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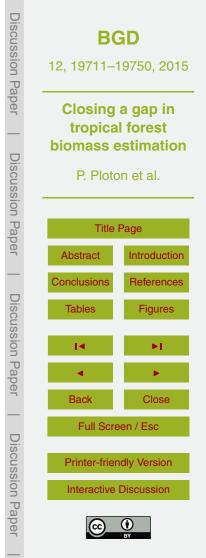
## Closing a gap in tropical forest biomass estimation: accounting for crown mass variation in pantropical allometries

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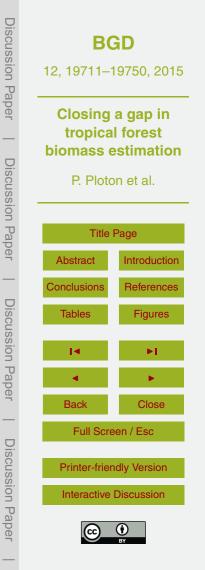
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### Abstract

Accurately monitoring tropical forest carbon stocks is an outstanding challenge. Allometric models that consider tree diameter, height and wood density as predictors are currently used in most tropical forest carbon studies. In particular, a pantropical biomass model has been widely used for approximately a decade, and its most recent version will certainly constitute a reference in the coming years. However, this refer-

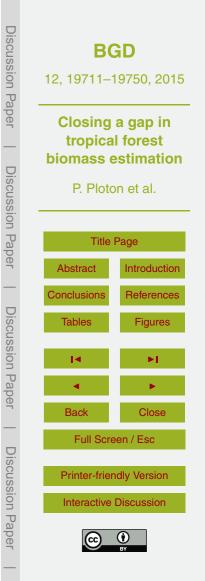
- ence model shows a systematic bias for the largest trees. Because large trees are key drivers of forest carbon stocks and dynamics, understanding the origin and the consequences of this bias is of utmost concern. In this study, we compiled a unique tree mass
  dataset on 673 trees measured in five tropical countries (101 trees > 100 cm in diam-
- eter) and an original dataset of 130 forest plots (1 ha) from central Africa to quantify the error of biomass allometric models at the individual and plot levels when explicitly accounting or not accounting for crown mass variations. We first showed that the proportion of crown to total tree aboveground biomass is highly variable among trees,
- <sup>15</sup> ranging from 3 to 88 %. This proportion was constant on average for trees < 10 Mg (mean of 34 %) but, above this threshold, increased sharply with tree mass and exceeded 50 % on average for trees ≥ 45 Mg. This increase coincided with a progressive deviation between the pantropical biomass model estimations and actual tree mass. Accounting for a crown mass proxy in a newly developed model consistently removed</p>
- the bias observed for large trees (> 1 Mg) and reduced the range of plot-level error from -23-16 to 0-10%. The disproportionally higher allocation of large trees to crown mass may thus explain the bias observed recently in the reference pantropical model. This bias leads to far-from-negligible, but often overlooked, systematic errors at the plot level and may be easily corrected by accounting for a crown mass proxy for the largest
- trees in a stand, thus suggesting that the accuracy of forest carbon estimates can be significantly improved at a minimal cost.



## 1 Introduction

Monitoring forest carbon variation in space and time is both a sociopolitical challenge for climate change mitigation and a scientific challenge, especially in tropical forests, which play a major role in the world carbon balance (Hansen et al., 2013; Harris
et al., 2012; Saatchi et al., 2011). Significant milestones have been reached in the last decade thanks to the development of broad-scale remote sensing approaches (Baccini et al., 2012; Malhi et al., 2006; Mitchard et al., 2013; Saatchi et al., 2011). However, local forest biomass estimations are still the bedrock of most (if not all) of these approaches for the calibration and validation of remote sensing models. As
a consequence, uncertainties and errors in local biomass estimations may propagate dramatically to broad-scale forest carbon stock assessment (Avitabile et al., 2011; Pelletier et al., 2011; Réjou-Méchain et al., 2014). Aboveground biomass (AGB) is the major pool of biomass in tropical forests (Eggleston et al., 2006). The AGB of a tree (or TAGB) is generally predicted by empirically derived allometric equations that use

- <sup>15</sup> measurements of the size of an individual tree as predictors of its mass (Clark and Kellner, 2012). Among these predictors, diameter at breast height (*D*) and total tree height (*H*) are often used to capture volume variations between trees, whereas wood density ( $\rho$ ) is used to convert volume to dry mass (Brown et al., 1989). The most currently used allometric equations for tropical forests (Chave et al., 2005, 2014) have the
- following form: TAGB =  $\alpha \times (D^2 \times H \times \rho)^{\beta}$ , where diameter, height and wood density are combined into a single compound variable related to dry mass through a power law of parameters  $\alpha$  and  $\beta$ . This model form, referred to hereafter as our reference allometric model form, performs well when  $\beta = 1$  or close to 1 (Chave et al., 2005, 2014), meaning that trees can roughly be viewed as a standard geometric solid for which the
- <sup>25</sup> parameter  $\alpha$  determines the shape (or form factor) of the geometric approximation. However, the uncertainty associated with this model is still very high, with an average error of 50 % at the tree level, illustrating the high natural variability of mass between trees with similar *D*, *H* and  $\rho$  values. More importantly, this reference allometric model

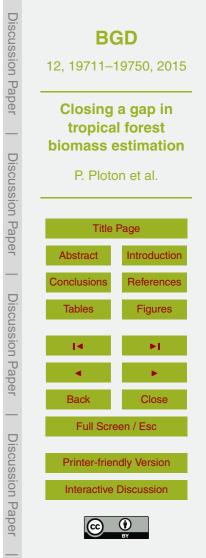


shows a systematic underestimation of TAGB of approximately 20% in average for the heaviest trees (> 30 Mg) (Fig. 2 in Chave et al., 2014), which may contribute strongly to uncertainty in biomass estimates at the plot level. It is often argued that, by definition, the least-squares regression model implies that tree-level errors are globally centered

- on 0, thus limiting the plot-level prediction error to approximately 5–10% for a standard 1 ha forest plot (Chave et al., 2014; Moundounga Mavouroulou et al., 2014). However, systematic errors associated with large trees are expected to disproportionally propagate to plot-level predictions because of their prominent contribution to plot AGB (Bastin et al., 2015; Clark and Clark, 1996; Sist et al., 2014; Slik et al., 2013; Stephenson et al., 0014). Thus, identifying the grinding of sustained is even to such bismess ellowetric errors.
- <sup>10</sup> 2014). Thus, identifying the origin of systematic errors in such biomass allometric models is a prerequisite for improving local biomass estimations and thus limiting the risk of uncontrolled error propagation to broad-scale extrapolations.

As foresters have known for decades, it is reasonable to approximate stem volume using a geometric shape. Such an approximation, however, is questionable for assess-

- <sup>15</sup> ing the total tree volume, including the crown. Because  $\beta$  is generally close to 1 in the reference allometric model, the relative proportion of crown to total tree mass (or crown mass ratio) directly affects the adjustment of the tree form factor  $\alpha$  (e.g., Cannell, 1984). Moreover, the crown mass ratio is known to vary greatly between species, reflecting different strategies of carbon allocation. For instance, Cannell (1984) observed
- that coniferous species have a lower proportion of crown mass (10–20%) than tropical broadleaved species (over 35%), whereas temperate softwood species were found to have a lower and less variable crown mass ratio (20–30%) than temperate hardwood species (20–70%; Freedman et al., 1982; Jenkins et al., 2003). In the tropics, distinct crown size allometries have been documented among species functional groups
- <sup>25</sup> (Poorter et al. 2003, 2006; Van Gelder, Poorter and Sterck, 2006). For instance, at comparable stem diameters, pioneer species tend to be taller and to have shorter and narrower crowns than understory species (Poorter et al., 2006). These differences reflect strategies of energy investment (tree height vs. crown development) that are likely to result in different crown mass ratios among trees with similar  $D^2$ , H and  $\rho$  values.

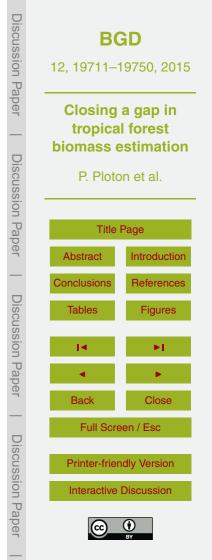


Indeed, Goodman et al. (2014) obtained a substantially improved biomass allometric model when crown diameter was incorporated into the equation to account for individual variation in crown size.

- Destructive data on tropical trees featuring information on both crown mass and classical biometric measurements  $(D, H, \rho)$  are scarce and theoretical work on crown properties largely remains to be validated with field data. In most empirical studies published to date, crown mass models use trunk diameter as a single predictor (e.g., Nogueira et al., 2008; Chambers et al., 2001). Such models often provide good results  $(R^2 \ge 0.9)$ , which reflect the strong biophysical constraints exerted by the diameter of the first pipe (the trunk) on the volume of the branching network (Shinozaki et al., 1964). However, theoretical results suggest that several crown metrics would scale with crown mass. For instance, Mäkelä and Valentine (2006) modified the allometric scaling theory (Enquist, 2002; West et al., 1999) by incorporating self-pruning processes into the crown. The authors showed that crown mass is expected to be a power function of
- the total length of the branching network, which they approximated by crown depth (i.e., total tree height minus trunk height). The construction of the crown and its structural properties have also largely been studied in the light of the mechanical stresses faced by trees (such as gravity and wind; e.g., McMahon and Kronauer, 1976; Eloy, 2011). Within this theoretical frame, crown mass can also be expressed as a power function of crown diameter (King and Loucks, 1978).
- <sup>20</sup> of crown diameter (King and Loucks, 1978).

In the present study, we used a unique tree mass dataset containing crown mass information on 673 trees from five tropical countries and a network of forest plots covering 130 ha in central Africa to (i) quantify the variation in crown mass ratio in tropical trees; (ii) assess the contribution of crown mass variation to the reference pantropi-

cal model error, either at the tree level or when propagated at the plot level; and (iii) propose a new operational strategy to explicitly account for crown mass variation in biomass allometric equations. We hypothesize that the variation in crown mass ratio in tropical trees is a major source of error in current biomass allometric models and



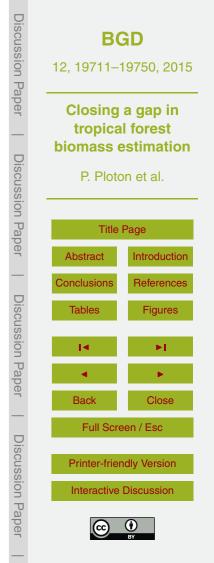
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that accounting for this variation would significantly reduce uncertainty associated with plot-level biomass predictions.

## 2 Materials and methods

## 2.1 Biomass data

- We compiled tree AGB data from published and unpublished sources providing information on crown mass for 673 tropical trees belonging to 132 genera (144 identified species), with a wide tree size range (i.e., diameter at breast height, D: 10–212 cm) and aboveground tree masses of up to 76 Mg. An unpublished dataset for 77 large trees (with  $D \ge 67 \,\mathrm{cm}$ ) was obtained from the fieldwork of P. Ploton, N. Barbier and S. T. Momo in semi-deciduous forests of Eastern Cameroon (site characteristics and 10 field protocol in the Supplement S1.1 and S1.2.1). The remaining datasets were gathered from relevant published studies: 29 trees from Ghana (Henry et al., 2010), 285 trees from Madagascar (Vieilledent et al., 2011), 51 trees from Peru (Goodman et al., 2014, 2013), 132 trees from Cameroon (Fayolle et al., 2013) and 99 trees from Gabon (Ngomanda et al., 2014). The whole dataset is available from the Dryad Data 15 Repository (Dryad, 2015), with details about the protocol used to integrate data from published studies presented in the Supplement S1.2.2. For the purpose of some analyses, we extracted from this crown mass database (hereafter referred to as Data<sub>CM1</sub>) a subset of 541 trees for which total tree height was available (Data<sub>CM2</sub>; all but Fayolle
- et al., 2013) and another subset of 119 trees for which crown diameter was also available (Data<sub>CD</sub>; all but Vieilledent et al. 2011; Fayolle et al. 2013; Ngomanda et al. 2014 and 38 trees from our unpublished dataset). Finally, we used as a reference the data from Chave et al. (2014) on the total mass (but not crown mass) of 4004 destructively sampled trees of many different species from all around the tropical world (Data<sub>BFF</sub>).



#### 2.2 Forest inventory data

We used a set of 81 large forest plots (> 1 ha), covering a total area of 130 ha, to propagate TAGB estimation errors to plot-level predictions. The forest inventory data contained the taxonomic identification of all trees with a diameter at breast height

- $_{5}$  (*D*)  $\geq$  10 cm, as well as total tree height measurements (*H*) for a subset of trees, from which we established plot-level *H* vs. *D* relationships to predict the tree height of the remaining trees. Details about the inventory protocol along with statistical procedures used to compute plot AGB (or PAGB) from field measurements are provided in the Supplement S1.3. Among these plots, 80 were from a network of 1 ha plots established in
- <sup>10</sup> humid evergreen to semi-deciduous forests belonging to 13 sites in Cameroon, Gabon and the Democratic Republic of Congo (unpublished data<sup>1</sup>). In addition, we included a 50 ha permanent plot from Korup National Park, in the evergreen Atlantic forest of western Cameroon (Chuyong et al., 2004), which we subdivided into 1 ha subplots. Overall, the inventory data encompassed a high diversity of stand structural profiles
- <sup>15</sup> ranging from open-canopy *Marantaceae* forests to old-growth monodominant *Gilbertiodendron dewevrei* stands and including mixed *terra firme* forests with various levels of degradation.

#### 2.3 Allometric model fitting

We fitted the pantropical allometric model of Chave et al. (2014) to log-transformed data using ordinary least-squares regression:

 $\ln(\mathsf{TAGB}) = \alpha + \beta \times \ln(D^2 \times H \times \rho) + \varepsilon$ 

with TAGB (in kg) representing the aboveground tree mass, D (in cm) the tree stem diameter, H (in m) the total tree height,  $\rho$  (in g cm<sup>-3</sup>) the wood density and  $\varepsilon$  the error

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term, which is assumed to follow a normal distribution  $N \sim (0, RSE^2)$ , where RSE is the residual standard error of the model. This model, denoted  $m_0$ , was considered as the reference model.

To assess the sensitivity of  $m_0$  to crown mass variations, we built a model  $(m_1)$ that restricted the volume approximation to the trunk compartment and included actual crown mass as an additional covariate:

 $\ln(\mathsf{TAGB}) = \alpha + \beta \times \ln(D^2 \times H \times \rho) + \gamma \times \ln(\mathsf{Cm}) + \varepsilon$ 

with Cm representing the crown mass (in kg) and Ht the trunk height (i.e., height to the first living branch, in m). Note that model  $m_1$  cannot be operationally implemented (which would require destructive measurements of crowns) but quantifies the maximal improvement that can be made through the inclusion of crown mass proxies in a biomass allometric model.

#### 2.4 Development of crown mass proxies

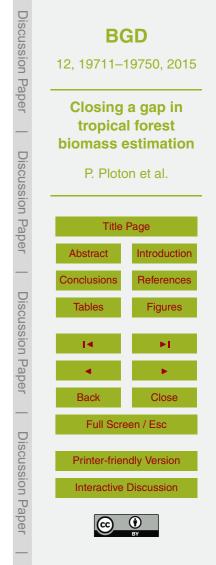
We further developed crown mass proxies to be incorporated in place of the real crown
 mass (Cm) in the allometric model m<sub>1</sub>. From preliminary tests of various model forms (see Appendix A), we selected a crown mass sub-model based on a volume approximation similar to that made for the trunk component (sm<sub>1</sub>):

 $\ln(\text{Cm}) \sim \alpha + \beta \times \ln(D^2 \times \text{Hc} \times \rho) + \varepsilon$ 

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where *D* is the trunk diameter at breast height (in cm) and Hc the crown depth (that is H - Ht, in m), available in our dataset Data<sub>CM2</sub> (n = 541).

In this sub-model, tree crowns of short stature but large width are assigned a small Hc, thus a small mass, whereas the volume they occupy is more horizontal than vertical. We thus tested in sub-model  $sm_2$  (Eq. 4) whether using the mean crown size (Eq. 5), which accounts for both Hc and Cd (the crown diameter in m available in our



(2)

(3)

dataset  $Data_{CD}$  (*n* = 119)) reduces the error associated with sm<sub>1</sub>:

$$ln(Cm) = \alpha + \beta \times ln(D^{2} \times Cs \times \rho) + \varepsilon$$
$$Cs = \frac{(Hc + Cd)}{2}$$

Finally, Sillett et al. (2010) showed that for large, old trees, a temporal increment of <sup>5</sup> *D* and *H* poorly reflects the high rate of mass accumulation within crowns. We thus hypothesized that the relationship between Cm and  $D^2 \times \text{Hc} \times \rho$  (or  $D^2 \times \text{Cs} \times \rho$ ) depends on tree size and fitted a quadratic (second-order) polynomial model to account for this phenomenon (Niklas, 1995), if any:

$$\ln(Cm) = \alpha + \beta \times \ln(D^2 \times Hc \times \rho) + \gamma \times \ln(D^2 \times Hc \times \rho)^2 + \varepsilon$$
(6)

<sup>10</sup> 
$$\ln(\text{Cm}) = \alpha + \beta \times \ln(D^2 \times \text{Cs} \times \rho) + \gamma \times \ln(D^2 \times \text{Cs} \times \rho)^2 + \varepsilon$$

where Eqs. (6) and (7) are referred to as sub-models 3 and 4, respectively.

#### 2.5 Model error evaluation

#### 2.5.1 Tree-level

From biomass allometric equations, we estimated crown mass (denoted Cm<sub>est</sub>) or total tree aboveground mass (denoted TAGB<sub>est</sub>) including (Baskerville, 1972) bias correction during back-transformation from the logarithmic scale to the original mass unit (i.e., kg). In addition to classical criteria of model fit assessment (adjusted *R*<sup>2</sup>, Residual Standard Error, Akaike Information Criterion ), we quantified model uncertainty based on the distribution of individual relative residuals (in %), which is defined as follows:

$$S_{i} = \left(\frac{Y_{\text{est},i} - Y_{\text{obs},i}}{Y_{\text{obs},i}}\right) \times 100$$

(4)

(5)

(7)

(8)

where  $Y_{obs,i}$  and  $Y_{est,i}$  are the crown or tree biomass values in the calibration dataset (i.e., measured in the field) and those allometrically estimated for tree *i*, respectively. We reported the median of  $|s_i|$  values, hereafter referred to as "*S*", as an indicator of model precision. For a tree biomass allometric model to be unbiased, we expect  $s_i$ to be locally centered on zero for any given small range of the tree mass gradient. We thus investigated the distribution of  $s_i$  values with respect to tree mass using local regression (loess method; Cleveland et al., 1992).

#### 2.5.2 Plot level

Allometric models are mostly used to make plot-level AGB predictions from nondestructive forest inventory data. Such plot-level predictions are obtained by simply summing individual predictions over all trees in a plot (PAGB<sub>pred</sub> =  $\sum_i TAGB_{pred}$ ). Prediction errors at the tree level are thus expected to yield an error at the plot level, which may depend on the actual tree mass distribution in the sample plot when the model is locally biased. To account for this effect, we developed a simulation procedure, implemented in two steps, that propagated TAGB<sub>pred</sub> errors to PAGB<sub>pred</sub>. The first step consists in attributing to each tree *i* in a given plot a value of TAGB<sub>sim</sub> corresponding to the actual AGB of a similar felled tree selected in Data<sub>REF</sub> based on its nearest neighbor in the space of the centered-reduced variables *D*, *H* and  $\rho$  (here taken as species average from Dryad Global Wood Density Database, Chave et al., 2009; Zanne et al., 20 2009). In a second step, the simulation propagates individual errors of a given allometric medel using the local distribution of a values as predicted by the locae regression.

ric model using the local distribution of  $s_i$  values as predicted by the loess regression: for each TAGB<sub>sim</sub>, we drew a  $s_{sim}$  value from a local normal distribution fitted with the loess parameters (i.e., local mean and standard deviation) predicted for that particular TAGB<sub>sim</sub>. Thus, we generated for each 1 ha plot a realistic PAGB<sub>sim</sub> (i.e., based on observed felled trees) with repeated realizations of a plot-level prediction error (in %)



computed for *n* trees as follows:

$$S_{\text{plot}} = \frac{\sum_{i=1}^{n} (s_{\text{sim}}(i) \times \text{TAGB}_{\text{sim}}(i))}{\sum_{i=1}^{n} \text{TAGB}_{\text{sim}}(i)}$$

For each of the simulated plots, we provided the mean and standard deviation of 1000 realizations of the plot-level prediction error.

All analyses were performed with *R* statistical software 2.15.2 (R Core Team, 2012), using packages Imodel2 (Legendre, 2011), segmented (Muggeo, 2003), FNN (Beygelz-imer et al., 2013) and msir (Scrucca, 2011).

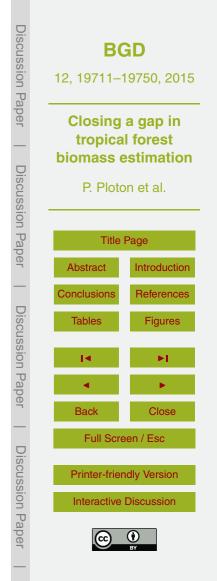
#### 3 Results

#### 3.1 Contribution of crown to tree mass

- <sup>10</sup> Our crown mass database (Data<sub>CM1</sub>; 673 trees, including 128 trees > 10 Mg) revealed a huge variation in the contribution of crown to total tree mass, ranging from 2.5 to 87.5% of total aboveground biomass, with a mean of 35.6% (±16.2%). Despite this variation, a linear regression (model II) revealed a significant increase in the crown mass ratio with tree mass of approximately 3.7% per 10 Mg (Fig. 1a). A similar trend <sup>15</sup> was observed at every site, except for the Ghana dataset (Henry et al., 2010), for which the largest sampled tree (72 Mg) had a rather low crown mass ratio (46%). Overall, this trend appeared to have been driven by the largest trees in the database (Fig. 1b). Indeed, the crown mass ratio appeared to be nearly constant for trees  $\leq$  10 Mg with an average of 34.0% (±16.9%), and then to increase progressively with tree mass, <sup>20</sup> exceeding 50% on average for trees  $\geq$  45 Mg.
- $\sim$  exceeding 50 % on average for frees  $\geq$

#### 3.2 Crown mass sub-models

All crown mass sub-models provided good fits to our data ( $R^2 \ge 0.9$ , see Table 1). However, when information on crown diameter was available (Data<sub>CD</sub>), models that in-



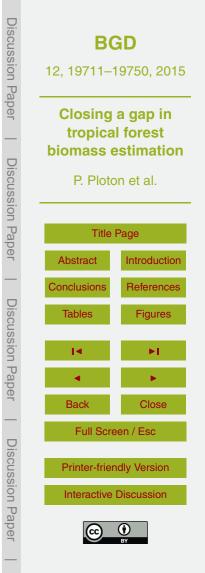
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cluded mean crown size in the compound variable (i.e., Cs, a combination of crown depth and diameter, in sm<sub>2</sub> and sm<sub>4</sub>) gave lower AICs and errors (RSE and *S*) than models that included the simpler crown depth metric (i.e., Hc in sm<sub>1</sub> and sm<sub>3</sub>). The quadratic model form provided a better fit than the linear model form (e.g., sm<sub>3</sub> vs. sm<sub>1</sub> fitted on Data<sub>CM2</sub>), which can be explained by the non-linear increase in crown mass with either of the two proxy variables ( $D^2 \times \text{Hc} \times \rho$  or  $D^2 \times \text{Cs} \times \rho$ ). The slope of the relationship between crown mass and, for example,  $D^2 \times \text{Hc} \times \rho$  presented a breaking point at approximately 7.5 Mg (Davies' test *P* < 0.001) that was not captured by submodel sm<sub>1</sub> (Fig. 2a, full line), leading to a substantial bias in back-transformed crown mass estimations (approximately 50% of observed crown mass for Cm<sub>obs</sub> ≥ 10 Mg, Fig. 2b). The quadratic sub-model sm<sub>3</sub> provided fairly unbiased crown mass estimations (Fig. 2c). Because the first-order term was never significant in the quadratic submodels, we retained only the second-order term as a crown mass proxy in the biomass allometric models (i.e.,  $(D^2 \times \text{Hc} \times \rho)^2$  for model  $m_2$  and  $(D^2 \times \text{Cs} \times \rho)^2$  for model  $m_3$ ).

#### **3.3** Accounting for crown mass in biomass allometric models

The reference model  $(m_0)$  proposed by Chave et al. (2014) presented, when fitted to DATA<sub>REF</sub>, a bias that was a function of tree mass, with a systematic AGB overestimation for trees < approximately 10 Mg and an under-estimation for larger trees, reaching approximately 25% for trees greater than 30 Mg (Fig. 3a). This bias pattern reflected a breaking point in the relationship between  $D^2 \times H \times \rho$  and TAGB<sub>obs</sub> (Davies' test *P* < 0.001) located at approximately 10 Mg (Fig. 3b). Accounting for actual crown mass (Cm) in the biomass allometric model (i.e., model  $m_1$ ) corrected for a similar bias pattern observed when  $m_0$  was fitted to DATA<sub>CM2</sub> (Fig. 4a). This result shows that variation in crown mass among trees is a major source of bias in the reference biomass allometric model,  $m_0$ .

Using our simulation procedure, we propagated individual prediction errors of  $m_0$  and  $m_1$  to the 130 1 ha field plots from central Africa (Fig. 4b). This process revealed that the reference pantropical model ( $m_0$ ) led to an average plot-level relative prediction



error ( $S_{\text{plot}}$ ) ranging from -23 to +16% (mean = +6.8%) on PAGB<sub>pred</sub>, which dropped to +1 to +4% (mean = +2.6%) when the model accounted for crown mass ( $m_1$ ).

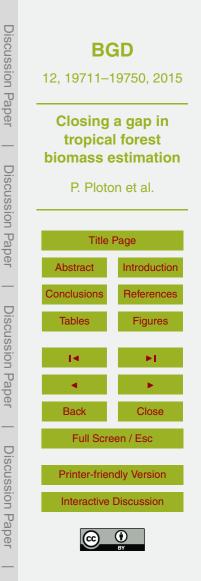
Because in practice crown mass cannot be routinely measured in the field, we tested the potential of crown mass proxies to improve biomass allometric models. Model  $m_2$ ,

- <sup>5</sup> which used a compound variable integrating crown depth i.e.,  $(D^2 \times \text{Hc} \times \rho)^2$  as a proxy of crown mass outperformed  $m_0$  (Table 2). Although the gain in precision (RSE and *S*) over  $m_0$  was rather low, the model provided the striking advantage of being free of significant local bias on large trees (> 1 Mg; Fig. 5a). At the plot level, this model provided a much higher precision (0 to 10% on PAGB<sub>pred</sub>) and a lower bias (average error of 5%) than the reference pantropical model  $m_0$  (Fig. 5b). Using a compound variable
- integrating crown size i.e.,  $(D^2 \times Cs \times \rho)^2$  as a crown mass proxy (model  $m_3$ ), thus requiring both crown depth and diameter measurements, significantly improved model precision ( $m_3$  vs.  $m_2$ , Table 2) while preserving the relatively unbiased distribution of relative residuals (results not shown).

#### 15 4 Discussion

Using a dataset of 673 individuals including most of the largest trees that have been destructively sampled to date, we discovered tremendous variation in the crown mass ratio among tropical trees, ranging from 3 to 88 %, with an average of 36 %. This variation was not independent of tree size, as indicated by a marked increase in the crown mass ratio with tree mass for trees ≥ 10 Mg. This threshold echoed a breaking point in the relationship between total tree mass and the compound predictor variable used in the reference allometric model of Chave et al. (2014). When the compound variable is limited to trunk mass prediction, and a crown mass predictor is added to the model, the bias towards large trees is significantly reduced. As a consequence, error propagation

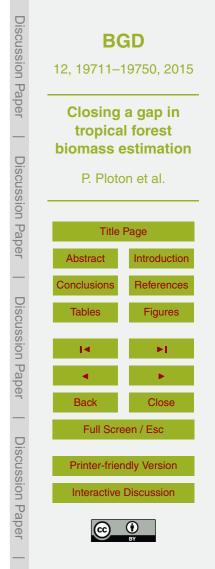
to plot-level AGB estimations is largely reduced. In the following section, we discuss the significance and implication of these results from both an ecological and a practi-



cal point of view with respect to resource allocation to the tree compartments and to carbon storage in forest aboveground biomass.

## 4.1 Crown mass ratio and the reference biomass model error

- We observed an overall systematic increase in the crown mass ratio with tree mass. This ontogenetic trend has already been reported for some tropical canopy species (O'Brien et al., 1995) and likely reflects changes in the pattern of resource allocation underlying crown edification in most forest canopy trees (Barthélémy and Caraglio, 2007; Hasenauer and Monserud, 1996; Holdaway, 1986; Moorby and Wareing, 1963; Perry, 1985). The overall increase in the carbon accumulation rate with tree size is a well-established trend (Stephenson et al., 2014), but the relative contribution of the trunk and the crown to that pattern has rarely been investigated, particularly on large trees for which branch growth monitoring involves a tremendous amount of work. Sillett et al. (2010) collected a unique dataset in this regard, with detailed growth measurements on very old (up to 1850 years) and large (up to 648 cm *D*) individuals of
- <sup>15</sup> *Eucalyptus regnans* and *Sequoia sempervirens* species. For these two species, the contribution of crown to AGB growth increased linearly with tree size and thus the crown mass ratio. We observed the same tendency in our data for trees  $\geq 10 \text{ Mg}$  (typically with D > 100 cm). This result thus suggests that biomass allometric relationships may differ among small and large trees, thus explaining the systematic underestimation
- of AGB for large trees observed by Chave et al. (2014). The latter authors suggested that this model underestimation was due to a potential "majestic tree" sampling bias, in which scientists would have more systematically sampled trees with well-formed boles and healthy crowns. We agree that such an effect cannot be completely ruled out, and it is probably all the more significant that trees ≥ 10 Mg represent only 3% of the ref-
- erence dataset of Chave et al. (2014). Collecting more field data on the largest tree size classes should therefore constitute a priority if we are to improve multi-specific, broad-scale allometric models, and the recent development of non-destructive AGB estimation methods based on terrestrial LiDAR data should help in this regard (e.g.,



Calders et al., 2014). However, regardless of whether the non-linear increase in crown mass ratio with tree mass held to a sampling artifact, we have shown that it was the source of systematic error in the reference model that used a unique geometric approximation with an average form factor for all trees. This finding agrees with the results of

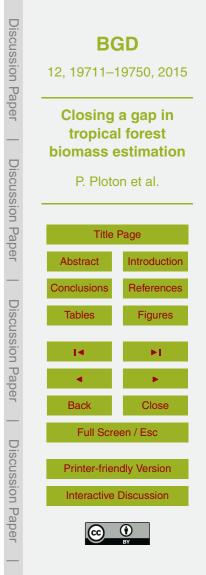
Goodman et al. (2014) in Peru, who found significant improvements in biomass estimates of large trees when biomass models included tree crown radius, thus partially accounting for crown ratio variations. Identifying predictable patterns of crown mass ratio variation, as performed for crown size allometries specific to some functional groups (Poorter et al., 2003, 2006; Van Gelder et al., 2006), therefore appears to be a potential way to improve allometric models performance.

#### 4.2 Model error propagation depends on targeted plot structure

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The reference pantropical model provided by Chave et al. (2014) presents a bias pattern that is a function of tree size (i.e., average over-estimation of small tree AGB and average underestimation of large tree AGB). Propagation of individual errors to the plot level therefore depends on tree size distribution in the sample plot, with over- or underestimations depending on the relative importance of small or large trees in the stand (e.g., young secondary forests vs. old-growth forests; see Appendix B for more information on the interaction between model error, plot structure and plot size). This effect is not consistent with the general assumption that individual errors should compensate

- at the plot level. Although the dependence of error propagation on tree size distribution has already been raised (Magnabosco Marra et al., 2015; Mascaro et al., 2011), it is generally omitted from error propagation procedures (e.g., Picard et al., 2014; Moundounga Mavouroulou et al., 2014; Chen et al., 2015). At a larger scale, such as the landscape or regional scale, plot-level errors may average out if the study area
- is a mosaic of forests with varying tree size distributions. However, if plot estimations are used to calibrate remote sensing products, individual plot errors may propagate as a systematic bias in the final extrapolation (Réjou-Méchain et al., 2014).

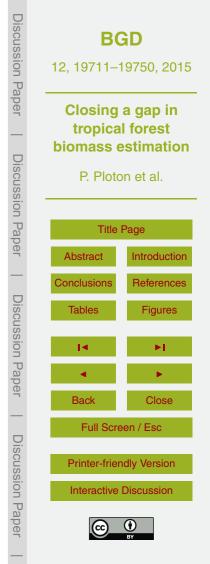


#### 4.3 Accounting for crown mass variation in allometric models

We propose a modeling strategy that decomposes total tree mass into trunk and crown masses. A direct benefit of addressing these two components separately is that it should reduce the error in trunk mass estimation because the trunk form factor is less variable across species than the whole-tree form factor (Cannell, 1984). We modeled tree crown using a geometric solid whose basal diameter and height were the trunk diameter and crown depth, respectively. Crown volume was thus considered as the volume occupied by branches if they were squeezed onto the main stem ("as if a ring were passed up the stem"; Cannell, 1984). Using a simple linear model to relate crown mass to the geometric approximation (sm<sub>1</sub>, sm<sub>2</sub>) led to an under-estimation bias that gradually increased with crown mass (Fig. 2b). A similar pattern was observed on all crown mass models based on trunk diameter (Appendix A) and reflected a significant change in the relationship between the two variables with crown size. Consistently, a second-order polynomial model better captured such a non-linear increase in crown

- mass with trunk diameter-based proxies and thus provided unbiased crown mass estimates (Fig. 2c). Our results agree with those of Sillett et al. (2010), who showed that ground-based measurements such as trunk diameter do not properly render the high rate of mass accumulation in large trees, notably in tree crowns, and may also explain why the dynamics of forest biomass are inferred differently from top-down (e.g., airborne LiDAR) or bottom-up views (e.g., field measurement; Réjou-Méchain et al.,
- 20 airborne LIDAR) or bottom-up views (e.g., field measurement; Rejou-Mechain et 2015).

From a practical point of view, our tree biomass model  $m_2$ , which requires only extra information on trunk height (if total height is already measured) provides a better fit than the reference pantropical model and removes estimation bias on large trees. In <sup>25</sup> scientific forest inventories, total tree height is often measured on a sub-sample of trees, including most of the largest trees in each plot, to calibrate local allometries between *H* and *D*. We believe that measuring trunk height on those trees does not represent a cumbersome amount of additional effort because trunk height is much



more easily measured than total tree height. We thus recommend using model  $m_2$  – at least for the largest trees, i.e., those with  $D \ge 100 \text{ cm}$  – and encourage future studies to assess its performance from independent datasets.

#### Appendix A: Crown mass sub-models

#### 5 A1 Method

Several tree metrics are expected to scale with crown mass, particularly crown height (Mäkelä and Valentine, 2006), crown diameter (King and Loucks, 1978) or trunk diameter (e.g., Nogueira et al., 2008; Chambers et al., 2001). In this study, we tested whether any of these variables (i.e., trunk diameter, crown height and crown diameter) prevailed over the others in explaining crown mass variations. Power functions were fitted in log-transformed form using ordinary least-squares regression techniques (models  $sm_{1-x}$ ):

 $\ln(\text{Cm}) = \alpha + \beta \times \ln(X) + \varepsilon$ 

where Cm is the crown mass (in kg); X is the structural variable of interest, namely D for trunk diameter at breast height (in cm), Hc for crown depth (in m), or Cd for crown diameter (in m);  $\alpha$  and  $\beta$  are the model coefficients and is  $\varepsilon$  the error term assumed to

follow a normal distribution.

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We also assessed the predictive power of the three structural variables on crown mass while controlling for variations in wood density ( $\rho$ , in g cm<sup>-3</sup>), leading to models sm<sub>2-X</sub>:

In(Cm) = 
$$\alpha + \beta \times \ln(X) + \gamma \times \ln(\rho) + \varepsilon$$

(A2)

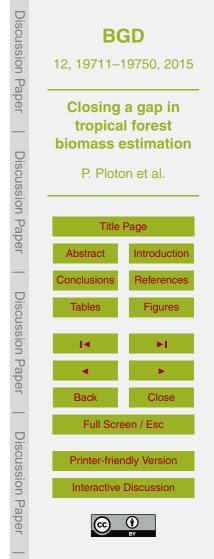
(A3)

(A1)

where  $\gamma$  is the model coefficient of  $\rho$ .

Similarly to the cylindrical approximation of a tree trunk, we further established a compound variable for tree crown based on D and Hc, leading to model sm<sub>3</sub>:

$$\ln(\mathrm{Cm}) = \alpha + \beta \times \ln(D^2 \times \mathrm{Hc} \times \rho) + \varepsilon$$



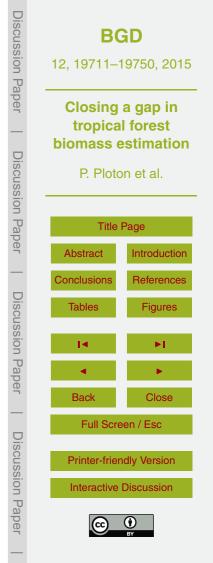
where crown height is a proxy for the length of the branching network. Results obtained using  $sm_3$  are presented in the manuscript as well as in this appendix for comparison with those obtained using  $sm_{1-x}$  and  $sm_{2-x}$ .

#### A2 Results and discussion

- <sup>5</sup> Among the three structural variables tested as proxies for crown mass, trunk diameter provided the best results. Model 1-D presented a high R<sup>2</sup> (0.88), but its precision was low, with an *S* (i.e., the median of unsigned  $s_i$  values) of 43 % (Table A1). Moreover, model error increased appreciably with crown mass (Fig. A1, caption a). For instance, model estimations for an observed crown mass of approximately 20 Mg ranged between 5 and 55 Mg. Nevertheless,  $sm_{1-D}$  outperformed  $sm_{1-Hc}$  (Data<sub>CM2</sub>, AIC of 1182 vs. 1603, respectively) and was slightly better than  $sm_{1-Cd}$  (Data<sub>CD</sub>, AIC of 257 vs. 263, respectively), suggesting that the width of the first branching network pipe is a stronger constraint on branches' mass than the external dimensions of the network (i.e., Hc, Cd).
- The model based on crown depth (sm<sub>1-Hc</sub>) was subjected to a large error (*S* of c. 80%; Table A1) and clearly saturated for a crown mass ≥ 10 Mg (Fig. A1, caption b). Because crown depth does not account for branch angle, it does not properly render the length of the branching network. The saturation threshold observed on large crowns supports the observations of Sillett et al. (2010): tree height, from which crown depth
   directly derives, levels off in large/adult trees, but mass accumulation notably within
- directly derives, levels off in large/adult trees, but mass accumulation notably within the crowns – continues far beyond this point. It follows that crown depth alone does not allow for the detection of the highest mass levels in large/old tree crowns.

The model based on crown diameter presented a weaker fit than  $sm_{1-D}$ , with a higher AIC (Data<sub>CD</sub>, 263 vs. 257) and an individual relative error approximately 10% higher

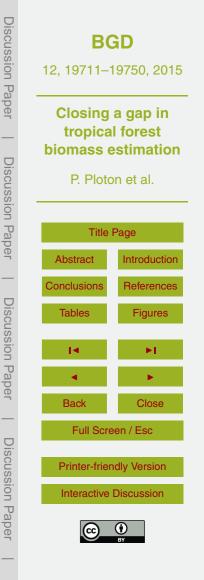
<sup>25</sup> (*S* of approximately 50 and 40%, respectively; Table A1). However, crown diameter appeared more informative regarding the mass of the largest crowns than trunk diameter (Fig. A2, captions a and b). In fact, the individual relative error of  $sm_{1-Cd}$  on crowns  $\geq 10 Mg$  was only 26%, vs. 47% for  $sm_{1-D}$ .



Accounting for variations in wood density improved the model based on trunk diameter. As shown in Fig. A1, using a color code for wood density highlighted a predictable error pattern in model estimations: trunk diameter tends to over- or under-estimate the crown mass of trees with high or low wood density, respectively. This pattern is corrected for in  $sm_{2,D}$ , which presents a lower AIC than  $sm_{1,D}$  (i.e., 1079) and an individual relative error approximately 15% lower (i.e., 37%; Table A1). Interestingly, whereas  $sm_{2,D}$  appeared to be more accurate than  $sm_{1,D}$  in its estimations of large crown mass (Fig. A1, caption c), it also presented an under-estimation bias that gradually increased with crown mass. Including  $\rho$  in the model based on Cd improved the model fit (AIC of 251 vs. 262 for sm<sub>2-Cd</sub> and sm<sub>1-Cd</sub>, respectively) and decreased the individual rela-10 tive error by approximately 15%. Similarly to sm<sub>1-Cd</sub>, sm<sub>2-Cd</sub> was outperformed by its counterpart based on D (AIC of 185). Moreover, the gain in precision in  $sm_{2-Cd}$  was localized on small crowns, whereas estimations on large crowns were fairly equivalent (Fig. A2, caption c and d). Model 2-D was more precise on crowns  $\geq$  10 Mg, with an individual relative error of 23 vs. 32 % for sm<sub>2-Cd</sub>. 15

The strongest crown mass predictor, *D*, was used as the basis of a geometric solid approximating crown volume ( $D^2 \times Hc$ ) and, in turn, mass ( $D^2 \times Hc \times \rho$  in model sm<sub>3</sub>). With one less parameter than sm<sub>2-D</sub>, sm<sub>3</sub> presented a lower AIC than the former model (i.e., 1012), but the two models provided a fairly similar fit to the observations (RSE of 0.65 vs. 0.61 and *S* of 37 vs. 36% for sm<sub>2-D</sub> and sm<sub>3</sub>, respectively). This result indicates that when *D* and  $\rho$  are known, information on crown depth is of minor im-

- portance for predicting crown mass. However, this conclusion applies to our dataset only because Hc might be more informative regarding crown mass variations when considering sites/species with more highly contrasting D-H or D-Hc relationships.
- <sup>25</sup> Similarly to sm<sub>2-D</sub>, sm<sub>3</sub> presented an under-estimation bias that increased gradually with crown mass (illustrated in Fig. A1 caption d).



#### Appendix B: Plot-level error propagation

We used the error propagation procedure described in the Methods section of the manuscript to estimate the mean plot-level AGB prediction error that could be expected from  $m_0$  calibrated on DATA<sub>REF</sub> (i.e., the pantropical model proposed in Chave

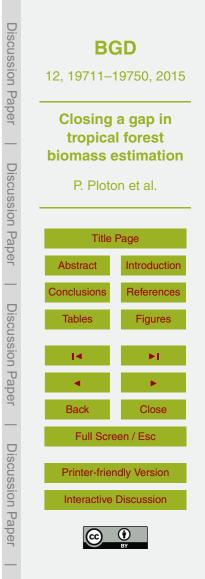
et al., 2014). Model error was propagated on 130 1 ha sample plots of tropical forest in central Africa, a network of 80 1 ha plots (field inventory protocol in the Supplement S1.3) to which we added 50 1 ha plots from Korup 50 ha permanent plot (Chuyong et al., 2004). We further sub-sampled Korup 50 ha permanent plot in sub-plots of varying sizes (from 25 to 0.1 ha) to evaluate the effect of plot size on plot-level AGB
 prediction error.

From the simulated  $PAGB_{sim}$  for the 130 1 ha plots, we estimated that the reference pantropical model,  $m_0$ , propagated to  $PAGB_{pred}$  a mean prediction error (over 1000 realizations of  $S_{plot}$ ) that ranged between -15 and +7.7% (Fig. B1a), mostly caused by trees with mass  $\geq 20 \text{ Mg}$  (Fig. B1b). This trend was particularly evident in the undisturbed evergreen stands of Korup (triangles in Fig. B1a–b), where patches of

<sup>15</sup> the undisturbed evergreen stands of Korup (mangles in Fig. BTa–b), where patches of *Lecomtedoxa klaineana* (Pierre ex Engl) individuals largely drove the PAGB predictions  $(R^2 = 0.87, \text{ model II OLS method})$ . This species generates high-statured individuals of high wood density, which frequently exceed 20 Mg and result in underestimates of plot-level biomass. Interestingly, some high-biomass plots could still be over-estimated <sup>20</sup> when PAGB<sub>pred</sub> was concentrated in trees weighting less than 20 Mg.

As a consequence of  $m_0$  bias concentration in large trees, plot-level prediction errors for the 50 ha in Korup tended to stabilize near 0 for subplots  $\geq$  5 ha only. Below this threshold (i.e., for subplots  $\leq$  1 ha), the median error is positive but negative outliers are more frequent (Fig. B2). Indeed, on the one hand, small plots are less likely to encom-

<sup>25</sup> pass large trees and have a positive prediction error of up to approximately +7.5%. On the other hand, a single large tree can strongly affect  $PAGB_{pred}$ , occasionally leading to a large underestimation of small plots AGB that can exceed -15% for a 0.25 ha and -20% for a 0.1 ha subplot.



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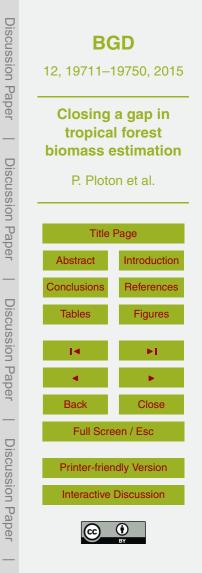
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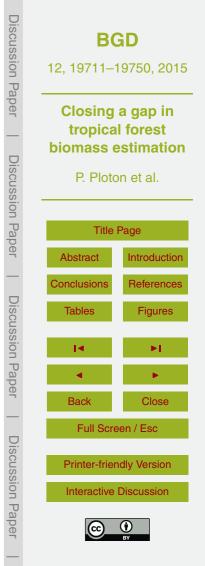
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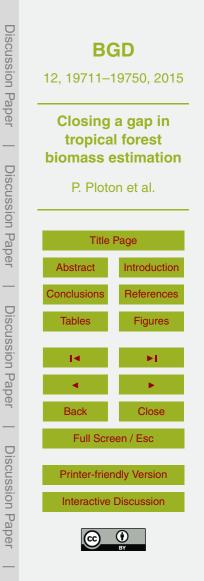
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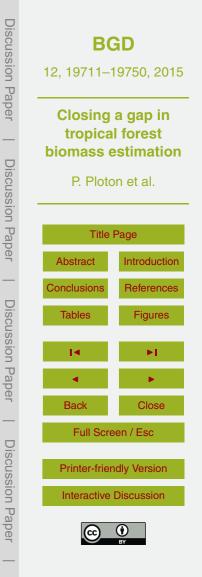


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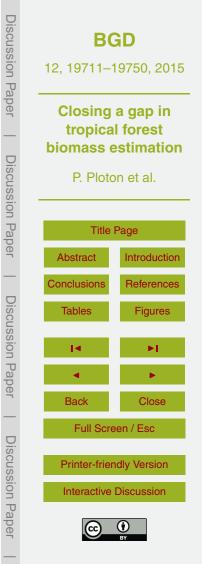
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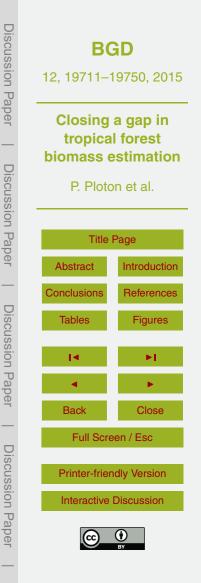
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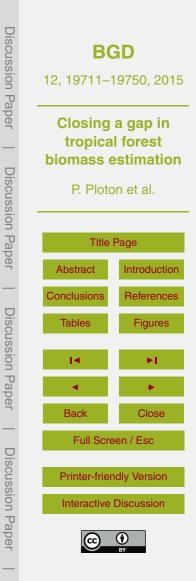
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**Table 1.** Crown mass sub-models. Model variables are Cm (crown mass, kg), *D* (diameter at breast height, cm), Hc (crown depth, m), Cs (average of Hc and crown diameter, m) and  $\rho$  (wood density, g cm<sup>-3</sup>). The general form of the models is  $\ln(Y) = a + b \times \ln(X) + c \times \ln(X)^2$ . Model coefficient estimates are provided along with the associated standard error denoted SE<sub>*i*</sub>, with *i* as the coefficient.

model	Dataset		Model i	nput	Model parameters							Model performance					
		Y	Х	X <sup>2</sup>	а	b	С	SE <sub>a</sub>	SE <sub>b</sub>	$SE_c$	$R^2$	RSE	S	AIC	d <i>F</i>		
sm <sub>1</sub>	Data <sub>CM2</sub>	Cm	$D^2 \times \text{Hc} \times \rho$	-	-2.6345 <sup>a</sup>	0.9368 <sup>a</sup>		0.1145	0.0125		0.91	0.615	36.0	1012.6	539		
sm3	( <i>n</i> = 541)		$D^2 \times Hc \times \rho$	$(D^2 \times Hc \times \rho)^2$	0.9017 <sup>d</sup>	0.1143 <sup>e</sup>	0.0452 <sup>a</sup>	0.5049	0.1153	0.0063	0.92	0.588	35.2	965.2	538		
			-	$(D^2 \times \text{Hc} \times \rho)^2$	1.3990 <sup>a</sup>		0.0514 <sup>a</sup>	0.0605		0.0007	0.92	0.588	35.5	964.2	539		
sm <sub>1</sub>	Data <sub>CD</sub>	Cm	$D^2 \times \text{Hc} \times \rho$	-	-2.9115 <sup>a</sup>	0.9843 <sup>a</sup>		0.3139	0.0289		0.91	0.516	31.8	184.1	117		
sm <sub>2</sub>	( <i>n</i> = 119)		$D^2 \times Cs \times \rho$	-	-3.0716 <sup>a</sup>	0.9958 <sup>a</sup>		0.2514	0.0231		0.94	0.414	21.8	131.9	117		
sm <sub>3</sub>			$D^2 \times Hc \times \rho$	$(D^2 \times \text{Hc} \times \rho)^2$	-0.2682 <sup>e</sup>	0.4272 <sup>e</sup>	0.0283 <sup>d</sup>	1.4077	0.2908	0.0147	0.91	0.510	29.7	182.3	116		
			-	$(D^2 \times Hc \times \rho)^2$	1.7830 <sup>a</sup>		0.0498 <sup>a</sup>	0.1774		0.0015	0.91	0.512	32.2	182.5	117		
sm <sub>4</sub>			$D^2 \times Cs \times \rho$	$(D^2 \times Cs \times \rho)^2$	-0.5265 <sup>e</sup>	0.4617 <sup>d</sup>	0.0270 <sup>c</sup>	1.1443	0.2356	0.0119	0.94	0.407	128.7	25.9	116		
			-	$(D^2 \times Cs \times \rho)^2$	1.6994 <sup>a</sup>		0.0502 <sup>a</sup>	0.1421		0.0012	0.94	0.412	130.5	25.8	117		

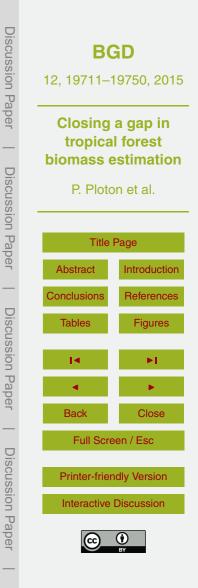
Coefficients' probability value (pv) is coded as follows: <sup>a</sup> pv ≤ 10<sup>-4</sup>, <sup>b</sup> pv ≤ 10<sup>-3</sup>, <sup>c</sup> pv ≤ 10<sup>-2</sup>, <sup>d</sup> pv ≤ 0.05 and <sup>e</sup> pv ≥ 0.05. Models' performance parameters are R<sup>2</sup> (adjusted R square), RSE (residual standard error), S (median of unsigned relative individual errors, in %), AIC (Akaike Information Criterion), dF (degree of freedom).



**Table 2.** Models used to estimate tree AGB. Model parameters are *D* (diameter at breast height, cm), *H* (total height, m), Ht (trunk height, m), Hc (crown depth, m), Cm (crown mass, kg), Cs (average of Hc and crown diameter, m) and  $\rho$  (wood density, g cm<sup>-3</sup>). The general form of the models is  $\ln(Y) = a + b \times \ln(X_1) + c \times \ln(X_2)$ . Model coefficient estimates are provided along with the associated standard error denoted SE<sub>*i*</sub>, with *i* as the coefficient.

model	Dataset		Model in	nput	Model parameters							Model performance					
		Y	<i>X</i> <sub>1</sub>	X <sub>2</sub>	а	b	С	SE <sub>a</sub>	SE <sub>b</sub>	$SE_c$	$R^2$	RSE	S	AIC	dF		
<i>m</i> <sub>0</sub>	Data <sub>REF</sub> ( <i>n</i> = 4004)	AGB	$D^2 \times H \times \rho$		-2.7628 <sup>a</sup>	0.9759 <sup>a</sup>		0.0211	0.0026		0.97	0.358	22.1	3130.7	4002		
<i>m</i> <sub>0</sub>	Data <sub>CM2</sub>	AGB	$D^2 \times H \times \rho$ $D^2 \times Ht \times \rho$	0	-2.5860 <sup>a</sup> -0.5619 <sup>a</sup>	0.9603 <sup>a</sup>	0.40408	0.0659	0.0066		0.98	0.314	18.9	284.8	539		
т <sub>1</sub> т <sub>2</sub>	( <i>n</i> = 541)				-0.5619 0.3757 <sup>a</sup>	0.5049 <sup>a</sup> 0.4451 <sup>a</sup>	0.4816 <sup>a</sup> 0.0281 <sup>a</sup>	0.0469 0.0974	0.0098 0.0186	0.0096 0.0010	0.99 0.98	0.199 0.298	9.8 17.8	-205.7 231.5	538 538		
mo	Data <sub>CD</sub>	AGB	$D^2 \times H \times \rho$		-3.1105 <sup>a</sup>	1.0119 <sup>a</sup>		0.1866	0.0160		0.97	0.268	15.0	28.1	117		
m <sub>1</sub>	(n = 119)		$D^2 \times Ht \times \rho$	Cm	-0.5851 <sup>a</sup>	0.4784 <sup>a</sup>	0.5172 <sup>a</sup>	0.1117	0.0203	0.0185	0.99	0.142	7.0	-121.2	116		
$m_2$			$D^2 \times Ht \times \rho$	$(D^2 \times Hc \times \rho)^2$	-0.2853 <sup>e</sup>	0.5804 <sup>a</sup>	0.0216 <sup>a</sup>	0.2499	0.0397	0.0019	0.97	0.272	14.5	32.5	116		
m <sub>3</sub>			$D^2 \times Ht \times \rho$	$(D^2 \times Cs \times \rho)^2$	0.5800 <sup>c</sup>	0.4263 <sup>a</sup>	0.0283 <sup>a</sup>	0.2662	0.0444	0.0021	0.98	0.246	12.3	9.3	116		

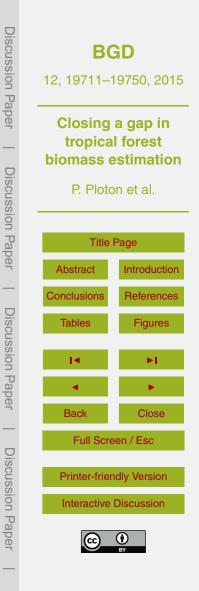
Coefficients' probability value (pv) is coded as follows: <sup>a</sup> pv ≤ 10<sup>-4</sup>, <sup>b</sup> pv ≤ 10<sup>-2</sup>, <sup>c</sup> pv ≤ 0.05 and <sup>a</sup> pv ≥ 0.05. Models' performance parameters are R<sup>2</sup> (adjusted R square), RSE (residual standard error), S (median of unsigned relative individual errors, in %), AIC (Akaike Information Criterion), dF (degree of freedom).

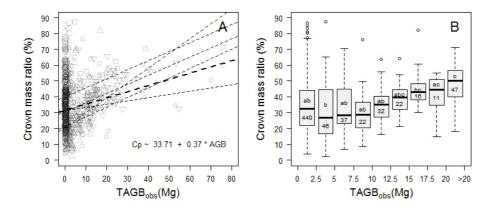


**Table A1.** Preliminary crown mass sub-models. Model parameters are *D* (diameter at breast height, cm), Hc (crown depth, m), Cm (crown mass, kg), Cd (crown diameter, in m), Cs (average of Hc and Cd, m) and  $\rho$  (wood density, gcm<sup>-3</sup>). The general form of the models is  $\ln(Y) = a + b \times \ln(X_1) + c \times \ln(X_2)$ . Model coefficients' estimates are provided along with the associated standard error denoted SE<sub>*i*</sub>, with *i* as the coefficient.

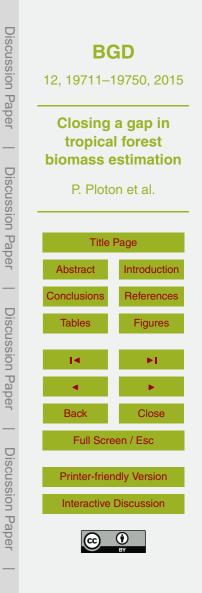
model	Dataset		Model input	Model parameters								Model performance					
		Υ	<i>X</i> <sub>1</sub>	$X_2$	а	b	С	SEa	SEb	SEc	R <sup>2</sup>	RSE	S	AIC	dF		
1-D	Data <sub>CM2</sub>	Cm	D		-3.6163 <sup>a</sup>	2,5786 <sup>a</sup>		0.1514	0.0409		0.88	0.719	42.8	1181.6	539		
1-Hc	(n = 541)		Hc		-0.1711 <sup>e</sup>	2.6387 <sup>a</sup>		0.1574	0.0673		0.74	1.060	82.2	1602.8	539		
2-D			D	ρ	-3.0876 <sup>a</sup>	2.6048 <sup>a</sup>	1.1202 <sup>a</sup>	0.1462	0.0372	0.1048	0.90	0.653	36.7	1079.4	538		
2-Hc			Hc	ρ	-0.3952 <sup>c</sup>	2.6574 <sup>a</sup>	-0.3274 <sup>d</sup>	0.1959	0.0679	0.1712	0.74	1.058	80.6	1601.1	538		
3			$D^2 \times Hc \times \rho$		-2.6345 <sup>a</sup>	0.9368 <sup>a</sup>		0.1145	0.0125		0.91	0.615	36.0	1012.6	539		
1-D	Data <sub>CD</sub>	Cm	D		-3.4603 <sup>a</sup>	2.5684 <sup>a</sup>		0.4692	0.1075		0.83	0.702	39.8	257.4	117		
1-Hc	( <i>n</i> = 119)		Hc		1.3923 <sup>c</sup>	2.2907 <sup>a</sup>		0.5392	0.1938		0.54	1.149	77.4	374.7	117		
1-Cd			Cd		-0.1181 <sup>e</sup>	2.8298 <sup>a</sup>		0.3403	0.1218		0.82	0.718	52.7	262.8	117		
2-D			D	ρ	-2.7296 <sup>a</sup>	2.6293 <sup>a</sup>	1.5243 <sup>a</sup>	0.3528	0.0793	0.1523	0.91	0.516	30.5	185.3	116		
2-Hc			Hc	ρ	1.1181 <sup>e</sup>	2.3356 <sup>a</sup>	-0.2326 <sup>e</sup>	0.6869	0.2063	0.3596	0.54	1.152	82.9	376.3	116		
2-Cd			Cd	ρ	0.4677 <sup>e</sup>	2.7954 <sup>a</sup>	0.7538 <sup>a</sup>	0.3585	0.1158	0.2009	0.84	0.681	44.5	251.2	116		

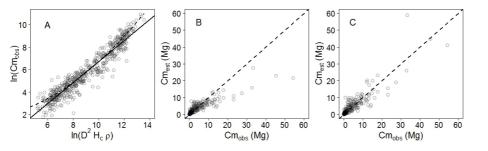
Coefficients' probability value (pv) is coded as follows: <sup>a</sup>  $pv \le 10^{-4}$ , <sup>b</sup>  $pv \le 10^{-2}$ , <sup>d</sup>  $pv \le 0.05$  and <sup>e</sup>  $pv \ge 0.05$ . Models' performance parameters are  $R^2$  (adjusted R square), RSE (residual standard error), S (median of unsigned relative individual errors, in %), AIC (Akaike Information Criterion), dF (degree of freedom).



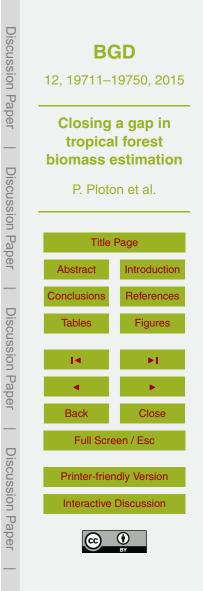


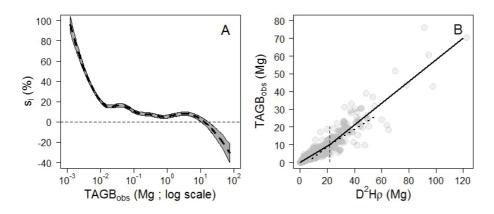
**Figure 1. (a)** Distribution of crown mass ratio (in %) along the range of tree mass (TAGB<sub>obs</sub>, in Mg) for 673 trees. Dashed lines represent the fit of robust regressions (model II linear regression fitted using ordinary least square) performed on the full crown mass dataset (thick line; one-tailed permutation test on slope: *p* value < 0.001) and on each separate source (thin lines), with symbols indicating the source: empty circles from Vieilledent et al. (2011; regression line not represented since the largest tree is 3.7 Mg only); solid circles from Fayolle et al. (2013); squares from Goodman et al. (2013, 2014); diamonds from Henry et al. (2010); head-up triangles from Ngomanda et al. (2014); and head-down triangles from the un-published data set from Cameroon. (b) Boxplot representing the variation in crown mass ratio (in %) across tree mass bins of equal width (2.5 Mg). The last bin contains all trees  $\geq$  20 Mg. The number of individuals per bin and the results of non-parametric pairwise comparisons are represented below and above the median lines, respectively.



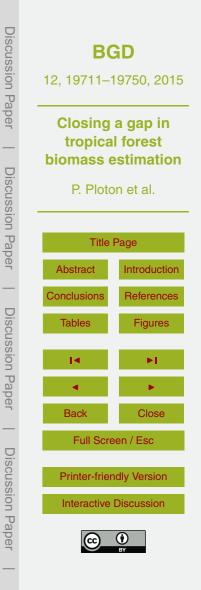


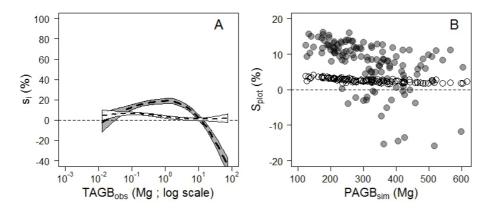
**Figure 2. (a)** Observed crown mass vs. the compound variable  $D^2 \times \text{Hc} \times \rho$  (in log scale), displaying a slightly concave relationship. The crown mass sub-model 1 does not capture this effect (model fit represented with a full line in caption **a**), resulting in biased model predictions (caption **b**), whereas sub-model 3 does not present this error pattern (model fit represented as a dashed line in caption (**a**), observed crown mass against model predictions in caption **c**). Models were fitted on Data<sub>CM2</sub>.

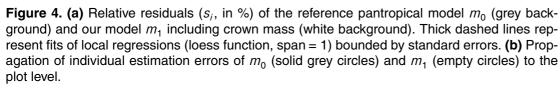




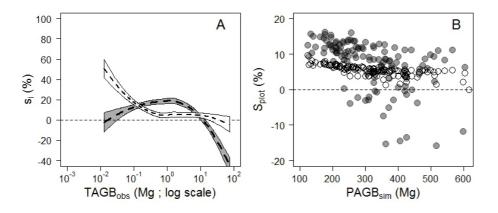
**Figure 3. (a)** Relative individual residuals ( $s_i$  in %) of the reference pantropical model of Chave et al. (2014) against the tree AGB gradient. The thick dashed line represents the fit of a local regression (loess function, span = 0.5) bounded by standard errors. (b) Observed tree AGB (TAGB<sub>obs</sub>) vs. the compound variable  $D^2 \times H \times \rho$  with D and H being the tree stem diameter and height, respectively, and  $\rho$  the wood density. A segmented regression revealed a significant break point (thin vertical dashed line) at approximately 10 Mg of TAGB<sub>obs</sub> (Davies test p value <  $2.2 \times 10^{-16}$ ).



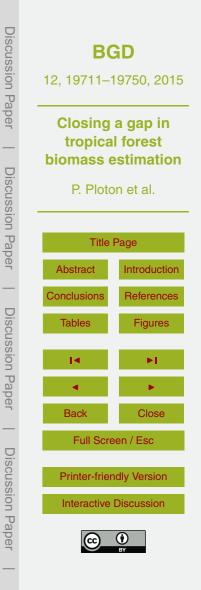


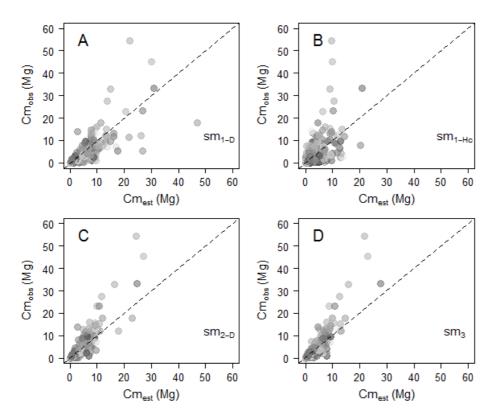




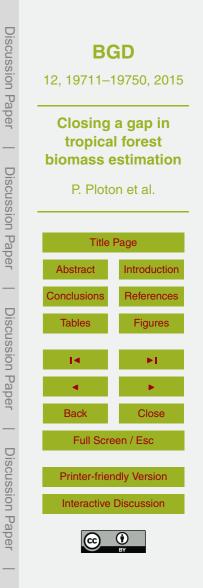


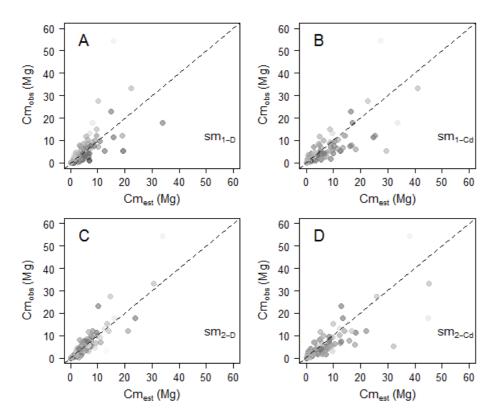
**Figure 5. (a)** Relative individual residuals ( $s_i$ , in %) obtained with the reference pantropical model  $m_0$  (grey background) and with our model including a crown mass proxy,  $m_2$  (white background). Thick dashed lines represent fits of local regressions (loess function, span = 1) bounded by standard errors. **(b)** Propagation of individual residual errors of  $m_0$  (solid grey circles) and  $m_2$  (empty circles) to the plot level.



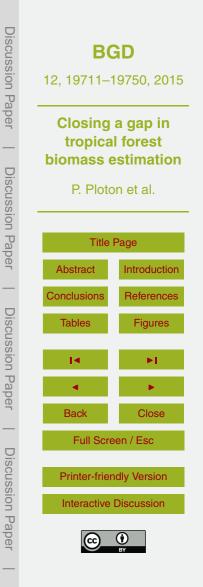


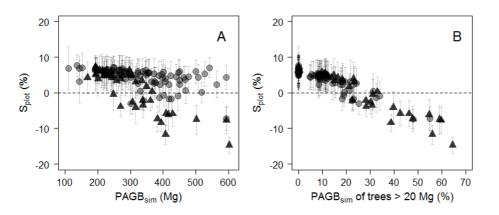
**Figure A1.** Observed against estimated crown mass (in Mg) for models 1-D (caption **a**), 1-Hc (caption **b**), 2-D (caption **c**), 3 (caption **d**). Models were calibrated on  $\text{Data}_{\text{CM2}}$ . Tree wood density was standardized to range between 0 and 1 and represented as a grayscale (with black the lowest values and white the highest values).





**Figure A2.** Observed vs. estimated crown mass (in Mg) for models 1-D (caption **a**), 1-Cd (caption **b**), 2-D (caption **c**), 2-Cd (caption **d**). Models were calibrated on  $\text{Data}_{\text{CD}}$ . Tree wood density was standardized to range between 0 and 1 and is represented as a grayscale (with black the lowest values and white the highest values).





**Figure B1.** Plot-level propagation of individual-level model error. **(a)** Mean relative error ( $S_{plot}$ , in %) and standard deviation of 1000 random error sampling against simulated plot AGB and **(b)** against the fraction (%) of simulated plot AGB accounted for by trees > 20 Mg. Plots from Korup permanent plot are represented by triangles.

