

Reviewer comments in black, our replies in green.

REVIEWER 1:

In this manuscript, the authors present newly estimated global ocean N₂O flux to the atmosphere and its confidence interval using observations and two submodels of N₂O production. The paper provides interesting insights but the writing could be improved to make the manuscript clearer. The main problem of the paper, as I see it, is that there are not enough details to assess the validity of the model and results.

We thank the reviewer for the comments. We have tried to clarify the methodology throughout the manuscript.

Below are some major comments and questions, followed by minor edits.

Major comments/questions:

It is unclear how the authors calculate the best estimate of N₂O production using observations (l. 82). How is the range obtained in this case? I thought that the authors might be using the maximums and the minimums of each factor to calculate the range but that does not seem likely.

Errors were calculated with standard error propagation; we added the line: “Here and in the rest of the paper, errors were propagated in the usual way:

$$\text{error} = (((\text{error of A})/A)^2 + ((\text{error of B})/B)^2 + \dots)^{0.5} \times A \times B \times \dots$$

I am having hard time understanding the equation 1. How is this equation derived and why are such large significant figures used? This equation does not account for the latitudinal dependence of pN₂O - wouldn't that be a problem? Isn't it better to use atmospheric model results validated by atmospheric measurements of N₂O?

Eq. 1 is derived from the data in Freing et al. 2009. However, the numbers stated in that paper as the fit to their data are in error, so we here provide the correct numbers as provided by Alina Freing in a pers. comm.. We initially used the numbers exactly as given to us by Alina Freing, but it's true that the number of significant digits is larger than is warranted and we've reduced the significant digits to 7 or 8, so that pN₂O is accurate to 2 decimal places.

We added monthly atmospheric measurements at 12 latitudes. Because the observations were not accurate enough prior to 2000 to show a consistent latitudinal gradient and seasonal cycle, the gradient and seasonal cycle were calculated from the data from 2000-2016 and then added to the older global average observations. We added this description to Section 2.6:

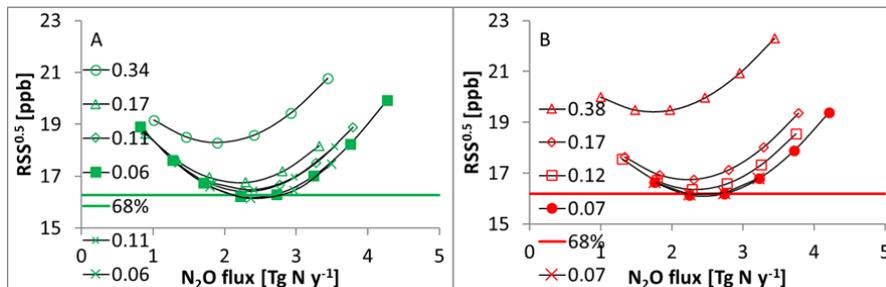
“we also ran a series of simulations with the NOAA pN₂O_{atm} observational data that included seasonal and latitudinal variations. Between 2000 and 2014, we used the monthly observations for the 12 available latitudes. Monthly anomalies relative to the global average were calculated at each available latitude from the 2000-2016 observations. These were added to Eq. 1 from 1965 and 1976, and to the global average observations between 1977 and 1999. In the model simulation, the data were linearly interpolated between the 12 latitudes and monthly observations.”

And we added to Section 3.2:

“When we used observed atmospheric pN₂O that varied with latitude and month (see Section 2.2) the result was essentially the same, with an N₂O flux of 2.4 ± 0.3

Tg N y⁻¹ for the diagnostic sub-model and 2.6 ± 0.3 Tg N y⁻¹ for the prognostic sub-model (data not shown).”

Although not included in the manuscript, we here include a modified Fig. 11 (was Fig. 10 in the submitted manuscript), with the additional simulations using the NOAA pN2O_{atm} observations shown as crosses (at two low O₂ production rates for the diagnostic model and at the optimum net low O₂ production rate for the prognostic model), which shows that when we used the observed atmospheric pN₂O the results were essentially the same:



See also the reply to the comment by reviewer 2 on Line 219-220.

I think there might be a mistake in equation 2. Otherwise, I do not see how a value of 2 could mean that the model deviates from the observations by a factor of 2 in either direction. $10^{(10\log 2)} = 1024$ and it is nothing close to a value of 2. Please explain.

Perhaps, the standard mathematical notation (summation and the number of observations n rather than “average”) would be more appropriate here.

The 10 before log indicated that it’s the 10-base logarithm. This has been corrected to \log_{10} , $\log_{10}(2)=0.31$ and $10^{0.31}=2$. We’ve converted the manuscript to Latex, which allows a subscript inside a superscript, which makes this distinction more clear. We’ve changed the formula to $\Sigma \dots / n$.

It would be useful if the N₂O flux calculation in section 2.7 is explained in a little more detail, rather than stating that it “is calculated with the piston velocity from Sweeney et al. (2007).” I am not familiar with this calculation and would love more explanations on how the ocean N₂O flux is estimated but the Sweeney et al. (2007) is not listed in the references either.

We’ve added the equation for the N₂O flux calculation, including the piston velocity and the reference to Sweeney:

“N₂O flux (=air-sea gas exchange) is calculated as:

$$\text{N}_2\text{O flux} = (\text{pN}_2\text{O}_{\text{atm}} * K_0 * (1 - \text{p}_{\text{watervapor}}) - \text{pN}_2\text{O}) * \text{piston_velocity} * \{660 / \text{Schmidt_number_N}_2\text{O}\}^{0.5} * (1 - \text{ice_cover})$$

, in which K_0 is the solubility {WeissPrice80}, $\text{p}_{\text{watervapor}}$ is the water vapor pressure {Sarmiento92}, $\text{piston_velocity} = 0.27 * (\text{wind speed})^2$ {Sweeney07}, which is optimised for use with the NCEP reanalysis data used here, the Schmidt number for N₂O was taken from {Wanninkhof92}, and the ice cover is calculated by the sea ice model LIM2.”

I am not sure how equation 3 is used to determine the global air-sea flux of N₂O that best fits the $\Delta\text{pN}_2\text{O}$ data, if $\text{RSS}/\text{RSS}_{\text{min}}$ just depends on the number of observations. I do not understand how different model simulations would have different values of $\text{RSS}/\text{RSS}_{\text{min}}$ if the number of observations is the same.

It is not n that varies but rather RSS varies as the results of different model simulations are compared to the same observations. We added information about regridding and the calculation procedure in Section 2.3, Eq. 4 in Section 2.8, and added clarifications to the legend of Fig. 9:

“The 1σ confidence interval, where RSS equals the value calculated from Eq. 3, is indicated by the horizontal lines. A) diagnostic submodel, each point represents a simulation with a different low O₂ slope, B) prognostic model, “no c” is with no N₂O consumption i.e. net production = gross production. All other lines have a constant gross production, and net production varies with different N₂O consumption rates. Range of parameter values is given in Section 8.7 of the supplementary material.” and of Fig. 11: “MSE^{0.5} for the two N₂O submodels compared to the Δp N₂O database as a function of global N₂O flux at different (net) N₂O production rates in the low O₂ regions. A) diagnostic submodel, the four lines represent the four best low O₂ production rates from Fig. 9A, each point represents a simulation, different symbols indicate different low O₂ slopes, points with the same symbols have different oxic N₂O production slopes. B) prognostic submodel, the four lines represent the optimised net production rates at the four best gross production rates from Fig 9B, points with the same symbols have different N₂O slopes for nitrification.”

As for equation 4, I think that its application should be described within the methodology section, rather than just mentioning a little in the discussion section.

Since the F-test at large sample size is insensitive to non-normal distributions we have deleted the equation and accompanying text.

Also, how did the authors optimize various model parameters? And is it not a problem that the optimized oxic $\Delta N_2O/AOU$ slope of $12.7 \mu\text{mol N}_2\text{O} (\text{mol O}_2)^{-1}$ is so different from the global average given earlier in lines 77-78 ($81.5 \pm 1.4 \text{ nmol/mmol}$)? What is the value for this parameter in the prognostic model?

The observed slope of $81.5 \mu\text{mol N}_2\text{O} (\text{mol O}_2)^{-1}$ in figure 3 is a weighted average of the low O₂ slope and the oxic slope. The optimised slopes in the model are $1700 \mu\text{mol N}_2\text{O} (\text{mol O}_2)^{-1}$ under low O₂ and $12.7 \mu\text{mol N}_2\text{O} (\text{mol O}_2)^{-1}$ under oxic conditions. For the weighted average of these model slopes to equal the observed slope of 81.5, the fraction of N₂O that is produced by the low O₂ regions would need to be 4.1% ($= (81.5 - 12.7) / (1700 - 12.7)$). This is close to the 6% for the diagnostic model and 4% for the prognostic model that we find. Since this 4.1% is simply a sanity check that the optimised model does a reasonable job of reproducing the data, but is not an independent estimate, we have not added this calculation to the paper.

The slopes for the prognostic model are given relative to the substrate for each pathway (NH₄ for nitrification, NO₃ for denitrification). To allow for an approximate conversion to O₂ specific slopes (i.e. under the simplifying assumption that NH₄ and NO₃ are consumed at the same place where they are produced), we've added to section 2.5 that: “Phytoplankton (and all other organic matter) have a fixed C:N:O₂ ratio of 122:16:-172.” From this it can be calculated that the prognostic model oxic slope of $123 \mu\text{mol N}_2\text{O} (\text{mol NH}_4^+)^{-1}$ approximately converts to $11.5 \mu\text{mol N}_2\text{O} (\text{mol O}_2)^{-1}$. Because reviewer 3 was not entirely clear whether denitrification in the model is actual denitrification using NO₃, we did not add this O₂ based slope in the manuscript, as it would add to the potential confusion.

Minor comments

1. L. 24 “It also currently” a· “It is also currently”

Changed.

2. There are several places in the text, where more detailed or clearer explanations would help readers understand the paper better. For example, l. 53-56 is unclear what the sentence means. Do the authors mean that $\Delta\text{N}_2\text{O}/\text{AOU}$ slope becomes negative under suboxic conditions and that leads to the ambiguity of how much N_2O is produced in this region? Please clarify.

We’ve expanded on the ambiguity to clarify potential reasons for it.

3. L. 71 “observationally derived” a· “observationally-derived”

The Chicago manual of style says not to hyphenate adverbs ending in -ly.

4. L. 75 Since not all readers of this paper are experts in oceanic biogeochemistry, it would be helpful to explain that the f-ratio is the fraction of total primary production by nitrate.

Added.

5. L. 79 What is the “-O₂:C ratio”? What is the dash for?

We’ve added that “(the - sign indicates that O₂ is consumed as CO₂ is produced)”

6. L. 233 “N cycle based” a· “N cycle-based”

Changed to N-cycle-based.

7. L. 242-246 “This estimate...” run-on sentence and needs to be rewritten.

This was split into two sentences.

8. L. 263-267 “It should also...” run-on sentence and needs to be rewritten.

This was rewritten and split into 4 sentences.

9. L. 286 “140 pm” a· “140 ppm”

Changed

10. L. 290-294 “On the one hand...” run-on sentence and needs to be rewritten.

This was split into two sentences.

11. N-cycle data database used in this paper are shown as embargoed in the data source pointed by the authors (<https://www.uea.ac.uk/green-ocean/data>). Will the data be publicly available?

The data have now been made publicly available.

REVIEWER 2:

I strongly support the goal of this paper, to better constrain the oceanic N_2O flux using optimization techniques based on a compilation of datasets of N_2O and related N cycle

variables, combined with process based models. However, the methodology is difficult to follow and it is hard to believe that all 4 data-based approaches converge to basically the same answer and have the same relatively narrow range of uncertainty, which is governed primarily by uncertainty in piston velocity. There is also no overall sense of what sets this paper apart from earlier efforts, since it seems to be based heavily on what is largely the same delta pN₂O data set used before. While I support publication in principle, I think there are many details that should be clarified and explored before this paper is ready for publication.

We thank the reviewer for the comments. We have tried to clarify the methodology throughout the manuscript.

Although four databases were used in our paper, two of these databases, the nitrification rate and the NH₄ concentration, were used to formulate a model that was as realistic as possible. They were not used to calculate the N₂O flux. We were gratified that the two other databases of depth resolved N₂O concentration and surface ΔpN₂O converged on the same answer of a low contribution of N₂O production in the low O₂ region. We have rewritten the end of the introduction to clarify how the four databases are used.

While the literature on N₂O fluxes is growing, the only earlier estimate of global N₂O flux based on ΔpN₂O was by Nevison et al. 1995, 22 years ago, before the MEMENTO database was available. It used interpolation rather than a mechanistic model to obtain fluxes where there are no observations. Therefore our analysis goes beyond existing publications and uses a larger and more complete dataset and process modelling.

Specific comments

L24 Typo: It (is) also currently estimated as the dominant contributor

Corrected.

L32 It's worth mentioning (up front) that this wide range is governed in large part by the possibility of very large coastal and estuarine fluxes. Later on line 87 we learn that the dataset resolution used here is 1x1 degree or 1.1 x 2 degree (plankTOM10.2, line 164), i.e., probably not good enough to resolve these coastal areas.

We have commented on the ambiguity about whether emissions from estuaries are included in oceanic emissions or not in the introduction:

“Part of the uncertainty in the oceanic emissions is whether estuaries are included, which could emit as much as 2.3 - 3.6 Tg N y⁻¹ (Bange et al. 1996).”

We have added a calculation of the contribution of coastal seas, the deep offshore and East equatorial Pacific oceans to N₂O flux in Section 3.2 and the Discussion (Table 2 and associated text).

We have expanded on the information about coastal seas and estuaries at the end of the discussion:

“The largest coastal seas are resolved in our model although the processes related to specific coastal environments are not, such as the interactions with sediments and with tides. Our results do not include emissions from estuaries.”

L43 although there are additional pathways, such as (please give brief list).

We initially wrote it like this because the reference for this statement, Klawonn et al. 2015, measured a large number of N-transformation reactions, so that a list would not be brief. However, to respond to the reviewer's comment that the statement needed more detail, we have replaced it with “, although denitrification may be significant in the anaerobic centres of large marine snow particles in oxic waters”, because that is the most important pathway identified by Klawonn et al.

L72 probably should mention up front that the $\Delta\text{N}_2\text{O}/\text{AOU}$ data are based on MEMENTO. Otherwise, it's a bit confusing to know the basis of this calculation.

This information was moved from the Fig. 3 legend to the main text: "The globally averaged $\Delta\text{N}_2\text{O}/\text{AOU}$ ratio was calculated from the MEMENTO database (Bange et al. 2009) as $81.5 \pm 1.4 \mu\text{mol}/\text{mol}$ (Fig. 3)."

L76 NPP is estimated at $58 \pm 7 \text{ PgC}/\text{yr}$ based on what? An ocean model? Satellite data? Even at the lower end of $51 \text{ PgC}/\text{yr}$, this is on the high side of satellite-based estimates.

This estimate is based on our previously published work (Buitenhuis et al. 2013a). It uses the same methodology as in the present paper. We have added the following text to clarify the origin of the estimate: "based on ^{14}C primary production measurements ($n=50,050$), parameter perturbations of a previous version of the model used here, and Eq. 3". Our estimate is broadly within satellite algorithm estimates, which range from $38\text{-}70.7 \text{ Pg C}/\text{y}$. We have found that the vertically integrated primary production from our model reproduces the observations better than the best satellite algorithm. It also had the second lowest error (root mean square difference) of vertically integrated primary production relative to observations in the Arctic only out of 21 biogeochemical models (Lee et al. 2016 doi:10.1002/2016JC01193). Depth resolved primary production constrains global NPP even better than that at $58 \pm 7 \text{ PgC}/\text{y}$, as discussed in Buitenhuis et al. 2013a.

L83, please list relevant references rather than just saying "(see Introduction)".

We have replaced this by a reference to Fig. 4 (was Fig. 11) which includes all the references.

Line 92-93. Since pN_2O is close to equilibrium in much of the ocean, it seems important to consider the quality of these pN_2O measurements. For example, surface measurements made with underway systems tend to have much higher precision than analyses based on bottle collection. Was the uncertainty comparable across the MEMENTO database and if not, were the differences in data quality accounted for in the subsequent calculations?

Annette Kock (who does the technical support for MEMENTO in the group of H. Bange) informally estimates that more than 95% of the surface pN_2O data entries included in MEMENTO have been measured with underway systems. In addition, comparison experiments between underway and discrete measurements show an overall good agreement between both methods (Arévalo-Martínez et al., 2013, doi: 10.5194/os-9-1071-2013). We have added a caveat to the manuscript: "Since there is at present no formal quality control beyond that performed by individual contributors to the MEMENTO database and a check by the database administrators that the values make physical sense (Kock, A., and Bange, H. W.: Counting the ocean's greenhouse gas emissions, *Eos*, 96, 10-13, 10.1029/2015EO023665, 2015), we have taken the MEMENTO database at face value."

L125 Ocean models often do a poor job of reproducing observed O_2 . Suntharalingam 2012 used WOA O_2 rather than model O_2 for that reason. Presumably, the sensitivity to light, temperature and O_2 described here is based on values from plankTOM10.2 (if not, please clarify). How well does plankTOM10.2 reproduce O_2 relative to observations? (Note: I saw later that my question was addressed in the Results on lines 184-188. That material belongs up front in the methods description.

We have added this information to section 2

"As will be described more fully in Section 3.1, we used observed O_2 concentrations in the simulations (Bianchi et al. 2012) rather than interactively modelled O_2 , to minimise the impact of model biases in simulated O_2 fields (Suntharalingam et al. 2012)."

L132 paragraph starting here. This paragraph could be written more clearly, especially the sentence spanning L137-138. What is a variable N quota? Is the model using Michaelis Menten kinetics?

The paragraph was reworded, and references were added that provide further documentation of the model formulation and the contrast between a quota model and a Michaelis-Menten kinetics model:

“The model uses a fixed C:N:O₂ ratio for all organic matter of 122:16:-172, and Michaelis-Menten kinetics for growth rate based on inorganic N uptake by phytoplankton (Buitenhuis et al. 2013a, supplementary material Eq. 8, 9). We therefore need a K_{1/2} for growth rather than for uptake to be consistent with the fixed C:N ratio (Morel 1987).”

On line 144, a low cost function of 3.3 is better than the cost functions of >4 described for the previous model, correct? Yet, the sentence beginning on L142 with “However” suggests a large uncertainty.

This is indeed confusing (yes, 3.3 is better than >4), and it was rewritten to give a more equal balance between the small scale unexplained variability and the large scale pattern that is well reproduced by the model:

“Due to the highly dynamic nature of NH₄⁺ turnover, the ability of the model to reproduce the observed NH₄⁺ concentrations at the same times and places was by no means perfect, but the large scale pattern of surface NH₄⁺ concentration shows an increase with latitude, consistent with the observations (Fig. 6), which translates into a cost function of 3.0.”

L155-156 What is meant by “The slopes of the three processes” ?

We have changed this from slopes to ratios, and added an explanation at the end of the second paragraph of the introduction:

“Throughout the manuscript we will refer to N₂O stoichiometries relative to O₂, NH₄ and NO₃ as ratios, because they have been optimised against global databases of concentration measurements, rather than from microbiological yields. Using the latter would be more mechanistically satisfying, but the relevant yields are at present insufficiently constrained by observations.”

Section 2.2-2.8. General question. Do the 4 databases described in section 2.2 correspond to the specific sections 2.4-2.7? If so, where does section 2.8 fit in? Is Equation 3 an alternative cost function to Equation 2 described in Section 2.3? The apparent switch from Equation 2 to Equation 3 as the optimization technique is confusing and unclear.

The 4 databases correspond to sections 2.4, 2.5, 3.1 and 3.2. It was split in that way because the nitrification and phytoplankton NH₄ use are necessary model developments before we can implement the prognostic model, but they are not part of the main result of the paper, which is an estimate of the ocean-atmosphere N₂O flux and its confidence interval. The switch between Eq. 2 and 3 is split in the same way. We’ve been using Eq. 2 in multiple previous publications because it gives equal weight to biases in small and large numerical values, and is therefore more appropriate for optimising a global model that spans a range of conditions. We have added this to Section 2.8:

“In previous versions of the PlankTOM model (Buitenhuis et al. 2006, Buitenhuis et al. 2010, Buitenhuis et al. 2013a) we have used Eq. 2 to evaluate the model because it minimises relative error, which we have found to be more appropriate when the observations span several orders of magnitude. Unfortunately, statistical confidence intervals have only been defined for χ^2 -statistics such as Eq. 3 and 4, which minimise absolute error, so that we end up with two cost functions (Eq. 2, 3), depending on the application.”

Line 190 and Figure 6. The model substantially underestimates N₂O in the most important hotspots of production. Doesn’t this mean it will tend to underestimate global N₂O production? It seems like this concern is dismissed somewhat casually with handwaving arguments, e.g., the text starting on line 289.

We have given considerable attention to the underestimation of N₂O at depth in the low O₂ regions, and discuss it from different angles in paragraphs 3, 6 and 7 of the discussion.

We have added Table 2 and a paragraph in Section 3.2 (second paragraph, starting “High N₂O fluxes”), that analyses the contribution of N₂O hotspots to global N₂O flux.

We have rewritten paragraph 3 (starting with ‘This lack of knowledge’) of the discussion to more explicitly present the balance of evidence whether or not the underestimate of N₂O concentrations at 500-1000m depth (Fig. 7) influences N₂O flux at the surface. On balance, including the new Table 2, our analysis still suggests a small global significance of the hotspots. This conclusion was also reached by Freing et al. (2012), and we added a reference to this: “Freing et al. (2012) also estimated a small fraction of 7% of the global total contributed by denitrification/low O₂ N₂O production.”

Line 201-202 Please clarify how these results link together. Line 201 says that both hypoxic production AND CONSUMPTION were optimized. The subsequent results mention GROSS production of 0.33 TgN/yr, then optimized N₂O production of 0.12 or 0.16 TgN/yr. Are the latter results net production? Can we infer that about 0.17- 0.21TgN/yr is consumed in suboxic zones?

Yes the results are for net production and we have added the word net to clarify this. Yes, the optimised consumption is 0.21 Tg N/y. We have also added clarifications throughout the manuscript on which processes occur in suboxic, hypoxic and oxic waters.

Line 202-203 Total production of 0.12-0.33 TgN y⁻¹ in low O₂ is only about 10% on average of total production. This is much lower than the 33% suggested by Suntharalingam et al. 2012. Does this mean that the authors are concluding that the OMZs are only responsible for a small fraction of global N₂O production? Please expand on this point and call it out more explicitly in the Discussion.

We are not confident that the lower attribution to denitrification produced by our current model version is better than published by Suntharalingam et al 2012. This is detailed in the Discussion, to which we’ve added references:

“Both the diagnostic and the prognostic models assign a small percentage of the total N₂O production to the denitrification pathway, 6 and 4% respectively. However, because of the large bias between the observed and modeled N₂O concentration depth profiles (Fig. 6) these may be underestimates (Suntharalingam et al. 2012, Arevalo-Martinez et al. 2015).”

We have revised the text to discuss the possible implications of this shortcoming, which we argue do not significantly affect our results for the total global N₂O flux. See our reply to the comment above on Line 190 and Figure 6, that outlines changes we made to Section 3.2 and paragraph 3 of the Discussion to more clearly present the balance of evidence.

Line 204 perhaps add a clause clarifying that the .0017 molN₂O/molO₂ slope is about 20 times the mean deltaN₂O/AOU ratio of 8.15e-5 from line 82.

The .0017 slope is the gross production slope in the low O₂ regions. The 8.15e-5 slope is the net slope averaged over the whole ocean. It is therefore to be expected that the former is larger than the latter. See changes made in response to the next two comments.

Line 205 production for the prognostic model is given in units of umol N₂O (mol NO₃)-1. Does this represent NO₃- consumed by denitrification, or produced by nitrification? Can you provide an estimate of how this relates to the previous units of mol N₂O/mol O₂?

We have added clarifications on which slopes apply to denitrification and to suboxic, hypoxic and oxic waters. Since NO₃- consumption and O₂ consumption are spatially separated, stating a N₂O/O₂ slope would be confusing, but we have added the model N:O₂ ratio in Section 2.5, so that the magnitudes can be placed in context.

Line 216 Please use consistent N₂O (mol O₂)-1 slope units. Here the units are umol/mol. On line 78 they were nmol/mol. On line 204, they were mol/mol.

All slopes have been converted to a denominator in mol, and a numerator in μmol, or in mmol if it was >1000 μmol.

Line 217 How does this nitrification slope in units of $\mu\text{molN}_2\text{O}/\text{molNH}_4^+$ relate to the “ N_2O production slope” on line 206 in units of $\text{mol N}_2\text{O}/\text{mol NO}_3^-$?

We have added clarifications on which slopes apply to denitrification and to suboxic, hypoxic and oxic waters.

Line 219-220 Are all measurements really of $\Delta\text{pN}_2\text{O}$, or are most of pN_2O in the surface ocean? In the latter case, what is the uncertainty in $\text{pN}_2\text{O}_{\text{atm}}$, e.g., from Eq 1?

We have added in Section 2.2 that:

“The average absolute difference relative to the global average $\text{pN}_2\text{O}_{\text{atm}}$ data from the NOAA/ESRL Global Monitoring Division (ftp://ftp.cmdl.noaa.gov/hats/n2o/combined/HATS_global_N2O.txt) is 0.5 ppb between 1977 and 2014 and 0.3 ppb between 2000 and 2014.” See also the reply to the comment by reviewer 1 on equation 1, in response to which we ran the optimisation using the NOAA/ESRL data, and got essentially the same results.

Line 220 On what basis was this 1978 estimate made? Is there updated information that could be used?

It is cited in Cohen and Gordon 1978 as a personal communication from Weiss, who calculated the solubility we used based on published data. No further details are given, but because it’s an order of magnitude less than the uncertainty in the piston velocity, this doesn’t strike us as a problem. We are not aware of more recent measurements. The Sarmiento and Gruber textbook (2006, Ocean biogeochemical dynamics, ISBN: 9781400849079) also gives the solubility we used as the most up to date one.

Line 233 Typo or confusing sentence.

Based on the comments of reviewer 1, we hyphenated “N-cycle-based”.

Line 248-250. It would be good to provide references to support these claims.

We have added references to the C-cycle data, and refer to the figures with observational data for the N-cycle data.

Line 282 – paragraph starting here. This exercise, combined with large data gaps in Figure 9a, including in both the ETSP and ETNP, suggest to me that the authors are overstating the degree of certainty in their confidence interval. There are large areas of the ocean with no data, including in the most important hotspots for N_2O production.

The observations are in fact fairly evenly spread (Table 2). There are observations in the ETSP and ETNP. The observations include upwelling regions. The analysis we present of a hypothetical undersampling of high values suggests that constraining the piston velocity would narrow the confidence interval more than making more pN_2O measurements. As mentioned in response to the reviewer’s comment on L32, we have added an analysis of N_2O flux in coastal seas, the deep offshore and East equatorial Pacific oceans to quantify the contribution of these hotspots.

Line 303-304. This is the first mention of the fact that the model produces low fluxes from the Southern Ocean. Can you cite the relevant figure here and call attention to this point earlier in the Results section? (Figure 9b,c,d all seem to indicate a substantial flux from the Southern Ocean.)

It is the atmospheric inversions that produce low fluxes in the Southern Ocean, rather than the process models presented here. We have rewritten these sentences to make this clearer:

“However, N_2O emissions from inversions in the Southern Ocean are lower than the priors (Hirsch06, Huang08, Thompson14, Saikawa14). These low Southern Ocean emissions ($0.02 - 0.72 \text{ Tg N y}^{-1}$) are consistent with our results ($0.68 - 0.79 \text{ Tg N y}^{-1}$). South of 30°S , 88% of

the Earth surface is ocean, resulting in a clearer attribution in the inversions of the atmospheric N₂O anomalies to ocean fluxes. We suggest that the higher emissions estimates from inversions could be due to a combination of overestimated priors of ocean fluxes in combination with insufficient observational constraints at latitudes North of 30S to allow correct partitioning between land and ocean fluxes.”

Line 308-310. The neglect of estuaries is indeed a key uncertainty, which needs to be mentioned much earlier, i.e., in the Introduction. It is also debatable whether coastal areas are adequately represented in the models presented here, which 2x1 or 1x1 resolution.

See reply to question on L32.

L487 Figure 2. This figure suggests very high f-ratios, e.g., of 0.8-0.9 in the northern subtropical gyres, that are a little hard to believe. The global mean looks to be on the order of 0.4! Are these generally accepted values or are they biased by measurements in highly productive coastal waters?

This one point of 0.8 is the average of 2 measurements (0.8 ± 0.1) made at 14N21W and 21N21W, about 4° West of Africa (Varela et al. 2005). In the Discussion we point out (first paragraph) that the f-ratio (global mean = 0.29 ± 0.18) is the largest contributor to the uncertainty in N₂O production we estimate from the N-cycle-budget. We also explicitly state that further (synthesis of) observations would help constrain this uncertainty. We think that trying to ensure a representative mean by weighting some values more (e.g. open ocean measurements) would be too subjective / sensitive to the exact methodology used.

L505, “Model results are for the same months and longitudes as the observations.” What about latitudes?

We have added the clarification to the panel D legend:

“Latitude y-axis to the left of panel A.”

L527 This plot is dominated by the error bars and somewhat obscures the focus on the mean value, which arguably is the more important quantity. The current study makes a much more detailed effort to quantify uncertainty than most of the previous studies (some of which make no effort at all). Could a separate panel with a narrower Y-axis range be plotted to better compare the mean value of the fluxes? And can you please provide some discussion of the main factors contributing to the differences in mean value?

Error bars are important when comparing different estimates. We have decreased the aspect ratio of the figure to 1, so that differences along the y-axis become easier to read.

We have added a discussion of the two main factors contributing to the different N₂O flux in Nevison95:

“Because of differences in methodology it is not possible to provide reasons for why our estimate is lower than the more recent estimates. We can, however, compare our estimate to that of (Nevison95), because it is also based on a database of ΔpN_2O . Compared to their high end estimate using the piston velocity of Wanninkhof of 5.2 ± 3.6 Tg N y⁻¹, our estimate is lower because we use the more recent 13% lower estimate of piston velocity of (Sweeney et al. 2007), and because our ΔpN_2O of 7.6 ± 18.1 ppb is 25 - 28% lower compared to 10.55 natm in Nevison (1995) (the range is calculated based on the water vapor correction for conversion between ppb and natm, which increases from 0.6 - 4.1% at temperatures from 0 - 30 °C, which brings the values slightly closer together)”

Gianna Battaglia:

Thanks for this contribution to global marine N₂O modeling. May I ask some questions regarding the model formulation and applied parameter sampling:

Line 148: Is there nitrification at 1 $\mu\text{molO}_2/\text{l}$?

Almost none in our analysis. Nitrification declines in the same way with O₂ as remineralisation switches from O₂ to NO₃. We added: “Since nitrification consumes O₂, in the model it decreases as remineralisation switches from O₂ to NO₃ (supplementary material Eq. 70, 61, 67).”

Line 156: How is N₂O consumption modeled? As a first order consumption term as applied in other studies? How large is gross consumption? What O₂ threshold do you use to separate nitrification, production from denitrification and consumption from denitrification? How large are aerobic and anaerobic remineralization fluxes in the model?

We added to Section 2.6:

“The ratios of the three processes are globally invariant (supplementary material Eq. 70, 61, 63, 71). The functional form of the O₂ dependence of N₂O consumption (suppl. Eq. 71) was the same as that of denitrification (suppl. Eq. 67), and with an O₂ response function that is 1.5 μmol L⁻¹ lower than that of denitrification, which is similar to that used by Babbin et al. (2015). We independently optimised the ratios of N₂O production and consumption from denitrification (Section 3.1), which controls the net N₂O production as a function of O₂ concentration. There is not enough information at present to optimise the O₂ concentration parameters of denitrification and N₂O consumption as well.”

We have added the full set of equations for nitrous oxide to the model description as supplementary material, with references to the relevant equations throughout the Materials and Methods section. Optimised gross consumption is 0.21 Tg N/y, see the answer to reviewer 2 question on Line 201-202. The O₂ thresholds for N₂O production (34 μmol O₂ L⁻¹) and consumption (28 μmol O₂ L⁻¹) are stated in Section 3.1, the O₂ threshold for nitrification is 0 μmol O₂ L⁻¹ (see previous comment). Primary production is 64.5 Pg C/y, of which 99.5% is remineralised aerobically (using 7540 Tmol O₂/y) and 0.008% is remineralised by denitrification (using 0.485 Tmol NO₃/y). The rest is partitioned between removal of nutrients at the sediment to compensate for nutrients added by rivers (da Cunha et al. 2007, GBC) and changes in the inventory of total organic matter.

Line 166: Are modeled N₂O concentrations not drifting substantially after such a spin

The length of the spin-up is a trade-off between keeping the runs short enough that the nutrient distributions are close to observed ones, so that the model behaves realistically when it is formulated and parameterised using physiological and ecological observations (Buitenhuis et al. 2006 Global Biogeochemical Cycles, 2010 Global Biogeochemical Cycles, 2013a, Le Quere et al. 2016), and long enough that the N₂O concentration and ΔpN₂O distributions can be used to optimised N₂O process rates. Our optimized model is by definition as close as possible to observations, even if the deep ocean is not fully at equilibrium. With this method we were able to conduct a large number of model experiments, a sub-ensemble of which are presented here. We note in Section 3.1 that N₂O production below 1600 m, where there is an increase in concentration, is only 5% of the total production. Given the slow ventilation of the deep sea, this accumulation will have a negligible effect on the optimised flux, and keeping the simulation short actually helps with this. We have added an analysis of the effect of variability to Section 3.1 and corresponding text as follows: “The results were the same in both diagnostic and prognostic submodels for the 2000-2004 and 2005-2009 averages, showing that the model was sufficiently spun up.”

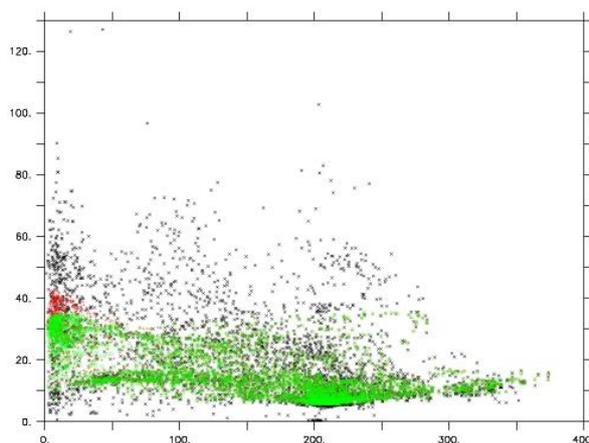
Line 199: How many parameter perturbation simulations did you run? Which sampling technique is applied to vary parameters? Over which range are parameters varied? What does the legend in Fig 8/10 stand for? Could you illustrate the sampled slopes and resulting optimal slope? Are fluxes tied

stoichiometrically to remineralization fluxes? Why is N2O consumption slope given as N2O/NO3-? Does this make sense stoichiometrically?

We did a large number of parameter perturbations, 6 of which were used to constrain the low O2 N2O production in the diagnostic model (Fig. 9A), 23 to constrain the low O2 N2O production in the prognostic model (Fig. 9B), 27 to constrain total N2O flux in the diagnostic model (Fig. 11A) and 26 to constrain total N2O flux in the prognostic model (Fig. 11B). Parameters were varied until they constrained the optimised rates and their confidence intervals. We've added to the Fig. 9 legend that "each point represents a simulation with a different low O2 slope". We clarified the text following Eq. 2 : "To calculate the cost function (and also to calculate RSS in Eq. 3), the model was regridded to the same grid as the observations, and residuals were calculated at months and places where there are observations." We added to the Fig. 9 legend: "Range of parameter values is given in the supplementary material Section 8.7." Based on the question of reviewer 3 about Eq. 3 we have clarified the legend of Fig. 9 (was Fig. 8). Section 8.7 of the supplementary material also gives the optimal slopes, which are also given in Sections 3.1 and 3.2. N2O consumption occurs because N2O is consumed during denitrification. This was added in Section 3.1. NO3 is the substrate of denitrification, and N2O is an intermediary, so it does make stoichiometric sense that N2O can act as an alternate substrate for denitrification.

Figure 6: Many global N2O modeling studies present N2O versus O2 scatter plots for evaluation. What does this relationship look like in the model? The N2O flux estimate of 2.4+/-0.8 Tg N yr-1 is much lower than what was reported in Suntharalingam et al. 2000/2012, on which the model builds ('4.6 Tg N yr-1 (comprised of 3.0 Tg N yr-1 from the 'nitrification' pathway, and 1.6 Tg N yr1 from the low-oxygen pathway', Suntharalingam et al. 2012). How come? Does your prior include these previous fluxes? Your N2O production at low O2 is now ~10 times smaller compared to this previous model.

We present the modelled N2O and observed N2O next to each other in Fig. 7. Since this shows N2O as a function of depth for different basins, this has a higher information content than a scatter plot.



x-axis O2(μmol L-1), y-axis N2O(nmol L-1), black observations, green diagnostic model, red prognostic model.

The observational O2 are used in the model, so this plot does not add any information relative to Fig. 7, and we have not included it in the manuscript.

We have added a discussion of the two main factors contributing to the different N2O flux in Nevison95:

"Because of differences in methodology it is not possible to provide reasons for why our estimate is lower than the more recent estimates. We can, however, compare our estimate

to that of (Nevison95), because it is also based on a database of ΔpN_2O . Compared to their high end estimate using the piston velocity of Wanninkhof of $5.2 \pm 3.6 \text{ Tg N y}^{-1}$, our estimate is lower because we use the more recent 13% lower estimate of piston velocity of (Sweeney07), and because our ΔpN_2O of $7.6 \pm 18.1 \text{ ppb}$ is 25 - 28% lower compared to 10.55 natm in Nevison (1995) (the range is calculate based on the water vapor correction for conversion between ppb and natm, which increases from 0.6 - 4.1% at temperatures from 0 - 30 °C, which brings the values slightly closer together)”

This is the only estimate where the methodologies are comparable enough (based on an observational database of ΔpN_2O , and using a piston velocity that is a function of the square of the windspeed) that we can isolate quantitative reasons for the differences in the estimates.

This is not an inversion, so there's no prior.

REVIEWER 3:

The manuscript by Buitenhuis and Coauthors describes the results of simulations with an ocean biogeochemical model that includes different parameterizations of N_2O production, constrained with available N_2O observations. The main finding is a net N_2O outgassing to the atmosphere of $2.4 \pm 0.8 \text{ TgN/year}$, which is substantially lower than many of the estimates previously reported, and also less uncertain. A very small proportion of the N_2O production comes from denitrification-associated pathways in suboxic waters. The estimate also appears robust to the choice of the parameterization of N_2O production.

This is a short and potentially useful paper, although not particularly original. But I think that, if better supported, the results will push other scientists to reconsider estimates of N_2O emissions from the ocean (as well as from other sources) in light of the low values suggested. That said, I also think the paper is poorly written, in particular when it comes to the description of the methods employed - for example the model equations, the rational and choices behind the parameterizations, the steps behind the optimization. Furthermore, I have some additional concerns about the results that prevent me from fully supporting publication of the manuscript as is.

We thank the reviewer for the comments. We have tried to clarify the methodology throughout the manuscript.

Specific comments:

- The model formulation is quite hard to follow, partly because equations are not show. This makes it difficult at times to judge the validity of the model's assumption. I strongly encourage the Authors to show all the pertinent equations, either in the main text, or in an appendix.

We have added the full set of equations for nitrous oxide to the model description as supplementary material. This has all the equations, parameter values, and how it is set up. We have also made multiple clarifications in the text following the reviewer's comments. Please see point-by-point responses below (and in response to the other reviewers).

- The choice of some of the model equations and parameterization is unclear and could be better justified. The Authors could do a much better job explaining why certain functional forms have been utilized, and what consequences these choices may have, if any. For example, looking at Table 1, line 3 lists an equation that uses the logarithm of O_2 . Is there any reason for this form? The logarithm will expand the range at very low O_2 concentration - do we trust O_2 measurements there? Further, this form breaks down at $O_2=0$; does this ever happen in the model/observations, and is there any limit applied to prevent it? Finally, all of these equation should represent a process ultimately limited by O_2 . Is there any limitation as O_2 goes to zero?

On the specific justification for the use of logarithm of O₂, the choice is due to a better fit to the data. We now explained this in the text:

“A logarithmic function fit the data better than linear, exponential, or power functions.”

We have also added an explanation why the N₂O consumption equation and parameters were used:

“The functional form of the O₂ dependence of N₂O consumption (suppl. Eq. 71) was the same as that of denitrification (suppl. Eq. 67), and with an O₂ response function that is 1.5 μmol L⁻¹ lower than that of denitrification, which is similar to that used by Babbin et al. (2015). We independently optimised the ratios of N₂O production and consumption from denitrification (Section 3.1), which controls the net N₂O production as a function of O₂ concentration. There is not enough information at present to optimise the O₂ concentration parameters of denitrification and N₂O consumption as well.”

The choice of model equations for the preferential algal uptake are justified in Vallina and Le Quéré (2008).

The lowest O₂ concentration in the Bianchi et al. 2012 database (after regridding onto the model grid) is 1.15 μmol O₂/L. The lowest concentration for which there is a yield measurement is 5.4 μmol O₂/L. It is therefore true that the logarithm extrapolates the N₂O/AOU ratio from 232 μmol/mol at 5.4 μmol O₂ to 251 μmol/mol at 1.15 μmol O₂. Given the variability in the measurements this is an insignificant extrapolation beyond the range of the measurements. Also, nitrification rate decreases with O₂, so that the N₂O production rate is low.

- I found the distinction between the prognostic and diagnostic model (for N₂O) somewhat confusing. In both models N₂O is carried as a prognostic tracer - except in the first model it does not depend on other N-cycle tracers, and is not consumed, but only produced and passively advected until it outgassed from the surface. What makes one model diagnostic and another prognostic?

In this manuscript we use the distinction between diagnostic and prognostic model to mean that the former is based on statistical relationships with observations, while the later is based on process understanding and representation. The N₂O field from models are indeed transported in the same way. We clarified this in Section 2.6 as follows:

“N₂O production is implemented as two distinct submodels. The diagnostic submodel is based on statistical relationships of DeltaN₂O/AOU ratios taken from observations and has previously been published {Suntharalingam00,Suntharalingam12}.”,

“The prognostic submodel presented here is based on process understanding and explicitly represents the primary N₂O formation and consumption pathways associated with the marine nitrogen cycle (Fig. 1).”

and “The N₂O concentrations from both the diagnostic and the prognostic model are transported in the same way by physical transport and the formulation of their gas exchange is also identical.”

- Regarding the prognostic model - the Authors say that it explicitly represent the redox transformations that lead to the conversion of NH₄⁺ to eventually N₂O (actually only a subset, as for example, the model does not include NO₂-), but the model seems to still parameterize them heavily. For example the current understanding is that N₂O is an obligate intermediary during heterotrophic denitrification, so that one should expect a gross N₂O production comparable to the denitrification rate (i.e. ~70 Tg N/year)

However, the Authors indicate a suboxic gross production of only 0.33 Tg N year – a very small rate in comparison. This may be explained by the use of “slopes” in the prognostic model that relates N₂O to other tracers (more on these slopes in the next comment). This implicitly assumes a tight coupling between production and consumption at suboxic levels, with only a fraction of the N cycled by denitrification escaping to the water column. It may be fine as a parameterization - especially

since it is one that is optimized against observations. However it may be problematic if the model is to be used under varying circulation or climate - the coupling between production and consumption may vary, and given the large gross N₂O fluxes this may impact net production and accumulation of N₂O.

The model only represents the process of denitrification, it does not represent a state variable for denitrifiers (first sentence of Section 2.4). Therefore, reactions that happen intracellularly in denitrifiers are not represented either, and gross production from denitrification represents N₂O production that is exuded/leaks into the surrounding seawater and stays there long enough to leave a measured increase in N₂O concentration. The small net production rate is a result of the optimisation against observations, there is no implicit assumption built into the model that production and consumption should be tightly coupled. We don't present climate change simulations here, so we cannot comment on whether using the present model for climate change projections would be more or less problematic than using any of the other available models.

- It is unclear what "slopes" are used in the prognostic model. Are these slopes actual yields (e.g. N₂O production per NH₄⁺ oxidized), relationships with O₂ consumed, or just empirical relationships based on data syntheses? And what is then the slope of the third step of N₂O cycling (consumption of N₂O by denitrification)? Is it a relationship with O₂, with NH₄⁺ or with NO₃⁻? (and specifically, is there explicit denitrification in the model, so that one could relate N₂O production to NO₃⁻ deficit?).

We have changed slopes to ratios, and explained our reasoning in using the word ratios rather than yields at the end of the second paragraph of the introduction:

"Throughout the manuscript we will refer to N₂O stoichiometries relative to O₂, NH₄ and NO₃ as ratios, because they have been optimised against global databases of concentration measurements, rather than from microbiological yields. Using the latter would be more mechanistically satisfying, but the relevant yields are at present insufficiently constrained by observations."

Yes, denitrification is explicitly represented, as stated in Section 2.4. N₂O consumption is therefore proportional to NO₃⁻ consumption, as stated in Section 3.1. Yes, it would be possible to calculate a NO₃⁻ deficit, such as N*. We judged this to be outside the scope of the paper, because denitrification can be accompanied by both N₂O production and consumption, so model validation of denitrification rate against observations of N* would not help constrain the N₂O budget. We added supplementary material to this paper which contains a detailed description of the biogeochemistry model equations (taken from Le Quere et al. 2016, and now updated with a description of both N₂O submodels (section 6.5 and 6.6).

- The lack of spinup in the model is worrisome: the model was apparently initialized in 1965 and run for 49 years through 2014. This is a short running time, and it completely misses a spinup phase. It may very well be the case that the N₂O inventory of the ocean over the last 5 years is still adjusting from the initial condition, in a way that could bias the outgassing estimates. For example, there seems to be a substantial accumulation of N₂O in the deep ocean - if this is still ongoing after 49 years, then the outgassing estimated by the Authors could be a lower estimate. A comparison between the total net production in the interior and the outgassing could give a sense of any disequilibrium. Note that a similar modeling study by Martinez Rey et al., 2013, BGS (incidentally finding about 4Tg/year emissions) suggested a 150-year spinup was not enough to eliminate drifts in N₂O and other biogeochemical variables. Any drift should be discussed in the paper, and the consequences assessed.

We have added an analysis of the optimised N₂O flux for the 2000-2004 and 2005-2009 periods, which show the same result. We note in Section 3.1 that N₂O production below 1600 m, where there is an increase in concentration, is only 5% of the total production. Given the slow ventilation of the deep sea, this accumulation will have a negligible effect on the optimised flux, and keeping the simulation short actually helps with this. The frequency distribution of ΔpN₂O in the submodels

closely matches that in the observations (Fig. 12), which supports the conclusion from the small error attributed to the model-observation ΔpN_2O mismatch, that the model does not have a major bias.

Martinez-Rey et al. do climate change simulations, and spin up the model so that they don't have to include control simulations and present the climate impacts relative to the control. Our study is different, where we initialise from the available observations and optimize model parameters using the available observations to derive the present day oceanic N_2O flux. See also our reply to the comment of Gianna Battaglia on Line 166.

- I found the description of the optimization steps very unclear. It took me a while to figure out what steps the Author follow and how the model is actually compared to the data, and I'm still not sure about them. Now my understanding is that a first optimization is carried out for the NH_4 -cycle using nitrification rates and NH_4^+ concentrations; then a second optimization is performed with interior N_2O data to determine parameters for low- O_2 pathways (but does this apply to both the prognostic and diagnostic model?); and finally a third optimization (presumably with some parameters fixed by the previous steps?) using surface ΔpN_2O data for the global source terms, used to determine the final air-sea fluxes. That's my understanding but I am still not sure I got it right, and some aspects remain puzzling. I think this could be much better explained from the start, for example by a method section outlining the optimization strategy in more detail.

We do carry out 3 optimisations, but we split the presentation into two parts, one where we develop the model so that we can implement the prognostic model, and the other where we use the model to optimise the model to the two N_2O datasets. We do not include NH_4 concentration database in the optimisation because the high turnover rates and the many processes that are involved would make this a process that would require a whole paper by itself, which is outside the scope of the present paper. Fortunately, the many processes turn out to be reasonably well constrained by observations we present in this and previous papers (Buitenhuis et al. 2006, 2010), so that we judge the resulting NH_4 concentration distribution to be fit for the purpose of optimising the N_2O cycle which we undertake here. We have more explicitly described the progressive steps of how we use each observational dataset at the end of the introduction, from model development of the N-cycle in Section 2 to identifying N_2O rates that best fit the observations in Section 3. See also the reply to the first comment of reviewer 2. We have clarified the legends of Fig. 9 and 11, see reply to reviewer 1 comment on Eq. 3. See also the reply to reviewer 2 on Section 2.2-2.8.

- Related to the previous comment, the equations for the optimization are absolutely opaque and unclear. They need to be substantially clarified: ideally anyone should be able to apply them after reading the paper, which is not the case. For example equation (1) is not very specific: instead of "average", "model", "observations" the actual mathematical form could be given - this would also help knowing how the average was done, whether the in situ or gridded data were used, how the model was sampled etc.

We have changed the mathematical form of Eq. 3 and 6 to replace average by the sum divided by the number of observations. We added Eq. 6 to give the actual mathematical form of the model and observation data used. We have added that the model was converted to the same grid as the observations, and sampled where there are observations in Section 2.3. See clarification added in response to Gianna Battaglia's comment on Line 199.

Similarly I am completely at loss with section 2.8, and I could not trace back the steps applied by the Authors based on this description alone. How is RSS/RRS_{min} (equation 3) used, how does it relate to the quantities shown in Fig. 8 and 10, and why does it only contain the number of observations but no information on the actual variables?

We explained how Eq. 5 (was Eq. 3) relates to Fig. 9 and 11 (was Fig. 8 and 10) in the legends of these figures: " MSE_{min} was obtained as the minimum of a second order polynomial fit (black lines).

The 1σ confidence interval, where MSE equals the value calculated from Eq. 5, is indicated by the horizontal lines.” We have added Eq. 6 to show how the actual variables (observations and model results) are included in the calculation of MSE ($=RSS/n$).

What does the “phi” term (equation 4) represent, and how is it actually used?

Because the paper we discussed only tested sample sizes that were more than 2 orders of magnitude smaller than our database, we decided to delete this equation and text.

- Regarding the final estimate of N₂O air-sea flux, I think it could be couched much better into the context of previous estimates (also, a table would help), and what could be behind the potential discrepancies in light of the substantially lower revision. This could be especially interesting given that many modeling studies use a similar approach. The Authors also present an “observational” estimate of N₂O production whose central value (4.6 TgN/year) is quite different than the final model estimate - this discrepancy could be added to the discussion. I am not particularly surprised by the lack of sensitivity of N₂O production to the choice of diagnostic and prognostic models, since both are optimized versus observations. Surface pN₂O should be a quite powerful constraint to outgassing fluxes. However, one may still expect different sensitivities to interannual variability and climate change, so this is not a strong argument in favor of not resolving complex pathways that characterize the low-O₂ N₂O cycle.

We present the context of previous estimates in Fig. 4. We have added a discussion of the discrepancy with the Nevison et al. 1995 estimate using Wanninkhof piston velocity in the 4th paragraph of the discussion (paragraph starting “Despite these shortcomings”). Because the methods of other previous estimates are different, we can’t give specific reasons why our results are different from the other estimates. The observational estimate in Section 2.1 is similar to (NOT quite different from) the combined model-observation estimate: the confidence interval of that estimate completely overlaps our better constrained estimate in Section 3.2. We have added this to the discussion:

“This estimate of global marine N₂O production derived from analyzing the N cycle is statistically indistinguishable from the N₂O flux derived from ΔpN_2O observations, but has a much larger error.”

We note that our estimate of the optimised N₂O flux is sensitive to the observational dataset used, but not to the details of the model. Since our model parameters are optimised using a database spanning multiple years, and not on a year to year basis, we note that this model specification is more suited to estimating long-term or climatological fluxes, and not interannual variability.

- The model is biased in its representation of export and remineralization, as well as N₂O distribution. The discussion of the effect of these biases (e.g. lines 289-300) is not especially thorough - so the conclusion, in particular regarding the narrower range of the new estimate, is not very convincing. Furthermore, there are hidden resolution biases. For example, the model can not resolve low-O₂ coastal upwelling regions, which have been shown to be powerful conduits to N₂O outgassing (e.g. Arevalo Martinez et al., 2015, Nature Geosciences). The abstract/conclusions could be more cautious with respect to the real uncertainties.

We have rewritten the discussion of the bias due to the too deep remineralisation, to more explicitly present the balance of evidence whether or not the underestimate of N₂O concentrations at 500-1000m depth (Fig. 7) influences N₂O flux at the surface:

“it should also be noted, first, that the optimization using surface ΔpN_2O agrees with the optimization using N₂O concentration that the contribution of the low O₂ N₂O production needs to be low (Fig. 11). Second, the error contribution from the model vs. observed ΔpN_2O comparison is low, with confidence intervals of 0.3 Tg N y⁻¹ for both submodels. Third, ΔpN_2O is equally well modelled above the low O₂ regions as in the rest of the ocean (Fig. 10, 12), and the contribution of the coastal and deep offshore ocean are nearly

proportional to their surface areas (Table 2). These three features are supporting evidence for our results that suggest that the low O₂ regions make a small contribution to the global ocean N₂O production. They should be balanced against the model bias of the vertical distribution of N₂O concentrations, which suggests a larger contribution from the low O₂ regions. Freing et al. (2012) also estimated a small fraction of 7% of the global total contributed by denitrification / low O₂ N₂O production.”

We have added a calculation of the contribution of coastal seas, the deep offshore and East equatorial Pacific oceans to N₂O flux in Section 3.2 and the Discussion (Table 2 and associated text). And we have expanded on the information about coastal seas and estuaries at the end of the discussion:

“The largest coastal seas are resolved in our model although the processes related to specific coastal environments are not, such as the interactions with sediments and with tides. Our results do not include emissions from estuaries.”

- Line 43: The reference to Klawonn et al., 2015 is missing.

The reference was added.

- Line 95, equation 2: More information should be given on this equation, and how it was used in the model/observation comparison. Does using this equation mean that the N₂O flux is calculated for a specific period, or that it varies in time? This is unclear.

We have clarified that the model/observations comparison is done at places and months where there are observations. See reply to Gianna Battaglia’s comment on Line 199.

Also, there number of significant digits in the various coefficients is way larger than any believable uncertainty associated with the measurements the equations should fit.

We reduced the number of significant digits in Eq. 1. See reply to the same comment on Eq. 1 by reviewer 1.

- Section 2.4, Table 1. Maybe some effort can be done to evaluate the improvements associated with each model: by adding terms the cost function decreases minimally - is the improvement significant? Does it justify the increase in the model degrees of freedom?

We have used model representations that have relatively few parameters (=degrees of freedom), because the observational data that has been synthesised on a global scale cannot constrain more parameters. Because the prognostic model is an explicit part of the model N-cycle processes, the representations of which are independently constrained by additional observations, it actually has one parameter less (4) than the diagnostic model (5). Akaike’s Information Criterion (a criterion that quantifies whether models with more degrees of freedom are “justified” by their increased predictive power $AIC=1/(n_{\text{observations}}-n_{\text{parameters}})*\log(RSS)+2n_{\text{parameters}}$) of the prognostic submodel is 5.9 lower than the diagnostic submodel. This is in the range (2-10) where there is more support for the prognostic model, but there is still some support for the diagnostic model (Burnham, K.P., and D. R. Anderson (1998) Model selection and inference, a practical information-theoretic approach. Springer).

- Line 133-134. The equation could be shown.

We have added: “(Eq. 9 in the supplementary material)” and have also added references to the other relevant equations in the supplementary material in the rest of the Materials and Methods.

- Section 2.6. The slopes (of what, with respect to what?) and relationships used for the model should be clarified with equations, and maybe with corresponding figures (e.g. the observational constraints used). Also, what is the range from which the various slopes were drawn in order to run the different model versions for the optimization?

How were they determined? What values were actually used? Finally, there must be concentration thresholds associated to the transitions between different slopes (e.g. O₂). How were these thresholds determined? Were they also optimized for?

The equations, optimised ratios, and range of values tested are given in the supplementary material, we have added references to the relevant equations in Sections 2.4 – 2.6.

- Line 211-212. The reasoning is unclear: an increase in outgassing for a given atmospheric concentration should be driven by a parallel increase in surface concentrations, since the flux is proportional to the concentration (or pN₂O) difference. For example, in the limit of removing the saturation N₂O concentration, a doubling of the interior production of N₂O should double both the outgassing and the surface concentration.

No, a doubling of production leads to a doubling of ΔpN_2O , but $\Delta pN_2O/pN_2O$ is small in most of the surface ocean, and the surface concentration increase is proportional to pN₂O, not ΔpN_2O , so we are correct in stating that a doubling in production leads to only a small increase in surface N₂O concentration. We have added this clarification to the manuscript.

- Lines 242-247. This entire paragraph is very unclear, please clarify.

We have clarified this paragraph:

“further observational constraints could not only reduce the error, but also further our understanding of the whole N cycle, including the option of evaluating their model representation against observations, and not just the part that N₂O plays in them. Such further constraints are also likely to provide the most productive way to reduce unexplained variability that is found in the observations but not in the present models. E.g., we have shown that both the N₂O and NO₃ are underestimated at ~300 - 1500 m depth and overestimated below ~2000 m (Fig. 6, 7). Thus, improved representation of mesopelagic remineralisation might lead in improved representation of the N₂O depth distribution. However, this falls outside the scope of this study.”

- Lines 270-271. Constraining remineralization backwards from N₂O production seems a bit far-fetched, given how hard it is to even constrain processes like denitrification alone.

Our point is that the current lack of constraints is not cast in stone. Addressing questions concerning the nitrogen cycle from different angles and integrating the different sources of information in a falsifiable model is more robust than constraining it from the more usual angles of export and nutrient concentrations alone. We added to the end of this paragraph: “Although there are relatively few N₂O concentration observations, nitrification and denitrification respond to specific environmental queues (in particular O₂ concentration), so that they could contribute a relatively large observational constraint over the full range of environmental conditions.”

- Lines 279-281. Please clarify.

See reply to question about Eq. 4 above: Because the paper we discussed only tested sample sizes that were more than 2 orders of magnitude smaller than our database, we decided to delete this paragraph from the discussion.

- Lines 294-297. The issue of biases in model circulation could be assessed by using ventilation tracers, e.g. CFCs. Are they available for this mode?

We are currently including CFCs in our model but this will require time for the development, tuning and validation. The results will not be available for the current study but will inform follow up developments.

- Line 308: do the Authors really think their model can capture coastal N₂O dynamic, and the massive air-sea fluxes observed there (see Arevalo Martinez et al., 2015), especially in eastern boundary upwellings?

We have added separate analysis of the main N₂O hotspots: coastal seas, deep offshore, and East equatorial Pacific oceans. This analysis shows that our two submodels are able to reproduce the observations (see in particular the close correspondence between both submodels and the observations in the high end tail in Fig. 12). Arevalo-Martinez et al. (2015) use the mean N₂O flux to represent the whole Peruvian upwelling region. This is similar to linear interpolation with correlation length-scales of the whole region and the whole year. Since their plots suggest that the N₂O fluxes are not linearly distributed, this could lead to overestimation of the N₂O flux. Therefore we believe our mechanistic model is much more likely to capture realistic N₂O dynamics, including in the hotspots, than previously published estimates. For further details see replies to reviewer 2's questions on L32 and L282.