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Date: 02 February 2016

Dear Dr. Akihiko Ito,

Please find our revised manuscript. Both referees provided helpful and insightful comments that have helped to improve the manuscript. The response to the referees is given underneath this letter. We hope that we have addressed the comments to the satisfaction of both referees.

In general we have reworded or extended the relevant sections in order to address the referees' comments. We have referred to these changes in the response to the referees. We have also taken the opportunity to edit and revise the manuscript to improve the clarity. Unless specifically requested by the referees, we have not substantively altered the content or format of the paper. In the revised manuscript, the text that is reordered is highlighted in blue. New text is highlighted in red. Deleted text is not indicated. The term "previous manuscript" used below belongs to published Biogeosciences discussion paper. The term "revised manuscript" belongs to the manuscript attached at the end.

We would like to clarify some points:

- 1. We have combined section 2 and 3 in the previous manuscripts as one section 2 in the revised manuscript following referee #2 comments.
- 2. We have moved P13974 L23-28 and P13975 L1-7 from the previous manuscript to section 2.2 in the revised manuscript (P7 L14-26).
- 3. We have combined sections 4 and 5 in the previous manuscript as one section 3 in the revised manuscript with new heading "Results and discussion" following both referees' suggestion.
- P13984 L22-25 and P13985 L1-6 in the previous manuscript are deleted to avoid repetition. P13985 L6-18 in the previous manuscript are moved to section 3.3 in the revised manuscript (P19 L6-18).
- 5. P13985 L20-27 and P13986 L1-13 in the previous manuscript are moved to section 3.2 in the revised manuscript (P17 L27-28, P18 L1-13).
- 6. Section 5.3 of the previous manuscript appears as new section 3.4 in the revised manuscript with heading "Some issues and limitations of this study in estimating uncertainty using the NRH model".

Old figure number in the previous manuscript	New figure number in the revised manuscript
Figure 1	Figure 1
Figure 2	Figure 2
Figure 3	Figure 3
Figure 4	Figure 6
Figure 5	Figure 7
Figure 6	Figure 8

7. We revise some figures in the manuscript as follows:

Figure 7	Figure 5
Figure S4a	Figure 4

8. The following references have been added in the revised manuscript.

Beer, C., Reichstein, M., Tomelleri, E., Ciais, P., Jung, M., Carvalhais, N., Rödenbeck, C., Arain,
M. A., Baldocchi, D., Bonan, G. B., Bondeau, A., Cescatti, A., Lasslop, G., Lindroth, A., Lomas,
M., Luyssaert, S., Margolis, H., Oleson, K. W., Roupsard, O., Veenendaal, E., Viovy, N.,
Williams, C., Woodward, F. I., and Papale, D.: Terrestrial Gross Carbon Dioxide Uptake: Global
Distribution and Covariation with Climate, Science, 329 (5993), 834–838, 2010.

Goulden, M. L., Munger, J. W., Fan, S.-M., Daube, B. C., Wofsy, S. C.: Measurements of carbon sequestration by long-term eddy covariance: methods and a critical evaluation of accuracy, Global Change Biol., 2(3), 169–182, 1996.

Moncrieff, J. B., Malhi, Y., Leuning, R.: The propagation of errors in long-term measurements of land-atmosphere fluxes of carbon and water. Glob. Change Biol. 2 (3), 231–240, 1996.

Rabinowitch, E. I: Photosynthesis and Related Processes, Soil Science, 72, 482, 1951.

Richardson, A.D., Hollinger, D.Y., Burba, G.G., Davis, K.J., Flanagan, L.B., Katul, G.G., Munger, J.W., Ricciuto, D.M., Stoy, P.C., Suyker, A.E., Verma, S.B., Wofsy, S.C.: A multi-site analysis of random error in tower-based measurements of carbon and energy fluxes. Agric. Forest Meteorol., 136, 1–18, 2006b.

Richardson, A. D., Mahecha, M. D., Falge, E., Kattge, J., Moffat, A. M., Papale, D., Reichstein, M., Stauch, V. J., Braswell, B. H., Churkina, G., Kruijt, B., Hollinger, D. Y.: Statistical properties of random CO 2 flux measurement uncertainty inferred from model residuals. Agric. Forest Meteorol., 148, 38–50, 2008.

Sun, J., Guan, D., Wu, J., Jing, Y., Yuan, F., Wang, A., and Jin, C.: Day and night respiration of three tree species in a temperate forest of northeastern China, iForest - Biogeosciences and Forestry, 8 (1), 25-32, 2015.

Teskey, R.O., Saveyn, A., Steppe, K., and McGuire, M.A.: Origin, fate and significance of CO_2 in tree stems, New Phytol., 177 (1), 17-32, 2008.

We look forward to hearing from you.

Yours sincerely

Mr Rahul Raj (on behalf of all authors)

Response to Referee #1 for "Uncertainty analysis of gross primary production partitioned from net ecosystem exchange measurements" by R. Raj et al.

We thank for the constructive and helpful comments for our manuscript. We have carefully considered all comments and these have incorporated in our revised manuscript accordingly. We have inserted our response to each comment. We use "RC" for referee's comment and "AR" for author's response.

General comments of Referee #1:

RC 1: Raj et al. present a new way to evaluate the uncertainty tied to the estimation of the gross primary productivity (GPP) derived from the eddy covariance measurements of net ecosystem exchange (NEE). They use a Bayesian approach, moving from the regression analysis of rectangular hyperbola fitting daytime data. The argument treated is within the scope of Biogeosciences and the computational instrument they developed is promising. Nevertheless, at this current stage the study suffer from several limitations, not only in the presentational form but also in the substance. In fact, several sources of uncertainty exist in the partitioning the GPP from eddy covariance data. GPP is not directly measured and must be extrapolated from available NEE. Both extrapolation approaches, from night-time or daytime data, can suffer from systematic errors. At least, the authors should acknowledge that a) day respiration can be significantly different from night respiration in reason of the different processes occurring at leaf level (photorespiration or dark respiration). Lower respiration values are expected during the day, see Sun et al. (2015), although compensatory effect could occur (Reichstein et al, 2005); b) the shape of the light response curve measured by eddy covariance can be significantly biased by an inadequate quantification of the storage contribution of the NEE flux, particularly if measurements are taken above high canopies like in the present study. I'm unsure that the authors can quantify these potential sources of bias using the data they have, but at least they should clearly state that they analysed only a component of the possible uncertainty sources. Overall, the approach used by Beer et al., 2010, still seems more solid.

AR 1: Indeed these are important issues. We used a temperature dependent respiration term that is equal for day and night. The fact that we have not parameterized respiration separately for day and night (or separately for vegetation and soil) can be considered as limitations of our model. Indeed the respiration of the vegetation may depend on other factors such as irradiance (Sun et al., 2015). Some other terms are also not included our respiration estimates: photorespiration (because it is nearly proportional to GPP), and respiration terms of which the produced CO₂ remains in the trees (Teskey et al., 2008). Our GPP estimates are uncorrected for these particular respiration terms. It is technically possible to extend the model by including more parameters and statistically test whether the model fit with additional parameters performs better, but we doubt whether this will improve the estimates of GPP, given the limitations of our data: we do not have independent measurements of respiration terms (by means of gas chambers).

The night time storage can indeed affect the diurnal shape of the NEE measurements, in particular when CO_2 builds up below the sensor height during stable nights which is released when the surface layer becomes unstable after sunrise. Even though some of the stable night time data have been excluded by the quality filtering due to insufficient turbulence, we cannot exclude that the diurnal cycle is affected by storage effects. In the revision, we will acknowledge these limitations of our study. Nevertheless, we believe that the method to establish credible intervals (metrics of uncertainty) in the parameter estimates for the non-rectangular hyperbola (NRH) model with

temperature dependent respiration term is useful. For most sites this is still the best we can do, and by providing an algorithm at least the uncertainties of the model parameters can be estimated.

The approach of Beer et al. (2010) is an extensive study with a wide scope. They partitioned GPP (at FLUXNET sites) from NEE both using a rectangular hyperbola (RH) light-response curve (Lasslop et al., 2010) and conventional night-time data based approach (Reichstein et al., 2005). They used these partitioned GPP to calibrate five highly diverse diagnostic models for GPP to produce the distribution of global GPP. In our study, we tried to understand better the uncertainty in partitioning GPP using NRH light-response curve. Future research can build on our findings and extend our approach in order to estimate uncertainty across various flux tower sites with different GPP characteristics. We have already highlighted the importance of our findings in the manuscript (P13988 L21 to L 23).

We have clarified all the above points in our revised manuscript (P20 L11-26, P21 L13-19).

Comments of Referee #1 on the structure of the paper:

RC 2: Much of the text is used to present and define the computational approach used. If this could perfectly fit for a Journal like Geoscientific Model Development, it could become probably excessively complicated for a wide audience like that of Biogeosciences. Even more importantly, the sections defined as '4. Results' and '5. Discussion', are similarly presenting some of the results and partially discuss them. In the revision, I recommend to decide if the paper will have a discussion section separated from the presentation of the results, since what is done in the current text version is confusing. Overall, I recommend this study for publication, but only after a thorough work of revision.

AR 2: We understand that the computational approach used in this study may be complicated to some of the audience of Biogeosciences. We have tried to explain the flux partitioning in a Bayesian framework in a clear way and we have given this further attention in the revised manuscript. We trust that the audience of Biogeoscience will not have any problem to understand our computational approach. We have followed the advice of the referee to combine the Results and discussion section in the revised manuscript.

Specific comments of Referee #1:

RC 3: P13972 L23 'ecosystem scientists' use positive values of GPP. To my knowledge, GPP is always positive since it represents a production, and production was represented with positive values much earlier than Brahmagupta, in the 7th century, described negative numbers. If we use the micrometeorological approach, the most correct term will be probably gross ecosystem exchange (GEE), which is defined as negative since it represents the quantity of CO2 which enters in the ecosystem.

AR 3: We have also used positive sign for GPP. To avoid the confusion that only ecosystem scientists use positive value for GPP, we have removed the term "ecosystem scientist" (line P13971 L23 in the previous manuscript) in the revised manuscript. We have also rephrased P13971 L23 to L25 to clarify that GPP is always positive as it represents production. Please check P6 L14-16 in the revised manuscript.

RC 4: P13972L16-18 Units are missing in the passage from 'Pa' to 'GPP'. In fact, NEE is generally expressed in terms of micromoles m-2 s-1, and GPP with the same units or in terms of g m-2 d-1. Here, in table 1, both quantities are expressed in terms of g CO2 m-2 s-1, so the proposed conversion factor of 12/44 shouldn't be present. In any case, it converts for instance micromoles of CO2 into micrograms of C.

AR 4: The conversion of unit from μ mole CO₂ m⁻² s⁻¹ to g C m⁻² s⁻¹ requires the multiplication of factor by 12/44. Originally, we had the unit of NEE in micromoles CO₂ m⁻² s⁻¹ and we converted it to mg CO₂ m⁻² s⁻¹ (This unit appears in Table 1 for NEE and also for Pa) that does not require the multiplication by factor 12/44. We have expressed GPP in g C m⁻² s⁻¹, so we multiplied Pa by 12/44 in order to account only carbon (C) in the unit of GPP. We agree that this was not clearly expressed in the previous manuscript. We have given a clear explanation of unit and its conversion in the revised manuscript (P7 L10-13).

RC 5: P13974 L13-14 'NEE data were corrected for storage of CO2 in the air between the sensor and the ground'. The storage is a relevant component or in the mixing ratio conservation equation (e.g, Kowalski and Argueso, 2011) and hence in the correct computation of NEE. Although the storage terms tend to cancel out when producing annual sums, it is well established that they can asymmetrically influence the apparent light response curve, presenting opposite values in the evening and in the morning and a significant hysteresis. It has been clearly established that a convenient number of measurement points have to be established when measurements are dove above forests (Yang et al., 2007), but there is no mention about the instrumentation used. More information is needed!

AR 5: We regret that we have made a mistake in the data description. We have not carried out a storage correction of the CO_2 flux since profile measurements were unavailable. We had installed a second Eddy Covariance system at 35 m height, and there was no significant difference in magnitude of the flux and shape of the diurnal cycle compared to the height of 46 m. However, we did not have flux or concentration measurements below this height, thus within the canopy, the place where storage effects will be most significant. The storage effects on daily or annual NEE may be limited, but we agree that it most likely affects the light response curves. The morning-afternoon hysteresis effect will contribute to higher scatter in the model fit, and thus to more uncertainty in the retrieved parameters and the GPP estimates. We have discuss this in the revised manuscript (P20 L18-26).

RC 6: P13982 'credible interval spanned zero'. After this sentence there is one paragraph of discussion. What the authors mean exactly? Was the mean zero and the distribution of values partially above it, or there was a bias?

AR 6: A Bayesian prediction gives a probability distribution, this can be summarized by the median and the 95% credible interval as a quantification of uncertainty. Hence the actual value is likely to be somewhere in this interval and not necessarily at the median. The predicted median is negative during the night; however, the credible interval spans zero, implying that the actual value could be positive. Clearly this is not physically possible, but is an artefact of the statistical approach and highlights that we are indeed uncertain about these predictions. We have explained the possible reasons in P13983 from L1 to L12 in the previous manuscript. We have given more clarification in the revised manuscript (P15 L18-19, P16 L26-28).

RC 7: P1396 L2 'was obtained from the literature'. Please be specific.

AR 7: We have refereed the section here in the revised manuscript (P9 L21-23) that provides the proper citations for the prior information about each parameter.

RC 8: P13978: 'the photosynthetic capacity. . . is reached when the photosynthesis is Rubisco limited varies among different tree species'. At canopy level, the photosynthetic capacity depends also on the structure of the canopy, when multiple leaf layers are present Amax increases. Please read carefully the cited paper of Ruimy et al., 1995.

AR 8: Non-rectangular hyperbola (NRH) model used in this study requires Amax at canopy level. We agree with the referee that the photosynthesis capacity at the canopy level also depends on the structure of the canopy (i.e. arrangement of the canopy leaves) and the area of leaves available to absorb photons. Both are determined by leaf area index (Ruimy et al., 1995). It should be noted that we have also used leaf area index to determine canopy Amax using a model that incorporates a radiative transfer scheme and a vertically declining needle-level Amax. We have given clear explanation of canopy level Amax in the revised manuscript (P11 L20-22).

RC 9: P13978 L15. 'in the literature were 0.0097...', again, please be specific on the sources and also add units (is mg CO2 m-2s-1 valid for all the numbers reported?).

AR 9: We have already provided the sources in L16 at the end of the sentence. Please refer to P12 L8-11 in the revised manuscript. The unit of mg CO_2 m⁻²s⁻¹ is valid for all numbers reported.

RC 10: P13980 L 13-14: 'but was short enough that we could observe temporal change between the 10-day blocks'. This is strange, possibly the authors were meaning the contrary (long enough)?

AR 10: When selecting the block length there was a trade-off between selecting a block that was LONG enough to contain sufficient measurements for accurate modelling yet SHORT enough to allow us to observe changes between the blocks. Thus the temporal change is observed between consecutive blocks, not within a block. We have clarified this in the revised manuscripts (P14 L12-15).

RC 11: P13982 L6-7: 'The chains were thoroughly interdigitating, indicating that the the Markov chains had mixed and converged. . .' Besides the repeated article, I cannot understand. In any case, I recommend to avoid lab jargon.

AR 11: We have explained in P13973 L20 to L27 that the stationary distribution of the Markov chains is the posterior distribution of parameters. The stationary distribution can be assessed graphically (Fig. S3 in the supplementary file) when the Markov chains interlock with each other (in other words, chains thoroughly interdigitate) showing the proper mixing of the chains. We have clarified this in the revised manuscript (P14 L21-26, P16 L6-7).

RC 12: Figure 1: Please define what Y axis represents.

AR 12: Y axis represents the density of the distribution of NRH parameter. We have added this in the caption of figure 1 in the revised manuscript.

RC 13: Figure 3: What are the frequency units in the Y axes?

AR 13: In the histogram, the Y axis has no unit. Y axis represents the frequency or the number of GPP points.

RC 14: Figure 4: What are the units in the Y axes?

AR 14: At the end of figure 4 caption, we have mentioned that information about NRH parameters (showed as symbol in the Y axis of the plots) is given in Table 1 that shows the meaning and the unit of the symbol of NRH parameters. Figure 4 is now Figure 6 in the revised manuscript.

RC 15: Figure 5: What are the units in the Y axes? I add that in this set of images, a magnifier is needed to distinguish what is reported along the axes, at least for many readers including myself.

AR 15: We have written "as Fig. 4" at the start of the figure 5 caption. This means that our response AR 14 is also valid here for the unit. We have redrawn the figure 4 and 5 (which are figure 6 and 7 in the revised manuscript) to make the values along the axis more visible in the revised manuscript.

Minor/language remarks of referee 2:

RC 16: Page (P) 1397 Line (L) 21 'a non linear empirical models': please check the consistency between article and noun. P1397 L26-27: 'a single optimized values', same as above.

AR 16: We have corrected this in the revised manuscript (P3 L20, P4 L24-25).

RC 17: P13974 L8 Cambell->Campbell

AR 17: We have correct this in the revised manuscript (P5 L21).

RC 18: P13982: Lay->Laid

AR 18: We have corrected this in the revised manuscript (P16 L15).

RC 19: P13984 L24-25. 'In order to undertake a Bayesian analysis it is necessary to specify the prior distributions on the NRH parameters.' Written in this way, it seems that the use of NRH parameters is a general rule in Bayesian analysis, but it is not.

AR 19: We agree with the referee. It should be noted that this sentence now doesn't appear in the revised manuscript after combining Results and Discussion section.

RC 20: 13985 L8-9: 'This wide variation in Amax was chosen as the non-informative priors led to spikes in the value of Amax in the posterior (Fig. 5e).' Remove 'was' and possibly reformulate the sentence.

AR 20: We have rephrased this sentence in the revised manuscript (P19 L6-10).

References:

Beer, C., Reichstein, M., Tomelleri, E., Ciais, P., Jung, M., Carvalhais, N., Rödenbeck, C., Arain, M.A., Baldocchi, D., Bonan, G.B., Bondeau, A., Cescatti, A., Lasslop, G., Lindroth, A., Lomas, M., Luyssaert, S., Margolis, H., Oleson, K.W., Roupsard, O., Veenendaal, E., Viovy, N., Williams, C., Woodward, F.I., Papale, D., 2010. Terrestrial Gross Carbon Dioxide Uptake: Global Distribution and Covariation with Climate. Science 329 (5993), 834-838. Kowalski, A.S., ArgÜEso, D., 2011. Scalar arguments of the mathematical functions defining molecular and turbulent transport of heat and mass in compressible fluids. Tellus B 63 (5), 1059-1066.

Lasslop, G., Reichstein, M., Papale, D., Richardson, A.D., Arneth, A., Barr, A., Stoy, P., Wohlfahrt, G., 2010. Separation of net ecosystem exchange into assimilation and respiration using a light response curve approach: critical issues and global evaluation. Global Change Biology 16 (1), 187-208.

Reichstein, M., Falge, E., Baldocchi, D., Papale, D., Aubinet, M., Berbigier, P., Bernhofer, C., Buchmann, N., Gilmanov, T., Granier, A., Grünwald, T., Havránková, K., Ilvesniemi, H., Janous, D., Knohl, A., Laurila, T., Lohila, A., Loustau, D., Matteucci, G., Meyers, T., Miglietta, F., Ourcival, J.-M., Pumpanen, J., Rambal, S., Rotenberg, E., Sanz, M., Tenhunen, J., Seufert, G., Vaccari, F., Vesala, T., Yakir, D., Valentini, R., 2005. On the separation of net ecosystem exchange into assimilation and ecosystem respiration: review and improved algorithm. Global Change Biology 11 (9), 1424-1439.

Ruimy, A., Jarvis, P., Baldocchi, D., Saugier, B., 1995. CO2 Fluxes over Plant Canopies and Solar Radiation: A Review. Advances in Ecological Research 26, 1-68.

Sun, J., Guan, D., Wu, J., Jing, Y., Yuan, F., Wang, A., Jin, C., 2015. Day and night respiration of three tree species in a temperate forest of northeastern China. iForest - Biogeosciences and Forestry 8 (1), 25-32.

Teskey, R.O., Saveyn, A., Steppe, K., McGuire, M.A., 2008. Origin, fate and significance of CO₂ in tree stems. New Phytologist 177 (1), 17-32.

Yang, B., Hanson, P.J., Riggs, J.S., Pallardy, S.G., Heuer, M., Hosman, K.P., Meyers, T.P., Wullschleger, S.D., Gu, L.-H., 2007. Biases of CO2 storage in eddy flux measurements in a forest pertinent to vertical configurations of a profile system and CO2 density averaging. Journal of Geophysical Research: Atmospheres 112 (D20123).

Response to Referee #2 for "Uncertainty analysis of gross primary production partitioned from net ecosystem exchange measurements" by R. Raj et al.

We would like to thank for the constructive and helpful comments for our manuscript. We have carefully considered all comments and these have incorporated in our revised manuscript accordingly. We have inserted our response to each comment. We use "RC" for referee's comment and "AR" for author's response.

Major comments of Referee #2:

RC 1: The residual term in equation 6 is not the uncertainty for measured NEE (P15L9-10). The socalled uncertainty for NEE is from the NRH model used in this study. Some statistical flux-partitioning methods (like NRH used in this study) could be used to either estimate GPP and ER or fill missing data. The authors have to carefully state the usage of their approach. Don't go too far and away from parameter uncertainty analysis.

AR 1: We do not fully agree with the referee that the residual term in equation 6 is not the uncertainty in measured NEE. The residual term contains the model representation error and the random measurement error. Richardson et al. (2008) showed that the uncertainty estimates inferred from the model residuals of the tuned empirical models, which are fitted to NEE data, are comparable to the total random measurement error in NEE data estimated using pair measurements approach (Richardson et al., 2006). In our study, we have fitted the empirical non-rectangular hyperbola (NRH) model to the measured NEE. We can expect, based on the finding of Richardson et al. (2008), that the residual term in equation 6 is comparable in magnitude to the uncertainty due to the total random error in NEE measurements at the study site. However, this is not claimed in our study as we have not compared the model residuals with the uncertainty estimates from the pair measurements approach at the study site. Such a comparison may be the potential future work at the study site. Due to the lack of such comparison, we do not say that what we estimate is the uncertainty in measured NEE. Instead, we say that this is the uncertainty in posterior prediction of NEE (section 3.4 in the manuscript) that results from both the model residuals and the uncertainty in the posterior prediction of NRH parameters. It was checked in this study whether we would obtain realistic credible intervals of uncertainty in the posterior prediction of NEE after fitting the NRH model in a Bayesian framework (section 3.4 in the manuscript). In this way, we verified that realistic credible intervals of uncertainty in partitioned GPP were also obtained. This was all well in line with the main objective of this study, namely to estimate uncertainty in partitioned GPP (and hence not in NEE). Our approach can also be used to either estimate ER or fill missing NEE data, but we focused mainly on partitioning GPP with uncertainty.

Apart from the random errors, systematic errors also give rise to uncertainty in NEE measurements (Moncrieff et al., 1996, Aubinet et al., 2012). We have applied the Foken classification system (Foken et al., 2005, section 3.1 in the manuscript) to filter out the low quality NEE measurements that contain high systematic errors. This reduces the systematic errors on the posterior prediction of NRH parameters and model residuals. Therefore, we expect that the posterior prediction of NEE and GPP are less influenced by the systematic errors in NEE measurements.

We have included all above points in the revised manuscript (P20 L5-26)

RC 2: The authors have to acknowledge that the uncertainty quantified in this study is just a part of GPP uncertainty sources, since some factors (such as water and nutrient limitations) were missing in the photosynthesis model. The authors only quantified the GPP uncertainty based on a photosynthesis model.

AR 2: We agree that the factors such as water and nutrient limitations are missing in the NRH model. Hence we agree with the reviewer that we only quantified uncertainty based on the photosynthesis model. However, a particular feature of our implementation is that we estimated the parameters in 10-day blocks and did not assume constant values for the whole study period. This approach is recommended by Aubinet et al. (2012), since the parameters may vary over time for example due to dependencies on factors that are not included in the model (e.g., water and nutrient limitations). Hence, although these variables are not included in the model our implementation does account for them. We have also obtained the posterior distribution of NRH parameters separately for each 10day block during the study period and finally in the prediction of GPP. This is mentioned in the previous manuscript (second paragraph of section 3.3 and first paragraph of section 5.3). We have clarified the above points in the revised manuscript (P14 L5-17, P19 L22-28, and P20 L1-4)

RC 3: Content: The verification of the approach is important, but could go to supplementary.

AR 3: We have verified our approach in two ways: (1) we examined the trace plot of the three Markov chains and Gelman-Rubin PSRF statistics of each NRH parameter. This is explained briefly in the first paragraph of section 4.1 in the manuscript. We have already provided the details in sections 1 to 4 in the supplementary file; and (b) we showed the 95% credible interval of the posterior predictions of half-hourly NEE against measured half-hourly NEE. In this way, we checked whether realistic credible intervals were obtained (see also the second paragraph of AR 1). We, however, discussed this in the previous manuscript (paragraphs 2 and 3 in section 4.1) as we think that this is important in the context of verifying indirectly the credible intervals of GPP. The section 4.1 is now section 3.1 in the revised manuscript.

RC 4: Structure: Introduction could be more concise. For example, NEE = ER–GPP or NEP = GPP-ER. One sentence might be enough. The section 3 could be included in section 2 (Methods). The results should not include discussion. Anyway, the authors have to re-structure the manuscript.

AR 4: We have revised the manuscript to improve the readability. We have combined section 2 and 3. We have also combined results and discussion section.

Specific comments of Referee #2:

RC 5: P3 L8-9: remove ",which is partitioned from NEE,"

AR 5: We understand the concern of the referee that GPP can be obtained from other sources also. Therefore, the general statement like in line P3 L8-9 in the previous manuscript should not include the specific source of GPP via partitioning. We have removed this in our revised manuscript.

RC 6: P3 L9-11: Not only measured NEE but also derived GPP and ER are used to test the processbased models.

AR 6: We agree with the referee. We have already mentioned this in lines P3 L11 -15 in the previous manuscript. We have added GPP and R_{eco} after component flux to clarify it in the revised manuscript (P3 L11).

RC 7: P3 L12: after component fluxes, add (GPP and Reco).

AR 7: As mentioned in AR 6, we have added this in the revised manuscript (P3 L11).

RC 8: P4 L5: Better to cite the original reference for NRH photosynthesis model. Rabinowitch 1951 could be better.

AR 8: We are thankful to referee for this suggestion. We have added this reference in the revised manuscript.

RC 9: P4 L9-12: Move after P4 L3, it was still talking about RH model.

AR 9: We have moved these lines accordingly in the revised manuscript (P4 L2-5).

RC 10: P4: L12: repeat?

AR 10: We have addressed this in the revised manuscript.

RC 11: P4 L24: "for the calibration of process-based models"

AR 11: We have rephrased the sentence accordingly in the revised manuscript (P4 L22).

RC 12: P6 L1: Rabinowithc 1951 might be better.

AR 12: We have include this reference in the revised manuscript.

RC 13: P8 L 22-P9 L7: It could go early. The authors suggested that the effects of VPD could be neglected, but I did not see any VPD term in equations 1-4 or 6.

AR 13: Some versions of equation 2 include the VPD term (e.g., Gilmanov et al., 2013); however we have removed it because VPD in our study area is always low and below the critical value where it will have an effect. That is why we have explained in P8 L23 in the previous manuscript (P7 L14-16 in the revised manuscript) that VPD-response function is simply multiplied with equation 2 to incorporate the effect of VPD. Further, in P8 L24 to L28 and P9 L 1 to L7 in the previous manuscript (P7 L16-26 in the revised manuscript), we have explained why we have not included VPD-response function in equation 2.

RC 14: P9 L16: RHS Represent?

AR 14: RHS represents right hand side. We have mentioned this in the revised manuscript (P9 L11).

RC 15: P9 L23: I'm confused. Here the authors said a non-informative prior was selected and afterwards two methods (non-informative and informative prior distributions) were compared.

AR 15: In Bayesian analysis a prior distribution is required for all parameters, i.e., for precision and for other coefficients (NRH parameters in this study). We have used the same non-informative prior distribution for precision for both choices of informative and non-informative prior distributions of NRH parameters. We have clarified this in the revised manuscript (P9 L16-25).

RC 16: P17 L1-2: Remove ", so it is important to . . . means."

AR 16: We have removed this in the revised manuscript.

RC 17: P17 L7: In the Results section? The authors might combine results and discussion as one section.

AR 17: Considering the advice of both reviewers we have decided to combine the results and discussion sections into a single section. We have done this in the revised manuscript.

RC 18: P18 L20 –P19 L18: the unrealistic estimates for parameters could attribute to the statistic method itself. It's not necessary to describe the results of non-informative prior distribution, as two methods may get similar results. Except that the authors would recommend using non-informative prior distribution, it will not change the story.

AR 18: The choice of non-informative priors for NRH parameters can be easily questioned by the readers as these are not site and species specific. We believe that the recommendation about the choice of non-informative priors over informative priors only by statement is not sufficient and will not give confidence to the readers who want to use it for specific site and species. Therefore, we have compared the results, wherever it was possible, to support the choice of non-informative priors over informative priors. Actually, we do recommend the use of non-informative priors for NRH parameters. We have revised the manuscript to provide a clearer explanation of the methods in order to make the paper more accessible to those who are not familiar with Bayesian statistics.

RC 19: P21 L2-4: As I mentioned early, this study is not appreciate to estimate the uncertainty of NEE that has been measured through the eddy covariance technique.

AR 19: Please note our responses to AR 1, we have carefully rephrased this in the revised manuscript.

RC 20: Table 1: VPD related parameters just appeared in the text. I would suggest add to the equations.

AR20: Please refer to our response AR 13.

RC 21: Fig 2, 4, and 5: no difference I can detect for non-informative prior distributions and informative prior distributions. Again, to my opinion, there is no need to compare.

AR 21: Please see our response AR 18.

RC 22: Fig.3: The distribution of simulated GPP in the morning or in the afternoon does not give me expected information. The daily GPP distribution might be interesting, as it showed the uncertainty of estimated GPP.

AR 22: We have provided the results of the distribution of half-hourly GPP in the morning and afternoon to visualize the uncertainty within a day. These results also allowed us to see that partitioned half-hourly GPP follow the expected changes within a day with radiation. Therefore, it is

important to keep these results in the manuscript. We have emphasized this even further by showing the distribution of daily GPP for two days (Fig. 3). In addition, we have moved Fig. S4a from supplementary file to the revised manuscript (Fig. 4) to show the distribution of daily GPP over the study period.

RC 23: Fig S4-5. The key results (Fig. S4) can be put in the main paper.

AR 23: We have moved Fig. S4a (Fig. 4) in the revised manuscript. However, we keep Fig. S4b in the supplement as Fig. S4a is sufficient to show the distribution of daily GPP over the study period.

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Uncertainty analysis of gross primary production partitioned from net ecosystem exchange measurements

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Abstract

Gross primary production (GPP) can be separated from flux tower measurements of net ecosystem exchange (NEE) of CO₂. This is used increasingly to validate process-based simulators and remote sensing-derived estimates of simulated GPP at various time steps. Proper validation includes the uncertainty associated with this separation. In this study, 5 uncertainty assessment was done in a Bayesian framework. It was applied to data from the Speulderbos forest site, The Netherlands. We estimated the uncertainty in GPP at half hourly time steps, using a non-rectangular hyperbola (NRH) model for its separation from the flux tower measurements. The NRH model provides a robust empirical relationship between radiation and GPP. It includes the degree of curvature of the light response curve, 10 radiation and temperature. Parameters of the NRH model were fitted to the measured NEE data for every 10-day period during the growing season (April to October) in 2009. We defined the prior distribution of each NRH parameter and used Markov chain Monte Carlo (MCMC) simulation to estimate the uncertainty in the separated GPP from the posterior distribution at half-hourly time steps. This time series also allowed us to estimate the un-15 certainty at daily time steps. We compared the informative with the non-informative prior distributions of the NRH parameters and found that both choices produced similar posterior distributions of GPP. This will provide relevant and important information for the validation of process-based simulators in the future. Furthermore, the obtained posterior distributions

²⁰ of NEE and the NRH parameters are of interest for a range of applications.

Introduction 1

Net ecosystem exchange (NEE) is a terrestrial component of the global carbon cycle. It is the exchange of CO_2 between the terrestrial ecosystem and the atmosphere. The measurement of NEE by the eddy covariance technique is well-established (Baldocchi, 2003). Specifically, NEE is the balance between the CO₂ released by the ecosystem respiration 5 (R_{eco}) and the gross CO₂ assimilated via photosynthesis. The fraction of carbon in the assimilated CO₂ is the gross primary production (GPP). Estimates of GPP provide information about the physiological processes that contribute to NEE (Aubinet et al., 2012). Measured NEE data are used to validate the NEE that is simulated by ecosystem process-based simulators such as BIOME-BGC (BioGeochemical Cycles) (Thornton, 1998). It is often desirable 10

- to validate the simulated component flux (R_{eco} and GPP) independently. This is particularly important for diagnosing the misrepresentation (overestimation or underestimation) of assimilation processes in the simulator (Reichstein et al., 2005), which can only be achieved by comparing the GPP partitioned from NEE data with the simulated one. Furthermore,
- remote sensing-derived light use efficiency (LUE) models address the spatial and temporal 15 dynamics of GPP (Running et al., 2004). The reliability of such models at the regional scale relies on the validation using GPP partitioned from NEE data (Wang et al., 2010; Li et al., 2013).

Flux partitioning methods (FPM) are used to partition NEE into its component flux (GPP and R_{eco}). These methods are based on fitting a non-linear empirical model to the mea-20 sured NEE data and other meteorological data in order to estimate the parameters. The estimated parameters of the non-linear model are then used to predict daytime R_{eco} and GPP. There are two types of FPM: (1) those that use only nighttime NEE data, and (2) those that use either daytime NEE data or both daytime and nighttime data (Lasslop et al., 2010; Stoy et al., 2006; Aubinet et al., 2012). 25

A nighttime-based FPM assumes that NEE is equal to R_{eco} (GPP = 0 during the night) and that it varies with air and soil temperature (Richardson et al., 2006a). A daytime-based FPM assumes that the variation of NEE occurs with photosynthetic photon flux density (PPFD) and the light response curve (plot of NEE against PPFD) can be represented by a rectangular hyperbola (RH) model (Ruimy et al., 1995). Lasslop et al. (2010) proposed a daytime-based FPM using the RH model by incorporating the variation of NEE as a function of global radiation, air temperature, and vapour pressure deficit (VPD) because these

- ⁵ affect GPP via stomatal regulation. A daytime-based FPM was proposed that uses the nonrectangular hyperbola (NRH) model to incorporate the effect of the degree of curvature (θ) of the light response curve (Gilmanov et al., 2003; Rabinowitch , 1951). θ represents the convexity of the light response curve as the NEE and radiation relationship approaches saturation. Further, the light response curve represented by the NRH model has been found
- ¹⁰ to fit NEE data better than the RH model (Gilmanov et al., 2003; Aubinet et al., 2012). Gilmanov et al. (2013) further improved the NRH model by incorporating the effect of VPD and temperature as proposed by Lasslop et al. (2010). They used PPFD and soil temperature instead of global radiation and air temperature respectively. This improvement incorporates the influence of PPFD, air or soil temperature, VPD, and θ by taking advantage of better representation of the light response curve by comparison to the RH model.

A quantification of uncertainty in partitioned GPP provides an associated credible interval that can be used for proper implementation of calibration and validation of a process-based simulator against partitioned GPP (Hagen et al., 2006). The temporal resolution of processbased simulators may vary from half-hourly to monthly. It is therefore necessary to quantify uncertainty associated with the partitioned GPP at half-hourly to monthly time scales. For example, the partitioned GPP and associated uncertainty at a daily time scale can provide data for the calibration of process-based simulators such as BIOME-BGC.

In this study, we adopted the NRH model to partition half-hourly GPP from NEE data. In the past, numerical optimization has been used to estimate a single optimized value of each model parameters (Gilmanov et al., 2003, 2013). This did not quantify the uncertainty in half-hourly partitioned GPP. The measurements of half-hourly NEE are uncertain. Therefore, the optimized parameters are also uncertain (Richardson and Hollinger, 2005). Obtaining the underlying probability distribution of the NRH parameters gives a measure of uncertainty in parameters, which can be further propagated towards the NRH model to

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estimate uncertainty in partitioned GPP. A Bayesian implementation provides a solution to quantify the uncertainty in model parameters in the form of probability distributions (Gelman et al., 2013). The Bayesian approach was used in other studies to constrain the parameters of process-based simulators by using either eddy covariance data, biometric data, or both (Du et al., 2015; Minet et al., 2015; Ricciuto et al., 2008). We applied the Bayesian approach to a different type of model. We fitted the non-linear empirical NRH model to NEE data and quantified the uncertainty in NRH parameters to partition GPP with uncertainty.

The objective of this study was to implement a Bayesian approach for quantification of the uncertainty in half-hourly partitioned GPP using the NRH model given the availability of half-hourly NEE and other meteorological data. The time series of empirical distributions

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of half-hourly NEE and other meteorological data. The time series of empirical distributions of half-hourly GPP values also allowed us to estimate the uncertainty in GPP at daily time steps. Data were available from a flux tower in the central Netherlands at the Speulderbos forest. This will provide relevant and important information for the validation of process-based simulators.

15 2 Methods

2.1 Study area and data

The Speulderbos forest is located at 52°15′08″ N, 5°41′25″ E within a large forested area in the Netherlands. There is a flux tower within a dense 2.5 ha Douglas fir stand. The stand was planted in 1962. The vegetation, soil, and climate of this site have been thoroughly
described elsewhere (Steingrover and Jans, 1994; Su et al., 2009; van Wijk et al., 2001).

The CSAT3, Campbell Sci, LI7500 LiCor Inc, and CR5000 instruments were installed in June 2006 and have been maintained, and the data processed (software AltEddy, Alterra) by C. van der Tol (University of Twente, co-author) and A. Frumau (Energy Centre Netherlands). We examined half-hourly NEE data (measured at the flux tower) for the growing season (April to October) of 2009. The quality of the NEE data were assessed using the Foken classification system, which provides a flag to each half-hourly NEE datum from 1

through 9 (Foken et al., 2005). Each flag is associated with: (a) the range of the steady state condition of the covariance of vertical wind speed and CO_2 concentration of half-hour duration, (b) the range of the integral turbulence characteristic parameter indicating the developed turbulence; and (c) the range of the orientation of the sonic anemometer to make sure that the probe is omnidirectional at the time of measurements. We followed the suggestion of Foken et al. (2005) and accepted only those NEE data that were labelled from 1 to 3. For the growing season, we acquired half-hourly PPFD from the sensor PARlite (Kipp & Zonen. Delft, the Netherlands) and half-hourly T_a from the weather sensor WXT510 (Vaisala, Finland) installed at the flux tower.

10 2.2 The non-rectangular hyperbola (NRH) model

NEE is given as:

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$$\mathsf{NEE} = P_{\mathsf{a}} - R_{\mathsf{eco}}$$

where NEE is measured by the eddy covariance technique and P_a is gross CO_2 assimilation. The exchange of carbon into the system through photosynthesis is considered a pos-

¹⁵ itive flux because it represents production and the loss of carbon through respiration is considered a negative flux.

The light response curve is represented using the NRH model (Gilmanov et al., 2003; Rabinowitch , 1951):

$$P_{\mathsf{a}} = \frac{1}{2\theta} \times \left(\alpha \cdot \mathsf{PPFD} + A_{\mathsf{max}} - \sqrt{(\alpha \cdot \mathsf{PPFD} + A_{\mathsf{max}})^2 - 4\alpha \cdot A_{\mathsf{max}} \cdot \theta \cdot \mathsf{PPFD}} \right)$$
(2)

where α is the apparent quantum yield, A_{max} is the photosynthetic capacity at light saturation, and θ is the degree of curvature of the light response curve.

Gilmanov et al. (2013) modelled ecosystem respiration R_{eco} using the temperature dependent term according to Van't-Hoff's equation in its exponential form (Thornley and Johnson, 2000):

²⁵
$$R_{eco} = r_0 \times \exp(k_T T_a)$$

(3)

(1)

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(4)

where T_a is the air temperature and r_0 and k_T are the temperature sensitivity coefficients. Eqs. 2 and 3 are substituted in Eq. (1) to obtain the model for net ecosystem exchange NEE:

$$\begin{split} \mathsf{NEE} &= \frac{1}{2\theta} \times \left(\alpha \cdot \mathsf{PPFD} + A_{\mathsf{max}} - \sqrt{(\alpha \cdot \mathsf{PPFD} + A_{\mathsf{max}})^2 - 4\alpha \cdot A_{\mathsf{max}} \cdot \theta \cdot \mathsf{PPFD}} \right) \\ &- r_0 \times \exp(k_{\mathsf{T}} T_{\mathsf{a}}). \end{split}$$

Both daytime and nighttime half-hourly NEE, PPFD, and T_a data were used to estimate the NRH model parameters $\beta = (\theta, \alpha, A_{max}, r_0, k_T)$ (Eq. 4). For nighttime data, Eq. (4) includes only the respiration term because PPFD is equal to zero during the night. These estimated parameters, together with half-hourly PPFD, were used in Eq. (2) to calculate half-hourly P_a . Values of half-hourly GPP were calculated by multiplying P_a by 12/44 (12 10 is the atomic mass of carbon, and 44 is the atomic mass of CO₂) in order to convert the mass of CO₂ into the mass of carbon (C). This gives GPP in mg C m⁻² s⁻¹, whereas the unit of P_a is the same as the unit of measured NEE in mg CO₂m⁻²s⁻¹. The unit of each parameter and other variables used in the above equations are shown in Table 1. Gilmanov et al. (2013) proposed to incorporate the effect of VPD by multiplying Eq. (2) by the VPD-15 response function, ϕ , that accounts for the VPD limitation on P_a . The function ϕ is set equal to 1 if VPD is below some critical value (VPD_{cr}) that indicates that water stress does not affect photosynthesis. Above the critical value (VPD > VPD_{cr}), ϕ decreases exponentially with the curvature parameter σ_{VPD} , which may vary between 1 and 30 kPa. Low values of σ_{VPD} indicate a strong water stress effect, whereas higher values indicate a weak water 20 stress effect. We calculated half-hourly VPD from relative humidity (RH) using the procedure provided in Monteith and Unsworth (1990). We found that 90 % of the total half-hourly VPD values in the growing season of 2009 were less than 1 kPa and 9% were between 1 kPa and 1.5 kPa. We therefore neglected the influence of VPD as a limiting factor for the water stress at Speulderbos. This follows Körner (1995) and Lasslop et al. (2010) who specified 25

 $VPD_{cr} = 1$. We, therefore, assumed ϕ equal to 1.

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2.3 Theory of Bayesian inference for the model parameters

Bayesian inference treats all parameters as random variables (Gelman et al., 2013). Bayes rule is given as

$$p(\boldsymbol{\beta}|\mathbf{y}) = \frac{p(\mathbf{y}|\boldsymbol{\beta})p(\boldsymbol{\beta})}{p(\mathbf{y})} \propto \text{likelihood} \times \text{prior}$$
(5)

- ⁵ where $p(\beta)$ is the prior distribution, representing the prior understanding of uncertainty in the model parameters values before the observations are taken into account. This understanding may come from expert judgement or previously published research on the parameters (Oakley and O'Hagan, 2007; Raj et al., 2014). If no prior knowledge is available, non-informative priors may be used (i.e., a wide prior distribution that conveys no prior information). The term $p(\beta|\mathbf{y})$ is the posterior distribution of β after combining prior knowledge and data \mathbf{y} and represents the uncertainty in β given the data and the prior. The marginal
- effect of each parameter $p(\beta_i | \mathbf{y}), i = 1, 2, ..., n$, is the main quantity of interest, expressing the uncertainty in each parameter separately. The term $p(\mathbf{y}|\beta)$ is the conditional probability of observing data \mathbf{y} given β and is also called the likelihood. The term $p(\mathbf{y})$ is the probability
- ¹⁵ of observing the data **y** before observations were taken. This acts as the normalising constant that ensures that $p(\beta|\mathbf{y})$ is a valid probability distribution that integrates to 1. For most real-world problems it is not possible to write down analytical solutions for Eq. (5) and it is usual to perform inference using Markov Chain Monte Carlo (MCMC) simulation (Gelman et al., 2013).
- ²⁰ MCMC is a method for conducting inference on $p(\beta|\mathbf{y})$. It requires evaluation of the joint distribution $p(\mathbf{y}|\beta)p(\beta)$, which represents the dependence structure in the data. MCMC constructs Markov chains of the parameters space and generates samples $\beta^{(1)}$, $\beta^{(2)}, \ldots, \beta^{(m)}$ of β whose unique stationary distribution is the posterior distribution of interest $p(\beta|\mathbf{y})$. The *m* samples are then used to conduct inference on each β_i . For example the mean, median and 95% credible interval can all be calculated over these *m* samples. It is usual to construct multiple Markov chains and to assess whether they converge to the same

(6)

stationary distribution. The reader referred to chapter 4 in Lunn et al. (2013) and chapter 11 in Gelman et al. (2013) for further explanation.

2.4 Implementation of Bayesian inference for the NRH model parameters

We treated Eq. (4) as a non-linear regression problem:

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$$y_i = \frac{1}{2\theta} \times \left(\alpha \cdot \mathsf{PPFD}_i + A_{\max} - \sqrt{(\alpha \cdot \mathsf{PPFD}_i + A_{\max})^2 - 4\alpha \cdot A_{\max} \cdot \theta \cdot \mathsf{PPFD}_i} \right)$$

- $r_0 \times \exp(k_T T_{a_i}) + \varepsilon_i$
= $\mu_i - \nu_i + \varepsilon_i$

where y is the response variable (NEE), PPFD and T_a are the predictor variables and ε is the residual error. The residual error arose because the model did not perfectly fit the data. The subscript *i* indicates a single observation. For brevity we use μ_i to refer to the first term on the RHS and ν_i to refer to the second term on the right hand side of Eq. 6.

As is usual in regression modelling, we assumed normally distributed errors, hence $\varepsilon_i \sim N(0, \sigma^2)$ and the likelihood also followed a normal distribution, such that $y_i \sim N(\mu_i - \nu_i, \sigma^2)$. In the above notation, $\beta = (\alpha, A_{\max}, \theta, r_0, k_T)^T$ and the likelihood is $p(\mathbf{y}|\beta, \sigma^2)$, where $\mathbf{y} = (y_1, y_2, \dots, y_n)^T$ for *n* observations.

In Bayesian analysis it is usual to refer to precision, which is the inverse of the variance, hence $\tau_e = 1/\sigma^2$. Further, the assumption of prior distributions for each β_i together with τ_e is required. No prior information was available for τ_e so a non-informative prior was selected. We assumed a Gamma distribution for τ_e with shape and rate parameters equal to 0.001. This ensures a non-negative non-informative prior for τ_e (Lunn et al., 2013).

We made two choices for the prior distribution for each β_i . First, a non-informative prior was used (Sect. 2.4.1). Second, prior information for each β_i was obtained from the literature, being called an informative prior distribution (Sect. 2.4.2). Note that the same non-informative prior for τ_e was used in both choices. The results for informative an noninformative priors were compared.

2.4.1 Non-informative prior distributions

We assumed a normal distribution for each β_i with mean equal to 0 and standard deviation equal to 32, which gives small value of the the precision equal to 0.001 to make the distribution wide. NRH is a non-linear model and therefore appropriate constraints should be imposed to ensure the meaningful values of the prior parameter distribution (Lunn et al., 2013). Each β_i parameter must be positive (Sect. 2.4.2) so we truncated the normal distribution on each β_i except θ to ensure only positive values. For θ , we truncated the normal distribution to occur between 0 and 1 by setting the obvious limit to this parameter (see also item 2 in Sect. 2.4.2). The above choices ensure wide non-informative prior distributions whilst specifically excluding physically unrealistic values.

2.4.2 Informative prior distributions

Below we justify choices for the informative prior distributions on β .

- 1. The quantum yield, α , represents the amount of absorbed CO₂ per quanta of absorbed light. Cannell and Thornley (1998) reported that α varies little among C₃ species and has a value from 0.09 to 0.11 and from 0.04 to 0.075 mol CO₂ (mol quanta)⁻¹ in saturated and ambient CO₂ conditions respectively. The typical value of α equals 0.05 mol CO₂ (mol quanta)⁻¹ for a C₃ species in an ambient atmosphere (Skillman, 2008; Long et al., 2006; Bonan et al., 2002). Douglas fir at Speulderbos is a C₃ species. We used this information to construct the prior distribution on α , as follows:
 - A value of α around 0.05 has the highest probability. The probability decreases as the value of α decreases or increases from 0.05 and cannot be negative. The maximum value that α can attain is 0.11.
 - We assumed a normal distribution of α with mean, $\mu_{\alpha} = 0.05$, and variance, $\sigma_{\alpha}^2 = (0.015)^2$ (i.e, standard deviation, $\sigma_{\alpha} = 0.015$). The choice of mean ensures that the highest probability is assigned to the values around 0.05. The choice of variance ensures that 99.7% ($\mu \pm 3\sigma_{\alpha}$) of α is positive and lies in

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the interval between 0 and 0.11. We also truncated 0.3% of negative α values from the assumed normal distribution. In the unit of mg CO₂ (µmol quanta)⁻¹, the assumed normal distribution ($N(\mu_{\alpha} = 0.05, \sigma_{\alpha} = 0.015)$) is expressed as N(0.0022, 0.00066) (Fig. 1a).

- 2. The curvature parameter θ can take values from 0, which reduces Eq. (4) to the sim-5 pler rectangular hyperbola, to 1, which describes the Blackman response of two intersecting lines (Blackman, 1905). The physiological range for θ has been observed to be between 0.5 and 0.99 (Ogren, 1993; Cannell and Thornley, 1998). A value of $\theta = 0.9$ was recommended by Thornley (2002) and at $\theta = 0.8$ by Johnson et al. (2010) and Johnson (2013). The estimate of θ , as a result of fitting the NRH model to ei-10 ther measured photosynthesis or NEE data was found to be in the range of 0.7 to 0.99 (Gilmanov et al., 2010, 2003). These findings for θ indicated that a higher probability should be assigned to the values around 0.8 and the probability should approach to zero below 0.5. This means that the distribution of θ can be assumed to be negatively skewed with $Pr(\theta < 0.5)$ approaching zero and $Pr(\theta \approx 0.8)$ at a maximum. These 15 conditions were modelled using a beta distribution with shape parameters at 10 and 3 for θ (Fig. 1b).
 - 3. The photosynthetic capacity at light saturation A_{max} is reached when the photosynthesis is Rubisco limited and varies among different tree species (Cannell and Thornley, 1998). At the canopy level, A_{max} also depends upon the structure of the canopy (i.e., arrangement of the canopy leaves) and the area of leaves available to absorb photons. Both are determined by the leaf area index (LAI) (Ruimy et al., 1995). We compiled the prior information on A_{max} for Douglas fir species from the literature. Values of A_{max} were mainly reported for needles, whereas the NRH model (Eq. 4) requires A_{max} values for the canopy. Scaling A_{max} from needle to the canopy equivalent is not a trivial task because this depends on the light distribution and the vertical profile of A_{max} in the canopy. Here we analysed plateau values of photosynthesis at needle and canopy level with simulations by a model that takes this into account: the

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model SCOPE (van der Tol et al., 2009). These simulations (not shown) indicated that the relation between the two plateaus (canopy:needle A_{max}) increased with LAI but saturated at a value of 2.8. The mean value of LAI at the Speulderbos site is high (approximately 9 van Wijk et al., 2000; Steingrover and Jans, 1994) and therefore we could translate the reported range of A_{max} values for the Speulderbos (Mohren, 1987) of 0.26 to 0.52 mg CO_2 m⁻² s⁻¹ into values of 0.73–1.46 mg CO_2 m⁻² s⁻¹ for canopy A_{max} . van Wijk et al. (2002) reported slightly higher canopy A_{max} values of 1.86 and 1.06 mg CO₂ m⁻² s⁻¹ at the Speulderbos site. The highest and lowest value for needle A_{max} for Douglas fir (irrespective of the site) we found in the literature were 0.097 (canopy $A_{max} = 0.27$) and 1.01 mg CO₂ m⁻² s⁻¹ (canopy $A_{max} = 2.8$) respectively (Ripullone et al., 2003; Warren et al., 2003; Lewis et al., 2000). To cover this rather wide range of values, a Gamma distribution with shape and rate parameters equal to 4 and 2.5 respectively was selected to ensure higher probabilities are assigned to the values between 1 and 2.5 with decreasing probabilities down to 0 and up to 4.5 (Fig. 1c). The A_{max} values at Speulderbos are well placed in the overall distribution.

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4. The parameters for temperature sensitivity $k_{\rm T}$ and Q_{10} are related as $Q_{10} = \exp(10k_{\rm T})$ (Davidson et al., 2006). Q_{10} is the factor by which respiration (Eq. 3) is multiplied when temperature increases by 10 °C. (Mahecha et al., 2010) carried out experiments across 60 FLUXNET sites to check the sensitivity of ecosystem respiration to air temperature. They suggested that Q_{10} does not differ among biomes and is confined to values around 1.4 ± 0.1 (corresponding to $k_{\rm T}$ around 0.034 ± 0.008). Hence $k_{\rm T} \approx 0.034$ should have the highest probability of occurrence. Q_{10} data reported in the supporting material of Mahecha et al. (2010) showed that that Q_{10} becomes less frequent as it increases or decreases from 1.4 and attains a highest value of ~ 2.72 (corresponding to $k_{\rm T} = 0.1$). To model these conditions a Gamma prior distribution was chosen with shape and rate parameters equal to 4 and 120 respectively (Fig. 1d).

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(7)

- 5. The r_0 parameter represents the ecosystem respiration at 0 °C. We adopted the following steps to define the prior distribution for r_0 .
 - Mahecha et al. (2010) presented a graph of seasonal variation of ecosystem respiration at 15 °C (R_b) for 60 FLUXNET sites. We extracted the values of R_b (in g CO₂ m⁻² day⁻¹) from the graph for those sites that belong to evergreen needle leaf forest (ENF). We obtained the values of r₀ from R_b using the following equations:

$$r_0 = \frac{R_b}{\exp(k_{\rm T} \times 15)}$$

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where $k_{\rm T}$ was obtained from Q_{10} as reported in point 4 above. Site specific Q_{10} value is used here. The unit of r_0 is converted into mg CO₂ m⁻² s⁻¹.

- We identified values of r_0 for ENF in the range 0.013 to 0.07 mg CO₂ m⁻² s⁻¹. We also identified values of r_0 in the range 0.019 to 0.043 at the Loobos FLUXNET site in the Netherlands (Mahecha et al., 2010), which is close to Speulderbos. Therefore, we assumed that the most frequent values of r_0 at Speulderbos are in this range. To model these conditions we chose a Beta distribution with shape parameters at 2 and 64 (Fig. 1e).

2.4.3 Bayesian inference of β

We used WinBUGS software version 1.4.3 (Lunn et al., 2000) to implement the Bayesian full probability models (Eq. 5) for the inference of β . WinBUGS is a windows implementation of the original BUGS (Bayesian Inference Using Gibbs Sampling) software. This was a joint initiative between the MRC Biostatistics Unit, Cambridge and the Imperial College School of Medicine, London (Lunn et al., 2013). WinBUGS implements MCMC for Bayesian inference. The major inputs of WinBUGS are: (a) the model file specifying the definition of the prior distribution of each β_i and likelihood function, (b) the number of Markov chains to create, (c) the number of iterations for MCMC to carry out for each Markov chain, (d) the burn-in

period for which the MCMC runs are discarded, (e) initial values of each β_i for each Markov chain. The burn-in period is the number of samples after which the Markov chains converge to a stationary distribution. The post burn-in samples are used to perform inference on the β_i s.

- ⁵ We obtained the posterior distribution of each β_i for every 10-day block (total 22 blocks) in the growing season of 2009. More precisely, we obtained varying parameters and did not assume values to be constant for the whole study period. This approach is recommended by Aubinet et al. (2012), since obtaining varying parameters incorporates indirectly the temporal changes in the factors such as canopy structure, soil moisture and ecosystem
- nutrient levels that affect GPP. NRH model does not include these factors directly. Hence, although these factors are not included in the NRH model our implementation does account for them. The 10-day block was chosen because it was sufficiently long to ensure a suitably large NEE dataset *within* the 10-day block but was short enough that we could account for temporal changes *between* the 10-day blocks. Thus the temporal change is observed between consecutive blocks, not within a block. The sample size within a 10-day block was
- limited because \sim 30% of the data were typically discarded as being of low quality (Foken flag 4 or higher, see Sect. 2.1).

We identified the appropriate length of the burn-in for both informative and noninformative prior distributions. We calculated the Gelman–Rubin potential scale reduction

- factor (PSRF) to evaluate the convergence of Markov chains for each β_i for the post burn-in period. Graphically, we assessed the convergence of Markov chains by plotting them together for each β_i . This plot is known as trace plot. A visual observation of a proper mixing of these chains indicates the convergence of Markov chains to the stationary distribution. An explanation of PSRF and the identification of the length of the burn-in are given in the
- ²⁵ Supplement. We refer the reader to pages 71–76 in Lunn et al. (2013) and pages 281– 285 in Gelman et al. (2013) for further explanation. Based on that analysis we used three Markov chains with 16 000 and 25 000 iterations for each chain for informative and noninformative prior distributions respectively. We stored the posterior samples of each β_i and

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 $\tau_{\rm e}$ for the remaining 30 000 samples (i.e., 10 000 post burn-in samples for each of three Markov chains). The BUGS code (model file for WinBUGS) is given in the Supplement.

2.5 Posterior prediction

To perform prediction for a given PPFD₀ and T_{a_0} , m post burn-in samples of β and σ^2 were used as follows:

$$\mu_{0}^{(l)} = \frac{1}{2\theta^{(l)}} \times \left(\alpha^{(l)} \cdot \mathsf{PPFD}_{0} + A_{\max}^{(l)} - \sqrt{(\alpha^{(l)} \cdot \mathsf{PPFD}_{0} + A_{\max}^{(l)})^{2} - 4\alpha^{(l)} \cdot A_{\max}^{(l)} \cdot \theta^{(l)} \cdot \mathsf{PPFD}_{0}} \right)$$

$$\nu_{0}^{(l)} = r_{0}^{(l)} \times \exp\left(k_{\mathsf{T}}^{(l)} T_{\mathsf{a}_{0}}\right)$$

$$y_{0}^{(l)} \sim N(\mu_{0}^{(l)} - \nu_{0}^{(l)}, \sigma^{2(l)})$$
(8)

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- where (l) is not an exponent, but indicates a specific sample. Other terms are as defined for Eq. (6). The m samples were used to build up the posterior predictive distribution. In this way posterior predictions of GPP (μ_0) and NEE (y_0) were obtained. Note that the uncertainty in the posterior predictions of GPP arose due to uncertainty in the posterior estimates of β . Uncertainty in the posterior prediction of NEE also considered the uncertainty arising due to the residual error.
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Prediction was performed for each 10-day sample for m = 30000 samples (3 chains and 10000 samples per chain). These were then summarized (median and 95% credible interval) to obtain the posterior predictive inference for NEE and GPP for each 10-day block. These 95% credible intervals show the uncertainty. Hence the actual values of NEE and GPP are likely to be in this interval, but not necessarily at the median. We reported the number of half-hourly NEE measurements that lie inside and outside of 95% credible inter-

20 vals of the corresponding half-hourly modelled NEE distributions. In this way, we checked whether realistic credible intervals were obtained. Validation against a separate or hold-out dataset was in principle possible, but was not necessary in this study, because we did not use the NRH model to predict at blocks outside the range of the data. Moreover, we did not use the posterior β values outside the blocks where they were fitted. 25

3 Results and discussion

3.1 Performance of MCMC

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We examined the trace plots of the three Markov chains for each β_i and τ_e obtained for each 10-day block for both choices of informative and non-informative prior distributions. Trace plots for one 10-day block (1 May to 10 May 2009) are shown in Fig. S3 in the Supplement. We observed a proper mixing of the three Markov chains, indicating the convergence of three Markov chains to a stationary distribution that could be used for inference. The Gelman–Rubin PSRF was close to 1 (Table S1 in the Supplement) for each β_i and τ_e , providing further support for the convergence of the Markov chains. The post burn-in samples were used for inference for each 10-day block in the growing season of 2009.

Figure 2 shows the posterior prediction of half-hourly NEE for a 10-day block (1 May to 10 May 2009) for the choice of informative and non-informative prior distributions. The half-hourly NEE was summarized by the median and the 2.5 and 97.5% iles (i.e., 95% credible intervals). Out of 338 available half-hourly NEE measurements in this 10-day block, 6%

- ¹⁵ laid outside the 95% credible intervals for both choices of prior distribution. This showed that the coverage of the 95% credible interval was appropriate. There was no substantial difference in the shape of the percentiles curve between the choices of prior distribution. This indicated that the choice of informative or non-informative priors did not influence the posterior prediction of NEE. Similar results were observed for other 10-day blocks. Over
- the entire 2009 growing season 94 % of the 7126 available half-hourly NEE measurements were bracketed by the 95 % credible intervals for posterior predicted NEE. The choice of informative or non-informative priors did not lead to any substantial difference in the posterior predicted median or 95 % credible intervals.

The 10-day block shown in Fig. 2 shows that the posterior predicted median of NEE was positive during the day and negative during the night. This is to be expected owing to the lack of photosynthesis at night. However, at night the 95% credible interval spanned zero implying that, when prediction uncertainty is considered, the actual predicted NEE *might* be positive. This is not possible physically, but is an artefact of the statistical approach. Since this is a non-linear regression-type problem the uncertainty in the prediction arises due to both the uncertainty in the estimated regression parameters, β and the residual uncertainty. This residual uncertainty was assumed to follow a normal distribution with zero mean and precision, τ_e , and reflects the scatter of the observations round the posterior median prediction. Following our discussion above, this correctly represents the uncertainty in prediction. A consequence of this was that that the prediction intervals were wide and the predictions were potentially positive during the night. This could potentially be addressed by introducing further constraints into the model to allow τ_e to vary temporally (e.g., Hamm et al., 2012). We leave that as a topic for future research whilst noting that our dataset is not very large and we have already fitted a complicated model.

3.2 Uncertainty in partitioned GPP at half-hourly and daily time step

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Figure 3 shows the histograms of the posterior distribution of half-hourly and daily-summed GPP for Julian days 121 (1 May) and 196 (15 July) for the choice of both informative and non-informative prior distributions. These allow visualization of the uncertainty within a day and between days for late spring and mid-summer. Clearly the predictions resulting from in-15 formative and non-informative priors were similar. For both days higher values of GPP were observed in the afternoon compared to the morning on both Julian days. This reflected the increase in GPP predictions with increasing PPFD from morning to afternoon. The assimilation of carbon was also expected to increase from the start of the growing season to the peak (summer time) of the growing season. It was clear that higher values in GPP were predicted on Julian day 196 compared to Julian day 121 for both morning and after-

- noon. Seasonal variation in daily GPP was also observed in the daily sum of GPP, which increased from 7–9 g C m⁻² d⁻¹ on Julian day 121 to 10.5-12.5 g C m⁻² d⁻¹ on Julian day 196. Variation in daily GPP during the 2009 growing season for the choice of informative
- priors is shown in Fig 4. The same plot for the choice of non-informative priors is shown in 25 Fig. S4.

We tested whether within the posterior half-hourly GPP distributions, the non-rectangular hyperbolic relationship of GPP with PPFD had been preserved. Figure 5 shows, for an Discussion Paper

example 10-day block (Julian days 121–130), posterior GPP versus PPDF. The resulting curve shows that the non-rectangular hyperbolic relationship was indeed preserved, and GPP values initially rose and reached a plateau with increasing PPFD. This is important since our daily GPP estimates were obtained by summing half-hourly values. Since the range of PPDF values during the day is large and the relationship between PPFD and GPP

⁵ range of PPDF values during the day is large and the relationship between PPFD and GPP non-linear, a realistic representation of the light response curve of GPP is important.

We concluded that the posterior predictions of half-hourly and daily GPP were reliable. We used the posterior distribution of the NRH parameters to predict half-hourly NEE and the 95% credible intervals bracketed 94% of the available half-hourly NEE measurements

(Sect. 3.1 and Fig. 2). This indicated that our posterior predictions accurately captured the uncertainty in the measured NEE values. We used the same posterior distributions of the NRH parameters to estimate uncertainty in half-hourly GPP. Therefore, we expect that the underlying uncertainty in half-hourly GPP was also accurate.

3.3 Posterior distributions of β

Figure 6 and 7 show the temporal profile (mean and 95% credible interval) for β for each 10-day block for informative and non-informative prior β distributions respectively.

A clear seasonal pattern in the posterior distribution of α and A_{max} was observed. When using non-informative priors, spikes in the 97.5% iles for A_{max} were observed at 41, 47, and 59 mg CO₂ m⁻² s⁻¹ (Fig. 7e) for three 10-day blocks (Julian days 91–100, 281–290, and 291–300). These values are physically unrealistic (see Sect. 2.4.2). When using informative priors, the same three 10-day blocks also showed spikes in the 97.5% iles for A_{max} (Fig. 6e); however these spikes were much smaller and were physically realistic. For other 10-day blocks, both choices of prior yielded comparable posterior distributions of A_{max} (Figs. 6e and 7f) with uncertainty less than that of the informative and non-informative prior distributions (Fig. 1c and Sect. 2.4.1). The posterior distributions of α , r_0 , and k_T were similar for both choices of prior distribution. The choice of non-informative prior yielded wider credible intervals for θ compared to the choice of informative priors (Figs. 6b and 7b). We calculated the sum of daily GPP for each of the above mentioned 10-day blocks (91– 100, 281–290, and 291–300) for both choices of prior (Fig. S5). We found no significant difference in the range of GPP for each block. For example, the range of daily-summed values for 10-day block 281–290 was 26–38 g C m⁻² d⁻¹ for both choices of prior. This indicated that the unrealistic spikes in the posterior distributions of A_{max} did not affect the prediction of GPP. This led us to evaluate the sensitivity of GPP to A_{max} . We fixed the value of the NRH parameters α , θ , r_0 , and k_T at their mean. We varied A_{max} from 0 to 100 mg CO₂ m⁻² s⁻¹ at an interval of 0.5. We estimated the value of GPP at each interval using Eq. 2. A_{max} was varied from 0 to 100 mg CO₂ m⁻² s⁻¹ so that it could cover the spikes in the posterior distributions of A_{max} (Fig. 7e).

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The plot of A_{max} against GPP (Fig. 8) revealed that GPP varied strongly up to $A_{\text{max}} = 5 \text{ mg CO}_2 \text{ m}^{-2} \text{ s}^{-1}$. After this value GPP saturated. The underlying reason is the fact that in light limited conditions, i.e., $A_{\text{max}} \gg \alpha \times \text{PPFD}$, Eq. (2) reduces to $P_a = \alpha \times \text{PPFD}$ and hence P_a and thus GPP becomes independent of A_{max} . This explains why the GPP posterior predictions were not affected by the unrealistic values of A_{max} occurring in periods of low light intensities. The choice of prior distribution therefore played a minimal role in the prediction of GPP. The use of informative priors, however, constrained the estimation of the posterior distributions of the parameters.

20 3.4 Some issues and limitations of this study in estimating uncertainty using the NRH model

The Bayesian approach applied to the NRH model is a solid method to quantify the model parameters and their uncertainty. The 10-day block although suited for the purpose of this study, is insufficient to incorporate the effects of more rapid changes (day to day) in soil moisture and nutrient levels in the NRH model. In principle, these rapid changes could be incorporated by daily estimation of the NRH parameters (Aubinet et al., 2012; Gilmanov et al., 2013), although this could not be achieved in this study due to the lack of continuous high quality, half-hourly NEE data. The temporal variation in soil moisture and nutrient level

for the study site should be investigated further. This may help to select an optimum block size where the within-block variation is limited. The availability of continuous high quality NEE data, however, may impose further constraints on the selection of an optimum block size.

The residual term ε_i in Eq (6) contains the model representation error and the ran-5 dom measurement error. We were unable to separate ε_i into these two components. It is possible to calculate the random measurement error using the paired-measurement approach (Richardson et al., 2006b). Richardson et al. (2008) compared the random measurement error in NEE to ε_i , and concluded that ε_i is mainly due to the random measurement error. We assumed the same to hold for our study, although we could not evaluate this 10 using the paired-measurement approach. Model representation errors included, for example, the fact that we have not parameterized respiration separately for day and night, or separately for vegetation and soil. Vegetation respiration depends also upon other factors, such as irradiance (Sun et al., 2015), photorespiration (because it is nearly proportional to GPP) and produced CO₂ that remains in the trees (Teskey et al., 2008). It is not feasible 15 to model all these processes separately. Thus our model can be expected to contain some representation errors.

Systematic errors also result in uncertainty in NEE measurements (Moncrieff et al., 1996; Aubinet et al., 2012). We have applied the Foken classification system (Sect. 2.1) to filter
out the low quality NEE measurements that contain high systematic errors. This reduced the effect of systematic errors on the posterior prediction of NRH parameters and on the model residuals. A source of systematic error that we could not account for was storage of CO₂ below the measurement height during stable conditions at night (Goulden et al., 1996). The turbulent mixing after sunrise may cause hysteresis in the light response curve between morning and late afternoon hours. This hysteresis will contribute to the scatter in the model fit, and thus to the uncertainty in the estimated parameters.

The implementation of the NRH model assumed that PPFD and T_a were known without error and all uncertainty was attributed to the response variable (NEE). This assumption is usual in statistical regression modelling, but is unlikely to be correct in this case. There

is scope to incorporate information about uncertainty in PPFD and T_a , although this would lead to a more complicated model. Future research could examine whether relaxing this assumption would improve the model.

- We focused in the growing season in 2009. This short period was chosen to illustrate the implementation of the Bayesian approach to quantify the uncertainty in half-hourly partitioned GPP using the NRH model. The study could be extended towards multiple years, allowing a multi-year comparison although that was outside the scope of our methodological focus. Further, different models have been investigated previously to partition GPP (Desai et al., 2008; Richardson et al., 2006a). Any model is a source of uncertainty in itself because it cannot account for every process. The scope of this study can therefore be further wideped by addressing multiple actablished ways of partitioning CBP and thus applying
 - widened by addressing multiple established ways of partitioning GPP and thus analysing uncertainty associated with these.

Beer et al. (2010) partitioned GPP from NEE both using the rectangular hyperbola (RH) light-response curve (Lasslop et al., 2010) and a conventional night-time data based approach (Reichstein et al., 2005) for many FLUXNET sites, and further used the partitioned GPP to calibrate five highly diverse diagnostic models for GPP to produce the distribution of global GPP. Although the present study focused on better understanding the uncertainty in partitioning GPP using NRH light-response curve, future research can build on our findings and extend our approach to other sites and years.

20 4 Conclusions

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The study concluded that the choice of informative and non-informative prior distributions of the NRH model parameters led to similar posterior distributions for both GPP and NEE. Obtaining informative priors is time consuming because the values of each parameter are not explicitly mentioned in the literature. Informative priors also require the acquisition of information on species or site specific values of photosynthetic capacity at light saturation (A_{max}) and ecosystem respiration at reference temperature (r_0) parameter. As an alternative, noninformative priors can be obtained with proper constraints using minimum information on the NRH parameters such as the positivity of A_{max} . Therefore, non-informative priors can

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be used for any species type irrespective of study sites. These findings are valuable to conduct uncertainty analysis across a larger sample of sites with different GPP characteristics, e.g., by obtaining NEE and other meteorological data from the FLUXNET data base. The downside of non-informative prior is the production of spikes in the posterior of A_{max} for some days in this study. Therefore, if such values are of interest in a particular study (e.g., photosynthesis nitrogen use efficiency that relies on the ratio of A_{max} and leaf nitrogen) then informative prior should be used.

The estimates of the NRH model parameters were obtained for 10-day blocks. The values of the posterior parameters and their variation over time could provide further understanding of how the forest responds to factors not included in the model, such as soil moisture, nutrition or tree age.

Quantifying uncertainty estimates as empirical distributions in half-hourly gross primary production (GPP) was implemented in the Bayesian framework using the non-rectangular hyperbola (NRH) model. These uncertainty estimates were provided at daily time steps.

- The approach could be extended to include the uncertainty in meteorological forcing, in particular photosynthetic photon flux density and air temperature. The distributions in half-hourly GPP can be further used to obtain distributions at any desired time steps, such as 8-day and monthly. The uncertainty in GPP estimated in this study can be used further to quantify the propagated uncertainty in the validation of satellite GPP products such as
- ²⁰ MODIS 17 or process-based simulators such as BIOME-BGC. Although we focussed on quantifying the uncertainty in GPP partitioning, our approach could also be used to either estimate R_{eco} or fill missing NEE data and this will be achieved in a future study.

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Table 1. List of symbols with unit.

NEE, y	net ecosystem exchange	mg $\mathrm{CO}_2\mathrm{m}^{-2}\mathrm{s}^{-1}$
P_{a}	gross CO ₂ assimilation	mg CO $_2$ m $^{-2}$ s $^{-1}$
GPP	gross primary production	mg C m $^{-2}$ s $^{-1}$; g C m $^{-2}$ s $^{-1}$
R_{eco}	ecosystem respiration	mg CO $_2$ m $^{-2}$ s $^{-1}$
PPFD	photosynthetic photon flux density	μ mol quanta m $^{-2}$ s $^{-1}$
T_{a}	air temperature	°C
α	quantum yield	mg CO $_2$ (μ mol quanta) $^{-1}$
θ	degree of curvature of light response curve	unitless
$A_{\sf max}$	photosynthetic capacity at light saturation	mg CO ₂ m ^{-2} s ^{-1}
k_{T}	temperature sensitive parameter	(°C) ⁻¹
r_0	ecosystem respiration at reference temper-	mg $CO_2 m^{-2} s^{-1}$
	ature $T_a = 0 ^{\circ} C$	
$ au_{e}$	precision of the normal distribution of the	
	likelihood	
$oldsymbol{eta}$	$(\theta, \alpha, A_{\max}, r_0, k_{T})$	
R_b	ecosystem respiration at reference temper-	$g CO_2 m^{-2} s^{-1}$
	ature $T_a = 15 ^{\circ}\text{C}$	
Q_{10}	multiplication factor to respiration with 10 $^\circ$ C	
	increase in T_{a}	
RH	relative humidity	%
VPD	vapour pressure deficit	kPa
VPD _{cr}	critical value of vapour pressure deficit	kPa
ϕ	vapour pressure deficit response function	
σ_{VPD}	curvature parameter for ϕ	kPa



Figure 1. Informative prior distribution of the NRH model parameters: (a) $\alpha \sim N(\mu_{\alpha} = 0.0022, \sigma_{\alpha} = 0.00066)$, (b) $\theta \sim \text{Beta}(\text{shape1} = 10, \text{shape2} = 3)$, (c) $A_{\text{max}} \sim \text{Gamma}(\text{shape} = 4, \text{rate} = 2.5)$, (d) $k_{\text{T}} \sim \text{Gamma}(\text{shape} = 4, \text{rate} = 120)$, (e) $r_0 \sim \text{Beta}(\text{shape1} = 2, \text{shape2} = 64)$. Information about the NRH parameters is given in Table 1. The *y* axis represents the density of corresponding distribution.



Figure 2. Median (solid lines) and 95 % credible intervals (dashed lines) of the posterior distribution of NEE together with half-hourly NEE measurements (solid points) for a 10-day block (1 May to 10 May 2009, Julian days 121 to 130): **(a)** when using informative prior distributions, **(b)** when using non-informative prior distributions.



Figure 3. Histograms of half hourly GPP (Morning and afternoon) and daily sum of GPP when using: (a) informative priors on Julian day 121 (1 May 2009), (b) non-informative priors on Julian day 121, (c) informative priors on Julian day 196 (15 July 2009), (d) non-informative priors on Julian day 196. The morning and afternoon time belong to half-hour 8:00 CET to 8:30 CET and 13:00 CET to 13:30 CET respectively. The y axis is frequency; CET is Central European Time.



Figure 4. Median (solida line) and 95% credible intervals (dashed lines) of daily GPP distributions during the growing season of 2009 (1st April to 31st October 2009, Julian days 91 to 304) for the choice of informative prior distributions.



Figure 5. Median (solid line) and 95% credible intervals (dashed lines) of half-hourly gross primary production (GPP) with photosynthetic photon flux density (PPFD) for a 10-day block (1 May to 10 May 2009, Julian days 121 to 130) for the choice of informative prior distributions.



Figure 6. Median (solid lines) and 95% credible intervals (dashed lines) of the posterior distributions of the NRH parameters when using informative prior distributions for each 10-day block during the growing season in 2009. The x axis is the first Julian day of each 10-day block. The y axis represents NRH parameter. Information about the NRH parameters is given in Table 1.



Figure 7. As Fig. 6 when using non-informative prior distributions. To help visualization of A_{max} we have added a subfigure (f) with the spikes removed (i.e., without the blocks of Julian days 91–100, 281–290, and 291–300).



Figure 8. Variation of gross primary production (GPP) with the variation of photosynthetic capacity (A_{max}) from 0 to 100 mg CO₂ m⁻² s⁻¹. The values of quantum yield (α), degree of curvature (θ), ecosystem respiration at reference temperature (r_0), and temperature sensitive paramete (k_T) are fixed at 0.7, 0.0022, 0.1, 0.07 respectively. Air temperature (T_a) and photosynthetic photon flux density (PPFD) are fixed at 10 °C and 900 µmol quanta m⁻² s⁻¹.