# 1 An objective prior error quantification for regional atmospheric

# 2 inverse applications

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# 1 Abstract

2 Assigning proper prior uncertainties for inverse modeling of CO<sub>2</sub> is of high importance, both to regularize the otherwise ill-constrained inverse problem, and to quantitatively characterize the 3 magnitude and structure of the error between prior and "true" flux. We use surface fluxes derived 4 from three biosphere models VPRM, ORCHIDEE, and 5PM, and compare them against daily 5 6 averaged fluxes from 53 Eddy Covariance sites across Europe for the year 2007, and against repeated aircraft flux measurements encompassing spatial transects. In addition we create synthetic 7 8 observations using modeled fluxes instead of the observed ones, to explore the potential to infer 9 prior uncertainties from model-model residuals. To ensure the realism of the synthetic data analysis, 10 a random measurement noise was added to the modeled tower fluxes which were used as reference. The temporal autocorrelation time for tower model-data residuals was found to be around 30 days 11 12 for both VPRM and ORCHIDEE, but significantly different for the 5PM model with 70 days. This difference is caused by a few sites with large biases between the data and the 5PM model. The 13 14 spatial correlation of the model-data residuals for all models was found to be very short, up to few 15 tens of km but with uncertainties up to 100% of this estimation. Propagating this error structure to 16 annual continental - scale yields an uncertainty of 0.06 Gt C and strongly underestimates uncertainties typically used from atmospheric inversion systems, revealing the existence of another 17 18 potential source of errors. Long spatial e-folding correlation lengths up to several hundreds of km 19 were determined when synthetic data were used. Results from repeated aircraft transects in south-20 western France, are consistent with those obtained from the tower sites in terms of spatial autocorrelation (35 km on average) while temporal autocorrelation is markedly lower (13 days). 21 22 Our findings suggest that the different prior models have a common temporal error structure. 23 Separating the analysis of the statistics for the model data residuals by seasons did not result in any 24 significant differences of the spatial e-folding correlation lengths.

## 1 1 Introduction

2 Atmospheric inversions are widely used to infer surface CO<sub>2</sub> fluxes from observed CO<sub>2</sub> dry mole fractions with a Bayesian approach (Ciais et al., 2000, Gurney et al., 2002, Lauvaux et al., 2008). In 3 4 this approach a limited number of observations of atmospheric CO<sub>2</sub> mixing ratios are used to solve for generally a much larger number of unknowns, making this an ill-posed problem. By using prior 5 6 knowledge of the surface-atmosphere exchange fluxes and by using an associated prior uncertainty. 7 the information retrieved in the inversion from the observations is spread out in space and time 8 corresponding to the spatiotemporal structure of the prior uncertainty. In this way, the solution of 9 the otherwise ill-posed problem is regularized in the sense that the optimization problem becomes 10 one with a unique solution. This prior knowledge typically comes from process-oriented or 11 diagnostic biosphere models that simulate the spatiotemporal patterns of terrestrial fluxes, as well as 12 from inventories providing information regarding anthropogenic fluxes such as energy 13 consumption, transportation, industry, and forest fires.

The Bayesian formulation of the inverse problem is a balance between the a priori and the observational constraints. It is crucial to introduce a suitable prior flux field and assign to it proper uncertainties. When prior information is combined with inappropriate prior uncertainties, this can lead to poorly retrieved fluxes (Wu et al., 2011). Here, we are interested in biosphere-atmosphere exchange fluxes and their uncertainties, and make the usual assumption that the uncertainties in anthropogenic emission fluxes are not strongly affecting the atmospheric observations at the rural sites that are used in the regional inversions of biosphere-atmosphere fluxes.

Typically inversions assume that prior uncertainties have a normal and unbiased distribution, and thus can be represented in the form of a covariance matrix. The covariance matrix is a method to weigh our confidence of the prior estimates. The prior error covariance determines to what extent the posterior flux estimates will be constrained by the prior fluxes. Ideally the prior uncertainty should reflect the mismatch between the prior guess and the actual (true) biosphere-atmosphere exchange fluxes. In this sense it needs to also have the corresponding error structure with its spatial and temporal correlations.

A number of different assumptions of the error structure have been considered by atmospheric CO<sub>2</sub> inversion studies. Coarser scale inversions often neglect spatial and temporal correlations as the resolution is low enough for the inverse problem to be regularized (Bousquet et al., 1999, Rödenbeck et al., 2003a) or assume large spatial correlation lengths (several hundreds of km) over land (Houweling et al., 2004, Rödenbeck et al., 2003b). For the former case large correlation scales are implicitly assumed since fluxes within a grid-cell are fully correlated. For regional scale inversions, with higher spatial grid resolutions which are often less than 100 km, the spatial

1 correlations are decreased (Chevallier et al., 2012) and the error structure need to be carefully 2 defined. A variety of different assumptions exist. This is because only recently an objective approach to define prior uncertainties based on mismatch between modeled and observed fluxes has 3 4 been developed (Chevallier et al., 2006 and 2012). In some regional studies, the same correlations 5 are used as in large scale inversions in order to regularize the problem, although the change of 6 resolution could lead to different correlation scales (Schuh et al., 2010). Alternatively, they are 7 defined with a correlation length representing typical synoptic meteorological systems (Carouge et 8 al., 2010). In other cases, ad-hoc solutions are adopted, where the correlation lengths are assumed to 9 be smaller than in the case of global inversions (Peylin et al., 2005), or derived from climatological 10 and ecological considerations (Peters et al., 2007) where correlation lengths only within the same 11 ecosystem types have a value of 2000 km. In addition some studies use a number of different 12 correlation structures in order to analyze which seems to be the most appropriate one based on 13 cross-validation of the simulated against observed CO<sub>2</sub> mole fractions. The simulated mole 14 fractions were derived using the influence functions and the inverted fluxes (Lauvaux et al., 2012). 15 Michalak et al., (2004) applied a geostatistical approach based on the Bayesian method, in which 16 the prior probability density function is based on an assumed form of the spatial and temporal 17 correlation and no prior flux estimates are required. It optimizes the prior error covariance 18 parameters, the variance and the spatial correlation length by maximizing the probability density 19 function of the observations with respect to these parameters.

20 A recent study by Broquet et al. (2013) obtained good agreements between the statistical 21 uncertainties as derived from the inversion system and the actual misfits calculated by comparing 22 the posterior fluxes to local flux measurements at the European and 1-month scale. These good 23 agreements relied in large part on their definition of the prior uncertainties based on the statistics 24 derived in an objective way from model-data mismatch by Chevallier et al., (2006) and Chevallier 25 et al., (2012). In these studies, modeled daily fluxes from a site scale configuration of the 26 ORCHIDEE model are compared with flux observations made within the global FLUXNET site 27 network, based on the eddy covariance method (Baldocchi et al., 2001), and a statistical upscaling 28 technique is used to derive estimates of the uncertainties in ORCHIDEE simulations at lower 29 resolutions. While typical inversion systems have a resolution ranging from tens of kilometers up to 30 several degrees (hundreds of km), with the true resolution of the inverse flux estimates being even 31 coarser, the spatial representativity of the flux observations typically covers an area with a radius of 32 around a kilometer. Considering also the scarcity of the observing sites in the flux network, the 33 spatial information they bring is limited without methods for up-scaling such as the one applied by 34 Chevallier et al., (2012). Typical approaches to up-scale site level fluxes deploy for example model 35 tree algorithms, a machine learning algorithm which is trained to predict carbon flux estimates

based on meteorological data, vegetation properties and types (Jung et al., 2009, Xiao et al., 2008),
or neural networks (Papale and Valentini 2003). Nevertheless eddy covariance measurements
provide a unique opportunity to infer estimates of the prior uncertainties by examining model-data
misfits for spatial and temporal autocorrelation structures.

5 Hilton et al., (2012) studied also the spatial model – data residual error structure using a 6 geostatistical method. Hilton's study is focused on the seasonal scale, i.e. investigated residual 7 errors of seasonally aggregated fluxes. However, the state space (variables to be optimized 8 considering also their temporal resolution) of current inversion systems is often at high temporal 9 resolution (daily or even three-hourly optimizations). Further, the statistical consistency between the 10 error covariance and the state space is crucial. Thus the error structure at the daily time-scale is of 11 interest here, and can be used in atmospheric inversions of the same temporal resolution. Similar to 12 Hilton's study we select an exponentially decaying model to fit the spatial residual autocorrelation.

13 In this study, we augment the approach of Chevallier et al., (2006 and 2012), to a multi-model - data 14 comparison, investigating among others a potential generalization of the error statistics, suitable to be applied by inversions using different biosphere models as priors. This expectation is derived 15 16 from the observation that the biosphere models, despite their potential differences typically have 17 much information in common, such as driving meteorological fields, land use maps, or remotely 18 sensed vegetation properties, and sometimes even process descriptions. We evaluate model – model 19 mismatches to (I) investigate intra-model autocorrelation patterns and (II) to explore whether they 20 are consistent with the spatial and temporal e-folding correlation lengths of the model - data 21 mismatch comparisons. Model comparisons have been used in the past to infer the structure of the 22 prior uncertainties. For example, Rödenbeck et al., (2003b) used prior correlation lengths based on 23 statistical analyses of the variations within an ensemble of biospheric models. This approach is to a 24 certain degree questionable, as it is unclear how far the ensemble of models actually can be used as 25 representative of differences between modeled and true fluxes. However, if a relationship between 26 model - data and model - model statistics can be established for a region with dense network of 27 flux observations, it could be used to derive prior error structure also for regions with a less dense observational network. 28

Moreover, to improve the knowledge of spatial flux error patterns, we make use of a unique set of aircraft fluxes measured on 2-km spatial windows along intensively sampled transects of several tens of km, ideally resolving spatial and temporal variability of ecosystem fluxes across the landscape without the limitation of the flux network with spatial gaps in between measurement locations. Lauvaux et al., (2009) compared results of a regional inversion against measurements of fluxes from aircraft and towers, while this is the first attempt to use aircraft flux measurements to 1 assess spatial and temporal error correlation structures.

This study focuses on the European domain for 2007 (tower data) and 2005 (aircraft data) and uses output from high-resolution biosphere models that have been used for regional inversions. Eddy covariance tower fluxes were derived from the FLUXNET ecosystem network (Baldocchi et al., 2001), while aircraft fluxes were acquired within the CarboEurope Regional Experiment (CERES) in southern France. The methods and basic information regarding the models are summarized in Section 2. The results from model-data and model-model comparisons are detailed in Section 3. Discussion and conclusions are following in Section 4.

9

### 10 2 Data and Methods

11 Appropriate error statistics for the prior error covariance matrix are derived from comparing the 12 output of three biosphere models which are used as priors for regional scale inversions with flux data from the ecosystem network and aircraft. We investigate spatial and temporal autocorrelation 13 14 structures of the model-data residuals. The temporal autocorrelation is a measure of similarity between residuals at different times but at the same location as a function of the time difference. 15 16 The spatial autocorrelation refers to the correlation, at a given time, of the model-data residuals at 17 different locations as a function of spatial distance. With this analysis we can formulate and fit an 18 error model such as an exponentially decaying model, which can be directly used in the mesoscale 19 inversion system to describe the prior error covariance.

20

### 21 2.1 Observations

A number of tower sites within the European domain, roughly expanding from -12° E to 35° E and 22 35° N to 61° N (see also Fig. 1), provide us with direct measurements of CO<sub>2</sub> biospheric fluxes 23 24 using the eddy covariance technique. This technique computes fluxes from the covariance between vertical wind velocity and CO<sub>2</sub> dry mole fraction (Aubinet et al., 1999). We use Level 3, quality 25 26 checked, half hourly observations of net ecosystem exchange fluxes (NEE), downloaded from the European Flux Database (www.europe-fluxdata.eu), and listed by site in Table 1. Each site is 27 28 categorized into different vegetation types (Table 1). A land cover classification is used to label the 29 sites as crop (17 sites), deciduous forest (6), evergreen forest (17), grassland (8), mixed forest (3), 30 savannah (1 site), and shrub land (1). For the current study we focus on observations from these 53 31 European sites during the year 2007 (Fig. 1).

Additionally, aircraft fluxes are used, obtained with an eddy covariance system installed onboard a
 SkyArrow ERA aircraft (Gioli et al., 2006). Flights were made in southern France during CERES

(CarboEurope Regional Experiment) from May 17 to June 22, 2005. Eddy covariance fluxes were
 computed on 2-km length spatial windows along transects of 69-km above forest and 78-km above
 agricultural land, flown 52 and 54 times respectively, covering the daily course. Exact routes are
 reported in Dolman et al., 2006.

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### 6 **2.2 Biosphere models**

7 We simulate CO<sub>2</sub> terrestrial fluxes for 2007 with three different biosphere models described in the 8 following. The "Vegetation Photosynthesis and Respiration Model" (VPRM) (Mahadevan et al., 9 2008), used to produce prior flux fields for inverse studies (Pillai et al., 2012), is a diagnostic model 10 that uses EVI - enhanced vegetation index and LSWI - land surface water index from MODIS, a 11 vegetation map (Synmap, Jung et al., 2006) and meteorological data (temperature at 2m and downward shortwave radiative flux extracted from ECMWF short term forecast fields at 0.25 12 13 degrees resolution) to derive gross biogenic fluxes. VPRM parameters controlling respiration and 14 photosynthesis for different vegetation types (a total of four parameters per vegetation type) were 15 optimized using eddy covariance data for the year 2005 collected during the CarboEuropeIP project (Pillai et al., 2012). For this study, VPRM fluxes are provided at hourly temporal resolution and at 16 17 three spatial resolutions of 1, 10 and 50 km (referred to as VPRM1, VPRM10 and VPRM50). The 18 difference between the 1,10 and 50 km resolution version is the aggregation of MODIS indices to 19 either 1, 10 or 50 km, otherwise the same meteorology and VPRM parameters are used. At 10 km 20 resolution VPRM uses a tiled approach, with fractional coverage for the different vegetation types, 21 and vegetation type specific values for MODIS indices. For the comparison with the aircraft data 22 VPRM produced fluxes for 2005 at 10 km spatial resolution.

23 The "Organizing Carbon and Hydrology In Dynamic Ecosystems", ORCHIDEE, model (Krinner et 24 al., 2005) is a process based site scale to global land surface model that simulates the water and 25 carbon cycle using meteorological forcing (temperature, precipitation, humidity, wind, radiation, 26 pressure). The water balance is solved at a half-hourly time step while the main carbon processes 27 (computation of a prognostic LAI, allocation, respiration, turnover) are called on a daily basis. It 28 uses a tiled approach, with fractional coverage for 13 Plant Functional Types (PFT). It has been 29 extensively used as prior information in regional and global scale inversions (Piao et al., 2009, 30 Broquet et al., 2013). For the present simulation, we use a global configuration of the version 1.9.6 of ORCHIDEE, where no parameter has been optimized against eddy covariance data. The model is 31 32 forced with 0.5° WFDEI meteorological fields (Weedon et al., 2014). The PFT map is derived from 33 an Olson land cover map (Olson 1994) based on AVHRR remote sensing data (Eidenshink and 34 Faundeen 1994). The fluxes are diagnosed at 3-hourly temporal resolution and at 0.5 degree

1 horizontal resolution.

2 The "5 parameter model" (5PM) (Groenendijk et al., 2011), also used in atmospheric inversions (Tolk et al., 2011, Meesters et al., 2012), is a physiological model describing transpiration, 3 4 photosynthesis, and respiration. It uses MODIS LAI (leaf area index) at 10km resolution, 5 meteorological data (temperature, moisture, and downward shortwave radiative flux, presently from 6 ECMWF at 0.25 degrees resolution), and differentiates PFTs for different vegetation types and 7 climate regions. 5PM fluxes are at hourly temporal resolution. The optimization has been done with 8 EC-data from Fluxnet as described (except for heterotrophic respiration) in Groenendijk et al., 2011. Regarding the heterotrophic respiration, an ad hoc optimization using Fluxnet EC-data from 9 10 2007 was performed since no previous optimization was available.

11 Modeled fluxes for all above mentioned sites have been provided by the different models by 12 extracting the fluxes from the grid cells which encompass the EC station location using vegetation 13 type specific simulated fluxes, i.e. using the vegetation type within the respective grid cell for which 14 the eddy covariance site is assumed representative. For most of the sites the same vegetation type was used for model extraction as long as this vegetation type is represented within the grid-cell. As 15 VPRM uses a tile approach, for two cases ("IT-Amp", "IT-MBo") the represented vegetation type 16 (crop) differ from the actual one (grass). For these cases, the fluxes corresponding to crop were 17 18 extracted. Fluxes were aggregated to daily fluxes in the following way: first, fluxes from VPRM 19 and 5PM as well as the observed fluxes were temporally aggregated to match with the ORCHIDEE 20 3-hourly resolution; in a second step we created gaps in the modeled fluxes where no observations 21 were available; the last step aggregated to daily resolution on the premise that a) the gaps covered 22 less than 50% of the day, and b) the number of gaps (number of individual 3-hourly missing values) 23 during day and during night were similar (not different by more than a factor two) to avoid biasing.

Spatial and temporal correlation structures and the standard deviation of flux residuals (model-24 25 observations) were examined for daily fluxes over the year 2007. Simulated fluxes from the different models are at different spatial resolution, which makes comparisons difficult to interpret. 26 27 For the model-data residual analysis, the models VPRM1, VPRM10, ORCHIDEE and 5PM were used. We note that VPRM1 with 1 km resolution is considered compatible when comparing with 28 29 local measurements. For the model-model analysis we use VPRM50 at 50km resolution when comparing with ORCHIDEE fluxes as both models share the same resolution. VPRM10 is 30 31 considered also appropriate for comparisons with 5PM model as they both share same resolution (MODIS LAI resolution of 1 km aggregated to 10 km and meteorological resolution at 0.25 32 33 degrees). Following we compare VPRM50 with 5PM to investigate if the different spatial resolution 34 influences the correlation scale as a measure of how trustful might be the derived scales from

1 ORCHIDEE – 5PM comparisons.

2 For the aircraft analysis, only the VPRM was used since it is the only model with spatial resolution 3 (10 km) comparable with aircraft flux footprint and capable of resolving spatial variability in 4 relatively short flight distances. Aircraft NEE data, natively at 2 km resolution along the track, have 5 been aggregated into 10 km segments, to maximize the overlap with the VPRM grid, obtaining 6 6 grid points in forest transects and 8 in agricultural land transects. Footprint areas of aircraft fluxes 7 were computed with the analytical model of Hsieh et al. (2000), yielding an average footprint width 8 containing 90% of the flux of 3.9 km. Averaging also over the different wind directions 9 (perpendicular or parallel to the flight direction), and taking into account the 10 km length of the segments, the area that the aircraft flux data corresponds to, is arround 23.5 km<sup>2</sup>  $\pm$  12 km<sup>2</sup>. VPRM 10 11 fluxes at each aircraft grid cell were extracted, and then linearly interpolated to the time of each flux 12 observation.

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# 14 **2.3 Analysis of model-observation differences**

Observed and modeled fluxes are represented as the sum of the measured or simulated values and an error term, respectively. When we compare modeled to observed data this error term is a combination of model (the prior uncertainty we are interested in) and observation error. Separating the observation error from the model error in the statistical analysis of the model-observation mismatch is not possible; therefore e-folding correlation length estimations do include the observation error term. Nevertheless later in the analysis of model-model differences we assess the impact of the observation error on estimated e-folding correlation lengths.

The tower temporal autocorrelation is computed between the time series of model-observations differences  $x_{l,i}$  at site *l* and the same series lagged by a time unit k (Eq. 1), where  $\overline{x}$  is the overall mean and N the number of observations:

25 
$$r_{l}(k) = \frac{\sum_{i=1}^{N-k} (x_{l,i} - \overline{x_{l}}) \cdot (x_{l,i+k} - \overline{x_{l}})}{\sum_{i=1}^{N} (x_{l,i} - \overline{x_{l}})^{2}}$$
(1)

In order to reduce boundary effects in the computation of the autocorrelation at lag times around one year, the one-year flux time series data (model and observations) for each site was replicated four times. This follows the approach of Chevallier et al., (2012), where sites with at least three consecutive years of measurements have been used.

30 In the current analysis we introduce the all-site temporal autocorrelation by simultaneously

1 computing the autocorrelation for all the observation sites, with M the number of the sites:

. . . . .

$$_{2} r(k) = \frac{\sum_{l=1}^{M} \sum_{i=1}^{N-k} (x_{l,i} - \overline{x_{l}}) \cdot (x_{l,i+k} - \overline{x_{l}})}{\sum_{l=1}^{M} \sum_{i=1}^{N} (x_{l,i} - \overline{x_{l}})^{2}} (2)$$

3 Temporal correlation scales  $\tau$  were derived by fitting an exponentially decaying model:

$$4 \qquad r = (1 - \alpha) \cdot e^{-\frac{t}{\tau}} \tag{3}$$

5 Here *t* is the time lag. For the exponential fit, lags up to 180 days were used (thus the increase in 6 correlations for lag times larger than 10 months is excluded). At zero lag time the correlogram has a 7 value of one (fully correlated), however for even small lag times this drops to values smaller than 8 one, also known as the nugget effect. The nugget effect is driven by measurement errors and 9 variations at distances (spatial or temporal) smaller than the sampling interval. For this we include 10 the nugget effect variable  $\alpha$ .

The aircraft temporal autocorrelation was similarly computed according to Eq. 1 using VPRM, and the same exponentially decaying model (Eq. 3) was used to fit the individual flight flux data. The temporal interval was limited at 36 days by the experiment duration.

14 For the spatial analysis the correlation between model-observation residuals at two different 15 locations (i.e sites or aircraft grid points) separated by a specific distance was computed in a way 16 similar to the temporal correlation, and involved all possible pairs of sites and aircraft grid points. 17 Additional data treatment for the spatial analysis was applied to reduce the impact of tower data 18 gaps, as it is possible that the time series for two sites might have missing data at different times. 19 Thus in order to have more robust results, we also examined spatial structures by setting a minimum 20 threshold of 150 days of overlapping observations within each site pair. Furthermore spatial 21 correlation was investigated for seasonal dependence, where seasons are defined as summer (JJA), 22 fall (SON), winter (DJF for the same year), and spring (MAM). In those cases a different threshold 23 of 20 days of overlapping observations was applied. We note that we do not intend to investigate the 24 errors at the seasonal scale but rather to study if different seasons trigger different error correlation 25 structures.

To estimate the spatial correlation scales, the pairwise correlations were grouped into bins of 100 km distance for towers and 10 km for aircraft data, respectively (*dist*). Following the median for each bin was calculated, and a model similar to Eq. 3 was fitted, but omitting the nugget effect variable:

$$r = e^{\frac{dist}{d}}$$
(4)

2 The nugget effect could not be constrained simultaneously with the spatial correlation scale d, given 3 the relatively coarse distance groups, the fast drop in the median correlation from one at zero 4 distance to small values for the first distance bin combined with somewhat variations at larger 5 distances. Note that this difference between the spatial and the temporal correlation becomes 6 obvious in the results section 3.

7 Confidence intervals for the estimated model parameters were computed based on the profile 8 likelihood (Venzon and Moolgavkar, 1987) as implemented within the "confint" function from 9 MASS package inside the R statistical language.

10 As aircraft fluxes cannot obviously be measured at the same time at different locations, given the 11 relatively short flight duration (about one hour) we treated aircraft flux transect as instantaneous 12 'snapshots' of the flux spatial pattern across a landscape, neglecting temporal variability that may 13 have occurred during flight.

14

1

#### 15 2.4 Analysis of model-model differences

16 We evaluate both model-data flux residuals and model-model differences in a sense of pairwise 17 model comparisons, in order to assess if model-model differences can be used as proxy for the prior 18 uncertainty, assuming that models have independent prior errors. For the model-model analysis 19 fluxes derived from the model pairs VPRM50-ORCHIDEE and VPRM10-5PM share the same 20 spatial resolution and therefore are fully comparable. Similar to the model-observation analysis, the 21 statistical analysis gives a combined effect of both model errors. We assess the impact in the error 22 structure between model-observation and model-model comparisons caused by the observation 23 error by adding a random measurement error to each model-model comparison. This error has the 24 same characteristics as the observation error which is typically associated with eddy covariance 25 observations; the error characteristics were derived from the paired observation approach 26 (Richardson et al., 2008). Specifically, we implement the flux observation error as a random process 27 (white noise) with a double-exponential probability density function. This can be achieved by 28 selecting a random variable u drawn from the uniform distribution in the interval (-1/2, 1/2), and 29 then applying Eq. 5 to get a Laplace distribution (also referred to as the double-exponential)

30 
$$x = \mu - \frac{\sigma}{\sqrt{2}} \cdot \operatorname{sgn}(u) \cdot \ln(1 - 2 \cdot |u|)$$
 (5)

31 Here  $\mu=0$  and  $\sigma$  is the standard deviation of the double-exponential. We compute the  $\sigma$  according to 1 Richardson et al., (2006) as

$$2 \qquad \sigma = \alpha_1 + \alpha_2 \cdot |F| \tag{6}$$

where F is the flux and  $\alpha_1$ ,  $\alpha_2$  are scalars specific to the different vegetation classes. Lasslop et al., 3 (2008) found that the autocorrelation of the half hourly random errors is below 0.7 for a lag of 30 4 5 min, and falls off rapidly for longer lag times. Thus we assume the standard deviation for hourly 6 random errors to be comparable with the half hourly errors. Hourly random errors specific for each 7 reference model are generated for each site individually. With ORCHIDEE as reference with fluxes 8 at 3-hourly resolution, a new ensemble of 3-hourly random noise was generated with  $\sigma$  for the 3-9 hourly errors modified (divided by the square root of three to be coherent with the hourly  $\sigma$ ). As both modeled and observed fluxes share the same gaps, the random errors were aggregated to daily 10 resolution, with gaps such to match those of observed fluxes. Finally the daily random errors were 11 12 added to the modeled fluxes.

13

### 14 3 Results

### 15 **3.1 Model-data comparison for tower and aircraft fluxes**

16 Observed daily averaged NEE fluxes, for all ground sites and the full time-series, yield a standard 17 deviation of 3.01  $\mu$ mol m<sup>-2</sup> s<sup>-1</sup>, while the modeled fluxes were found to be less spatially varying and 18 with a standard deviation of 2.84, 2.80, 2.53, 2.64  $\mu$ mol m<sup>-2</sup> s<sup>-1</sup> for VPRM10, VPRM1, ORCHIDEE 19 and 5PM respectively.

20 The residual distribution of the models defined as the difference between simulated and observed daily flux averages for the full year 2007 was found to have a standard deviation of 2.47, 2.49, 2.7 21 and 2.25 µmol m<sup>-2</sup> s<sup>-1</sup> for VPRM10, VPRM1, ORCHIDEE and 5PM respectively. Those values are 22 23 only slightly smaller than the standard deviations of the observed or modeled fluxes themselves. 24 This fact is in line with the generally low fraction of explained variance with r-square values of 25 0.31, 0.27, 0.12, and 0.25 for VPRM10, VPRM1, ORCHIDEE and 5PM respectively. When using site-specific correlations (correlations computed for each site, then averaged over all sites), the 26 27 average fraction of explained variance increases to 0.38, 0.36, 0.35, and 0.42, for VPRM10, VPRM1, ORCHIDEE and 5PM, respectively. Note that for deseasonalized time-series (using a 2<sup>nd</sup> 28 29 order harmonic, not shown) the same picture emerges with increased averaged site specific 30 correlation compared to correlations using all sites. This indicates better performance for the models 31 to simulate temporal changes (not only seasonal, but also synoptic) at the site level. Further, the 32 differences between site-specific to the overall r-square values indicate limitation of the models to 33 reproduce observed spatial (site to site) differences. Figure 2 shows the correlation between 34 modeled and observed daily fluxes as a function of the vegetation type characterizing each site. All

models exhibit a significant scatter of the correlation ranging from 0.9 for some sites to 0 or even
negative correlation for some crop sites, with the highest correlation coefficients for deciduous and
mixed forest.

The distribution is biased by -0.07, 0.26, 0.92 and 0.25  $\mu$ mol m<sup>-2</sup> s<sup>-1</sup> for VPRM10, VPRM1, ORCHIDEE and 5PM, respectively. Figure 3 shows the distribution of bias (defined as modeled – observed fluxes) for different vegetation types. Bias and standard deviation seem to depend on the vegetation type for all models, without a clear general pattern.

8 The temporal autocorrelation was calculated for model-data residuals for each of the flux sites ("site 9 data" in Fig. 4), but also for the full dataset ("all-site" in Fig. 4). The "all site" temporal 10 autocorrelation structure of the residuals appears to have the same pattern for all models. It decays 11 smoothly for time lags up to 3 months and then remains constant near to 0 or to some small 12 negative values. The temporal autocorrelation increases again for time lags > 10 months, which is 13 caused by the seasonal cycle. These temporal autocorrelation results agree with the findings of 14 Chevallier et al., (2012).

15 The exponentially decaying model in Eq. 3 was used to fit the data. At zero separation time (t=0) 16 the correlogram value is 1. However the correlogram exhibits a nugget effect (values ranging from 17 0.31 to 0.48 for the different models) as a consequence of an uncorrelated part of the error. For the 18 current analyses we fit the exponential model with an initial correlation different from 1. The fit has 19 a root mean square error ranging from 0.036 to 0.059 for the different biosphere models. The 20 normalized RMSE (i.e. RMSE divided by the range of the autocorrelation) results in values ranging 21 from 0.061 to 0.092 indicating relative errors in the fit of less than 10%. The e-folding time (defined 22 as the lag required for the correlation to decrease by a factor of e (63% of its initial value) ranged 23 between 26-70 days for the different models (see Table 2). Specifically, for VPRM10 and VPRM1 24 the e-folding time is 32 and 33 days respectively (30-34 days within 95% confidence interval for 25 both). Confidence intervals for the e-folding time were calculated by computing the confidence intervals of the parameter in the fitted model. For ORCHIDEE best fit was 26 days (23-28 days 26 27 within 95% confidence interval). In contrast, 5PM yields a significantly longer correlation time 28 between 65-75 days (95% confidence interval) with the best fit being 70 days.

For a number of sites a large model-data bias was found. In order to assess how the result depends on individual sites where model-data residuals are more strongly biased the analysis was repeated under exclusion of sites with an annual mean of model-data flux residuals larger than 2.5µmol/m<sup>2</sup>s. This threshold value is roughly half of the most deviant bias. In total 9 sites ("CH-Lae", "ES-ES2", "FR-Pue", "IT-Amp", "IT-Cpz", "IT-Lav", "IT-Lec", "IT-Ro2", "PT-Esp") across all model-data residuals were excluded. From these sites "CH-Lae" appears to have serious problems related to the

1 steep terrain, where the basic assumptions made for eddy covariance flux measurements are not 2 applicable (Göckede et al., 2008). The rest of the sites are located in the Mediterranean region, and suffer from summer drought according to the Köppen-Geiger climate classification map (Kottek et 3 4 al., 2006); in those cases a large model - data bias is expected as existing models tend to have 5 difficulties to estimate carbon fluxes for drought prone periods (Keenan et al., 2009). The modeldata bias at those sites does not necessarily exceed the abovementioned threshold of 2.5µmol/m<sup>2</sup>s 6 7 simultaneously for each individual model, but a larger bias than the average was detected. After 8 exclusion of those sites the temporal correlation times were found to be between 33-35 days within 9 95% confidence interval for 5PM with the best fit value being 34 days. The rest of the models had temporal e-folding times of 27, 29 and 24 days (1<sup>st</sup> row of Table 2), while the all-site correlation 10 remains positive for lags <76, <79, <66 days for VPRM10, VPRM1 and ORCHIDEE respectively. 11 Some weak negative correlations exist, with a minimum value of -0.06, -0.02, -0.09, -0.005 for 12 13 VPRM10, VPRM1, ORCHIDEE and 5PM respectively.

The temporal correlation of differences between VPRM10 and aircraft flux measurements could be computed for time intervals up to 36 days (Fig. 5) corresponding to the duration of the campaign. The correlation shows an exponential decrease, and levels off after about 25 days with an e-folding correlation time of 13 days (range of 10 - 16 days within the 95% confidence interval). Whilst the general behavior is consistent with results obtained for VPRM-observation residuals for flux sites, the correlation time is two times smaller.

20 Regarding spatial error correlations, results for all models show a dependence on the distance 21 between pairs of sites. The median correlation drops within very short distances (Fig. 6). Fitting the 22 simple exponentially decaying model (Eq. 4) to the correlation as a function of distance we find an 23 e-folding correlation length d of 40, 37, 32 and 31 km with a root mean square error (RMSE) of 24 0.14, 0.09, 0.05 and 0.07 for VPRM10, VPRM1, ORCHIDEE and 5PM, respectively. The 25 normalized RMSE is found to have values ranging from 0.05 to 0.084 indicating relative errors of 26 the fit less than 9%. Spatial correlation scales are also computed for a number of different data 27 selections (cases) in addition to the standard case shown in Fig. 6 (case S): using only pairs with at 28 least 150 overlapping days of non-missing data (case S\*), using only pairs with identical PFT (case 29 I), using only pairs with different PFT (case D), and using only pairs with at least 150 overlapping 30 days for the D and I cases (cases D\*, I\*). The results for these cases are summarized in Fig. 7. Also 31 95% confidence intervals were computed, and the spread spatial correlation was found to be 32 markedly more critical than for the time correlations. Note that for some cases the 2.5%-ile (the 33 lower bound of the confidence interval) hit the lower bound for correlation lengths (0 km). The e-34 folding correlation lengths are similar for each of the models: this also means that no dependence on

the spatial resolution was detectable. Further we examined also the spatial autocorrelation from
 VPRM50-data residuals with no significant difference compared to previous results.

3 Interestingly, if we restrict the analysis to pairs with at least 150 overlapping days between site 4 pairs, larger correlation scales are found (case S\* in Fig. 7). Considering only pairs with different PFT (case D), consistently, all e-folding correlation lengths are found to be smaller compared to the 5 6 standard case (S). This is expected to a certain degree, as model errors should be more strongly 7 correlated between sites with similar PFTs than between sites with different PFTs. By considering 8 only pairs within the same vegetation type (case I) we observe a significant increase of the e-folding 9 correlation length relative to case S for VPRM at 10 and 1 km resolution to values of 432 km and 10 305 km, respectively. The ORCHIDEE and 5PM models show some (although not significant) 11 increase in e-folding correlation length. Restricting again the analysis to pairs with at least 150 12 overlapping days for the D and I cases (D\*, I\*) we observe an increase of the e-folding correlation 13 lengths that is however significant only for VPRM at 10 and 1 km.

Seasonal dependence of the e-folding correlation lengths for at least 20 overlapping days per season and for all site-pairs is also shown in Fig. 7. VPRM showed somewhat longer correlation lengths during spring and summer, ORCHIDEE had the largest lengths occurring during summer and fall, and 5PM e-folding correlation lengths show slightly enhanced values during spring and summer. However, none of these seasonal differences are significant with respect to the 95% confidence interval.

20 The spatial error correlation between VPRM10 model and aircraft fluxes measured during May-21 June along continuous transects at forest and agriculture land use (Fig. 8) shows an exponential 22 decay up to the maximum distance that was encompassed during flights (i.e. 70 km). Of note is that 23 only two measurements were available at 60 km distance and none for larger distances making it 24 difficult to identify where the asymptote lies. Nevertheless fitting the decay model (Eq. 4) leads to d25 = 35km (26 - 46 km within the 95% confidence interval), which is in good agreement with the spatial correlation scale derived for VPRM10 using flux sites during both spring and summer (Fig. 26 27 7).

28

# 29 **3.2 Model-model comparison**

We investigate the model-model error structure of NEE estimates by replacing the observed fluxes which were used as reference, with simulated fluxes from all the biosphere models. Note that for consistency with the model-data analysis, the simulated fluxes contained the same gaps as the observed flux time series. The e-folding correlation time is found to be slightly larger compared to

1 the model-data correlation times, for most of the cases. An exception is the 5PM-VPRM10 pair 2 which produced remarkably larger correlation time (Table 2). Specifically, VPRM50-ORCHIDEE 3 and VPRM10-5PM residuals show correlation times of 28 days (range between 24-32 days within 4 95% confidence interval) and 131 (range between 128-137 days within 95% confidence interval), 5 respectively. Significantly different e-folding correlation times are found for VPRM50-5PM compared to VPRM10-5PM with correlation times of 52 days (range between 49-56 days within 6 7 95% confidence interval). Repeating the analysis excluding sites with residual bias larger than 8 2.5µmol/m<sup>2</sup>s, correlation times of 28 and 100 days for VPRM50-ORCHIDEE and VPRM10-5PM 9 are found, respectively. If we use ORCHIDEE-5PM pair the e-folding correlation time found to be 10 38 days (range between 35-41 days within 95% confidence interval).

11 Although the e-folding correlation times show but minor differences compared to the model-data 12 residuals, this is not the case for the spatial correlation lengths (Fig. 9). The standard case (S) was 13 applied for the annual analysis, with no minimum number of days with overlapping non-missing 14 data for each site within the pairs. Taking VPRM50 as reference, much larger e-folding correlation 15 lengths of 371 km with a range of 286-462 km within 95% confidence interval yielded for VPRM50-ORCHIDEE comparisons, and 1066 km for VPRM50-5PM were found. However 16 17 VPRM10-5PM analysis which is also considered appropriate in terms of the spatial resolution compatibility contrary to the VPRM50-5PM pair, is in good agreement with VPRM50-ORCHIDEE 18 19 spatial scale (230-440 km range within 95% confidence interval with the best fit being 335 km). 20 With ORCHIDEE as reference the e-folding correlation length for the ORCHIDEE-5PM 21 comparison is 276 km with a range of 183-360 km within 95% confidence interval. However the 22 later correlation length might be affected by the different spatial resolution as the difference 23 between VPRM10 and VPRM50 against 5PM suggests. Seasonal e-folding correlation lengths, 24 using a minimum of 20 days overlap in the site-pairs per season (Fig. 9), are also significantly 25 larger compared with those from the model-data analysis.

26 When we add the random measurement error to the modeled fluxes used as reference (crosses in 27 Fig. 9), we observe only slight changes in the annual e-folding correlation lengths, without a clear pattern. The correlation lengths show a random increase or decrease but limited up to 6%. 28 29 Interestingly, the seasonal e-folding correlation lengths for most of the cases show a more clear 30 decrease. For example, the correlation length of the VPRM10-5PM residuals during winter, 31 decreases by 22% or even more for spring season. Despite this decrease, the e-folding seasonal 32 correlation lengths remain significantly larger in comparison to those from the model-data analysis. 33 Overall, all models when used as reference show the same behavior with large e-folding correlation 34 lengths that mostly decrease slightly when the random measurement error is included. Although the random measurement error was added as "missing part" to the modeled fluxes to better mimic actual flux observations, it did not lead to correlation lengths similar to those from the model-data residual analysis. To investigate if a larger random measurement error could cause spatial correlation scales in model-model differences, we repeated the analysis with artificially increased random measurement error (multiplying with a factor between 1 and 15). Only for very large random measurement errors did the model-model e-folding correlation lengths start coinciding with those of the model-data residuals (Fig. 10).

8

# 9 4. Discussion and conclusions

10 We analyzed the error structure of a-priori NEE uncertainties derived from a multi-model - data 11 comparison by comparing fluxes simulated by three different vegetation models to daily averages of 12 observed fluxes from 53 sites across Europe, categorized into 7 land cover classes. The different 13 models showed comparable performance with respect to reproducing the observed fluxes; we found 14 mostly insignificant differences in the mean of the residuals (bias) and in the variance. Site-specific 15 correlations between simulated and observed fluxes are significantly higher than overall 16 correlations for all models, which suggest that the models struggle with reproducing observed 17 spatial flux differences between sites. Furthermore, the site-specific correlations reveal a large 18 spread even within the same vegetation class, especially for crops (Fig. 2). This is likely due to the 19 fact that none of the models uses a specific crop model that differentiates between the different crop 20 types and their phenology. The models using remotely sensed vegetation indices (VPRM and 5PM) 21 better capture the phenology; ORCHIDEE is the only model that differentiates between C<sub>3</sub> and C<sub>4</sub> 22 plants, but shows the largest spread in correlation for the crop. Differences in correlations between 23 the different vegetation types were identified for all the biosphere models, however it must be noted 24 that the number of sites per vegetation type is less than 10 except for crop and evergreen forests.

Model-data flux residual correlations were investigated to give insights regarding prior error temporal scales which can be adopted by atmospheric inversion systems. Whilst fluxes from ORCHIDEE model are at much coarser resolution compared to the representative area from the flux measurements, VPRM1 fluxes (1 km resolution and only the meteorology at 25 km) are considered appropriate for the comparisons. Despite the scale mismatch results are in good agreement across all model-data pairs.

Exponentially decaying correlation models are a dominant technique among atmospheric inverse studies to represent temporal and spatial flux autocorrelations (Rödenbeck et al., 2009, Broquet et al., 2011, Broquet et al., 2013). However, regarding the temporal error structure we need to note the weakness of this model to capture the slightly negative values at 2-10 months lags and, more

1 importantly, the increase in correlations for lag times larger than about 10 months. Error 2 correlations were parameterized differently by Chevalier et al., (2012) where the prior error was investigated without implementing it to atmospheric inversions. Polynomial and hyperbolic 3 4 equations were used to fit temporal and spatial correlations respectively. Nevertheless, we use here 5 e-folding lengths not only for their simplicity in describing the temporal correlation structure with a single number, but also because this error model ensures a positive definite covariance matrix (as 6 7 required for a covariance). This is crucial for atmospheric inversions as otherwise negative, 8 spatially and temporally integrated uncertainties may be introduced. In addition it can keep the 9 computational costs low; this is because the hyperbolic equation has significant contributions from 10 larger distances: for the case of the VPRM1 model, at 200 km distance the correlation according to 11 Chevallier et al., hyperbolic equation is 0.16, compared to 0.004 for the exponential model. As a 12 consequence, more none-zero elements are introduced to the covariance matrix, which increases 13 computational costs in the inversion systems. Using the same hyberbolic equation for the spatial correlation, d-values of 73, 39, 12 and 20 km were found with a RMSE of 0.11, 0.07, 0.05, 0.07 for 14 15 VPRM10, VPRM1, ORCHIDEE and 5PM respectively. A similar RMSE was found when using the 16 exponential (0.14, 0.09, 0.05 and 0.07), indicating similar performance of both approaches with 17 respect to fitting the spatial correlation.

Autocorrelation times were found to be in line with findings of Chevallier et al., (2012). The model-18 19 data residuals were found to have an e-folding time of 32 and 26 days for VPRM and ORCHIDEE 20 respectively, and 70 days for 5PM. This significant difference appears to have a strong dependence on the set of sites used in the analysis. Excluding nine sites with large residual bias, the 21 22 autocorrelation time from the 5PM-data residuals drastically decreased and became coherent with 23 the times of the other biosphere models. The all-models and all-sites autocorrelation time was found 24 to be 39 days, which reduces to 30 days (28-31 days within 95% confidence interval), when 25 excluding the sites with large residual bias, coherent with the single model times. From the model-26 model residual correlation analysis, the correlation time appear to be consistent with the above-27 mentioned results, and lies between 28 and 46 days for most of the ensemble members. However 28 model-model pairs consisting of the VPRM and 5PM models produced larger times up to 131 days; 29 omitting sites with large residual biases this is reduced to 100 days (99-105 days within 95% confidence interval). This finding could be attributed to the fact that despite the conceptual 30 31 difference between those models, they do have some common properties. Both models were optimized against eddy covariance data although for different years (2005 and 2007 respectively), 32 33 while no eddy covariance data were used for the optimization of ORCHIDEE. In addition, VPRM 34 and 5PM both use data acquired from MODIS, although they estimate photosynthetic fluxes by 35 using different indices of reflectance data. Summarizing the temporal correlation structure, it appears reasonable to a) use same error correlation in atmospheric inversions regardless which
 biospheric model is used as prior, b) use an autocorrelation length of around 30 days.

Only weak spatial correlations for model-data residuals were found, comparable to those identified 3 4 by Chevallier et al. (2012) limited to short lengths up to 40 km without any significant difference between the biospheric models (31 - 40 km). Hilton et al. (2012) estimated spatial correlation 5 6 lengths of around 400km. However we note that significant differences exist between this study and 7 Hilton et al. (2012) regarding the methods that were used and the landscape heterogeneity of the 8 domain of interest. With respect to the first aspect the time resolution is much coarser (seasonal 9 averaged flux residuals) compared to the daily averaged residuals used here. Furthermore spatial 10 bins of 300 km were used for the autocorrelation analysis, which is far larger than the approximate 11 bin width of 100 km that were used in our study. Regarding the second aspect North America has a 12 more homogenous landscape compared to the European domain. The scales for each ecosystem 13 type (e.g. forests, agricultural land etc.) are drastically larger than those in Europe as can be seen 14 from MODIS retrievals (Friedl et al., 2002).

15 Although the estimated spatial scales are shorter than the spatial resolution that we are solving for 16 (100 km bins), the autocorrelation analysis of aircraft measurements made during CERES supports 17 the short scale correlations. These measurements have the advantage of providing continuous 18 spatial flux transects along specific tracks that were sampled routinely (in this case over period of 19 36 days at various times of the day), thus resolving flux spatial variability also at small scales, 20 where pairs of eddy covariance sites may not be sufficiently close. On the other hand, aircraft 21 surveys are necessarily sporadic in time. Of note is that the eddy covariance observation error has 22 no significant impact on the error structure, as the addition of an observation error to the analysis of 23 model-model differences had only minor influence on the error structure. We note that the current 24 analysis focuses to daily time scale and therefore the error statistics with respect to the estimated 25 spatial and temporal e-folding correlation lengths are valid for such scales.

26 Model-data residual e-folding correlation lengths show a clear difference, between the cases where 27 pairs only with different (D) or identical (I) PFT were considered, with the latter resulting in longer 28 correlation lengths, but only identified for the VPRM model at both resolutions. The "D" case has 29 slightly shorter lengths for all models than the standard case (S). One could argue that as VPRM 30 uses PFT specific parameters that were optimized against 2005 observations, the resulting PFT 31 specific bias could lead to longer spatial correlations. However ORCHIDEE and 5PM also show 32 comparable biases (Fig. 3), but long correlation scales were not found. Moreover we repeated the 33 spatial analysis after subtracting the PFT specific bias from the fluxes, and the resulting correlation 34 lengths showed no significant change. The impact of data gaps was also investigated by setting a

1 threshold value of overlapping observations between site pairs. Setting this to 150 days results in an 2 increase for the "S" case up to 60 km, but only for the VPRM model. For the "D" and "I" cases when setting the same threshold value  $(D^* \text{ and } I^*)$  we only found an insignificant increase, 3 indicating that data gaps are hardly affecting the "D" and "I" cases. These findings suggest that 4 5 high-resolution diagnostic models might be able to highlight the increase of the spatial correlation length between identical PFTs vs. different PFTs. Note that the Chevallier et al., (2012) study 6 7 concluded that assigning vegetation type specific spatial correlations is not justified, based on 8 comparisons of eddy covariance observations with ORCHIDEE simulated fluxes. The current study 9 could not further investigate this dependence, as the number of pairs within a distance bin is not 10 large enough for statistical analyses, when using only sites within the same PFT. With respect to the 11 seasonal analysis, spatial correlations are at the same range among all models and seasons. 12 Although in some cases (VPRM10 and VPRM1 spring) the scales are larger, they suffer from large 13 uncertainties. Hence, implementing distinct and seasonally dependent spatial correlation lengths in 14 inversion systems cannot be justified.

15 The analysis of model-model differences did not reproduce the same spatial scales as those from the 16 model-data differences, but instead spatial e-folding correlation lengths were found to be 17 dramatically larger. Adding a random measurement error to the modeled fluxes used as reference slightly reduced the spatial correlation lengths to values ranging from 278 to 1058 km. Even when 18 19 largely inflating the measurement error, the resulting spatial correlation lengths (Fig. 10) still do not approach those derived from model-data residuals. Only when the measurement error is scaled up 20 by a factor of 8 or larger (which is quite unrealistic as this corresponds to a mean error of 1.46 µmol 21  $m^{-2}$  s<sup>-1</sup> or larger, which is comparable to the model-data mismatch where a standard deviation of 22 around 2.5 µmol m<sup>-2</sup> s<sup>-1</sup> was found), the e-folding correlation lengths are consistent with those based 23 24 on model-data differences. Whilst the EC observations are sensitive to a footprint area of about 1 km<sup>2</sup>, the model resolution is too coarse to capture variations at such a small scale. This local 25 26 uncorrelated error has not been taken into account by the analysis of model-data residuals as the 27 error model could not be fitted with a nugget term included, favoring therefore smaller correlation 28 scales. The analysis of differences between two coarser models does not involve such a small scale 29 component, thus resulting in larger correlation scales. This would suggest that for inversion studies 30 targeting scales much larger than the eddy covariance footprint scale, the statistical properties of the 31 prior error should be derived from the model-model comparisons.

The large e-folding correlation lengths yielded from this model-model residual analysis suggest that the models are more similar to each other than to the observed terrestrial fluxes, at least on spatial scales up to a few hundred kilometers regardless of their conceptual differences. This might be 1 expected to some extent due to elements that the models share. Respiration and photosynthetic 2 fluxes are strongly driven by temperature and downward radiation, respectively, and those 3 meteorological fields have significant commonalities between the different models. VPRM and 4 5PM both use temperature and radiation from ECMWF analysis and short-term forecasts. Also the 5 WFDEI temperature and radiation fields used in ORCHIDEE are basically from the ERA-Interim 6 reanalysis, which also involves the integrated forecasting system (IFS) used at ECMWF (Dee et al., 7 2011). Regarding the vegetation classification all models are site specific and therefore are using the 8 same PFT for each corresponding grid-cell. Photosynthetic fluxes are derived with the use of 9 MODIS indices in VPRM (EVI and LSWI) and in 5PM (LAI and albedo).

Using full flux fields from the model ensemble (rather than fluxes at specific locations with observation sites only) to assess spatial correlations in model-model differences is not expected to give significantly different results, as the sites are representative for quite a range of geographic locations and vegetation types within the domain investigated here.

The current study intended to provide insight on the error structure that can be used for atmospheric inversions. Typically, inversion systems have a pixel size ranging from 10 to 100 km for regional and continental inversions, and as large as several degrees (hundreds of km) for global inversions. If a higher resolution system assumes such small-scale correlations (as those found in the current analysis), in the covariance matrix, of note is that this leads to very small prior uncertainties when aggregating over large areas and over longer time periods. To aggregate the uncertainty to large temporal and spatial scales, we used the following equation (after Rodgers, 2000):

$$21 \qquad Ua = u \times Q_c \times u^T \tag{7}$$

Where " $\times$ " denotes matrix multiplication,  $Q_c$  is the prior error covariance matrix and u a scalar 22 23 operator that aggregates the full covariance to the target quantity (e.g. domain-wide and full year). 24 For example, with a 30 km spatial and a 40 day temporal correlation scale, annually and domain-25 wide (Fig. 1) aggregated uncertainties are around 0.06 GtC. This is about a factor ten smaller than 26 uncertainties typically used e.g. in the Jena inversion system (Rödenbeck et al., 2005). This value is 27 also 8 times smaller when comparing it to the variance of the signal between 11 global inversions 28 reported in Peylin et al., (2013) which was found to be 0.45 GtC/y, proving that the aggregated 29 uncertainties are unrealistically small. In addition, the aggregated uncertainties using the VPRM10-30 ORCHIDEE error structure (32 days and 320 km temporal and spatial correlation scales) are found 31 to be 0.46 GtC/y which is also much smaller than the difference between VPRM10 (NEE= - 1.45 32 GtC/y) and ORCHIDEE (NEE= - 0.2 GtC/y), when aggregated over the domain shown in Fig. 1. Although this analysis does capture the dominating spatiotemporal correlation scale in the error 33 34 structure, it fails in terms of the error budget, suggesting that also other parts of the error structure are important as well. Therefore additional degrees of freedom (e.g. for a large-scale bias) need to
 be introduced in the inversion systems to fully describe the error structure.

3

Whilst temporal scales found from this study have already been used in inversion studies, this is not the case to our best knowledge for the short spatial scales. The impact of the prior error structure derived from this analysis, on posterior flux estimates and uncertainties will be assessed in a subsequent paper. For that purpose, findings from this study are currently implemented in three different regional inversion systems aiming to focus on network design for the ICOS atmospheric network.

10

### 11 Acknowledgements.

12 The research leading to these results has received funding from the European Community's Seventh 13 Framework Program ([FP7/2007-2013]) under grant agreement n°313169 (ICOS-INWIRE) and 14 under grant agreement n°283080 (GEOCARBON). The EC data used in this study were funded by 15 the European Community's sixth and seventh framework program and by national funding agencies. 16 In the following sites are listed, sorted by project/funding agency: "BE-Bra", "BE-Lon", "BE-Vie", "CH-Lae", "CH-Oe1", "CH-Oe2", "CZ-BK1", "DE-Geb", "DE-Gri", "DE-Hai", "DE-Kli", "DE-17 18 Tha", "DK-Lva", "ES-ES2", "ES-LMa", "FI-Hyy", "FR-Fon", "FR-Hes", "FR-LBr", "FR-Lq1", "FR-Lq2", "FR-Pue", "IT-SRo", "NL-Dij", "NL-Loo", "PT-Esp", "PT-Mi2", "SE-Kno", "SE-Nor", 19 "SE-Sk1", "SK-Tat", "UK-AMo", "UK-EBu" funded by CarboEuropeIP (grand agreement nº 20 21 GOCE-CT-2003-505572); "UK-AMo", "UK-EBu" also co-funded by EU FP7 ECLAIRE project and NERC-CEH; "IT-BCi", "IT-Cas", "IT-Lav", "IT-LMa" funded by CarboItaly (IT-FISR), "IT-22 23 Amp", "IT-Col", "IT-Cpz", "IT-MBo", "IT-Ren", "IT-Ro2" co-funded by CarboEuropeIP and by 24 CarboItaly, "CH-Cha", "CH-Dav", "CH-Fru" co-funded by CarboExtreme (grant agreement n° 25 226701) and GHG-Europe (grant agreement n° 244122), "ES-Agu" funded by GHG-Europe, "FR-26 Mau" co-funded by CNRM/GAME (METEO-FRANCE, CNRS), CNES and ONERA. We also 27 acknowledge funding agencies for the sites "FR-Aur", "FR-Avi", "HU-Mat".

The authors would like to thank Anna Michalak and the anonymous reviewer whose insightfulcomments helped the development of the manuscript.

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- 1 Table 1: Eddy covariance sites measuring CO<sub>2</sub> fluxes that were used in the analysis. The land cover
- 2 classification which is used, is coded as follows; CRO, DCF, EVG, MF, GRA, OSH, SAV for crops,
- 3 deciduous forest, evergreen forest, mixed forest, grass, shrub and savanna respectively.
- 4

Site code	Site name	Land cover classification	Latitude	Longitude	Citation
BE-Bra	Brasschaat	MF	51.31	4.52	Gielen et al., 2013
BE-Lon	Lonzee	CRO	50.55	4.74	Moureaux et al., 2006
BE-Vie	Vielsalm	MF	50.31	6.00	Aubinet et al., 2001
CH-Cha	Chamau	GRA	47.21	8.41	Zeeman et al., 2010
CH-Dav	Davos	ENF	46.82	9.86	Zweifel et al., 2010
CH-Fru	Frebel	GRA	47.12	8.54	Zeeman et al., 2010
CH-Lae	Laegern	MF	47.48	8.37	Etzold et al., 2010
	Oensingen				Ammann et al., 2009
CH-Oe1	grassland	GRA	47.29	7.73	
CH-Oe2	Oensingen crop	CRO	47.29	7.73	Dietiker et al., 2010
CZ-BK1	Bily Kriz forest	ENF	49.50	18.54	Taufarova et al., 2014
DE-Geb	Gebesee	CRO	51.10	10.91	Kutsch et al., 2010
DE-Gri	Grillenburg	GRA	50.95	13.51	Prescher et al., 2010
DE-Hai	Hainich	DBF	50.79	10.45	Knohl et al., 2003
DE-Kli	Klingenberg	CRO	50.89	13.52	Prescher et al., 2010
DE-Tha	Tharandt	ENF	50.96	13.57	Prescher et al., 2010
DK-Lva	Rimi	GRA	55.68	12.08	Soussana et al., 2007
ES-Agu	Aguamarga	OSH	36.94	-2.03	Rey et al., 2012

ES-ES2	El Saler-Sueca (Valencia)	CRO	39.28	-0.32	-
					Casala et al. 2011
ES-LMa	Las Majadas del Tietar (Caceres)	SAV	39.94	-5.77	Casals et al., 2011
FI-Hyy	Hyytiälä	ENF	61.85	24.30	Suni et al., 2003
FR-Aur	AuradeŽ	CRO	43.55	1.11	Tallec et al., 2013
FR-Avi	Avignon	CRO	43.92	4.88	Garrigues et al., 2014
FR-Fon	Fontainebleau	DBF	48.48	2.78	Delpierre et al., 2009
FR-Hes	Hesse	DBF	48.67	7.07	Longdoz et al., 2008
FR-LBr	Le Bray	ENF	44.72	-0.77	Jarosz el al., 2008
	Laqueuille				Klumpp et al., 2011
FR-Lq1	intensive	GRA	45.64	2.74	
	Laqueuille			2.74	Klumpp et al., 2011
FR-Lq2	extensive	GRA	45.64	2.74	
FR-Mau	Mauzac	GRA	43.39	1.29	Albergel et al., 2010
FR-Pue	Puechabon	EBF	43.74	3.60	Allard et al., 2008
HU-Mat	Matra	CRO	47.85	19.73	Nagy et al., 2007
IT-Amp	Amplero	GRA	41.90	13.61	Barcza et al., 2007
IT-BCi	Borgo Cioffi	CRO	40.52	14.96	Kutsch et al., 2010
IT-Cas	Castellaro	CRO	45.07	8.72	Meijide et al., 2011
IT-Col	Collelongo	DBF	41.85	13.59	Guidolotti et al., 2013
IT-Cpz	Castelporziano	EBF	41.71	12.38	Garbulsky et al., 2008
IT-Lav	Lavarone	ENF	45.96	11.28	Marcolla et al., 2003

IT-Lec	Lecceto	EBF	43.30	11.27	Chiesi et al., 2011
IT-LMa	Malga Arpaco	GRA	46.11	11.70	Soussana et al., 2007
IT-MBo	Monte Bondone	GRA	46.01	11.05	Marcolla et al., 2011
IT-Ren	Renon	ENF	46.59	11.43	Marcolla et al., 2005
T-Ro2	Roccarespampani 2	DBF	42.39	11.92	Wei et al., 2014
T-SRo	San Rossore	ENF	43.73	10.28	Matteucci et al., 2014
NL-Dij	Dijkgraaf	CRO	51.99	5.65	Jans et al., 2010
NL-Loo	Loobos	ENF	52.17	5.74	Elbers et al., 2011
NL-Lut	Lutjewad	CRO	53.40	6.36	Moors et al., 2010
PT-Esp	Espirra	EBF	38.64	-8.60	Gabriel et al., 2013
PT-Mi2	Mitra IV (Tojal)	GRA	38.48	-8.02	Jongen et al., 2011
SE-Kno	KnottŒsen	ENF	61.00	16.22	-
SE-Nor	Norunda	ENF	60.09	17.48	-
SE-Sk1	Skyttorp 1	ENF	60.13	17.92	-
SK-Tat	Tatra	ENF	49.12	20.16	-
UK-AMo	Auchencorth Moss	GRA	55.79	-3.24	Helfter et al., 2015
UK-EBu	Easter Bush	GRA	55.87	-3.21	Skiba et al., 2013

Table 2: Annual temporal autocorrelation times in days, from model-data and model-model residuals. The number within the brackets shows the correlation times when excluding sites with large model-data bias from the analysis.

Reference	VPRM10 [days]	VPRM1 [days]	ORCHIDEE [days]	5PM [days]
OBSERVATION	32 (27)	33 (29)	26 (24)	70 (34)
VPRM50	-	-	28 (28)	52 (46)
VPRM10	-	-	-	131 (100)
ORCHIDEE	-	-	-	38 (32)
5PM	-	-	-	-

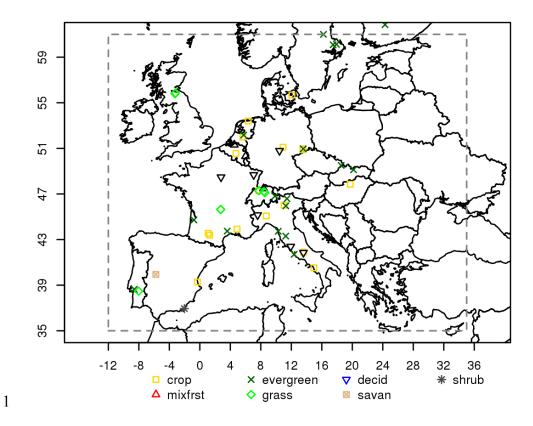
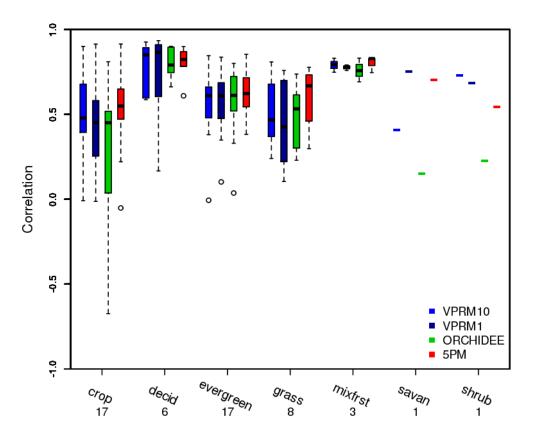


Figure 1. Eddy covariance sites used in the study. The dashed line delimits the exact domain used to calculate the aggregated fluxes.



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Figure 2. Box and whisker plot for site-specific correlation coefficients between modeled and observed daily fluxes as a function of the vegetation type. The numbers beneath the x-axis indicate the number of sites involved. The bottom and the top of the box denote the first and the third quartiles. The band inside the box indicates the central 50% and the line within is the median. Upper and lower line edges denote the maximum and the minimum values excluding outliers. Outliers are shown as circles.

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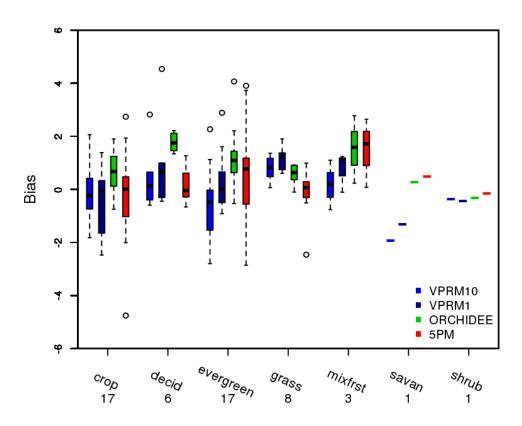


Figure 3. Box and whisker plot for the annual site-specific biases of the models differentiated by vegetation type. Units at y-axis are in  $\mu$ mol m<sup>-2</sup> s<sup>-1</sup> (for conversion to gC m<sup>-2</sup> yr<sup>-1</sup> reported values in y axis should be multiplied by 378,7694).

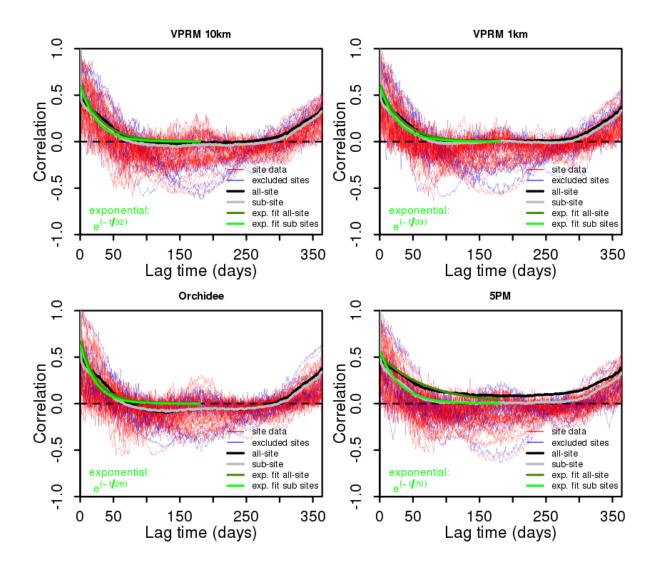


Figure 4. Temporal lagged autocorrelation from model-data daily averaged NEE residuals for all models. Thin red lines correspond to different sites, while the blue thin lines reveal the sites with a bias larger than  $\pm -2.5 \mu mol m^{-2} s^{-1}$ . The thick black line shows the all-site autocorrelation, and the thick grey line indicates the all-site autocorrelation but for a sub-set that excludes sites with large model-data bias ("sub-site"). The dark green line is the all-site exponential fit, and the light green line shows the all-site autocorrelation excluding the sites with large bias. The exponential fits use lag times up to 180 days.

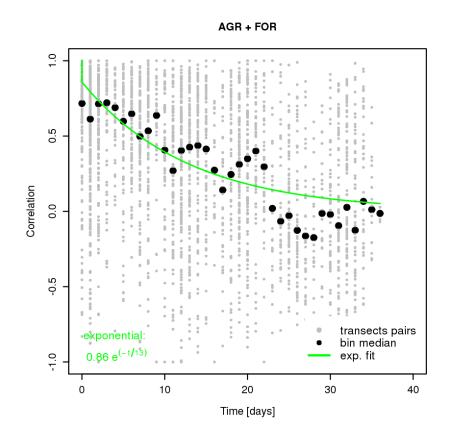


Figure 5. Temporal autocorrelation for VPRM10 – aircraft NEE residuals. Black dots represent
individual flux transects pairs sampled at different times as function of time separation. Black
circles represent daily scale binned data.

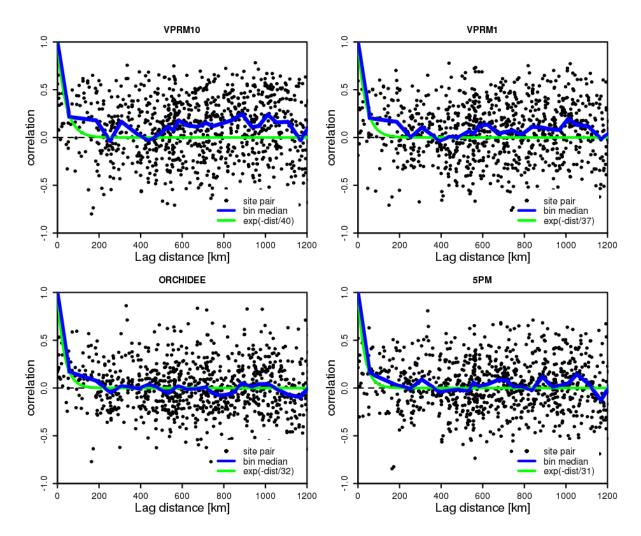
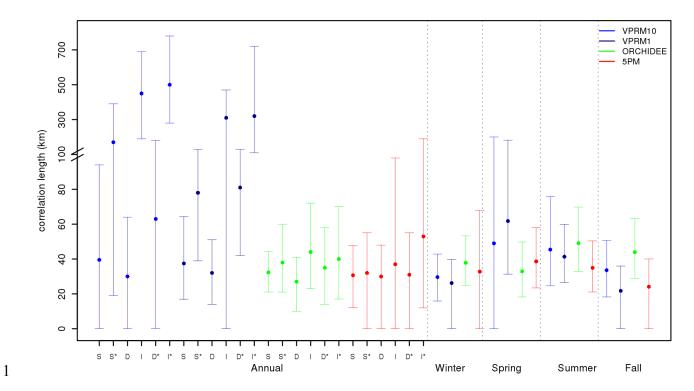


Figure 6. Distance correlogram for the daily net ecosystem exchange (NEE) residuals using all sites. Black dots represent the different site pairs; the blue line represents the median value of the points per 100-km bin and the green an exponential fit. Results are shown for residuals of VPRM at a resolution of 10 km (top left) and 1 km (top right), ORCHIDEE (bottom left), 5PM (bottom right).



2 Figure 7. Annual and seasonal e-folding correlation length of the daily averaged model-data NEE 3 residuals for VPRM at 10 and 1 km resolution, ORCHIDEE and 5PM. "S" refers to the standard 4 case where all pairs were used, "D" refers to the case where only pairs with different vegetation types were used, "I" denotes the case in which only pairs with identical vegetation type were 5 considered, and "\*" denotes that in addition 150 days of common non-missing data are required for 6 7 each pair of sites. The dot represents the best-fit value when fitting the exponential model. The 8 upper and the lower edge of the error bars show the 2.5 and 97.5 percentiles of the length value. 9 Note the scale change in the y-axis at 100 km.

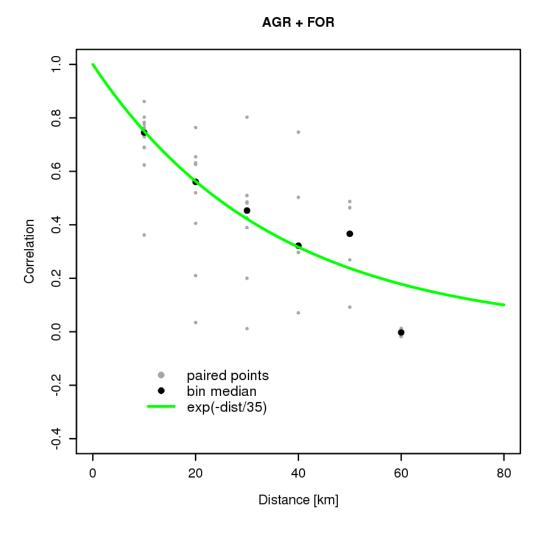
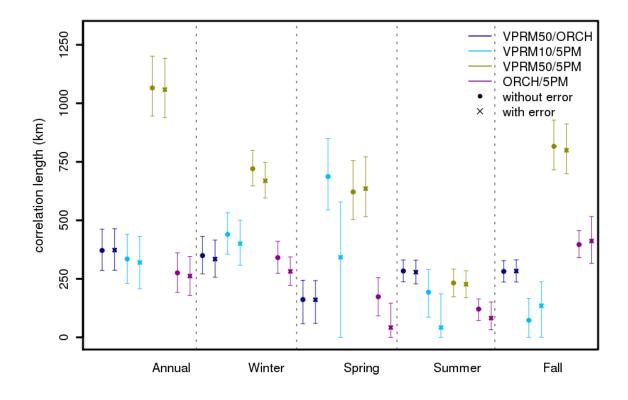


Figure 8. Distance correlogram between VPRM10 and aircraft NEE measurements. Black dots represents the different aircraft grid points pairs; black circles represent 10 km scale binned data.



2 Figure 9. Annual and seasonal e-folding correlation length for an ensemble of daily averaged NEE 3 differences between two models without (filled circle) and with random measurement errors added 4 to the modeled fluxes used as reference (crosses). The symbols represents the best fit value when 5 fitting the exponential model, and the upper and lower edge of the error bars show the 2.5 and 97.5 6 percentiles of the correlation length. The first acronym at the legend represents the model used as 7 reference and the second the model which was compared with. Note that for the VPRM10/VPRM1 8 case during spring (with and without random error), the 97.5 percentile of the length value exceeds 9 the y-axis and has a value of 1073, 1626 km respectively.

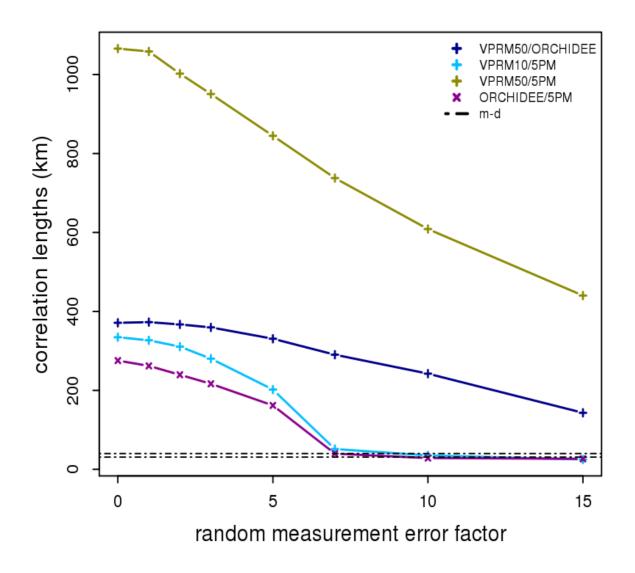


Figure 10. Annual e-folding correlation lengths as a function of the factor used for scaling the random measurement error, for all model-model combinations. The black dot-dash lines reveal the range of the spatial correlation lengths generated from the model-data comparisons.