

1 **Closing a gap in tropical forest biomass estimation: Accounting for crown**
2 **mass variation in pantropical allometries**

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10

11 **Abstract**

12 Accurately monitoring tropical forest carbon stocks is an outstanding challenge. Allometric
13 models that consider tree diameter, height and wood density as predictors are currently used
14 in most tropical forest carbon studies. In particular, a pantropical biomass model has been
15 widely used for approximately a decade, and its most recent version will certainly constitute
16 a reference in the coming years. However, this reference model shows a systematic bias for
17 the largest trees. Because large trees are key drivers of forest carbon stocks and dynamics,
18 understanding the origin and the consequences of this bias is of utmost concern. In this
19 study, we compiled a unique tree mass dataset on 673 trees destructively sampled in five
20 tropical countries (101 trees > 100 cm in diameter) and an original dataset of 130 forest plots
21 (1 ha) from central Africa to quantify the prediction error of biomass allometric models at
22 the individual and plot levels when explicitly accounting or not for crown mass variations.
23 We first showed that the proportion of crown to total tree aboveground biomass is highly
24 variable among trees, ranging from 3 to 88 %. This proportion was constant on average for
25 trees < 10 Mg (mean of 34 %) but, above this threshold, increased sharply with tree mass
26 and exceeded 50 % on average for trees \geq 45 Mg. This increase coincided with a progressive
27 deviation between the pantropical biomass model estimations and actual tree mass.
28 Accounting for a crown mass proxy in a newly developed model consistently removed the
29 bias observed for large trees (> 1 Mg) and reduced the range of plot-level error from -23–16
30 % to 0–10 %. The disproportionately higher allocation of large trees to crown mass may thus
31 explain the bias observed recently in the reference pantropical model. This bias leads to far-

1 from-negligible, but often overlooked, systematic errors at the plot level and may be easily
2 corrected by accounting for a crown mass proxy for the largest trees in a stand, thus
3 suggesting that the accuracy of forest carbon estimates can be significantly improved at a
4 minimal cost.

6 **1 Introduction**

7 Monitoring forest carbon variation in space and time is both a sociopolitical challenge for
8 climate change mitigation and a scientific challenge, especially in tropical forests, which play
9 a major role in the global carbon balance (Hansen et al., 2013; Harris et al., 2012; Saatchi et
10 al., 2011). Significant milestones have been reached in the last decade thanks to the
11 development of broad-scale remote sensing approaches (Baccini et al., 2012; Malhi et al.,
12 2006; Mitchard et al., 2013; Saatchi et al., 2011). However, local forest biomass estimations
13 commonly represent the foundation for the calibration and validation of remote sensing
14 models. As a consequence, uncertainties and errors in local biomass estimations may
15 propagate dramatically to broad-scale forest carbon stock assessment (Avitabile et al., 2011;
16 Pelletier et al., 2011; Réjou-Méchain et al., 2014). Aboveground biomass (*AGB*) is the major
17 pool of biomass in tropical forests (Eggleston et al., 2006). The *AGB* of a tree (or *TAGB*) is
18 generally predicted by empirically derived allometric equations that use measurements of the
19 size of an individual tree as predictors of its mass (Clark and Kellner, 2012). Among these
20 predictors, diameter at breast height (*D*) and total tree height (*H*) are often used to capture
21 volume variations between trees, whereas wood density (ρ) is used to convert volume to dry
22 mass (Brown et al., 1989). The most frequently used allometric equations for tropical forests
23 (Chave et al., 2005, 2014) have the following form: $TAGB = \alpha * (D^2 * H * \rho)^\beta$, where
24 diameter, height and wood density are combined into a single compound variable related to
25 dry mass through a power law of parameters α and β . This model form, referred to hereafter
26 as our reference allometric model form, performs well when $\beta = 1$ or close to 1 (Chave et al.,
27 2005, 2014), meaning that trees can roughly be viewed as a standard geometric solid for
28 which the parameter α determines the shape (or form factor) of the geometric approximation.
29 However, the uncertainty associated with this model is still very high, with an average error
30 of 50 % at the tree level, illustrating the high natural variability of mass between trees with
31 similar *D*, *H* and ρ values. More importantly, this reference allometric model shows a
32 systematic underestimation of *TAGB* of approximately 20 % in average for the heaviest trees
33 (> 30 Mg) (Fig. 2 in Chave et al. 2014), which may contribute strongly to uncertainty in

1 biomass estimates at the plot level. It is often argued that, by definition, the least-squares
2 regression model implies that tree-level errors are globally centered on 0, thus limiting the
3 plot-level prediction error to approximately 5-10 % for a standard 1-ha forest plot (Chave et
4 al., 2014; Moundounga Mavouroulou et al., 2014). However, systematic errors associated
5 with large trees are expected to disproportionately propagate to plot-level predictions because
6 of their prominent contribution to plot *AGB* (Bastin et al., 2015; Clark and Clark, 1996; Sist et
7 al., 2014; Slik et al., 2013; Stephenson et al., 2014). Thus, identifying the origin of systematic
8 errors in such biomass allometric models is a prerequisite for improving local biomass
9 estimations and thus limiting the risk of uncontrolled error propagation to broad-scale
10 extrapolations.

11 As foresters have known for decades, it is reasonable to approximate stem volume
12 using a geometric shape. Such an approximation, however, is questionable for assessing the
13 total tree volume, including the crown. Because β is generally close to 1 in the reference
14 allometric model, the relative proportion of crown to total tree mass (or crown mass ratio)
15 directly affects the adjustment of the tree form factor α (e.g., Cannell 1984). Moreover, the
16 crown mass ratio is known to vary greatly between species, reflecting different strategies of
17 carbon allocation. For instance, Cannell (1984) observed that coniferous species have a lower
18 proportion of crown mass (10-20 %) than tropical broadleaved species (over 35 %), whereas
19 temperate softwood species were found to have a lower and less variable crown mass ratio
20 (20-30 %) than temperate hardwood species (20-70 %; Freedman et al., 1982; Jenkins et al.,
21 2003). In the tropics, distinct crown size allometries have been documented among species
22 functional groups (Poorter et al. 2003; Poorter, Bongers, et Bongers 2006; Van Gelder,
23 Poorter, et Sterck 2006). For instance, at comparable stem diameters, pioneer species tend to
24 be taller and to have shorter and narrower crowns than understory species (Poorter et al.,
25 2006). These differences reflect strategies of energy investment (tree height vs. crown
26 development) are likely to result in different crown mass ratios among trees with similar D^2 ,
27 H and ρ values. Indeed, Goodman et al. (2014) obtained a substantially improved biomass
28 allometric model when crown diameter was incorporated into the equation to account for
29 individual variation in crown size.

30 Destructive data on tropical trees featuring information on both crown mass and
31 classical biometric measurements (D , H , ρ) are scarce and theoretical work on crown
32 properties largely remains to be validated with field data. In most empirical studies published
33 to date, crown mass models use trunk diameter as a single predictor (e.g., Nogueira et al.

1 2008; Chambers et al. 2001). Such models often provide good results ($R^2 \geq 0.9$), which reflect
2 the strong biophysical constraints exerted by the diameter of the first pipe (the trunk) on the
3 volume of the branching network (Shinozaki et al., 1964). However, theoretical results
4 suggest that several crown metrics would scale with crown mass. For instance, Mäkelä et
5 Valentine (2006) modified the allometric scaling theory (Enquist, 2002; West et al., 1999) by
6 incorporating self-pruning processes into the crown. The authors showed that crown mass is
7 expected to be a power function of the total length of the branching network, which they
8 approximated by crown depth (i.e., total tree height minus trunk height). The construction of
9 the crown and its structural properties have also largely been studied in the light of the
10 mechanical stresses faced by trees (such as gravity and wind; e.g., McMahon et Kronauer
11 1976; Eloy 2011). Within this theoretical frame, crown mass can also be expressed as a power
12 function of crown diameter (King and Loucks, 1978).

13 In the present study, we used a unique tree mass dataset containing crown mass
14 information on 673 trees from five tropical countries and a network of forest plots covering
15 130 ha in central Africa to (i) quantify the variation in crown mass ratio in tropical trees; (ii)
16 assess the contribution of crown mass variation to the reference pantropical model error,
17 either at the tree level or when propagated at the plot level; and (iii) propose a new operational
18 strategy to explicitly account for crown mass variation in biomass allometric equations. We
19 hypothesize that the variation in crown mass ratio in tropical trees is a major source of error in
20 current biomass allometric models and that accounting for this variation would significantly
21 reduce uncertainty associated with plot-level biomass predictions.

22

23 **2 Materials and Methods**

24 **2.1 Biomass data**

25 We compiled tree *AGB* data from published and unpublished sources providing information
26 on crown mass for 673 tropical trees belonging to 132 genera (144 identified species), with a
27 wide tree size range (i.e., diameter at breast height, D : 10-212 cm) and aboveground tree
28 masses of up to 76 Mg. An unpublished dataset for 77 large trees (with $D \geq 67$ cm) was
29 obtained from the fieldwork of PP, NB and SM in semi-deciduous forests of Eastern
30 Cameroon (site characteristics and field protocol in Supplement S1.1 and S1.2.1). The
31 remaining datasets were gathered from relevant published studies: 29 trees from Ghana
32 (Henry et al., 2010), 285 trees from Madagascar (Vieilledent et al., 2011), 51 trees from Peru

1 (Goodman et al., 2014, 2013), 132 trees from Cameroon (Fayolle et al., 2013) and 99 trees
2 from Gabon (Ngomanda et al., 2014). The whole dataset is available from the Dryad Data
3 Repository (<http://dx.doi.org/10.5061/dryad.f2b52>), with details about the protocol used to
4 integrate data from published studies presented in the Supplementary Information (S1.2.2).
5 For the purpose of some analyses, we extracted from this crown mass database (hereafter
6 referred to as Data_{CM1}) a subset of 541 trees for which total tree height was available
7 (Data_{CM2}; all but Fayolle et al. 2013) and another subset of 119 trees for which crown
8 diameter was also available (Data_{CD}; all but Vieilledent et al. 2011, Fayolle et al. 2013,
9 Ngomanda et al. 2014 and 38 trees from our unpublished dataset). Finally, we used as a
10 reference the data from Chave et al. (2014) on the total mass (but not crown mass) of 4,004
11 destructively sampled trees of many different species from all around the tropical world
12 (Data_{REF}).

13

14 **2.2 Forest inventory data**

15 We used a set of 81 large forest plots (> 1 ha), covering a total area of 130 ha, to propagate
16 *TAGB* estimation errors to plot-level predictions. The forest inventory data contained the
17 taxonomic identification of all trees with a diameter at breast height (D) ≥ 10 cm, as well as
18 total tree height measurements (H) for a subset of trees, from which we established plot-level
19 H vs. D relationships to predict the tree height of the remaining trees. Details about the
20 inventory protocol along with statistical procedures used to compute plot *AGB* (or *PAGB*)
21 from field measurements are provided in the Supplementary Information (S1.3). Among these
22 plots, 80 were from a network of 1-ha plots established in humid evergreen to semi-deciduous
23 forests belonging to 13 sites in Cameroon, Gabon and the Democratic Republic of Congo
24 (unpublished data¹). In addition, we included a 50-ha permanent plot from Korup National
25 Park, in the evergreen Atlantic forest of western Cameroon (Chuyong et al., 2004), which we
26 subdivided into 1-ha subplots. Overall, the inventory data encompassed a high diversity of
27 stand structural profiles ranging from open-canopy *Marantaceae* forests to old-growth
28 monodominant *Gilbertiodendron dewevrei* stands and including mixed *terra firme* forests
29 with various levels of degradation.

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¹metadata available at <http://vmamapgn-test.mpl.ird.fr:8080/geonetwork/srv/eng/search#|7dd46c7d-db2f-4bb0-920a-8afe4832f1b3>

1 **2.3 Allometric model fitting**

2 We fitted the pantropical allometric model of Chave et al. (2014) to log-transformed data
3 using ordinary least-squares regression:

$$4 \ln(TAGB) = \alpha + \beta * \ln(D^2 * H * \rho) + \varepsilon \quad (1)$$

5 with *TAGB* (in kg) representing the aboveground tree mass, *D* (in cm) the tree stem diameter,
6 *H* (in m) the total tree height, ρ (in g.cm^{-3}) the wood density and ε the error term, which is
7 assumed to follow a normal distribution $N \sim (0, \text{RSE}^2)$, where RSE is the residual standard
8 error of the model. This model, denoted m_0 , was considered as the reference model.

9 To assess the sensitivity of m_0 to crown mass variations, we built a model (m_1) that
10 restricted the volume approximation to the trunk compartment and included actual crown
11 mass as an additional covariate:

$$12 \ln(TAGB) = \alpha + \beta * \ln(D^2 * Ht * \rho) + \gamma * \ln(Cm) + \varepsilon \quad (2)$$

13 with *Cm* representing the crown mass (in kg) and *Ht* the trunk height (i.e., height of the first
14 main branch, in m). Note that model m_1 cannot be operationally implemented (which would
15 require destructive measurements of crowns) but quantifies the maximal improvement that
16 can be made through the inclusion of crown mass proxies in a biomass allometric model.

17

18 **2.4 Development of crown mass proxies**

19 We further developed crown mass proxies to be incorporated in place of the real crown mass
20 (*Cm*) in the allometric model m_1 . From preliminary tests of various model forms (see
21 Appendix A), we selected a crown mass sub-model based on a volume approximation similar
22 to that made for the trunk component (sm_1):

$$23 \ln(Cm) = \alpha + \beta * \ln(D^2 * Hc * \rho) + \varepsilon \quad (3)$$

24 where *D* is the trunk diameter at breast height (in cm) and *Hc* the crown depth (that is $H - Ht$,
25 in m), available in our dataset Data_{CM2} (n=541).

26 In this sub-model, tree crowns of short stature but large width are assigned a small *Hc*,
27 thus a small mass, whereas the volume they occupy is more horizontal than vertical. We thus
28 tested in sub-model sm_2 (eq. 4) whether using the mean crown size (eq. 5), which accounts for
29 both *Hc* and *Cd* (the crown diameter in m available in our dataset Data_{CD} (n=119)) reduces
30 the error associated with sm_1 :

$$1 \quad \ln(Cm) = \alpha + \beta * \ln(D^2 * Cs * \rho) + \varepsilon \quad (4)$$

$$2 \quad Cs = \frac{(Hc+Cd)}{2} \quad (5)$$

3 Finally, Sillett et al. (2010) showed that for large, old trees, a temporal increment of D and H
 4 poorly reflects the high rate of mass accumulation within crowns. We thus hypothesized that
 5 the relationship between Cm and $D^2*Hc*\rho$ (or $D^2*Cs*\rho$) depends on tree size and fitted a
 6 quadratic (second-order) polynomial model to account for this phenomenon (Niklas, 1995), if
 7 any:

$$8 \quad \ln(Cm) = \alpha + \beta * \ln(D^2 * Hc * \rho) + \gamma * \ln(D^2 * Hc * \rho)^2 + \varepsilon \quad (6)$$

$$9 \quad \ln(Cm) = \alpha + \beta * \ln(D^2 * Cs * \rho) + \gamma * \ln(D^2 * Cs * \rho)^2 + \varepsilon \quad (7)$$

10 where eqs. 6 and 7 are referred to as sub-models 3 and 4, respectively.

11

12 **2.5 Model error evaluation**

13 **2.5.1 Tree-level**

14 From biomass allometric equations, we estimated crown mass (denoted Cm_{est}) or total tree
 15 aboveground mass (denoted $TAGB_{est}$) including (Baskerville, 1972) bias correction during
 16 back-transformation from the logarithmic scale to the original mass unit (i.e., kg). In addition
 17 to classical criteria of model fit assessment (adjusted R^2 , Residual Standard Error, Akaike
 18 Information Criterion), we quantified model uncertainty based on the distribution of
 19 individual relative residuals (in %), which is defined as follows:

$$20 \quad s_i = \left(\frac{Y_{est,i} - Y_{obs,i}}{Y_{obs,i}} \right) * 100 \quad (8)$$

21 where $Y_{obs,i}$ and $Y_{est,i}$ are the crown or tree biomass values in the calibration dataset (i.e.,
 22 measured in the field) and those allometrically estimated for tree i , respectively. We reported
 23 the median of $|s_i|$ values, hereafter referred to as “ S ”, as an indicator of model precision. For a
 24 tree biomass allometric model to be unbiased, we expect s_i to be locally centered on zero for
 25 any given small range of the tree mass gradient. We thus investigated the distribution of s_i
 26 values with respect to tree mass using local regression (loess method; Cleveland, Grosse &
 27 Shyu 1992).

28

29 **2.5.2 Plot level**

1 Allometric models are mostly used to make plot-level *AGB* predictions from non-destructive
2 forest inventory data. Such plot-level predictions are obtained by simply summing individual
3 predictions over all trees in a plot ($PAGB_{pred} = \sum_i TAGB_{pred}$). Prediction errors at the tree
4 level are thus expected to yield an error at the plot level, which may depend on the actual tree
5 mass distribution in the sample plot when the model is locally biased. To account for this
6 effect, we developed a simulation procedure, implemented in two steps, which propagated
7 $TAGB_{pred}$ errors to $PAGB_{pred}$. The first step consists in attributing to each tree i in a given plot
8 a value of $TAGB_{sim}$ corresponding to the actual *AGB* of a similar felled tree selected in
9 $Data_{REF}$ based on its nearest neighbor in the space of the centered-reduced variables D , H and
10 ρ (here taken as species average from Dryad Global Wood Density Database, Chave et al.,
11 2009; Zanne et al., 2009). In a second step, the simulation propagates individual errors of a
12 given allometric model using the local distribution of s_i values as predicted by the loess
13 regression: For each $TAGB_{sim}$, we drew a s_{sim} value from a local normal distribution fitted with
14 the loess parameters (i.e., local mean and standard deviation) predicted for that particular
15 $TAGB_{sim}$. Thus, we generated for each 1-ha plot a realistic $PAGB_{sim}$ (i.e., based on observed
16 felled trees) with repeated realizations of a plot-level prediction error (in %) computed for n
17 trees as follows:

$$18 \quad S_{plot} = \frac{\sum_{i=1}^n (s_{sim}(i) * TAGB_{sim}(i))}{\sum_{i=1}^n TAGB_{sim}(i)}. \quad (9)$$

19 For each of the simulated plots, we provided the mean and standard deviation of 1000
20 realizations of the plot-level prediction error.

21 All analyses were performed with R statistical software 2.15.2 (R Core Team, 2012),
22 using packages lmodel2 (Legendre, 2011), segmented (Muggeo, 2003), FNN (Beygelzimer et
23 al., 2013) and msir (Scrucca, 2011).

24

25 **3 Results**

26 **3.1 Contribution of crown to tree mass**

27 Our crown mass database ($Data_{CMI}$; 673 trees, including 128 trees > 10 Mg) revealed a huge
28 variation in the contribution of crown to total tree mass, ranging from 2.5 to 87.5 % of total
29 aboveground biomass, with a mean of 35.6 % (\pm 16.2 %). Despite this variation, a linear
30 regression (model II) revealed a significant increase in the crown mass ratio with tree mass of
31 approximately 3.7 % per 10 Mg (Fig. 1-A). A similar trend was observed at every site, except

1 for the Ghana dataset (Henry et al. 2010), for which the largest sampled tree (72 Mg) had a
2 rather low crown mass ratio (46 %). Overall, this trend appeared to have been driven by the
3 largest trees in the database (Fig. 1-B). Indeed, the crown mass ratio appeared to be nearly
4 constant for trees ≤ 10 Mg with an average of 34.0 % (± 16.9 %), and then to increase
5 progressively with tree mass, exceeding 50 % on average for trees ≥ 45 Mg.

6

7 **3.2 Crown mass sub-models**

8 All crown mass sub-models provided good fits to our data ($R^2 \geq 0.9$, see Table 1). However,
9 when information on crown diameter was available (Data_{CD}), models that included mean
10 crown size in the compound variable (i.e., C_s , a combination of crown depth and diameter, in
11 sm_2 and sm_4) gave lower AICs and errors (RSE and S) than models that included the simpler
12 crown depth metric (i.e., H_c in sm_1 and sm_3). The quadratic model form provided a better fit
13 than the linear model form (e.g., sm_3 vs. sm_1 fitted on Data_{CM2}), which can be explained by
14 the non-linear increase in crown mass with either of the two proxy variables ($D^2 * H_c * \rho$ or
15 $D^2 * C_s * \rho$). The slope of the relationship between crown mass and, for example, $D^2 * H_c * \rho$
16 presented a breaking point at approximately 7.5 Mg (Davies' test $P < 0.001$) that was not
17 captured by sub-model sm_1 (Fig. 2-A, full line), leading to a substantial bias in back-
18 transformed crown mass estimations (approximately 50 % of observed crown mass for $C_{m_{\text{obs}}} \geq 10$
19 Mg, Fig. 2-B). The quadratic sub-model sm_3 provided fairly unbiased crown mass
20 estimations (Fig. 2-C). Because the first-order term was never significant in the quadratic sub-
21 models, we retained only the second-order term as a crown mass proxy in the biomass
22 allometric models (i.e., $(D^2 * H_c * \rho)^2$ for model m_2 and $(D^2 * C_s * \rho)^2$ for model m_3).

23

24 **3.3 Accounting for crown mass in biomass allometric models**

25 The reference model (m_0) proposed by Chave et al. (2014) presented, when fitted to
26 DATA_{REF} , a bias that was a function of tree mass, with a systematic *AGB* over-estimation for
27 trees $<$ approximately 10 Mg and an under-estimation for larger trees, reaching approximately
28 25 % for trees greater than 30 Mg (Fig. 3-A). This bias pattern reflected a breaking point in
29 the relationship between $D^2 * H * \rho$ and TAGB_{obs} (Davies' test $P < 0.001$) located at
30 approximately 10 Mg (Fig. 3-B). Accounting for actual crown mass (C_m) in the biomass
31 allometric model (i.e., model m_1) corrected for a similar bias pattern observed when m_0 was

1 fitted to $DATA_{CM2}$ (Fig. 4-A). This result shows that variation in crown mass among trees is a
2 major source of bias in the reference biomass allometric model, m_0 .

3 Using our simulation procedure, we propagated individual prediction errors of m_0 and
4 m_1 to the 130 1-ha field plots from central Africa (Fig. 4-B). This process revealed that the
5 reference pantropical model (m_0) led to an average plot-level relative prediction error (S_{plot})
6 ranging from -23 % to +16 % (mean = +6.8 %) on $PAGB_{pred}$, which dropped to +1 to +4 %
7 (mean = +2.6 %) when the model accounted for crown mass (m_1).

8 Because in practice crown mass cannot be routinely measured in the field, we tested
9 the potential of crown mass proxies to improve biomass allometric models. Model m_2 , which
10 used a compound variable integrating crown depth i.e., $(D^2 * Hc * \rho)^2$ as a proxy of crown
11 mass outperformed m_0 (Table 2). Although the gain in precision (RSE and S) over m_0 was
12 rather low, the model provided the major advantage of being free of significant local bias on
13 large trees (> 1 Mg; Fig. 5-A). At the plot level, this model provided a much higher precision
14 (0 to 10 % on $PAGB_{pred}$) and a lower bias (average error of 5 %) than the reference
15 pantropical model m_0 (Fig. 5-B). Using a compound variable integrating crown size i.e.,
16 $(D^2 * Cs * \rho)^2$ as a crown mass proxy (model m_3), thus requiring both crown depth and
17 diameter measurements, significantly improved model precision (m_3 vs. m_2 , Table 2) while
18 preserving the relatively unbiased distribution of relative residuals (results not shown).

19

20 **4 Discussion**

21 Using a dataset of 673 individuals including most of the largest trees that have been
22 destructively sampled to date, we discovered tremendous variation in the crown mass ratio
23 among tropical trees, ranging from 3 to 88 %, with an average of 36 %. This variation was not
24 independent of tree size, as indicated by a marked increase in the crown mass ratio with tree
25 mass for trees ≥ 10 Mg. This threshold was mirrored by a breaking point in the relationship
26 between total tree mass and the compound predictor variable used in the reference allometric
27 model of Chave et al. (2014). When the compound variable is limited to trunk mass
28 prediction, and a crown mass predictor is added to the model, the bias towards large trees is
29 significantly reduced. As a consequence, error propagation to plot-level AGB estimations is
30 largely reduced. In the following section, we discuss the significance and implication of these
31 results from both an ecological and a practical point of view with respect to resource
32 allocation to the tree compartments and to carbon storage in forest aboveground biomass.

1

2 **4.1 Crown mass ratio and the reference biomass model error**

3 We observed an overall systematic increase in the crown mass ratio with tree mass. This
4 ontogenetic trend has already been reported for some tropical canopy species (O'Brien et al.,
5 1995) and likely reflects changes in the pattern of resource allocation underlying crown
6 edification in most forest canopy trees (Barthélémy and Caraglio, 2007; Hasenauer and
7 Monserud, 1996; Holdaway, 1986; Moorby and Wareing, 1963; Perry, 1985). The overall
8 increase in the carbon accumulation rate with tree size is a well-established trend (Stephenson
9 et al., 2014), but the relative contribution of the trunk and the crown to that pattern has rarely
10 been investigated, particularly on large trees for which branch growth monitoring involves a
11 tremendous amount of work. Sillett et al. (2010) collected a unique dataset in this regard, with
12 detailed growth measurements on very old (up to 1850 years) and large (up to 648 cm D)
13 individuals of *Eucalyptus regnans* and *Sequoia sempervirens* species. For these two species,
14 the contribution of crown to AGB growth increased linearly with tree size and thus the crown
15 mass ratio. We observed the same tendency in our data for trees ≥ 10 Mg (typically with $D >$
16 100 cm). This result thus suggests that biomass allometric relationships may differ among
17 small and large trees, thus explaining the systematic underestimation of AGB for large trees
18 observed by Chave et al. (2014). The latter authors suggested that underestimations induced
19 by their model was due to a potential “majestic tree” sampling bias, in which scientists would
20 have more systematically sampled trees with well-formed boles and healthy crowns. We
21 agree that such an effect cannot be completely ruled out, and it is probably all the more
22 significant that trees ≥ 10 Mg represent only 3 % of the reference dataset of Chave et al.
23 (2014). Collecting more field data on the largest tree size classes should therefore constitute a
24 priority if we are to improve multi-specific, broad-scale allometric models, and the recent
25 development of non-destructive AGB estimation methods based on terrestrial LiDAR data
26 should help in this regard (e.g., Calders et al., 2015). However, regardless of whether the non-
27 linear increase in crown mass ratio with tree mass held to a sampling artifact, we have shown
28 that it was the source of systematic error in the reference model that used a unique geometric
29 approximation with an average form factor for all trees. This finding agrees with the results of
30 Goodman et al. (2014) in Peru, who found significant improvements in biomass estimates of
31 large trees when biomass models included tree crown radius, thus partially accounting for
32 crown ratio variations. Identifying predictable patterns of crown mass ratio variation, as
33 performed for crown size allometries specific to some functional groups (Poorter et al. 2003;

1 Poorter, Bongers, et Bongers 2006; Van Gelder, Poorter, et Sterck 2006), therefore appears to
2 be a potential way to improve allometric models performance.

3

4 **4.2 Model error propagation depends on targeted plot structure**

5 The reference pantropical model provided by Chave et al. (2014) presents a bias pattern that is
6 a function of tree size (i.e., average over-estimation of small tree *AGB* and average
7 underestimation of large tree *AGB*). Propagation of individual errors to the plot level therefore
8 depends on tree size distribution in the sample plot, with over- or under-estimations
9 depending on the relative importance of small or large trees in the stand (e.g., young
10 secondary forests vs. old-growth forests; see Appendix B for more information on the
11 interaction between model error, plot structure and plot size). This effect is not consistent with
12 the general assumption that individual errors should compensate at the plot level. Although
13 the dependence of error propagation on tree size distribution has already been raised
14 (Magnabosco Marra et al., 2015; Mascaro et al., 2011), it is generally omitted from error
15 propagation procedures (e.g., Picard, Bosela, et Rossi 2014; Moundounga Mavouroulou et al.
16 2014; Chen, Vaglio Laurin, et Valentini 2015). When propagating local bias to 130 1-ha plots
17 in central Africa, the reference pantropical model led to plot-level errors ranging from -15%
18 to +8%. The presence of large trees, in particular their relative contribution to stand total
19 *AGB*, explained most between-plots error variation (Appendix B). We can therefore
20 hypothesize that in the Neotropics where large trees are less common in forests than in the
21 Paleotropics (Lewis et al., 2013; Slik et al., 2013), the model would more systematically over-
22 estimate plots *AGB*. Interestingly, most of the plots undergoing a systematic *AGB* under-
23 estimation (i.e. high number of large trees) were located in the Atlantic forests of Western
24 Cameroon (Korup NP), where large individuals of *Lecomtedoxa klaineana* (Pierre ex Engl) –
25 a so-called “biomass hyperdominant” species (*sensu* Bastin et al. 2015) – are particularly
26 abundant. Interactions between model error and forest structure may thus also hinder the
27 detection of spatial variations in forests *AGB* between forest types as well as at local scales
28 e.g., between patches dominated or not by *Lecomtedoxa klaineana* trees. At the landscape or
29 regional scale, plot-level errors may average out if the study area is a mosaic of forests with
30 varying tree size distributions. However, if plot estimations are used to calibrate remote
31 sensing products, individual plot errors may propagate as a systematic bias in the final
32 extrapolation (Réjou-Méchain et al. 2014).

1

2 **4.3 Accounting for crown mass variation in allometric models**

3 We propose a modeling strategy that decomposes total tree mass into trunk and crown
4 masses. A direct benefit of addressing these two components separately is that it should
5 reduce the error in trunk mass estimation because the trunk form factor is less variable across
6 species than the whole-tree form factor (Cannell, 1984). We modeled tree crown using a
7 geometric solid whose basal diameter and height were the trunk diameter and crown depth,
8 respectively. Crown volume was thus considered as the volume occupied by branches if they
9 were squeezed onto the main stem (“as if a ring were passed up the stem”; Cannell 1984).
10 Using a simple linear model to relate crown mass to the geometric approximation (sm_1 , sm_2)
11 led to an under-estimation bias that gradually increased with crown mass (Fig. 2-B). A similar
12 pattern was observed on all crown mass models based on trunk diameter (Appendix A) and
13 reflected a significant change in the relationship between the two variables with crown size.
14 Consistently, a second-order polynomial model better captured such a non-linear increase in
15 crown mass with trunk diameter-based proxies and thus provided unbiased crown mass
16 estimates (Fig. 2-C). Our results agree with those of Sillett et al. (2010), who showed that
17 ground-based measurements such as trunk diameter do not properly render the high rate of
18 mass accumulation in large trees, notably in tree crowns, and may also explain why the
19 dynamics of forest biomass are inferred differently from top-down (e.g., airborne LiDAR) or
20 bottom-up views (e.g., field measurement; Réjou-Méchain et al., 2015).
21 Changes in trunk and crown mass along tree ontogeny are not independent and indeed, both
22 variables appeared tightly correlated in our dataset. Including crown mass (or a proxy for this
23 variable) as an additive covariate to the trunk mass proxy may thus raise the debate on
24 collinearity between predictors in biomass allometry models (see Picard et al., 2015; Sileshi,
25 2014). For instance, models m_1 and m_2 calibrated on $Data_{CM2}$ led to a variance inflation factor
26 (VIF) of 5.4 and 8.8, respectively, which is higher than the range of values commonly
27 considered as critical (2-5, Sileshi, 2014). Yet, we have shown that the inclusion of a separate
28 crown component to the models reduced model residuals (greater precision) and improved
29 their distribution over the *AGB* gradient (greater accuracy), because it allowed us to capture a
30 general trend in our dataset of a relative increase of crown mass proportion with tree mass.
31 Assuming that this phenomenon holds in new sets of tropical trees and that we adequately
32 sampled the correlation structure between crown and trunk masses, the issue of predictors

1 collinearity should therefore not dramatically inflate model prediction errors (Picard et al.,
2 2015).

3 From a practical point of view, our tree biomass model m_2 , which requires only extra
4 information on trunk height (if total height is already measured) provides a better fit than the
5 reference pantropical model and removes estimation bias on large trees. In scientific forest
6 inventories, total tree height is often measured on a sub-sample of trees, including most of the
7 largest trees in each plot, to calibrate local allometries between H and D . We believe that
8 measuring trunk height on those trees does not represent a cumbersome amount of additional
9 effort because trunk height is much more easily measured than total tree height. We thus
10 recommend using model m_2 —at least for the largest trees, i.e., those with $D \geq 100$ cm — and
11 encourage future studies to assess its performance from independent datasets. Including more
12 detailed crown measurements into biomass allometric equations could also become a
13 reasonable option in a near future, provided the development of new technologies, like
14 (mobile) terrestrial Lidar scanning, will make it possible to easily extract crown data and
15 gather large-scale datasets.

16

17 **Appendix A: Crown mass sub-models**

18 **A.1 Method**

19 Several tree metrics are expected to scale with crown mass, particularly crown height (Mäkelä
20 and Valentine, 2006), crown diameter (King and Loucks, 1978) or trunk diameter (e.g.,
21 Nogueira et al. 2008; Chambers et al. 2001). In this study, we tested whether any of these
22 variables (i.e., trunk diameter, crown height and crown diameter) prevailed over the others in
23 explaining crown mass variations. Power functions were fitted in log-transformed form using
24 ordinary least-squares regression techniques (models sm_{1-X}):

$$25 \ln(Cm) = \alpha + \beta * \ln(X) + \varepsilon \quad (A1)$$

26 where Cm is the crown mass (in kg); X is the structural variable of interest, namely D for
27 trunk diameter at breast height (in cm), Hc for crown depth (in m), or Cd for crown diameter
28 (in m); α and β are the model coefficients and ε is the error term assumed to follow a normal
29 distribution.

30 We also assessed the predictive power of the three structural variables on crown mass while
31 controlling for variations in wood density (ρ , in g.cm^{-3}), leading to models sm_{2-X} :

$$\ln(Cm) = \alpha + \beta * \ln(X) + \gamma * \ln(\rho) + \varepsilon \quad (\text{A2})$$

where γ is the model coefficient of ρ .

Similarly to the cylindrical approximation of a tree trunk, we further established a compound variable for tree crown based on D and Hc , leading to model sm_3 :

$$\ln(Cm) = \alpha + \beta * \ln(D^2 * Hc * \rho) + \varepsilon \quad (\text{A3})$$

where crown height is a proxy for the length of the branching network. Results obtained using sm_3 are presented in the manuscript as well as in this appendix for comparison with those obtained using sm_{1-x} and sm_{2-x} .

A.2 Results & Discussion

Among the three structural variables tested as proxies for crown mass, trunk diameter provided the best results. Model 1-D presented a high R^2 (0.88), but its precision was low, with an S (i.e., the median of unsigned s_i values) of 43 % (Table A1). Moreover, model error increased appreciably with crown mass (Fig. A1, caption A). For instance, model estimations for an observed crown mass of approximately 20 Mg ranged between 5 and 55 Mg. Nevertheless, sm_{1-D} outperformed sm_{1-Hc} ($Data_{CM2}$, AIC of 1182 vs. 1603, respectively) and was slightly better than sm_{1-Cd} ($Data_{CD}$, AIC of 257 vs. 263, respectively), suggesting that the width of the first branching network pipe is a stronger constraint on branches' mass than the external dimensions of the network (i.e., Hc , Cd).

The model based on crown depth (sm_{1-Hc}) was subjected to a large error (S of c. 80 %; Table A1) and clearly saturated for a crown mass ≥ 10 Mg (Fig. A1, caption B). Because crown depth does not account for branch angle, it does not properly render the length of the branching network. The saturation threshold observed on large crowns supports the observations of Sillett et al. (2010): Tree height, from which crown depth directly derives, levels off in large/adult trees, but mass accumulation—notably within the crowns—continues far beyond this point. It follows that crown depth alone does not allow for the detection of the highest mass levels in large/old tree crowns.

The model based on crown diameter presented a weaker fit than sm_{1-D} , with a higher AIC ($Data_{CD}$, 263 vs. 257) and an individual relative error approximately 10 % higher (S of approximately 50 % and 40 %, respectively; Table A1). However, crown diameter appeared more informative regarding the mass of the largest crowns than trunk diameter (Fig. A2,

1 captions A and B). In fact, the individual relative error of sm_{1-Cd} on crowns ≥ 10 Mg was only
2 26 %, versus 47 % for sm_{1-D} .

3 Accounting for variations in wood density improved the model based on trunk
4 diameter. As shown in Fig. A1, using a color code for wood density highlighted a predictable
5 error pattern in model estimations: Trunk diameter tends to over- or under-estimate the crown
6 mass of trees with high or low wood density, respectively. This pattern is corrected for in sm_{2-}
7 D , which presents a lower AIC than sm_{1-D} (i.e., 1079) and an individual relative error
8 approximately 15 % lower (i.e., 37 %; Table A1). Interestingly, whereas sm_{2-D} appeared to be
9 more accurate than sm_{1-D} in its estimations of large crown mass (Fig. A1, caption C), it also
10 presented an under-estimation bias that gradually increased with crown mass. Including ρ in
11 the model based on Cd improved the model fit (AIC of 251 vs. 262 for sm_{2-Cd} and sm_{1-Cd} ,
12 respectively) and decreased the individual relative error by approximately 15 %. Similarly to
13 sm_{1-Cd} , sm_{2-Cd} was outperformed by its counterpart based on D (AIC of 185). Moreover, the
14 gain in precision in sm_{2-Cd} was localized on small crowns, whereas estimations on large
15 crowns were fairly equivalent (Fig. A2, caption C-D). Model 2-D was more precise on
16 crowns ≥ 10 Mg, with an individual relative error of 23 % versus 32 % for sm_{2-Cd} .

17 The strongest crown mass predictor, D , was used as the basis of a geometric solid
18 approximating crown volume (D^2*Hc) and, in turn, mass ($D^2*Hc*\rho$) in model sm_3 . With one
19 less parameter than sm_{2-D} , sm_3 presented a lower AIC than the former model (i.e., 1012), but
20 the two models provided a fairly similar fit to the observations (RSE of 0.65 vs. 0.61 and S of
21 37 % vs. 36 % for sm_{2-D} and sm_3 , respectively). This result indicates that when D and ρ are
22 known, information on crown depth is of minor importance for predicting crown mass.
23 However, this conclusion applies to our dataset only because Hc might be more informative
24 regarding crown mass variations when considering sites/species with more highly contrasting
25 $D-H$ or $D-Hc$ relationships.

26 Similarly to sm_{2-D} , sm_3 presented an under-estimation bias that increased gradually
27 with crown mass (illustrated in Fig. A1 caption D).

28

29

30

31 **Appendix B: Plot-level error propagation**

1 We used the error propagation procedure described in the Methods section of the manuscript
2 to estimate the mean plot-level *AGB* prediction error that could be expected from m_0
3 calibrated on $DATA_{REF}$ (i.e., the pantropical model proposed in Chave et al. 2014). Model
4 error was propagated on 130 1-ha sample plots of tropical forest in central Africa, a network
5 of 80 1-ha plots (field inventory protocol in Supplement Information S1.3) to which we added
6 50 1-ha plots from Korup 50-ha permanent plot (Chuyong et al., 2004). We further sub-
7 sampled Korup 50-ha permanent plot in sub-plots of varying sizes (from 25 ha to 0.1 ha) to
8 evaluate the effect of plot size on plot-level *AGB* prediction error.

9 From the simulated $PAGB_{sim}$ for the 130 1-ha plots, we estimated that the reference
10 pantropical model, m_0 , propagated to $PAGB_{pred}$ a mean prediction error (over 1000
11 realizations of S_{plot}) that ranged between -15 % and +7.7 % (Fig. B1-A), mostly caused by
12 trees with mass ≥ 20 Mg (Fig. B1-B). This trend was particularly evident in the undisturbed
13 evergreen stands of Korup (triangles in Fig. B1-A-B), where patches of *Lecomtedoxa*
14 *klaineana* (Pierre ex Engl) individuals largely drove the $PAGB$ predictions ($R^2= 0.87$, model
15 II OLS method). This species generates high-statured individuals of high wood density, which
16 frequently exceed 20 Mg and result in underestimates of plot-level biomass. Interestingly,
17 some high-biomass plots could still be over-estimated when $PAGB_{pred}$ was concentrated in
18 trees weighting less than 20 Mg.

19 As a consequence of m_0 bias concentration in large trees, plot-level prediction errors
20 for the 50 ha in Korup tended to stabilize near 0 for subplots ≥ 5 ha only. Below this threshold
21 (i.e., for subplots ≤ 1 ha), the median error is positive but negative outliers are more frequent
22 (Fig. B2). Indeed, on the one hand, small plots are less likely to encompass large trees and
23 have a positive prediction error of up to approximately +7.5 %. On the other hand, a single
24 large tree can strongly affect $PAGB_{pred}$, occasionally leading to a large underestimation of
25 small plots *AGB* that can exceed -15 % for a 0.25-ha and -20 % for a 0.1-ha subplot.

26

27 *Author contributions.* Conceived and designed the experiments: PP, NB and RP. Collected
28 data (unpublished destructive data and field inventories): SM, BS, NGK, ML, DZ, NT, FBB,
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30 Analysis feedback: RP, NB, VR, MRM, UB. Wrote the paper: PP, RP and MRM. Writing
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8

9 **Data Accessibility**

10 Destructive dataset available at <http://dx.doi.org/10.5061/dryad.f2b52>

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Table 1. Crown mass sub-models. Model variables are Cm (crown mass, kg), D (diameter at breast height, cm), Hc (crown depth, m), Cs (average of Hc and crown diameter, m) and ρ (wood density, $\text{g}\cdot\text{cm}^{-3}$). The general form of the models is $\ln(Y) = a + b \cdot \ln(X) + c \cdot \ln(X)^2$. Model coefficient estimates are provided along with the associated standard error denoted SE_i , with i as the coefficient. Coefficients' probability value (pv) is coded as follows: $pv \leq 10^{-4}$: '***', $pv \leq 10^{-3}$: '**', $pv \leq 10^{-2}$: '*', $pv \leq 0.05$: '.' and $pv \geq 0.05$: 'ns'. Models' performance parameters are R^2 (adjusted R square), RSE (residual standard error), S (median of unsigned relative individual errors, in %), AIC (Akaike Information Criterion), dF (degree of freedom).

model	Dataset	Model input			Model parameters						Model performance					
		Y	X	X ²	a	b	c	SE _a	SE _b	SE _c	R ²	RSE	S	AIC	dF	
sm ₁	Data _{CM2} (n=541)		$D^2 \cdot Hc \cdot \rho$	-	-2.6345***	0.9368***		0.1145	0.0125		0.91	0.615	36.0	1012.6	539	
sm ₃		Cm	$D^2 \cdot Hc \cdot \rho$	$(D^2 \cdot Hc \cdot \rho)^2$	0.9017.	0.1143ns	0.0452***	0.5049	0.1153	0.0063	0.92	0.588	35.2	965.2	538	
				-	$(D^2 \cdot Hc \cdot \rho)^2$	1.3990***		0.0514***		0.0605	0.0007	0.92	0.588	35.5	964.2	539
sm ₁	Data _{CD} (n=119)		$D^2 \cdot Hc \cdot \rho$	-	-2.9115***	0.9843***		0.3139	0.0289		0.91	0.516	31.8	184.1	117	
sm ₂			$D^2 \cdot Cs \cdot \rho$	-	-3.0716***	0.9958***		0.2514	0.0231		0.94	0.414	21.8	131.9	117	
sm ₃		Cm	$D^2 \cdot Hc \cdot \rho$	$(D^2 \cdot Hc \cdot \rho)^2$	-0.2682ns	0.4272 ns	0.0283.	1.4077	0.2908	0.0147	0.91	0.510	29.7	182.3	116	
				-	$(D^2 \cdot Hc \cdot \rho)^2$	1.7830***		0.0498***		0.1774	0.0015	0.91	0.512	32.2	182.5	117
sm ₄			$D^2 \cdot Cs \cdot \rho$	$(D^2 \cdot Cs \cdot \rho)^2$	-0.5265ns	0.4617.	0.0270*	1.1443	0.2356	0.0119	0.94	0.407	128.7	25.9	116	
			-	$(D^2 \cdot Cs \cdot \rho)^2$	1.6994***		0.0502***		0.1421	0.0012	0.94	0.412	130.5	25.8	117	

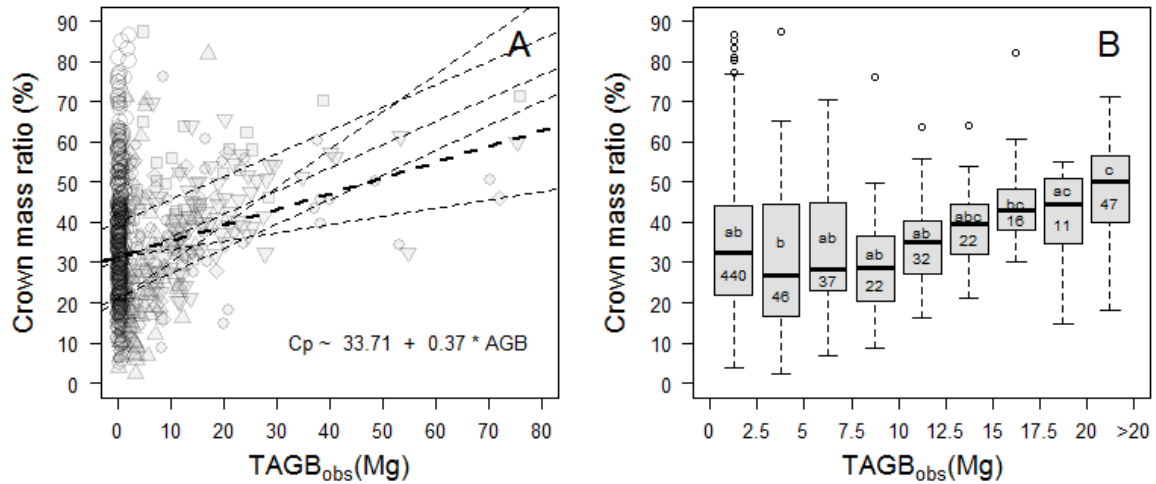
Table 2. Models used to estimate tree AGB. Model parameters are D (diameter at breast height, cm), H (total height, m), Ht (trunk height, m), Hc (crown depth, m), Cm (crown mass, kg), Cs (average of Hc and crown diameter, m) and ρ (wood density, $\text{g}\cdot\text{cm}^{-3}$). The general form of the models is $\ln(Y) = a + b \cdot \ln(X_1) + c \cdot \ln(X_2)$. Model coefficient estimates are provided along with the associated standard error denoted SE_i , with i as the coefficient. Coefficients' probability value (pv) is coded as follows: $\text{pv} \leq 10^{-4}$: '***', $\text{pv} \leq 10^{-3}$: '**', $\text{pv} \leq 10^{-2}$: '*', $\text{pv} \leq 0.05$: '.' and $\text{pv} \geq 0.05$: 'ns'. Models' performance parameters are R^2 (adjusted R square), RSE (residual standard error), S (median of unsigned relative individual errors, in %), AIC (Akaike Information Criterion), dF (degree of freedom).

model	Dataset	Y	Model input		Model parameters					Model performance					
			X_1	X_2	a	b	c	SE_a	SE_b	SE_c	R^2	RSE	S	AIC	dF
m_0	Data _{REF} (n=4004)	AGB	$D^2 \cdot H \cdot \rho$		-2.7628***	0.9759***		0.0211	0.0026		0.97	0.358	22.1	3130.7	4002
m_0	Data _{CM2} (n=541)	AGB	$D^2 \cdot H \cdot \rho$		-2.5860***	0.9603***		0.0659	0.0066		0.98	0.314	18.9	284.8	539
m_1			$D^2 \cdot Ht \cdot \rho$	Cm	-0.5619***	0.5049***	0.4816***	0.0469	0.0098	0.0096	0.99	0.199	9.8	-205.7	538
m_2			$D^2 \cdot Ht \cdot \rho$	$(D^2 \cdot Hc \cdot \rho)^2$	0.3757***	0.4451***	0.0281***	0.0974	0.0186	0.0010	0.98	0.298	17.8	231.5	538
m_0	Data _{CD} (n=119)	AGB	$D^2 \cdot H \cdot \rho$		-3.1105***	1.0119***		0.1866	0.0160		0.97	0.268	15.0	28.1	117
m_1			$D^2 \cdot Ht \cdot \rho$	Cm	-0.5851***	0.4784***	0.5172***	0.1117	0.0203	0.0185	0.99	0.142	7.0	-121.2	116
m_2			$D^2 \cdot Ht \cdot \rho$	$(D^2 \cdot Hc \cdot \rho)^2$	-0.2853ns	0.5804***	0.0216***	0.2499	0.0397	0.0019	0.97	0.272	14.5	32.5	116
m_3			$D^2 \cdot Ht \cdot \rho$	$(D^2 \cdot Cs \cdot \rho)^2$	0.5800*	0.4263***	0.0283***	0.2662	0.0444	0.0021	0.98	0.246	12.3	9.3	116

Table A1. Preliminary crown mass sub-models. Model parameters are D (diameter at breast height, cm), Hc (crown depth, m), Cm (crown mass, kg), Cd (crown diameter, in m), Cs (average of Hc and Cd , m) and ρ (wood density, $\text{g}\cdot\text{cm}^{-3}$). The general form of the models is $\ln(Y) = a + b\cdot\ln(X_1) + c\cdot\ln(X_2)$. Model coefficients' estimates are provided along with the associated standard error denoted SE_i , with i as the coefficient. Coefficients' probability value (pv) is coded as follows: $pv \leq 10^{-4}$: '***', $pv \leq 10^{-3}$: '**', $pv \leq 10^{-2}$: '*', $pv \leq 0.05$: '.' and $pv \geq 0.05$: 'ns'. Models' performance parameters are R^2 (adjusted R square), RSE (residual standard error), S (median of unsigned relative individual errors, in %), AIC (Akaike Information Criterion), dF (degree of freedom).

model	Dataset	Model input			Model parameters						Model performance				
		Y	X_1	X_2	a	b	c	SE_a	SE_b	SE_c	R^2	RSE	S	AIC	dF
1-D	Data _{CM2} (n=541)		D		-3.6163***	2,5786***		0.1514	0.0409		0.88	0.719	42.8	1181.6	539
1-Hc			Hc		-0.1711ns	2.6387***		0.1574	0.0673		0.74	1.060	82.2	1602.8	539
2-D		Cm	D	ρ	-3.0876***	2.6048***	1.1202***	0.1462	0.0372	0.1048	0.90	0.653	36.7	1079.4	538
2-Hc			Hc	ρ	-0.3952*	2.6574***	-0.3274.	0.1959	0.0679	0.1712	0.74	1.058	80.6	1601.1	538
3				$D^2*Hc*\rho$		-2.6345***	0.9368***		0.1145	0.0125		0.91	0.615	36.0	1012.6

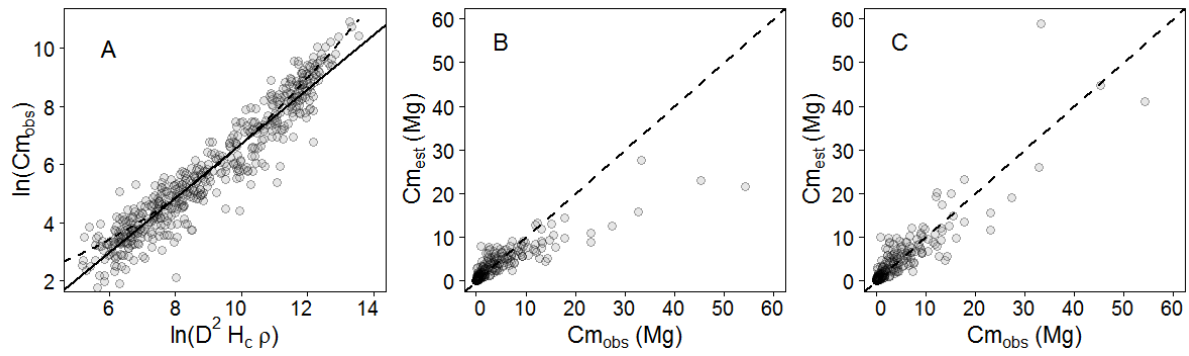
1-D	Data _{CD} (n=119)		D		-3.4603***	2.5684***		0.4692	0.1075		0.83	0.702	39.8	257.4	117
1-Hc			Hc		1.3923*	2.2907***		0.5392	0.1938		0.54	1.149	77.4	374.7	117
1-Cd		Cm	Cd		-0.1181ns	2.8298***		0.3403	0.1218		0.82	0.718	52.7	262.8	117
2-D			D	ρ	-2.7296***	2.6293***	1.5243***	0.3528	0.0793	0.1523	0.91	0.516	30.5	185.3	116
2-Hc			Hc	ρ	1.1181ns	2.3356***	-0.2326ns	0.6869	0.2063	0.3596	0.54	1.152	82.9	376.3	116
2-Cd			Cd	ρ	0.4677ns	2.7954***	0.7538***	0.3585	0.1158	0.2009	0.84	0.681	44.5	251.2	116



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2 Figure 1. (A) Distribution of crown mass ratio (in %) along the range of tree mass ($TAGB_{obs}$,
3 in Mg) for 673 trees. Dashed lines represent the fit of robust regressions (model II linear
4 regression fitted using ordinary least square) performed on the full crown mass dataset (thick
5 line; one-tailed permutation test on slope: p-value < 0.001) and on each separate source (thin
6 lines), with symbols indicating the source: empty circles from Vieilledent et al. (2011;
7 regression line not represented since the largest tree is 3.7 Mg only); solid circles from
8 Fayolle et al. (2013); squares from Goodman et al. (2013, 2014); diamonds from Henry et al.
9 (2010); head-up triangles from Ngomanda et al. (2014); and head-down triangles from the un-
10 published data set from Cameroon. (B) Boxplot representing the variation in crown mass ratio
11 (in %) across tree mass bins of equal width (2.5 Mg). The last bin contains all trees ≥ 20 Mg.
12 The number of individuals per bin and the results of non-parametric pairwise comparisons are
13 represented below and above the median lines, respectively.

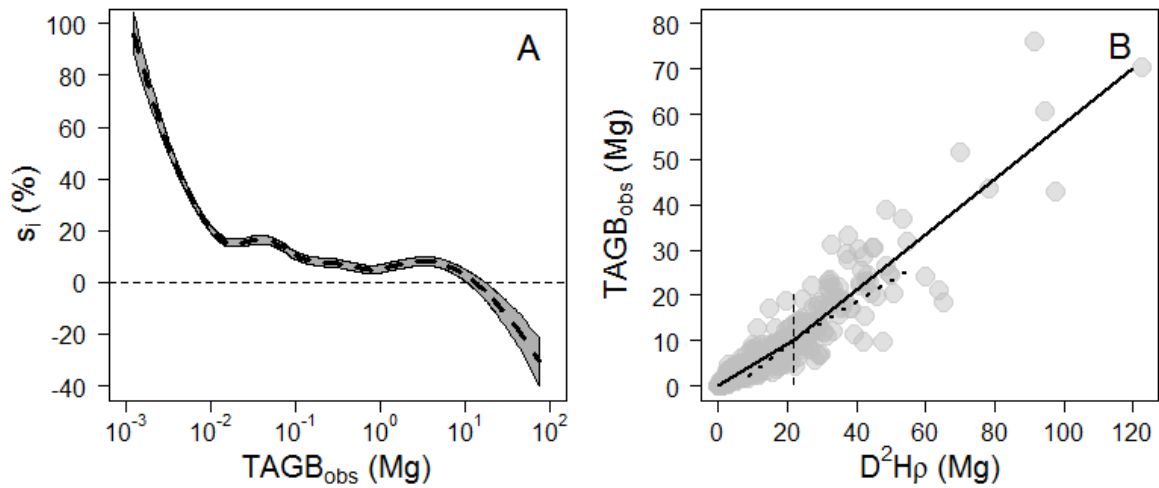
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2 Figure 2. (A) Observed crown mass versus the compound variable $D^2 * Hc * \rho$ (in log scale),
 3 displaying a slightly concave relationship. The crown mass sub-model 1 does not capture this
 4 effect (model fit represented with a full line in caption A), resulting in biased model
 5 predictions (caption B), whereas sub-model 3 does not present this error pattern (model fit
 6 represented as a dashed line in caption A, observed crown mass against model predictions in
 7 caption C). Models were fitted on $Data_{CM2}$.

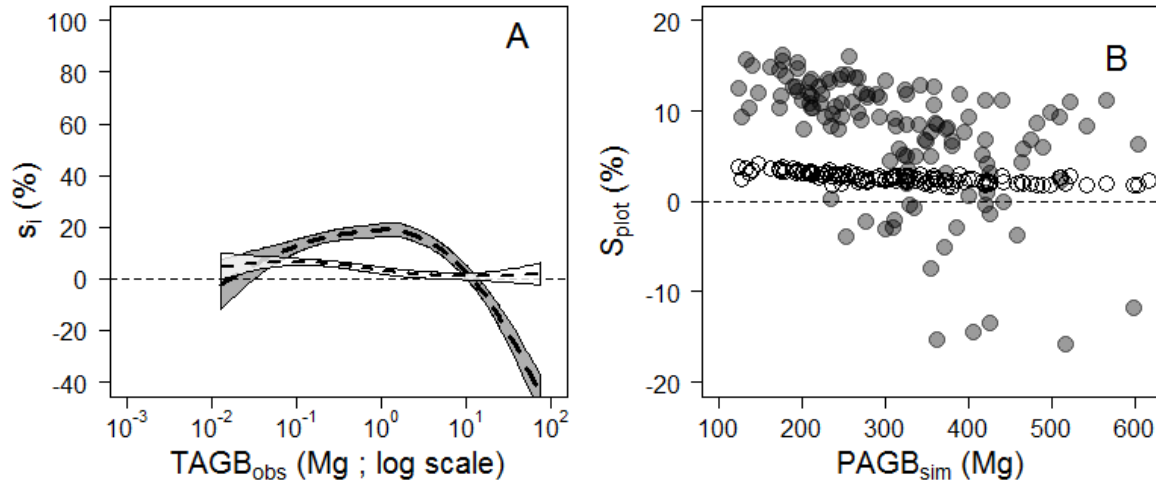
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2 Figure 3. (A) Relative individual residuals (s_i in %) of the reference pantropical model of
 3 Chave et al. (2014) against the tree *AGB* gradient. The thick dashed line represents the fit of a
 4 local regression (loess function, span = 0.5) bounded by standard errors. (B) Observed tree
 5 *AGB* ($TAGB_{obs}$) versus the compound variable $D^2*H*\rho$ with D and H being the tree stem
 6 diameter and height, respectively, and ρ the wood density. A segmented regression revealed a
 7 significant break point (thin vertical dashed line) at approximately 10 Mg of $TAGB_{obs}$ (Davies
 8 test p-value < 2.2e-16).

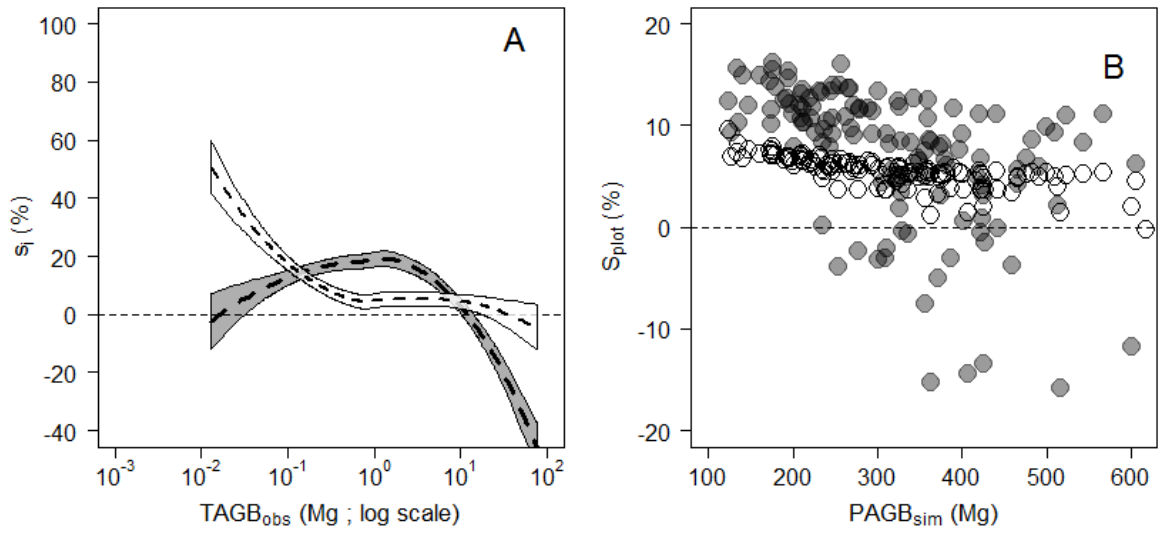
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2 Figure 4. (A) Relative residuals (s_i , in %) of the reference pantropical model m_0 (grey
 3 background) and our model m_1 including crown mass (white background). Thick dashed lines
 4 represent fits of local regressions (loess function, span = 1) bounded by standard errors. (B)
 5 Propagation of individual estimation errors of m_0 (solid grey circles) and m_1 (empty circles) to
 6 the plot level.

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2 Figure 5. (A) Relative individual residuals (s_i , in %) obtained with the reference pantropical
 3 model m_0 (grey background) and with our model including a crown mass proxy, m_2 (white
 4 background). Thick dashed lines represent fits of local regressions (loess function, span = 1)
 5 bounded by standard errors. (B) Propagation of individual residual errors of m_0 (solid grey
 6 circles) and m_2 (empty circles) to the plot level.

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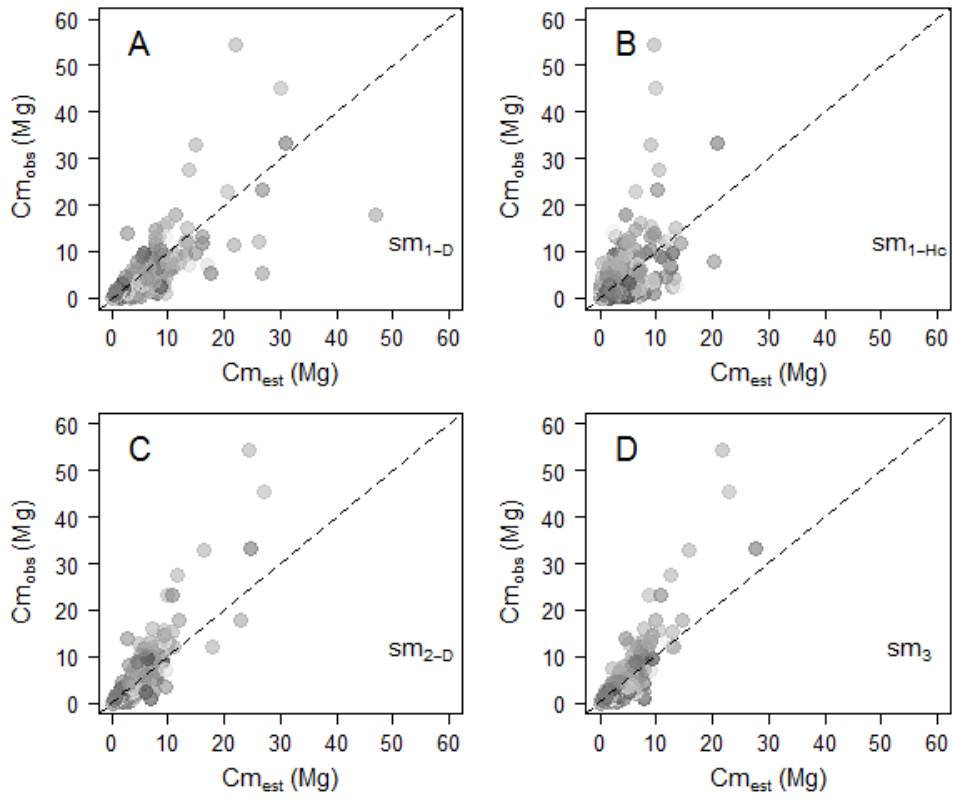


Figure A1. Observed against estimated crown mass (in Mg) for models 1-D (caption A), 1-Hc (caption B), 2-D (caption C), 3 (caption D). Models were calibrated on Data_{CM2}. Tree wood density was standardized to range between 0 and 1 and represented as a grayscale (with black the lowest values and white the highest values).

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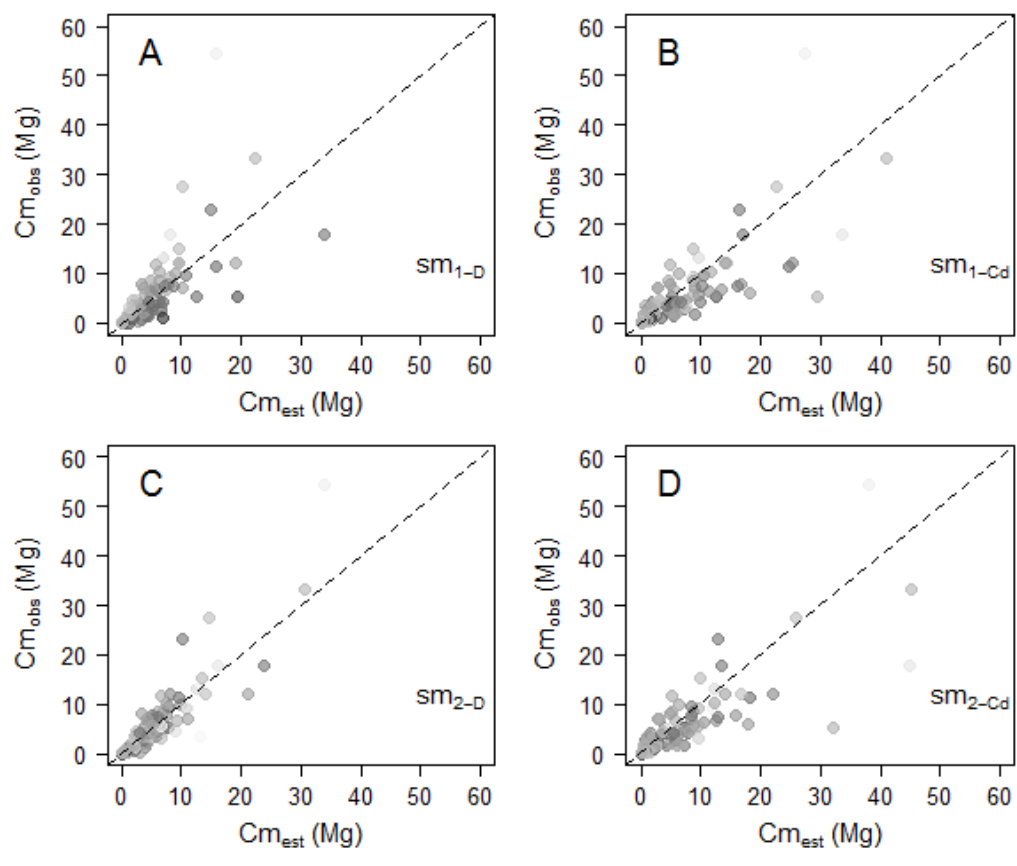
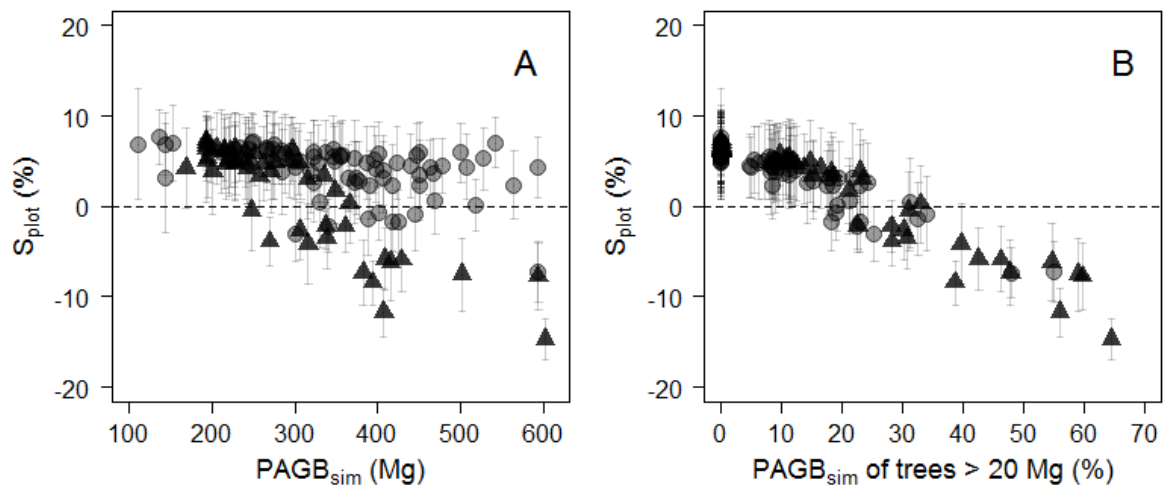


Figure A2. Observed versus estimated crown mass (in Mg) for models 1-D (caption A), 1-Cd (caption B), 2-D (caption C), 2-Cd (caption D). Models were calibrated on Data_{CD}. Tree wood density was standardized to range between 0 and 1 and is represented as a grayscale (with black the lowest values and white the highest values).



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2 Figure B1. Plot-level propagation of individual-level model error. (A) Mean relative error
 3 (S_{plot} , in %) and standard deviation of 1000 random error sampling against simulated plot
 4 *AGB* and (B) against the fraction (%) of simulated plot *AGB* accounted for by trees > 20
 5 Mg. Plots from Korup permanent plot are represented by triangles.

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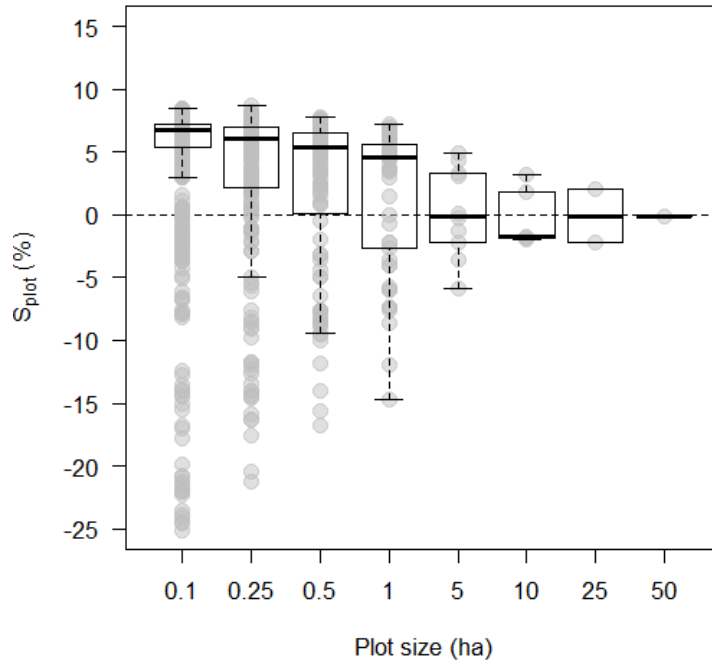


Figure B2. Plot-level relative error (S_{plot} , in %) as a function of plot size (in ha) in Korup permanent plot. Individual plot values are represented by grey dots.