

Analytical solution of nitracline with the evolution of subsurface chlorophyll maximum in stratified water columns

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Abstract:

In a stratified water column, the nitracline is a layer where the nitrate concentration increases below the nutrient-depleted upper layer, exhibiting a strong vertical gradient in the euphotic zone. The subsurface chlorophyll maximum layer (SCML) forms near the bottom of euphotic zone, acting as a trap to diminish the upward nutrient supply. Depth and steepness of the nitracline are important measurable parameters related to the vertical transport of nitrate into the euphotic zone. The correlation between the SCML and the nitracline has been widely reported in the literature, but the analytic solution for the relationship between them is not well established. By incorporating a piecewise function for the approximate Gaussian vertical profile of chlorophyll, we derive analytical solutions of a specified nutrient-phytoplankton model. The model is well suited to explain basic dependencies between a nitracline and a SCML. The

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- 30 analytical solution shows that the nitracline depth is deeper than the depth of SCML, shoaling with an increase in light attenuation coefficient and with a decrease in surface light intensity. The inverse proportional relationship between the light level at the nitracline depth and the maximum rate of new primary production is derived. Analytic solutions also show that a thinner SCML corresponds to a steeper nitracline.
- 35 The nitracline steepness is positively related to light attenuation coefficient, but independent of surface light intensity. The derived equations of the nitracline in relation to the SCML provide further insight into the important role of the nitracline in marine pelagic ecosystems.

1 Introduction

40 Nitrogen availability, especially the nitrate upward supply to the euphotic zone where light intensity is sufficient to support net photosynthesis, limits the primary productivity in a stratified water column (Falkowski et al., 1998). Specifically, the nitrate supply from below and the light attenuated from above with the depth collaboratively affect the growth of phytoplankton and lead to the subsurface
45 chlorophyll maximum (SCM) (Riley et al., 1949; Steele and Yentsch, 1960; Herbland and Voituriez, 1979; Cullen, 1982). The SCM layer (SCML) has attracted much attention since Riley (1949) because the layer contributes significantly to new primary production (NPP) in stratified waters (Probyn et al., 1995; Ross and Sharples, 2007; Fernand et al., 2013). The synergistic physical and biological interaction leads to a
50 strong vertical nitrate gradient, conventionally referred to as the nitracline (Eppley et al., 1978; Herbland and Voituriez, 1979; Cullen and Eppley, 1981). Depth and steepness of the nitracline are important measurable parameters in regulating the supply of nitrate to the euphotic zone, and hence affecting NPP (Lewis et al., 1986; Bahamón et al., 2003; Aksnes et al., 2007; Cermeno et al., 2008; Omand and
55 Mahadevan, 2015).

The nitracline depth physically depends on the degree of water-column stratification and the magnitude of momentum transfer associated with wind stress (Denman and Gargett, 1983; Laanemets et al., 2004). It also depends on momentum transfer from below (Lipschultz et al., 2002) and in some cases, vertical advection
60 such as upwelling (Laanemets et al., 2004). However, in a relatively stable environment, the SCML may restrict the diffusive flux of nitrates to the euphotic zone and continually erode the nitracline supposing that sufficient light is available (Probyn et al., 1995). The SCML thereby acts as an effective nutrient trap, regulating the nitracline depth (Banse, 1982; Beckmann and Hense, 2007; Klausmeier and Litchman,
65 2001; Probyn et al., 1995). However, variation of nitracline steepness, which is critical to determine the nitrate supply, was poorly understood due to lack of high vertical resolution data, e.g., both bottle data and Argo data tend to have low vertical

resolution sampling. Some studies showed that nitrogen flux is dependent more on the nitracline steepness than on the density gradients regulating turbulent diffusion (Bahamón and Cruzado, 2003; Bahamón et al., 2003; Lavigne et al., 2015). Thus, these measurable features of nitracline and their correlation with SCML may provide insightful information for mechanisms of the productivity in pelagic ecosystem, and the analytic solutions for these parameters may fill the knowledge gap.

Although a close relationship between the nitracline and SCML is always observed, the quantitative nature of nitracline in relation to the SCML formation has not been studied. The system of phytoplankton and the limiting nutrient on the vertical axis was often utilized to study the depth, intensity, and persistence of the SCML. Major theoretical results include photoacclimation (increase of chlorophyll per cell) (Steele, 1964; Fennel and Boss, 2003), bistability (Yoshiyama and Nakajima, 2002; Ryabov et al., 2010), oscillating SCM (Huisman et al., 2006), hysteresis conditions (Kiefer and Kremer, 1981; Navarro and Ruiz, 2013), and the ESS (evolutionary stable strategy) depth obtained by game-theory approach (Klausmeier and Litchman, 2001; Mellard et al., 2011). Recent mathematical studies solved the persistence and uniqueness of the steady state solution (Du and Hsu, 2010; Hsu and Yuan, 2010; Du and Mei, 2011), and gave rigorous proofs for the above-mentioned ESS depth and the game-theory approach (Du and Hsu, 2008a, b). Additionally, several modeling studies have been conducted to quantitatively assess the importance of different physical-biological processes leading to SCML (Jamart et al., 1977; Jamart et al., 1979; Varela et al., 1994; Klausmeier and Litchman, 2001; Hodges and Rudnick, 2004; Beckmann and Hense, 2007).

Among the studies using the nutrient-phytoplankton model, Klausmeier and Litchman (2001) first analytically derived the vertical nutrient distribution with the development of the SCML. In that model, the concentration of the limiting nutrient was found to be low and constant above the SCML and linearly increasing with depth below this layer in poorly mixed water column. Building on that model, Mellard et al. (2011) added stratification and surface nutrient input, which can make phytoplankton

grow in both the surface mixed layer and deep layer (SCML) simultaneously. Fennel and Boss (2003) derived that the sum of nutrients and phytoplankton at steady state will increase monotonically below the surface mixed layer until it equals the fixed
100 nutrient concentration. By incorporating a generalized Gaussian function for vertical chlorophyll profile into the nutrient-phytoplankton dynamic equation, Gong et al. (2015) obtained that the steady-state nitrate concentration increased from the upper community compensation depth to the SCML depth. None of the studies, however, focused on the quantitative nature of nitracline in relation to the SCML in the
105 stratified waters.

In this paper, we modified the nutrient-phytoplankton model by Gong et al. (2015) to study the roles of SCM in reshaping the nitracline. Two additional terms, atmospheric input, which promotes the growth of phytoplankton in the surface mixed layer, and the phytoplankton self-shading, which regulates the light penetration, were
110 introduced into the previous model. Accordingly, a piecewise function comprising a constant value within the surface mixed layer and a Gaussian function below this layer was used as a fit to the steady state vertical chlorophyll profiles simulated by the nutrient-phytoplankton model. By incorporating the piecewise function into the nutrient-phytoplankton model, we derived the analytic solutions for the properties of
115 the nitracline and the SCML in steady state, and the relationship between them was examined in response to light availability, surface nutrient input, and vertical diffusivity.

2 Definitions and Models

2.1 Models

2.1.1 Dynamic equations

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We consider the following equations for phytoplankton and nutrient dynamics in stratified waters (Eqs. 1-2), where light and nitrogen are two limiting factors for phytoplankton growth (Fig. 1). The change in phytoplankton at depth z is the balance of the growth and death, and the passive moving (sinking and mixing) (Eq. 1). An

125 eddy diffusion coefficient K_v redistributes phytoplankton in the water column. Depth z is increasing toward the seabed.

$$\begin{cases} \frac{\partial P}{\partial t} = \mu_m \min(f(I), g(N))P - \varepsilon P - w \frac{\partial P}{\partial z} + \frac{\partial}{\partial z} \left(K_v(z) \frac{\partial P}{\partial z} \right) \\ \frac{\partial N}{\partial t} = -\gamma \mu_m \min(f(I), g(N))P + \gamma \alpha \varepsilon P + N_{in}(z) + \frac{\partial}{\partial z} \left(K_v(z) \frac{\partial N}{\partial z} \right) \end{cases}$$

where P denotes the chlorophyll concentration (mg m^{-3}). We assume the chlorophyll distribution to represent the distribution of phytoplankton biomass (that means that the photoacclimation of phytoplankton is ignored, and the SCM refers to the subsurface biomass maximum, SBM). This is a significant simplification. In fact, phytoplankton increases inter-cellular pigment concentration when light level decreases (Cullen, 1982; Fennel and Boss, 2003; Cullen, 2015). Usually, the depths of SCML and SBML are separate, and the latter is shallower than the former.

135 Nitrogen N (in unit: mmol N m^{-3}) taken up by phytoplankton includes three sources, i.e., recycling from dead phytoplankton, atmospheric input to the surface mixed layer, and supply by mixing from deep water (Eq. 2). γ is the nitrogen content of the phytoplankton (mmol N per mg Chl). Following Mellard et al. (2011), we consider the nitrogen input from atmosphere at the rate of $N_{in}(z)$, setting as a delta function at $z=0$ with the total nutrient input in the surface mixed layer N_{inML} , $N_{inML} = \int_0^{z_s} N_{in}(z) dz$, where z_s is the depth of surface mixed layer. Note that nitrogen input through the activity of nitrogen fixers is excluded. However, Trichodesmium, if they are at the surface, will be modeled similarly to the atmospheric input term.

μ_m is the maximum growth rate of phytoplankton, ε is the loss rate of phytoplankton (including respiration, mortality, zooplankton grazing), and α is the recycling efficiency of dead phytoplankton ($0 < \alpha < 1$). The specific rate of loss processes (ε) is assumed to be vertically homogeneous due to lack of data (similar to Sverdrup, 1953). The treatment of grazing loss, is, in the least, an oversimplification, though many numerical models used a similar one (e.g., Klausmeier and Litchman, 2001; Fennel and Boss, 2003; Huisman et al., 2006). The growth-limited function for light I and

nitrogen N is given by $\mu_m \min(f(I), g(N))$. The Michaelis-Menten form for the light-limiting function $f(I)$ and nitrogen-limiting function $g(N)$, $f(I)=I/(K_I+I)$ and $g(N)=N/(K_N+N)$ is used, where K_I and K_N denote the half-saturation constants for light and nitrogen, respectively. The net growth rate, $\mu_m \min(f(I), g(N)) - \varepsilon$, is positive
 155 only if both light-limiting term $\mu_m f(I)$ and nitrogen-limiting term $\mu_m g(N)$ are larger than the loss rate ε .

Light intensity I decreases exponentially with depth according to the Lambert-Beer law,

$$I(z) = I_0 \exp\left(-K_w z - K_c \int_0^z P dz\right) \quad (3)$$

160 where I_0 is the surface light intensity, K_w and K_c are light attenuation coefficients of water and phytoplankton, respectively. For the sake of simplicity, we assume that both K_w and K_c are constant with depth.

The sinking velocity of phytoplankton w is non-negative in the chosen coordinate system. We assumed it to be constant with depth, neglecting the influencing of density
 165 gradients (pycnoclines), which may cause vertical variations in sinking.

To describe the water-column stratification, we assume that the vertical eddy diffusivity K_v depends on depth,

$$K_v(z) = \begin{cases} K_{v1} & 0 \leq z \leq z_s \\ K_{v2} & z_s < z < z_b \end{cases} \quad (4)$$

where z_b is set to the bottom boundary of this model and is assumed to be sufficiently
 170 deep where the chlorophyll concentration approaches to zero. We assume that surface diffusivity (K_{v1}) and subsurface diffusivity (K_{v2}) (Lande and Wood, 1987; Hodges and Rudnick, 2004) are constant and K_{v1} is large enough to homogenize the chlorophyll and nitrogen concentration in the surface mixed layer. A gradual transition from the surface mixed layer to the deep one (in the vicinity of z_s) can be written in terms of a
 175 generalized Fermi function (Ryabov et al., 2010), $K_v(z) = K_{v2} + \frac{K_{v1} - K_{v2}}{1 + e^{z - z_s/l}}$, where parameter l characterizes the width of the transition layer. In our numerical study, we

assumed this transition layer is 2 m. For simplicity, parameter l is set to infinitely thin in analytic solutions. A comprehensive list of symbols is given in Table 1.

The zero-flux boundary condition for the phytoplankton at the surface is used. At the bottom boundary of the model domain ($z=z_b$) the Dirichlet or fixed concentration boundary condition is used, i.e., $P \rightarrow 0$ for $z \rightarrow z_b$. Fennel and Boss (2003) used an infinite depth as z_b ($z_b \rightarrow \infty$). For the nitrogen distribution we set $N=N_{inML}$ at the surface and diffusing into the water column a prescribed nitrate gradient, n , at the bottom. That is,

$$\left\{ \begin{array}{l} \left(wP - K_{v1} \frac{\partial P}{\partial z} \right) \Big|_{z=0} = 0, \quad P(z_b) = 0. \\ N \Big|_{z=0} = N_{inML}, \quad \frac{\partial N}{\partial z} \Big|_{z=z_b} = n. \end{array} \right. \quad (5)$$

2.1.2 Fitting equation for vertical chlorophyll profile

In many stratified water columns, the vertical distribution of chlorophyll concentration is homogeneous within the surface mixed layer and appears a Gaussian below this layer (Fig. 2a), which is typical in open oceans (Uitz et al., 2006), shelf seas (Sharples et al., 2001), stratified estuary (Lund-Hansen, 2011), and arctic waters (Martin et al., 2012). The non-uniform vertical profile of chlorophyll within an SCML was first modeled by a generalized Gaussian function (Lewis et al., 1983), which has subsequently been widely used with small modifications. For example, Platt et al. (1988) superimposed a constant background on the generalized Gaussian, and fitted it to field data on the vertical distribution of chlorophyll from coastal, upwelling, open oceans and Arctic waters. Afterward, some studies introduced a parameter to represent the slope of the Gaussian curve (Matsumura and Shiomoto, 1993; Mu Oz Anderson et al., 2015). In particular, to account for the observed characteristic that surface values always exceed the bottom ones (Fig. 2a), the generalized Gaussian functional form has been modified with a superimposition of a background linearly or exponentially decreasing with depth (Uitz et al., 2006; Mignot et al., 2011; Ardyna et al., 2013).

For simplicity, to analytically study the role of the SCML on shaping the nitracline,

we therefore propose a piecewise function comprising a constant value in the surface mixed layer and below a general Gaussian function (Eq. 6) to approximate the vertical profile of chlorophyll concentration in Fig. 2a.

$$P = \begin{cases} P_0 & 0 \leq z \leq z_s \\ P_{\max} \exp\left[-\frac{(z - z_m)^2}{2\sigma^2}\right] & z_s < z < z_b \end{cases} \quad (6)$$

where P is chlorophyll concentration as a function of depth z , P_0 is the chlorophyll concentration within the surface mixed layer, and $P_{\max} = h/(\sigma\sqrt{2\pi})$ represents the maximum value of chlorophyll below the surface mixed layer. Considering the influence of the surface mixed layer on the chlorophyll vertical distribution, h is less than the total chlorophyll concentration integrated through the water column. Note that the vertical distribution of chlorophyll is an incomplete general Gaussian function below the surface mixed layer (*see* Fig. 2a). The three Gaussian parameters (P_{\max} , z_m , σ) can characterize the SCM phenomenon. Thus, z_m is the depth of the maximum chlorophyll (the peak of the bell shape), and σ is the standard deviation of Gaussian function, which controls the width of the SCML. The upper and lower boundary of SCML can be defined as $z_m - \sigma$ and $z_m + \sigma$, respectively, which are at the depths where there is the balance between phytoplankton growth and losses and thus reflect the physical-biological ecosystem dynamics associated with SCML (Beckmann and Hense, 2007; Gong et al., 2015). To explore the SCML in stratified waters, we assume the surface mixed layer is shallower than the upper boundary of the SCML, i.e., $z_s < z_m - \sigma$. Examples of the piecewise function that reasonably well fitted to vertical chlorophyll profiles in the northern South China Sea (SCS) can be found in Gong et al. (2014).

The piecewise function approximation (Eq. 6) was evaluated and justified through numerical simulation of the nutrient-phytoplankton system (Eqs. 1-2), which is solved with a semi-implicit time stepping scheme. The vertical resolution is uniform (2 m), extending down to 200 m. We assumed a small uniformly distributed concentration of phytoplankton ($P(z,0)=0.1 \text{ mg m}^{-3}$) and nitrogen ($N(z,0)=0.1 \text{ mmol N m}^{-3}$) as the

230 initial conditions and run the model until in converge to a steady state (The modeling results show that the steady state has no relationship with the initial values of phytoplankton and nitrogen). We use the biologically reasonable parameter values given in Table 1 to represent the system at Station SEATS (South East Asia Time Series) in the northern SCS. Thus, the specific (calibrated) model solution is
235 considered as an example to obtain the analytic solutions of nitracline.

Fig. 3 shows the numerically simulated equilibrium distributions of nitrogen, light, and chlorophyll. In addition, the simulated vertical profile of chlorophyll is fitted well by the piecewise function of chlorophyll using the least square method (Fig. 3). Many numerical solutions of the nutrient-phytoplankton system have reproduced the vertical
240 chlorophyll profile with the SCML (Fennel and Boss, 2003; Huisman et al., 2006; Ryabov et al., 2010). Thus, analogous to the study by Klausmeier and Litchman (2001), we incorporate the piecewise function (Eq. 6) to the nutrient-phytoplankton system (Eqs. 1-2) at steady state to examine the roles of the SCML in reshaping the nitracline. We note that the useful delta function approximation in Klausmeier and
245 Litchman (2001) was verified by both simulation and rigorous mathematics (Du and Hsu, 2008a, b). As presented above, the assumption of the piecewise function approximation is physically practical.

2.2 Definition of the nitracline

The vertical distributions of nitrate often exhibit a strong gradient in depth (the
250 nitracline), but the feature of nitracline (depth, steepness) is variable in euphotic zones due to the combined effect of physical and biological processes.

Many studies define the nitracline depth as the location where the maximum vertical gradient in nitrate concentrations occurs (Eppley et al., 1979; Bahamón et al., 2003; Wong et al., 2007; Beckmann and Hense, 2007; Martin et al., 2010). To
255 measure the defined depth, a high vertical resolution of nitrate concentrations is needed and this is a big technical challenge existing for a long time. Thus, some definitions were also proposed to make the depth measurable. For example, one

definition is the depth where the nitrate concentration reaches a prescribed concentration, e.g., 0.05, 0.1, 1.0, or 12 mmol N m⁻³ (Cullen and Eppley, 1981; Koeve
 260 et al., 1993; Martin and Pondaven, 2003). Some studies choose it to be the first depth
 where nitrogen is detectable (e.g., 0.05 or 0.1 mmol N m⁻³) (Cermeno et al., 2008;
 Hickman et al., 2012) or where the nitrogen concentration exceeds the mixed layer
 value by a prescribed concentration difference (e.g., 0.05 mmol N m⁻³) (Laanemets et
 al., 2004). Significant differences exist between these defined depths, i.e., the depth of
 265 maximal nitrate gradient was found to be deeper by 10 m from the first depth where
 nitrate can be detected (Eppley et al., 1978), while the nitrate gradient at the first
 detectable depth of nitrate is nearly zero (Cermeno et al., 2008).

With the development of nearly continuous nitrate profile measurement using the In
 Situ Ultraviolet Spectrophotometer (ISUS) optical nitrate sensor (Johnson and Coletti,
 270 2002; Johnson et al., 2010), the detection of the maximum nitrate gradient could be
 more accurate than before. In this study, we adopt the location of the maximum nitrate
 gradient ($\max(dN/dz)$) in the euphotic zone as the nitracline depth (z_n), which can be

expressed by $\frac{d^2N}{dz^2}\Big|_{z_n} = 0$ and $\frac{d^3N}{dz^3}\Big|_{z_n} < 0$.

Below the surface mixed layer, the steady-state version of Eq. (2) reduces to
 275 $\gamma\mu_m \min(f(I), g(N))P - \gamma\alpha\varepsilon P = K_{v2} \frac{d^2N}{dz^2}$. Thus, according to our model approach (Eq. 2)

the nitracline depth where $\frac{d^2N}{dz^2} = 0$ represents a balance between the nutrient uptake
 and the recycling of phytoplankton loss, i.e., $\mu_m \min(f(I), g(N)) = \alpha\varepsilon$.

In this study the nitracline steepness is defined as the nitrate gradient at the
 nitracline depth ($\frac{dN}{dz}\Big|_{z_n}$) (Laanemets et al., 2004; Aksnes et al., 2007).

280 2.3 Data sources

The nitrate profiles were obtained from the ISUS measurement at the SEATS
 station during the CHOICE-C 2012 summer cruise. Nine casts were conducted during

Aug. 6-7, 2012. The raw ISUS nitrate data, which employed temperature-compensation, were first calibrated by the AutoAnalyzer 3 (AA3), and then smoothed to remove noise. The sampling frequency was set at 5 Hz and the raw data were thus smoothed with a 25-point moving average in the surface mixed layer, a 5-point moving average in the SCML, and a 15-point moving average below the SCML. The data were then interpolated by a cubic spline function. The corresponding temperature was obtained from Conductivity-Temperature-Depth (CTD) measurements. Overall, nine sets of profiles are available to examine our analytical solutions.

3 Results

3.1 Relations between nitracline and SCML

3.1.1 Nitracline depth and SCML

At steady state, multiplying Eq. (1) by γ then adding Eqs. (1) and (2) leads to:

$$(\alpha - 1)\varepsilon P - w \frac{dP}{dz} + \frac{d}{dz} \left(K_v(z) \frac{dP}{dz} \right) + \frac{1}{\gamma} \frac{d}{dz} \left(K_v(z) \frac{dN}{dz} \right) + \frac{N_m(z)}{\gamma} = 0 \quad (7)$$

By substituting the expression of eddy diffusivity (Eq. 4) and the fitted, depth dependent function of chlorophyll ($P(z)$, Eq. 6) into Eq. (7), we obtain the diffusive term of nitrate below the surface mixed layer, that is,

$$K_{v2} \frac{d^2 N}{dz^2} = \left[-\frac{K_{v2}}{\sigma^2} \left(\frac{z - z_m}{\sigma} \right)^2 - \frac{w}{\sigma} \left(\frac{z - z_m}{\sigma} \right) + \frac{K_{v2}}{\sigma^2} + (1 - \alpha) \varepsilon \right] \gamma P \quad z_s < z < z_b \quad (8)$$

Letting $d^2 N / dz^2 = 0$ in Eq. (8), for $P > 0$ one gets

$$-\frac{K_{v2}}{\sigma^2} \left(\frac{z - z_m}{\sigma} \right)^2 - \frac{w}{\sigma} \left(\frac{z - z_m}{\sigma} \right) + \frac{K_{v2}}{\sigma^2} + (1 - \alpha) \varepsilon = 0 \quad z_s < z < z_b \quad (9)$$

Solving this quadratic equation of depth z , we obtain the depths z_{n1} and z_{n2} ,

$$\begin{cases} z_{n1} = z_m - \frac{w\sigma^2}{2K_{v2}} - \sqrt{\frac{w^2\sigma^4}{4K_{v2}^2} + \frac{(1-\alpha)\varepsilon\sigma^4}{K_{v2}} + \sigma^2} \\ z_{n2} = z_m - \frac{w\sigma^2}{2K_{v2}} + \sqrt{\frac{w^2\sigma^4}{4K_{v2}^2} + \frac{(1-\alpha)\varepsilon\sigma^4}{K_{v2}} + \sigma^2} \end{cases} \quad (10)$$

305 Taking the derivative of Eq. (8) with respect to depth z , we get
 $K_{v2} \frac{d^3N}{dz^3} = \left[-\frac{2K_{v2}}{\sigma^4} (z - z_m) - \frac{w}{\sigma^2} \right] \gamma P - K_{v2} \frac{d^2N}{dz^2} \frac{z - z_m}{\sigma^2}$. Obviously, at depth z_{n1} , $d^3N/dz^3 > 0$,
and at depth z_{n2} , $d^3N/dz^3 < 0$. That is, z_{n2} is the location of maximum nitrate gradients.
We obtain that the nitracline depth refers to the depth z_{n2} , i.e.,

$$z_n = z_{n2} = z_m - \frac{w\sigma^2}{2K_{v2}} + \sqrt{\frac{w^2\sigma^4}{4K_{v2}^2} + \frac{(1-\alpha)\varepsilon\sigma^4}{K_{v2}} + \sigma^2} \quad (11)$$

310 Particularly, Eq. (9) becomes a linear function of depth z when the second order
item coefficient (K_{v2}/σ^4) is zero, thus has only one solution. In fact, in typical stratified
waters the diffusivity below the surface mixed layer (K_{v2}) is $1-9 \times 10^{-5} \text{ m}^2 \text{ s}^{-1}$, and the
thickness of SCML (2σ) is from several meters to tens of meters (Cullen, 2015), thus,
 K_{v2}/σ^4 (values from 8.64×10^{-9} to $7.78 \text{ m}^{-2} \text{ s}^{-1}$) can be neglected in some cases. When
315 $K_{v2}/\sigma^4 \rightarrow 0$, for non-zero sinking velocity we get one solution from Eq. (9),

$$z_n = z_m + \frac{(1-\alpha)\varepsilon\sigma^2}{w} \quad w \neq 0 \quad (12)$$

Both Eqs. (11) and (12) show that the nitracline depth is located below the SCML
depth, i.e., $z_n > z_m$ (Fig. 1). A numerical study in weak vertical mixing environments
showed a similar result (Beckmann and Hense, 2007). Note that the SCML represents
320 the SBML in our model. In some oligotrophic oceans, the SCML will be deeper than
the SBML due to the effect of photoacclimation on the vertical distribution of
chlorophyll (Fennel and Boss, 2003). For example, Li et al. (2015) showed that the
modeled maximum nitrate gradient (nitracline) occurred below the depth of SCML in
the northern SCS, and then we can deduce that the nitracline depth is also deeper than
325 the depth of SBML. In the Mediterranean Sea, Bahamón et al. (2003) found that the

nitracline occurred below the depth of SCML at 88% of the stations (50 out of 57 stations). As well known, the SCML in the Mediterranean is often due to photoacclimation. It is not surprising that the other 12% of the stations (7 out of 57) in the Mediterranean Sea are against $z_n > z_m$ because photoacclimation leads to a much deeper SCML than the SBML. Thus, we conclude that the nitracline depth is located below the SBML depth.

3.2.2 Nitracline steepness and SCML

To illustrate the relationship between the nitracline steepness and the SCML, by integrating Eq. (8) from depth z_n to z_b and using the assumption for phytoplankton at the bottom boundary, i.e., $P \rightarrow 0$ for $z \rightarrow z_b$ (Eq. 5), we get

$$\left. \frac{dN}{dz} \right|_{z_n} = \left. \frac{dN}{dz} \right|_{z_b} + \left(\frac{z_n - z_m}{\sigma^2} + \frac{w}{K_{v2}} \right) \gamma P \Big|_{z_n} - \frac{(1-\alpha)\varepsilon\gamma}{K_{v2}} \int_{z_n}^{z_b} P dz \quad (13)$$

This equality indicates that the nitracline gets steeper as the distance between the depths of nitracline layer and SCML is increased.

Incorporating Eq. (11) into Eq. (13) leads to

$$\left. \frac{dN}{dz} \right|_{z_n} = \left. \frac{dN}{dz} \right|_{z_b} + \left(\sqrt{\frac{w^2}{4K_{v2}^2} + \frac{(1-\alpha)\varepsilon}{K_{v2}} + \frac{1}{\sigma^2}} + \frac{w}{2K_{v2}} \right) \gamma P \Big|_{z_n} - \frac{(1-\alpha)\varepsilon\gamma}{K_{v2}} \int_{z_n}^{z_b} P dz \quad (14)$$

Equation (14) indicates that the nitracline steepness is negatively related to the thickness of SCML.

3.2 Analytical solutions for nitracline features

3.2.1 Depth of the nitracline

By substituting the general Gaussian function for chlorophyll below the surface mixed layer (Eq. 6) into Eq. (1), we obtain the steady-state net growth rate of phytoplankton below the surface mixed layer:

$$\mu_m \min(f(I), g(N)) - \varepsilon = -K_{v2} \left(z - \left(z_m - \frac{w\sigma^2}{2K_{v2}} \right) \right)^2 / \left(\sigma^4 + w^2/4K_{v2} + K_{v2}/\sigma^2 \right) \quad (15)$$

Let $z_0 = z_m - w\sigma^2/(2K_{v2})$ in the first term of the right-hand of Eq. (15). From the
 350 result given by Gong et al. (2015), we know that z_0 is the location of the maximum
 growth rate of phytoplankton (hereafter named as the depth of optimal growth), where
 the transition from nutrients limitation to light limitation occurs (i.e., $f(I)=g(N)$ at
 depth z_0).

Clearly, $z_n > z_0$ (Eq. 11). Hence, the growth of phytoplankton at the nitracline depth
 355 z_n is limited by light, i.e., $\mu_m \min(f(I), g(N))|_{z_n} = \mu_m f(I)|_{z_n}$. In other words, the
 growth rate of phytoplankton at the nitracline depth is a function of the light level at
 the nitracline depth, $I(z_n)$. Thus, from Eqs. (11) and (15), we obtain the growth rate of
 phytoplankton at the nitracline depth, that is,

$$\mu_m f(I)|_{z_n} = \alpha \varepsilon \quad (16)$$

360 Note that the derivation of Eq. (16) only works when light and nutrient limitation
 (Blackman's law of limiting factors) is applied. Substituting the Michaelis-Menten
 form for $f(I)$ into Eq. (16), we have

$$I(z_n) = \frac{K_I}{\mu_m/\alpha \varepsilon - 1} \quad (17)$$

Rearranging Eq. (17), we find $\mu_m - \alpha \varepsilon = \alpha \varepsilon K_I / I(z_n)$. This equality indicates that the
 365 maximum rate of NPP, $(\mu_m - \alpha \varepsilon)P$, is inversely proportional to the light level at the
 nitracline depth, $I(z_n)$. Lande et al. (1989) found that higher maximum rates of
 population growth corresponded to shallower nitracline depths in the central North
 Atlantic.

Furthermore, insertion of Eq. (3) into Eq. (17) yields another expression of the
 370 nitracline depth:

$$z_n = \frac{1}{K_w} \ln \frac{I_0 (\mu_m / \alpha \varepsilon - 1)}{K_I} - \frac{K_c}{K_w} \int_0^{z_n} P dz \quad (18)$$

Note that Eq. (18) is obtained on the premise that the nitracline depth exists. This

equality shows that the nitracline depth is inversely proportional to the light attenuation coefficient of water (K_w), and it deepens logarithmically with increasing surface light intensity (I_0). It is noted that the nitracline depth has a negative relation with the self-shading of phytoplankton ($K_c \int_0^{z_n} P dz$).

Importantly, Eq. (18) predicts that the nitracline depth has no relation with subsurface diffusivity. Aksnes et al. (2007) also proposed a similar result that a shoaling nitracline per se cannot be taken as an unequivocal sign of increased upwelling, as well as eddy diffusion. However, this does not mean that fluid dynamics are unimportant in shaping vertical distribution of nitrate.

Equation (18) also indicates that both a higher recycling efficiency (α) and a larger loss rate (ε) lead to a shallower nitracline, while the enhanced maximum growth rate of phytoplankton (μ_m) moves the nitracline depth downward. Modeling results showed that the nitracline was shoaled by 24% (from 84 m upwards to 64 m) when both the recycling efficiency (α , from 0.6 to 0.8) and the loss rate (ε , from 0.3 d⁻¹ to 0.4 d⁻¹) were increased by 33%. Accordingly, the predicted nitracline depth from Eq. (18) varied from 86 m to 71 m. Increasing μ_m by 33% (from 0.9 d⁻¹ to 1.2 d⁻¹) makes the simulated nitracline deepening slightly (from 84 m to 88 m), leading to the predicted nitracline depth changing from 86 m to 92 m. The experiments with varying parameter values indicate that the updated z_n (based on the model runs) matches well the predicted z_n of Eq. (18).

3.2.2 Steepness of the nitracline

In steady state, integrating Eq. (2) from the nitracline depth z_n to the bottom boundary z_b , and considering the light limitation of phytoplankton growth below depth z_n (Eq. 15), we obtain the nitrate gradient below the surface mixed layer,

$$\left. \frac{dN}{dz} \right|_{z_n} = \left. \frac{dN}{dz} \right|_{z_b} + \frac{1}{K_{v2}} \int_{z_n}^{z_b} (\alpha\varepsilon - \mu_m f(I)) \gamma P dz \quad (19)$$

This equality shows that the nitracline steepness enhances with increasing nitrate

gradient at the bottom boundary ($\frac{dN}{dz}|_{z_b}$) which depends on the intensity of nitrate

400 intrusion from below. The vertical diffusion negatively influences the nitracline steepness. The modeled time-series distributions of nitrate gradients and diffusive nitrate fluxes in the northern SCS and the upstream Kuroshio Current showed similar results (Li et al., 2015). Beckmann and Hense (2007) conducted sensitivity analysis of both vertical diffusivity and nutrient concentration at the bottom boundary to examine
405 the vertical phytoplankton and nutrient profiles in oligotrophic oceans and their numerical results support the relations presented in Eq. (19).

3.3 Analytical solutions for SCM characteristics

Similar to methods used by Gong et al. (2015), the piecewise function for vertical chlorophyll profile (Eq. 6) was incorporated into the nutrient-phytoplankton model
410 (Eqs. 1-2) at steady state to derive the three SCM characteristics (SCML thickness, its depth and intensity).

For $z = z_m$ and $z = z_m + \sigma$, the net growth rate of phytoplankton (Eq. 15) can be respectively expressed as follows:

$$\mu_m f(I)|_{z=z_m} - \varepsilon = K_{v2}/\sigma^2 \quad (20)$$

415
$$\mu_m f(I)|_{z=z_m+\sigma} - \varepsilon = -w/\sigma \quad (21)$$

By substituting the growth limitation function for light to Eq. (20) or Eq. (21), we obtain the expression of parameter z_m , i.e.,

$$z_m = \frac{1}{K_w} \ln \left[\left(\frac{\mu_m}{\varepsilon + K_{v2}/\sigma^2} - 1 \right) \frac{I_0}{K_l} \right] - \frac{K_c}{K_w} \int_0^{z_m} P dz \quad (22)$$

or

420
$$z_m = \frac{1}{K_w} \ln \left[\left(\frac{\mu_m}{\varepsilon - w/\sigma} - 1 \right) \frac{I_0}{K_l} \right] - \frac{K_c}{K_w} \int_0^{z_m+\sigma} P dz - \sigma \quad (23)$$

Subtracting Eqs. (22) and (23), and rearranging, we obtain the expression of parameter σ :

$$\left(\frac{\mu_m}{\mu_m - \varepsilon + w/\sigma} - 1 \right) \exp^{K_w \sigma + K_c \int_{z_m}^{z_m + \sigma} P dz} = \frac{\mu_m}{\mu_m - \varepsilon - K_{v2}/\sigma^2} - 1 \quad (24)$$

Neglecting terms including self-shading of phytoplankton (K_c) in Eqs. (22-24), both
 425 the analytical solutions of the depth and thickness of SCML are the same as the results
 presented in Gong et al. (2015). The self-shading effect of phytoplankton plays an
 important role in vertical pattern of chlorophyll (Shigesada and Okubo, 1981;
 Klausmeier and Litchman, 2001; Beckmann and Hense, 2007). In line with common
 sense, our analytic results indicate that a higher self-shading of phytoplankton
 430 negatively influences the depth and thickness of the SCML (Eq. 22 and Eq. 24),
 having similarly effect as an increasing light attenuation coefficient of water, K_w .

The expression of the SCML intensity is different from the results presented in
 Gong et al. (2015). Integrating Eq. (7) from the surface of water to the bottom of
 surface mixed layer (z_s), and from the bottom of surface mixed layer to the base of our
 435 model domain (z_b) respectively, gives:

$$(1 - \alpha) \varepsilon \gamma P_0 z_s = K_{v2} \frac{dN}{dz} \Big|_{z_s+0} + N_{inML} \quad (25)$$

$$(1 - \alpha) \varepsilon \gamma \lambda h = K_{v2} \frac{dN}{dz} \Big|_{z_b} - K_{v2} \frac{dN}{dz} \Big|_{z_s+0} \quad (26)$$

Parameter λh (mg/m^2) is assumed as the integrated chlorophyll concentration below
 the surface mixed layer. Based on the properties of Gaussian function, λ can be
 440 expressed as $\lambda = \Phi\left(\frac{z_b - z_m}{\sigma}\right) - \Phi\left(\frac{z_s - z_m}{\sigma}\right)$, where $\Phi\left(\frac{z_b - z_m}{\sigma}\right)$ and $\Phi\left(\frac{z_s - z_m}{\sigma}\right)$ can
 be obtained from the standard normal table. According to the property of Gaussian
 function, we have $0.68 < \lambda < 1.00$, $z_s < z < z_b$, under the assumption of $z_s < z_m - \sigma$.

Adding Eqs. (25) and (26) yields:

$$(1-\alpha)\varepsilon\gamma(\lambda h + P_0 z_s) = K_{v2} \frac{dN}{dz} \Big|_{z_b} + N_{inML} \quad (27)$$

445 Nitrogen input to the surface mixed layer (N_{inML}) causes an increase of surface chlorophyll concentration (Eq. 25). Hence, the total chlorophyll in stratified water columns ($\lambda h + P_0 z_s$) increases with increasing N_{inML} (Eq. 27), which has also been predicted by the numerical study of Mellard et al. (2011) and supported by the experimental test of Mellard et al. (2012).

450 Because recycling processes are assumed to not immediately convert dead phytoplankton back into dissolved nutrients below the surface mixed layer, i.e., $\alpha \neq 1$, the total chlorophyll concentration below the surface mixed layer and the intensity of SCML can be respectively expressed as:

$$\lambda h = \frac{K_{v2}}{(1-\alpha)\varepsilon\gamma} \frac{dN}{dz} \Big|_{z_b} + \frac{N_{inML} - (1-\alpha)\varepsilon P_0 z_s}{(1-\alpha)\varepsilon\gamma} \quad (28)$$

$$455 \quad P_{\max} = \frac{1}{\lambda\sqrt{2\pi\sigma}} \left(\frac{K_{v2}}{(1-\alpha)\varepsilon\gamma} \frac{dN}{dz} \Big|_{z_b} + \frac{N_{inML} - (1-\alpha)\varepsilon P_0 z_s}{(1-\alpha)\varepsilon\gamma} \right) \quad (29)$$

The integrated chlorophyll concentration below the surface mixed layer (λh) and the intensity of SCML (P_{\max}) are influenced by N_{inML} positively and by P_0 negatively (Eqs. 28-29). That is to say, the influence of nitrate input to the surface mixed layer on the SCML intensity (also on the integrated chlorophyll concentration below the surface mixed layer) is non-linear. Hence, their changes (λh and P_{\max}) with varying N_{inML} cannot be obtained from the steady-state solutions straight forwardly, depending on the specific parameter combinations in the model. For example, λh and P_{\max} decrease when increasing nutrient enrichment directly to the surface mixed layer in the ecosystem given by Mellard et al. (2011), while they are nearly unchanged in
465 oligotrophic oceans (Varela et al., 1994).

Our results (Eqs. 28-29) also show that enhanced subsurface diffusivity (K_{v2}) increases the integrated chlorophyll concentration and the intensity of the SCML (λh and P_{\max}), as a result of a higher nitrate flux ($K_{v2}n$). Physical upward transport of

nitrate across the bottom of nitracline is indeed the main nitrogen source for NPP in
470 the euphotic zone (Ward et al., 1989).

4 Discussion

4.1 Light effects on nitracline with SCML

We now examine how the steady state nitracline in relate to SCML depends on light
availability, especially light level at the nitracline depth.

475 Substituting Eq. (17) to Eq. (28) and rearranging, we have

$$\frac{K_{v2}}{\lambda h + P_0 z_s} \frac{dN}{dz} \Big|_{z_b} + \frac{N_{inML}}{\lambda h + P_0 z_s} = \varepsilon \gamma - \frac{\mu_m \gamma}{K_I / I(z_n) + 1} \quad (30)$$

This equality indicates that the light level at the nitracline depth, $I(z_n)$, is positively
related to the integrated chlorophyll concentration in the whole water column,
 $\lambda h + P_0 z_s$. we can derive from Eq. (3) that the nitracline depth (z_n) is inversely related
480 to integrated chlorophyll. This inverse relationship has been observed in many regions.
In southern California coastal waters, the phytoplankton standing stock and its
primary production rate were positively related to the reciprocal nitracline depth
(Eppley et al., 1978; Eppley et al., 1979). Bahamón et al. (2003) found that larger
depth-integrated chlorophyll with an average deeper SCML and nitracline (~129m,
485 ~136m, respectively) occurred in the Western Sargasso, Central Sargasso and Eastern
Atlantic, compared with that in the Canary Current zone.

The nitracline depth deepens with increasing surface light intensity but with
decreasing light attenuation coefficients (K_w and K_c). These results were consistent
with observations, e.g., Letelier et al. (2004) found the depth of the nitracline to
490 coincide with an isolume, a depth of constant light level in the North Pacific
Subtropical Gyre.

The predicted effect of surface light intensity and light attenuation coefficient on
the nitracline depth (Eq. 18) implies that the nitracline depth in stratified waters may
have seasonal variations. In the North Pacific Subtropical Gyre, Letelier et al. (2004)

495 found that the nitracline depth differences between winter and summer disappeared
when nitrate concentrations were plotted against light level in the water column.
Aksnes et al. (2007) found that the seasonal pattern of nitracline depth was governed
by seasonality in light attenuation coefficient, rather than in surface light intensity.
Particularly, the inverse proportional relationship between the nitracline depth and
500 light attenuation coefficient (Eq. 18) has also been derived from a steady-state model
by Aksnes et al. (2007), which is consistent with observations in the coastal upwelling
region off Southern California (Aksnes et al., 2007). Tiera et al. (2005) found a
significant positive correlation between the nitracline depth and the depth of 1%
surface light intensity (the proportion of reciprocal light attenuation coefficient) in the
505 Eastern North Atlantic Subtropical Gyre. Bahamón et al. (2003) showed that the
nitracline depth remained relatively constant around 1% surface light intensity depth
in Western Sargasso.

The nitracline steepens with a higher light attenuation coefficient (K_w and K_c) due to
 K_w and K_c negatively influencing SCML thickness (Eqs. 14 and 25). Numerical
510 modeling showed that a higher K_w leads to a thinner SCML and thus a steeper
nitracline layer (Beckmann and Hense, 2007). Aksnes et al. (2007) also found that the
fluctuations in the nitracline steepness were positively correlated with the fluctuations
in reciprocal Secchi depth (i.e., light attenuation coefficient) in the upwelling area off
the coast of the Southern California. We further point out that the nitracline steepness
515 almost stays constant when changing surface light intensity (I_0), because surface light
intensity has no relation to the SCML thickness (Eq. 25). The sensitivity analysis of a
one-dimensional (vertical) model showed that the vertical nutrient profiles were
almost paralleling with each other when increasing surface light intensity (Beckmann
and Hense, 2007).

520 The inverse effects of light attenuation coefficient on the nitracline steepness and its
depth imply that the nitracline becomes steeper as the nitracline shoals. Aksnes et al.
(2007) found this consistent pattern in the upwelling area off the coast of the Southern
California.

4.2 In presence of surface nutrient input

525 Current evidences and modeling analyses suggest that climate warming will increase ocean stratification, and hence reduce nutrient exchange between the ocean interior and the upper mixed layer (Cermeno et al., 2008; Chavez et al., 2011). Therefore, nutrient input directly to the euphotic layer due to atmospheric deposition may become a relatively more important nutrient supply mechanism to the euphotic
530 layer (Mackey et al., 2010; Okin et al., 2011; Mellard et al., 2011). However, few model studies (e.g., Mellard et al. 2011) have explored the influences of external surface nutrient supply on vertical phytoplankton distribution.

Observations show that an inter-zone exists between the transition of the surface mixed layer and the deep layer, where the nutrient gradient equals nearly zero
535 $\frac{dN}{dz}\Big|_{z_s+0} = 0$ (Fig. 3), leading to the solution in Eq. (26). It follows that the total chlorophyll in the surface mixed layer depends on the surface nutrient supply (N_{inML}) (Eq. 26). In this case, if N_{inML} is negligible, Eq. (26) degenerates to

$$(1-\alpha)\varepsilon\gamma P_0 z_s = 0 \quad (31)$$

In this case, the dead phytoplankton in surface mixed layer must be fully recycled,
540 i.e., $\alpha=1$, in order to sustain the positive chlorophyll concentration ($P_0>0$). In other words, if the dead phytoplankton cannot be fully recycled in the surface mixed layer, external nutrient supply to the layer is needed to fuel the growth of phytoplankton. Thus, the term, external nutrient supply to the surface mixed layer, should be included in the system equations at steady state to make a positive surface chlorophyll
545 concentration. Numerical results by Mallard et al. (2011) also showed that phytoplankton populations can grow in the mixed layer and in the deep layer together, when there is nutrient input directly to the mixed layer. However, a surface nutrient source is not a necessary term for a model approach where dissolved organic matter and detritus are explicitly resolved (Beckmann and Hense, 2007).

550 Accordingly, we treat the vertical phytoplankton distribution as a piecewise

function, comprised by a linear function in the surface mixed layer and a Gaussian function below, which is more realistic than the general Gaussian function. The assumption of the piecewise function for phytoplankton is also consistent with the assumption of piecewise vertical diffusivity. For simplicity, we assume that the transition layer between the surface mixed layer and the deep one is infinitely thin, and the chlorophyll is continuous within the transition layer. By assuming the SCML depth is significantly deeper than the base of the surface mixed layer, we obtain the steady state solutions for the SCML depth and thickness, similar to the solutions using the general Gaussian function. However, the intensity of the SCML is affected by surface nutrient supply with an associated positive increase in phytoplankton concentration.

4.3 SCML trapping Nutrient

Observations and numerical simulations showed that SCML played a role as a nutrient trap in some regions, restricting the diffusive flux of nitrates to the surface mixed layer (Anderson, 1969; Klausmeier and Litchman, 2001; Navarro and Ruiz, 2013).

From Eq. (10), we know $z_s < z_{n1} < z_0 - \sigma < z_m - \sigma$ (Fig. 1). That is, the SCML occurred below depth z_{n1} . For $z_m < z_n$ (Eq. 10), we know that the upward diffusive nitrate is sufficient to sustain the fast growth of phytoplankton in the lower part of the SCML ($z_m < z < z_m + \sigma$). To explore the SCML restricting nitrates into the surface mixed layer, next, we examine if the nitrate concentration at depth z_{n1} above the upper boundary of the SCML ($z_{n1} < z_m - \sigma$) is depleted.

According to the definition of the depth z_0 (where $f(I) = g(N)$ holds) and $z_0 > z_{n1}$ (Eq. 10, Fig. 1), we know that the growth of phytoplankton at depth z_{n1} is nitrate-limited, i.e., $\mu_m \min(f(I), g(N))|_{z_{n1}} = \mu_m g(N)|_{z_{n1}}$. From Eq. (14), we get that at depth z_{n1} , the growth rate of phytoplankton equals the recycling efficiency of dead phytoplankton, i.e., $\mu_m g(N)|_{z_{n1}} = \alpha \varepsilon$. Inserting the Michaelis-Menten form for $g(N)$

into this equality yields: $N(z_{n1}) = K_N / (\mu_m / \alpha \varepsilon - 1)$. Phytoplankton maximum growth rates (μ_m) of 0.2 to 1 per day are typical in optical environmental conditions (Banse, 1982; Timmermans et al., 2005). We choose 0.5 per day to illustrate the result. Loss rate (ε), although not well documented, is often quoted as 10% of the growth rate (Parsons et al., 1984). A reasonable choice for the remineralization efficiency seems to be $\alpha=0.5$ (Huisman et al., 2006). The typical value of half-saturation constants for nitrate (K_N) is between 0.1 and 0.7 mmol N m⁻³ in oceans (Eppley et al., 1969). We adopt 0.4 mmol N m⁻³. Thus, we obtain that the nitrate concentration at depth z_{n1} , $N(z_{n1})$, is equal to 0.03 mmol N m⁻³, a value lower than the detection limit, indicating the depletion of nitrate above depth z_{n1} .

Because the SCML acts as a nutrient barrier, it is easy to understand that the rate of NPP in the SCML ($(\mu_m \min(f(I), g(N)) - \alpha \varepsilon)P, z_m - \sigma < z < z_m + \sigma$) is positively related to upward nitrate flux that is trapped. This condition can simply be derived by integrating Eq. (2) vertically at steady state, i.e., $\int_{z_m - \sigma}^{z_m + \sigma} (\mu_m \min(f(I), g(N)) - \alpha \varepsilon) \gamma P dz = K_{v2} dN/dz \Big|_{z_m - \sigma}^{z_m + \sigma}$. This result suggests that, the production within the SCML is fuelled mainly, by nitrate and is thus NPP. Because at the nitracline depth the gross growth rate $\mu_m \min(f(I), g(N))$ equals the recycling of dead phytoplankton $\alpha \varepsilon$, for the constant $\alpha \varepsilon$ we assumed, within the nitracline layer ($z_{n1} < z_m - \sigma$ and $z_m < z_{n2}$) the nitrate uptake by phytoplankton has to be supplied by the vertical diffusion. Observations also showed that most of the primary production in SCML was supported by nitrate from vertical diffusion, with an average f -ratio (i.e., relative contribution of the nitrate uptake to the total nitrogen uptake) of 0.74 ± 0.26 during early summer in Canadian Arctic waters (Martin et al., 2012).

4.4 Vertical profile of nitrate gradients

From the monotonicity of the quadratic function of depth z in the left-hand of Eq. (9), we know that $d^2N/dz^2 < 0$ when $z_s < z < z_{n1}$ and $z_{n2} < z < z_b$, but $d^2N/dz^2 > 0$ when $z_{n1} < z < z_{n2}$. In other words, the vertical gradient of the nitrate concentration (dN/dz)

605 decreases with depth on the interval (z_s, z_{n1}) , while increases on the interval (z_{n1}, z_{n2}) ,
and then decreases on the interval (z_{n2}, z_b) . If we consider the distribution of vertical
nitrate gradients as continuous across the base of the surface mixed layer, then we get
 $dN/dz < 0$ for $z_s < z < z_{n1}$ under the assumptions of the uniform nitrate distribution within
the surface mixed layer (i.e., $dN/dz = 0, 0 < z < z_s$). The schematic of vertical profiles of
610 nitrate gradients and chlorophyll concentrations in stratified waters is shown in Fig. 1.

The negative gradient of nitrate below the surface mixed layer ($dN/dz < 0$ for
 $z_s < z < z_{n1}$) indicates that the nitrate concentration decreases with depth on the interval
 (z_s, z_{n1}) . This decreasing nitrate feature has rarely been observed by traditional
measurements probably due to the technique-limited low resolution. Some float data
615 showed this feature in vertical nitrate profiles, for example, Sakamoto et al. (2009)
found it at depths below the base of surface mixed layer (~45-50 m) by the ISUS
temperature-compensated data at an eastern Pacific oligotrophic station. Our in situ
time series measurements using the ISUS at SEATS station also showed this
decreasing feature at depths ~25-30 m (Fig. 4). We note that this decreasing nitrate
620 feature will disappear in our derivation if the subsurface vertical diffusion is too weak
(Eq. 12) or the surface mixed layer is deeper than depth z_{n1} . Simulating results showed
that the negative gradient of nitrate becomes smaller with increasing the sinking
velocity (w) and the recycling efficiency (α). This implies that the negative gradient is
likely the result of the consumption of nitrate by phytoplankton exceeding the supply
625 of nitrate.

4.5 Limitation and application

The model in this study integrates a number of physical, chemical, and biological
processes that act together to determine the vertical distribution of phytoplankton and
nitrate, under the assumption that the system is strictly vertical and in steady state. A
630 few processes such as oxygen status, photoacclimation, luxury uptake of nutrients,
phytoplankton motility, concentration-dependent-herbivory, and depth-dependent
herbivory are not included, although they can affect the vertical distribution of
phytoplankton and nitrate. Detritus, dissolved organic matter, and zooplankton are not

included explicitly, and all loss processes, except sinking, are set to be linearly
635 proportional to phytoplankton. The sinking velocity of phytoplankton is assumed
independent of density gradients. Further, the vertical transport of nutrients is only by
eddy diffusion in our model; in reality, nutrients can be supplied by many processes
(turbulence, internal waves, storms, slant-wise and vertical convection), especially by
upwelling (Katsumi and Hitomi, 2003; Aksnes et al., 2007).

640 In this study, the sinking velocity of phytoplankton is set independent of nitrate
concentration. Vertically-varying sinking velocity have been observed as
physiological response to variations in light or nutrient levels (Steele and Yentsch,
1960; Bienfang and Harrison, 1984; Richardson and Cullen, 1995). The sinking
velocity reduces with decreased light level and with increased nutrient concentration,
645 and the resulting divergence in sinking velocity can be large enough to affect the
location of the phytoplankton particle maximum. However, numerical results given by
Fennel and Boss (2003) showed analytically that the divergence of the sinking rate
contributes to the location of the SBM layer in a significant way only when the
divergence in sinking rates occurred above the compensation depth in stable,
650 oligotrophic environments. They also derived that in stable, oligotrophic
environments with a predominance of small cells, the biomass maximum is located at
the depth where growth and losses are equal, leaving few influence by sinking
divergence.

It is worth pointing out that, in extreme oligotrophic regions, the SCML is very
655 deep and attributable mostly to photoacclimation of chlorophyll content rather than to
a peak of biomass (Steele 1964; Fennel and Boss, 2003; Cullen, 2015). The process of
photoacclimation is also important for the nutrient-phytoplankton system (with
stratified conditions) we focused on. To explore the influence of photoacclimation on
the nitracline, we parameterized Chl:C using the mathematical description by Cloern
660 et al. (1995), i.e., $\text{Chl:C} = 0.003 + 0.0154 \exp(0.050T) \exp(-0.059I) \mu'$. That is, Chl:C
is the ratio of Chl a to C in phytoplankton growth at steady state under defined
temperature T (°C), daily irradiance I (mol quanta $\text{m}^{-2} \text{d}^{-1}$), and at nutrient-limited

growth rate μ' ($\mu' = N/(K_N + N)$). The ratio Chl:C increases when temperature T or nitrogen concentration N increases, while decreases with increasing daily irradiance I .
665 Let $R = \text{Chl:C}$, then the nitrogen content of phytoplankton can be written as $\gamma = 1/(6.625 \cdot 12 \cdot R)$, corresponding to a C:N ratio of 6.625 and a carbon atomic mass of 12. From the expression of nitracline depth (Eq. 18), we know that the ratio Chl:C has no influence on the nitracline depth. While the nitracline steepness increases with increasing parameter γ (Eq. 19). In other words, the nitracline gets steeper with a
670 lower ratio Chl:C. Note that a certainly more realistic model would be one with equations that explicitly resolve variations of the Chl a-to-carbon and nitrogen-to-carbon ratio of phytoplankton.

The piecewise equation (Eq.6) can be used to mimic a large variety of vertical chlorophyll profiles from coastal, upwelling, open oceans and high latitude waters
675 (Fig. 2). For example, for $z_s > 0$, when the depth of surface mixed layer equals or is deeper than the depth of SCML, the vertical profiles like Fig. 2b and 2c are often found in well-mixed waters (Uitz et al., 2006). For $z_s = 0$, the vertical distribution of chlorophyll concentration (Fig. 2d) can be expressed by a Gaussian function, which is usually found in coastal upwelling waters (Xiu et al., 2008). Particularly, when $z_s = 0$
680 and $z_m = 0$, the surface bloom occurs (Fig. 2e). In general, the vertical profiles of chlorophyll can be classified into two types, i.e., one peak distribution or uniform distribution in large regions of lakes and oceans (Uitz et al., 2006; Lavigne et al., 2015). Note that the skewed profiles of chlorophyll with a sharp SCM was not considered in this study. The small-scale (1 m or less) vertical heterogeneity in
685 chlorophyll distribution has been shown to be common features in coastal waters (Sullivan et al., 2010; Prairie et al., 2011; Durham and Stocker, 2012), named as thin layer.

Choosing the values of model parameters represented the system in the northern South China Sea (given in Table 1), we can retrieve the nitracline depth and steepness,
690 the optimal depth and the three SCM characteristics. To make calculation easy, we neglect the term of self-shading by phytoplankton in the calculation, because a higher

self-shading parameter has the same effect as an increasing light attenuation coefficient by water. The calculated and observed values of these parameters are listed at Table 2. All these parameters calculated are in a reasonable range, although there
695 are some discrepancies compared with observations. In fact, this is not surprising, considering that we assume a single phytoplankton group and neglect the microbial loop and the dynamics of the dissolved organic matter and detritus pools.

We stress that the analytical solutions of nitracline are valid only for estimates of z_m , h , and σ that are consistent with the model's numerical steady-state solution. The
700 numerical steady-state solution in turn depends on the combination of parameter values and on the forcing, boundary conditions. The approximations of z_m , h , and σ are entirely conditioned by the modeling results and thus also depend on the combination of model parameter values. To combine the analytical steady state solutions with observed z_m , h , and σ (as derived from vertical profiles of chlorophyll a
705 concentration) is only meaningful after model calibration (identifying a model solution that is in some agreement with the observed z_m , h , and σ).

5 Summary

We have presented a theoretical framework to investigate the interaction of phytoplankton and nutrient in stratified water column. A piecewise function for
710 chlorophyll profiles comprising a linear function in the surface mixed layer and a Gaussian function below is assumed in the nutrient-phytoplankton model at steady state. A number of important findings are obtained under conditions of the model equations imposed.

In steady state, the nitracline is confined between two depths where the gross
715 growth rate equals the recycling efficiency of dead phytoplankton, indicating that within the nitracline, nitrate consumption by phytoplankton has to be replenished by the upward flux of nitrate. This layer thereby is the major contributor to new primary production.

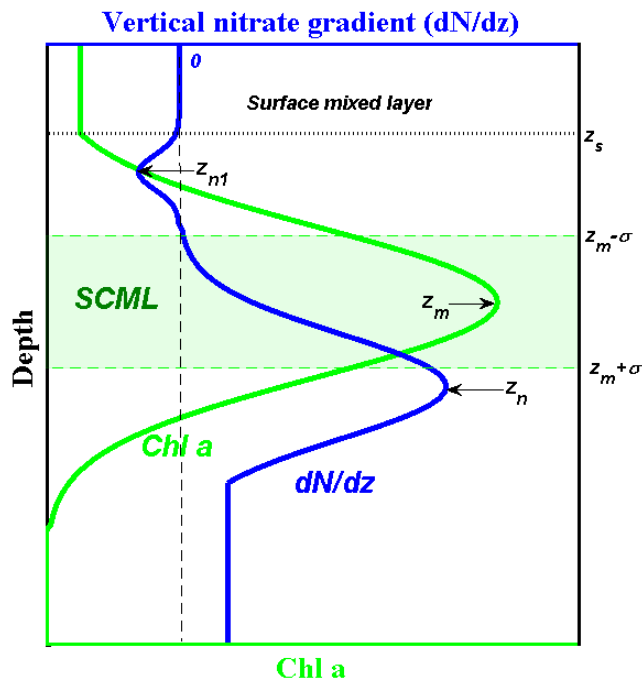
The nitracline depth locates below the SCML depth; both two depths deepen with

720 either increased surface light intensity or decreased light attenuation coefficient. The
nitracline depth does not depend on the value of the subsurface diffusivity. The
nitracline is steeper with a thinner SCML. The nitracline steepness is positively
influenced by the light attenuation coefficient, yet, responds insignificantly to surface
light intensity.

725 Our analytical solutions show that phytoplankton in the SCML acts as an efficient
nutrient trap, filtering out the upward nitrate supply. The light level at the nitracline
depth has a positive relation with the depth-integrated chlorophyll concentration in the
whole water column and with the maximum rate of NPP, acting as the indicator of
integrated NPP. The NPP is constructed from the model equations that rely in
730 Blackman's law of limiting factor for the growth rate.

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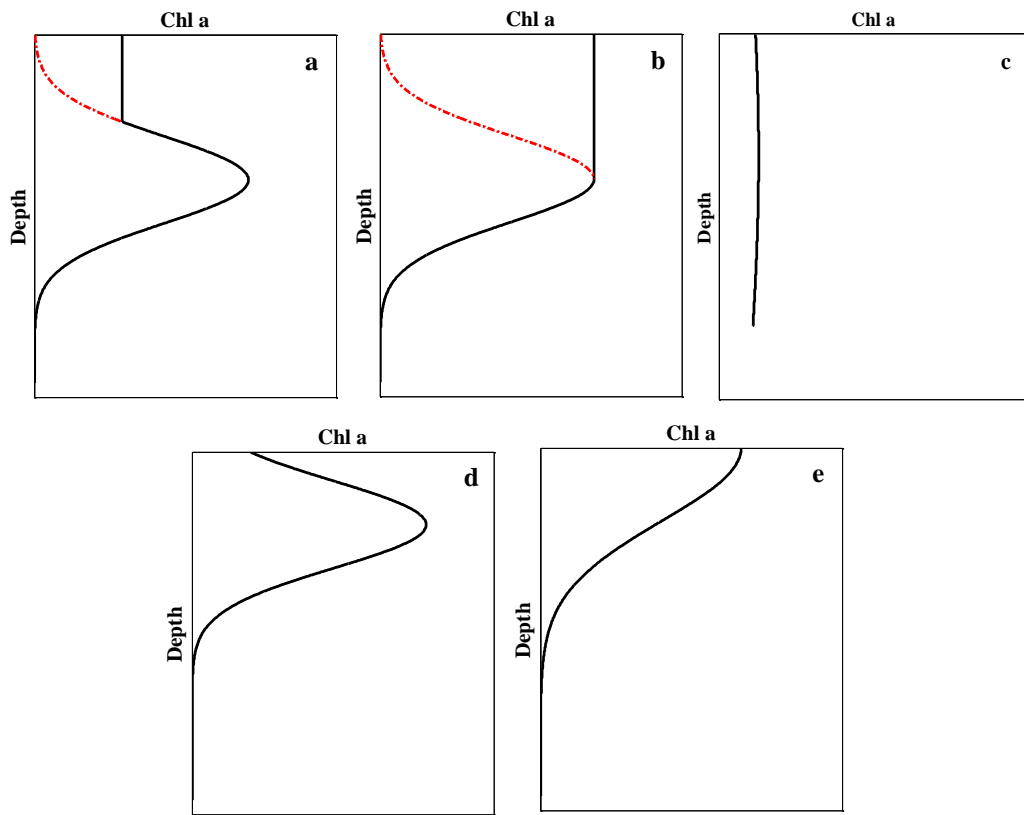
740 Figures
 Figure 1



745 Fig. 1 Schematic picture of vertical profiles of nitrate gradient and chlorophyll (Chl a) in stratified water columns. (blue solid line is the vertical profile of nitrate gradient; green solid line is Chl a concentration as a function of depth; red solid line represents the growth limitation by light, red dotted line by nitrate; horizontal green solid lines indicate the locations of the upper and lower SCML, $z_m - \sigma$, $z_m + \sigma$, respectively; horizontal black dotted line indicates the depth of the surface mixed layer, z_s ; vertical dotted black line represents zero nitrate gradient; z_{n1} and z_n are the locations of extreme nitrate gradients, z_n is the nitracline depth, and z_m is the depth of maximum chlorophyll concentration)

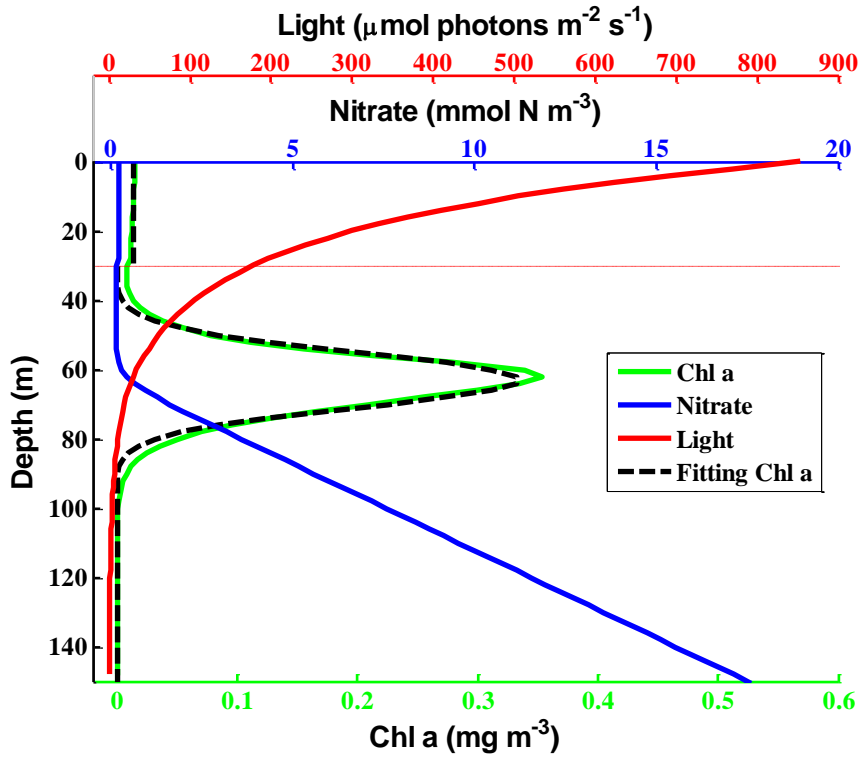
750

Figure 2



755 Fig. 2 Examples of the vertical profiles of chlorophyll (black solid line). (red dotted lines represent the parts of Gaussian fitting curves, not the actual chlorophyll)

Figure 3



760

Fig. 3 Steady-state vertical distributions of chlorophyll, nitrate, and light determined by numerical solutions of Eqs. (1) and (2). Horizontal red dash-dotted line indicates the depth of the surface mixed layer. Black dash line represents the fitting curve of vertical chl a profile. The fitting

equation is

$$P = \begin{cases} 0.013 & 0 \leq z \leq 30 \\ 0.33 \exp\left[-\frac{(z-63)^2}{2 \times 9^2}\right] & 30 < z < 200 \end{cases}$$

765 Figure 4

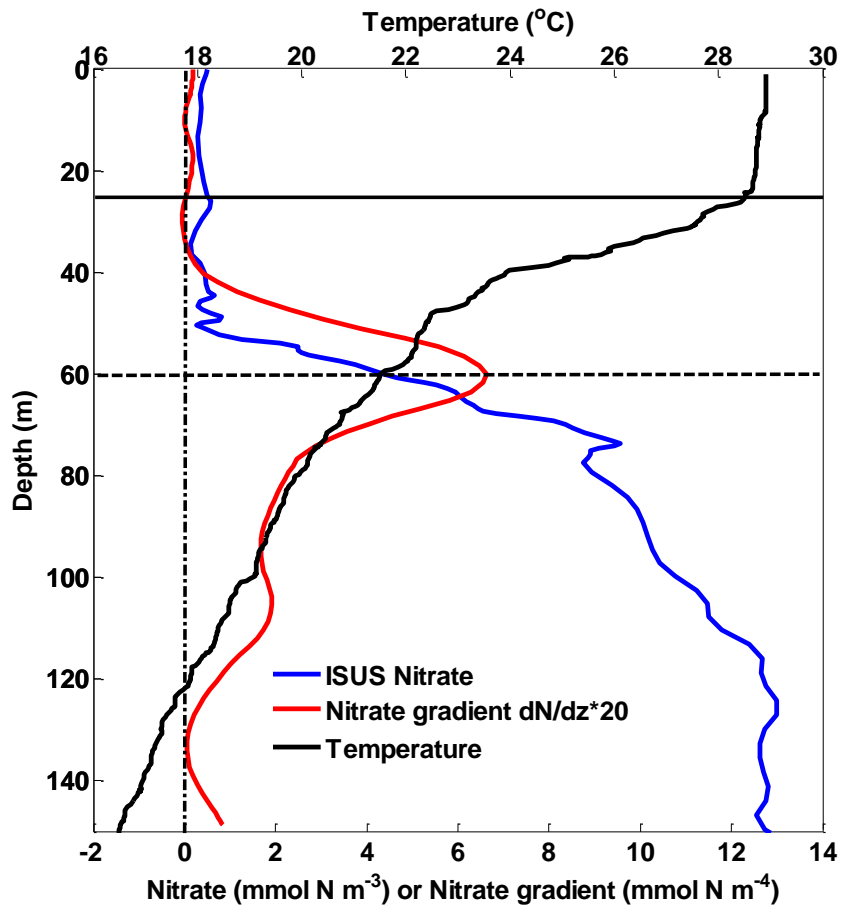


Fig. 4 Vertical nitrate gradient, ISUS nitrate and temperature at SEATS station (2012, cast 36) (horizontal line indicates the depth of the surface mixed layer, horizontal dotted line indicates the depth of nitracline, and the vertical dash-dotted line represents zero nitrate gradient).

Table 1 List of symbols and their values used in models at SEATS station in northern SCS

Model parameters	Description (unit)	Values (range)
I_0	Surface light intensity ($\mu\text{mol photons m}^{-2} \text{s}^{-1}$)	900 (200-1700) ^(1, 2)
K_w	Light attenuation coefficient of water (m^{-1})	0.052 ^(1, 3)
K_c	Light attenuation coefficient of phytoplankton ($\text{m}^2 (\text{mmol N})^{-1}$)	0.05 ^(1, 3)
K_I	Half-saturation constant of light limited growth ($\mu\text{mol photons m}^{-2} \text{s}^{-1}$)	40 ⁽⁴⁾
K_{v1}	Surface diffusivity ($(\times 10^{-4}) \text{m}^2 \text{s}^{-1}$)	2 ⁽⁵⁾
K_{v2}	Subsurface diffusivity ($(\times 10^{-5}) \text{m}^2 \text{s}^{-1}$)	5 ⁽⁵⁾
w	Sinking velocity of phytoplankton (m d^{-1})	1 ⁽⁶⁾
ε	Loss rate of phytoplankton (d^{-1})	0.3 ⁽⁷⁾
α	Nutrient recycling coefficient (dimensionless)	0.6 ⁽⁷⁾
K_N	Half-saturation constant of nutrient uptake (mmol N m^{-3})	0.4 ⁽⁸⁾
μ_m	Maximum growth rate of phytoplankton (d^{-1})	0.9 ^(5, 7)
N_{inML}	Mixed layer nitrate input ($(\times 10^{-7}) \text{mmol N m}^{-2} \text{s}^{-1}$)	4 ^(9, 10)
γ	Nitrate content of phytoplankton (mmol N per mg Chl)	1/1.59 ^(11, 12)
λ	Proportion of integrated chlorophyll below surface mixed layer	0.9
z_s	Depth of surface mixed layer (m)	30 (10-80) ^(13, 14)
z_b	Bottom boundary of model domain (m)	200
$\frac{dN}{dz} \Big _{z=z_b}$	Nitrate gradient at the bottom boundary of model domain (mmol N m^{-4})	0.2 (0-0.2) ^(15, 16, 17)

Superscripts refer to the references that provide the source for the parameter value and the citations are as follows: ⁽¹⁾<http://oceandata.sci.gsfc.nasa.gov/SeaWiFS/Mapped/Annual/9km/>;
⁽²⁾Wu and Gao, 2011; ⁽³⁾Lee Chen et al., 2005; ⁽⁴⁾Raven and Richardson, 1986; ⁽⁵⁾Lu et al., 2010;
775 ⁽⁶⁾Bienfang and Harrison, 1984; ⁽⁷⁾Liu et al., 2007; ⁽⁸⁾Eppley et al., 1969; ⁽⁹⁾Kim et al., 2014;
⁽¹⁰⁾Duce et al., 2008; ⁽¹¹⁾Cloern et al., 1995; ⁽¹²⁾Oschlies, 2001; ⁽¹³⁾Wong et al., 2002; ⁽¹⁴⁾Tseng et
al., 2005; ⁽¹⁵⁾Chen et al., 2006; ⁽¹⁶⁾Our observations; ⁽¹⁷⁾Li et al., 2015.

Table 2 Estimated results and observed values at SEATS station

Variables	Estimated results	Observations
Nitracline depth (m)	86	20-90 ^(1, 2, 3)
Nitracline steepness ($mmol\ N\ m^{-4}$)	0.21	0.30-0.50 ⁽³⁾
Depth of SCML (m)	70	10-75 ^(4, 5, 6)
Intensity of SCML ($mg\ m^{-3}$)	0.47	0.40-0.90 ^(4, 5, 6)
Thickness of SCML (m)	24	10-55 ^(4, 5, 6)

780 Superscripts refer to the references that provide the source for the parameter value and the citations are as follows: ⁽¹⁾Tseng et al., 2005; ⁽²⁾Wong et al., 2007; ⁽³⁾Our observations; ⁽⁴⁾Chen et al., 2006; ⁽⁵⁾Liu et al., 2002; ⁽⁶⁾Liu et al., 2007.

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