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Dear Editor
Dr. Katja Fennel

   Please find enclosed our revised manuscript "***Comment on "Solute specific scaling of inorganic nitrogen and phosphorus uptake in streams" by Hall et al. (2013).***". We are very pleased to see that our comment has already generated a very productive discussion within the biogeosciences community. As you have seen, we have replied in a timely manner to the comments submitted by the reviewers and other registered peers.

   We have addressed and incorporated the revisions outlined in our responses on the discussion forum. In the final version of our manuscript, we also addressed the recent comments by Hall et al. We have reorganized the comment by sections and have added new text, new equations and a new table in an effort to make our points clearer to the broader scientific community.

   Regarding your specific request about addressing Hall et al.'s point that "the covariate was not used on both sides of the regression, and their statement: "We would lose the ability to deduce mechanism, or test the functional form of relationships if we assume that unmeasured covariates negate the utility of the regression approach"", we have added the text below, which is preceded by a new section demonstrating the derivation of the uptake length metric.

   "In Table 1 we present the different forms that S_w vs. Q/w from Hall et al. (2013) would take if such relationship was estimated for two general types of natural channel geometries.

Table 1. The relationship S_w vs. Q/w for natural channel geometries.

Quantity or relationship	Rectangular channel	Non-rectangular channel
A	$w \cdot h$	$f(w, h)$
Q	$u \cdot A$	$u \cdot A$
S_w	u/K_c	u/K_c
Q/w	$u \cdot h$	$u \cdot (f(w,h)/w)$
S_w vs. Q/w	u/K_c vs. $u \cdot h$	u/K_c vs. $u \cdot (f(w,h)/w)$

Note that each side of S_w vs. Q/w shares the common (hidden) variable u. Therefore, an increase in u (e.g., with stream order or increasing discharge) would increase both sides of the proportion, likely forcing a strong correlation between the variables. This would happen regardless of whether u is measured in the field or not because S_w is an abstract quantity derived from u and K_c (cf. equations 2-3) and, by definition, $Q = u \cdot A$. The fact that Hall et al. (2013) used only estimates of S_w, and field measurements of Q and w to seek a mechanistic relationship from S_w vs. Q/w (cf. equation (4)) does not change the induced correlation created by having the factor u playing a key quantitative role on both sides of the relationship. Since the form of S_w is dependent on the transport model presented in equations (1-2), the only way to negate the role of u in S_w (note that it cannot be negated in Q/w) is to select a completely different transport model and perform a completely different set of field experiments. Also, under the ideal scenario in which we could actually measure S_w in streams (i.e., if S_w was not an abstract variable), the regression S_w vs. Q/w would mainly support the development of conceptual models for S_w, which already exist."

We look forward to receiving your final decision and we want to thank you for all your hard work.

Sincerely,

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Comment on "Solute specific scaling of inorganic nitrogen and phosphorus uptake in streams" by Hall et al. (2013).

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Keywords: nutrient uptake, scaling, spurious correlations, streams, solute transport.

Abstract

Hall et al. (2013) presented a synthesis on 969 nutrient tracer experiments conducted primarily in headwater streams (generally < 4th order streams), with discharges < 200 L/s for ~90% of the experiments, and used a scaling method to test the hypothesis that nutrient demand is constant with increasing stream size (i.e., along a river continuum). In this comment, we present a reanalysis of a subset of the data used by Hall et al. (2013) and propose that their correlations between nutrient uptake lengths of ecologically important solutes and specific discharge are inadvertently spurious. Therefore, the conclusions derived from such correlations are debatable. We conclude the comment highlighting some of the uncertainties associated with using modeling frameworks for scaling nutrient uptake in stream ecosystems.

Estimating uptake lengths; Transport model used by Hall et al. (2013)

Hall et al. (2013) analyzed a dataset of in-stream nutrient uptake experiments performed using plateau tracer injections. The basis of these experiments and estimation of nutrient uptake metrics come from the advection-dispersion equation (equation 1), with the addition of a first-order uptake rate coefficient (Stream Solute Workshop, 1990; Runkel, 2007):

$$\frac{dc}{dt} = -u\frac{dc}{dx} + D\frac{d^2c}{dx^2} - K_c\, c, \qquad (1)$$

where c [M L^{-3}] is the concentration of the reactive solute at a cross-section located downstream of the solute injection site; u [LT^{-1}] the mean flow velocity; D [LT^{-2}] the dispersion coefficient; K_c [T^{-1}] the first-order rate coefficient representing nutrient uptake; x [L] longitudinal distance; and t [T] time. Assuming that dispersion is negligible at plateau concentrations (i.e., when $dc/dt = 0$), equation (1) can be solved for downstream solute concentration:

$$c = c_o \exp(-(K_c/u)\, x), \qquad (2)$$

where c_o [M L^{-3}] represents the initial (or upstream) concentration. The form of this solution motivated the introduction of the uptake length metric, $S_w = u/K_c$, which is a representation of the average distance traveled by a nutrient molecule in inorganic phase prior to uptake (Ensign and Doyle, 2006). Due to experimental simplicity, equation (2) has guided data collection efforts on nutrient cycling where an experimentalist estimates S_w by measuring the plateau concentrations upstream (c_{up}) and downstream (c_{dn}) of a study reach of length L:

$$S_w = u/K_c = L/\ln(C_{up}/C_{dn}). \qquad (3)$$

Note that equations (1-3) support estimates of S_w, given stream conditions satisfy model assumptions, i.e., stream reaches with constant discharge and where dispersion and transient storage do not play important roles (Runkel, 2007). The uptake length derived from equations (1-

3) is equivalent to S_w^I in Runkel (2007), who derived four different uptake lengths ($S_w^I, S_w^{II}, S_w^{III}, S_w^{IV}$) from solute transport models with increased complexity (i.e., adding transient storage, lateral inflows and dispersion). Following Runkel (2007), uptake lengths can be generally represented by a velocity term and an uptake term.

It is important to keep in mind that S_w is an abstract variable represented by model parameters that cannot be simultaneously measured. Since u and K_c are likely to be highly variable along a stream reach, measurements of longitudinal decline in tracer concentrations (c_{up}, c_{dn}) and stream length (L) offer a more tractable approach to estimating S_w through the use of equation 3. While the use of equation 3 circumvents errors associated with estimating u and K_c at the reach scale, the estimation of S_w using c_{up}, c_{dn}, and L must be numerically equivalent to u/K_c at the reach scale. As is the case with any abstract variable derived from a mathematical model, using S_w to infer stream processes entails acknowledging the quantitative role of the model parameters u and K_c from where it was derived.

Critique to the scaling approach used by Hall et al. (2013)

The analysis presented by Hall et al. (2013) was based on plateau experiments conducted in multiple stream ecosystems, where S_w was estimated for each experiment using equation (3). Hall et al. correlated nutrient uptake length, S_w (L), with specific discharge, Q/w ($L^2\ T^{-1}$), to test the hypothesis that nutrient uptake demand is constant across stream orders.

$$S_w \propto (Q/w)^a, \qquad\qquad\qquad (4)$$

$$v_f = \frac{Q/w}{S_w}, \qquad\qquad\qquad (5)$$

where Q ($L^3 T^{-1}$) is stream discharge, w (L) is stream width, a is a scaling exponent and v_f (L T^{-1}) is the nutrient uptake demand (or nutrient uptake velocity, as it has been traditionally called).

In their hypothesis testing, the existence of a constant nutrient uptake demand (constant v_f) was implied by a scaling exponent $a = 1$ (isometric scaling), whereas a scaling exponent $a \neq 1$ (allometric scaling) would imply the reverse. Note that in this context, the existence of a constant nutrient uptake demand would be useful to scale and predict nutrient uptake in stream ecosystems.

In Table 1 we present the different forms that S_w vs. Q/w from Hall et al. (2013) would take if such relationship was estimated for two general types of natural channel geometries.

Table 1. The relationship S_w vs. Q/w for natural channel geometries.

Quantity or relationship	Rectangular channel	Non-rectangular channel
A	$w \cdot h$	$f(w, h)$
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S_w vs. Q/w	u/K_c vs. $u \cdot h$	u/K_c vs. $u \cdot (f(w,h)/w)$

106   Note that each side of S_w vs. Q/w shares the common (hidden) variable u. Therefore, an
107 increase in u (e.g., with stream order or increasing discharge) would increase both sides of the
108 proportion, likely forcing a strong correlation between the variables. This would happen
109 regardless of whether u is measured in the field or not because S_w is an abstract quantity derived
110 from u and K_c (cf. equations 2-3) and, by definition, $Q = u \cdot A$. The fact that Hall et al. (2013)
111 used only estimates of S_w, and field measurements of Q and w to seek a mechanistic relationship
112 from S_w vs. Q/w (cf. equation (4)) does not change the induced correlation created by having the
113 factor u playing a key quantitative role on both sides of the relationship. Since the form of S_w is
114 dependent on the transport model presented in equations (1-2), the only way to negate the role of
115 u in S_w (note that it cannot be negated in Q/w) is to select a completely different transport model
116 and perform a completely different set of field experiments. Also, under the ideal scenario in
117 which we could actually measure S_w in streams (i.e., if S_w was not an abstract variable), the
118 regression S_w vs. Q/w would mainly support the development of conceptual models for S_w,
119 which already exist.
120   We propose that if a meaningful, significant correlation exists between S_w and Q/w, there
121 should be a significant correlation between the underlying parameters (i.e., $1/K_c$ vs. h in
122 rectangular channels or $1/K_c$ vs. $f(w,h)/w$ in other types of natural channels). However, if there
123 is not a corresponding correlation in both of these cases, then the correlation between S_w and
124 Q/w would be falsely influenced by the presence of u in both products. Benson (1965) and
125 Kenney (1982) demonstrated that spurious correlations can result from the use of ratios or
126 products that share a common factor and are more likely when working with complex variables
127 and dimensional analysis. The relationship from Hall et al. (2013) that we deem spurious is
128 analogous to that of Model II presented by Benson (1965) for the spurious correlation of products
129 sharing a common factor (i.e., $X_1 \cdot X_2$ vs. $X_3 \cdot X_2$; where $X_1 = 1/K_c$, $X_2 = u$, $X_3 = h$ or
130 $X_3 = f(w,h)/w$, cf. Table 2 in Benson (1965)). As shown by Benson (1965), the correlation of
131 complex variables (i.e., S_w and Q/w) is dependent on the coefficients of correlation and variation
132 of the three original component variables. Due to the presence of a common factor in the scaling
133 relationship proposed by Hall et al. (2013), we hypothesize that it is a spurious correlation (u
134 influences both S_w and Q/w) that may be mechanistically irrelevant for scaling in-stream nutrient
135 uptake.
136   We tested our hypothesis using the dataset published by Tank et al. (2008), another meta-
137 analysis of nutrient addition experiments which was included in the Hall et al. (2013) meta-
138 analysis. This dataset was chosen because it reports values for S_w, Q, w, and h for nutrient
139 experiments with NH_4 and NO_3 (SRP not included), even though these values were not reported
140 for all the studies ($n=143$ for NH_4, $n=210$ for NO_3). Note that since we do not know the particular
141 geometry for each channel where the tracer experiments were conducted (i.e., we do not know
142 $f(w,h)$), we assumed a rectangular channel geometry (i.e., $A = f(w,h) = w\,h$), which is the
143 same assumption made by Hall et al. (2013) while defining their equations for uptake length and
144 uptake velocity (cf. equations 1-2 in Hall et al (2013)). The dataset published by Hall et al. (2013)
145 does not include values of h, hence we were not able to use it for our analysis. While the
146 assumption of having rectangular channels might be seen as an overgeneralization, it is the only
147 one that allows us to see trends given the scarce information available on the channel geometries
148 of the headwater streams where the experiments were conducted. Furthermore, the transport
149 model implicitly used by Hall et al. (2013) assumes uniform flow (i.e., $dh/dx = 0$, $dw/dx = 0$),

170 which supports our assumption of using a prismatic channel for testing our spurious correlation
171 hypothesis.
172 We proposed a null condition in which we removed the common variable u from the scaling
173 relationship and compared the correlation with that of the original scaling relationship (i.e., we
174 compared $1/K_c$ vs. h and S_w vs. Q/w). We calculated mean stream velocity as $u = Q/(w \cdot h)$.
175 This allowed us to produce values for the relationship $1/K_c$ vs. h, by dividing S_w and Q/w by u
176 (cf. Table 1). By doing so, we were able to evaluate the scaling relationship with and without the
177 common term u to compare the coefficient of determination, r^2, for both relationships. Results of
178 this analysis are shown for NH_4 and NO_3 in Figures 1 and 2.
179 Our results show that $1/K_c$ vs. h are weakly correlated ($r^2_{(NH4)}$=0.029, $p_{(NH4)}$=0.042;
180 $r^2_{(NO3)}$=0.036, $p_{(NO3)}$=0.0057). However, the correlation S_w vs. Q/w is higher ($r^2_{(NH4)}$=0.161,
181 $p_{(NH4)}$<0.00001; $r^2_{(NO3)}$=0.151, $p_{(NO3)}$<0.00001), i.e., r^2 is improved by 452% and 317% for NH_4
182 and NO_3, respectively. These findings suggest that the correlation S_w vs. Q/w is spurious because
183 it is driven by the shared velocity (u) term, rather than by an inherent correlation between the
184 inverse of the nutrient uptake rate constant ($1/K_c$) and stream depth (h). The correlations shown
185 in Figures 1 and 2 are comparable to those reported by Hall et al. (2013). However, we note that
186 the r^2 values do not match because of different datasets (we were limited by the number of studies
187 reporting all parameters S_w, Q, w, h), and our aggregation of reference and altered streams.
188 Regardless, our analysis suggests that the inclusion of the parameter u falsely improves the
189 correlation of the investigated relationships.
190 The mechanism producing spurious correlation in the dataset by Hall et al. (2013) can be
191 viewed more clearly using three arbitrary and uncorrelated variables to represent the relationship
192 between $X_1 \cdot X_2$ and $X_3 \cdot X_2$. We gathered mean daily values for specific conductance (X_1, μS/cm)
193 in the Potomac River (DC) (USGS, 2008a), turbidity (X_2, FNU) in the Little Arkansas River (KS)
194 (USGS, 2008b), and temperature (X_3, °C) in the Rio Grande (NM) (USGS, 2008c) for the year
195 2008. First, we isolated the common factor X_2 and plotted X_1 versus X_3, as shown in Figure 3 (r^2
196 = 0.020, p = 0.012). As expected, there was no statistically significant correlation between these
197 water quality parameters. However, when we incorporated the turbidity (X_2) from a remote
198 location by plotting $X_1 \cdot X_2$ vs. $X_3 \cdot X_2$ (n=313), we found a positive correlation (Figure 4) with a
199 drastic improvement in r^2 (r^2 = 0.846, p < 0.00001). Despite the evident correlation in this
200 relationship, the result is mechanistically irrelevant. Analogous to this case example where the
201 correlation is driven by X_2 (turbidity), the correlation S_w vs. Q/w seems to be driven by u (recall
202 $S_w = u / K_c$ and $Q/w = u \cdot h$ or $Q/w = u \cdot (f(w,h)/w)$). Thus, our findings suggest that the
203 results produced by Hall et al. (2013) regarding the isometric scaling (a=1) of NH_4, and
204 allometric scaling (a>1) of NO_3 and SRP, resulted from an unintentional spurious correlation of
205 S_w vs. Q/w.
206 In addition to scaling nutrient uptake length with specific discharge, Hall et al. (2013) also
207 provide a method for scaling nutrient uptake with stream length using several parameters
208 including the scaling exponent a obtained from the analysis of the scaling relationship shown in
209 equation (2). Our findings have implications for these results as well. While Hall et al. (2013)
210 commented that their results for scaling uptake with stream length was most influenced by b
211 (hydraulic geometry exponent), their analysis still relies on the spurious correlation S_w vs. Q/w
212 not only for parameter a, but also for their subsequent derivations (cf. equations 3-10 in Hall et
213 al. (2013)). Therefore, we also find those results debatable.

Concluding remarks

    The majority of nutrient addition experiments have been performed in headwater streams because they are more experimentally tractable (Tank et al., 2008). Consequently, the dearth of empirical evidence of nutrient processing in large rivers limits our understanding of the role of these rivers in nutrient processing at the catchment scale. While empirical and theoretical advances are being made toward performing nutrient addition experiments in large rivers (Tank et al., 2008; Covino et al., 2010), the need to understand and quantify nutrient export from these systems has driven the development and use of scaling relationships. This motivated the work by Hall et al. (2013) and their results after correlating S_w vs. Q/w for a large dataset of field nutrient experiments suggest that uptake demand (v_f) for NH_4 is relatively constant across stream orders, whereas that for soluble reactive phosphorous (SRP) and NO_3 declines with increasing specific discharge. Here, we demonstrated that these conclusions are subject to debate due to unintentional spurious correlations present in their scaling relationships.

    We also suggest that S_w should be used with extreme caution to scale nutrient uptake because, even though its magnitude can be directly estimated from relatively simple field measurements, its mechanistic interpretation strongly depends on the type of model assumed to describe the real-world system (cf. Table 1 in Runkel (2007)). This is because the same estimate of the magnitude of S_w may be arbitrarily used to co-estimate or constrain the magnitude of parameters describing different (arbitrary) sets of processes (see Cases I-IV in Runkel (2007)). Finally, when a model describing a given set of processes is chosen to interpret how nutrient uptake scales along a river continuum, the main assumption is that such processes operate analogously along the continuum. For example, if the model of advection-decay chosen by Hall et al. (2013) to interpret S_w across stream orders were correct, our analysis presented in Figures 1 and 2 would suggest that headwater streams tend to have higher nutrient uptake rate coefficients, which might be mechanistically supported by their higher ratio of benthic area to cross-sectional area. However, this (biased) analysis would not provide insight into how mass-transfer processes between the main-channel and transient storage zones may control nutrient uptake and retention along the river continuum. Paradoxically, increasing the complexity of the transport models used to derive S_w (e.g., Cases II-IV in Runkel (2007)) does not necessarily improve the mechanistic understanding gained on how nutrient uptake scales along the river continuum because such models are poorly constrained (González-Pinzón et al., 2013), i.e., the number of parameters introduce more degrees of freedom than the data collected (from field and remote measurements) can constrain.

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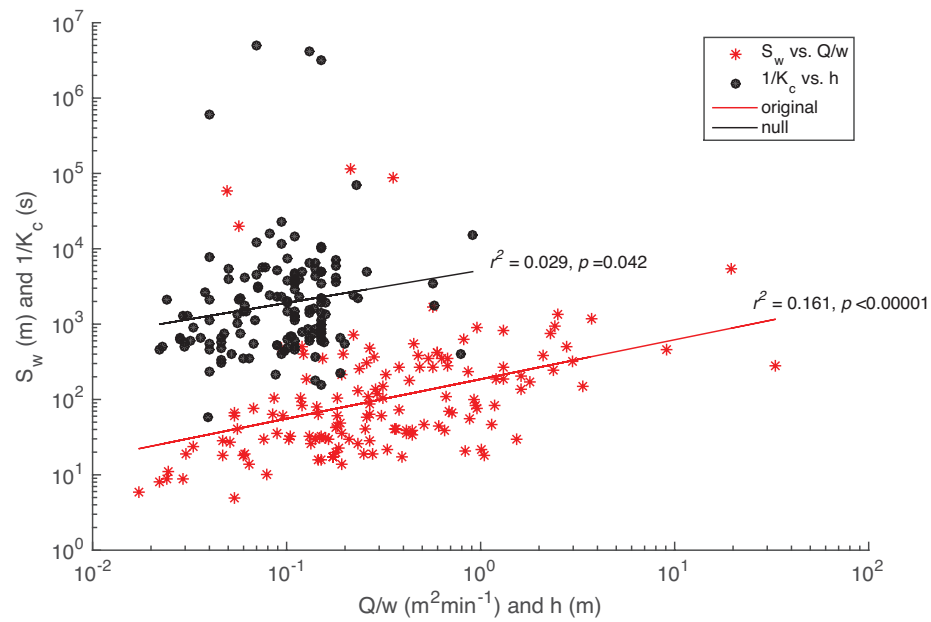
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325 **Figures**
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Figure with axes labeled S_w (m) and $1/K_c$ (s) on the vertical axis (ranging from 10^0 to 10^7) and Q/w (m^{2}min^{-1}) and h (m) on the horizontal axis (ranging from 10^{-2} to 10^2). Legend: S_w vs. Q/w (red asterisk), $1/K_c$ vs. h (black dot), original (red line), null (black line). Annotations: r^2 = 0.029, p =0.042 and r^2 = 0.161, p <0.00001.

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329 **Figure 1 – NH$_4$ scaling relationship with and without shared velocity term. The original**
330 **relationship is represented by S_w vs. Q/w and the null condition by $1/K_c$ vs. h.**
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Figure 2 – NO$_3$ scaling relationship with and without shared velocity term. The original
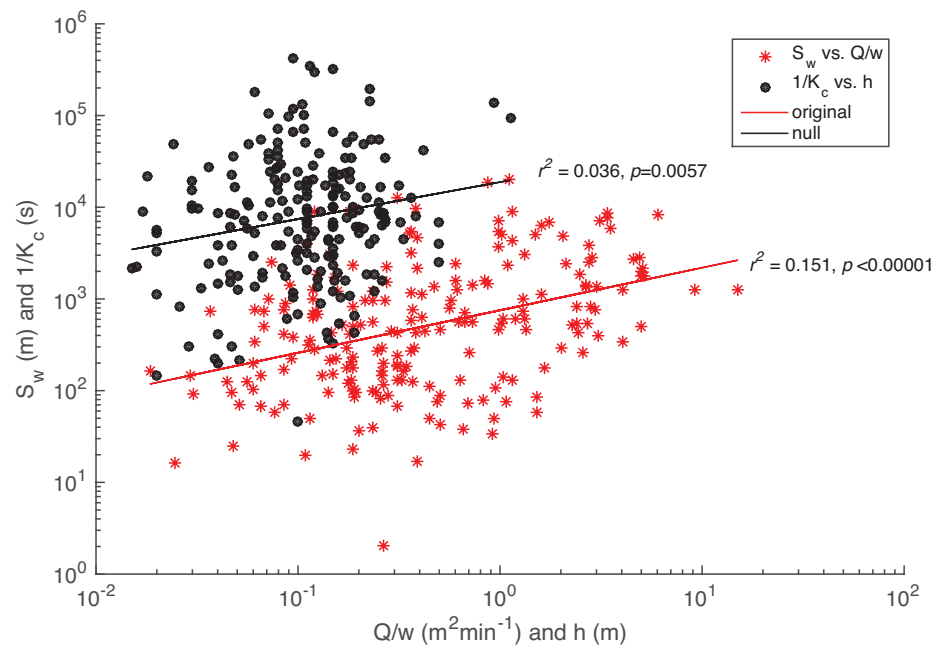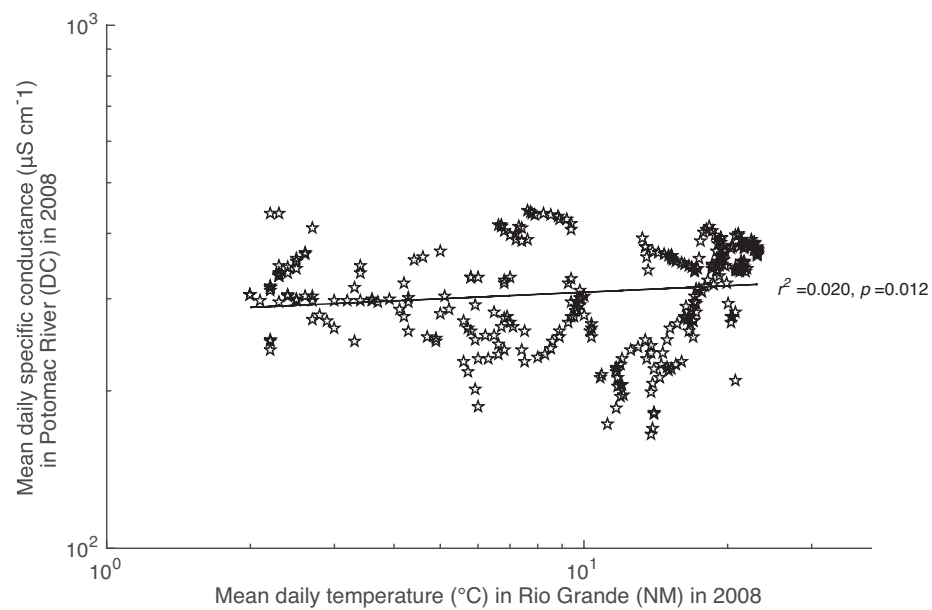relationship is represented by S_w vs. Q/w and the null condition by $1/K_c$ vs. h.

The y-axis label: Mean daily specific conductance (µS cm^{-1}) in Potomac River (DC) in 2008

The x-axis label: Mean daily temperature (°C) in Rio Grande (NM) in 2008

$r^2 = 0.020$, $p = 0.012$

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341 **Figure 3 – Synthetic data correlation, type X_1 vs. X_3, without common parameter, X_2.**
342 **There is a weak correlation between these water quality parameters.**
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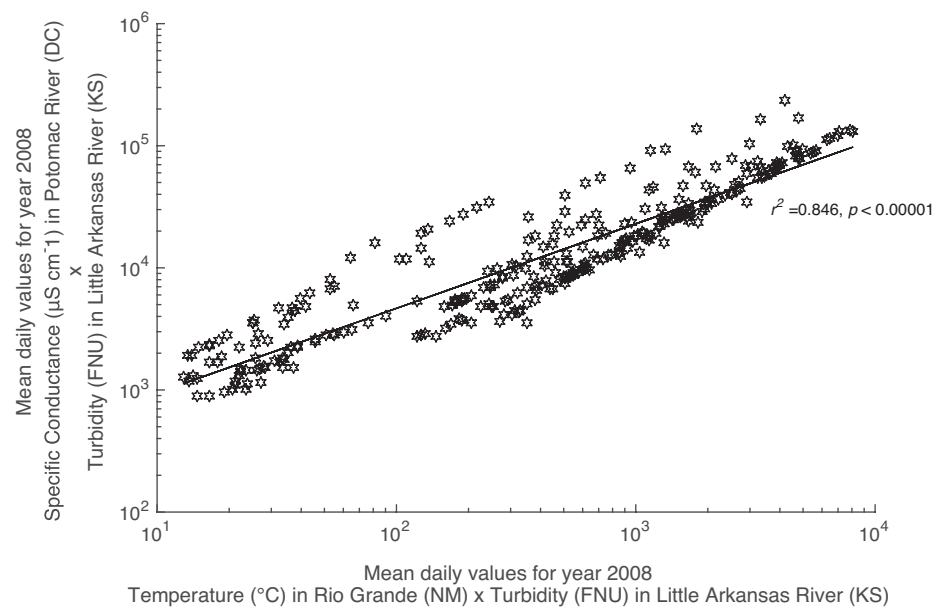
Figure 4 – Synthetic data correlation, type $X_1 \cdot X_2$ vs. $X_3 \cdot X_2$, with common parameter X_2. This spurious correlation results simply because X_2 is common to both quantities.

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