

Interactive  
Comment

## ***Interactive comment on “Dynamics of global atmospheric CO<sub>2</sub> concentration from 1850 to 2010: a linear approximation” by W. Wang and R. Nemani***

I G Enting (Referee)

ian.g.enting@gmail.com

Received and published: 26 December 2014

### **Additional comment 4: On ambiguity and feedback.**

In my initial report (Enting, 2014) on the paper by Wang and Nemani (Wang and Nemani, 2014a), I questioned their claim to estimate an additional carbon flux by combining their carbon model with their temperature effect.

With regard to their equation (2b) (i.e.

$\dot{E}' - \dot{A} = [\alpha_A + \alpha_S] \cdot A' - \alpha_S \cdot E' - \beta_T \cdot T'$ , Wang and Nemani (2014a) state that ‘collinearity between the two regressors prevents us from determining the coefficients associated with them separately’. (i.e. only a combination of  $\alpha_S$  and  $\alpha_S$  can be estimated).

Full Screen / Esc

Printer-friendly Version

Interactive Discussion

Discussion Paper

My argument is that one needs to go one step further and acknowledge that because of the high degree of collinearity between  $T'$ ,  $E'$  and  $A'$  only a combination of  $\beta_T$ ,  $\alpha_S$  and  $\alpha_S$  can be estimated. Wang and Nemani (2014a) have an estimate of  $\beta_T$  derived from their earlier work, but my argument implies that the estimate of the combination of  $\alpha_S$  and  $\alpha_S$  will depend on the value of  $\beta_T$ .

In discussing this issue, my report (Enting, 2014) referred to some of my earlier work (Enting, 2010). Since some readers may find this work difficult to access, I reproduce the discussion. The analysis is in terms of perturbations  $Q(t)$  and  $W(t)$  for concentration and temperature, non-CO<sub>2</sub> radiative forcing  $F(t)$ , anthropogenic emissions  $S(t)$ . Response functions  $U(t)$  and  $R(t)$  connect forcing to warming and emissions to concentrations respectively. A response function  $H(t)$  describes CO<sub>2</sub> emissions due to temperature change. A factor  $\eta$  ( $\alpha$  in the original) gives the (linearised) radiative forcing from CO<sub>2</sub>). The Laplace transforms of these functions are specified by lowercase letters:  $q(p)$ ,  $w(p)$ ,  $f(p)$ ,  $s(p)$ ,  $u(p)$ ,  $R(p)$  and  $h(p)$  respectively. Under the Laplace transform the convolutions with the response functions reduce to products so one has

$$w(p) = u(p)[f(p) + \eta q(p)]$$

and

$$q(p) = r(p)[s(p) + h(p)w(p)]$$

whence

$$q(p) = \frac{r(p)[s(p) + f(p) h(p) u(p)]}{1 - \eta u(p) r(p) h(p)}$$

Thus the observed airborne fraction  $\gamma$ , is not given by  $pr(p)$  but rather by  $pr(p)/[1 - \eta u(p) r(p) h(p)]$  (in the absence of other forcing). Thus estimates of  $r(p)$  (or parameters thereof) based on  $\gamma$  are going to depend on  $h(p)$  (i.e. on  $\beta_T$  in the specific model of Wang and Nemani (2014a)). Furthermore, there is no scope for estimating an additional flux  $\Phi(t)$  by taking  $q(p) = r(p)[s(p) + h(p)w(p) + \phi(p)]$   $\phi(p) = q(r)/r(p) - s(p) - h(p)w(p)$  with  $q(r)/r(p) - s(p)$  set to zero on the basis that

$r(p)$  is fitted to the observed airborne fraction. S noted above, the observed airborne fraction will be  $pr(p)/[1 - \eta u(p) r(p) h(p)]$ .

In my view the responses Wang and Nemani (2014b,c) have not addressed this criticism.

## References

- Enting, I. G.: Inverse Problems and Complexity in Earth System Science, in: Complex Physical, Biophysical and Econophysical Systems., edited by Dewar, R. L. and Detering, F., World Scientific, Singapore, 2010.
- Enting, I. G.: Interactive comment on “Dynamics of global atmospheric CO<sub>2</sub>...” (initial report by 1st referee), Biogeosciences Discussions, 11, C6416–C6422, 2014.
- Wang, W. and Nemani, R.: Dynamics of global atmospheric CO<sub>2</sub> concentration from 1850 to 2010: a linear approximation., Biogeosciences Discussions, 11, 13 957—13 983, 2014a.
- Wang, W. and Nemani, R.: Interactive comment on “Dynamics of global atmospheric CO<sub>2</sub>...” (response to first referee’s report), Biogeosciences Discussions, 11, C6624–C6629, 2014b.
- Wang, W. and Nemani, R.: Interactive comment on “Dynamics of global atmospheric CO<sub>2</sub>...” (response to second referee and additional comment (1) by 1st referee, Biogeosciences Discussions, 11, C7237–C7249, 2014c.

---

Interactive comment on Biogeosciences Discuss., 11, 13957, 2014.

**BGD**

11, C7629–C7631, 2014

---

Interactive  
Comment

Full Screen / Esc

Printer-friendly Version

Interactive Discussion

Discussion Paper

