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# Capturing optically important constituents and properties in a marine biogeochemical and ecosystem model

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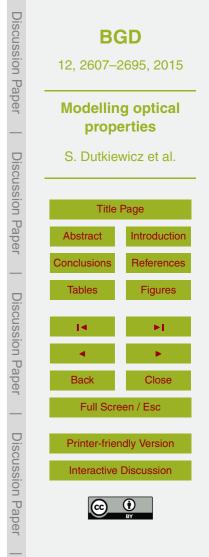
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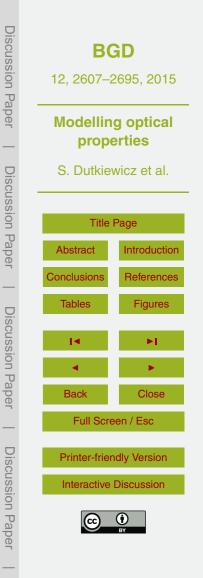
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# Abstract

We present a numerical model of the ocean that couples a three-stream radiative transfer component with a marine biogeochemical-ecosystem in a dynamic threedimensional physical framework. The radiative transfer component resolves spectral <sup>5</sup> irradiance as it is absorbed and scattered within the water column. We explicitly include the effect of several optically important water constituents (the phytoplankton community, detrital particles, and coloured dissolved organic matter, CDOM). The model is evaluated against in situ observed and satellite derived products. In particular we compare to concurrently measured biogeochemical, ecosystem and optical data along a north–south transect of the Atlantic Ocean. The simulation captures the patterns and magnitudes of these data, and estimates surface upwelling irradiance analogous to that observed by ocean colour satellite instruments. We conduct a series of sensitivity experiments to demonstrate, globally, the relative importance of each of the water constituents, and the crucial feedbacks between the light field and the relative

- fitness of phytoplankton types, and the biogeochemistry of the ocean. CDOM has proportionally more importance at short wavelengths and in more productive waters, phytoplankton absorption is especially important at the deep chlorophyll *a* (Chl *a*) maximum, and absorption by water molecules is relatively most important in the highly oligotrophic gyres. Sensitivity experiments in which absorption by any of the optical
- <sup>20</sup> constituents was increased led to a decrease in the size of the oligotrophic regions of the subtropical gyres: lateral nutrient supplies were enhanced as a result of decreasing high latitude productivity. Scattering does not as strongly affect the ecosystem and biogeochemistry fields within the water column but is important for setting the surface upwelling irradiance, and hence sea surface reflectance. Having a model capable of
- <sup>25</sup> capturing bio-optical feedbacks will be important for improving our understanding of the role of light and optical constituents on ocean biogeochemistry, especially in a changing environment. The potential benefits of capturing surface upwelling irradiance will be important for making closer connections to satellite derived products in the future.



# 1 Introduction

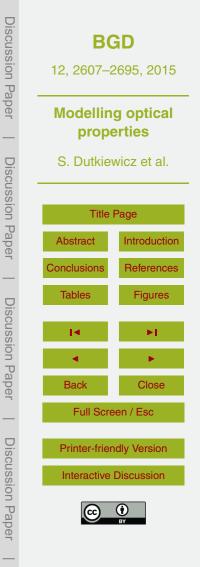
Light is fundamental to phytoplankton and photosynthesis. Understanding ocean production therefore requires detailed knowledge of how light penetrates through the seawater. Attenuation of light within the water column is an interaction of absorption and scattering by "optically important constituents", including water molecules, detrital

matter, coloured dissolved organic matter (CDOM) and the phytoplankton themselves.
Phytoplankton absorb light in the visible spectrum (400 and 700 nm). The optical constituents attenuate these wavelengths differently. For instance, water molecules absorb very strongly in the longer wavelengths (Fig. 1a), while detrital matter and
<sup>10</sup> CDOM absorb more in the shorter wavelengths (Fig. 1b, c). Thus the spectrum of light

- at any location is a complex function of the combination of different optical constituents in the overlying water. Previous studies have highlighted the importance of resolving the spectral light field (e.g. Fujii et al., 2007; Kettle and Merchant, 2009), especially as different species of phytoplankton have different light absorption spectra (e.g. Stramksi
- et al., 2001; Sathyendranath and Platt, 2007). This difference in efficiency of light absorption by phytoplankton is important for their relative fitness and biogeography (Bidigare et al., 1990a; Huisman and Weissing, 1995; Stomp et al., 2004; Hickman et al., 2010).

Much is known about the optics of water (e.g. Pope and Fry, 1997; Smith and Baker,
 1981; Morel, 1974; Zhang and Hu, 2009; Kirk, 1994). Although much is known about the distributions of colored dissolved (Nelson and Siegel, 2013), detritus (Loisel, 2002) and phytoplankton (IOCCG report 15, 2014) it remains unclear how their distributions feed back to phytoplankton community structure and biogeochemistry. Numerical models provide useful tools to explore these interactions, but to do so requires an appropriately detailed description of the photosynthetically available radiation (PAR).

Several recent models resolve the light spectrum and some of the absorption and scattering properties of different constituents (e.g. Mobley et al., 2009; Fujii et al., 2007; Gregg and Casey, 2007; Bisset et al., 1999). Such models include fully coupled



radiative transfer, but differ in the levels of simplification for computational efficiency (e.g. Fujii et al., 2007; Gregg and Casey, 2007) and differ in which and how they treat the different water constituents. For instance CDOM is treated as uniform in Fujii et al. (2007), and linked to chlorophyll a (Chl a) in Gregg and Casey (2007).

- In Sect. 2 we introduce an updated version of the MIT biogeochemistry and ecosystem model (Follows et al., 2007; Dutkiewicz et al., 2012) with a radiative transfer component as well as the explicit treatment of several optical constituents (water molecules, detrital matter, CDOM, and a community of optically-distinct phytoplankton types). Specifically each constituent is treated independently. The fully coupled
   radiative transfer allows us to calculate spectral surface upwelling irradiance; a product
- similar to that measured by ocean colour satellites. We show results from this new coupled model where the light field is a dynamic function of the different optical constituents and evaluate against several data sets (Sect. 3). In particular we use a comprehensive data set from an Atlantic Meridional Transect cruise which includes
- detailed concurrent optical, biogeochemical, and ecosystem observations between the UK and South Africa in September/October of 2004 (AMT-15). Some of the observations are published here for the first time. The data set is ideal for evaluating how our model captures the amount and nature of the light that penetrates the water column across basin scale along with the relevant ecological properties.
- <sup>20</sup> We perform a number of sensitivity experiments that explore the role of each of the water constituents (Sect. 4) and their relative importance. The model allows us to investigate changes to any constituent feeds back to the system, impacting phytoplankton biogeography, biogeochemistry and surface reflectance of irradiance.

#### 2 Model description

<sup>25</sup> The biogeochemical/ecosystem model resolves the cycling of carbon, phosphorus, nitrogen, silica, iron, and oxygen through inorganic, living, dissolved and particulate organic phases as discussed in Follows et al. (2007), Dutkiewicz et al. (2009, 2012),



and Hickman et al. (2010). The biogeochemical and biological tracers are transported and mixed by a the MIT general circulation model (MITgcm) (Marshall et al., 1997). The physical framework is flexible, but here we employ a global configuration which is constrained to be consistent with altimetric and hydrographic observations (the

- <sup>5</sup> ECCO-GODAE state estimates, Wunsch and Heimbach, 2007). This three dimensional configuration has 1° × 1° horizontal resolution and 24 levels ranging from 10 m in the surface to 500 m at depth. These physical fields have been used in many previous biogeochemical/ecosystem studies (e.g. Follows et al., 2007; Dutkiewicz et al., 2009, 2012; Ward et al., 2012; Prowe et al., 2012).
- <sup>10</sup> Similar to several of these previous studies, we resolve several phytoplankton types,  $P_j$  as well as two simple grazers,  $Z_k$ . The biogeochemical and biological tracers interact through the formation, transformation and remineralization of organic matter. Excretion and mortality transfer living organic material into sinking particulate and dissolved organic detritus which are respired back to inorganic form. Aeolian iron fluxes to the <sup>15</sup> ocean surface are provided by Luo et al. (2008).

We provide complete model equations, description and parameter values in Appendix A and Tables 1 to 6. Here we focus on the relevant new features: in particular an explicit radiative transfer component that allows us to consider absorption and scattering of light spectrally and with attention to each of the relevant optical constituents.

## 2.1 Radiative transfer model

Irradiance just below the surface of the ocean is provided by the Ocean–Atmosphere Spectral Irradiance Model (OASIM) (Gregg and Casey, 2009) in two downward streams: direct ( $E_{d_o}^{below}$ ) and diffuse ( $E_{s_o}^{below}$ ). OASIM includes the impact of clouds, water vapour and aerosols in the atmosphere and surface reflectance at the ocean surface. Irradiance are provided in 25 nm wavebands from 400 to 700 nm. The two downward light streams (direct and diffuse,  $E_d$ ,  $E_s$ ) in each waveband are followed through the water column. Irradiance is attenuated by absorption (*a*), and scattering



(*b*), which includes both forward ( $b_f$ ), and backwards ( $b_b$ ) components. Scattering diverts irradiance from the direct and diffuse beams and partitions it between the downward diffuse and an upwelling stream ( $E_u$ ).

We parameterize this "three-stream" irradiance model following Aas (1987), 5 Ackleson et al. (1994), and Gregg (2002). The model is described by the simultaneous equations for the light streams in each waveband ( $\lambda$ ) with depth (*z*):

$$\frac{dE_{d}(\lambda)}{dz} = -\frac{a(\lambda) + b(\lambda)}{\overline{v_{d}}}E_{d}(\lambda)$$

$$\frac{\mathrm{d}E_{\mathrm{s}}(\lambda)}{\mathrm{d}z} = -\frac{a(\lambda) + r_{\mathrm{s}}b_{\mathrm{b}}(\lambda)}{\overline{\upsilon_{\mathrm{s}}}}E_{\mathrm{s}}(\lambda) + \frac{r_{\mathrm{u}}b_{\mathrm{b}}(\lambda)}{\overline{\upsilon_{\mathrm{u}}}}E_{\mathrm{u}}(\lambda) + \frac{b_{\mathrm{f}}(\lambda)}{\overline{\upsilon_{\mathrm{d}}}}E_{\mathrm{d}}(\lambda)$$

$$-\frac{dE_{u}(\lambda)}{dz} = -\frac{a(\lambda) + r_{u}b_{b}(\lambda)}{\overline{v_{u}}}E_{u}(\lambda) + \frac{r_{s}b_{b}(\lambda)}{\overline{v_{s}}}E_{s}(\lambda) + \frac{b_{b}(\lambda)}{\overline{v_{d}}}E_{d}(\lambda)$$
(3)

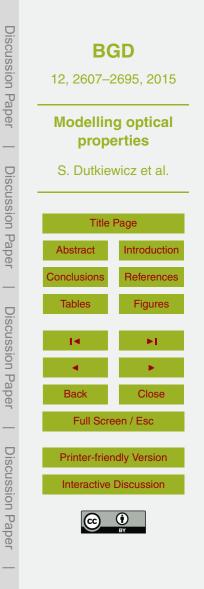
where  $r_s$ ,  $r_u$  and  $r_d$  are the effective scattering coefficients, normalized by backward scattering coefficients,  $\overline{\upsilon_d}$ ,  $\overline{\upsilon_s}$ , and  $\overline{\upsilon_u}$  are the average cosines (definition in Appendix B), and the radiance is separated in the a direct beam and a diffuse component.

This set of equations can be simplified following Aas (1987) by approximating  $r_s$ ,  $r_u$ ,  $r_d$ ,  $\overline{v_s}$  and  $\overline{v_u}$  with constant values (see Appendix B). With these assumptions, the set of equations can be reduced to a tri-diagonal system. In contrast to Aas (1987), Ackleson et al. (1994), and Gregg (2002) we solve  $E_d(\lambda)$ ,  $E_s(\lambda)$  and  $E_u(\lambda)$  directly at each location and at each depth using Gaussian elimination.

We calculate total scalar irradiance,  $E_0(\lambda)$  in each waveband at each location and layer (averaged, multiplicatively, between the top and bottom) by scaling the irradiance by the inverse average cosines:

$$E_{0}(\lambda) = \frac{E_{d}(\lambda)}{\overline{\upsilon_{d}}} + \frac{E_{s}(\lambda)}{\overline{\upsilon_{s}}} + \frac{E_{u}(\lambda)}{\overline{\upsilon_{u}}}$$

This is the light available to the phytoplankton.



(1)

(2)

(4)

#### 2.2 Surface reflectance

Since the model resolves an upwelling stream of irradiance, we can calculate a surface reflectance:

$$R(\lambda) = \frac{E_{u}^{below}(\lambda)|_{k=0}}{E_{d_{o}}^{below}(\lambda) + E_{s_{o}}^{below}(\lambda)}$$

<sup>5</sup> where  $E_{u}^{below}(\lambda)|_{k=0}$  is upwelling irradiance just below the surface and  $E_{d_o}^{below}(\lambda) + E_{s_o}^{below}(\lambda)$  are the downward (direct and diffuse) irradiance just below the surface as provided by OASIM.

To compare to remotely sensed reflectance ( $R_{RS}$ ) we convert between model subsurface reflectance and the slant upward radiance seen by satellite by using a bidirectional function Q:

$$R_{\rm RS}(\lambda) = \frac{R(\lambda)}{Q} \tag{6}$$

The bidirection function Q has values 3.5 and 5 sr depending on many variables, including inherent optical properties of the water, wavelength and solar zenith angles (Morel et al., 2002; Voss et al., 2007). For simplicity here we assume that Q = 4 sr. Model  $R_{\rm RS}$  is therefore analogous, but not exactly the same as that measured by satellite.

#### 2.3 Treatment of water constituents

15

Attenuation of irradiance results from absorption by water molecules  $(a_w)$ , phytoplankton  $(a_{phy})$ , detrital particles  $(a_{det})$  and coloured dissolved organic matter  $(a_{cdom})$  and by scattering by water molecules  $(b_w)$ , phytoplankton  $(b_{phy})$  and detrital particles  $(b_{det})$ . The absorption (a), total scattering (b) and backward scattering  $(b_b)$ 

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(5)

(all with units of  $m^{-1}$ ) are represented as a function of waveband:

$$a(\lambda) = a_{w}(\lambda) + a_{phy}(\lambda) + a_{det}(\lambda) + a_{cdom}(\lambda)$$

$$b(\lambda) = b_w(\lambda) + b_{phy}(\lambda) + b_{det}(\lambda)$$

 $b_{\rm b}(\lambda) = b_{\rm bw}(\lambda) + b_{\rm bphy}(\lambda) + b_{\rm bdet}(\lambda)$ 

#### 5 2.3.1 Water molecules

We assume absorption by water molecules  $(a_w, b_w, b_{bw})$  to follow the spectra of Pope and Fry 1997). Scattering is taken from Smith and Baker (1981) and Morel (1974), and backscattering from Morel (1974) and Morel et al. (2007). The spectra for these are shown in Fig. 1a.

# 10 2.3.2 Detrital matter

15

The model uses the absorption and scattering spectrum for detrital matter from Stramski et al. (2001). Since these spectra (Fig. 1b) were calculated as a function of concentration of particles, we introduce the coefficient  $p_{part}$  to convert the model particulate organic carbon (POC) to number of particles. The absorption and scattering by particles is described as:

$$a_{det}(\lambda) = a_{det}^{part}(\lambda) \frac{POC}{\rho_{part}}$$
(10)  

$$b_{det}(\lambda) = b_{det}^{part}(\lambda) \frac{POC}{\rho_{part}}$$
(11)  

$$b_{bdet}(\lambda) = b_{bdet}^{part}(\lambda) \frac{POC}{\rho_{part}}$$
(12)

Here we use the convention that the superscript on the *a*, *b*, and  $b_{\rm b}$  terms refers to the normalization variable, here particle concentration. Units of  $a_{\rm det}^{\rm part}(\lambda)$ ,  $b_{\rm det}^{\rm part}(\lambda)$  and  $b_{\rm bdet}^{\rm part}(\lambda)$  are m<sup>2</sup> particle<sup>-1</sup>.



(7)

(8)

(9)

#### 2.3.3 Coloured dissolved organic matter

CDOM absorbs highly in the short wavelengths and absorption decreases exponentially with increasing wavelength (Kitidis et al., 2006; Nelson and Siegel, 2013). CDOM is not usually explicitly resolved in marine ecosystem models (exceptions are <sup>5</sup> Xiu and Chai (2014) and Bissett et al., 1999). Here we have resolved an explicit CDOMlike tracer (denoted "CDOM") similar to Bissett et al. (1999). The model CDOM has units of concentration (mmol Cm<sup>-3</sup>), and is assumed have a source that is a fraction ( $f_{cdom}$ ) of DOM production, to have a long remineralization time scales ( $d_{cdom}$ ) and to be bleached under high light conditions. The bleaching is parameterized to reach a maximum rate,  $\iota_{cdom}$ , when PAR is above  $I_{cdom}$ , and linearly decrease at lower PAR. The sources and sinks of this CDOM-like tracer are therefore parameterized as:

$$S_{\text{CDOM}} = f_{\text{cdom}} S_{\text{DOM}_{\text{S}}} - \left[ \gamma_{\text{T}} d_{\text{cdom}} + \iota_{\text{cdom}} \min\left(\frac{\sum_{\lambda=400}^{\lambda=700} E_0(\lambda)}{I_{\text{cdom}}}, 1\right) \right] \text{CDOM}$$
(13)

where  $S_{\text{DOM}_S}$  is the sources of DOM (see Appendix A), and  $\gamma_T$  is the temperature function affecting biological rates.

15

$$a_{\rm cdom}(\lambda) = a_{\rm cdom}^{\rm CDOM}(\lambda) \rm CDOM$$
(14)

We parameterize  $a_{cdom}(\lambda)$  as function of "CDOM" such that:

and

$$a_{\rm cdom}^{\rm CDOM}(\lambda) = c_{\rm cdom}(\lambda_o) e^{(-s_{\rm cdom}(\lambda - \lambda_o))}$$
(15)

where  $a_{cdom}^{CDOM}(\lambda)$  is the concentration specific absorption of the CDOM-like tracer (Fig. 1c). The value for the spectral slope,  $s_{cdom}$  is taken from literature (Kitidis et al., 2006), and  $c_{cdom}(\lambda_o)$  is the CDOM specific absorption at reference waveband,  $\lambda_o$ . Although CDOM is also strongly linked to terrestrial matter, we do not provide any land sources at present. We discuss the sensitivity of the function and parameters, and compare to previous model parameterizations in Sect. 4.

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# 2.3.4 Phytoplankton

The absorption and scattering by phytoplankton is the net effect of each phytoplankton type resolved in our model, *j*:

$$a_{\rm phy}(\lambda) = \sum_{j} a_{\rm phy_{j}}^{\rm chl}(\lambda) {\rm Chl}_{j}$$
(16)

$${}_{5} \quad b_{\text{phy}}(\lambda) = \sum_{j} b_{\text{phy}_{j}}^{\text{C}}(\lambda) M_{\text{C}j} P_{j}$$
(17)

$$b_{\text{bphy}}(\lambda) = \sum_{j} b_{\text{bphy}_{j}}^{C}(\lambda) M_{Cj} P_{j}$$
(18)

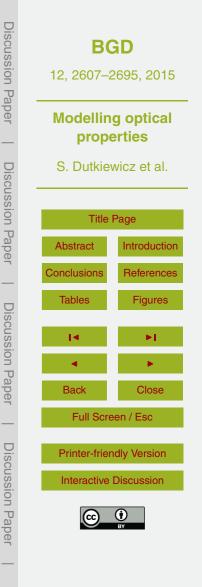
The Chl *a* specific absorption spectra  $a_{phy_j}^{chl}(\lambda)$  has units of m<sup>2</sup> (mgChl)<sup>-1</sup>, and the scattering  $(b_{phy_j}^{C}(\lambda))$  and backscattering  $(b_{bphy_j}^{C}(\lambda))$  are assumed to be function of phytoplankton biomass and has units m<sup>2</sup> (molC)<sup>-1</sup>. These spectra are specific to each of the phytoplankton types *j* (Fig. 1d–f) as taken from literature. See discussion in Sect. 2.5 and Appendix C.  $M_{Cj}$  is the C:P ratio in each phytoplankton type (see Appendix A).

#### 2.4 Phytoplankton growth

Phytoplankton growth is modelled as a function of temperature, irradiance, and nutrients as in Hickman et al. (2010) following Geider et al. (1998). The growth rate is equal to the carbon specific photosynthesis rate:

$$\mu_{j} = \mathsf{P}_{mj}^{\mathsf{C}} \left( 1 - \exp\left(\frac{-\Lambda_{Ej}\theta_{j}}{\mathsf{P}_{mj}^{\mathsf{C}}}\right) \right)$$

where  $P_{mj}^{C}$  is the light saturated photosynthesis rate that is a function of temperature and nutrient limitation (see Appendix A),  $\theta_j$  is the ratio of Chl *a* to C within each 2617



(19)

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(20)

phytoplankton *j* (discussed further below).  $\Lambda_{Ej}$  the scalar irradiance absorbed by each phytoplankton, *j* 

$$\Lambda_{Ej} = \phi_{\max_j} \sum_{\lambda=400}^{\lambda=700} a_{psj}^{chl}(\lambda) E_0(\lambda)$$

where  $\phi_{\max_j}$  is the maximum quantum yield, and  $a_{psj}^{chl}(\lambda)$  is the Chl *a* specific photosynthetic absorption spectra in each waveband  $\lambda$  (Fig. 1e), and  $E_0(\lambda)$  comes from the radiative transfer code (see Eq. 4).

Since some pigments are photo-protective, phytoplankton do not use all the light that they absorb for photosynthesis. Similar to Hickman et al. (2010) and Bisset et al. (1999) the total absorption spectra is therefore greater than the photosynthetic absorption spectra,  $a_{phyj}^{chl} > a_{psj}^{chl}$  (Fig. 1d, e). See discussion in Sect. 2.5. We also allow for photoinhibition, as in Hickman et al. (2010), such that  $P_{mj}^{C}$  reduces above a critical value at high light (see Appendix A).

#### 2.5 Plankton types

We resolve 9 phytoplankton "functional" types: these include analogues of diatoms, other large eukaryotes, coccolithophores, pico-eukaryotes, *Synechococcus*, high and low light *Prochlorococcus*, nitrogen fixing *Trichodesmium* and unicellular diazotrophs. These phytoplankton differ in their elemental composition (e.g. diatoms require silica), maximum growth rate, nutrient half saturation constants, sinking rates, maximum Chl *a* : C, and palatibility to grazers (see Tables 3 and 4).

<sup>20</sup> Cell size governs many traits. Smaller phytoplankton have lower nutrient half saturation constants and sink more slowly. The maximum growth rates are guided by observations; diatoms having the highest rates and *Prochlorococcus* having the lowest (see e.g. Irwin et al., 2006). The parameter values are within ranges found in the literature and previous ecosystem model (Dutkiewicz et al., 2012; Ward et al., 2013; Monteiro et al., 2010).

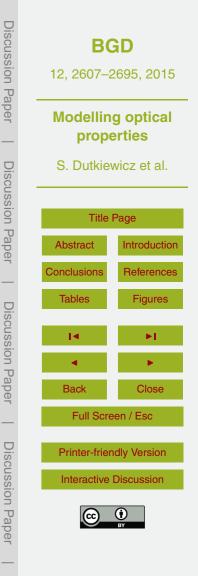
In this model we treat the phytoplankton light absorption and scattering explicitly (Sect. 2.3.4). The Chl *a* specific absorption spectra  $a_{phyj}^{chl}(\lambda)$  (units, m<sup>2</sup>mgChl<sup>-1</sup>) varies between species (Fig. 1d). These spectra were obtained from representative species in cultures grown at similar growth irradiance (see references in Appendix <sup>5</sup> C). The spectra capture differences in pigment composition and other taxon specific differences, including the "package effect" (Berner et al., 1989). For instance, the larger diatom has a flatter spectrum than the smaller phytoplankton (e.g. *Prochlorococcus*). Total light scattering spectra ( $b_{phyj}^{C}$ , Fig. 1f) were also obtained from representative species in culture, as were the backscatter to total scatter for each phytoplankton

 $b_{\text{bphyi}}^{\text{C}}$ , units m<sup>2</sup> mol C<sup>-1</sup>) (Stramski et al., 2001; Subramaniam et al., 1999).

Spectra for absorption by photosynthetic pigments  $(a_{psj}^{chl}, Fig. 1e)$  were derived using the pigment reconstruction technique (following Hickman et al., 2010; Babin et al., 1996). Light absorption spectra were reconstructed by scaling the weight-specific absorption coefficients for Chl *a*, Chl *b* and Chl *c*, photosynthetic carotenoids and non-<sup>15</sup> photosynthetic carotenoids, phycoeryththrobilin and phycourobilin-rich phycoerythrins (Bidigare et al., 1990b) to obtain the lowest sum of residuals between reconstructed and observed spectra.  $a_{psj}^{chl}$  was then calculated by adjusting the measured  $a_{phyj}^{chl}$  by the spectral ratio of the reconstructed spectra with and without non-photosynthetic pigments (Hickman et al., 2010).

<sup>20</sup> We parameterize all phytoplankton to have the same maximum quantum yield  $(\phi_{\max_j}, \text{ units mol C} \text{ fixed per moles photons})$  and all but diatoms to have the same maximum Chl *a*:C  $(\theta_{\max_j}, \text{ units mgChl}(\text{mmol C})^{-1})$  (MacIntyre et al., 2002). We parameterize low light *Prochlorococcus* as being photo-inhibited, as this is a distinct feature of the difference between high and low light strains (Moore and Chisholm, 1999; Hickman et al., 2010).

We resolve two zooplankton classes (large and small) that graze on the phytoplankton using a Holling III scheme (Holling, 1959). The large class preys preferentially on the diatoms, coccolithophores, and *Trichodesmium*, while the smaller



class preys preferentially on the smaller phytoplankton. We additionally parameterize diatoms and coccolithophores (hard shells) and *Trichodesmium* (toxicity) as having lower palatibility. Zooplankton grazing parameters are similar to those used in Prowe et al. (2012) which were determined from a mechanistic model of zooplankton feeding (see Table 6).

# 2.6 Simulation design

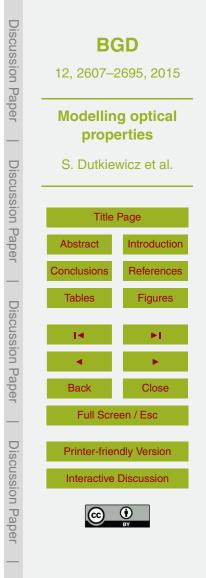
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We initialize the macronutrient fields (nitrate, phosphate and silicic acid) from World Ocean Atlas (Garcia et al., 2006) climatologies and the iron from previous model output. We also use previous model output to provide distribution of the ammonium, nitrite, dissolved and particulate matter. The total phytoplankton biomass is initialized from previous model output, divided equally between groups, except for the diazotrophs who are initialized at a much lower value so as not to flood the system with new nitrogen in the first few timesteps. Zooplankton are similarly initialized with equal distribution in both groups.

<sup>15</sup> We run the simulation forward for 10 years with a repeating generic "year" from the physical ECCO-GODAE products (Wunsch and Heimbach, 2007). Model results shown in this section are from the last year of the simulation. The phytoplankton establish a repeating pattern after about 3 years. A slow drift as deep water nutrient distributions adjust does not significantly change the results over the remaining time period.

## 20 3 Model results

We evaluate the model results against a range of in situ observations and satellite derived products. In particular we focus on the unique data set including biogeochemical, ecological and (some previously unpublished) optical properties that were obtained as part of the AMT-15 cruise.



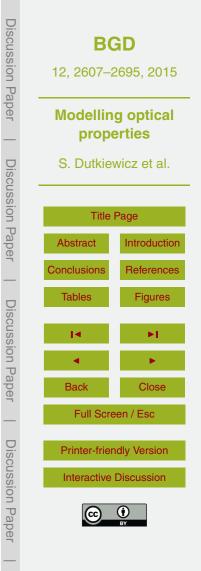
## 3.1 Atlantic meridional transect

The model broadly reproduces the horizontal gradients at the surface, but importantly also captures the deep ChI *a* maximum (Fig. 3a, b), and in particular its deepening in the subtropical gyres, especially in the South Atlantic. It does not capture the high ChI *a* 

- values in the North Africa upwelling zone since the coarse resolution model does not adequately represent the physics of these features. Model Chl *a* is too high just south of the equator, where the physical model captures an upwelling area that is not in the observations. The model also has a mixing event in October at about 35° S that mixes Chl *a* to depth, a feature not seen in the observations. The model captures the depth
  of the nitricline across the transect (Fig. 3c, d), especially the deep section (200 m) in
- the South Atlantic gyres. Again, as expected due the physical model issues, we do not capture the high nitrate supply in the North Africa upwelling zone, and nitrate is too high just south of the equator.

The model also captures observed variability of *a*<sub>cdom</sub> along the AMT-15 transect: low in the surface waters where CDOM is quickly bleached, and higher in deeper waters where CDOM accumulates. Values and regional patterns compare well between model and observations (Fig. 3e, f), except just south of the equator where Chl *a*, and nutrient supply are also too high (as discussed above). Absorption by phytoplankton (Fig. 3g) was only measured at the surface and the deep Chl *a* maximum. The model captures the higher value near the deep Chl *a* maximum (Fig. 3h).

We have used the AMT-15 measured downwelling irradiance and upwelling zenith radiance together with the inverse-modelling procedure of Gordon and Boynton (1997, 1998) to estimate the total absorption and total backscattering in several wavelengths (Fig. 4a, c, e, g). We discuss this inversion further in Appendix D. There is a large degree of uncertainty in this inversion process, and additional noisiness provides several spurious high/low values that are not realistic. Given this caveat, we find that the model qualitatively captures (Fig. 4b, d, f, h) the magnitudes and the pattern of higher absorption/lower scattering at the higher wavebands.



Since the model realistically captures much of the variability in optical constituents, it also accurately resolves the penetration of light through the water column (Fig. 5) as found in the AMT-15 data. We compare the depth of the 1 % light level: the depth where the downwelling irradiance in each waveband is 1 % of the surface value ( $E_{d_{-}}^{below}$  +

<sup>5</sup> E<sup>below</sup><sub>s<sub>o</sub></sub>). We find the shortest wavebands (e.g. purple line and symbols in Fig. 5) reach deepest in the South Atlantic gyre where concentrations of the optical constituents are lowest and less deep than medium wavebands (e.g. light and dark blue lines) in more equatorial regions. The penetration of blue wavebands leads to the the very deep Chl *a* maximum and draw down of nutrients at depth as observed in the AMT-15 transect and
 in the model. The 1 % depths are too deep in the North Atlantic upwelling region, since

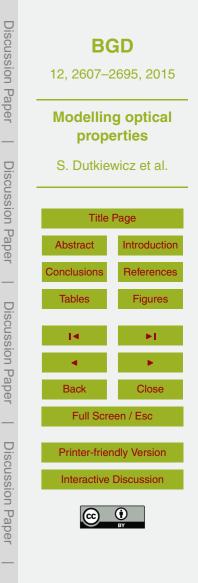
we do not capture this feature in the physics.

The model captures intricate patterns of absorption and scattering that develop from the interplay of different optical constituents and suggests the importance of treating each constituent separately for reproducing the in situ light field. We explore this further in Sect. 4.

3.2 Global results

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That the model captures much of the Chl *a*, nutrient and optical properties on basin scale and with depth as observed during the AMT-15 is very encouraging. The model also captures many of the global features (Fig. 6) in Chl *a* (derived from MODIS satellite), primary production (derived using Behrenfeld and Falkowski, 1997) as well as macronutrients (from the World Ocean Atlas, Garcia et al., 2006). The broad scale features of high nutrient, high Chl *a* and high productivity in the high latitudes and equatorial regions, and low nutrients, low Chl *a* in the subtropical gyres are resolved. We do not however capture coastal features as the physical model is too coarse to resolve the important mesoscale processes. This is also true in frontal zones (such as the Western boundary currents) where primary production is too low.



Relative to the composite of iron data (Taglibue et al., 2012), we also capture high iron in the Atlantic Ocean and lower iron over much of the Pacific (Fig. 6g, h). However, iron may be too low in the tropical South Pacific and Pacific equatorial regions. Here the model aeolian dust supply (based on Luo et al., 2008) may be too low, however the physical model also does not adequately resolve equatorial undercurrents which are likely responsible for supplying sedimentary iron to this region (Radic et al., 2011; Slemons et al., 2009). Since iron limitation is too strong in this region, productivity and Chl a are too low, and nitrate too high. The model also overestimates Chl a in the Southern Ocean relative to the satellite product. However, the satellite Chl a algorithm have have a factor of 2 range error (Campbell et al., 2002) and are especially problematic in the Southern Ocean (Szeto et al., 2011).

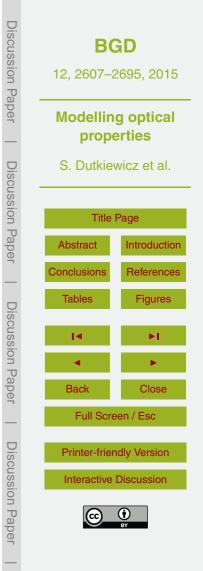
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We find that the spatial SD (between 0.85 and 1.15) and correlation (greater than 0.9) of the model vs. observed nutrients are encouraging (Fig. 7). Though we capture much of the spatial variability in the Chl a the correlations to satellite derived products

are not as good. The primary production is universally too low and too uniform relative 15 to the satellite derived product. However, we note that the satellite products of Chl a and primary production have large error margins associated with them that are not spatially homogeneous (Szeto et al., 2011).

The model ecosystem has distinctive seasonal cycles (Fig. 8) that mostly match the observed satellite derived and in situ Chl a at nine timeseries sites (locations 20 shown in Fig. 2) collected as part of JGOFS (Kleypas and Doney, 2001). In many locations the model overestimates the satellite derived peak of the bloom (consistent with annual mean Chl a being too high), but capture the non-bloom values more accurately. However, the in situ data broadly encompass the model values. We also

capture the satellite derived timing of the spring bloom, though notably miss the late 25 summer bloom in the northern Pacific (Station P), and instead have a spring bloom. At Kerfix (in the Southern Ocean) we also do not capture the bloom timing or magnitude. The spring bloom at NABE is too early relative to both in situ and satellite derived data.



It is likely that the model does not capture all the physical process occurring in these regions.

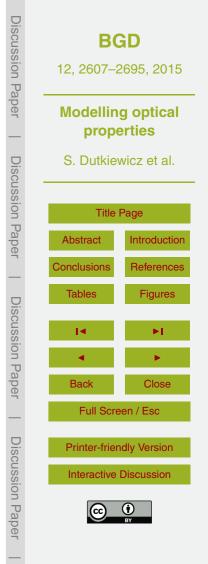
A unique feature of this model is reflectance output, which we have converted to remotely sensed reflectance ( $R_{\rm RS}$ ) using a fixed bidirectional function Q (see Sect. 2.2). <sup>5</sup> We compare this model output to MODIS remotely sensed reflectance,  $R_{\rm RS}(\lambda)$ . Despite the mismatch in wavelength and bandwidth and the oversimplification of a fixed Q, the model qualitatively captures the pattern of high reflectance in the subtropics relative to the higher productivity regions in low wavebands and the opposite pattern in higher wavebands. These initial results suggests that the model framework will be a useful laboratory for exploring satellite-like semi-analytical inversion algorithms (e.g. IOCCG report 5, 2006).

# 3.3 Phytoplankton biogeography

Eight of the 9 phytoplankton functional groups that we resolve have distinct biogeography (Fig. 10). This biogeography encompasses both horizontal and vertical patterns of phytoplankton biomass. The large eukaryote group does not survive in this model as it was given no specific trade off. It was large (low nutrient affinity) and had a low growth rate (typical of dinoflagellates).

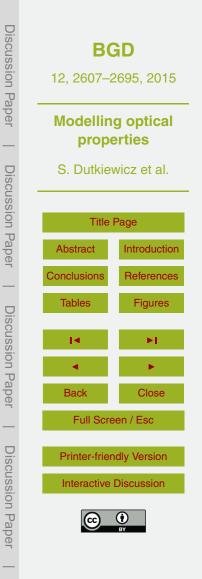
We compare simulated biomass of the pico-phytoplankton to observations from the AMT-15 (Fig. 11). AMT-15 cell counts were measured by analytical flow cytometry following methods of Heywood et al. (2006) and converted to biomass using constant factors (Zubkov et al., 1998) for comparison purposes. The smallest autotroph, *Prochlorococcus* has significant abundances through the subtropics and tropic that is largely captured by the model. The model *Prochlorococcus* dominate in the most oligotrophic regions (Dutkiewicz et al., 2009). In the 20 to 5° S region the model nutrient

source is too high and *Synechococcus*-analogues unrealistically dominate instead. This is also indicated by the Chl *a* and nitrate which is too high in this region (Fig. 3), discussed above. Other than this region, the model *Synechococcus* are only found in high concentration in African upwelling region and the northern poleward fringes of the



subtropics as is observed in the AMT-15 data. Pico-eukaryotes are more ubiquitous and are especially found in the deep Chl *a* maximum both in the observations and the model. Estimates of large phytoplankton biomass (e.g. diatoms, Coccolithophores) were not available from this cruise.

- The MAREDAT (MARine Ecosystem DATa, Buitenhuis et al., 2013) compilation provides a comprehensive, though still sparse, climatological distribution of several plankton functional groups. Here we re-grid the MAREDAT compilation onto a 5° grid with all observations between 0 and 50 m averaged together and compare this to the model output (Fig. 12). For the model results we sum the *Prochlorococcus*, *Synechococcus* and pico-eukaryote groups to compare to the observations of pico-
- and pico-eduaryote groups to compare to the observations of picophytoplankton. We find that the model captures the ubiquitous nature of the picophytoplankton (Fig. 12a, b). Lower values in the subtropical gyres are also captured by the model. The model tends to overestimate the coccolithophore biomass in general (Fig. 12c, d), but successfully reproduces the lack (or very low) values in subtropical
- <sup>15</sup> gyres and polar extent of the Southern Ocean. The model captures the observed high diatom values in the high latitudes and in the equatorial upwelling regions (Fig. 12e, f). Model diazotrophs peak too far south in the North Atlantic, but otherwise the lack (or very low) biomass in other regions of the global ocean is realistic relative to the MAREDAT compilation (Fig. 12g, h). We note that the regions with high model diagotroph peak performed by the deliver.
- diazotroph concentrations in the Indian and North Pacific are not covered by the Luo et al. (2013) data set, and there are observations (not included the in data set) of diazotrophs in the western South Pacific (Moisander et al., 2012). Though the MAREDAT compilation includes micro, meso and macro zooplankton, the former and the latter data are very sparse. Since we do not have direct analogues in the model,
- <sup>25</sup> we show here only the meso zooplankton biomass observations (Fig. 12i). The model captures the patterns of high and low values of zooplankton biomass, but at higher biomass since Fig. 12j includes all model grazers. However, we note that the model grazer population is too low in the subtropical gyres.



Given the sparsity of in situ measurements of phytoplankton types, it is natural to attempt to capture aspects of biogeography from space (IOCCG report 15, 2014; IOCCG report 9, 2009). Here we compare the model output to the PHYSAT product (Alvain et al., 2008) which empirically relates optical properties to specific (probably dominant) phytoplankton types (Fig. 13a, c) for January and July and compare to model dominant types (Fig. 13). In both model and PHYSAT we find that cyanobacteria dominate the tropics and subtropics. Diatoms play a substantial role in the summer biomass. PHYSAT also resolves Haptophytes (which includes coccolithophores) and *Phaeocystis*, while the model separates out instead pico eukaryotes and pico-eukaryotes as dominant in the mid-latitudes.

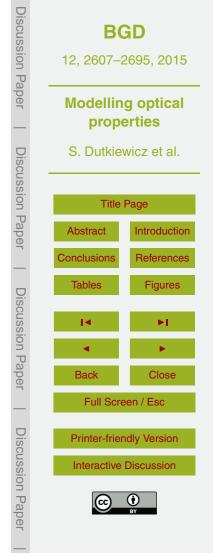
The model captures key patterns of observed optical and ecological properties. It provides a tool to explore aspects of the ocean biogeochemistry and ecosystem that are not possible with models that do not explicitly resolve radiative transfer, spectral irradiance, and an explicit resolution of the different water optical properties. In the next section we explore the role of the various water constituents on the irradiance spectrum

## 4 Sensitivity experiments: role of optical constituents

and how they impact biogeochemistry and ecosystem structures.

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The optical constituents play varying roles in their effect on irradiance attenuation (absorption and scattering). These roles differ between regions and depth (Figs. 14 and 15). Absorption by water molecules is most important at longer wavebands, but still has an impact at shorter wavebands (Fig. 14a, b, i, j). It is relatively more important in lower productive waters (e.g. South Atlantic gyre). Absorption by detrital matter plays a role, especially near the 1% depth in highly productive regions and at shorter
<sup>25</sup> wavebands (Fig. 14c, d, i, j). Absorption by phytoplankton plays a significant role where Chl *a* is highest (e.g. the deep Chl *a* maximum) at wavelengths less than 550 nm, and little role at longer wavelength (Fig. 14g, h, i, j, see also Fig. 1). Absorption by CDOM



at short wavebands is important in most regions, particularly where productivity is high where it is the dominant absorber. It also has, relative to other constituents, a large role at depth. At long wavebands CDOM plays very little role. Scattering by phytoplankton is relatively most important at shallower depths, while scattering by detrital matter is dominant deeper at all wavelengths (Fig. 15).

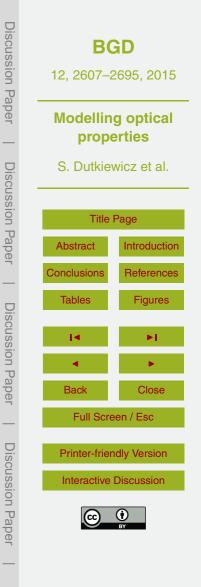
We perform a series of sensitivity experiments to explore the role of each constituent in setting the irradiance field in the ocean and on surface reflectance, and see how changes to these constituents feed back to the ecosystem and biogeochemistry. The range of values for these experiments are designed to cover and go be beyond the natural range of the absorption and scattering by the water constituents. We additionally explore how different assumptions and parameterizations for the optical constituents affects the simulation results.

## 4.1 Detrital matter

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We conduct several sensitivity studies to explore the relative importance of  $a_{det}$  and  $b_{det}$  (Fig. 16). We run each experiment from the same initial conditions as the "default" (EXP0) discussed in Sect. 3, and present results for the final year after 10 years of integration. We artificially alter  $a_{det}^{part}(\lambda)$  or  $b_{det}^{part}(\lambda)$  as noted below, such that  $a_{det}$  and  $b_{det}$  are manipulated. The experiments include the feedbacks to nutrients and productivity. In experiment EXP-D5 we explore a different parameterization for  $a_{det}(\lambda)$  that was used in Fujii et al. (2007).



1. EXP0: this is the default run where

$$a_{det}(\lambda) = a_{det}^{part}(\lambda) \frac{POC}{\rho_{part}}$$
$$b_{det}(\lambda) = b_{det}^{part}(\lambda) \frac{POC}{\rho_{part}}$$
$$b_{dbet}(\lambda) = b_{bdet}^{part}(\lambda) \frac{POC}{\rho_{part}}$$

5 2. EXP-D1: we set 
$$a_{det}^{part}(\lambda) = 0$$

3. EXP-D2: we set  $a_{det}^{part}(\lambda)$  artificially to four times the values used in EXP0

4. EXP-D3: we set 
$$b_{det}^{part}(\lambda) = 0$$

- 5. EXP-D4: we set  $b_{det}^{part}(\lambda)$  four times the value EXP0
- 6. EXP-D5: as in Fujji et al. (2007) we represent:

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$$a_{\text{det}}(\lambda) = a_{\text{det}}^{\text{POC}}(\lambda_o) \text{POC}e^{(-0.01(\lambda - \lambda_o))}$$

where  $a_{det}^{POC} = 0.1 \text{ m}^2 \text{ gC}^{-1}$  (Fujii et al., 2007) and  $\lambda_o = 450 \text{ nm}$ .

Removing the detrital absorption (EXP-D1) leads to bluer wavebands reaching to greater depth (Fig. 16a). This favours phytoplankton, at least in the subtropics, which absorb more efficiently in the blue part of the spectrum (i.e. *Prochlorococcus*, Fig. 16c). On the other hand, having stronger detrital absorption (EXP-D2) leads to shallower 1% light levels for the blue wavebands. The corresponding red-shifted light favours *Synechococcus* which absorb more efficiently in this part of the spectrum. With less irradiance absorbed in EXP-D1, we find a higher percentage is reflected at the shorter

wavebands (Fig. 16d). Similarly as more irradiance is absorbed (EXP-D2), there is a reduction in the reflectance.

We observe distinct biogeochemical feedbacks. With lower absorption by detritus (EXP-D1) the depth integrated phytoplankton biomass in the high latitudes increases

- <sup>5</sup> (Fig. 16b), leading to higher nutrient utilization in these locations. Thus the transport of nutrients to the lower latitudes is reduced (see e.g. Sarmiento et al., 2004; Dutkiewicz et al., 2005) reducing biomass in those locations. This will even further increase the 1% light depth for the blue wavebands and consequently favour *Prochlorococcus* more. The lower absorption by detritus therefore leads to expansion of the oligotrophic
- <sup>10</sup> subtropical gyres. Conversely, with more absorption (EXP-D2), we find lower depth integrated productivity in the high latitudes, higher nutrient supply to subtropics, reduced oligotrophic regions and stronger favouring of *Synechococcus*. This feedback between the light field and the biogeochemistry can only be captured by a fully threedimensional coupled ecosystem-radiative transfer model.
- <sup>15</sup> Alterations to the backscattering by detrital matter (EXP-D3 and EXP-D4) have little effect on the irradiance fields at depth (Fig. 16a) and thus little change to the community structure (Fig. 16c). However the changes to the reflectance is large (Fig. 16d).

In EXP0,  $a_{det}$  is calculated relative to number of detrital particles, whereas in EXP-D5 we parameterized it relative to particulate organic carbon (POC) concentrations (following Fujii et al., 2007). We find very similar patterns and magnitudes of  $a_{det}$ (450) using these two methods. Slight difference in magnitude can be attributed the values chosen for  $a_{det}^{POC}$  and  $p_{part}$  in the respective parameterizations. There is consequently little difference to biomass, phytoplankton distributions and reflectance between the two experiments.

# 25 4.2 Coloured dissolved organic matter

We conduct a series of sensitivity experiments that test assumptions about  $a_{cdom}$ . In two experiments (EXP-C1) and (EXP-C2) we assume no and significantly more absorption by CDOM respectively. In additional sensitivity experiments (EXP-C3, EXP-



C4, and EXP-C6 we explore the consequences of different parameterization of  $a_{cdom}$  as used in previous model studies (e.g. Greg and Casey, 2009; Mouw et al., 2012; Fujii et al., 2007; Hickman et al., 2010).

In all experiments  $a_{cdom}(\lambda)$  is an exponential function with wavelength:

5  $a_{cdom} = \chi_{cdom} e^{(-s_{cdom}(\lambda - \lambda_o))}$ 

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In the series of experiments we make different assumption on  $\chi_{cdom}$ :

1. EXP0:  $\chi_{cdom} = c_{cdom}(\lambda_o)CDOM$ 

This is our default experiment detailed in previous sections.

2. EXP0-C1: χ<sub>cdom</sub> = 0

This experiment artificially assumes that there is no  $a_{cdom}$ .

3. EXP-C2:  $\chi_{cdom} = 4 \cdot c_{cdom}(\lambda_o)$ CDOM

This experiment is the same as the default (EXP0), but with CDOM artificially able to absorb four times as much light in each waveband.

4. EXP-C3:  $\chi_{cdom} = c_{chl}(a_w(\lambda_o) + \sum_j a_{phyj}^{chl}(\lambda_o) Chl_j)$ 

Studies (e.g. Morel, 2009) have noted an empirical relationship between mean Chl *a* and  $a_{cdom}$ . But regionally there is a large variation in the ratio of Chl *a* and  $a_{cdom}$  (e.g. Kitidis et al., 2006; Morel et al., 2010). Here, as is done in Gregg and Casey (2007), we assume that  $a_{cdom}$  is a function of Chl *a*, and  $c_{chl} = 0.8$  (unitless) to match the magnitudes of EXP0.

5. EXP-C4:  $\chi_{cdom} = c_{cdom} f_{cdom}$ DOM Since CDOM is part of the DOM pool, a previous model-based study (Mouw et al., 2012) has assumed that some portion of the DOM pool ( $f_{cdom}$ ) is CDOM. Here we assume  $c_{dom} = 0.00508 \text{ m}^2 \text{ mg}^{-1}$  and  $f_{dom} = 0.0323$  following Bisset et al. (1999).

6. EXP-C5: 
$$\chi_{cdom} = 0.016 \text{ (m}^{-1}\text{)}$$
  
Other studies (e.g. Fujji et al., 2007; Hickman et al., 2010) have assumed 2630

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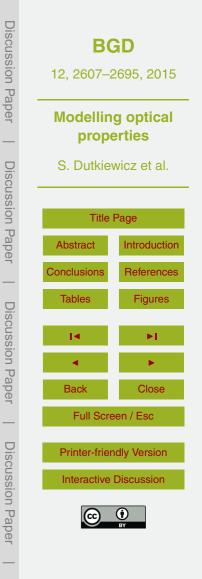
a uniform aCDOM at each wavelength. For specific regions of the ocean (e.g. clear subtropical water, Hickman et al., 2010) or for regional studies this may be appropriate. Here for comparison we use  $\chi_{cdom} = 0.016 \text{ (m}^{-1})$  as in Fujii et al. (2007).

<sup>5</sup> Community structure shifts significantly in response the the amount of irradiance that the CDOM absorbs (Fig. 17c). No CDOM absorption (EXP0-C1) favours bluer adapted *Prochlorococcus* and high absorption (EXP0-C2) leads to more *Synechococcus*. There is also similar impact on the biogeochemistry and shifting boundaries of the oligotrophic subtropical gyres as in the detrital experiments (Fig. 17b). The amount of absorption by
 <sup>10</sup> CDOM impacts the reflectance, again similar to the results seen with detrital absorption (Fig. 17d).

The three alternative parameterizations of  $\chi_{cdom}$  (EXP-C3, EXP-C4, and EXP-C5) lead to very different  $a_{cdom}$  fields (Fig. 17a). There are consequently shifts in the light fields and penetration depths of different wavebands, and corresponding regional shifts

- <sup>15</sup> in the community structure. In the parameterizations that either tie  $\chi_{cdom}$  to Chl *a* (EXP-C3) or to DOM (EXP-C4),  $a_{cdom}$  is almost non-existent below the 1 % light level, at odds with observations (Fig. 17). Above the 1 % light level the patterns of  $a_{cdom}$  are relatively realistic in these experiments, with higher  $a_{cdom}$  in productive regions and lower in less productive regions. However, there are significant differences to the default run
- <sup>20</sup> and community structure is altered (Fig. 17c). The uniform  $a_{cdom}$  simulation (EXP-C5) has a more uniform 1 % light depth along the transect, reflecting the importance of CDOM for spatial variability in the depth of the euphotic zone. Since alterations to  $a_{cdom}$  significantly affect the irradiance propagation, leading to changes in the upwelling, the impact of CDOM on the reflectance is important, and all experiments show a strong response (Fig. 17d).

These experiments illustrate that the parameterization of CDOM has very significant impact on community structure and reflectance, and suggests that it is crucial to explicitly include CDOM in models and that we learn more about its variability in the ocean (Morel et al., 2010; Nelson and Siegel, 2013).



## 4.3 Phytoplankton

Idealized experiments were also conducted to explore the sensitivity due to phytoplankton absorption and scattering (Fig. 18). We artificially manipulate  $a_{phyj}^{chl}(\lambda)$  and  $b_{phyj}^{C}$  affecting  $a_{phy}$  and  $b_{phy}$ .

- EXP0: this is the default run with each phytoplankton type has a specific absorption and scattering spectra (Fig. 1d, e, f).
  - 2. EXP-P1: we artificially set  $a_{phyj}^{chl}(\lambda) = 0$  for irradiance attenuation process, but still assume that phytoplankton growth depends on light as in EXP0. This is a highly hypothetical experiment.
- 3. EXP-P2: we artificially set  $a_{phyj}^{chl}(\lambda)$  to four times that of EXP0 for irradiance attenuation process, but still assume that phytoplankton growth depends on light as in EXP0. This is therefore also a highly hypothetical experiment.
  - 4. EXP-P3: we set  $b_{phyj}^{C} = 0$ .

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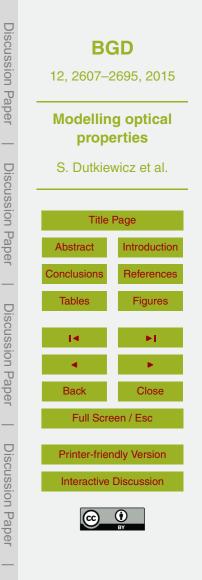
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- 5. EXP-P4: we assume all phytoplankton have the same absorption properties (the mean, black lines, in Fig. 1d, e) for both  $a_{phyi}^{chl}(\lambda)$  and  $a_{psi}^{chl}(\lambda)$ .
- 6. EXP-P5: we assume all phytoplankton types have the same scattering and backscattering properties (the mean, black line, in Fig. 1f).

Altering the absorption by phytoplankton (EXP-P1 and EXP-P2) has similar impact as altering CDOM or detritus (Fig. 18). There are similar changes to the irradiance field, community structure, and reflectance with consequent feedbacks to the biogeochemsitry.

When we assume no scattering by phytoplankton (EXP-P3) there is almost no change in community structure, but some (though small) change to reflectance compared to the default run (EXP0). An experiment with four times  $b_{phy}$  has similar results (not shown here).



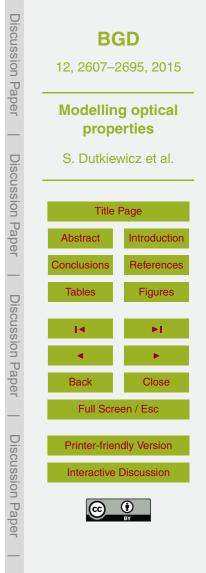
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In EXP-P4 and EXP-P5 we explore the importance of the phytoplankton type specific absorption and scattering spectra in setting their biogeography and biogeochemical consequences. Total  $a_{phy}$ , the irradiance field and light penetration depths of each waveband are altered when we assume a mean absorption for all phytoplankton (EXP-

- P4). Total a<sub>phy</sub> is generally increased in the high latitudes and decreases at low latitudes (Fig. 18a). This occurs because diatoms (which dominate the high latitudes) have lower absorption per unit Chl *a* than the mean spectra (see Fig. 1e), and pico-phytoplankton (that dominate the lower latitudes) have a higher absorption than the mean. Community structure is also altered (Fig. 18c) showing that the photosynthetetic absorption specific
- to each type is important for the emergent biogeography. In particular, coccolithophores have a spectra that absorbs well in the blue-green light. Once this advantage is removed diatoms take over their domain. Changes to reflectance also occur as a direct result (Fig. 18d).
- When assuming a mean scattering spectra for all phytoplankton (EXP-P5) we find almost no difference to the irradiance field, community or biogeography. There are, however, small changes to the reflectance. Changes in the reflectance are also apparent when the mean  $a_{phy}$  was used (EXP-P4).

#### 5 Discussion

In this paper we have presented a version of the MIT biogeochemistry-ecosystem
 model (the "Darwin Project" model) which now incorporates radiative transfer, spectrally resolved irradiance, and explicit representation of optically important water constituents. Our treatment of optical properties combines many features from prior studies (e.g. Gregg et al., 2007; Fujji et al., 2007; Mobley, 2011; Bissett et al., 1999, 2004), but is more comprehensive than most. In particular we include a detailed absorption by several different types of phytoplankton as in Gregg and Casey (2007), explicitly resolve a CDOM like tracer as in Xiu and Chai (2014) and Bisset et al. (1999), and also resolve detrital particulate matter similar to Fujii et al. (2007).

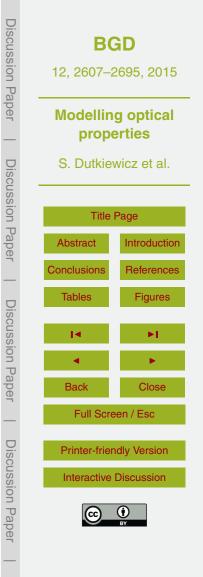


We have evaluated our model against a range of in situ observations and satellite derived products. The model captures the large scale biogeochemical, ecosystem and optical characteristics as suggested by these datasets. In particular we have used a unique dataset collected during AMT-15 which includes concurrent optical, biogeochemical and ecosystem measurements. The model captures the observed basin scale and vertical distribution. In many of the instances where the model does not compare well to the observations, we find that the physics of the model is at least partly responsible.

The model captures spatial light absorption by different optical constituents, and the relative magnitude of the scattering. However, the scattering, particularly by detrital particles, remains the least well constrained aspect. At the moment, we neglect variations in detrital particle size distributions. We resolve the main optically important water constituents, but still neglect minerals (e.g. Stramski et al., 2001) and particulate inorganic carbon (e.g. Balch and Itgoff, 2009) that may also be important.

Each of the optical constituents resolved in the model (water, CDOM, detrital particles and phytoplankton) have an important role in attenuating irradiance through the water column: but the relative importance differs between region, with depth, and with wavelength (Fig. 14). CDOM was relatively more important to light absorption in high productive regions, phytoplankton were important at the deep Chl *a* maximum and absorption by water was most important in the clear oligotrophic waters.

Our sensitivity experiments suggest that models that neglect the explicit and independently varying absorption by detrital particulate matter and CDOM are missing important components that have implications for the biogeochemistry and productivity of the model. For instance we find that the magnitude of the light absorption of any of the water constituents that we resolve is important in setting the penetration of irradiance in different wavebands. Changes to the irradiance spectrum will have important ramification for the community structure. Lower absorption by the optical constituents leads to deeper penetration of blue light and favours phytoplankton which absorb better in the shorter wavelengths (e.g. *Prochlorococcus*). However, the



penetration of light also has a large impact on the biogeochemistry and biogeography on global scales. In the sensitivity studies with less light absorption, there was more primary production at the higher latitudes, and reduced nutrients transport to the lower latitudes. Thus changes in absorption could impact the size of the oligotrophic regions, which in turn impacted the community structure.

An important product of the model is the surface reflectance that provides a more direct comparison to satellite data than derived products such as Chl *a* or primary production. These derived products rely on empirical algorithms to convert from more direct measurement of ocean colour (e.g. reflectance) which introduce a large degree of uncertainty to the output (see e.g. Campbell et al., 2002; Carr et al., 2006). Thus directly relating model output to satellite reflectance has exciting promise.

The absorption by any of the optical constituents strongly determines the amount of upwelling irradiance and consequently the surface reflectance. In particular, we found that the regional variations in CDOM are important in setting the patterns of reflectance

(see EXP-C5). Though alterations to scattering appears to have little effect on the inwater optical fields, they have significant impact on the surface reflectance fields. Even slight changes to the scattering by phytoplankton (see EXP-P5) has an effect on the reflectance. Such changes are important when attempting to retrieve information on the community structure from ocean colour satellite products (e.g. IOCCG report 15, 20 2014).

## 6 Conclusions

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The amount and type of irradiance that penetrates through the water column is an important issue when studying phytoplankton productivity and community structure. And yet, ocean models routinely offer very crude parameterizations of light attenuation and neglect the spectral quality. We have improved the MITgcm ecosystem and biogeochemistry model by incorporating spectral light, explicit radiative transfer and representations of several optical constituents. The model performed well when



compared to observations. The model provides a useful platform to explore the relative importance of different optical constituents for biogeography, biogeochemistry and optical properties such as those measured by satellite.

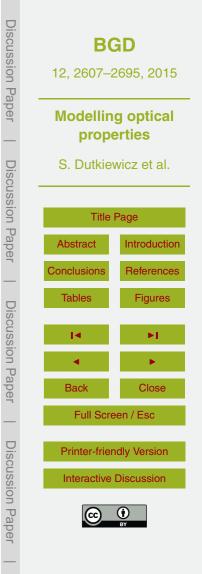
- The sensitivity studies were intentionally hypothetical to provide a wide range of responses. They provide evidence that capturing how each of the optical constituents absorbs and scatters irradiance has important ramifications for biogeochemistry and the phytoplankton community structure. This feedback between the light field and the biogeochemistry can only be captured by a fully three-dimensional coupled ecosystemradiative transfer model.
- <sup>10</sup> We believe that this model will useful in examining the role of the irradiance spectrum and pigments in setting biogeography (Hickman et al., 2015), how changes in irradiance and/or optical constituents will impact the future oceans, and in providing a laboratory to explore the use of water leaving radiance as a marker of changes in the ecosystem.

# 15 Appendix A: Ecosystem and biogeochemical model equations

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The model equations are based on those of Follows et al. (2007), Dutkiewicz et al. (2009, 2012), and Hickman et al. (2010). We consider the cycling of phosphorus, nitrogen, silica, iron as well as carbon, alkalinity, and dissolved oxygen (the latter three following Ullman et al., 2009). We also resolve here explicit dynamic Chl *a* (following Geider et al., 1998) and a tracer that mimics coloured dissolved organic matter (CDOM). We provide a complete set of the equations here.

Several nutrients  $N_i$  nourish many phytoplankton types  $P_j$  which are grazed by several zooplankton types  $Z_k$ . Mortality of and excretion from plankton, and sloppy feeding by zooplankton contribute to a dissolved organic matter DOM<sub>i</sub> pool and a sinking particulate organic matter pool POM<sub>j</sub>. Subscript *i* refers to a nutrient/element, *j* for a specific phytoplankton type, and *k* for a zooplankton type. Here *i* = PO<sub>4</sub>, inorganic fixed nitrogen (includes NO<sub>3</sub>, NO<sub>2</sub>, NH<sub>4</sub>), Fe, Si and C. Particulate inorganic



carbon (PIC), Alkalinity (A) and dissolved oxygen ( $O_2$ ) are also included in this framework. All tracers, X are advected and diffused by the three-dimensional flow fields:

$$\frac{\partial X}{\partial t} = -\nabla \cdot (\mathbf{u}X) + \nabla \cdot (\mathbf{K}\nabla X) + S_X$$

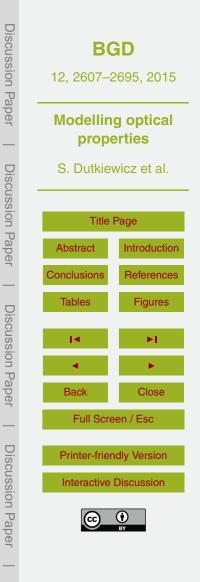
5 where

 $\mathbf{u} = (u, v, w)$ , velocity in physical model,

K are the mixing coefficients used in physical model,

 $S_X$  are sources and sinks of tracer X.

The source and sinks of each tracer,  $S_{\chi}$ , are different and including biological transformations, chemical reactions and external sources and sinks. Phytoplankton are assumed to have fixed elemental ratios following Redfield (1934). The base currency of the plankton equations is phosphorus.



(A1)

Nutrients:

$$\begin{split} S_{\text{PO}_4} &= -\sum_{j} [\mu_j P_j] + r_{\text{dop}} \gamma_{\text{T}} \text{DOP} \\ S_{\text{Si}} &= -\sum_{j} [\mu_j P_j \mathbf{M}_{\text{Si}_j}] + r_{\text{dosi}} \gamma_{\text{T}} \text{POSi} \\ S_{\text{FeT}} &= -\sum_{j} [\mu_j P_j \mathbf{M}_{\text{FeT}_j}] + r_{\text{dofe}} \gamma_{\text{T}} \text{DOFe} - c_{\text{scav}} \text{Fe}' + F_{\text{atmos}} + F_{\text{sed}} \end{split}$$

<sup>5</sup> 
$$S_{NO_3} = -\sum_j [\mu_j P_j \mathbf{M}_{IN_j} \Gamma_{no3_j}] + \zeta_{no3} NO_2 - (1 - H_{ocrit}) \frac{R_{dno3}}{R_{denit}} D_{denit}$$

$$S_{\text{NO}_2} = -\sum_j [\mu_j P_j \mathbf{M}_{\text{IN}_j} \Gamma_{\text{no}2_j}] + \zeta_{\text{no}2} \text{NH}_4 - \zeta_{\text{no}3} \text{NO}_2$$
(A6)

$$S_{\mathsf{NH}_4} = -\sum_{j} \left[ \mu_j P_j \mathbf{M}_{\mathsf{IN}_j} \Gamma_{\mathsf{nh4}_j} \right] + r_{\mathsf{don}} \gamma_{\mathsf{T}} \mathsf{DON}$$
(A7)

$$S_{\rm C} = -\sum_{j} [\mu_j P_j \mathbf{M}_{\rm C_j}] - \sum_{j} [\mu_j P_j R_{\rm rj}] + r_{\rm doc} \gamma_{\rm T} \text{DOC} + d_{\rm pic} \text{PIC} + F_{\rm C} + D_{\rm C}$$

Plankton:

<sup>10</sup> 
$$S_{P_j} = \mu_j P_j - m_{pj} \gamma_T P_j - \sum_k [g_{jk} Z_{k,i=1}] - \frac{\partial (w_{pj} P_j)}{\partial z}$$
 (A9)

$$S_{Z_{ki}} = Z_{ki} \sum_{j} [\zeta_{jk} g_{jk} \mathbf{M}_{ij}] - m_{zk} \gamma_{\mathsf{T}} Z_{ki} - m_{z2k} \gamma_{\mathsf{T}} Z_{ki}^2$$
(A10)

Chlorophyll a:

$$S_{\text{Chl}_{j}} = \mathbf{M}_{\text{C}j} \left( \rho_{j} \mu_{j} P_{j} - \theta_{j} m_{\text{p}j} \gamma_{\text{T}} P_{j} - \theta_{j} \sum_{k} [g_{jk} Z_{k,i=1}] - \frac{\partial(w_{\text{p}j} \text{Chl}_{j})}{\partial z} \right) + t_{\text{chl}} (\theta_{oj} - \mathbf{M}_{\text{C}j} \theta_{j} P_{j})$$

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(A2)

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(A5)

(A8)

(A11)

Particulate and dissolved matter:

10

$$S_{\text{POM}_{i}} = -\gamma_{\text{T}} r_{\text{pom}_{i}} \text{POM}_{i} - \frac{\partial (w_{\text{pom}_{i}} \text{POM}_{i})}{\partial z} + \sum_{j} [(1 - \varphi_{\text{mp}_{ij}}) m_{\text{p}j} P_{j} \mathbf{M}_{ij}]$$
  
+ 
$$\sum_{k} \sum_{j} [(1 - \varphi_{\text{mz}_{ik}}) \left( m_{zk} Z_{ik} + m_{z2k} Z_{ik}^{2} \right) ]$$
  
+ 
$$\sum_{k} \sum_{j} [(1 - \varphi_{g_{ijk}}) (1 - \zeta_{jk}) g_{ij} \mathbf{M}_{ij} Z_{k}]$$
(A12)

$$S_{\text{DOM}_{i}} = -\gamma_{\text{T}} r_{\text{dom}_{i}} \text{DOM}_{i} + (1 - f_{\text{cdom}}) \gamma_{\text{T}} r_{\text{pom}_{i}} \text{POM}_{i} + \sum_{j} [\varphi_{\text{mp}_{ij}} m_{\text{p}j} P_{j} \mathbf{M}_{ij}]$$

$$+\sum_{k} \left[ \varphi_{\mathrm{m}z_{ik}} \left( m_{zk} Z_{\mathrm{ik}} + m_{z2k} Z_{\mathrm{ik}}^{2} \right) \right] + \sum_{k} \sum_{j} \left[ \varphi_{\mathrm{g}_{ijk}} (1 - \zeta_{jk}) g_{ij} \mathbf{M}_{ij} Z_{\mathrm{ki}} \right]$$
$$+ \gamma_{\mathrm{T}} C \mathrm{DOM}_{i} \left[ d_{\mathrm{cdom}} + \iota_{\mathrm{cdom}} \mathrm{min} \left( \frac{\sum_{\lambda=400}^{\lambda=700} E_{0}(\lambda)}{I_{\mathrm{cdom}}}, 1 \right) \right]$$
(A13)

$$S_{CDOM_{i}} = f_{cdom} \left( \gamma_{T} r_{pom_{i}} POM_{i} + \sum_{j} [\varphi_{mp_{ij}} m_{pj} P_{j} \mathbf{M}_{ij}] + \sum_{k} \left[ \varphi_{mz_{ik}} \left( m_{zk} Z_{ki} + m_{z2k} Z_{ki}^{2} \right) \right] \right)$$

$$+\sum_{k}\sum_{j} \left[\varphi_{g_{ijk}}(1-\zeta_{jk})g_{ij}\mathbf{M}_{ij}Z_{ki}\right] \right)$$
$$-\gamma_{\mathrm{T}}C\mathrm{DOM}_{i}\left[d_{\mathrm{cdom}}+\iota_{\mathrm{cdom}}\min\left(\frac{\sum_{\lambda=400}^{\lambda=700}E_{0}(\lambda)}{I_{\mathrm{cdom}}},1\right)\right]$$
(A14)

$$S_{\text{PIC}} = -d_{\text{pic}}\text{PIC} - \frac{\partial(w_{\text{pic}}\text{PIC})}{\partial z} \sum_{j} [m_{\text{p}j}P_{j}R_{rj}] + \sum_{k} \sum_{j} [g_{ij}R_{rj}Z_{ki}]$$
(A15)

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Alkalinity:

$$S_{\mathsf{A}} = \sum_{j} [\mu_{j} P_{j} \mathbf{M}_{\mathsf{NO}_{3}j}] - S_{\mathsf{NO}_{3}} - 2\left(\sum_{j} [\mu_{j} P_{j} R_{\mathsf{r}j}] + d_{\mathsf{pic}} \mathsf{PIC}\right) + D_{\mathsf{A}}$$

Dissolved oxygen:

$$S_{O_2} = F_{O_2} + \mathbf{M}_{O_j} \sum_j \mu_j P_j - H_{\text{ocrit}} M_{O_j} \gamma_{\mathsf{T}} r_{\text{dom}_j} \text{DOM}_j$$
(A17)

5 where:

 $\mu_i$  is the growth rate of phytoplankton *j* (function provided below),  $\mathbf{M}_{ii}$  is the matrix of ratios of element *i* to phosphorus for phytoplankton *j* r<sub>dom</sub>, is remineralization rate of DOM for element *i*, here P, Fe, N, C r<sub>pom</sub> is degradation/remineralization rate of POM for element *i*, here P, Si, Fe, N, C  $d_{cdom}$  is degradation rate of CDOM to DOM for element *i*, here P, Fe, N, C  $\gamma_{\rm T}$  is temperature regulation of biological rates (function provided below),  $c_{\rm scav}$  is scavenging rate for free iron (function provided below), Fe' is free iron (description provided below),  $F_{\text{atmos}}$  is atmospheric deposition of iron dust on surface of model ocean,  $F_{sed}$  is the sedimentary source of iron (function provided below),  $\zeta_{no3}$  is oxidation rate of NO<sub>2</sub> to NO<sub>3</sub> (function provided below),  $\zeta_{no2}$  is oxidation rate of NH<sub>4</sub> to NO<sub>2</sub> (function provided below),  $\Gamma_{no3}$ , is fraction inorganic nitrogen uptake from nitrate (function provided below),  $\Gamma_{no2_i}$  is fraction inorganic nitrogen uptake from nitrite (function provided below),  $\Gamma_{nh4_i}$  is fraction inorganic nitrogen uptake from ammonium (function provided below),  $H_{\text{ocrit}} = 1$  if  $O > O_{\text{crit}}$  and 0 if  $O = < O_{\text{crit}}$ , O<sub>crit</sub> is critical oxygen level for denitrification,  $R_{\text{denit}}$  is N : P ratio in denitrification,  $R_{dpo3}$  is ratio of NO<sub>3</sub> relative to all N in denitrification, 2640

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(A16)

- $D_{\text{denit}}$  is denitrification rate (function provided below),
- $R_{rj}$  is ratio of inorganic carbon to organic phosphorus produced by phytoplankton *j*,
- $F_{\rm C}$  is air-sea flux of carbon dioxide (function provided below),
- $D_{\rm C}$  is dilution/concentration of carbon by addition/loss freshwater,
- 5 D<sub>A</sub> is dilution/concentration of alkalinity by addition/loss freshwater,
  - $F_{O_2}$  is air-sea flux of oxygen (function provided below),
  - $d_{\rm pic}$  is dissolution rate of PIC,
  - $m_{pj}$  is mortality/excretion rate for phytoplankton *j*,
  - $m_{zk}$  is mortality/excretion rate for zooplankton k,
- <sup>10</sup>  $m_{z2k}$  is quadratic mortality for zooplankton k,
  - $g_{jk}$  is grazing of zooplankton k on phytoplankton j (function provided below),
  - $\zeta_{ik}$  is grazing efficiency of zooplankton k on phytoplankton j (function provided below),
  - $\dot{w}_{pj}$  is sinking rate for phytoplankton *j*,
  - $w_{\text{pom}_i}$  is sinking rate for POM *i*,
- $_{15}$   $\dot{W}_{\rm pic}$  is sinking rate for PIC,
  - $\rho_i$  is Chl *a* : C of new growth (function provided below),
  - $\hat{\theta_i}$  is local Chl *a* : C ratio,
  - $\theta_{oi}$  is acclimated Chl *a* : C (function provided below),
  - $t_{chl}$  is acclimation timescale for Chl *a*,
- <sup>20</sup>  $\varphi_{mp_{ij}}$  is fraction of dead/respired phytoplankton organic matter that goes to DOM<sub>i</sub>,  $\varphi_{mz_{ik}}$  is fraction of dead/respired zooplankton organic matter that goes to DOM<sub>i</sub>,  $\varphi_{g_{ijk}}$  is fraction of sloppy grazing that goes to DOM<sub>i</sub>,  $f_{cdom}$  is fraction of DOM produced that enters CDOM pool,  $l_{cdom}$  is bleaching rate for CDOM,
- <sup>25</sup>  $\sum_{\lambda=400}^{\lambda=700} E_0(\lambda)$  is local total scale irradiance,  $I_{cdom}$  is PAR above which CDOM bleaches.

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# A1 Temperature regulation of biological rates

Biological rates (plankton growth and the parameterization of remineralization of organic matter) are represented as a function of temperature, following the Arrenhius equation (Kooijman, 2000), similar to Eppley (1972):

$${}_{5} \quad \gamma_{\rm T} = -\frac{1}{\tau_1} e^{\left(A_E \left(\frac{1}{T+273.15} - \frac{1}{T_0}\right)\right)} \tag{A18}$$

#### where

 $\tau_1$  is coefficient to normalize the maximum value,

 $A_E$ ,  $T_o$  regulate the form of the temperature modification function,

T is the local model ocean temperature.

# 10 A2 Phytoplankton growth

Phytoplankton growth is a function of temperature, irradiance, and nutrients. We follow Hickman et al. (2010), which in turn follows Geider et al. (1998), such that the growth rate is equal to the carbon specific photosynthesis rate:

$$\mathsf{P}_{j}^{\mathsf{C}} = \mathsf{P}_{mj}^{\mathsf{C}} \left( 1 - e^{\left(\frac{-\Lambda_{Ej}\theta_{j}}{p_{mj}^{\mathsf{C}}}\right)} \right)$$

15 where

 $P_{mj}^{C}$  is light saturated photosynthesis rate (see function below),  $\Lambda_{Ej}$  is light absorbed by each phytoplankton (see function below),  $\theta_{j}$  is Chl *a* : C for each phytoplankton (see function below).

<sup>20</sup> The light saturated photosynthesis rate is a function of nutrients and temperatures:

 $\mathsf{P}_{mj}^\mathsf{C} = \mathsf{P}_{m_{\max_j}}^\mathsf{C} \gamma_\mathsf{T} \gamma_{\mathsf{N}j}$ 

where:

 $P_{m_{\max_i}}^{C}$  is maximum photosynthesis rate of phytoplankton *j*,

 $\gamma_{\rm T}$  is modification of growth rate by temperature (see above)

 $\gamma_{Nj}$  is modification of growth rate by nutrients for phytoplankton *j* (see function below).

5

The light absorbed by each phytoplankton, j is

$$\Lambda_{Ej} = \phi_{\max_j} \sum_{\lambda=400}^{\lambda=700} a_{psj}^{chl}(\lambda) E_0(\lambda)$$

#### where:

 $\phi_{\max_i}$  is the maximum quantum yield

<sup>10</sup>  $a_{psj}^{chl}(\lambda)$  is the Chl *a* specific photosynthetic absorption spectra in each waveband  $\lambda$ . The local Chl *a* : C ratio  $\theta_j$  is:

$$\theta_j = \frac{\mathrm{Chl}_j}{P_j \mathbf{M}_{\mathrm{C}j}} \tag{A22}$$

The increase of Chl *a* due to growth term  $(\mathbf{M}_{C_j}\rho_j\mu_jP_j)$  in Eq. (A11) follows Geider et al. (1998), with:

$$\rho_{j} = \theta_{\max j} \frac{\mathsf{P}_{j}^{\mathsf{C}}}{\Lambda_{Ej} \theta_{oj}}$$

and the acclimated Chl a: C follows Geider et al. (1997):

$$\theta_{oj} = \frac{\theta_{\max j}}{1 + \frac{\Lambda_{Ej}\theta_{\max j}}{2\mathsf{P}_{mj}^{C}}}$$



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where  $\theta_{\max i}$  is maximum Chl *a* : C ratio each phytoplankton can reach.

Phytoplankton can be photo-inhibited (following Hickman et al., 2010), such that  $P_j^C$  reduces to  $P_{inhib_i}^C$  above  $E_{kj}$ :

$$\mathsf{P}_{\mathsf{inhib}_{j}}^{\mathsf{C}} = \mathsf{P}_{j}^{\mathsf{C}} \kappa_{\mathsf{inhib}} \frac{E_{kj}}{\sum_{\lambda=400}^{\lambda=700} E_{0}(\lambda)}$$
(A25)

<sup>5</sup> where  $\kappa_{\text{inhib}}$  is the inhibition coefficient and  $E_{ki}$  is the light saturation parameter.

$$E_{kj} = \frac{P_{mj}^{\rm C}}{\theta_j \overline{a_{\rm psj}^{\rm chl}(\lambda)}}$$
(A26)

where  $a_{psj}^{chl}(\lambda)$  is the mean light absorption by photosynthetic pigments between 400 and 700 nm.

Nutrient limitation is determined by the most limiting nutrient:

15

10 
$$\gamma_{Nj} = \min(N_{\lim j_j})$$

Limitation by  $PO_4$ , Si, Fe are all parameterized following the Michaelis–Menton formulation:

$$N_{\lim j_i} = \frac{N_i}{N_i + \kappa_{N_{ij}}}$$
(A28)

where  $\kappa_{N_{ij}}$  is the half saturation constant of nutrient *i* = PO<sub>4</sub>, Si, Fe, for phytoplankton *j*.

Nitrogen is available in three forms of which ammonia is the preferred type:

$$N_{\text{Nlim}j} = \frac{\text{NO}_3 + \text{NO}_2}{\text{NO}_3 + \text{NO}_2 + \kappa_{\text{in}_j}} e^{-\psi \text{NH}_4} + \frac{\text{NH}_4}{\text{NH}_4 + \kappa_{\text{nh}_j}} \frac{2644}{2644}$$

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where:

 $\kappa_{in_j}$  is the half saturation constant of IN = NO<sub>3</sub> + NO<sub>2</sub>,  $\kappa_{nh4_j}$  is the half saturation constant of NH<sub>4</sub>,  $\psi$  reflects the fixed nitrogen uptake inhibition by ammonia.

## **5 A3 Zooplankton parameterization**

Zooplankton grazing is parameterized as:

$$g_{jk} = g_{\max_{jk}} \gamma_{\mathsf{T}} \frac{\eta_{jk} P_j}{G_k} \frac{G_k^n}{G_k^n + \kappa_{pk}^n}$$

where

 $g_{\max_{ik}}$  is maximum grazing rate of zooplankton k on phytoplankton j,

 $\eta_{jk}$  is palatibility of plankton j to zooplankton k,

 $\vec{G}_k$  is palatibility (for zooplankton k) weighted total phytoplankton concentration, equal to  $\sum_i [\eta_{ik} P_i]$ 

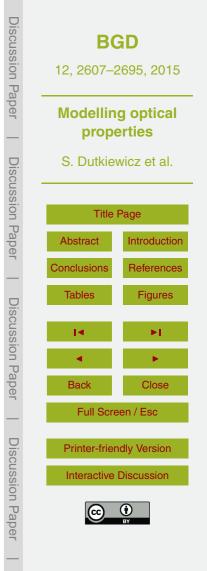
 $\kappa_{\rho k}$  is half-saturation constant for grazing of zooplankton k,

*n* is exponent for Holling Type II or III (n = 1 or 2), in this study n = 2.

The maximum grazing  $g_{\max_{jk}}$  depends of the relative size of the phytoplankton *j* and zooplankton *k*, with a faster rate if they are both small or both big ( $g_{\max_a}$ ), and slower if they are in different size classes ( $g_{\max_b}$ ).

Zooplankton are assumed to have both a linear and quadratic loss term. The linear term represents mortality, the quadratic loss terms represents grazing by higher trophic

<sup>20</sup> levels (Steele and Henderson, 1992) that are not explicitly resolved in this model.



(A30)

## A4 Nitrogen cycle

Phytoplankton take up DIN in three forms (NH<sub>4</sub>, NO<sub>2</sub> and NO<sub>3</sub>). To separate out how much comes from each source we have the functions  $\Gamma$  in Eqs. (A5)–(A7):

$$\Gamma_{no3_{j}} = \frac{\frac{NO_{3}}{NO_{3} + NO_{2} + \kappa_{in_{j}}}e^{-\psi NH_{4}}}{N_{Nim_{j}}}$$
(A31)  

$$\Gamma_{no2_{j}} = \frac{\frac{NO_{2}}{NO_{3} + NO_{2} + \kappa_{in_{j}}}e^{-\psi NH_{4}}}{N_{Nim_{j}}}$$
(A32)  

$$\Gamma_{nh4_{j}} = \frac{\frac{NH_{4}}{NH_{4} + \kappa_{nh4_{j}}}}{N_{Nim_{j}}}$$
(A33)

The oxidation of  $NH_4$  to  $NO_2$  and  $NO_2$  to  $NO_3$  are parameterized as a function of the total scalar irradiance:

$$\zeta_{no3} = \zeta_{ono3} \left( 1 - \frac{\sum_{\lambda=400}^{\lambda=700} E_0(\lambda)}{I_0} \right)$$
(A34)  
$$\zeta_{no2} = \zeta_{ono2} \left( 1 - \frac{\sum_{\lambda=400}^{\lambda=700} E_0(\lambda)}{I_0} \right)$$
(A35)

where  $\zeta_{ono3}$  and  $\zeta_{ono2}$  are maximum rates, and  $I_0$  is critical light level below which oxidation occurs.

Denitrification occurs when  $O < O_{crit}$  in which case  $O_2$  is not used during remineralization, but instead NO<sub>3</sub> is used such that:

<sup>15</sup> 
$$D_{\text{denit}} = R_{\text{denit}} r_{\text{dop}} \gamma_{\text{T}} \text{DOP}$$

10

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(A36)

We assume the denitrification formula suggested by Anderson (1995) for determining  $R_{\text{denit}}$ :

 $C_{117}N_{16}P + 120NO_3 \Rightarrow 117CO_2 + PO_4 + 68N_2$ 

# A5 Iron parameterization

<sup>5</sup> The iron model we use is based on that of Parekh et al. (2004, 2005). We explicitly model the complexation of iron with an organic ligand:

 $Fe' + L' \Leftrightarrow_{k_{d}}^{k_{f}} FeL$   $Fe_{T} = Fe' + FeL$   $L_{T} = L' + FeL$ 

10 where:

Fe', *L*' are free iron and ligand respectively FeL is ligand bound iron  $L_{T}$  is total organic ligand (assumed to be a constant)  $\beta_{fe} = \frac{k_{f}}{k_{d}}$  is ligand binding strength

 $_{15}$   $k_{\rm f}$  is the forward rate constant and  $k_{\rm d}$  is the reverse rate constant.

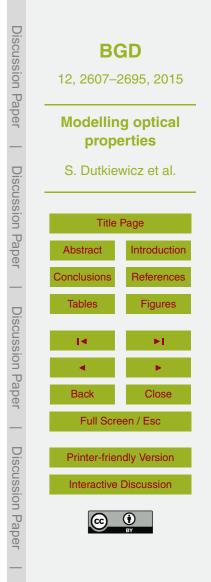
We assume that only the free iron (Fe<sup>'</sup>) can be scavenged,  $c_{scav}$ Fe<sup>'</sup>, and parametrize this as a function of the particulate organic carbon (POC) present (empirical values based on those found for Thorium, Honeyman et al., 1988), a similar approach was used in Parekh et al. (2005):

 $c_{\text{scav}} = c_o (R_{\text{C}:\text{P}} \text{POP})^{\xi}$ 

where:

20

 $\boldsymbol{c}_o$  determines maximum scavenging rate for iron



(A37)

 $\xi$  empirically determined constant

 $R_{C:P}$  is the carbon to phosphorus ratio of the POM.

The sedimentary source ( $F_{sed}$ ) is parameterized as a function of the sinking organic matter reaching the ocean bottom as suggested by Elrod et al. (2004):

$$F_{\text{sed}} = R_{\text{sed}} \frac{\partial w_{\text{pom}} \text{POP}}{\partial z}$$

where  $R_{sed}$  ratio of sediment iron to sinking organic matter.

## A6 Air-sea exchange

Air-sea exchange of  $CO_2$  and  $O_2$  are given by:

$$F_{\rm C} = k_{\rm wc}([\rm CO_2] - [\rm CO_2]_{sat})$$
$$F_{\rm O} = k_{\rm wo}([\rm O_2] - [\rm O_2]_{sat})$$

# where:

 $k_{wi}$  is the gas transfer velocity for  $i = CO_2, O_2,$ 

[CO<sub>2</sub>] is sea surface concentration of carbon dioxide,

 $[CO_2]_{sat}$  is the partial  $CO_2$  in the water if it were fully saturated,

<sup>15</sup> [O<sub>2</sub>] is sea surface concentration of oxygen,

 $[O_2]_{sat}$  is the partial pressure of  $O_2$  in the water if it were fully saturated.

Dissolved inorganic carbon (DIC) carried in the model is made up of carbon dioxide and carbonic acid and other carbonate species:

 $DIC = [CO_2^*] + [HCO_3] + [CO_3].$ 

<sup>20</sup> [CO<sub>2</sub>] is calculated from DIC and Alkalinity concentrations following Follows et al. (2006), which included deducing the pH at all surface locations. The gas transfer coefficient is parametrized following Wannikkof (1992) and is a function of the wind

(A38)

(A39) (A40) speed, and Schmidt number (a function of surface sea temperature).  $[CO_2]_{sat}$  is determined as a function of partial pressures of  $CO_2$  in the air, atmospheric pressure, sea surface temperature, and salinity.  $[O_2]_{sat}$  is provided by Garcia and Gordon (1992). All coefficients of the air–sea flux calculations are determined using the algorithms used in the ocean carbon modeling inter-comparison project (OCMIP) (e.g. Matsumoto et al., 2004).

#### Appendix B: Ocean radiative transfer model: three-stream parameterization

The radiance in the ocean in its most general form,  $L(\mathbf{x}, \theta, \varphi, \lambda)$ , depends on location and orientation in addition to wavelength (units W m<sup>-2</sup> sr<sup>-1</sup> nm<sup>-1</sup>). Neglecting horizontal gradients, the *z* dependence of *L* is described by the classical radiative transfer equation,

$$\frac{dL(\theta,\varphi)}{dz}\cos\theta = -cL(\theta,\varphi) + \int \beta(\theta,\varphi,\theta',\varphi')L(\theta',\varphi')d\Omega', \tag{B1}$$

where  $\beta(\theta, \varphi, \theta', \varphi')$  is the rate of scattering of light from  $\theta', \varphi'$  into  $\theta, \varphi$ . We assume the ocean is optically isotropic, so  $\beta$  is invariant under simultaneous rotation of original and scattered angles (in fact it depends only on the relative angle). The integral over one set of angles therefore yields an angle-independent value,

$$\int_{4\pi} \beta(\theta, \varphi, \theta', \varphi') \, \mathrm{d}\Omega = \int_{4\pi} \beta(\theta, \varphi, \theta', \varphi') \, \mathrm{d}\Omega' = b.$$

Here, b is then the total scattering coefficient and the total scattered light is

$$\iint \beta(\theta, \varphi, \theta', \varphi') L(\theta', \varphi') \, \mathrm{d}\Omega' \, \mathrm{d}\Omega = b \int L(\theta', \varphi') \, \mathrm{d}\Omega' = bE_0$$

and may be decomposed into forward and backward scattering coefficients,  $b = b_{\rm f} + b_{\rm b}$ , where

$$b_{\rm b} = \int_{\theta > \pi/2} \beta(\theta, \varphi, 0, 0) \,\mathrm{d}\Omega.$$

The attenuation coefficient *c* represents loss due to absorption and scattering, c = a + b.

At the sea surface, the downward part of  $L(\theta, \varphi)$  for  $\theta < \pi/2$  is required to equal the output of the atmospheric radiative transfer model (OASIM). The ocean is assumed to be infinitely deep, with vanishing light at infinite depth.

# 10 Three-stream equations

15

Following Aas (1987) and Ackelson et al. (1994), we first separate out the direct (collimated) beam from the radiance,

$$L(\theta, \varphi) = \delta(\cos \theta - \cos \theta_{\rm d}) \,\delta(\varphi - \varphi_{\rm d}) E_{\rm 0d}(z) + L'(\theta, \varphi).$$

where the downward scalar irradiance is  $E_{0d} = E_d / \cos \theta_d$ . The scattering term in Eq. (B1) does not have a collimated part, so the equation for  $E_d$  separates,

$$\frac{\mathrm{d}E_{\mathrm{d}}}{\mathrm{d}z} = -c\frac{E_{\mathrm{d}}}{\cos\theta_{\mathrm{d}}}$$

The downward diffuse and upward irradiance are defined as,

$$\begin{split} E_{\rm s} &= \int\limits_{\theta < \pi/2} L'(\theta, \varphi) \cos \theta \, \mathrm{d}\Omega, \\ E_{\rm u} &= \int\limits_{\theta > \pi/2} L(\theta, \varphi) \cos \theta \, \mathrm{d}\Omega. \end{split}$$

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(B2)

(B3)

and Eq. (B1) is integrated over the downward hemisphere,

$$\begin{aligned} \frac{\mathrm{d}E_{\mathrm{s}}}{\mathrm{d}z} &= \int\limits_{\theta < \pi/2} \frac{\mathrm{d}L(\theta, \varphi)}{\mathrm{d}z} \cos\theta \,\mathrm{d}\Omega - \frac{\mathrm{d}E_{\mathrm{d}}}{\mathrm{d}z} \cos\theta_{\mathrm{d}} \\ &= \int\limits_{\theta < \pi/2} \left[ -cL(\theta, \varphi) + \int\limits_{4\pi} \beta(\theta, \varphi, \theta', \varphi')L(\theta', \varphi') \,\mathrm{d}\Omega' \right] \,\mathrm{d}\Omega. \end{aligned}$$

The outer integral is split into contributions from  $E_d$  and down- and upwelling <sup>5</sup> irradiance, using Eq. (B2) to rewrite the inner integral,

$$\iint \dots = \left( b - \int_{\theta > \pi/2} \beta(\theta, \varphi, \theta_{d}, \varphi_{d}) d\Omega \right) E_{0d}$$
  
+ 
$$\int_{\theta' < \pi/2} \left( b - \int_{\theta > \pi/2} \beta(\theta, \varphi, \theta', \varphi') d\Omega \right) L'(\theta', \varphi') d\Omega'$$
  
+ 
$$\int_{\theta' > \pi/2\theta < \pi/2} \beta(\theta, \varphi, \theta', \varphi') d\Omega L(\theta', \varphi') d\Omega'$$

The effective backward scattering coefficients are defined as corrections to  $b_{\rm b}$ ,

$$\begin{split} r_{\rm s} b_{\rm b} &= \frac{1}{E_{\rm 0s}} \int\limits_{\theta' < \pi/2\theta > \pi/2} \beta(\theta, \varphi, \theta', \varphi') \, \mathrm{d}\Omega \, L'(\theta', \varphi') \, \mathrm{d}\Omega', \\ r_{\rm u} b_{\rm b} &= \frac{1}{E_{\rm 0u}} \int\limits_{\theta' > \pi/2\theta < \pi/2} \beta(\theta, \varphi, \theta', \varphi') \, \mathrm{d}\Omega \, L(\theta', \varphi') \, \mathrm{d}\Omega', \\ r_{\rm d} b_{\rm b} &= \int\limits_{\theta > \pi/2} \beta(\theta, \varphi, \theta_{\rm d}, \varphi_{\rm d}) \, \mathrm{d}\Omega, \end{split}$$

5 where

$$E_{0s} = \int_{\theta < \pi/2} L'(\theta, \varphi) d\Omega,$$
$$E_{0u} = \int_{\theta > \pi/2} L(\theta, \varphi) d\Omega.$$

In terms of the effective backscattering coefficients,

$$\frac{dE_{s}}{dz} = -cE_{0s} + (b - r_{s}b_{b})E_{0s} + r_{u}b_{b}E_{0u} + (b - r_{d}b_{b})E_{0d}$$

10 Likewise,

$$-\frac{dE_{u}}{dz} = -cE_{0u} + (b - r_{u}b_{b})E_{0u} + r_{s}b_{b}E_{0s} + r_{d}b_{b}E_{0d}.$$

 $E_{\rm 0s}$  is related to the downwelling irradiance  $E_{\rm s}$  by the average cosine of the zenith angle,

$$\bar{\upsilon}_{\rm s} = \frac{E_{\rm s}}{E_{\rm 0s}} = \frac{\int_{\theta < \pi/2} L' \cos \theta \, \mathrm{d}\Omega}{\int_{\theta < \pi/2} L' \, \mathrm{d}\Omega}$$

and similar for  $E_{0u}$ . The radiative transfer equations become

$$\frac{\mathrm{d}E_{\mathrm{s}}}{\mathrm{d}z} = -\frac{a + r_{\mathrm{s}}b_{\mathrm{b}}}{\bar{o}_{\mathrm{s}}}E_{\mathrm{s}} + \frac{r_{\mathrm{u}}b_{\mathrm{b}}}{\bar{o}_{\mathrm{u}}}E_{\mathrm{u}} + \frac{b - r_{\mathrm{d}}b_{\mathrm{b}}}{\cos\theta_{\mathrm{d}}}E_{\mathrm{d}},$$
$$-\frac{\mathrm{d}E_{\mathrm{u}}}{\mathrm{d}z} = -\frac{a + r_{\mathrm{u}}b_{\mathrm{b}}}{\bar{o}_{\mathrm{u}}}E_{\mathrm{u}} + \frac{r_{\mathrm{s}}b_{\mathrm{b}}}{\bar{o}_{\mathrm{s}}}E_{\mathrm{s}} + \frac{r_{\mathrm{d}}b_{\mathrm{b}}}{\cos\theta_{\mathrm{d}}}E_{\mathrm{d}}.$$

In general,  $\bar{v}_s$  and  $\bar{v}_u$  depend on the angular profile radiation field, and  $r_s$  and  $r_u$ , <sup>5</sup> which describe the scattering of downward into upward and upward into downward radiation, depend on both the scattering function and the radiation field.

We close the system of equations by by making the following assumptions (following Aas, 1987):

 $r_{\rm d} \approx 1.0$ ,

10  $r_{\rm s} \approx 1.5$ ,

 $r_{\rm u} \approx 3.0,$ 

$$\bar{\upsilon}_{s} \approx 0.83$$

 $\bar{\upsilon}_{\rm u} \approx 0.4.$ 

Equations (B3)–(B5) are the 3-stream equations (given in main text as Eqs. 1–3, though note that here we dispense with function of  $\lambda$  for simplicity).

The equation for  $E_d$  (Eqs. B3 or 1) is readily integrated,

$$E_{d}(z) = E_{d}(0) \exp \int_{0}^{z} \frac{-c(z')}{\cos \theta_{d}} dz'$$

In contrast to Aas (1987), Ackelson et al. (1994) and Gregg (2002) we do not make further approximations, but instead solve the remaining equations explicitly. We can write the remaining two equations (Eqs. B4 and B5, also Eqs. 2 and 3) as

 $\frac{\mathrm{d}}{\mathrm{d}z}\mathbf{E} = M\mathbf{E} + \mathbf{I}$ 

20

(B4)

(B5)

(B6)

where

$$M = \begin{pmatrix} -C_{\rm s} & B_{\rm u} \\ -B_{\rm s} & C_{\rm u} \end{pmatrix}, \quad \mathbf{E} = \begin{pmatrix} E_{\rm s} \\ E_{\rm u} \end{pmatrix}, \quad \mathbf{I} = \begin{pmatrix} F_{\rm d} \\ -B_{\rm d} \end{pmatrix} E_{\rm d}$$

and

$$C_{s} = \frac{a + r_{s}b_{b}}{\bar{v}_{s}}, \quad B_{u} = \frac{r_{u}b_{b}}{\bar{v}_{u}}, \quad F_{d} = \frac{b - r_{d}b_{b}}{\cos\theta_{d}},$$
  

$$S \quad C_{u} = \frac{a + r_{u}b_{b}}{\bar{v}_{u}}, \quad B_{s} = \frac{r_{s}b_{b}}{\bar{v}_{s}}, \quad B_{d} = \frac{r_{d}b_{b}}{\cos\theta_{d}}.$$

M,  $F_{d}$  and  $B_{d}$  are assumed to be piece-wise constant as a function of z. Following Kylling (1995) we write the inhomogeneous solution as

$$\mathbf{E} = \begin{pmatrix} x \\ y \end{pmatrix} E_{\mathsf{d}}$$

where x, y satisfy the equation

$${}_{10} \quad \begin{pmatrix} -C_{\rm s} + C_{\rm d} & B_{\rm u} \\ -B_{\rm s} & C_{\rm u} + C_{\rm d} \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix} + \begin{pmatrix} F_{\rm d} \\ -B_{\rm d} \end{pmatrix} = 0$$

with solution

$$\begin{pmatrix} x \\ y \end{pmatrix} = \frac{1}{(c_{d} - C_{s})(c_{d} + C_{u}) + B_{s}B_{u}} \cdot \begin{pmatrix} c_{d} + C_{u} & -B_{u} \\ B_{s} & c_{d} - C_{s} \end{pmatrix} \begin{pmatrix} -F_{d} \\ B_{d} \end{pmatrix}.$$

The eigenvalues of M are

$$\kappa^{-} = D - C_{s}$$

$$\kappa^{+} = C_{u} - D = -C_{s} + \frac{B_{s}B_{u}}{D}$$

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(B7)

(B8)

(B9)

where

$$D = \frac{1}{2} \left( C_{\rm s} + C_{\rm u} + \sqrt{(C_{\rm s} + C_{\rm u})^2 - 4B_{\rm s}B_{\rm u}} \right)$$

Within a computational layer, the general solution can be written as

$$\begin{pmatrix} E_{s}(z) \\ E_{u}(z) \end{pmatrix} = c_{k}^{+} \begin{pmatrix} 1 \\ r_{k}^{+} \end{pmatrix} e^{-\kappa_{k}^{+}(z-z_{k})} + c_{k}^{-} \begin{pmatrix} r_{k}^{-} \\ 1 \end{pmatrix} e^{\kappa_{k}^{-}(z-z_{k+1})} + \begin{pmatrix} x_{k} \\ y_{k} \end{pmatrix} E_{d}(z)$$

<sup>5</sup> where  $r^+ = R_2 = B_s/D$ ,  $r^- = 1/R_1 = B_u/D$ . The offsets in the exponents have been introduced so that both exponentials are smaller than 1. The coefficients  $c^+$  and  $c^$ have to be determined from boundary conditions. At the sea surface, we require  $E_s$ and  $E_d$  coincide with the output of OASIM,

$$C_1^+ + r_1^- e^{-\kappa_1^- z_1} C_1^- = E_{s_o}^{\text{below}} - x_1 E_{d_o}^{\text{below}}$$

<sup>10</sup> In the bottom layer,  $k_{\text{bot}}$ , we require zero light at infinite depth, i.e.,  $c_{k_{\text{bot}}}^- = 0$ . At layer boundaries,  $z_{k+1}$ , we require continuity,

$$e^{-\kappa_{k}^{+}(z_{k+1}-z_{k})}c_{k}^{+}+r_{k}^{-}c_{k}^{-}+x_{k}E_{d}(z_{k+1})=c_{k+1}^{+}+e^{\kappa_{k+1}^{-}(z_{k+1}-z_{k+2})}r_{k+1}^{-}c_{k+1}^{-}+x_{k+1}E_{d}(z_{k+1}),$$
  

$$e^{-\kappa_{k}^{+}(z_{k+1}-z_{k})}r_{k}^{+}c_{k}^{+}+c_{k}^{-}+y_{k}E_{d}(z_{k+1})=r_{k+1}^{+}c_{k+1}^{+}+e^{\kappa_{k+1}^{-}(z_{k+1}-z_{k+2})}c_{k+1}^{-}+y_{k+1}E_{d}(z_{k+1}).$$

In order to solve this coupled system of equations, we follow Kylling et al. (1995) and Toon et al. (1989) who observed that it can be transformed to tri-diagonal form by eliminating  $c_{k+1}^{-}$ ,

$$e_{k}^{+}(1 - r_{k}^{+}r_{k+1}^{-})c_{k}^{+} + (r_{k}^{-} - r_{k+1}^{-})c_{k}^{-} - (1 - r_{k+1}^{+}r_{k+1}^{-})c_{k+1}^{+} = [x_{k+1} - x_{k} - (y_{k+1} - y_{k})r_{k+1}^{-}]E_{d}(z_{k+1})$$
(B10)

resp.  $c_k^+$ ,

$$(1 - r_k^- r_k^+) c_k^- - (r_{k+1}^+ - r_k^+) c_{k+1}^+ - e_{k+1}^- (1 - r_{k+1}^- r_k^+) c_{k+1}^- = [y_{k+1} - y_k - (x_{k+1} - x_k) r_k^+] E_d(z_{k+1})$$
(B11)

where  $e_k^+ = e^{-\kappa_k^+(z_{k+1}-z_k)}$  and  $e_k^- = e^{-\kappa_k^-(z_{k+1}-z_k)}$ . The reduced system is solved explicitly using Gaussian elimination.

# Appendix C: Phytoplankton functional type specific absorption and scattering spectra

Phytoplankton total light absorption spectra show in Fig. 1d were obtained for representative species in culture: Syn, *Synechococcus* WH7803 (Suggett et al., 2004);
HLPro, *Prochlorococcus* MED4 (Moore et al., 1995); LLPro, *Prochlorococcus* SS120 (Moore et al., 1995); Cocco, *Emiliania huxleyi* (Suggett et al., 2007); SmEuk, *Isochrysis galbana* (Ahn et al., 1992); Diat, *Thalassiosira weissflogii* (Suggett et al., 2004); LgEuk, *Prorocentrum micans* (Ahn et al., 1992); Tricho, *Trichodesmium* sp. (Dupouy et al., 2008), Diaz, unicellular diazotroph absorption properties were assumed the same as Syn.

Total phytoplankton light scattering was also taken for representative species in culture, with every attempt to match species used for absorption: Syn, generic *Synechococcus* (Stramski et al., 2001, derived from Morel et al., 1993 and Stramksi et al., 1995); HLPro and LLPro, *Prochlorococcus* (Stramski et al., 2001, derived from Morel et al., 2001, where original data are from Ahn et al., 1992); SmEuk, *Isochrysis galbana* (Stramski et al., 2001, where original data are from Ahn et al., 1992); Diat, *Chaetoceros curvisetus* (Stramski et al., 2001, derived from Bricaud et al., 1988); LgEuk, *Prorocentrum micans* (Stramski et al., 2001, where original data are from Ahn
et al., 1992); *Trichodesmium* sp. (Dupouy et al., 2008), Diaz, unicellular diazotroph

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scattering properties were assumed the same as Syn. Backscattering to forward scattering ratios were obtained from Stramski et al. (2001), except for Tricho which was derived from Subramanian et al. (1999).

The absorption and scattering properties of the other optical constituents were also obtained from the literature, as outlined in the main text.

# Appendix D: Inversion of AMT-15 light field

In order to estimate backscattering  $b_{\rm b}$  from the observations made during AMT-15 we utilize the measured downwelling irradiance,  $E_{\rm dn}$ , and upwelling, zenithward radiance,  $L_{\rm u}$ . We use the procedure of Gordon and Boynton (1997, 1998) with the radiative transfer package DISORT, version 2.0 $\beta$ . We use the Gordon and Boynton (1997, 1998) parameterization rather than the the Quasi-Analytical Algorithm (Lee et al., 2002, 2007) since we are dealing with profiles not surface water leaving radiance.

Gordon and Boynton (1998) propose that  $R = E_u/E_{dn}$  and  $X = b_b/a$  are related as

$$3R(z) \approx \frac{\int_{z}^{\infty} X(z)q(z,z')\,\mathrm{d}z'}{\int_{z}^{\infty} q(z,z')\,\mathrm{d}z'}$$

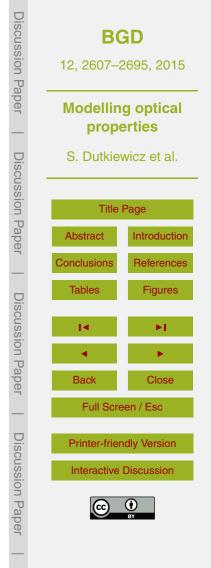
15 where

(

$$q(z,z') = \left(E_{dn}(z')/E_{dn}(z)\right)^2.$$

We drop  $E_{dn}(z)$  from numerator and denominator and discretize as

$$3R_i \approx \frac{\sum_{j=i}^{\infty} X_j q_j}{\sum_{j=i}^{\infty} q_j}$$



#### where

$$q_j = \int_{z_j}^{z_{j+1}} E_{dn}(z)^2 dz = \frac{E_j^2 - E_{j+1}^2}{2k_j}$$

and

$$k_j = \frac{1}{Z_{j+1} - Z_j} \ln \frac{E_j}{E_{j+1}}.$$

<sup>5</sup> In order to solve for X, we write

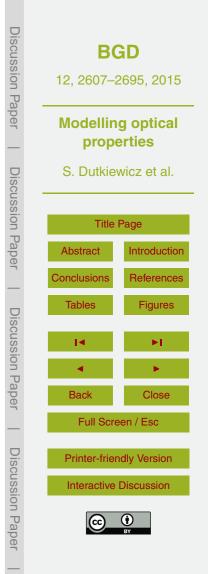
$$3R_i \approx \frac{X_i q_i + 3R_{i+1} \sum_{j=i+1}^{\infty} q_j}{q_i + \sum_{j=i+1}^{\infty} q_j}$$

and get

$$X_i \approx 3R_i - 3(R_{i+1} - R_i) \frac{1}{q_i} \sum_{j=i+1}^{\infty} q_j$$

For noisy data, this estimate of X may become negative. We drop the derivative term where this happens, i.e., X is approximated by 3R.

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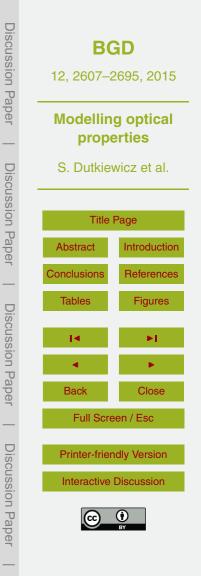
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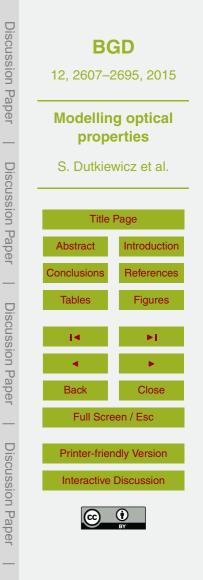
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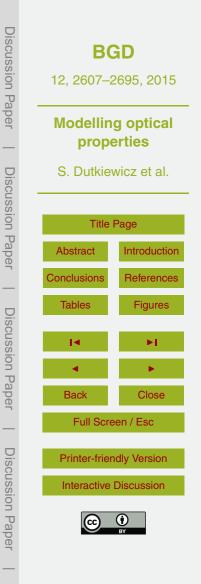
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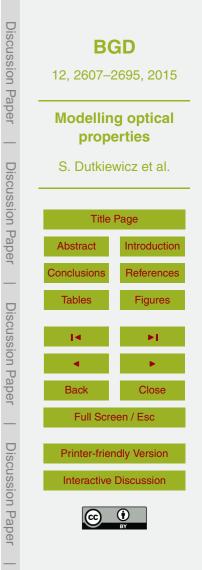
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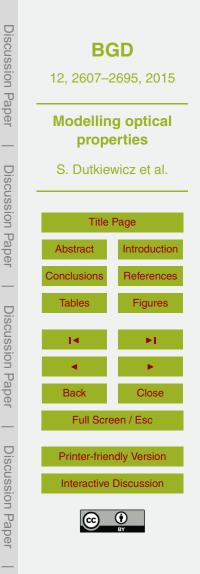
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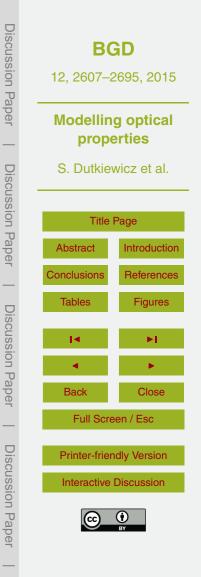
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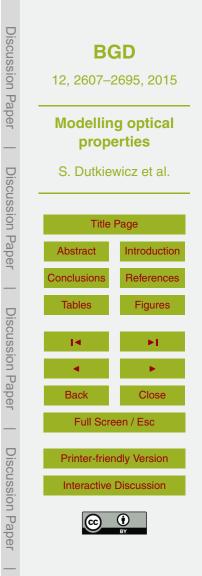
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Parameter	Symbol	Fixed value	Units
Falailletei	Symbol	Fixed value	UTIIIS
temperature coefficients	$A_E$	-4000	K
	T <sub>o</sub>	293.15	K
temperature normalization	$1/\tau_{1}$	0.5882	unitless
DOM remineralization	r <sub>dop</sub>	0.0333	$d^{-1}$
rate at 30 °C	r <sub>don</sub>	0.0333	$d^{-1}$
	r <sub>dofe</sub>	0.0333	$d^{-1}$
	r <sub>doc</sub>	0.0333	$d^{-1}$
POM remineralization	r <sub>pop</sub>	0.05	$d^{-1}$
rate at 30 °C	r <sub>pon</sub>	0.0333	$d^{-1}$
	r <sub>pofe</sub>	0.0333	$d^{-1}$
	r <sub>posi</sub>	0.0067	$d^{-1}$
	r <sub>poc</sub>	0.0333	$d^{-1}$
PIC dissolution rate	d <sub>pic</sub>	0.0033	$d^{-1}$
POM sinking rate	W <sub>pom</sub>	10	$md^{-1}$
PIC sinking rate	W <sub>pic</sub>	15	$md^{-1}$
fraction DOM to CDOM	f <sub>cdom</sub>	0.02	unitless
bleaching rate for CDOM	l <sub>cdom</sub>	0.167	$d^{-1}$
degradation rate for CDOM	$d_{\rm cdom}$	0.003	$d^{-1}$
light level for bleaching CDOM	/ <sub>cdom</sub>	60	μEinm <sup>-2</sup> s <sup>-1</sup>
CDOM absorption at $\lambda_o$	$C_{\rm cdom}(\lambda_o)$	20.5	$m^2$ (mmol P) <sup>-1</sup>
reference waveband	λο	450	nm
CDOM absorption spectral slope	S <sub>cdom</sub>	0.02061	(nm) <sup>-1</sup>
POP to particle conversion	$p_{part}$	1 × 10 <sup>-17</sup>	mmol P (particle) <sup><math>-1</math></sup>



Parameter	Symbol	Fixed value	Units
$NH_4$ to $NO_2$ oxidation rate	$\zeta_{no2}$	0.1	d <sup>-1</sup>
$NO_2$ to $NO_3$ oxidation rate	$\zeta_{nh4}$	0.1	$d^{-1}$
critical PAR for oxidation	I <sub>ox</sub>	10	µEin m <sup>−2</sup> s <sup>−1</sup>
critical oxygen for denitrification	0 <sub>crit</sub>	6	μMO <sub>2</sub>
ratio N: P in denitrification	R <sub>denit</sub>	120	unitless
ratio NO <sub>3</sub> to all N in denitrification	R <sub>dno3</sub>	104	unitless
ligand binding strength	$eta_{fe}$	2 × 10 <sup>5</sup>	$(\mu M Fe)^{-1}$
total ligand	L <sub>T</sub>	1 × 10 <sup>-3</sup>	μM Fe
scavenging rate coefficient	Co	1.2 × 10 <sup>-3</sup>	$d^{-1}$
scavenging power coefficient	ξ	0. 58	unitless
sedimentation rate ratio	$R_{\sf sed}$	$6.8 \times 10^{-4}$	$\mu$ M Fe( $\mu$ M POC) <sup>-1</sup>
Chl a acclimation timescale	t <sub>chl</sub>	0.5	$d^{-1}$
ammonia inhibition	Ψ	4.6	$(\mu M N)^{-1}$

### Table 2. Fixed biogeochemical/ecosystem model parameters (2).

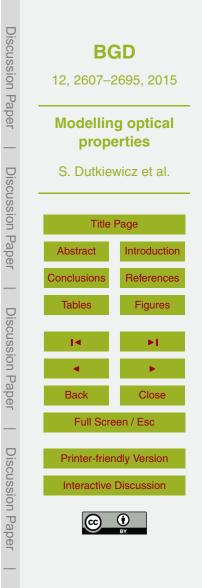


 Table 3. Phytoplankton specific parameters description.

Parameter	Symbol	Units
max photosyn rate at 30 °C	$P^{C}_{m_{\max_j}}$	d <sup>-1</sup>
max growth rate at 30 °C	$\mu_{\max_i}$	$d^{-1}$
elemental ratios	, M <sub>Si:Рi</sub>	$molSi(molP)^{-1}$
	$M_{N:P_i}$	$mol N (mol P)^{-1}$
	M <sub>Fe:Pi</sub>	$mmol Fe (mol P)^{-1}$
	M <sub>C:P</sub>	$mol C (mol P)^{-1}$
ratio IC to OP	$R_{rj}$	$mol C (mol P)^{-1}$
growth half saturation	K <sub>po4</sub>	μΜ Ρ
	κ <sub>in,</sub>	μΜ Ν
	κ <sub>nh4</sub> ,	μΜ Ν
	κ <sub>fe,</sub> ΄	nM Fe
	κ <sub>si,</sub>	μM Si
max quantum yield	$\phi_{\max_i}$	mmol C (mol photons) $^{-1}$
max Chl <i>a</i> : C	$\theta_{\max_i}$	mg Chl (mmol C) $^{-1}$
Chl a specific absorption	$a_{\mathrm{phy}_{j}}^{\mathrm{chl}}(\lambda)$	m <sup>2</sup> mg Chl <sup>-1</sup>
photosyn absorption	$a_{psj}^{chl}(\lambda)$	m <sup>2</sup> mg Chl <sup>-1</sup>
carbon specific scattering	$b_{\text{phy}_{i}}^{C}(\lambda)$	$m^2 mol C^{-1}$
backscattering	$b_{\text{bphy}_{j}}^{C}(\lambda)$	$m^2 mol C^{-1}$
sinking rate	W <sub>pj</sub>	$m d^{-1}$
light inhibition	κ <sub>inhb,</sub>	unitless
mortality rate at 30 °C	m <sub>pj</sub>	$d^{-1}$
DOM/POM partitioning	$\varphi_{mp_{ij}}$	unitless
grazing palatibility	$\eta_{jk}$	unitless

**Discussion** Paper **BGD** 12, 2607-2695, 2015 **Modelling optical** properties S. Dutkiewicz et al. **Discussion** Paper Title Page Abstract Introduction Conclusions References Tables Figures **Discussion** Paper ۶I [◀ ► ◄ Back Close Full Screen / Esc **Discussion Paper Printer-friendly Version** Interactive Discussion ۲

Parameter	Diatom	Lg Euk	Tricho	Coccol	Uni Diaz	Sm Euk	Syn	HL/LL Pro
$P_{m_{\max_j}}^{C}$	3.45	1.67	0.31	1.03	0.61	1.82	1.22	1.09
$\mu_{\max_i}$	1.63	1.01	0.230	0.68	0.42	1.11	0.78	0.70
M <sub>Si:P</sub>	16	0		0	0	0	0	0
M <sub>N:Pi</sub>	16	16	40	16	40	16	16	16
M <sub>Fe:P</sub>	1	1	4	1	4	1	1	1
M <sub>C:P</sub>	120	120	120	120	120	120	120	120
R <sub>rj</sub>	0	0	0	0.8	0	0	0	0
., К <sub>ро4,</sub>	0.0187	0.0069	0.0034	0.0046	0.0011	0.0018	0.0011	0.0004
K <sub>in,</sub>	0.300	0.110	0	0.074	0	0.029	0.018	0.007
κ <sub>nh4,</sub>	0.150	0.055	0	0.037	0	0.015	0.090	0.035
κ <sub>fe,</sub>	0.0187	0.0069	0.0136	0.0046	0.0052	0.0018	0.0081	0.0004
K <sub>si</sub>	0.300	0	0	0	0	0	0	0
$\phi_{\max_j}$	0.4	0.4	0.4	0.4	0.4	0.4	0.4	0.4
$\theta_{\max_j}$	0.3	0.2	0.2	0.2	0.2	0.2	0.2	0.2
W <sub>pj</sub>	0.36	0.23	0.45	0.23	0.10	0.07	0.06	0.03
K <sub>inhb</sub> ,	0	0	0	0	0	0	0	0/0.9
m <sub>pj</sub> ′	0.1	0.1	0.1	0.1	0.1	0.1	0.1	0.1
$\varphi_{mp_{ij}}$	0.5	0.5	0.5	0.5	0.2	0.2	0.2	0.2
$\eta_{jk}, k = \lg$	0.86	0.90	0.5	0.85	0.2	0.2	0.2	0.2
$\eta_{jk}, k = \mathrm{sm}$	0.17	0.18	0.1	0.17	1.0	1.0	1.0	1.0

 Table 4. Phytoplankton specific parameter values.

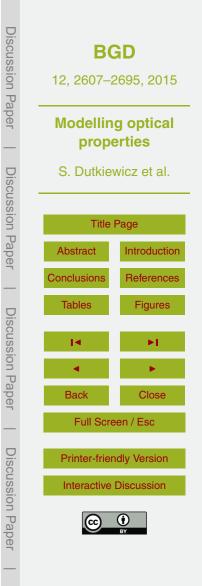
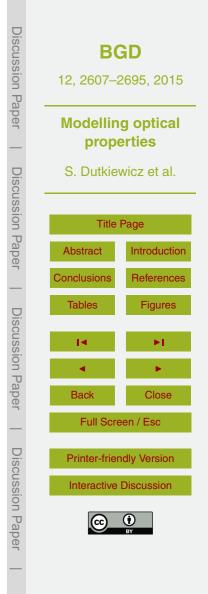


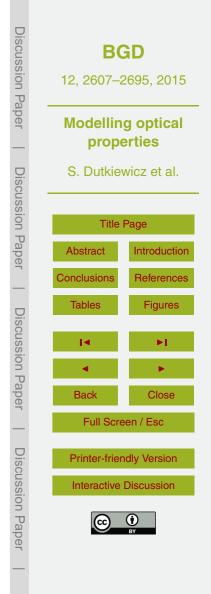
Table 5. Zooplankton/grazing	specific parameter description.
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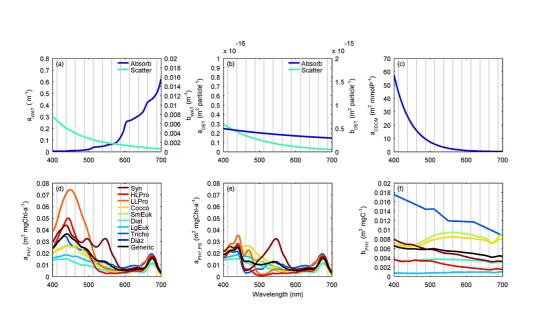
Parameter	Symbol	Units
max grazing rate	$g_{\max_{jk}}$	d <sup>-1</sup>
DOM/POM partitioning	$arphi_{{ extsf{g}}_{ijk}} \ arphi_{{ extsf{mz}}_{ik}}$	unitless unitless
mortality at 30 °C	$m_{zk}$	d <sup>-1</sup>
	m <sub>z2k</sub>	$d^{-1} (\mu M P)^{-1}$
grazing efficiency grazing half saturation	ζ <sub>jk</sub> K <sub>pk</sub>	unitless μΜ Ρ



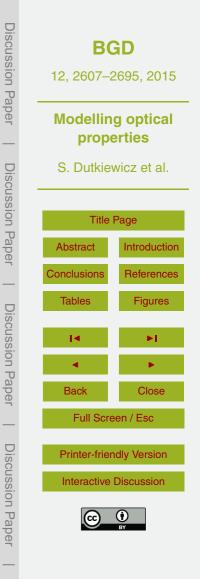
Parameter	k = large	k = small
$g_{\max_{jk}}$	<i>j</i> = large, 1;	<i>j</i> = large, 0.1;
<i>,</i> ,,	<i>j</i> = small, 0.1	<i>j</i> = small, 1.
$oldsymbol{arphi}_{g_{ijk}}$	0.7	0.2
$\varphi_{mz_{ik}}$	0.5	0.2
$m_{zk}$	0.067	0.067
$m_{z^{2k}}$	22.4	22.4
$\zeta_{ik}$	<i>j</i> = large, 0.85;	<i>j</i> = large, 0.5;
<b>,</b>	<i>j</i> = small, 0.95	<i>j</i> = small, 0.85
κ <sub>pk</sub>	0.027	0.027

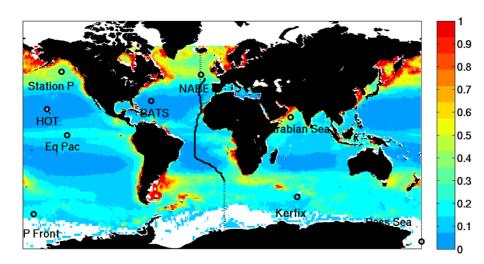
Table 6. Zooplankton/	/grazing specific parameter value	s.
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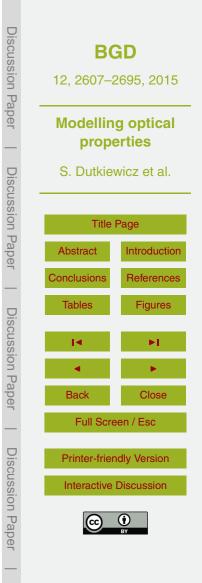


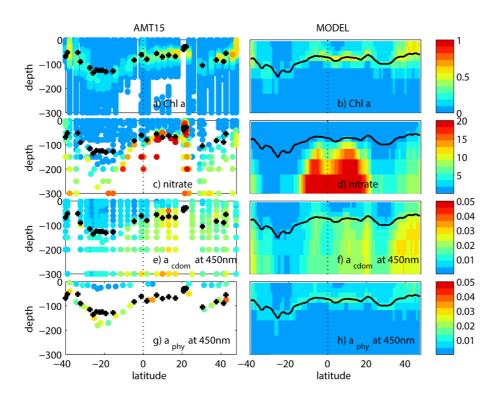
**Figure 1.** Spectra for (a) absorption and scattering by water molecules  $(a_w, b_w, m^{-1})$ ; (b) particle specific absorption and scattering by detritus  $(a_{det}^{part}, b_{det}^{part}, m^2 particle^{-1})$ ; and (c) CDOM-specific absorption by CDOM  $(a_{cdom}^{CDOM}, m^2 mmol P^{-1})$ ; (d) Chl *a* specific total absorption by phytoplankton  $(a_{phyj}^{chl}, m^2 mg Chl^{-1})$ ; (e) Chl *a* specific absorption by photosynthetic pigments  $(a_{psj}^{chl}, m^2 (mg Chl)^{-1})$ ; and (f) biomass specific scattering by phytoplankton  $(b_{phyj}^{C}, m^2 (mg C)^{-1})$ . Details on data sources are included in the main text and Appendix C. The black line in (d-f) is the mean of the coloured lines (i.e. the mean spectrum).



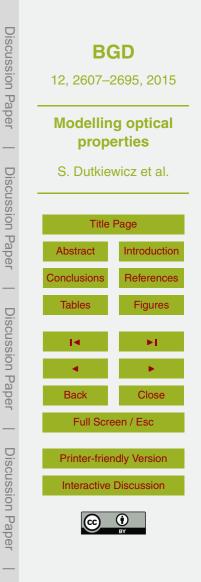


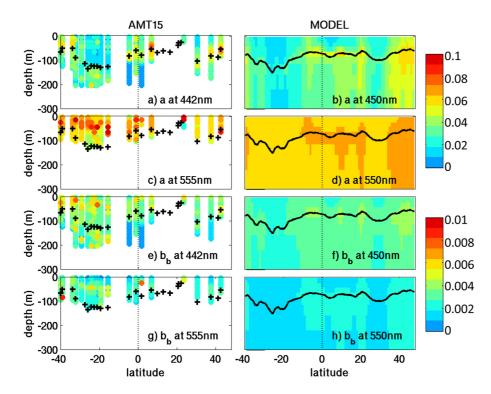
**Figure 2.** Satellite (MODIS) derived Chl *a* (mgm<sup>-3</sup>) overlain with the cruise track of the 15th Atlantic Meridional Transect (AMT-15) solid black line and 9 JGOFS timeseries site (black circles). We also show with dashed line the extension to the AMT-15 which is used in some transect figures to include model subpolar results.



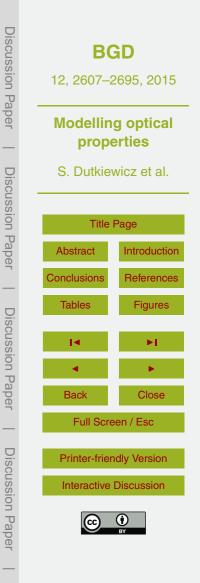


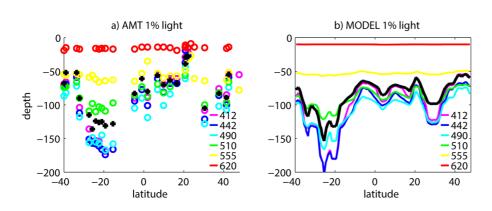
**Figure 3.** Comparison of model output (right column, October mean) with data collected during AMT-15 (left column, collected from late September to late October): **(a, b)** Chl *a* (mg Chlm<sup>-3</sup>); **(c, d)** nitrate (mmolNm<sup>-3</sup>); **(e, f)** absorption by colored dissolved matter ( $a_{cdom}$ ) (m<sup>-1</sup>); **(g, h)** absorption by phytoplankton ( $a_{phy}$ ) (m<sup>-1</sup>). The AMT-15 data is plotted as dots for each observation taken. Model data is presented across the whole transect. The black crosses indicate the depth where the total PAR is 1 % of the surface value in the AMT-15. Model 1 % irradiance depth is shown as a black line. Transect location is shown in Fig. 2. (AMT-15 optical data G. Moore, unpublished; CDOM, Stubbins et al., 2006).



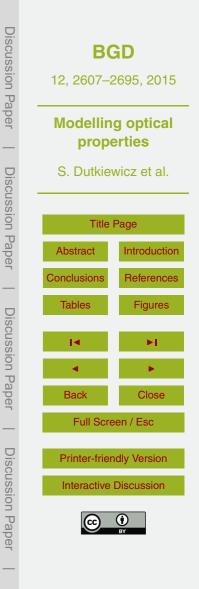


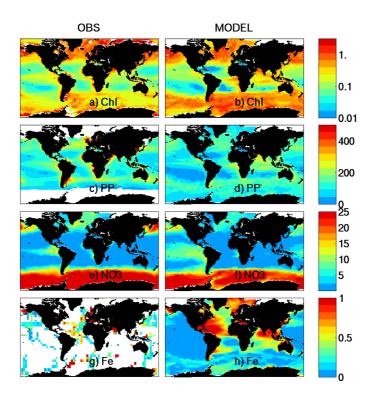
**Figure 4.** Comparison of model output (right column, October mean) with data collected during AMT-15 (left column): **(a)** derived total absorption at 443 nm (m<sup>-1</sup>); **(b)** model total absorption at 450 nm (m<sup>-1</sup>); **(c)** derived total absorption at 555 nm (m<sup>-1</sup>); **(d)** model total absorption at 550 nm (m<sup>-1</sup>); **(e)** derived total backscattering at 443 nm (m<sup>-1</sup>); **(f)** model total backscattering at 450 nm (m<sup>-1</sup>). **(g)** derived total backscattering at 555 nm (m<sup>-1</sup>); **(h)** model total backscattering at 550 nm (m<sup>-1</sup>). The derived properties were calculated with an inverse model of the downwelling and upwelling irradiance measured during AMT-15 (see text, and Appendix D). 1 % light level indicated with black lines/symbols. (AMT-15 optical data G. Moore, unpublished).



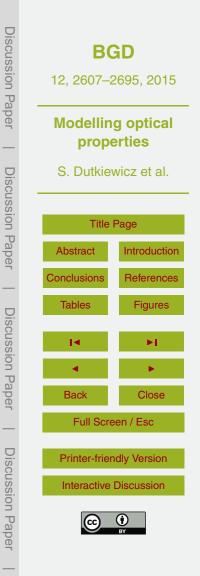


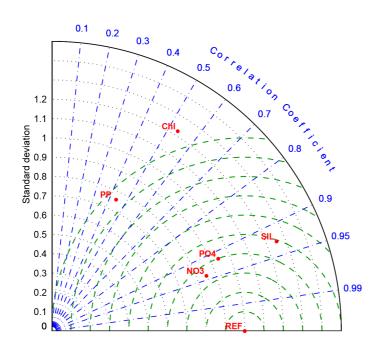
**Figure 5.** Comparison of data collected along AMT-15 (a) and model (October mean) (b); black symbols in (a), and black line in (b) indicate the depth of where the total irradiance is 1% of the surface value. Colored lines/symbols indicate where the irradiance in each of several wavelengths are 1% of the surface values. Model results are interpolated to same wavelength as the AMT-15 data. (AMT-15 optical data G. Moore, unpublished.)



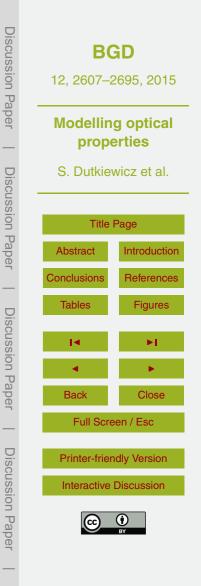


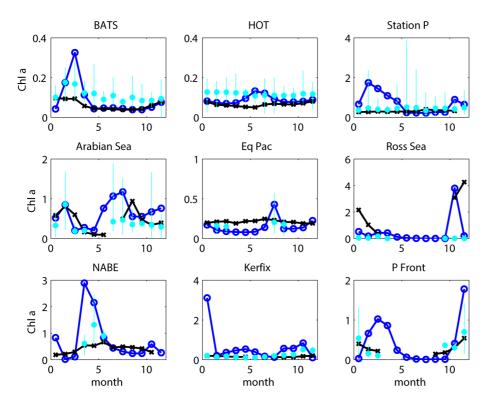
**Figure 6.** Comparison of model and satellite derived products and climatologies of in situ measurements for annual mean: **(a)** satellite derived (MODIS) Chl *a* (mg Chl m<sup>-2</sup>); **(b)** modelled Chl *a* (mean 0–50 m, mg Chl m<sup>-2</sup>); **(c)** satellite derived primary production (gC m<sup>-2</sup> yr<sup>-1</sup>) (Behrenfeld and Falkowski, 1997); **(d)** modelled primary production (column integrated,  $gCm^{-2}yr^{-1}$ ); **(e)** World Ocean Atlas nitrate (mean 0–50 m, mmol m<sup>-3</sup>) (Garcia et al., 2006); **(f)** modelled nitrate (mean 0–50 m, mmol m<sup>-3</sup>); **(g)** compiled iron observations (composite 0–50 m, nM) (Tagliubue et al., 2012); **(h)** modelled iron (mean 0–50 m, nM).





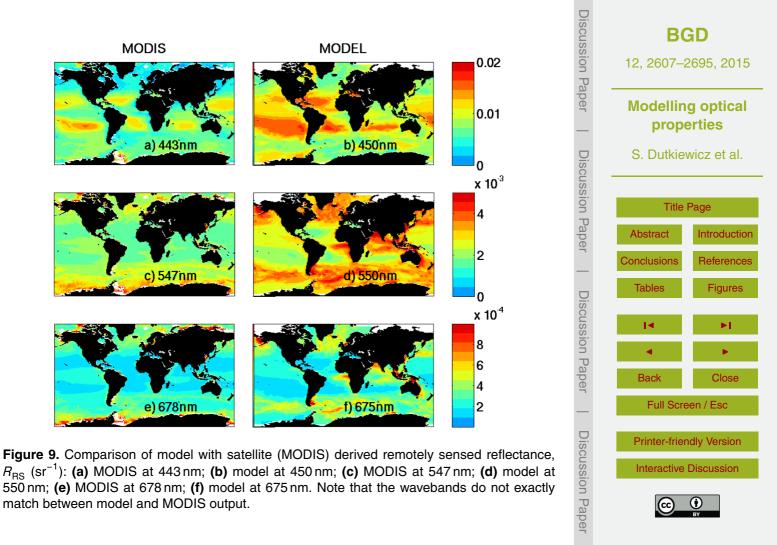
**Figure 7.** Taylor diagram showing correlation and normalized SD between annual mean modelled Chl *a*, primary production (PP), macro nutrient (NO<sub>3</sub>, PO<sub>4</sub> and silicic acid (SIL)). Satellite derived products (Chl *a* from MODIS and primary production following Behrenfeld and Falkowski, 1997) and World Ocean Atlas (Garcia et al., 2006) nutrients. A perfect match would be a correlation of 1 (i.e. on the *x* axis) and normalized SD of 1: this point is shown as "REF".

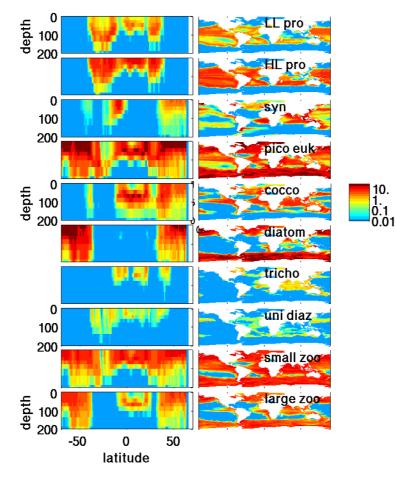




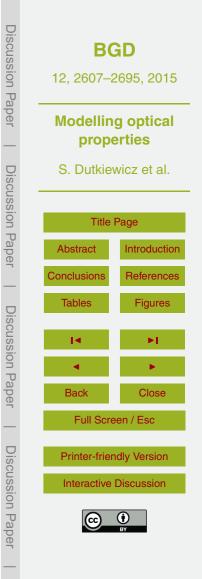
**Figure 8.** Comparison of monthly model Chl *a* (mg m<sup>-3</sup>) (dark blue) at nine sites (JGOFS data, Kleypas and Doney, 2001) with satellite (MODIS) derived Chl *a* (mg m<sup>-3</sup>) (black) and in situ (light blue). In situ show monthly mean of 0–15 m with symbol and line indicates range of values. Locations of sites are shown in Fig. 1.

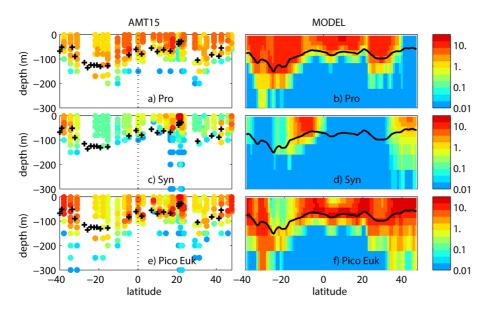




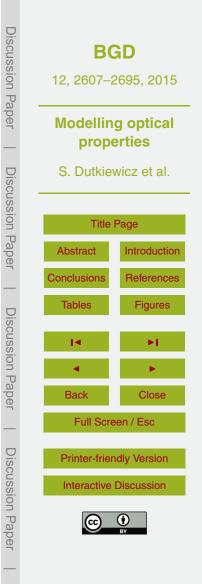


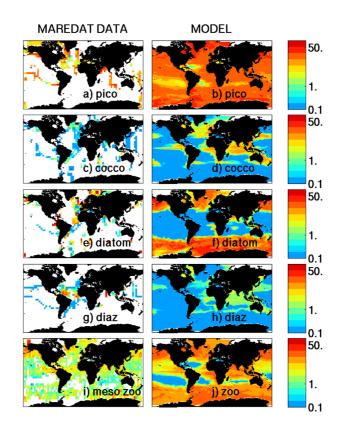
**Figure 10.** Model annual mean biomass  $(mgCm^{-3})$  of the plankton types for AMT-15 transect extended north and south to show the subpolar regions (left) and 0–50 m average (right). Shown are the 8 surviving phytoplankton types and the two zooplankton types.



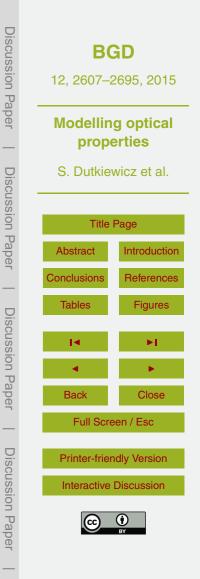


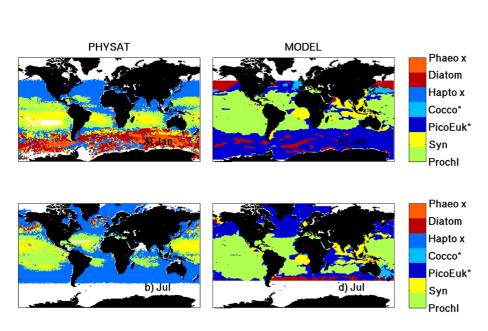
**Figure 11.** Comparison of model output (October mean) with data collected along AMT-15: **(a, b)** *Prochlorococcus*; **(c, d)** *Synechococcus*; **(e, f)** pico-eukaryotes. Results are shown in  $mgCm^{-3}$ ; AMT-15 observations were converted from cell count to biomass (Zubkov et al., 1998). AMT-15 data from Heywood et al. (2006).



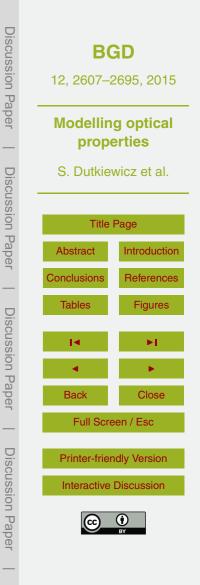


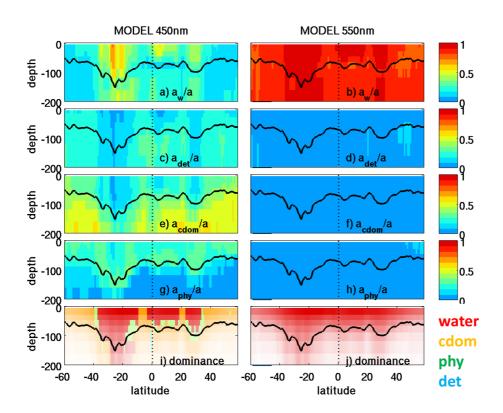
**Figure 12.** Comparison of model plankton type biomass (mg C m<sup>-3</sup>) with compilation of biomass from MAREDAT (pico-phytoplankton; Buitenhuis et al., 2012; coccolithophores, O'Brien et al., 2013; diatoms, Leblanc et al., 2012; diazotrophs, Luo et al., 2012; meso-zooplankton, Moriarty and O'Brien, 2013). Note that model output is annual average from 0 to 50 m; right column is compilation of all MAREDAT data in 5° bins between 0 and 50 m and does not represent an annual average.



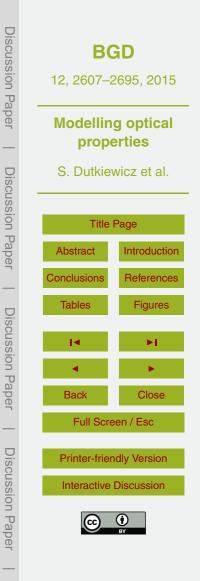


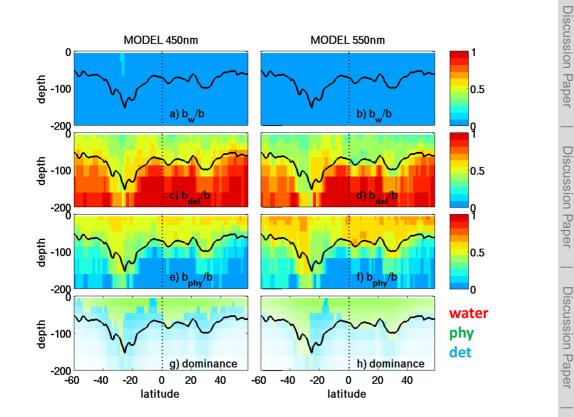
**Figure 13.** Comparison of model phytoplankton type dominate type with dominant type found from PHYSAT (Alvain et al., 2008) satellite derived product for **(a, b)** January and **(c, d)** July. Note that Haptophytes and *Phaeocystis* are not specifically resolved in the model, so are only shown in the PHYSAT plots. Coccolithophores (a subset of Haptophytes) and pico-eukaryotes are not resolved by the PHYSAT algorithm, so are only shown in the model results.



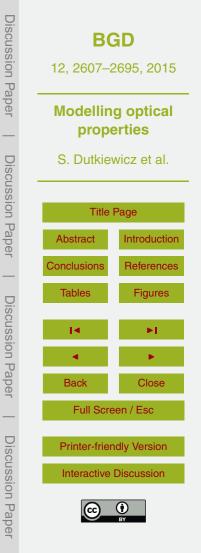


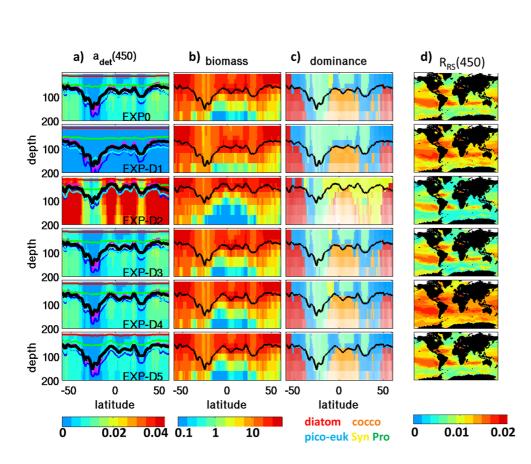
**Figure 14.** Model output along extended AMT-15 transect (annual mean) of (**a**–**h**) ratio of optical constituents contribution to total absorption: (**a**) water molecules,  $a_w/a$  at 450 nm; (**b**)  $a_w/a$  at 550 nm; (**c**) detrital matter,  $a_{det}/a$  at 450 nm; (**d**)  $a_{det}/a$  at 550 nm; (**e**) CDOM,  $a_{cdom}/a$  at 450 nm; (**f**)  $a_{cdom}/a$  at 550 nm; (**g**) total phytoplankton,  $a_{phy}/a$  at 450 nm; (**h**)  $a_{phy}/a$  at 550 nm. Dominant absorption constituent is shown in (**i**) for 450 nm and (**j**) for 550 nm: blue =  $a_{det}$ ; green =  $a_{phy}$ ; orange =  $a_{cdom}$ ; red =  $a_w$ . In (**i** and **j**) the opacity is scaled by the log of the total PAR.

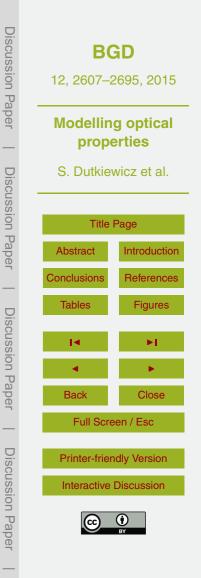




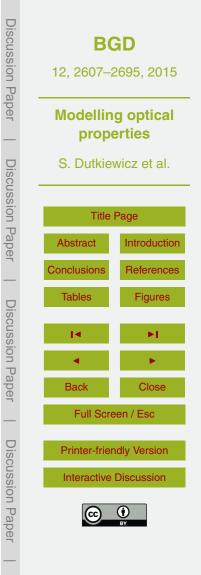
**Figure 15.** Model output along extended AMT-15 transect (annual mean) of (**a**–**f**) ratio of optical constituents contribution to total scattering: (**a**) water molecules,  $b_w/b$  at 450 nm; (**b**)  $b_w/b$  at 550 nm; (**c**) detrital matter,  $b_{det}/b$  at 450 nm; (**d**)  $b_{det}/b$  at 550 nm; (**e**) total phytoplankton,  $b_{phy}/b$  at 450 nm; (**f**)  $b_{phy}/b$  at 550 nm. Dominant scattering constituent is shown in (**g**) for 450 nm and (**h**) for 550 nm: blue =  $b_{det}$ ; green =  $b_{phy}$ . In (**g** and **h**) opacity is scaled by the log of the total PAR.

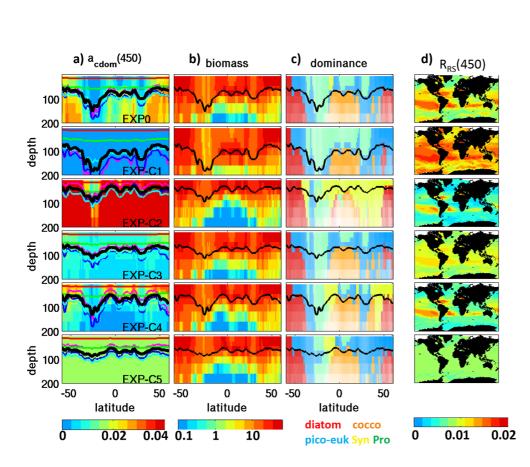






**Figure 16.** Detritus sensitivity experiments. **(a)** Absorption by detritus  $(a_{det}, units m^{-1})$  at 450 nm with 1% total light contour (black line) and for 400, 450, 500, 550, 600 nm wavebands (purple, dark blue, light blue, green, red). **(b)** Total phytoplankton biomass  $(mgCm^{-3})$ . **(c)** Dominant phytoplankton type (red = diatom, orange = coccolithophores, blue = pico-eukaryotes, yellow = *Synechococcus*, green = *Prochlorococcus*; opacity represents the total biomass). **(d)** 450 nm remotely sensed reflectance (sr<sup>-1</sup>). Black line in (**b** and **c**) indicated the 1% total irradiance contour. Each row represents a different experiment. EXP0 is the default experiment showcased in the earlier text. EXP-D1 = no  $a_{det}$ ; EXP-D3 =  $4 \cdot a_{det}$ ; EXP-D3 = no  $b_{det}$ ; EXP-D4 =  $4 \cdot b_{det}$ ; EXP-D5 =  $a_{det}$  parameterized as function of POC concentration.







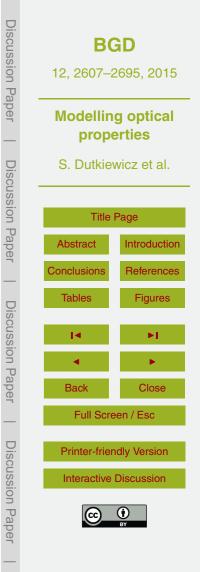
**Discussion** Paper

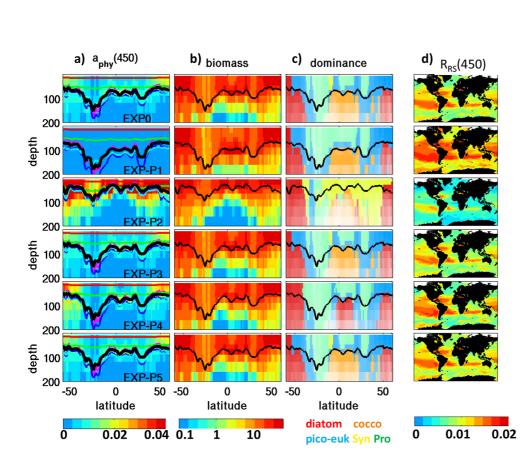
**Discussion** Paper

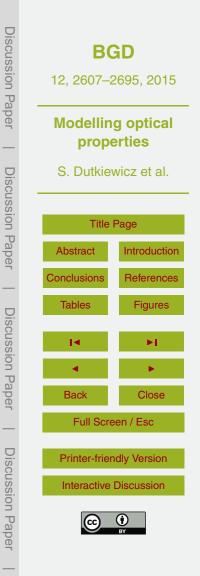
**Discussion Paper** 

**Discussion** Paper

**Figure 17.** CDOM sensitivity experiments. **(a)** Absorption by CDOM ( $a_{cdom}$ , units  $1m^{-1}$ ) at 450 nm with 1% total irradiance contour (black line) and for 400, 450, 500, 550, 600 nm wavebands (purple, dark blue, light blue, green, red). **(b)** Ttotal phytoplankton biomass (mgCm<sup>-3</sup>). **(c)** Dominant phytoplankton type (red = diatom, orange = coccolithophores, blue = pico-eukaryotes, yellow = *Synechococcus*, green = *Prochlorococcus*; opacity represents the total biomass). **(d)** 450 nm remotely sensed reflectance (sr<sup>-1</sup>). Black line in (**b** and **c**) indicated the 1% total irradiance contour. Each row represents a different experiment. EXP0 is the default experiment showcased in the earlier text. EXP-C1 = no  $a_{cdom}$ ; EXP-C2 =  $4 \cdot a_{cdom}$ ; EXP-C3 =  $a_{cdom}$  a function of Chl *a*; EXP-C4 =  $a_{cdom}$  a function of DOM; EXP-C5 =  $a_{cdom}$  uniform.







**Figure 18.** Phytoplankton sensitivity experiments. **(a)** Absorption by phytoplankton  $(a_{phy})$ , units  $m^{-1}$  at 450 nm with 1% total irradiance contour (black line) and for 400, 450, 500, 550, 600 nm wavebands (purple, dark blue, light blue, green, red). **(b)** Total phytoplankton biomass (mg C m<sup>-3</sup>). **(c)** Dominant phytoplankton type (red = diatom, orange = coccolithophores, blue = pico-eukaryotes, yellow = *Synechococcus*, green = *Prochlorococcus*; opacity represents the total biomass). **(d)** 450 nm remotely sensed reflectance (sr<sup>-1</sup>). Black line (**b** and **c**) indicated the 1% total irradiance contour. Each row represents a different experiment. EXP0 is the default experiment showcased in the earlier text. EXP-P1 = no  $a_{phy}$ ; EXP-P2 =  $4 \cdot a_{phy}$ ; EXP-P3 = no  $b_{phy}$ ; EXP-P4 =  $a_{phy}^{chl}$  spectrum mean for all phytoplankton; EXP-P5 =  $b_{phy}^{C}$  spectrum mean for all phytoplankton.

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