

1 **Soil nutrient competitive traits of plants, microbes, and mineral surfaces explain**  
2 **nutrient acquisition in tropical experimental manipulations**

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7 **Abstract**

8 Soil is a complex system where biotic (*e.g.*, plant roots, micro-organisms) and  
9 abiotic (*e.g.*, mineral surfaces) consumers compete for resources necessary for life (*e.g.*,  
10 nitrogen, phosphorus). This competition is ecologically significant, since it regulates the  
11 dynamics of soil nutrients and controls aboveground plant productivity. Here we develop,  
12 calibrate, and test a nutrient competition model that accounts for multiple soil nutrients  
13 interacting with multiple biotic and abiotic consumers. As applied here for tropical  
14 forests, the Nutrient Competition model (N-COM) includes three primary soil nutrients  
15 ( $\text{NH}_4^+$ ,  $\text{NO}_3^-$ , and  $\text{PO}_x$  (representing the sum of  $\text{PO}_4^{3-}$ ,  $\text{HPO}_4^{2-}$ , and  $\text{H}_2\text{PO}_4^-$ )) and five  
16 potential competitors (plant roots, decomposing microbes, nitrifiers, denitrifiers, and  
17 mineral surfaces). The competition is formulated with a quasi-steady-state chemical  
18 equilibrium approximation to account for substrate (multiple substrates share one  
19 consumer) and consumer (multiple consumers compete for one substrate) effects. N-  
20 COM successfully reproduced observed soil heterotrophic respiration,  $\text{N}_2\text{O}$  emissions,  
21 free phosphorus, sorbed phosphorus, and  $\text{NH}_4^+$  pools at a tropical forest site (Tapajos).  
22 The overall model uncertainty was moderately well constrained. Our sensitivity analysis  
23 revealed that soil nutrient competition was primarily regulated by consumer-substrate

24 affinity rather than environmental factors such as soil temperature or soil moisture. Our  
25 results also imply that under strong nutrient limitation, relative competitiveness depends  
26 strongly on the competitor functional traits (affinity and nutrient carrier enzyme  
27 abundance). We then applied the N-COM model to analyze field nitrogen and  
28 phosphorus perturbation experiments in two tropical forest sites (in Hawaii and Puerto  
29 Rico) not used in model development or calibration. Under soil inorganic nitrogen and  
30 phosphorus elevated conditions, the model accurately replicated the experimentally  
31 observed competition among nutrient consumers. Although we used as many  
32 observations as we could obtain, more nutrient addition experiments in tropical systems  
33 would greatly benefit model testing and calibration. In summary, the N-COM model  
34 provides an ecologically consistent representation of nutrient competition appropriate for  
35 land BGC models integrated in Earth System Models.

## 36 **1 Introduction**

37 Atmospheric CO<sub>2</sub> concentrations have risen sharply since the pre-industrial era,  
38 primarily due to anthropogenic fossil fuel combustion and land use and land cover  
39 change [Houghton, 2003; Le Quéré et al., 2013; Marland et al., 2003]. Terrestrial  
40 ecosystems mitigate the increasing atmospheric CO<sub>2</sub> trend by absorbing roughly a quarter  
41 of anthropogenic CO<sub>2</sub> emissions [Le Quéré et al., 2009]. However, it is still an open  
42 question whether the terrestrial CO<sub>2</sub> sink can be sustained [Sokolov et al., 2008; Zaehle et  
43 al., 2010], given that plant productivity is generally limited by soil nutrients [Elser et al.,  
44 2007; LeBauer and Treseder, 2008; Vitousek and Howarth, 1991] and soil nutrients could  
45 be quickly depleted through biogeochemical [Chauhan et al., 1981; Nordin et al., 2001;  
46 Shen et al., 2011] and hydrological [Dise and Wright, 1995; Perakis and Hedin, 2002]  
47 processes. Therefore, a holistic representation of soil nutrient dynamics is critically  
48 important to model the responses of terrestrial ecosystem CO<sub>2</sub> uptake to climate change.

49 Until recently, land models integrated in Earth System Models (ESMs) have  
50 largely ignored the close coupling between soil nutrient dynamics and the carbon cycle,  
51 although the impacts of soil nutrients (primarily Nitrogen and Phosphorus) regulating  
52 carbon-climate feedback are clearly required in ecosystem biogeochemistry and land  
53 models [Zaehle and Dalmonch, 2011; Zhang et al., 2011]. For example, none of the land  
54 models in C<sup>4</sup>MIP (Coupled Climate Carbon Cycle Model Intercomparison Project phase  
55 4) had coupled Carbon and Nitrogen dynamics [Friedlingstein et al., 2006]. The current  
56 generation of CMIP5 [Anav et al., 2013] models used for the recent IPCC  
57 (Intergovernmental Panel on Climate Change) assessment had only two members  
58 (CLM4CN: Thornton et al. [2007]; and BNU-ESM: [Ji et al., 2014]) that considered

59 nitrogen regulation of terrestrial carbon dynamics. However, as discussed below, several  
60 recent studies have shown that these models had large biases in most of the individual  
61 processes important for simulating nutrient dynamics. We therefore believe that, at the  
62 global scale, no credible representation of nutrient constraints on terrestrial carbon  
63 cycling yet exists in ESMs.

64 Further, none of the CMIP5 ESMs included a phosphorus cycle, which is likely  
65 important for tropical forest carbon budgets [*Vitousek and Sanford, 1986*]. The recent  
66 IPCC report highlights the importance of nitrogen and phosphorus availability on land  
67 carbon storage, even though the phosphorus limitation effect is uncertain [*Stocker et al.,*  
68 2013]. Since the next generation of ESMs participating in the CMIP6 synthesis will  
69 continue to focus on the impacts of a changing climate on terrestrial CO<sub>2</sub> and abiotic  
70 exchanges with the atmosphere [*Provides, 2014*], developing ecologically realistic and  
71 observationally-constrained representations of soil nutrient dynamics and carbon-nutrient  
72 interactions in ESMs is critical.

73 The importance of nutrient limitations in terrestrial ecosystems has been widely  
74 demonstrated by nitrogen and phosphorus fertilization experiments [*Elser et al., 2007*].  
75 For instance, plant Net Primary Production (NPP) is enhanced in plots with nutrient  
76 addition [*LeBauer and Treseder, 2008*]. Similarly, plant growth can be stimulated due to  
77 atmospheric nitrogen deposition [*Matson et al., 2002*]. Boreal forests are strongly limited  
78 by nitrogen availability [*Vitousek and Howarth, 1991*], because low temperatures reduce  
79 nitrogen mineralization [*Bonan and Cleve, 1992*] and N<sub>2</sub> fixation [*DeLuca et al., 2008*;  
80 *DeLuca et al., 2002*]. In contrast, tropical forests are often phosphorus limited [*Vitousek*  
81 *et al., 2010*], since tropical soils are old and phosphorus derived from parent material

82 weathering has been depleted through long-term pedogenesis processes [*Vitousek and*  
83 *Farrington, 1997; Walker and Syers, 1976*]. In natural ecosystems without external  
84 nutrients inputs (*e.g.*, N deposition), soil nitrogen or phosphorus (or both) are likely  
85 insufficient to satisfy both plant and microorganism demands [*Vitousek and Farrington,*  
86 *1997*]. Plants have to compete with microorganisms and mineral surfaces [*Kaye and*  
87 *Hart, 1997; Schimel et al., 1989*] to obtain sufficient nutrients to sustain their biological  
88 processes (*e.g.*, photosynthesis, respiration). Therefore, it is critical to improve the  
89 representation of nutrient competition to accurately model how terrestrial ecosystems will  
90 respond to perturbations in soil nutrient dynamics (*e.g.*, from elevated nitrogen deposition  
91 or CO<sub>2</sub> fertilization-induced nutrient requirements).

92 Intense competition between plants and microorganisms is a well-observed  
93 phenomenon in nutrient-limited systems [*Hodge et al., 2000a; Johnson, 1992; Kaye and*  
94 *Hart, 1997*]. Previously, plants were thought to be initial losers in nutrient competition,  
95 due to the fact that microbes are more intimately associated with substrates [*Woodmansee*  
96 *et al., 1981*]. However, increasing observational evidence indicates that plants compete  
97 effectively with soil microorganisms [*Schimel and Bennett, 2004*] under certain  
98 circumstances; sometime even outcompeting them and suppressing microbial growth [*Hu*  
99 *et al., 2001; J Wang and Lars, 1997*]. <sup>15</sup>N isotope studies have also demonstrated that  
100 plants can capture a large fraction of added nitrogen [*Hodge et al., 2000b; Marion et al.,*  
101 *1982*]. In the short term (days to months), plants maintain their competitiveness mainly  
102 through (1) establishing mycorrhizal fungi associations [*Drake et al., 2011; Rillig et al.,*  
103 *1998*], which help plants acquire organic and inorganic forms of nitrogen [*Hobbie and*  
104 *Hobbie, 2006; Hodge and Fitter, 2010*] and (2) root exudation of extracellular enzymes

105 that decompose rhizosphere soil organic matter [Phillips *et al.*, 2011]. In the relatively  
106 longer term (months to years), morphological adjustment occurs; for example, plants  
107 allocate more carbon to fine roots to explore laterally and deeper [Iversen *et al.*, 2011;  
108 Jackson *et al.*, 2009]. Finally, over the course of years to decades, plant succession can  
109 occur [Medvigy *et al.*, 2009; Moorcroft *et al.*, 2001] and the new plant demography will  
110 need to be considered to represent nutrient controls on this time scale.

111         Given these patterns from the observational literature, nutrient competition is  
112 either absent or over-simplified in existing Earth System Models (ESMs). One common  
113 representation of plant-microbe competition is that plants compete poorly against  
114 microbes in resource acquisition. For example, the O-CN land model [Zaehle and Friend,  
115 2010] assumes that soil decomposing microbes have the priority to immobilize soil  
116 mineral nitrogen. After microbes meet their demands, the remaining nitrogen is then  
117 available for plant uptake.

118         Another treatment in ESM land models is that microbial and plant nutrient  
119 acquisition competitiveness is based on their relative demands. For example, CLM4CN  
120 [Thornton *et al.*, 2007] assumes that the plant and microbial nitrogen demands are  
121 satisfied simultaneously. Under nitrogen infertile conditions, all nitrogen demands in the  
122 system are down-regulated proportional to the individual demands and subject to  
123 available soil mineral nitrogen. This approach led to unrealistic diurnal cycles of gross  
124 primary production (GPP), with midday depressions in GPP occurring because of  
125 predicted diurnal depletion of the soil mineral nitrogen pool. Emergent impacts of this  
126 conceptualization of nutrient constraints on GPP resulted in poor predictions compared to  
127 observations, with smaller than observed plant C growth responses to N deposition

128 [*Thomas et al.*, 2013a] and larger than observed responses to N fertilization [*Thomas et*  
129 *al.*, 2013b]. Further, most biogeochemistry models not integrated in ESMs also adopt one  
130 of these approaches. For instance, Biome-BGC [*Running and Coughlan*, 1988],  
131 CENTURY [*Parton et al.*, 1988], CASA (Carnegie-Ames-Stanford Approach; [*Potter et*  
132 *al.*, 1993]) and the Terrestrial Ecosystem Model - TEM [*McGuire et al.*, 1992] assume  
133 that available nutrients preferentially satisfy the soil microbial immobilization demand.

134         We believe the two conceptualizations of competition used in ESMs substantially  
135 over-simplify competitive interactions between plants and microbes and lead to biases in  
136 carbon cycle predictions. To begin to address the problems with these simplified  
137 approaches, Tang and Riley (2013) showed that complex consumer-substrate networks  
138 can be represented with an approach (called Equilibrium Chemical Approximation (ECA)  
139 kinetics) that simultaneously resolves multiple demands for multiple substrates, and  
140 demonstrated that the approach was consistent with observed litter decomposition  
141 observations. ECA kinetics has also recently been applied to analyze the emergent  
142 temperature response of SOM decomposition, considering equilibrium, non-equilibrium,  
143 and enzyme temperature sensitivities and abiotic interactions with mineral surfaces [*Tang*  
144 *and Riley*, 2014]. We extend on that work here by presenting an implementation of ECA  
145 kinetics to represent competition for multiple soil nutrients in a multiple consumer  
146 environment. We note that this paper demonstrates a method to handle instantaneous  
147 competition in the complex soil-plant network, but a robust competition representation  
148 for climate-scale models will require representation of dynamic changes in plant  
149 allocation and plant composition.

150           The aim of this study is to provide a reliable nutrient competition approach  
151 applicable for land models integrated in ESMs. However, before integration into an ESM,  
152 the competition model needs to be carefully calibrated and independently tested against  
153 observational data. This paper will therefore focus on model development and evaluation  
154 at several tropical forest sites where observations are available. Our objectives are to: (1)  
155 develop a soil biogeochemistry model with multiple nutrients (*i.e.*,  $\text{NH}_4^+$ ,  $\text{NO}_3^-$ , and  $\text{PO}_x$   
156 (represented as the sum of  $\text{PO}_4^{3-}$ ,  $\text{HPO}_4^{2-}$ , and  $\text{H}_2\text{PO}_4^-$ )) and multiple nutrient consumers  
157 (*i.e.*, decomposing microbes, plants, nitrifiers, denitrifiers, and mineral surfaces)  
158 competition using ECA kinetics [*Tang and Riley, 2013; Zhu and Riley, 2015*]; (2)  
159 constrain the model with *in situ* observational datasets of soil carbon, nitrogen, and  
160 phosphorus dynamics using a Markov Chain Monte Carlo (MCMC) approach; and (3)  
161 test model performance against nitrogen and phosphorus fertilization studies.



## 162 2 Method

### 163 2.1 Model development

164 The Nutrient COMpetition model (N-COM) is designed as a soil biogeochemistry  
165 model (Figure 1) to simulate soil carbon decomposition, nitrogen and phosphorus  
166 transformations, abiotic interactions, and plant demands. Although our ultimate goal is to  
167 incorporate N-COM into a decomposition model that represents active microbial activity  
168 as the primary driver of decomposition, we start here by presenting the N-COM approach  
169 using a Century-like [Koven *et al.*, 2013; Parton *et al.*, 1988] structure, with additions to  
170 account for phosphorus dynamics. In our approach, we calculate potential immobilization  
171 using literature-derived parameters (*e.g.*,  $V_{MAX}$ ,  $K_M$ ) in a Michaelis-Menten (MM)  
172 kinetics framework. The potential immobilization is subsequently modified using the  
173 ECA competition method.

174 Five pools of soil organic Carbon (C), Nitrogen (N), and Phosphorus (P) are  
175 considered: Coarse Wood Debris (CWD), litter, fast Soil Organic Matter (SOM) pool,  
176 medium SOM pool, and slow SOM pool. Litter is further divided into three sub-groups:  
177 metabolic, cellulose, and lignin. The soil organic C, N, and P decomposition ( $F_{C,j}^{dec}$ ,  $F_{N,j}^{dec}$ ,  
178  $F_{P,j}^{dec}$ ) follow first-order decay:

$$179 F_{C,j}^{dec} = k_j C_j r_{\theta} r_T \quad (1)$$

$$180 F_{N,j}^{dec} = k_j N_j r_{\theta} r_T \quad (2)$$

$$181 F_{P,j}^{dec} = k_j P_j r_{\theta} r_T \quad (3)$$

182 where  $k_j$  is the rate constant of soil organic matter decay ( $s^{-1}$ );  $C_j$ ,  $N_j$ , and  $P_j$  are pool  
183 sizes ( $g\ m^{-2}$ ) of carbon, nitrogen, and phosphorus, respectively ( $j$  from 1 to 7 represents  
184 the soil organic matter pools: CWD, metabolic litter, cellulose litter, lignin litter, fast

185 SOC, median SOC, slow SOC);  $r_t$  and  $r_o$  (dimensionless) are soil temperature and  
 186 moisture environmental regulators.

187 Decomposed carbon ( $F_{C,i}^{dec}$ ) (upstream  $i^{th}$  pool) either (1) enters a downstream  
 188 pool ( $j^{th}$ ) or (2) is lost as CO<sub>2</sub>. Soil organic carbon (downstream  $j^{th}$  pool) temporal change  
 189 is calculated as:

$$190 \quad \frac{dC_j}{dt} = -F_{C,j}^{dec} + \sum_{i=1}^N F_{C,ij}^{move} \quad (4)$$

191 where  $\sum_{i=1}^N F_{C,ij}^{move}$  is the summation of carbon fluxes that move from the upstream pool ( $i$ )  
 192 to the downstream pool ( $j$ ) due to the decomposition of upstream SOC. For each  
 193 upstream carbon pool ( $i = 1, 2, \dots, 7$ ), the fractions integrated into downstream pools ( $j =$   
 194  $1, 2, \dots, 7$ ) is summarized in a  $7 \times 7$  matrix  $f_{ij}$  (Table 2). The percentage of decomposed  
 195 carbon that is respired as CO<sub>2</sub> is represented by  $g_i$  (Table 2). Simultaneously, soil organic  
 196 N and P changes follow C decomposition:

$$197 \quad \frac{dN_j}{dt} = -F_{N,j}^{dec} + \sum_{i=1}^N F_{N,ij}^{move} + \sum_{i=1}^N F_{NH4,ij}^{immob} + \sum_{i=1}^N F_{NO3,ij}^{immob} \quad (5)$$

$$198 \quad \frac{dP_j}{dt} = -F_{P,j}^{dec} + \sum_{i=1}^N F_{P,ij}^{move} + \sum_{i=1}^N F_{P,ij}^{immob} \quad (6)$$

199 where  $F_{N,ij}^{move}$  and  $F_{P,ij}^{move}$  are fluxes of nitrogen and phosphorus moving from the upstream  
 200 ( $i$ ) to downstream ( $j$ ) pools.  $F_{NH4,ij}^{immob}$ ,  $F_{NO3,ij}^{immob}$ , and  $F_{P,ij}^{immob}$  are immobilization fluxes of soil  
 201 mineral nitrogen and phosphorus.  $F_{N,j}^{dec}$  and  $F_{P,j}^{dec}$  represent soil organic matter  
 202 decomposition losses.

203 Equations (5) and (6) state that changes in the  $j^{th}$  organic N or P pool are the  
 204 summation of three terms: (1) organic N and P lost during soil organic matter  
 205 mineralization ( $-F_{N,j}^{dec}$  and  $-F_{P,j}^{dec}$ ); (2) a fraction of the  $i^{th}$  organic N or P pool (upstream)  
 206 enters into the  $j^{th}$  pool (downstream) ( $F_{N,ij}^{move}$  and  $F_{P,ij}^{move}$ ); and (3) soil microbial  
 207 immobilization ( $F_{NH_4,ij}^{immob}$ ,  $F_{NO_3,ij}^{immob}$ , and  $F_{P,ij}^{immob}$ ). Immobilization occurs only when the newly  
 208 entering organic N is insufficient to sustain the soil C:N (or C:P) ratio (more details  
 209 described in Appendix A).

210 The inorganic nitrogen pools ( $NH_4^+$  and  $NO_3^-$  (Eqn. 7 -8)) are altered by  
 211 production (organic N mobilized by microbes), consumption (uptake by plants and  
 212 microbes, gaseous or aqueous losses), and transformation (nitrification and  
 213 denitrification). Inorganic P ( $PO_x$ ) is assumed to be either taken up by plants and  
 214 decomposing microbes or adsorbed to mineral surfaces (Eqn. 9). Plants utilize all forms  
 215 of phosphate (e.g.,  $PO_4^{3-}$ ,  $HPO_4^{2-}$ , and  $H_2PO_4^-$ ), but for simplicity we use the symbol  $PO_x$   
 216 to represent the sum of all possible phosphate forms throughout the paper.

$$217 \frac{d[NH_4]}{dt} = \sum_{j=1}^N \sum_{i=1}^N F_{NH_4,ij}^{mob} - F_{NH_4}^{nit} - F_{NH_4}^{plant} - F_{NH_4}^{immob} + F^{BNF} + F_{NH_4}^{dep} \quad (7)$$

$$218 \frac{d[NO_3]}{dt} = -F_{NO_3}^{den} + (1 - f^{N_2O})F_{NH_4}^{nit} - F_{NO_3}^{plant} - F_{NO_3}^{immob} - F_{NO_3}^{leach} + F_{NO_3}^{dep} \quad (8)$$

$$219 \frac{d[PO_x]}{dt} = \sum_{j=1}^N \sum_{i=1}^N F_{P,ij}^{mob} - F_P^{plant} - F_P^{immob} - F_P^{surf} - F_P^{leach} + F^{weather} \quad (9)$$

220 where  $F_{NH_4,ij}^{mob}$  and  $F_{P,ij}^{mob}$  are gross mineralization rates for nitrogen and phosphorus.  $F_{NH_4}^{nit}$   
 221 is the nitrification flux, part of which is lost through a gaseous pathway ( $f^{N_2O}$ ) and the  
 222 rest is incorporated into the  $NO_3^-$  pool.  $F_{NO_3}^{den}$  is the denitrification flux, which transforms  
 223 nitrate to  $N_2O$  and  $N_2$  which then leave the soil system. Plant uptake of soil  $NH_4^+$ ,  $NO_3^-$ ,

224 and  $PO_x$  are represented as  $F_{NH_4}^{plant}$ ,  $F_{NO_3}^{plant}$ , and  $F_P^{plant}$ , respectively. Soil decomposing  
 225 microbial immobilization of soil  $NH_4^+$ ,  $NO_3^-$ , and  $PO_x$  are represented as  $F_{NH_4}^{immob}$ ,  $F_{NO_3}^{immob}$ ,  
 226 and  $F_P^{immob}$ .  $F_{NO_3}^{leach}$ , and  $F_P^{leach}$  are leaching losses of soil  $NO_3^-$  and  $PO_x$ . External inputs  
 227 into soil inorganic N pools include atmospheric ammonia deposition ( $F_{NH_4}^{dep}$ ), atmospheric  
 228 nitrate deposition ( $F_{NO_3}^{dep}$ ), and biological nitrogen fixation ( $F^{BNF}$ ). External sources of  
 229 phosphate come from parent material weathering ( $F^{weather}$ ).

230 Finally, the dynamics of sorbed P ( $P_S$ ), occluded P ( $P_O$ ), and parent material P (  
 231  $P_P$ ) are modeled as:

$$232 \frac{d[P_S]}{dt} = F_P^{surf} - F_P^{occl} \quad (10)$$

$$233 \frac{d[P_O]}{dt} = F_P^{occl} \quad (11)$$

$$234 \frac{d[P_P]}{dt} = -F^{weather} + F_P^{dep} \quad (12)$$

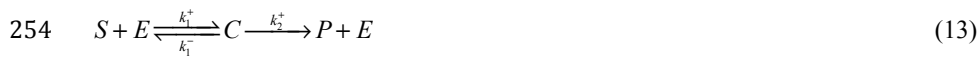
235 where the pool of sorbed P is balanced by the adsorption flux ( $F_P^{surf}$ ) and occlusion flux (  
 236  $F_P^{occl}$ ). Parent material is lost by weathering ( $F^{weather}$ ) and is slowly replenished by  
 237 external atmospheric phosphorus inputs ( $F_P^{dep}$ , such as dust). More detailed information  
 238 on the modeled C, N, and P fluxes is documented in Appendix A.

## 239 **2.2 Multiple-consumer-multiple-resource competition network**

240 The soil biogeochemistry model presented in **section 2.1** has multiple potential  
 241 nutrient consumers (plants, SOM decomposing microbes, nitrifiers, denitrifiers, mineral  
 242 surfaces) and multiple soil nutrients ( $NH_4^+$ ,  $NO_3^-$ ,  $PO_x$ ). The consumer-resource network  
 243 is summarized in Table 1. As in many land BGC models (CLM, Century, *etc.*), we have

244 not explicitly included the mineral surface adsorptions of  $\text{NH}_4^+$  and  $\text{NO}_3^-$ , since we  
 245 assume ammonia is quickly protected by mineral surfaces from leaching (no leaching  
 246 term in Eqn. 7) but then released for plant and microbial uptake when the biotic demand  
 247 arises. An improved treatment of these dynamics would necessitate a prognostic model  
 248 for pH, which is beyond the scope of this analysis. Unlike sorbed P (which can be  
 249 occluded), there is no further abiotic loss of sorbed ammonia. Therefore, the free  
 250 ammonia pool is interpreted in the current model structure as a potential free ammonia  
 251 pool (free + sorbed).

252 Competition between different consumers in acquiring different resources is  
 253 summarized in Table 1. Each consumer-substrate competition reaction is represented by:



255 The enzyme ( $E$ : e.g., *nutrient carrier enzyme produced by plants and microbes*)  
 256 and substrate ( $S$ : e.g.,  $\text{NH}_4^+$ ,  $\text{NO}_3^-$ ) reaction (reversible reaction) forms a substrate-  
 257 enzyme complex ( $C$ ). The following irreversible reaction leads to product ( $P$ : *meaning*  
 258 *the nutrients has been taken up*) and releases enzyme ( $E$ ) back into soil media. For the  
 259 whole complex reaction network, nutrient uptakes are formulated as:

$$260 \quad F_{\text{NH}_4}^{\text{plant}} = k_{\text{NH}_4}^{\text{plant}} \cdot \frac{[\text{NH}_4] \cdot [E_N^{\text{plant}}]}{K_M^{\text{plant, NH}_4} \left( 1 + \frac{[\text{NH}_4]}{K_M^{\text{plant, NH}_4}} + \frac{[\text{NO}_3]}{K_M^{\text{plant, NO}_3}} + \frac{[E_N^{\text{plant}}]}{K_M^{\text{plant, NH}_4}} + \frac{[E_N^{\text{mic}}]}{K_M^{\text{mic, NH}_4}} + \frac{[E_N^{\text{nit}}]}{K_M^{\text{nit, NH}_4}} \right)} \quad (14)$$

$$261 \quad F_{\text{NH}_4}^{\text{immob}} = k_{\text{NH}_4}^{\text{immob}} \cdot \frac{[\text{NH}_4] \cdot [E_N^{\text{mic}}]}{K_M^{\text{mic, NH}_4} \left( 1 + \frac{[\text{NH}_4]}{K_M^{\text{mic, NH}_4}} + \frac{[\text{NO}_3]}{K_M^{\text{mic, NO}_3}} + \frac{[E_N^{\text{plant}}]}{K_M^{\text{plant, NH}_4}} + \frac{[E_N^{\text{mic}}]}{K_M^{\text{mic, NH}_4}} + \frac{[E_N^{\text{nit}}]}{K_M^{\text{nit, NH}_4}} \right)} \quad (15)$$

$$262 \quad F_{\text{NH}_4}^{\text{nit}} = k_{\text{NH}_4}^{\text{nit}} \cdot \frac{[\text{NH}_4] \cdot [E_{\text{NH}_4}^{\text{nit}}]}{K_M^{\text{nit, NH}_4} \left( 1 + \frac{[\text{NH}_4]}{K_M^{\text{nit, NH}_4}} + \frac{[E_N^{\text{plant}}]}{K_M^{\text{plant, NH}_4}} + \frac{[E_N^{\text{mic}}]}{K_M^{\text{mic, NH}_4}} + \frac{[E_N^{\text{nit}}]}{K_M^{\text{nit, NH}_4}} \right)} \quad (16)$$

$$263 \quad F_{NO_3}^{plant} = k_{NO_3}^{plant} \cdot \frac{[NO_3] \cdot [E_N^{plant}]}{K_M^{plant,NO_3} \left( 1 + \frac{[NH_4]}{K_M^{plant,NH_4}} + \frac{[NO_3]}{K_M^{plant,NO_3}} + \frac{[E_N^{plant}]}{K_M^{plant,NO_3}} + \frac{[E_N^{mic}]}{K_M^{mic,NO_3}} + \frac{[E_N^{den}]}{K_M^{den,NO_3}} \right)} \quad (17)$$

$$264 \quad F_{NO_3}^{immob} = k_{NO_3}^{immob} \cdot \frac{[NO_3] \cdot [E_N^{mic}]}{K_M^{mic,NO_3} \left( 1 + \frac{[NH_4]}{K_M^{mic,NH_4}} + \frac{[NO_3]}{K_M^{mic,NO_3}} + \frac{[E_N^{plant}]}{K_M^{plant,NO_3}} + \frac{[E_N^{mic}]}{K_M^{mic,NO_3}} + \frac{[E_N^{den}]}{K_M^{den,NO_3}} \right)} \quad (18)$$

$$265 \quad F_{NO_3}^{den} = k_{NO_3}^{den} \cdot \frac{[NO_3] \cdot [E_{NO_3}^{den}]}{K_M^{den,NO_3} \left( 1 + \frac{[NO_3]}{K_M^{den,NO_3}} + \frac{[E_N^{plant}]}{K_M^{plant,NO_3}} + \frac{[E_N^{mic}]}{K_M^{mic,NO_3}} + \frac{[E_N^{den}]}{K_M^{den,NO_3}} \right)} \quad (19)$$

$$266 \quad F_P^{plant} = k_P^{plant} \cdot \frac{[PO_x] \cdot [E_P^{plant}]}{K_M^{plant,P} \left( 1 + \frac{[PO_x]}{K_M^{plant,P}} + \frac{[E_P^{plant}]}{K_M^{plant,P}} + \frac{[E_P^{mic}]}{K_M^{mic,P}} + \frac{[E_P^{surf}]}{K_M^{surf,P}} \right)} \quad (20)$$

$$267 \quad F_P^{mic} = k_P^{mic} \cdot \frac{[PO_x] \cdot [E_P^{mic}]}{K_M^{mic,P} \left( 1 + \frac{[PO_x]}{K_M^{mic,P}} + \frac{[E_P^{plant}]}{K_M^{plant,P}} + \frac{[E_P^{mic}]}{K_M^{mic,P}} + \frac{[E_P^{surf}]}{K_M^{surf,P}} \right)} \quad (21)$$

$$268 \quad F_P^{surf} = k_P^{surf} \cdot \frac{[PO_x] \cdot [E_P^{mic}]}{K_M^{surf,P} \left( 1 + \frac{[PO_x]}{K_M^{surf,P}} + \frac{[E_P^{plant}]}{K_M^{plant,P}} + \frac{[E_P^{mic}]}{K_M^{mic,P}} + \frac{[E_P^{surf}]}{K_M^{surf,P}} \right)} \quad (22)$$

269 where  $F$  represent the nutrient uptake fluxes and  $k$  is the base reaction rate that enzyme-  
 270 substrate complex forms product ( $k_2^+$  in Eqn. 13).  $[E]$  and  $K_M$  denote enzyme abundance  
 271 and half saturation constants (substrate-enzyme affinity). Superscripts and subscripts  
 272 refer to consumers and substrates, respectively. These equations account for the effect of  
 273 (1) multiple substrates (e.g.,  $NH_4^+$  and  $NO_3^-$ ) sharing one consumer, which inhibits the  
 274 effective binding between any specific substrate and the consumer (terms <sup>(1)</sup> and <sup>(2)</sup> in  
 275 Eqn. 14) and (2) multiple consumers (e.g., plants, decomposing microbes, and nitrifiers)

276 sharing one substrate (*e.g.*,  $\text{NH}_4^+$ ), which lowers the probability of effective binding  
 277 between any consumer and  $\text{NH}_4^+$  (terms <sup>(3)</sup>, <sup>(4)</sup>, and <sup>(5)</sup> in Eqn. 14).

278 For our reaction network (Eqn. 13 – 22), we assume that: (1) plant roots and  
 279 decomposing microbes possess two types of nutrient carrier enzymes (nutrient  
 280 transporters). One is for nitrogen ( $\text{NH}_4^+$  and  $\text{NO}_3^-$ ;  $E_N^{plant}, E_N^{mic}$ ), and the other is for  
 281 phosphorus, including different forms of phosphate ( $E_P^{plant}, E_P^{mic}$ ). (2) Nutrient carrier  
 282 enzyme abundance is scaled with biomass (fine root or microbial biomass). Scaling  
 283 factors are 0.0000125 (for plants) and 0.05 (for decomposing microbes) (Table 2). (3)  
 284 Mineral surface “effective enzyme” abundance ( $E_p^{surf}$ ) is approximated by the available  
 285 sorption surface area ( $VMAX_p^{surf} - [SP]$ ). (4) Nitrifiers and denitrifiers are not explicitly  
 286 simulated, therefore we assume that their biomass and associated nutrient transporter  
 287 abundance are fixed ( $E_N^{nit}, E_N^{denit}$ ).

288 For simplicity, we group the “decomposing microbes/nitrifier/denitrifier/mineral  
 289 surface nutrient carrier enzyme [ $E$ ]” and their “base reaction rate  $k$ ” into one single  
 290 variable “ $VMAX$ ” (see Appendix B for full derivation). Furthermore, we defined  
 291 “potential rates (potential immobilization, nitrification, denitrification, adsorption rates)”  
 292 and used them as proxies of “ $VMAX$ ”. Therefore, Eqn. 15, 16, 18, 19, 21, 22 become:

293 
$$F_{NH4}^{immob} = F_{NH4}^{immob,pot} \cdot \frac{[NH4]}{K_M^{mic,NH4} \left( 1 + \frac{[NH4]}{K_M^{mic,NH4}} + \frac{[NO3]}{K_M^{mic,NO3}} + \frac{[E_N^{plant}]}{K_M^{plant,NH4}} + \frac{[E_N^{mic}]}{K_M^{mic,NH4}} + \frac{[E_N^{nit}]}{K_M^{nit,NH4}} \right)} \quad (23)$$

294 
$$F_{NH4}^{nit} = F_{NH4}^{nit,pot} \cdot \frac{[NH4]}{K_M^{nit,NH4} \left( 1 + \frac{[NH4]}{K_M^{nit,NH4}} + \frac{[E_N^{plant}]}{K_M^{plant,NH4}} + \frac{[E_N^{mic}]}{K_M^{mic,NH4}} + \frac{[E_N^{nit}]}{K_M^{nit,NH4}} \right)} \quad (24)$$

$$295 \quad F_{NO_3}^{immob} = F_{NO_3}^{immob,pot} \cdot \frac{[NO_3]}{K_M^{mic,NO_3} \left( 1 + \frac{[NH_4]}{K_M^{mic,NH_4}} + \frac{[NO_3]}{K_M^{mic,NO_3}} + \frac{[E_N^{plant}]}{K_M^{plant,NO_3}} + \frac{[E_N^{mic}]}{K_M^{mic,NO_3}} + \frac{[E_N^{den}]}{K_M^{den,NO_3}} \right)} \quad (25)$$

$$296 \quad F_{NO_3}^{den} = F_{NO_3}^{den,pot} \cdot \frac{[NO_3]}{K_M^{den,NO_3} \left( 1 + \frac{[NO_3]}{K_M^{den,NO_3}} + \frac{[E_N^{plant}]}{K_M^{plant,NO_3}} + \frac{[E_N^{mic}]}{K_M^{mic,NO_3}} + \frac{[E_N^{den}]}{K_M^{den,NO_3}} \right)} \quad (26)$$

$$297 \quad F_P^{mic} = F_P^{immob,pot} \cdot \frac{[PO_x]}{K_M^{mic,P} \left( 1 + \frac{[PO_x]}{K_M^{mic,P}} + \frac{[E_P^{plant}]}{K_M^{plant,P}} + \frac{[E_P^{mic}]}{K_M^{mic,P}} + \frac{[E_P^{surf}]}{K_M^{surf,P}} \right)} \quad (27)$$

$$298 \quad F_P^{surf} = F_P^{surf,pot} \cdot \frac{[PO_x]}{K_M^{surf,P} \left( 1 + \frac{[PO_x]}{K_M^{surf,P}} + \frac{[E_P^{plant}]}{K_M^{plant,P}} + \frac{[E_P^{mic}]}{K_M^{mic,P}} + \frac{[E_P^{surf}]}{K_M^{surf,P}} \right)} \quad (28)$$

299           In this case, the potential rates are treated as maximum reaction rates (*VMAX*),  
300 because they are calculated without nutrient constraints or biotic and abiotic interactions.  
301 For example, potential P immobilization rate ( $F_P^{immob,pot}$ ) is based on the total phosphorus  
302 demand that can perfectly maintain the soil CP stoichiometry during soil organic matter  
303 decomposition (Eqn. A9). This potential immobilization rate represents the maximum  
304 phosphorus influx that the soil could take up at that moment. The maximum adsorption  
305 rate ( $F_P^{surf,pot}$ ) is the time derivative of the Langmuir equation (Eqn. A12), which is a  
306 theoretically maximal adsorption rate excluding all other biotic and abiotic interactions.  
307 The potential rates (*VMAX*) are updated by the model rather than calibrated, except for  
308  $VMAX_P^{surf}$ .  $VMAX_P^{surf}$  denotes the maximum adsorption capacity (not maximum  
309 adsorption rate), which affects the potential adsorption rate ( $F_P^{surf,pot}$ ).

310           The model is run on an hourly time step, initialized with state variables and  
311 critical parameters (Table 2). Since the model is designed to be a component of the



312 Community and ACME Land Models (CLM, ALM; which are essentially currently  
313 equivalent), we used CLM4.5 site-level simulations to acquire temporally-resolved: (1)  
314 soil temperature factors on decomposition ( $r_T$ ); (2) soil moisture factors on  
315 decomposition ( $r_\theta$ ); (3) the anoxic fraction of soil pores ( $f^{anox}$  in Appendix Eqn. A10-  
316 11); (4) annual NPP ( $NPP_{annual}$  in Appendix Eqn. A13); (5)  $\text{NH}_4^+$  deposition ( $F_{\text{NH}_4}^{dep}$ ); (6)  
317  $\text{NO}_3^-$  deposition ( $F_{\text{NO}_3}^{dep}$ ); and (7) hydrologic discharge ( $Q_{dis}$  in Appendix Eqn. A14).  
318 External inputs of mineral phosphorus are derived from Mahowald *et al.*, [2005, 2008].

### 319 **2.3 Model parameterization and sensitivity analysis**

320 We constrained model parameters and performed sensitivity analyses using a suite  
321 of observations distinct from the observations we used subsequently to test the model  
322 against the N and P manipulation experiments. Because tropical systems can be either  
323 nitrogen or phosphorous limited (or both) [Elser *et al.*, 2007; Vitousek *et al.*, 2010], we  
324 chose observations from a tropical forest site to constrain the N and P competition in our  
325 model (Tapajos National Forest, Para, Brazil (Table 3)).

326 In the parameter estimation procedure, several data streams are assimilated into  
327 the N-COM model, including measurements of soil  $\text{NH}_4^+$  concentrations, soil free  
328 phosphate concentrations, sorbed phosphate concentrations, and  $\text{N}_2\text{O}$  and  $\text{CO}_2$  flux  
329 measurements. The datasets are summarized in Table 3 and cover a wide range of N and  
330 P biogeochemistry dynamics. A set of model parameters is selected for calibration (Table  
331 4), which comprise nutrient competition kinetics parameters ( $k$  and  $K_M$ ) as well as the fast  
332 soil carbon turnover time ( $TURN_{SOM}$ ). Because we had only a short-term  $\text{CO}_2$  respiration  
333 flux record, we were unable to calibrate the longer turnover time parameters. However,  
334 since we test the calibrated model against short-term fertilization responses, this omission

335 will not affect our evaluation. Longer records from eddy covariance flux towers and <sup>14</sup>C  
336 soil measurements are required to constrain the longer turnover time pool values.

337 We employed the Markov Chain Monte Carlo (MCMC) approach [Ricciuto *et al.*,  
338 2008] to assimilate the observations into N-COM. MCMC directly draws samples from a  
339 pre-defined parameter space and tries to minimize a pre-defined cost function:

$$340 \quad J = (M(\theta) - D)^T R^{-1} (M(\theta) - D) \quad (29)$$

341 where  $M(\theta)$  and  $D$  are vectors of model outputs and observations including time series of  
342 different simulated variables (*e.g.*, soil CO<sub>2</sub> and N<sub>2</sub>O effluxes and soil concentrations of  
343 NH<sub>4</sub><sup>+</sup>, free PO<sub>x</sub>, and sorbed PO<sub>x</sub>);  $\theta$  is a vector of model parameters ( $\theta_i$ ); and  $i$  from 1 to  
344 20 represents the parameters that are calibrated (Table 4).  $R^{-1}$  is the inverse of data error  
345 covariance matrix. We assumed that diagonal elements are 40% of observed values and  
346 off-diagonal elements are zeros. We further assumed that the prior parameter follows a  
347 lognormal distribution.  $\mu$  and  $\sigma$  were 0.91 and 0.95 of their initial values, respectively  
348 (Table 4). We then ran MCMC to sample 50,000 parameter pairs (Fig. A1). The second  
349 half of the samples was fit to a Gaussian distribution. We also employed the Gelman-  
350 Rubin criterion to quantitatively show whether or not the MCMC chain converged. The  
351 calibrated model parameters are reported in term of means and standard deviations.  
352 Uncertainty Reduction ( $UR$ ) is calculated based on (1) variance (Eqn. 30a) and (2) 25%  
353 and 75% quantile (Eqn. 30b):

$$354 \quad UR_{\sigma} = \left(1 - \frac{\sigma_{posterior}}{\sigma_{prior}}\right) \cdot 100\% \quad (30a)$$

$$355 \quad UR_Q = \left(1 - \frac{Q_{posterior}^{75} - Q_{posterior}^{25}}{Q_{prior}^{75} - Q_{prior}^{25}}\right) \cdot 100\% \quad (30b)$$

356 where  $\sigma_{prior}$  is prior parameter uncertainty, which is 95% of the parameter initial value.  
357  $\sigma_{posterior}$  is calibrated parameter uncertainty, which is calculated by fitting the calibrated  
358 model parameters to a Gaussian distribution.  $Q^{75}$  and  $Q^{25}$  are 75% and 25% percentage  
359 quantile of each parameter. Uncertainty Reduction is a useful metric [Zhu and Zhuang,  
360 2014], because it quantitatively reveals the reduction in the range of a particular  
361 parameter after calibration with MCMC. It does not, however, indicate that the parameter  
362 itself is more consistent with observed values of the parameter. A large value of  $UR$   
363 implies a more robust model.

364 In addition, we conducted a sensitivity study to identify the dominant controlling  
365 factors regulating nutrient competition in N-COM. Three scenarios were considered: (1)  
366 baseline climate and soil conditions; (2) elevated soil temperature (by 5 °C); and (3)  
367 elevated soil moisture (by 50%). SOBOL sampling [Pappas *et al.*, 2013], a global  
368 sensitivity technique, is employed to calculate the sensitivities of output variables with  
369 respect to various inputs:

$$370 \quad S_i = \frac{VAR_{p_i} (E_{p_{-i}}(Y | p_i))}{VAR(Y)} \quad (31)$$

371 where  $S_i$  is the first order sensitivity index of the  $i^{th}$  parameter and ranges from 0 to 1. By  
372 comparing the values of  $S_i$ , we were able to evaluate which processes affect the pattern of  
373 nutrient competition.  $Y$  represents the model outputs of plant  $NH_4^+$ ,  $NO_3^-$ , or  $PO_x$  uptake;  
374  $p_i$  is the target parameter;  $p_{-i}$  denotes all parameters that are associated with nutrient  
375 competition except the target parameter; and  $VAR(.)$  and  $E(.)$  represent variance and  
376 mean, respectively.

#### 377 **2.4 Model application**

378 After calibration, we applied the N-COM model to several tropical forest nutrient  
379 fertilization studies not included in the calibration dataset, where isotopically labeled  
380 nitrogen or phosphorous fertilizer was injected into the soil. The fertilization experiments  
381 measured the fate of added nutrients; for example, identifying the fraction of added N or  
382 P that goes into the plant, is immobilized by microbes, or is stabilized by mineral  
383 surfaces. These measurements offer an effective baseline to test whether the N-COM  
384 model captures short-term nutrient competition.

385 Because we have focused in this paper on applications in tropical forests, we  
386 choose three tropical forest fertilization experiments with (1)  $\text{PO}_4^{3-}$ ; (2)  $\text{NH}_4^+$ ; and (3)  
387  $\text{NO}_3^-$  additions (Table 5). The  $\text{PO}_4^{3-}$  fertilization experiment [Olander and Vitousek,  
388 2005] was conducted in three Hawaiian tropical forests along a soil chronosequence (300,  
389 20000, and 4100000 year old soils) that were fertilized with  $10 \mu\text{g g}^{-1} {}^{32}\text{PO}_4^{3-}$ ,  
390 respectively, and microbial demand versus soil sorption was measured. We did not  
391 evaluate the role of plants in phosphorus competition for the Hawaii sites, since plant  
392 phosphorus uptake was not measured in those field studies. Our model discriminates the  
393 Hawaii sites along the chronosequence by setting distinct initial pool sizes (derived from  
394 [Olander and Vitousek, 2004; Olander and Vitousek, 2005]) of soil organic carbon,  
395 nitrogen and phosphorus, and soil parent material phosphorus.

396 We also used measurements from  $\text{NH}_4^+$  and  $\text{NO}_3^-$  fertilization studies located at  
397 the Luquillo tropical forest in Puerto Rico [Templer *et al.*, 2008]. In that study,  $4.6 \mu\text{g g}^{-1}$   
398  ${}^{15}\text{NH}_4^+$  was added into the highly weathered tropical forest soil and the consumption of  
399  ${}^{15}\text{NH}_4^+$  by plant roots, decomposing microbes, and nitrifiers were measured. In the same  
400 study,  $0.92 \mu\text{g g}^{-1} {}^{15}\text{NO}_3^-$  was added to the soil and the plant uptake and microbial

401 immobilization was measured. The measurements were made 24 or 48 hours after the  
402 fertilizers were added.

403 For the model scenarios, we (1) spun up the N-COM model for 100 years; (2)  
404 perturbed the soil nutrient pool by the same amount as the fertilization; (3) ran the model  
405 for 24 or 48 hours and calculated how much of the added nutrients were absorbed by  
406 plants, microbes, or mineral surfaces; and (4) compared our model simulations with the  
407 observed data to assess model predictability. The 100-year spin up simulation aimed at  
408 eliminating the effects of imposed initial inorganic pool sizes on fertilization  
409 experiments, rather than accumulating soil organic matter in the system, since we  
410 initialized the soil organic carbon pools from CLM4.5 steady state predictions.

411

### 412 **3. Results and discussion**

#### 413 **3.1 Calibrated model parameters**

414 Our best estimates (second half of the MCMC chain) of the selected model  
415 parameters based on the observations at the Tapajos National Forest, Para, Brazil are  
416 shown in Figure 2. We found that calibrated parameter samples were not heavily tailed  
417 and they generally follow Gaussian distributions (Figure A3). In order to quantitatively  
418 compare the calibrated parameter distributions with prior distributions, we fit parameter  
419 samples to a Gaussian distribution and estimated its means and standard deviations  
420 (Table 4).

421 Even though the parameter mean was improved, the uncertainty may still be  
422 relatively large. In other words, a prognostic prediction based on these calibrated  
423 parameters could be relatively uncertain [Scholze *et al.*, 2007], due to large uncertainty

424 associated with the calibrated parameters. Therefore, we calculated the variance-based  
425 Uncertainty Reduction ( $UR_\sigma$ ) (Eqn. 30a) to evaluate model improvement in terms of  
426 parameter uncertainty. We found that parameters' uncertainties were reduced by  
427 13%~98%. This calculation might either overestimate or underestimate the  $UR_\sigma$ , due to  
428 the fact that the calibrated parameters did not strictly follow Gaussian distributions. But  
429 the actual  $UR_\sigma$  should not be far from our estimates, because these samples were not  
430 widely spread across the potential parameter space (Figure 2). The least constrained  
431 parameter was  $k_{NO_3}^{plant}$  (reaction rate of plant nitrogen carrier enzyme with  $NO_3^-$  substrate).  
432 Two other  $NO_3^-$  dynamics related parameters were also not well constrained:  $UR_\sigma$  of  
433  $K_M^{mic,NO_3}$  (half-saturation constant for decomposing microbe  $NO_3^-$  immobilization) and  
434  $K_M^{den,NO_3}$  (half-saturation constant for denitrifier  $NO_3^-$  consumption) were only 63% and  
435 68%, respectively. Compared with  $NH_4^+$  or  $PO_x$  competition related parameters, we  
436 concluded that parameters associated with  $NO_3^-$  competition were the least constrained in  
437 the model. This result was primarily due to the lack of  $NO_3^-$  pool size data, and  
438 secondarily due to the fact that  $NO_3^-$  was not the major nitrogen source for plant or  
439 decomposing microbes. We also provide quantile-based Uncertainty Reduction for  
440 reference (Table 4). The above-mentioned conclusions still hold with quantile-based  $UR_Q$ ,  
441 although the quantile-based  $UR_Q$  is generally higher than variance-based  $UR_\sigma$ . One  
442 parameter was calibrated to be at the upper boundary of its prior ranges ( $k_p^{plant}$ ), implying  
443 that this tropical plant is highly efficient in phosphorus uptake. Although we do not have  
444 direct kinetic parameter observations for the specific tropical species involved in our  
445 study, an inferred high phosphorus uptake efficiency is reasonable for tropical species

446 that have adapted to these phosphorus deficient environments [Begum and Islam, 2005;  
 447 FÖHse et al., 1988].

448 Convergence of model parameters is reported with the Gelman-Rubin criterion  
 449 (Table 4 and Figure A2). Using this criterion, seven (out of twenty) parameters are found  
 450 to converge (Gelman-Rubin  $\leq 1.1$ ). The lack of convergence of the remaining  
 451 parameters is partly due to data paucity. In particular, starting from different prior values,  
 452 MCMC calibrations may result in different models that give rise to similar model-data  
 453 misfit (i.e., “equifinality” [Tang and Zhuang, 2008]). In this regard, high frequency  
 454 measurements may improve model calibration (see more discussion in section 3.3). The  
 455 non-convergence of model parameters implies an imperfect model. Therefore, for large-  
 456 scale model application, more work on data collection, parameter tuning, and uncertainty  
 457 analysis is needed. However, even with these caveats, the model predictability is  
 458 reasonably good when applied to the tropical forest fertilization experiments described in  
 459 Section 3.4.

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460 We re-organize the right hand sides of Eqns. 14 – 22 to be the product of potential  
 461 nutrient uptake rate and an ECA limitation term; for example for plant  $\text{NH}_4^+$  uptake:

$$462 \quad F_{\text{NH}_4}^{\text{plant}} = k_{\text{NH}_4}^{\text{plant}} \cdot ECA_{\text{NH}_4}^{\text{plant}} \quad (32)$$

$$463 \quad ECA_{\text{NH}_4}^{\text{plant}} = \frac{[\text{NH}_4] \cdot [E_N^{\text{plant}}]}{K_M^{\text{plant}, \text{NH}_4} \left( 1 + \frac{[\text{NH}_4]}{K_M^{\text{plant}, \text{NH}_4}} + \frac{[\text{NO}_3]}{K_M^{\text{plant}, \text{NO}_3}} + \frac{[E_N^{\text{plant}}]}{K_M^{\text{plant}, \text{NH}_4}} + \frac{[E_N^{\text{mic}}]}{K_M^{\text{mic}, \text{NH}_4}} + \frac{[E_N^{\text{nit}}]}{K_M^{\text{nit}, \text{NH}_4}} \right)} \quad (33)$$

464 Other “consumer-substrate reactions” have similar forms. Under a nutrient  
 465 abundant situation (e.g., fertilized agriculture ecosystem), the relative competitiveness of  
 466 each consumer (ECA) is dominated by its specific enzyme abundance ([E]). Under such  
 467 conditions, substrate affinity is no longer a controlling factor. In contrast, under nutrient

468 limited conditions (*e.g.*, many natural ecosystems), ECA is dominated by the specific  
469 enzyme abundance as well as the substrate affinity ( $[E]/K_M$ ). Therefore, consumers could  
470 either enable an alternative high affinity nutrient transporter system (low  $K_M$ ) or exude  
471 more enzyme to enhance competitiveness. For example, at the whole-soil scale it has  
472 been shown that root spatial occupation ( $C_{\text{root}}$ ) determines a plant's competitiveness  
473 when low soil nutrient diffusivity is limiting nutrient supply [Raynaud and Leadley,  
474 2004]. Consistently, our results highlighted the dominant role of nutrient carrier enzyme  
475 abundance ( $E$  proportional to  $C_{\text{root}}$ ) in controlling competition. If we further assumed  
476 that plants, decomposing microbes, and nitrifiers enzyme abundances were  
477 approximately equal, we will have that the relative their competitiveness in acquiring  
478  $\text{NH}_4^+$  was about 4:10:9 ( $1/K_M^{\text{plant},\text{NH}_4} : 1/K_M^{\text{mic},\text{NH}_4} : 1/K_M^{\text{nit},\text{NH}_4}$ ). However, such results  
479 could not be easily generalized to other ecosystems, because they heavily relied on the  
480 traits (affinity) of specific competitors. For a different ecosystem, those traits would be  
481 drastically different due to the change of, *e.g.*, plant species composition and microbial  
482 community structure. Even for the same ecosystem, those traits could be highly  
483 heterogeneous. For example, the community structure of decomposing microbes could be  
484 different in rhizosphere and bulk soil (with different  $K_M$ ). However, in this work we  
485 assumed a well-mixed environment (one soil column), in order to be consistent with  
486 large-scale ecosystem models. Although beyond the scope of the current study, the  
487 consequences of ignoring the rhizosphere versus bulk soil heterogeneity warrants further  
488 investigation. Large-scale models aim to quantify ecosystem level dynamics, although  
489 they are usually driven by parameters inferred from *in situ* field observations. In the  
490 absence of a model that explicitly represents this spatial heterogeneity, it is difficult to



491 quantify the impacts of using inferred rhizosphere decomposer affinities on model  
492 predictions of the whole soil [Schimel *et al.*, 1989]. Furthermore, the assumption of well-  
493 mixed environment in large-scale model is an inevitable flaw, because of large  
494 computational demands and a lack of scale-aware parameters and model structures for  
495 large-scale models to run fine scale simulations.

496 Although in this study ECA was applied to a large-scale model, the competition  
497 framework is readily applicable to fine scale models that consider soil heterogeneity. In  
498 fine-scale models, bulk soil nutrient competition can occur only among different  
499 microbes because they are ubiquitous in the soil (*e.g.*, nitrifier versus microbial  
500 decomposer), while rhizosphere nutrient competition occurs among plants and microbes  
501 (*e.g.*, nitrifier versus microbial decomposer versus roots). This distinction implies that the  
502 competitiveness parameters we infer here for N-COM, which does not currently  
503 explicitly represent bulk versus rhizosphere processes, subsume the range of fine scale  
504 processes controlling nutrient uptake. More research is required to link these different  
505 model spatial scales, theory, and parameterizations.

506 Our modeling framework highlights the important concept that “competitiveness”  
507 is a dynamic property of the competition network, and more importantly that it is linked  
508 to competitor functional traits (affinity and nutrient carrier enzyme abundance). This  
509 concept is in contrast to the prevailing assumption underlying all major large-scale  
510 ecosystem models, which either assume “relative demand competitiveness for different  
511 nutrient consumers” [Thornton *et al.*, 2007] or “soil microbes outcompete plants”  
512 [McGuire *et al.*, 1992; Parton *et al.*, 1988]. Imposing such pre-defined orders of  
513 competitiveness neglects the diversity of nutrient competitors (plants and microbes) and

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514 their differences in nutrient uptake capacity expressed by relevant functional traits. Our  
515 model framework offers a theoretically consistent approach to account for the diversity of  
516 nutrient competition in different competitor networks.

### 517 **3.2 Model sensitivity analysis**

518 Through sensitivity analysis, we separately investigated the factors controlling  
519 plant  $\text{NH}_4^+$ ,  $\text{NO}_3^-$ , and  $\text{PO}_x$  competition (Figure 3). Each sensitivity analysis consisted of  
520 three scenarios: (1) normal conditions (control); (2) elevated soil temperature ( $+T_s$ ); and  
521 (3) elevated soil moisture ( $+\theta$ ). The sensitivity analysis indicates that the model is highly  
522 sensitive to kinetics parameters (*e.g.*,  $K_M$ ). Furthermore, the model is consistently  
523 sensitive to the same parameters across all temperature and moisture conditions. The  
524 environment affects the nutrient competition primarily through altering the nutrient  
525 abundance. Enhanced soil temperature and soil moisture accelerated soil organic carbon  
526 turnover, thereby releasing more inorganic nutrient into the soil (gross mineralization).  
527 However, the impacts on plant nutrient uptake are limited (Figure 3) because the  
528 enhanced soil organic matter decay also requires higher immobilization fluxes to sustain  
529 the soil organic matter CNP stoichiometry. The enhancement of net mineralization would  
530 be limited, and therefore would not change soil nutrient status dramatically.

### 531 **3.3 Model performance**

532 The prior and calibrated models were compared against observational datasets of  
533 pool sizes of soil free phosphate, sorbed phosphate, and  $\text{NH}_4^+$ ,  $\text{CO}_2$  efflux, and  $\text{N}_2\text{O}$   
534 efflux (Figure 4). We note that although we attempted to acquire as many datasets that  
535 contained these five observations as possible, more observations in tropical ecosystems  
536 would clearly improve the parameter estimates. For example, in the experiment we

537 analyzed, only three measurements of soil free phosphate were made during 1999. Many  
538 detailed dynamics are therefore missing and could impact our parameter estimates. The  
539 prior model predicted an increasing trend of soil free  $\text{PO}_x$ , which resulted from  
540 underestimates of plant P uptake (by underestimating of  $k_p^{plant}$ ) and soil microbial P  
541 immobilization (by overestimating  $K_M^{mic.P}$ ). The calibrated model captured the seasonal  
542 dynamics of soil free  $\text{PO}_x$  reasonably well: increases during the wet season and gradual  
543 decreasing during the dry season (August to November). The prior model also largely  
544 underestimated the seasonal variability of nitrogen dynamics and underestimated the  
545  $\text{NH}_4^+$  pool size due to overestimation of plant  $\text{NH}_4^+$  uptake ( $k_{NH4}^{plant}$ ). In addition, it also  
546 underestimated the denitrification  $\text{N}_2\text{O}$  emissions, because of an underestimation of  $\text{NH}_4^+$   
547 to  $\text{NO}_3^-$  transformation rate ( $k_{nit}$ ). Consequently, there was not enough  $\text{NO}_3^-$  substrate to  
548 react with denitrifiers and release  $\text{N}_2\text{O}$ . The calibrated model, however, accurately  
549 reproduced the seasonal dynamics of both  $\text{NH}_4^+$  pool sizes and soil  $\text{N}_2\text{O}$  emissions. There  
550 were small differences between the prior and calibrated model predictions of soil  $\text{CO}_2$   
551 emissions. The  $\text{CO}_2$  and  $\text{N}_2\text{O}$  effluxes were more frequently observed at Tapajos National  
552 Forest during 1999 to 2001, compared with phosphorus data. Most of the measurements  
553 were collected during the wet season. Therefore the modeled  $\text{CO}_2$  and  $\text{N}_2\text{O}$  emissions  
554 were largely improved by assimilating these datasets.

555         The model performance implies that after assimilating multiple datasets, our  
556 model predictions were improved over the prior model. However, it is clear that more  
557 observations of the metrics applied in our MCMC approach would benefit the model  
558 calibration. Unfortunately, because of our focus on tropical sites, we were unable to  
559 acquire more datasets that had the full suite of measurements required. Datasets of soil

560 nutrient pool sizes (*e.g.*, NO<sub>3</sub><sup>-</sup>) and higher frequency sampling of those sparse  
561 measurements (*e.g.*, PO<sub>x</sub>) would significantly benefit the model uncertainty reduction.

### 562 **3.4 Model testing against nitrogen and phosphorus fertilization studies**

563 To test the calibrated N-COM model, we conducted short-term numerical  
564 competition experiments (24-hour or 48-hour simulations) by manually imposing an  
565 input flux into nutrient pools equivalent to the N and P fertilization experiments  
566 described above and in Table 5. The simulated results were compared with observations  
567 from the field manipulations.

568 In the P addition experiments across the Hawaiian chronosequence, the  
569 partitioning of phosphate between microbes and mineral surfaces was well represented by  
570 the N-COM model in the intermediate (20K yr) and old (4.1M yr) sites (Figures 5b and  
571 5c), with no significant differences between model predictions and observations. In the  
572 youngest Hawaiian site (300 yr; Figure 5a), the relative partitioning was correctly  
573 simulated, but the predicted PO<sub>4</sub><sup>3-</sup> magnitudes were lower than observations. Our  
574 simulations indicated that at the young soil site the added P exceeded microbial demand,  
575 resulting in lower predicted microbial P uptake than observed. This discrepancy reflected  
576 a possible deficiency of first-order SOC decay models (as we used here), which implicitly  
577 treat microbes as a part of soil organic matter. Since microbial nutrient immobilization is  
578 strictly regulated by the SOC turnover rate in this type of model, external nutrient inputs  
579 will no longer affect microbial nutrient uptake if the inputs exceed potential microbial  
580 demand. We therefore believe that explicit Microbe-Enzyme models might be able to  
581 better explain the strong microbe PO<sub>4</sub><sup>3-</sup> uptake signal observed at the young Hawaii  
582 fertilization experiment site. Microbial models explicitly simulate the dynamics of

583 microbial biomass, which might be able to capture the expected rapid growth of  
584 microbial communities under conditions of improved substrate quality [Kaspari *et al.*,  
585 2008; Wieder *et al.*, 2009].

586 In the Puerto Rican Luquillo forest nitrogen addition experiments, partitioning of  
587 added ammonium between plants and heterotrophic bacteria was well captured by the N-  
588 COM model, with no significant differences between model predictions and observations  
589 (Figure 5d). However, the model underestimated nitrifier  $\text{NH}_4^+$  uptake.  $\text{NO}_3^-$  competition  
590 in this site was also relatively accurately predicted (Figure 5e), although the  
591 measurements did not include denitrification. Model estimates of plant  $\text{NO}_3^-$  uptake and  
592 microbial  $\text{NO}_3^-$  immobilization were consistent with the observed ranges, but we  
593 highlight the large observational uncertainties, particularly for microbial  $\text{NO}_3^-$  uptake.

594 In the pseudo-first-order decomposition model we applied here to demonstrate the  
595 ECA competition methodology, the soil organic matter C:N:P ratio also limited microbial  
596 N and P uptake. For this type of decomposition model, stoichiometric differences  
597 between soil organic matter and microbes are not dynamically simulated. Such a  
598 simplification of soil and microbial stoichiometry favors large spatial scale model  
599 structures over long temporal periods, but hampers prediction of microbial short-term  
600 responses to N and P fertilization. For example, the observed difference between  
601 microbial and soil C:P ratios can be as large as 6-fold [Mooshammer *et al.*, 2014; Xu *et*  
602 *al.*, 2013]. Were that the case in the observations we applied, the potential soil P demand  
603 calculated based on a fixed soil organic matter C:P ratio could be only 17% of that based  
604 on microbial C:P ratio.

### 605 **3.5 Implications of ECA competition treatment**

606 Terrestrial ecosystem growth and function are continuously altered by climate  
607 (e.g., warming, drought; [Chaves *et al.*, 2003; Springate and Kover, 2014]), external  
608 nutrient inputs (e.g., N deposition; [Matson *et al.*, 2002; Matson *et al.*, 1999]), and  
609 atmospheric composition (e.g., CO<sub>2</sub> concentration; [Norby *et al.*, 2010; Oren *et al.*, 2001;  
610 Reich *et al.*, 2006]). Improved understanding of the underlying mechanisms regulating  
611 ecosystem responses to environmental changes has been obtained through *in situ* level to  
612 large-scale and long-term manipulation experiments. For example, decade-long Free-Air  
613 Carbon Dioxide Enrichment (FACE) experiments have revealed that nitrogen limitation  
614 diminished the CO<sub>2</sub> fertilization effect of forests [Norby *et al.*, 2010] and grasslands  
615 [Reich and Hobbie, 2013] ecosystems. However, fewer efforts have been made towards  
616 incorporating the observed process-level knowledge into Earth System Models (ESMs).  
617 Therefore, a major uncertainty that has limited the predictability of ESMs has been the  
618 incomplete representation of soil nutrient dynamics [Zaehle *et al.*, 2014]. Even though  
619 new soil nutrient cycle paradigms were proposed during recent decades [Korsaeth *et al.*,  
620 2001; Schimel and Bennett, 2004], they were restricted to either conceptual models or  
621 only applied to explain laboratory experiments.

622 Many large-scale terrestrial biogeochemistry models (e.g., O-CN, CASA, TEM)  
623 have adopted the classical paradigm that microbes decompose soil organic matter and  
624 release NH<sub>4</sub><sup>+</sup> as a “waste” product [Waksman, 1931]. The rate of this process is defined  
625 as “net N mineralization”, and is adopted as a “measure” of plant available inorganic N  
626 [Schimel and Bennett, 2004]. This classical paradigm overlooked the fact that “net N  
627 mineralization” actually comprised two individual processes - gross N mineralization and  
628 microbial N immobilization. Implicitly, the classical paradigm assumes that the microbes

629 have priority to assimilate as much of the available nutrient pool as possible. Soil  
630 nutrients were only available for plant uptake if there were not enough free energy  
631 materials (e.g., dissolved soil organic carbon) to support microbial metabolism. As a  
632 result, soil microbes were considered “victors” in the short-term nutrient competition.  
633 Some other large-scale terrestrial biogeochemistry models (e.g., CLM4CN), simplify the  
634 concept of nutrient competition differently. They calculate the plant N uptake and soil N  
635 immobilization separately; and then down-regulate the two fluxes according to the soil  
636 mineral N availability. As a result, plant and soil microbe competitiveness for nutrients is  
637 determined by their relative demand.

638         Climate-scale land models have over-simplified or ignored competition between  
639 plants, microbes, and abiotic mechanisms. In reality, under high nutrient stress  
640 conditions, plants can exude nutrient carrier enzymes or facilitate mycorrhizal fungi  
641 associations to enhance competitiveness for nutrient acquisition [*Drake et al.*, 2011;  
642 *Hobbie and Hobbie*, 2006; *Treseder and Vitousek*, 2001]. In addition, plants can adjust C  
643 allocation to construct more fine roots, which scavenge nutrients over larger soil volumes  
644 [*Iversen et al.*, 2011; *Jackson et al.*, 2009; *Norby et al.*, 2004]. Soil spatial heterogeneity  
645 might also contribute to the success of plant nutrient competition [*Korsaeth et al.*, 2001].  
646 Therefore, most ecosystem biogeochemistry models with traditional treatments of  
647 nutrient competition likely underestimate plant nutrient uptake.

648         Nutrient competition should be treated as a complex consumer-substrate reaction  
649 network: multiple ‘consumers’, including plant roots, soil heterotrophic microbes,  
650 nitrifiers, denitrifiers, and mineral surfaces, each competing for substrates of organic and  
651 inorganic nitrogen and phosphorus as nutrient supply. In such a model structure, the

652 success of any consumer in substrate acquisition is affected by its consumer-substrate  
653 affinity [Nedwell, 1999]. Such competitive interactions have been successfully applied to  
654 microbe-microbe and plant-microbe substrate competition modeling [Bonachela et al.,  
655 2011; Lambers et al., 2009; Maggi et al., 2008; Maggi and Riley, 2009; Moorhead and  
656 Sinsabaugh, 2006; Reynolds and Pacala, 1993] for many years.

657         Here, we applied the consumer-substrate network in a broader context of plant,  
658 microorganism, and abiotic mineral interactions. We analyzed the consumer-substrate  
659 network using a first-order accurate equilibrium chemistry approximation (ECA) [Tang  
660 and Riley, 2013; Zhu and Riley, 2015]. Our sensitivity analysis confirmed that the  
661 consumer-substrate affinity and nutrient carrier enzyme abundance were the most  
662 important factors regulating relatively short-term competitive interactions. The ECA  
663 competition treatment represents ecosystem responses to environmental changes and has  
664 the potential to be linked to a microbe-explicit land biogeochemistry model. The  
665 approach allows competition between plants, microbes, and mineral surfaces to be  
666 prognostically determined based on nutrient status and capabilities of each consumer.

667

#### 668 **4. Conclusions**

669         In this study, we developed a soil biogeochemistry model (N-COM) that resolves  
670 the dynamics of soil nitrogen and phosphorus, plant uptake of nutrients, microbial uptake,  
671 and abiotic interactions. We focused on the implementation, parameterization, and testing  
672 of the nutrient competition scheme that we plan to incorporate into the ESM land models  
673 CLM and ALM. We described the multiple-consumer and multiple-nutrient competition  
674 network with the Equilibrium Chemical Approximation (ECA) [Tang and Riley, 2013]



675 considering two inhibitive effects: (1) multiple substrates (*e.g.*,  $\text{NH}_4^+$  and  $\text{NO}_3^-$ ) sharing  
676 one consumer inhibits the effective binding between any specific substrate and the  
677 consumer and (2) multiple consumers (*e.g.*, plants, decomposing microbes, nitrifiers)  
678 sharing one substrate (*e.g.*,  $\text{NH}_4^+$ ) lowers the probability of effective binding between any  
679 consumer and that substrate. We calibrated the model at a tropical forest site with highly  
680 weathered soil (Tapajos National Forest, Para, Brazil), using multiple observational  
681 datasets with the Markov Chain Monte Carlo (MCMC) approach. The calibrated model  
682 compared to multiple categories of observational data was substantially improved over  
683 the prior model (Figure 4). The seasonal dynamics of soil carbon, nitrogen, and  
684 phosphorus were moderately well captured. However, our results would likely be more  
685 robust if more temporally resolved observations of carbon, nitrogen, and phosphorus  
686 were available. **Although the calibrated model is the best one we can derive based on  
687 limited data, several model parameters were not well converged. We therefore conclude  
688 that more work on data collection, parameter tuning, and uncertainty analysis is needed.**

689 To test the resulting model using the calibrated parameters, we applied N-COM to  
690 two other tropical forests (Hawaii tropical forest and Luquillo tropical forest) not used in  
691 the calibration process and conducted nutrient perturbation studies consistent with  
692 fertilization experiments at these sites. The results showed that N-COM simulated the  
693 nitrogen and phosphorus competition well for the majority of the observational metrics.  
694 However, the model underestimated  $\text{NH}_4^+$  uptake by nitrifiers, probably due to the  
695 loosely constrained nitrification parameters that were the result of  $\text{NO}_3^-$  pool size data  
696 paucity during calibration at the Brazil site (Table 4). Datasets of soil nutrient pool sizes

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697 and CO<sub>2</sub> and N<sub>2</sub>O effluxes with high frequency sampling would significantly benefit the  
698 model uncertainty reduction.

699 To date, many terrestrial ecosystem biogeochemistry models assume microbes  
700 outcompete plants and immobilize nutrients first [*Y P Wang et al.*, 2007; *Zaehle and*  
701 *Friend*, 2010; *Zhu and Zhuang*, 2013], although CLM currently assumes constant and  
702 relative demand competitiveness of plants and microbes. Few models, to our knowledge,  
703 consider the role of abiotic interactions in the competitive interactions. In the case of  
704 microbes outcompeting plants, the plant is only able to utilize the nutrients that exceed  
705 microbial demands during that time step. The leftover nutrients are defined as net  
706 mineralization, which is a widely adopted concept in soil biogeochemistry modeling  
707 [*Schimel and Bennett*, 2004]. These models oversimplify plant-microbe interactions by  
708 imposing dubious assumptions (*e.g.*, microbes always win against plants). We showed  
709 that (in section 3.1) “competitiveness” is a dynamic rather than fixed property of the  
710 competition network, and more importantly, it should be linked to competitor functional  
711 traits (affinity and nutrient carrier enzyme abundance).

712 This study is an important step towards implementing more realistic nutrient  
713 competition schemes in complex climate-scale land models. Traditional ESMs generally  
714 lack realistic soil nutrient competition, which likely biases the estimates of terrestrial  
715 ecosystem carbon productivity and biosphere-climate feedbacks. This study showed the  
716 effectiveness of ECA kinetics in representing soil multiple-consumer and multiple-  
717 nutrient competition networks. Offline calibration and independent site-level testing is  
718 critically important to ensuring the newly incorporated model will perform reasonably  
719 when integrated in a complex ESM. To this end, we provide a universal calibration

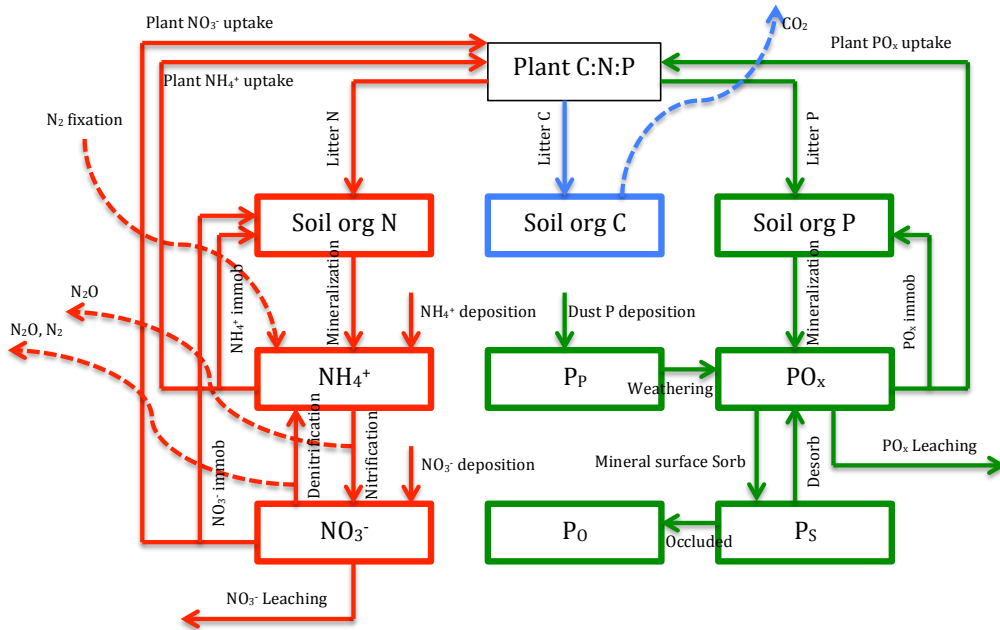
720 approach using MCMC, which could in the future be used to further constrain N-COM  
721 across plant functional types, climate, and soil types.

722

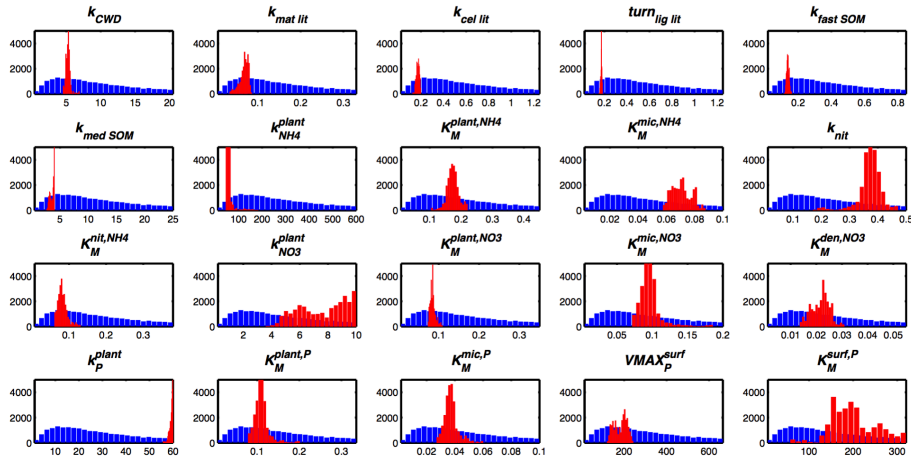
723 *Acknowledgements:* This research was supported by the Director, Office of Science,  
724 Office of Biological and Environmental Research of the US Department of Energy under  
725 Contract No. DE-AC02-05CH11231 as part of the Regional and Global Climate  
726 Modeling (RGCM) and ACME programs.

727 **Figure 1.** Model structure. Boxes represent pools, solid arrows represent aqueous fluxes,  
 728 and dashed arrows represent gaseous pathways out or into the system. Three essential  
 729 chemical elements (Carbon (C), Nitrogen (N) and Phosphorus (P)) are simulated in N-  
 730 COM (blue, red, and green represent C, N, and P pools and processes, respectively).

731



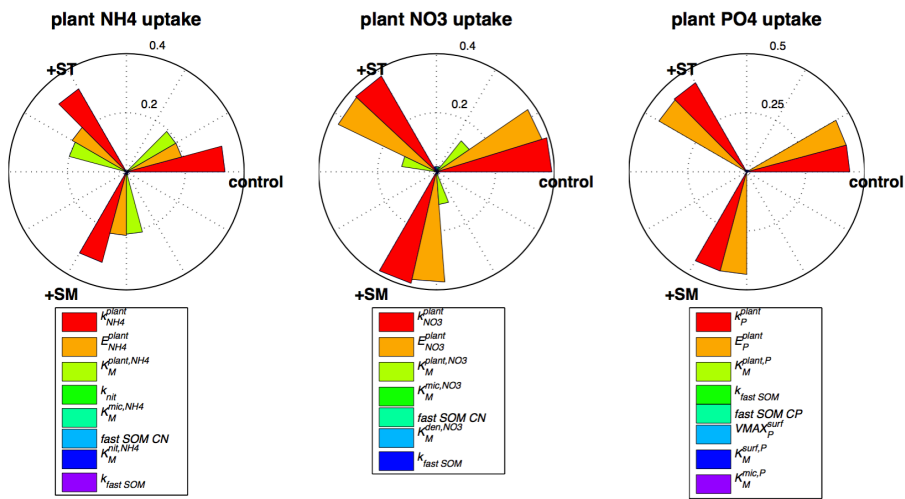
732 **Figure 2.** Distribution of prior and calibrated model parameters.



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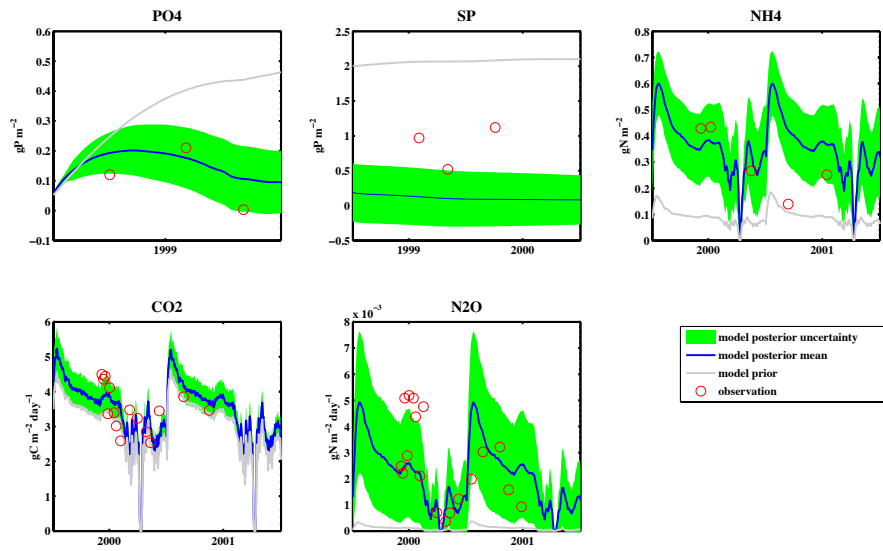
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735 **Figure 3.** Model sensitivity analysis with SOBOL sampling. For each metric, three  
 736 scenarios are shown: baseline (Control), elevated soil temperature by 5 °C (+ $T_s$ ), and  
 737 elevated soil moisture by 50% (+ $\theta$ ), respectively. The length of bar (plot in polar  
 738 coordinate) is the sensitivity (unit-less) of model output with respect to model input  
 739 variables. Our results showed that the plant nutrient uptake was mostly regulated by  
 740 internal consumer-substrate uptake kinetics rather than the external environmental  
 741 conditions (*e.g.*,  $T_s$ ,  $\theta$ ).

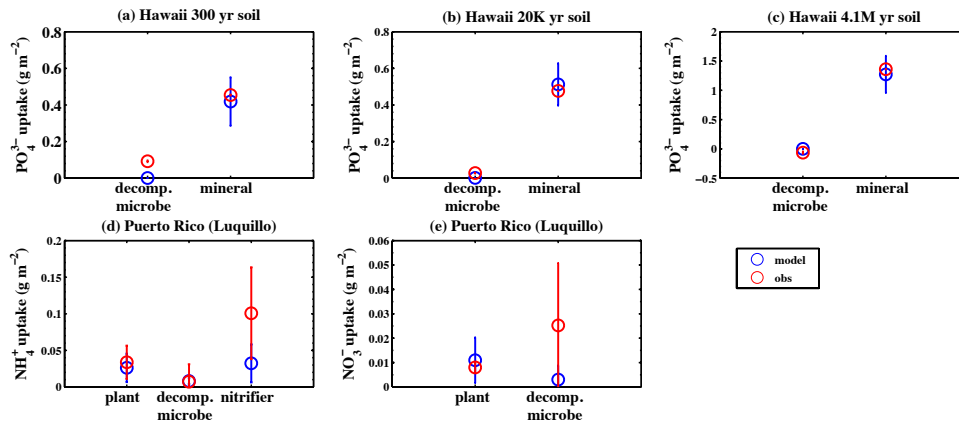


742  
 743

744 **Figure 4.** Model performance at Tapajos National Forest, Para, Brazil. Overall, the  
745 calibrated model (blue line) improved predictions over the prior model (grey line) when  
746 compared to observations. Green areas indicate the calibrated model uncertainties.



748 **Figure 5.** Model perturbation experiments compared with nitrogen and phosphorus  
 749 fertilization field experimental data. The blue dots show the difference between control  
 750 and perturbed simulations, which mean how much newly added nutrient each consumer  
 751 takes up. The red circles are recovered isotopically labeled nutrient within each  
 752 consumer. Since plants phosphorus uptake was not measured at Hawaii sites, we didn't  
 753 include the plants in the perturbation study.  
 754

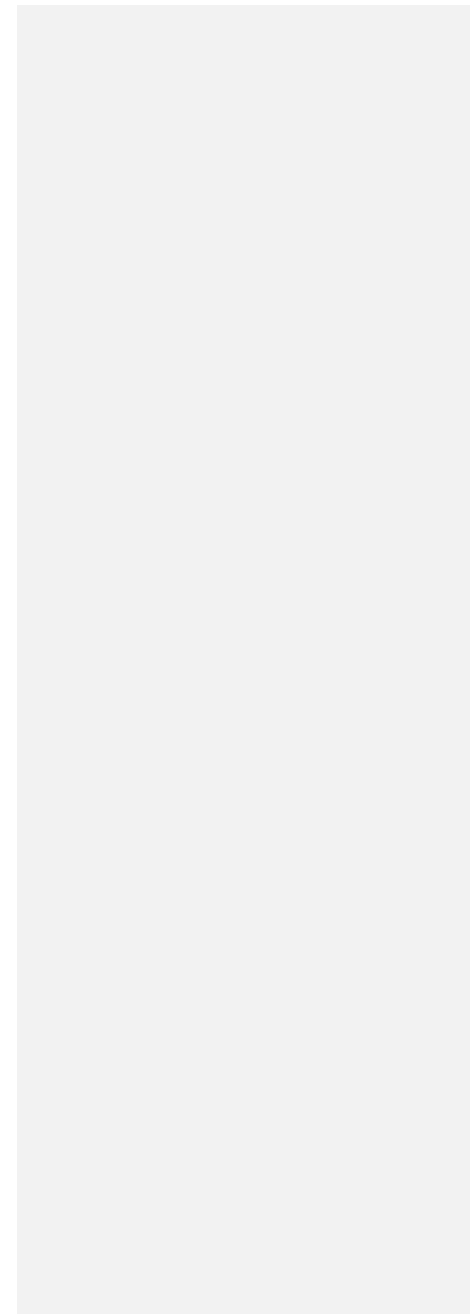




755 **Table 1.** A summary of the modeled consumer-resource competition network.

<b>Resources</b>		<b>Consumers</b>	
$\text{NH}_4^+$	Plant	Decomposing Microbe	Nitrifier
$\text{NO}_3^-$	Plant	Decomposing Microbe	Denitrifier
$\text{PO}_x$	Plant	Decomposing Microbe	Mineral surface

756



757 **Table 2.** Model parameters and baseline values.

<b>C associated</b>					
$g_i$	Percentage of carbon remains in the soil after decomposition of $i^{th}$ SOM	-	[1.0; 0.45; 0.5; 0.5; 0.83; 0.45; 0.45]	[Koven et al., 2013]	
$f_{ij}$	fraction of SOM leave from $i^{th}$ pool and enter into $j^{th}$ pool	-	[0, 0, 0.76, 0.24, 0, 0, 0; 0, 0, 0, 0, 1, 0, 0; 0, 0, 0, 0, 1, 0, 0; 0, 0, 0, 0, 0, 1, 0; 0, 0, 0, 0, 0, 0.995, 0.005; 0, 0, 0, 0, 0.93, 0, 0.07; 0, 0, 0, 0, 1, 0, 0]		[Koven et al., 2013]
CN	Soil organic matter CN ratio	-	[13,16,7.9]	[Parton et al., 1988]	
CP	Soil organic matter CP ratio	-	[110,320,114]	[Parton et al., 1988]	
$TUR_{SOM}$	Soil organic matter turn over [CWD, metabolic lit, cellulose lit, lignin lit, fast SOM, medium SOM, slow SOM]	year	[4.1, 0.066, 0.25, 0.25, 0.17, 5, 270]	[Koven et al., 2013]	
<b>N associated</b>					
$k_{NH_4}^{plant}$	Reaction rate of plant $NH_4^+$ carrier enzyme	day <sup>-1</sup>	120 <sup>(a)</sup>	[Jackson et al., 1997; Min et al., 2000]	
$K_M^{plant,NH_4}$	Half-saturation constant for plant $NH_4^+$ uptake	g m <sup>-2</sup>	0.09	[Kuzyakov and Xu, 2013]	
$K_M^{mic,NH_4}$	Half-saturation constant for decomposing microbe $NH_4^+$ immobilization	g m <sup>-2</sup>	0.02	[Kuzyakov and Xu, 2013]	
$K_{nit}$	Maximum fraction of $NH_4^+$ pool that could be utilized by nitrifiers	day <sup>-1</sup>	10%	[Parton et al., 2001]	
$K_M^{nit,NH_4}$	Half-saturation constant for nitrifier $NH_4^+$ consumption	g m <sup>-2</sup>	0.076	[Drtil et al., 1993]	
$k_{NO_3}^{plant}$	Reaction rate of plant $NO_3^-$ carrier enzyme	day <sup>-1</sup>	2 <sup>(a)</sup>	[Jackson et al., 1997; Min et al., 2000]	
$K_M^{plant,NO_3}$	Half-saturation constant for plant $NO_3^-$ uptake	g m <sup>-2</sup>	0.07	[Kuzyakov and Xu, 2013]	
$K_M^{mic,NO_3}$	Half-saturation constant for decomposing microbe $NO_3^-$ immobilization	g m <sup>-2</sup>	0.04	[Kuzyakov and Xu, 2013]	
$K_M^{den,NO_3}$	Half-saturation constant for denitrifier $NO_3^-$ consumption	g m <sup>-2</sup>	0.011	[Murray et al., 1989]	
$[E_N^{plant}]$	Plant nitrogen carrier enzyme abundance for nitrogen uptake	g m <sup>-2</sup>	$C_{root} \cdot 0.0000125^{(a)}$	[Tang and Riley, 2013; Trumbore et al., 2006]	
$[E_N^{mic}]$	Decomposing microbes nitrogen carrier enzyme abundance for nitrogen immobilization	g m <sup>-2</sup>	$\frac{F_N^{immob,pot}}{1000}^{(b)}$	[Tang and Riley, 2013]	
$[E_N^{nit}]$	Nitrifier nitrogen carrier enzyme abundance for $NH_4^+$ assimilation	g m <sup>-2</sup>	$1.2E^{-3}$	[Raynaud et al., 2006]	

$[E_N^{den}]$	Denitrifier nitrogen carrier enzyme abundance for $\text{NO}_3^-$ assimilation	$\text{g m}^{-2}$	$1.2\text{E}^{-3}$	[Raynaud et al., 2006]
$f^{N_2O}$	Fraction of nitrification flux lost as $\text{N}_2\text{O}$	-	$6\text{E}^{-4}$	[Li et al., 2000]
<b>P associated</b>				
$k_{weather}$	Parent material P weathering rate	$\text{g P m}^{-2} \text{ year}^{-1}$	0.004	[Y P Wang et al., 2010]
$k_{occl}$	P occlude rate	$\text{month}^{-1}$	$1.0\text{E}^{-6}$	[Yang et al., 2014]
$k_P^{plant}$	Reaction rate of plant $\text{PO}_x$ carrier enzyme	$\text{day}^{-1}$	12 <sup>(a)</sup>	[Colpaert et al., 1999]
$K_M^{plant,P}$	Half-saturation constant for plant $\text{PO}_x$ uptake	$\text{g m}^{-2}$	0.067	[Cogliatti and Clarkson, 1983]
$K_M^{mic,P}$	Half-saturation constant for decomposing microbe $\text{PO}_x$ immobilization	$\text{g m}^{-2}$	0.02	[Chen, 1974]
$VMAX_P^{surf}$	Maximum mineral surface $\text{PO}_x$ adsorption	$\text{g m}^{-2}$	133	[Y P Wang et al., 2010]
$K_M^{surf,P}$	Half-saturation constant for mineral surface $\text{PO}_x$ adsorption	$\text{g m}^{-2}$	64	[Y P Wang et al., 2010]
$[E_P^{plant}]$	Plant phosphorus carrier enzyme abundance for $\text{PO}_x$ uptake	$\text{g m}^{-2}$	$C_{froot} \cdot 0.0000125$ <sup>(a)</sup>	[Tang and Riley, 2013; Trumbore et al., 2006]
$[E_P^{mic}]$	Decomposing microbes phosphorus carrier enzyme abundance for $\text{PO}_x$ immobilization	$\text{g m}^{-2}$	$\frac{F_P^{immob,pot}}{800}$ <sup>(b)</sup>	[Tang and Riley, 2013]
$[E_P^{surf}]$	Mineral surface “effective enzyme” abundance for $\text{PO}_x$ adsorption	$\text{g m}^{-2}$	$VMAX_P^{surf} - [SP]$	[Tang and Riley, 2013]

(a) The scaling factor for plant nutrient enzyme abundance is 0.0000125. This number is inferred by assuming that growing season plant nutrient carrier enzymes are roughly the same order of magnitude compared with decomposing microbes'. Typical values for soil decomposing microbe biomass and tropical forest fine root biomass are 0.1 [Tang and Riley, 2013] and 400 [Trumbore et al., 2006]  $\text{gC m}^{-2}$ . A typical value of scaling factor that scales microbial biomass to enzyme abundance is 0.05 [Tang and Riley, 2013]. Therefore,  $C_{froot} \cdot x = C_{mic} \cdot 0.05$  or  $400 \cdot x = 0.1 \cdot 0.05$ . We have

$x = 0.0000125$ . Further, we have  $k_{NH4}^{plant} \cdot [E_N^{plant}] = VMAX_{NH4}^{plant}$ . We know that typical values for  $VMAX_{NH4}^{plant}$  and  $[E_N^{plant}]$  are  $0.6 \text{ g m}^{-2} \text{ day}^{-1}$  [Min et al., 2000] and  $0.005 \text{ g m}^{-2}$ . Then we have  $k_{NH4}^{plant} = 120 \text{ day}^{-1}$ . Similarly, we have  $k_{NO3}^{plant} \cdot [E_P^{plant}] = VMAX_{NO3}^{plant}$ ,  $k_P^{plant} \cdot [E_P^{plant}] = VMAX_P^{plant}$ . Knowing that typical values for  $VMAX_{NO3}^{plant}$  and  $VMAX_P^{plant}$  are 0.01 [Min et al., 2000] and 0.06 [Colpaert et al., 1999]  $\text{g m}^{-2} \text{ day}^{-1}$ , we have  $k_{NO3}^{plant} = 2$  and  $k_P^{plant} = 12 \text{ day}^{-1}$ .

(b) For decomposing microbes, we have  $VMAX_N^{mic} = k_N^{mic} \cdot [E_N^{mic}]$ . Typical values for  $VMAX_N^{mic}$  and  $[E_N^{mic}]$  are  $5 \text{ g m}^{-2} \text{ day}^{-1}$  [Kuzuyakov and Xu, 2013] and  $0.005 \text{ g m}^{-2}$  [Tang and Riley, 2013]. Therefore, we have  $k_N^{mic} = 1000$ . Since our model calculates potential N immobilization rates and approximates them as  $VMAX_N^{mic}$ . The changes of potential N immobilization rates at each time step

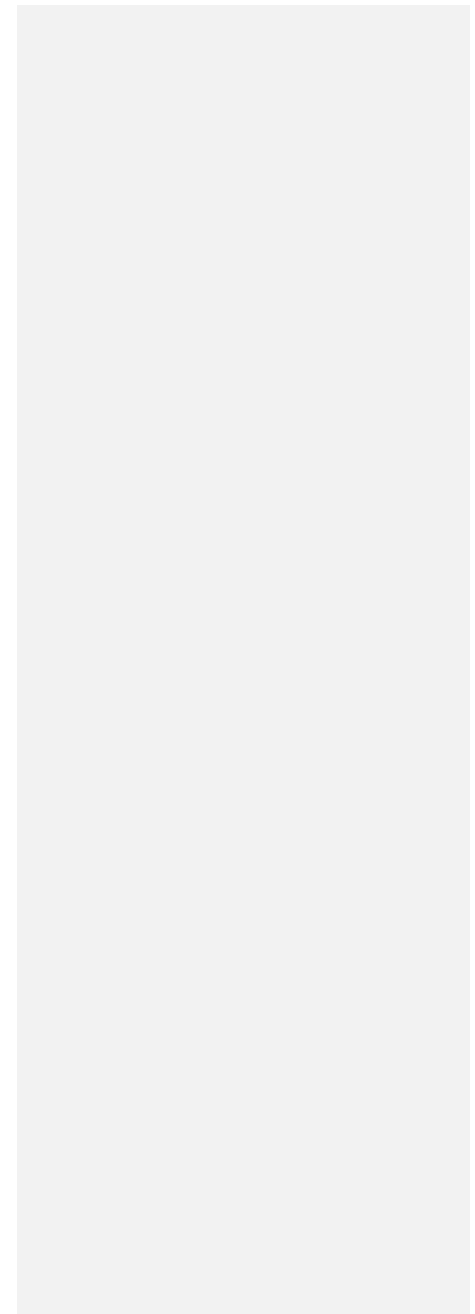
imply the changes of enzyme abundance through  $[E_N^{mic}] = \frac{F_N^{immob,pot}}{k_N^{mic}} = \frac{F_N^{immob,pot}}{1000}$ . Similarly, we have that  $VMAX_P^{immob}$  and  $[E_N^{mic}]$  are  $2 \text{ g m}^{-2} \text{ day}^{-1}$  [Chen, 1974] and  $0.005 \text{ g m}^{-2}$ . Therefore,  $k_P^{mic} = 800$

and  $E_P^{mic} = \frac{F_P^{immob,pot}}{800}$ .

760 **Table 3.** Observational datasets used for calibration. Number of observations for each data stream is included in brackets.

Processes	Datasets	Location	References
C associated	Soil heterotrophic respiration (20)	Tapajos National Forest, Para, Brazil	[ <i>Silver et al.</i> , 2012]
N associated	Soil NH <sub>4</sub> <sup>+</sup> (5)      N <sub>2</sub> O efflux (20)	Tapajos National Forest, Para, Brazil	[ <i>Silver et al.</i> , 2012]
P associated	Soil free phosphate (3)      Sorb phosphate (3)	Tapajos National Forest, Para, Brazil	[ <i>McGroddy et al.</i> , 2008]

761



762 **Table 4.** Calibrated parameters are reported in terms of (1) mean/standard deviation by fitting to a Gaussian distribution; (2) 25% and  
 763 75% quantile. Both variance-based and quantile-based parameters uncertainty reduction are provided; (3) Gelman-Rubin convergence  
 764 criterion.

Parameters	$\mu_{prior}$	$\sigma_{prior}$	$\mu_{posterior}$	$\sigma_{posterior}$	UR	$Q_{prior}^{25}$	$Q_{prior}^{75}$	$Q_{posterior}^{25}$	$Q_{posterior}^{75}$	UR	Gelman-Rubin criterion
$TURN_{SOM}$	[3.7,	[3.9,	[5.2,	[0.33,	[92, 83,	[5.33,	[19.32,	[5.05, 0.63,	[5.39, 0.076,	[97, 94, 97, 99,	[1.69, 1.03, 1.75,
[CWD,	0.06,	0.06,	0.07,	0.01,	96, 98,	0.086, 0.33,	0.31, 1.18,	0.16, 0.17, 0.13,	0.18, 0.18, 0.14,	98, 96	1.01, 1.06, 1.55]
metabolic,	0.23,	0.24,	0.17,	0.01,	96, 92]	0.33, 0.22,	1.18, 0.8,	3.2]	3.9]		
cellulose, lignin	0.23,0.16,	0.24,	0.17,	0.005,		6.5]	23.5]				
lit, fast, medium	4.6]	0.18, 4.8]	0.14, 3.6]	0.008,							
SOM]				0.37]							
$k_{NH4}^{plant}$	109	114	58	14	88	156.1	565.4	52.8	60.0	98	1.87
$K_M^{plant,NH4}$	0.082	0.086	0.173	0.018	79	0.12	0.42	0.16	0.18	93	2.86
$K_M^{mic,NH4}$	0.018	0.019	0.071	0.0067	65	0.026	0.094	0.065	0.076	85	1.94
$k_{nit}$	0.091	0.095	0.37	0.038	60	0.13	0.47	0.36	0.39	91	2.02
$K_M^{nit,NH4}$	0.069	0.072	0.082	0.012	83	0.10	0.36	0.07	0.09	94	1.95
$k_{NO3}^{plant}$	1.8	1.9	7.6	1.7	13	2.60	9.42	6.11	9.14	56	1.01

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 Comment [4]: Modified

$K_M^{plant,NO3}$	0.064	0.067	0.085	0.0064	90	0.09	0.33	0.08	0.09	97	3.17
$K_M^{mic,NO3}$	0.036	0.038	0.096	0.014	63	0.05	0.19	0.09	0.10	92	2.64
$K_M^{den,NO3}$	0.0101	0.0105	0.022	0.0034	68	0.014	0.052	0.019	0.024	87	1.03
$k_P^{plant}$	11	11.5	59	0.75	93	15.61	56.54	58.86	59.81	98	1.06
$K_M^{plant,P}$	0.061	0.064	0.11	0.015	77	0.09	0.32	0.10	0.12	94	1.52
$K_M^{mic,P}$	0.018	0.019	0.037	0.0047	75	0.026	0.094	0.034	0.039	93	2.86
$VMAX_P^{surf}$	121	127	182	30	76	173.0	626.6	156.5	206.3	89	2.25
$K_M^{surf,P}$	64	58	200	50	18	83.2	301.5	162.6	233.0	68	1.05

766 **Table 5.** Short-term (24 or 48 hours) fertilization experiments of  $\text{NH}_4^+$ ,  $\text{NO}_3^-$ , or  $\text{PO}_4^{3-}$  additions used to evaluate the performance of  
 767 the N-COM competition scheme.

Datasets	Added nutrient	Competitors		Duration (hour)	References
$\text{PO}_4^{3-}$ fertilization	$10 \mu\text{g g}^{-1}$	I. Mineral surface	II. Decomposing microbe	48	[Olander and Vitousek, 2005]
$\text{NH}_4^+$ fertilization	$4.6 \mu\text{g g}^{-1}$	I. Plant	II. Decomposing microbe	24	[Templer et al., 2008]
$\text{NO}_3^-$ fertilization	$0.92 \mu\text{g g}^{-1}$	I. Plant	II. Decomposing microbe	24	[Templer et al., 2008]

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