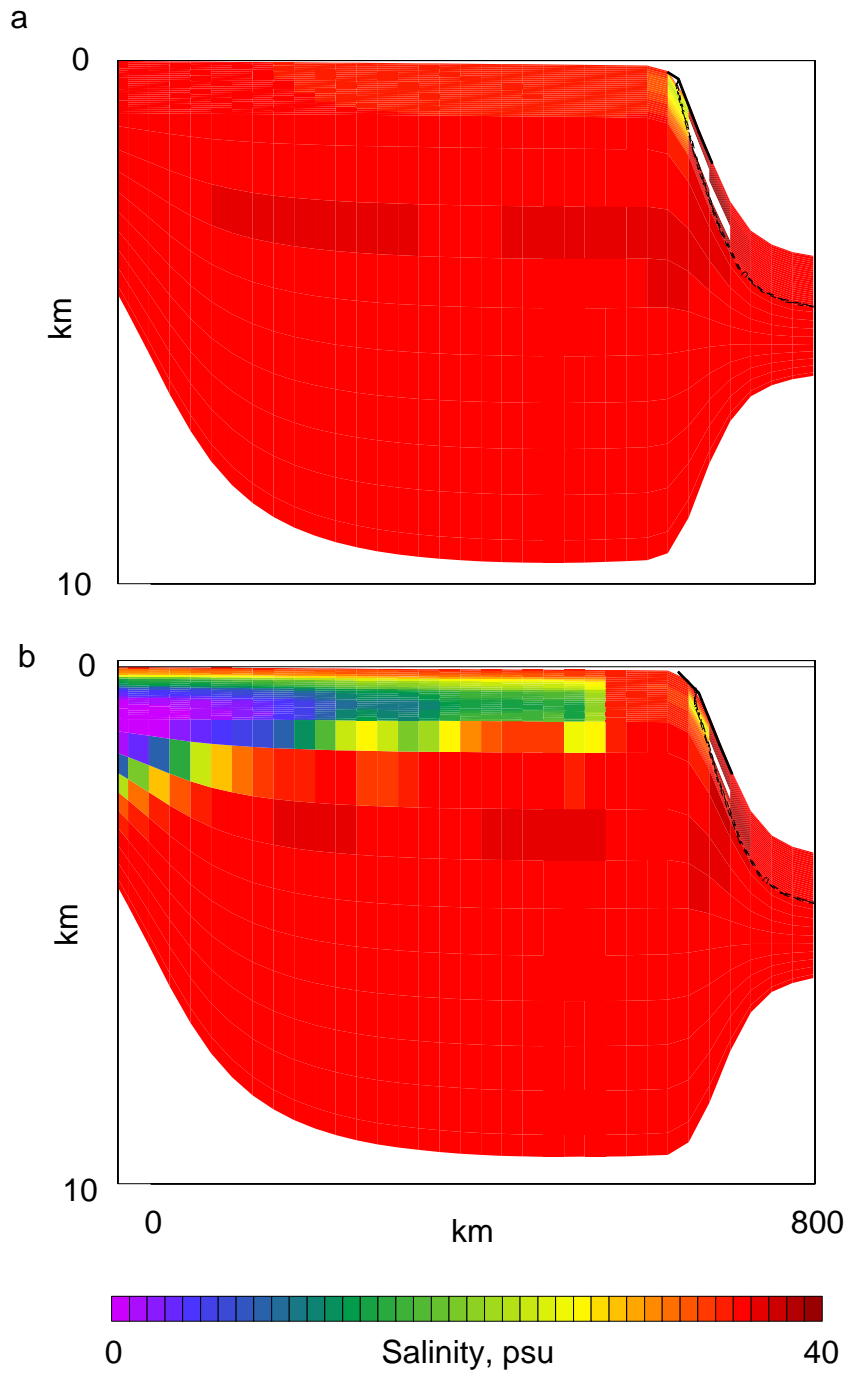


Figure 2

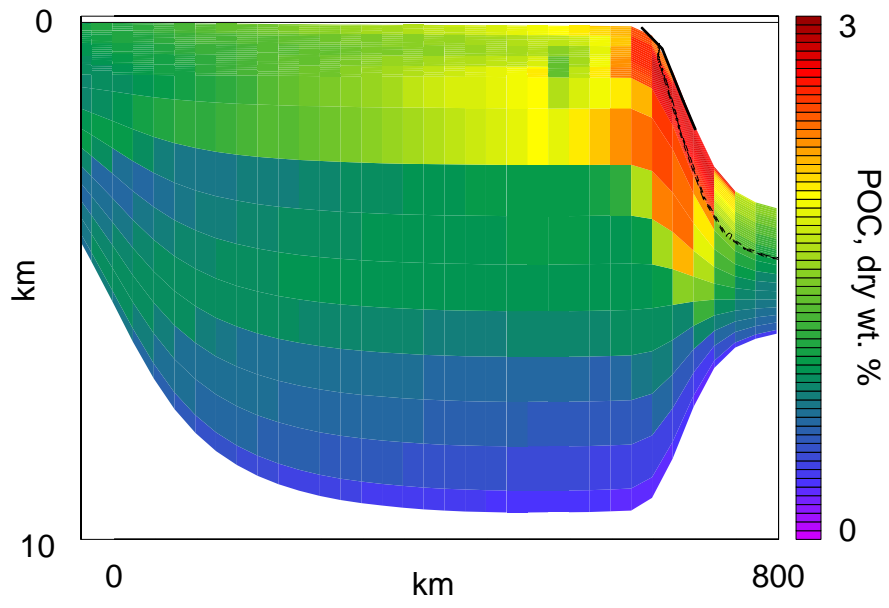


Figure 3

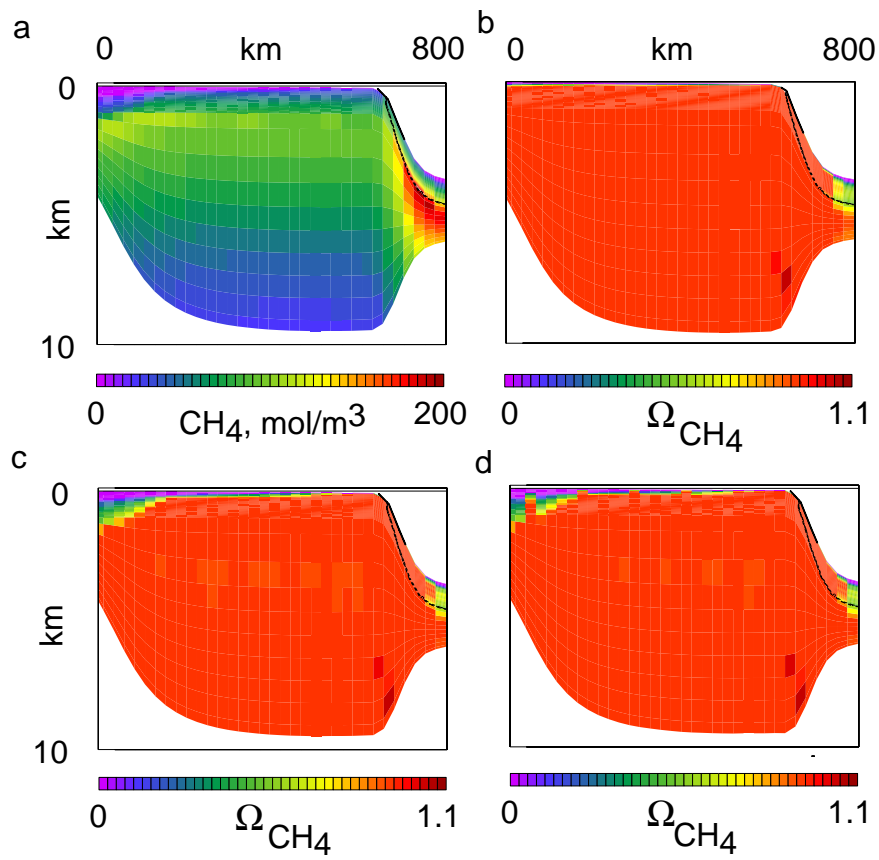


Figure 4

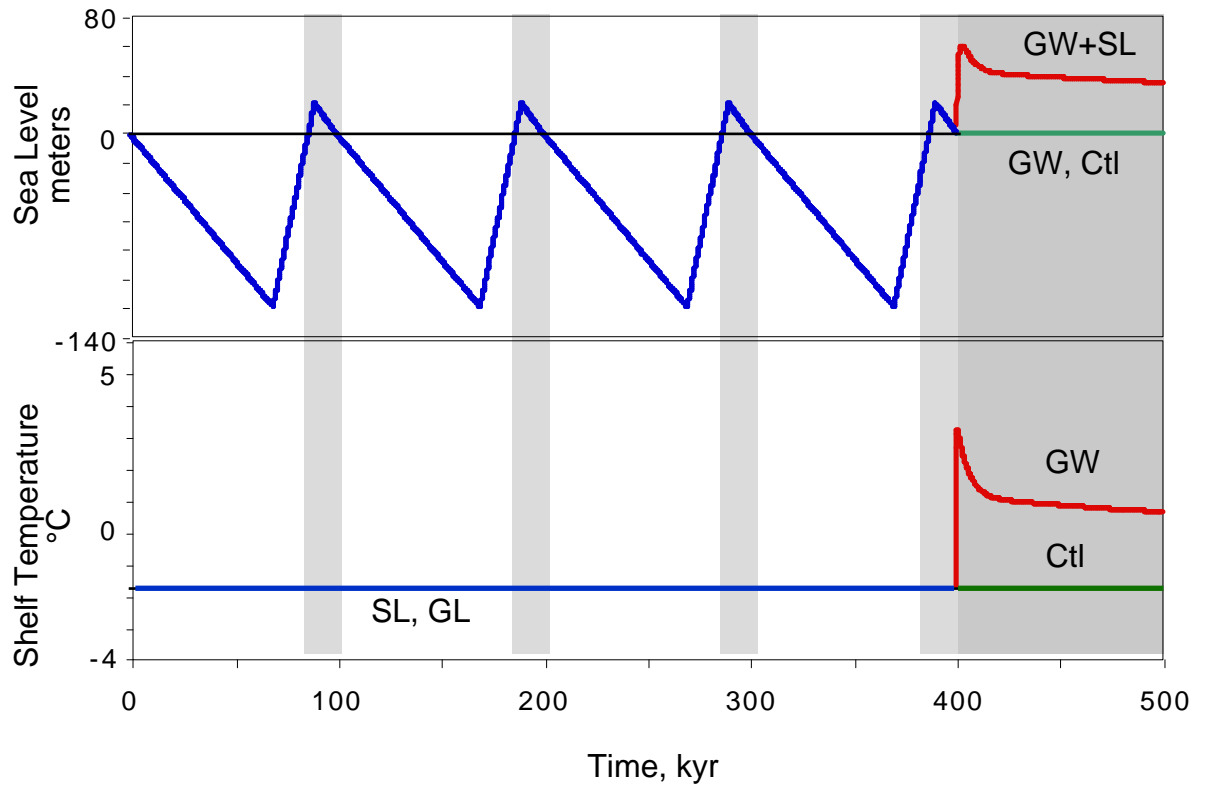


Figure 5

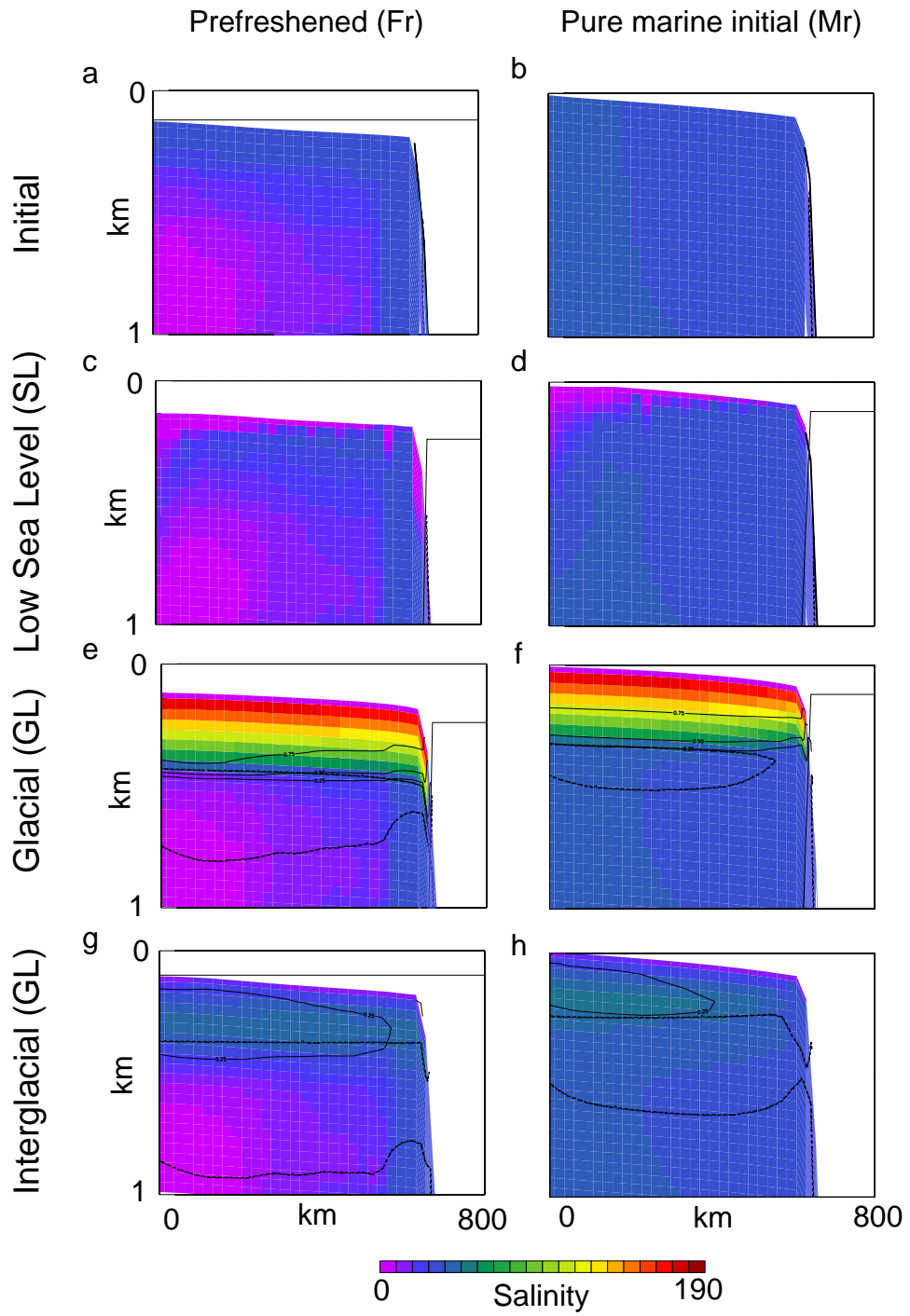


Figure 6

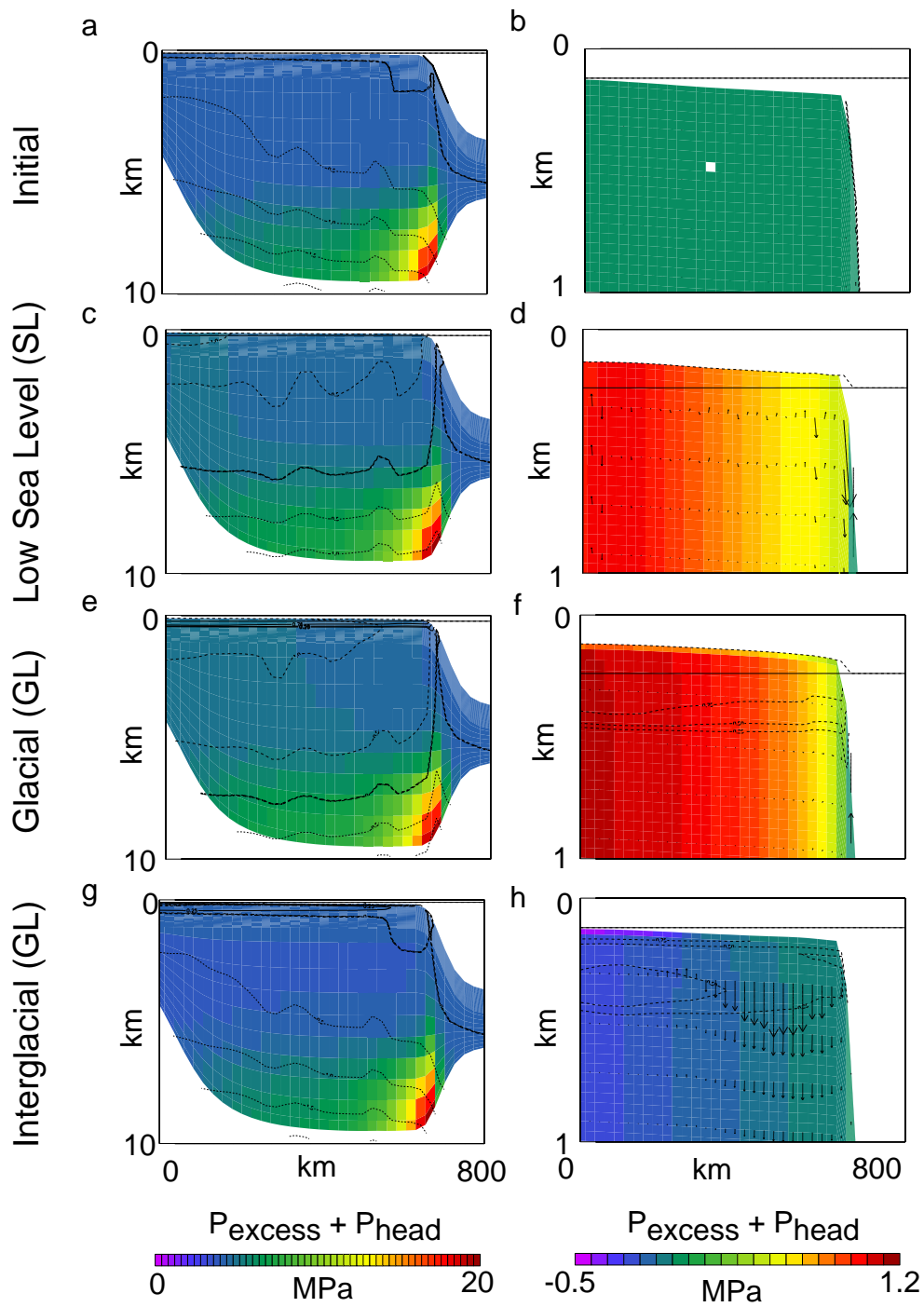


Figure 7

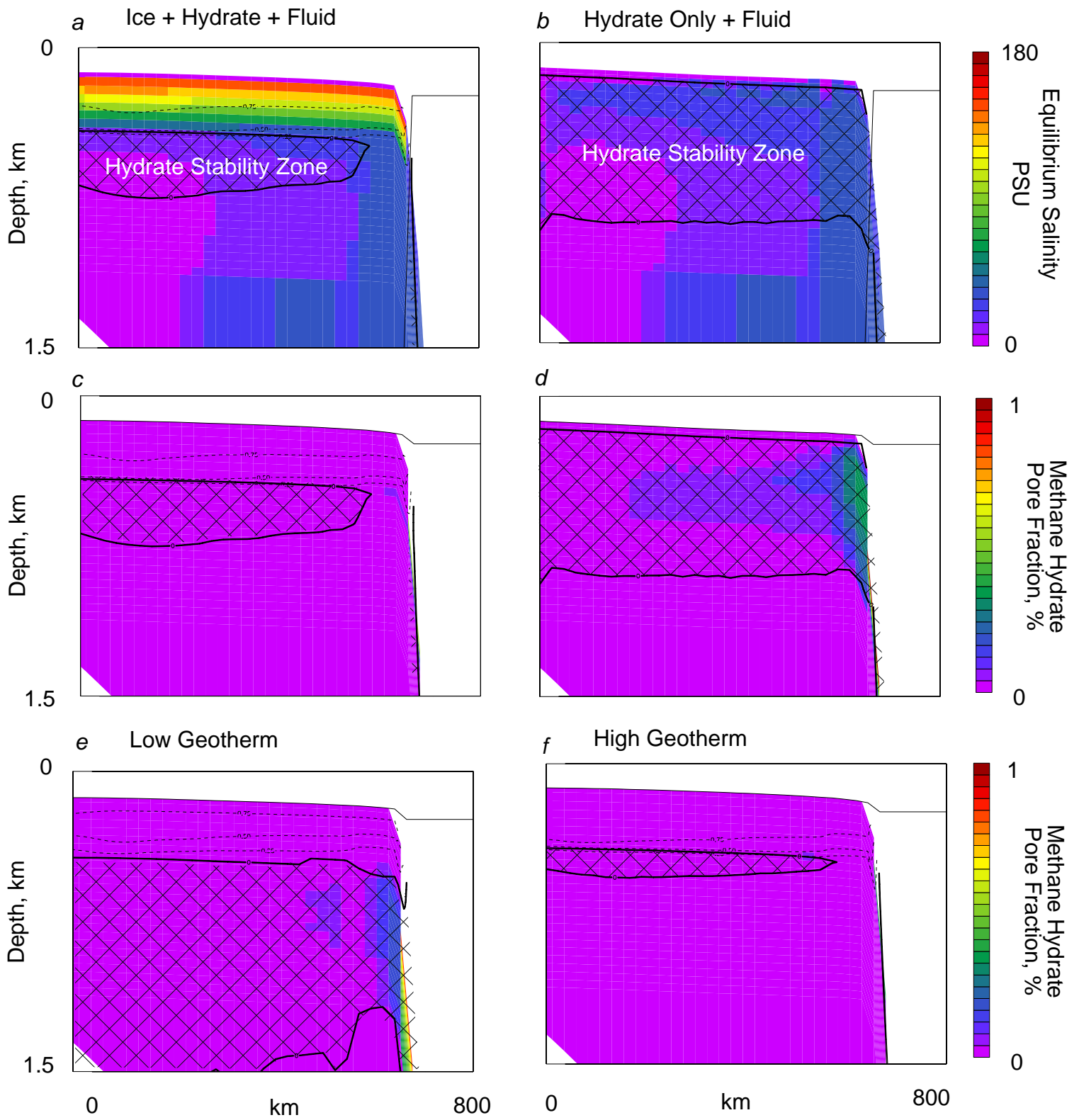


Figure 8

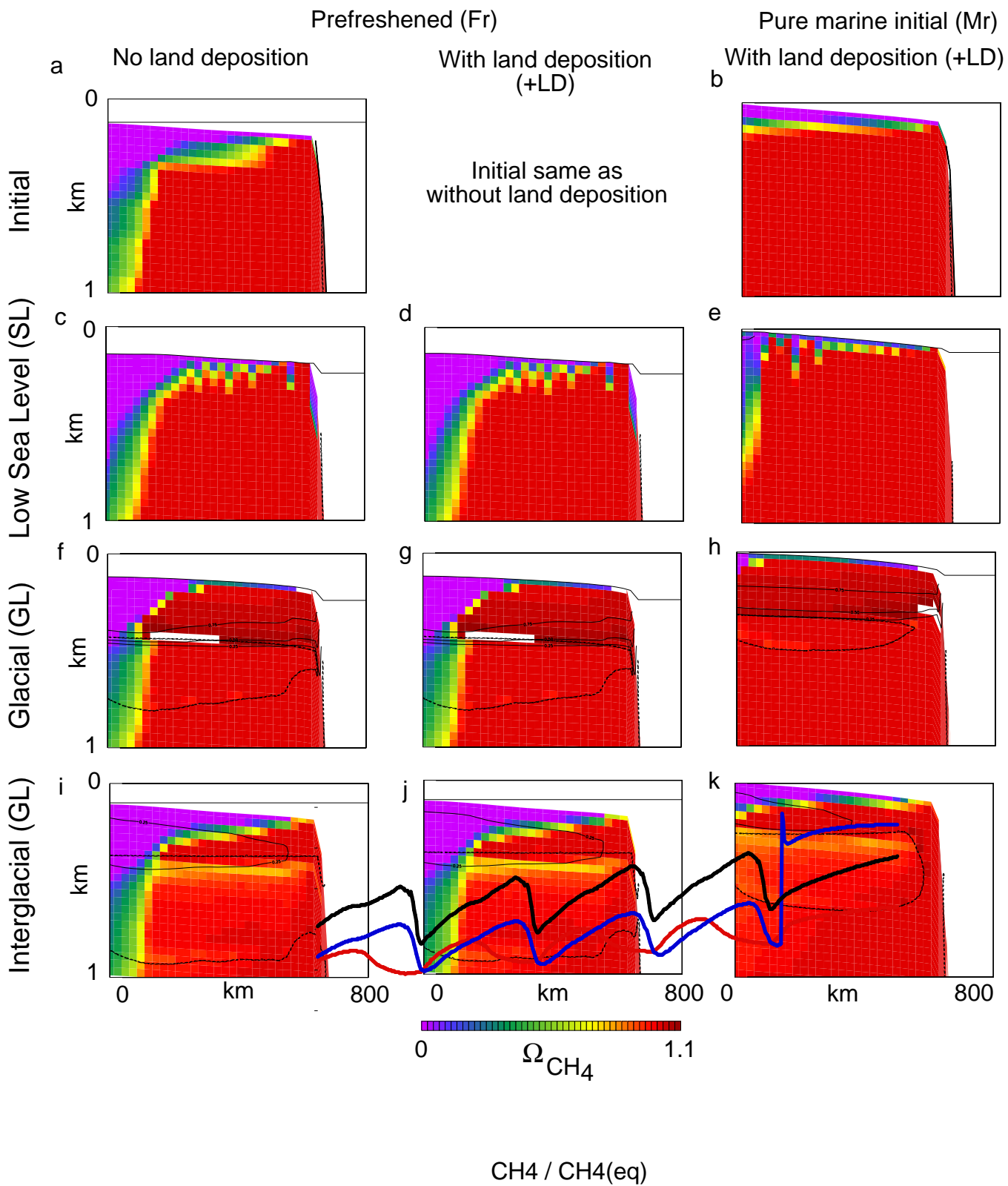


Figure 9

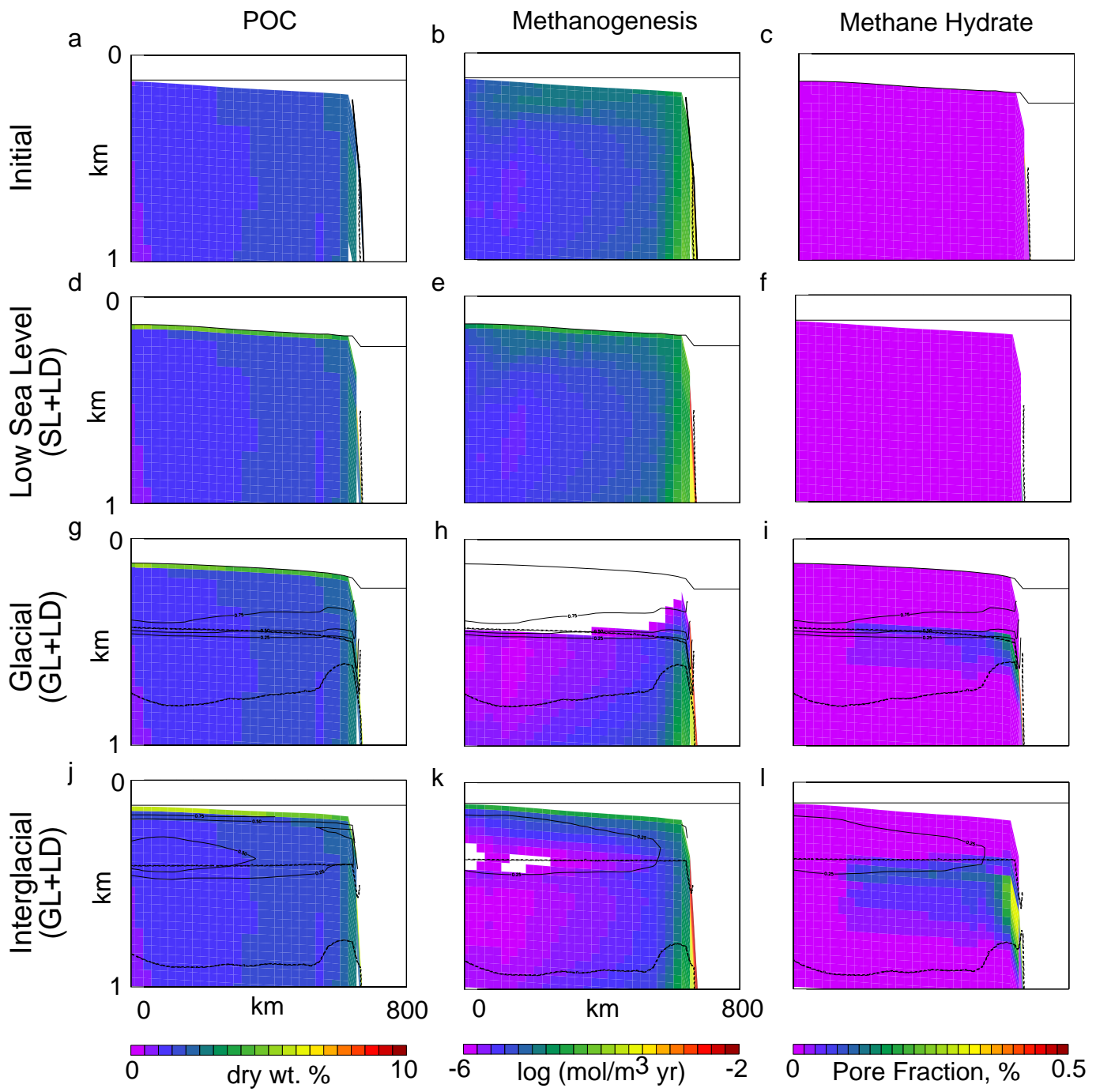


Figure 10

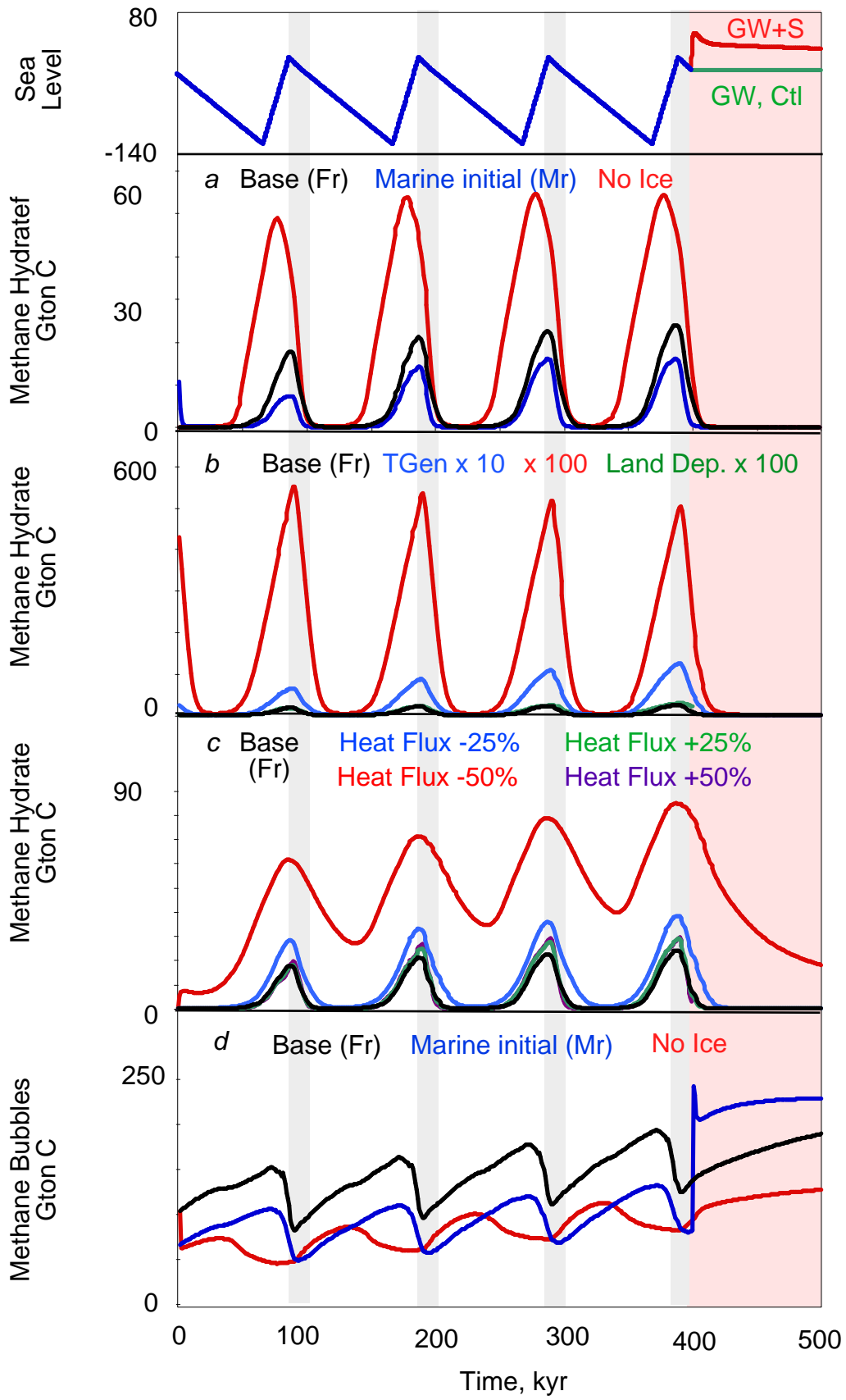


Figure 11

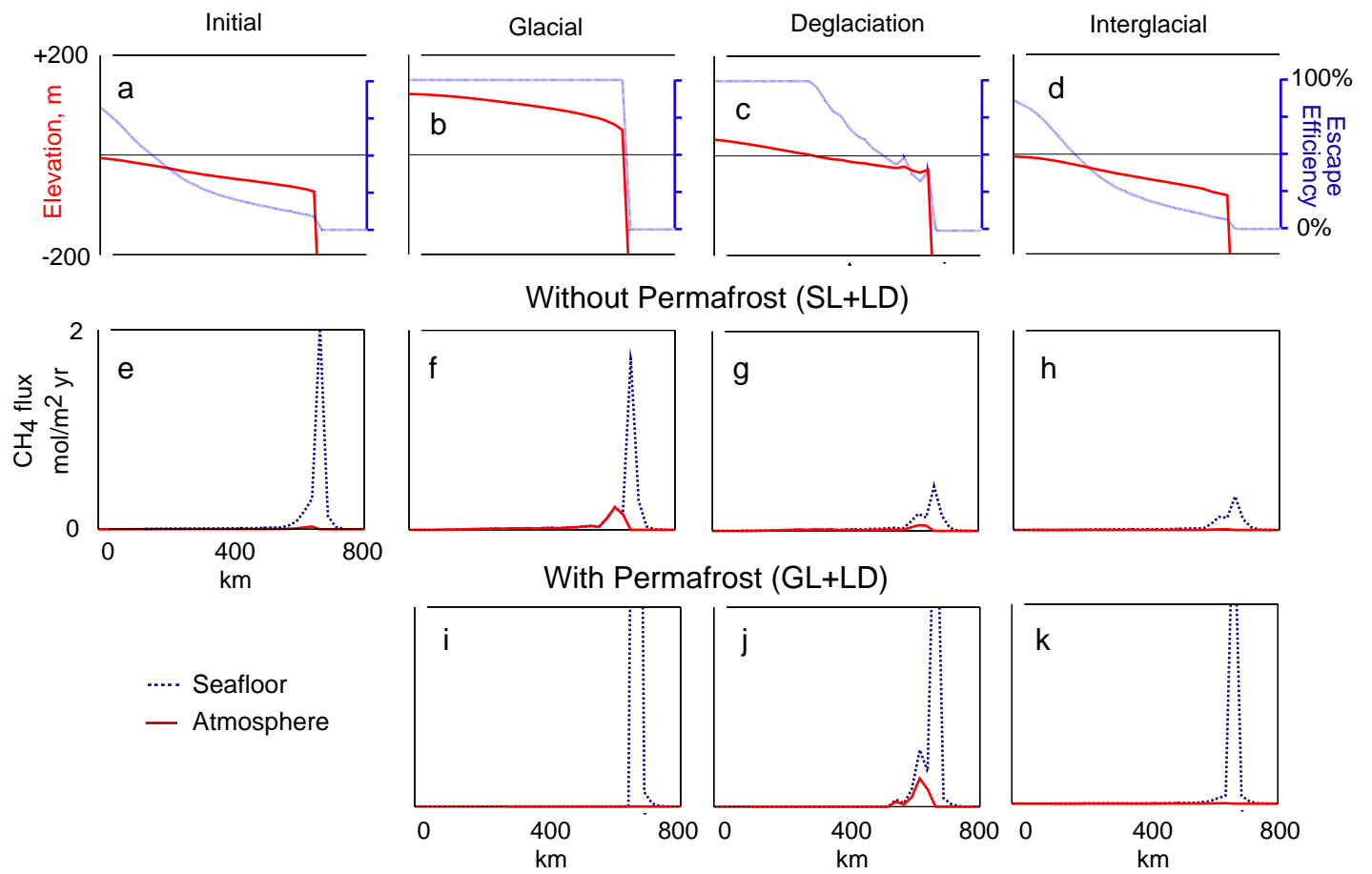


Figure 12

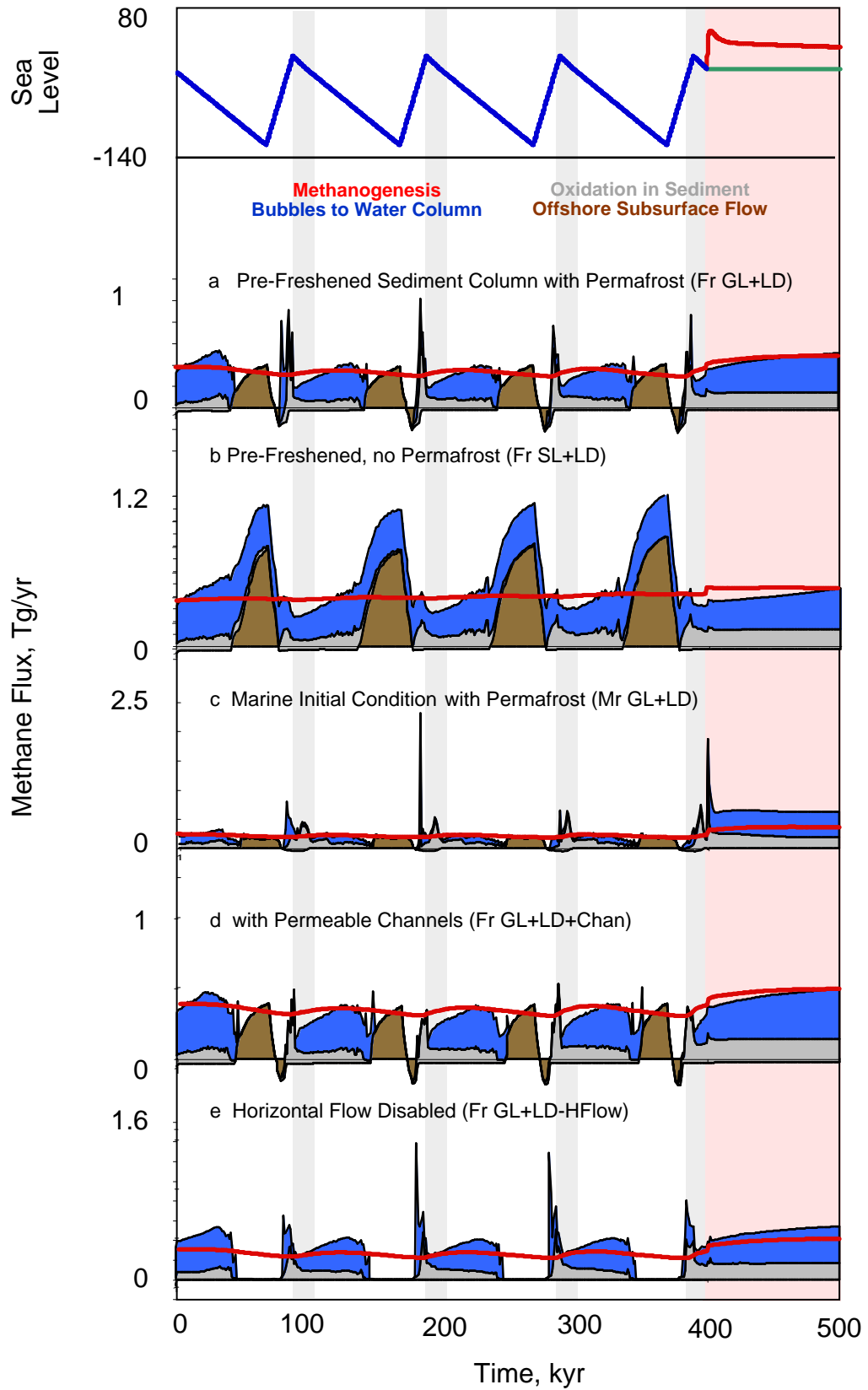


Figure 13

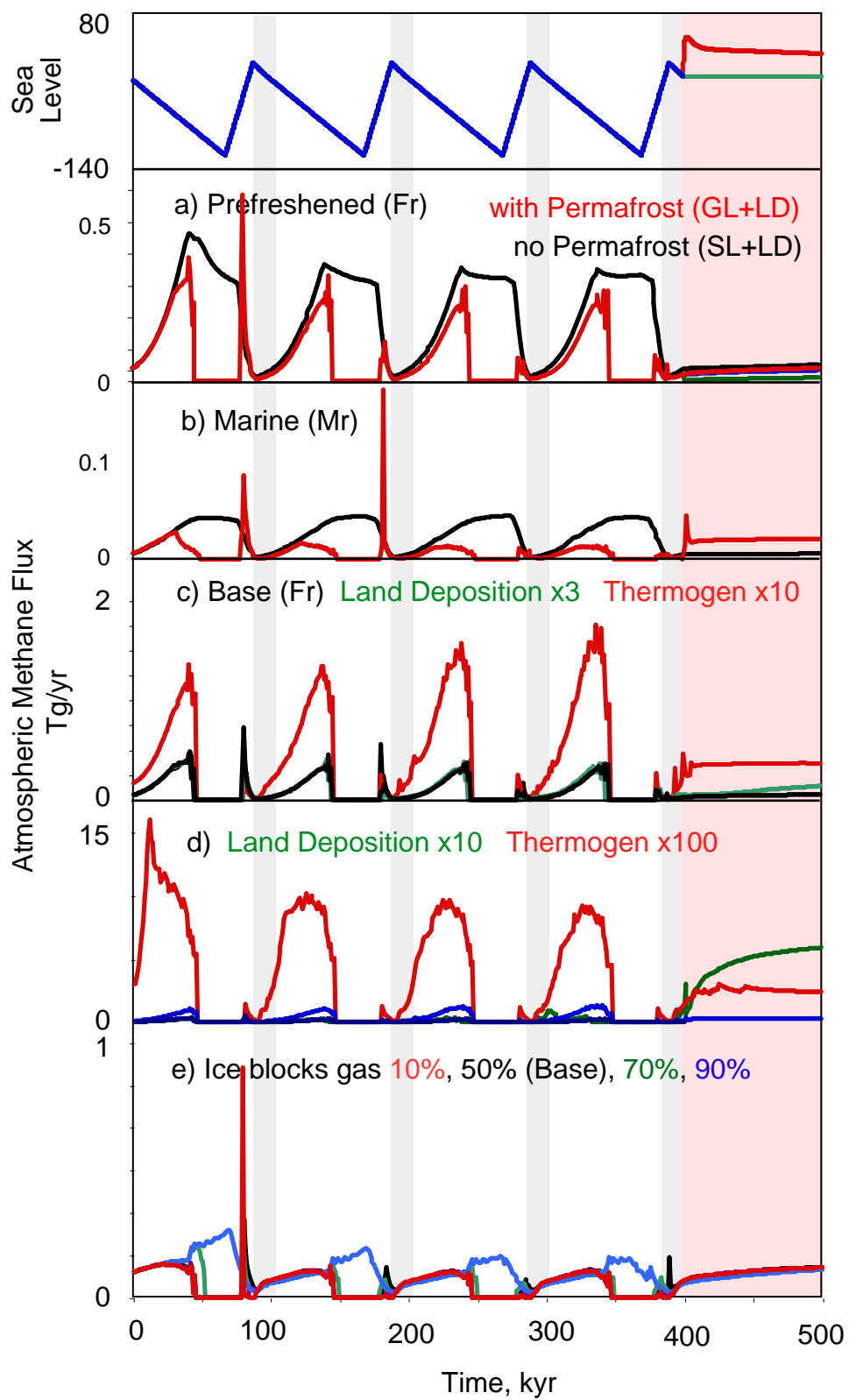


Figure 14

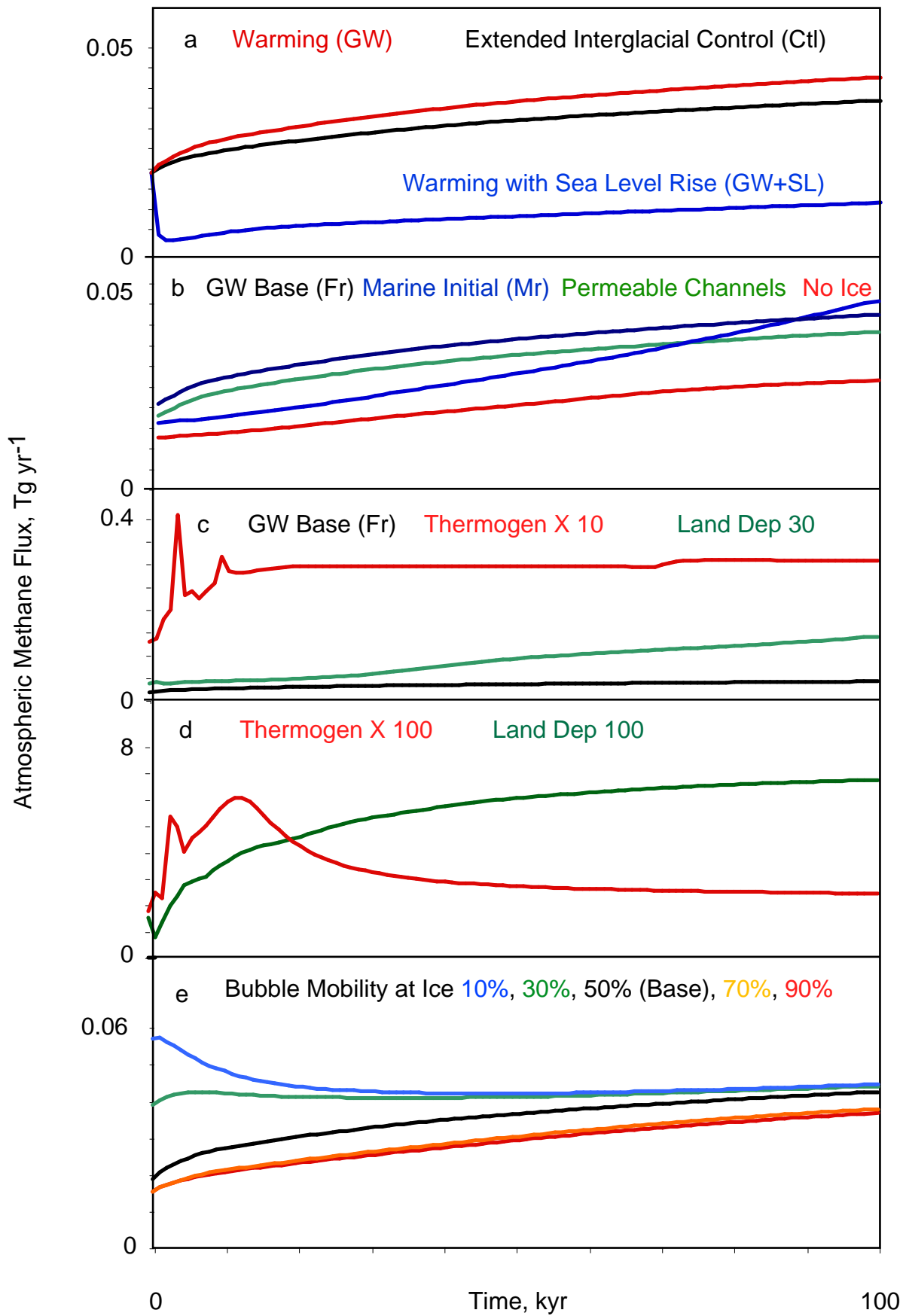
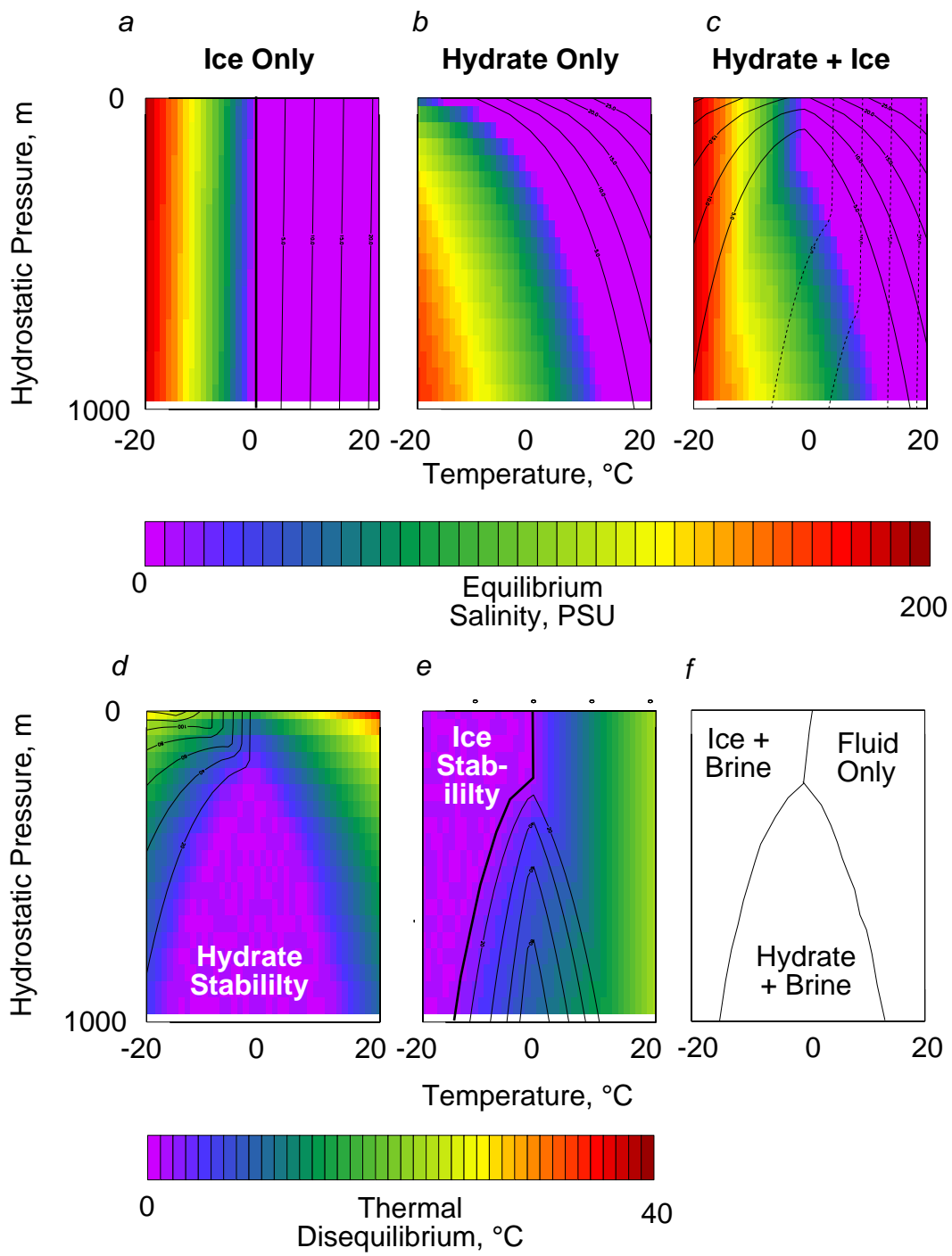
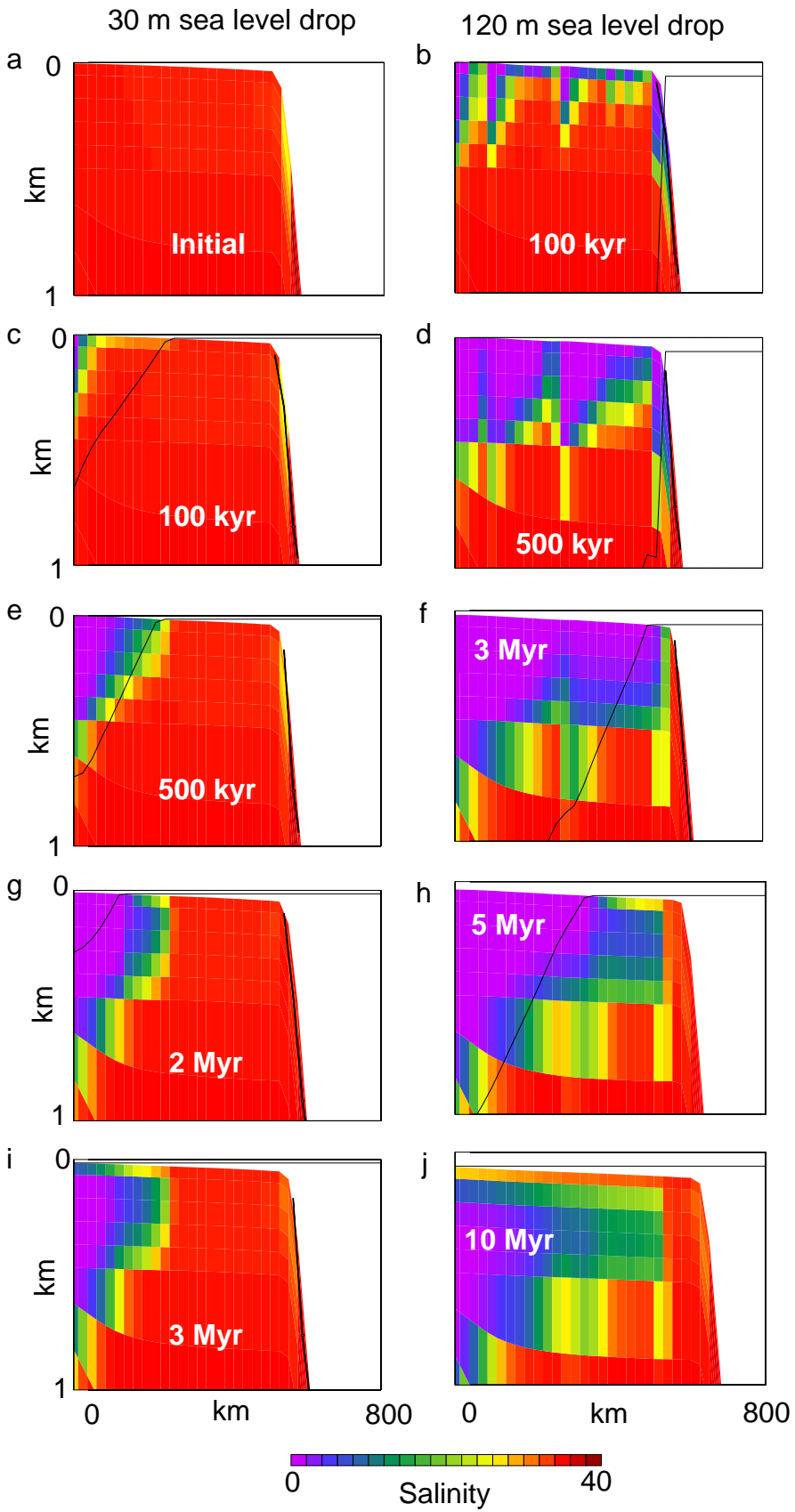


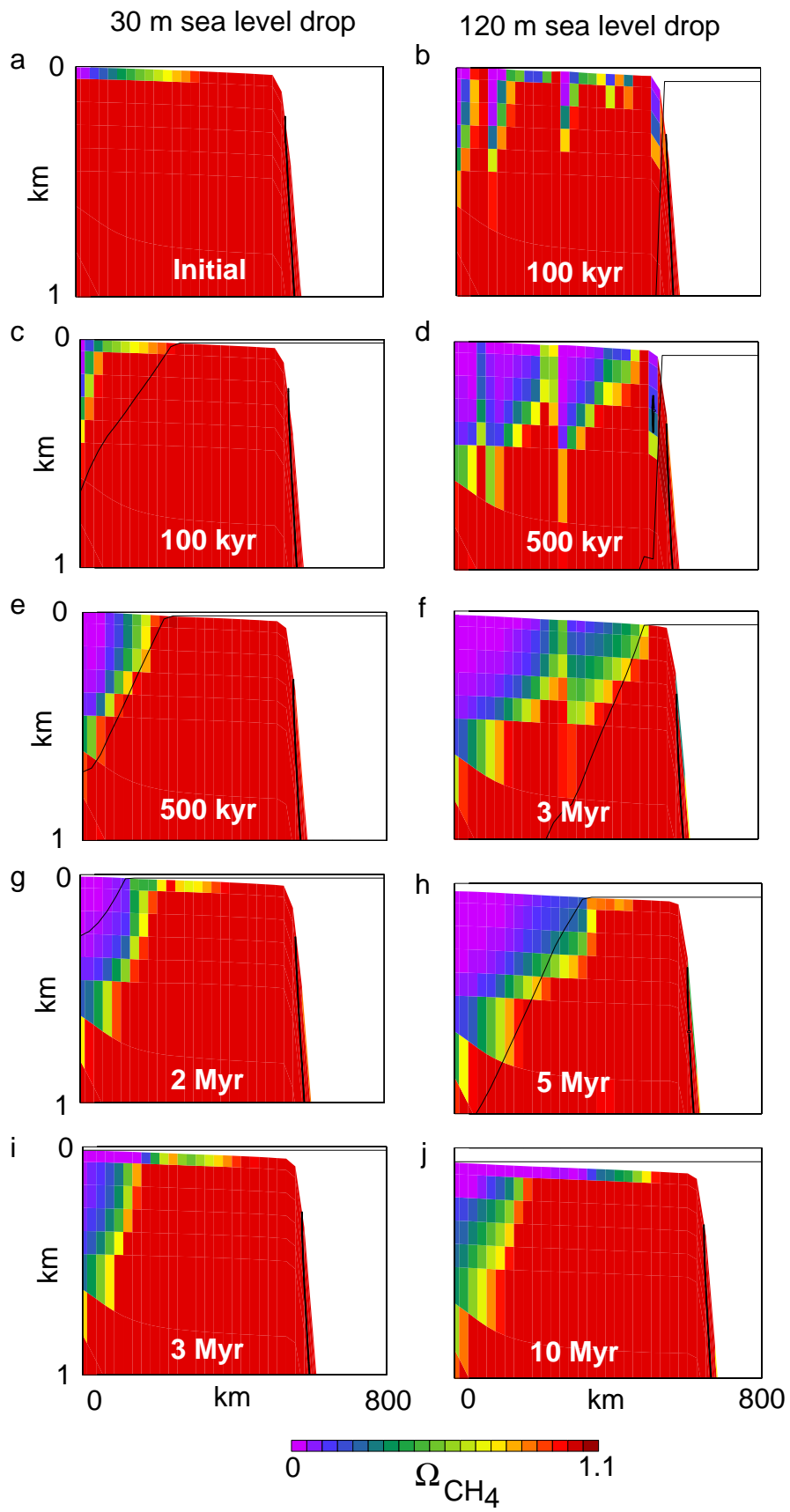
Figure 15



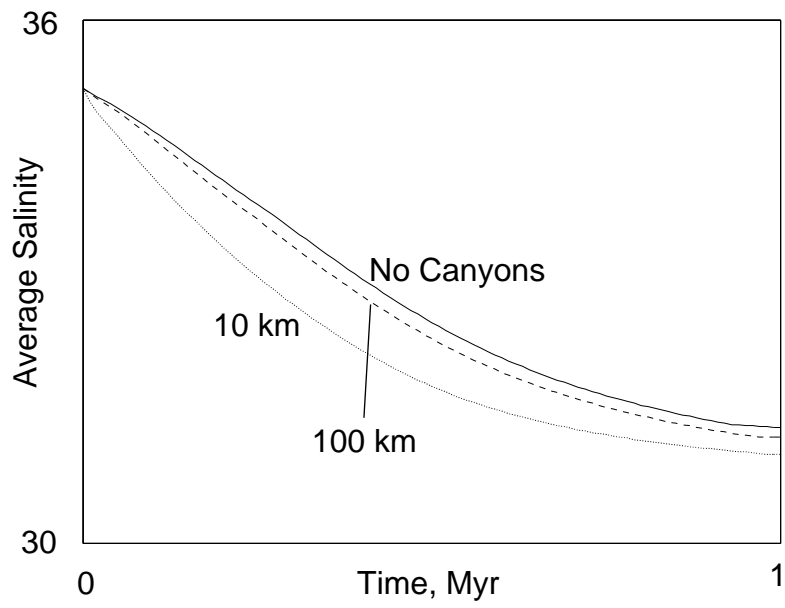
Supplemental Figure 1



Supplemental Figure 2



Supplemental Figure 3



Supplemental Figure 4