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A mechanistic model of an upper bound on oceanic carbon export as a function of mixed layer depth and temperature

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Abstract

Export production reflects the amount of organic matter transferred from the surface ocean to depth through biological processes. This export is in great part controlled by nutrient and light availability, which are conditioned by mixed layer depth (MLD). In this study, building on Sverdrup's critical depth hypothesis, we derive a mechanistic model of an upper bound on carbon export based on the metabolic balance between photosynthesis and respiration as a function of MLD and temperature. We find that the upper bound is a positively skewed bell-shaped function of MLD. Specifically, the upper bound increases with deepening mixed layers down to a critical depth, beyond which a long tail of decreasing carbon export is associated with increasing heterotrophic activity and decreasing light availability. We also show that in cold regions the upper bound on carbon export decreases with increasing temperature when mixed layers are deep, but increases with temperature when mixed layers are shallow. A metaanalysis shows that our model envelopes field estimates of carbon export from the mixed layer. When compared to satellite export production estimates, our model indicates that export production in some regions of the Southern Ocean, most particularly the Subantarctic Zone, is likely limited by light for a significant portion of the growing season.

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1. Introduction

Photosynthesis in excess of respiration at the ocean surface leads to the production of organic matter, part of which is transported to the deep ocean through sinking and mixing [*Volk and Hoffert*, 1985]. This biological process, known as export production (aka soft tissue biological carbon pump) lowers carbon dioxide (CO_2) concentrations at the ocean surface and facilitates the flux of CO_2 from the atmosphere into the ocean.

Export production is a function of net community production (NCP) which is defined as the balance between net primary production (NPP) and heterotrophic respiration (HR), or the difference between gross primary production (GPP) and community respiration (CR; HR plus autotrophic respiration (AR)) (the acronyms used in this study are presented in Table 1):

$$CO_2 + H_2O \xrightarrow[\underbrace{\overrightarrow{NCP}\;\;\overleftarrow{HR}}_{NPP}\;\;\overleftarrow{AR}]{\overrightarrow{GPP}} Organic\ matter + O_2 \qquad (1)$$

$$Export\ production = NCP - MLD \times \frac{d(POC + DOC)}{dt} \qquad (2)$$

where POC, DOC and MLD represent particulate organic carbon, dissolved organic carbon and mixed layer depth, respectively. If the organic carbon inventory (POC+DOC) in the mixed layer is at steady state, NCP is equal to export production (equation (2)). Without allochthonous sources of organic matter, if the organic matter inventory in the mixed layer decreases, NCP will be predicted to be transiently smaller than export production. Conversely, export may lag NPP [*Henson et al.*, 2015; *Stange et al.*, 2017], in which case NCP is expected to be greater than export production.

We define the upper bound on carbon export (NCP^*) from the mixed layer as the maximum export achievable should all limiting factors other than light (e.g., nutrients) be alleviated. Light availability exponentially decays with depth due to absorption by water and its constituents. The

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mixing of phytoplankton to depth therefore impacts phytoplankton physiology and productivity [*Cullen and Lewis*, 1988; *Lewis et al.*, 1984], with the depth-integrated NPP expected to increase down to the euphotic depth. Respiration, on the other hand, is often modeled to be some function of organic matter concentration, which is expected to be constant with depth if homogenously mixed within the mixed layer. Temperature is also believed to be an important control on carbon export because respiration is more temperature-sensitive than photosynthesis [*Laws et al.*, 2000; *Lopez-Urrutia et al.*, 2006; *Rivkin and Legendre*, 2001]. Field observations confirm that NCP is generally lower at high temperatures and consistently low when mixed layers are deep. These patterns have been attributed to the balance between depth-integrated photosynthesis and respiration as a function of MLD and temperature [*Cassar et al.*, 2011; *Eveleth et al.*, 2016; *Huang et al.*, 2012; *Shadwick et al.*, 2015; *Tortell et al.*, 2015]. However, descriptions of the underlying mechanisms heretofore remain qualitative.

In his seminal paper, Sverdrup presented an elegant model to demonstrate that vernal phytoplankton blooms (i.e., organic matter accumulation at the ocean surface) may be driven by increased light availability when the MLD shoals above a critical depth (Z_c) [*Sverdrup*, 1953]. In our study, we build upon *Sverdrup* [1953] and derive a mechanistic model of an upper bound on carbon export with respect to MLD, temperature, photosynthetically active radiation (PAR), phytoplankton maximum growth rate (μ_{max}), and heterotrophic activity. We compare our NCP^* model to observations, and use this model in conjunction with satellite export production estimates to identify regions in the world's oceans where light may limit export production.

2. Model description and comparison to observations

2.1. Net community production and light availability

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A conceptual representation of the metabolic balance between volumetric NCP, NPP, and HR profiles is presented in Figure 1(A). According to equation (1), the volumetric NCP flux at a given depth (z) in the mixed layer results from the difference between volumetric NPP and HR:

$$NCP(z) = NPP(z) - HR(z) \qquad (3)$$

where z increases with depth. $NPP(z)$ is a function of the autotroph's intrinsic growth rate (μ) times their biomass concentration (C). Assuming that the effect of nutrients and light on photosynthetic rates abides by Michaelis-Menten kinetics, and neglecting the effect of photoinhibition [*Dutkiewicz et al.*, 2001; *Huisman and Weissing*, 1994], $NPP(z)$ may be expressed as follows:

$$NPP(z) = \mu(z) \times C = \frac{N}{N + k_m^N} \times \frac{I(z)}{I(z) + k_m^I} \times \mu_{max} \times C \qquad (4)$$

where μ_{max} is the maximum intrinsic growth rate of the autotrophic community; N and k_m^N represent the nutrient concentration and half-saturation constant, respectively; and I and k_m^I represent the irradiance level and half-saturation constant, respectively. μ_{max}, N, k_m^N, k_m^I and C are assumed to be well mixed within the mixed layer. The first two terms on the right-hand side of equation (4) account for the effect of nutrient and light availability on autotrophic growth rates, and they are hereafter defined as follows for simplicity:

$$N_m = \frac{N}{N + k_m^N} \qquad (5a)$$

$$I_m(z) = \frac{I(z)}{I(z) + k_m^I} \qquad (5b)$$

$I(z)$ is modeled as an exponential decay of PAR just beneath the water surface (I_0):

$$I(z) = I_0 \times e^{-K_I \times z} \qquad (6)$$

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where K_I is diffusion attenuation coefficient which is assumed to be independent of depth in the mixed layer.

As a first approximation, we assume that $HR(z)$ is proportional to C as in previous studies [*Dutkiewicz et al.*, 2001; *Huisman and Weissing*, 1994; *Rivkin and Legendre*, 2001; *Sverdrup*, 1953; *White et al.*, 1991]:

$$HR(z) = r_{HR} \times C \quad (7)$$

where r_{HR} represents the intrinsic heterotrophic respiration rate which is assumed to be dependent on temperature (see below), and independent of depth. In reality, $HR(z)$ is likely best modeled as a function of the concentration of labile organic matter — an additional term could be included to account for the relationship of total labile organic matter to C.

NCP integrated over the mixed layer ($NCP(0, MLD)$) can be derived from equations (3-7):

$$\begin{aligned} NCP(0, MLD) &= NPP(0, MLD) - HR(0, MLD) \\ &= \int_0^{MLD} NPP(z)dz - \int_0^{MLD} HR(z)dz \\ &= N_m \times I_m(0, MLD) \times \mu_{max} \times C - r_{HR} \times MLD \times C \end{aligned} \quad (8)$$

The first term on the right side of equation (8) represents NPP integrated over the mixed layer ($NPP(0, MLD)$), which is equivalent to the product of $\int_0^{MLD} \mu(z)dz$ and C, where the former term is modeled to be a function of μ_{max} conditioned by nutrient and light availability within the mixed layer. $I_m(0, MLD)$ can be derived as follows:

$$I_m(0, MLD) = \int_0^{MLD} I_m(z)dz = -\frac{1}{K_I} \times ln\left(\frac{I_0 \times e^{-K_I \times MLD} + k_m^I}{I_0 + k_m^I}\right) \quad (9)$$

NCP integrated over the mixed layer (equation (8)) is a bell-shaped function of MLD as depicted in the schematic diagram of Figure 1(B).

2.2. Net community production and phytoplankton biomass concentration

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As can be seen from equation (8), $NCP(0, MLD)$ is a direct function of C because $NPP(0, MLD)$ and $HR(0, MLD)$ are proportional to C. $NCP(0, MLD)$ is also an indirect function of C due its effect on light attenuation (i.e., K_I). The attenuation coefficient K_I can be divided into water and non-water components ($K_I = K_I^w + K_I^{nw}$) [*Baker and Smith*, 1982; *Smith and Baker*, 1978a; b], where K_I^{nw} is controlled by the concentrations of phytoplankton, colored dissolved organic matter (CDOM), and non-algal particles (NAP). In the open ocean where CDOM and NAP co-vary with phytoplankton [*Morel and Prieur*, 1977], K_I can be related to C as follows:

$$K_I = K_I^w + k_c \times C \quad (10)$$

where k_c is a function of the solar zenith angle, the specific absorption and backscattering coefficients of phytoplankton, and the relationship between phytoplankton, CDOM, and NAP.

To calculate how $NCP(0, MLD)$ varies as a function of C, we examine its first ($\frac{dNCP(0,MLD)}{dC}$) and second ($\frac{d^2NCP(0,MLD)}{dC^2}$) derivatives with respect to C based on equations (8) and (10):

$$\frac{dNCP(0, MLD)}{dC} = N_m \times \mu_{max} \times \frac{K_I^w \times I_m(0, MLD) + k_c \times C \times MLD \times I_m(MLD)}{K_I^w + k_c \times C} - r_{HR} \times MLD \quad (11)$$

$$\frac{d^2NCP(0, MLD)}{dC^2} = N_m \times k_c \times \frac{\mu_{max}}{K_I} \times \left\{ \frac{2 \times K_I^w}{K_I} \times \left(MLD \times I_m(MLD) - I_m(0, MLD) \right) - \frac{k_c \times C \times I_m(MLD)^2 \times MLD^2 \times k_m^I}{I_0 \times e^{-K_I \times MLD}} \right\} \quad (12)$$

when $MLD > 0$, $I_m(0, MLD) > MLD \times I_m(MLD)$:

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$$I_m(0,MLD) = \int_0^{MLD} \frac{I_0 \times e^{-K_I \times z}}{I_0 \times e^{-K_I \times z} + k_m^I} dz$$

$$> \int_0^{MLD} \frac{I_0 \times e^{-K_I \times MLD}}{I_0 \times e^{-K_I \times MLD} + k_m^I} dz = MLD \times I_m(MLD) \qquad (13)$$

The detailed derivation of equations (11-12) can be found in the supplementary material. Substituting the inequality (13) into equation (12) gives $\frac{d^2NPP(0,MLD)}{dC^2} < 0$, which suggests that $\frac{dNCP(0,MLD)}{dC}$ decreases with increasing C reaching an asymptote of $\lim_{C\to\infty}\left(\frac{dNCP(0,MLD)}{dC}\right) = -r_{HR} \times MLD < 0$ (Figure 2(B)). Additionally, because $NCP(0,MLD)$ must be nil when there is no autotrophic biomass ($NCP(0,MLD)|_{C=0} = 0$), $\lim_{C\to 0}\left(\frac{dNCP(0,MLD)}{dC}\right)$ must be larger than 0, otherwise the ecosystem would be net heterotrophic which is unachievable without an allochthonous source of organic matter. $\lim_{C\to 0}\left(\frac{dNCP(0,MLD)}{dC}\right) > 0$ and $\lim_{C\to\infty}\left(\frac{dNCP(0,MLD)}{dC}\right) = -r_{HR} \times MLD < 0$ suggest the existence of $\frac{dNCP(0,MLD)}{dC}\Big|_{C=C^*} = 0$ where C^* corresponds to an autotrophic biomass concentration which maximizes $NCP(0,MLD)$ (i.e., NCP^*).

The dependence of $NCP(0,MLD)$ on C can be conceptually understood in the following way. Given a water column with sufficient nutrients, the critical depth Z_c and compensation depth Z_p are expected to shoal as C increases. When C is low, $NCP(0,MLD)$ increases with C because of its greater impact on $NPP(0,MLD)$ than on $HR(0,MLD)$. As C further increases, the increase in $NPP(0,MLD)$ with C slows because of light attenuation (i.e., K_I). There is therefore a C^* which maximizes the difference between $NPP(0,MLD)$ and $HR(0,MLD)$ leading to NCP^* (Figure 2). Beyond this point (C^*), further increasing C will cause self-shading and limit photosynthesis in the deep part of the mixed layer, as a result decreasing $NCP(0,MLD)$. Beyond a critical biomass

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(C_c), the ecosystem becomes net heterotrophic. Without an allochtonous source of organic carbon, this is only transiently sustainable.

2.3. Mixed layer depth and compensation depth

By definition, if $NCP(MLD)$ is smaller than 0 (i.e., net heterotrophy at the bottom of the mixed layer), the MLD must be deeper than Z_p ($MLD > Z_p$) (and vice versa). To determine the sign of $NCP(MLD)$, we substitute inequality (13) into equation (11). According to the inequality presented in equation (13), $\frac{K_I^W \times I_m(0,MLD) + k_c \times C \times MLD \times I_m(MLD)}{K_I^W + k_c \times C}$ in equation (11) must be larger than $\frac{K_I^W \times MLD \times I_m(MLD) + k_c \times C \times MLD \times I_m(MLD)}{K_I^W + k_c \times C}$ (which is equal to $MLD \times I_m(MLD)$). After simple rearrangements, the substitution of inequality (13) into equation (11) leads to:

$$\frac{dNCP(0,MLD)}{dC}$$

$$> MLD \times (N_m \times I_m(MLD) \times \mu_{max} - r_{HR}) = \frac{MLD}{C} \times NCP(MLD) \qquad (14)$$

The inequality in equation (14) in turn suggests that when $NCP(0,MLD)$ is maximized ($\frac{dNCP(0,MLD)}{dC} = 0$), $NCP(MLD)$ is negative (net heterotrophic) and hence the MLD is deeper than Z_p ($MLD > Z_p$). This counterintuitive result is attributable both to the uneven distribution of light availability in the water column (equation (13)) and to water which absorbs light but does not contribute to biomass accumulation. When the mixed layer is at the Z_p, a slight increase in C will leads to negative $NCP(MLD)$ due to decreasing light availability at the base of mixed layer, but will increase NCP higher in the water column because of the increase in biomass. The increase in NCP in the shallow parts of the mixed layer therefore overcompensates for the net heterotrophy at the bottom of the mixed layer, thus maximizing the depth-integrated NCP. If light were uniformly distributed in the water column (i.e., $I_m(0,MLD) = MLD \times I_m(MLD)$) and

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148 if water did not attenuate light ($K_I^w = 0$ in equation (11)), $MLD = Z_p$ would maximize
149 $NCP(0, MLD)$, which is consistent with *Huisman and Weissing* [1994].

150 **2.4. An upper bound on carbon export**

151 Equations (11-13) delineate the conditions for an upper bound on carbon export (NCP^*). In
152 order to simplify the relationship of NCP^* to MLD and temperature, we approximate
153 $I_m(0, MLD)$:

$$I_m(0, MLD) = -\frac{1}{K_I} \times ln\left(1 + \frac{I_0}{I_0 + k_m^I} \times (e^{-K_I \times MLD} - 1)\right)$$

$$\approx I_m(0) \times \frac{1 - e^{-K_I \times MLD}}{K_I}$$

$$\approx I_m(0) \times \frac{1}{K_I} \qquad (15)$$

154 where $I_m(0) = \frac{I_0}{I_0 + k_m^I}$. Based on equation (15), $NCP(0, MLD)$ in equation (8) can be
155 approximated as:

$$NCP(0, MLD) = C \times MLD \times \left(\frac{1}{K_I \times MLD} \times \mu^* - r_{HR}\right) \qquad (16)$$

156 where $\mu^* = I_m(0) \times N_m \times \mu_{max}$.

157 We first need to derive the C^* which maximizes $NCP(0, MLD)$ (i.e., NCP^*) in equation (16).
158 C^* can be solved from the first derivative of $NCP(0, MLD)$ in equation (16) with respect to C:

$$\left.\frac{dNCP(0, MLD)}{dC}\right|_{NCP(0,MLD)=NCP^*} = \mu^* \times \frac{K_I^w}{(k_c \times C^* + K_I^w)^2} - MLD \times r_{HR} = 0 \qquad (17)$$

159

160 and therefore:

161 $$C^* = \frac{1}{k_c} \times \left[-K_I^w + \sqrt{\frac{\mu^* \times K_I^w}{MLD \times r_{HR}}}\right] \qquad (18)$$

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Equation (18) decreases with MLD. As C^* is positive ($C^* \geq 0$) and cannot go to infinity ($C^* \leq C^*_{max}$), MLD should satisfy $MLD_{C^*_{max}} \leq MLD \leq \frac{\mu^*}{r_{HR} \times K_I^W}$, where $MLD_{C^*_{max}}$ represents the MLD corresponding to the maximum achievable autotroph's biomass concentration (C^*_{max}) in the surface ocean. Substituting C^* from equation (18) into equation (16):

$$\sqrt{NCP^*} = a_2 \times \sqrt{I_m(0)} + a_1 \times \sqrt{MLD} \qquad (19)$$

where $a_1 = -\sqrt{\frac{K_I^W \times r_{HR}}{k_c}}$ and $a_2 = \sqrt{\frac{N_m \times \mu_{max}}{k_c}}$. Constants a_1 and a_2 are functions of r_{HR} and μ_{max}, respectively, which are generally modeled to increase with temperature (T) [*Eppley*, 1972; *Rivkin and Legendre*, 2001]:

$$\mu_{max} \propto e^{P_t \times T} \qquad (20a)$$

$$r_{HR} \propto e^{B_t \times T} \qquad (20b)$$

where P_t and B_t are constants. P_t is commonly assumed to equal 0.0663 [*Eppley*, 1972]. Substituting equations (20a) and (20b) into equation (19) yields:

$$\sqrt{NCP^*} = a_4 \times \sqrt{e^{P_t \times T}} \times \sqrt{I_m(0)} + a_3 \times \sqrt{e^{B_t \times T}} \times \sqrt{MLD} \qquad (21)$$

where $a_3 = -\sqrt{\frac{K_I^W}{k_c}}$ and $a_4 = \sqrt{\frac{N_m}{k_c}}$. The NCP^* model for $0 \leq MLD < MLD_{C^*_{max}}$ is not discussed here, because we do not have data with very shallow MLD to constrain and evaluate the model. The derivation of the model can be found in the supplementary material.

2.5. Comparison to observations

2.5.1 Data products

We assess the performance of our modeled upper bound on carbon export using a global dataset of MLD, PAR, sea surface temperature (SST), O_2/Ar-derived NCP, and export production derived from sediment traps and ^{234}Th (see supplementary material). MLD was

derived from global Argo profiles (Global Ocean Data Assimilation Experiment; http://www.usgodae.org/) and CTD casts (National Oceanographic Data Center; https://www.nodc.noaa.gov/). PAR was downloaded from the NASA ocean color website (https://oceancolor.gsfc.nasa.gov/). The NCP estimates are based on a compilation of O_2/Ar measurements from *Li and Cassar* [2016], *Li et al.* [2016], *Shadwick et al.* [2015], and *Martin et al.* [2013]. The POC export production estimates were obtained from the recently compiled dataset of *Mouw et al.* [2016]. These estimates were adjusted to reflect a flux at the base of mixed layer using the Martin curve of organic carbon attenuation with depth [*Martin et al.*, 1987]. The constants k_c and K_I^w in equation (10) were derived assuming a carbon to chlorophyll *a* ratio of 90 [*Arrigo et al.*, 2008] and an empirical linear relationship between K_I and chlorophyll *a* concentration (see Figure S3), calculated based on the NOMAD dataset [*Werdell and Bailey*, 2005]. k_m^I was set at 4.1 Einstein m^{-2} d^{-1} following *Behrenfeld and Falkowski* [1997]. In our estimation of the upper bound on carbon export, we set N_m to 1 in the NCP^*calculations.

2.5.2 Results and discussion

Overall, we find that NCP^* calculated using published parameters [*Laws et al.*, 2000] does a good job of enveloping carbon export observations reported in the literature (Figure 3(A)). Samples on the NCP^* envelope (upper bound) are likely regulated by light availability. Conversely, points below the upper bound may be nutrient or in some cases light limited. As expected, NCP^* increases with μ^* and decreases with r_{HR}. Model parameters $a_1 = -1.80$ and $a_2 = 21.38$ (equation (19)) provide the best fit to the O_2/Ar-NCP and MLD estimates. When accounting for the effect of T on μ^* and r_{HR}, model constants $a_3 = -1.66$ and $a_4 = 20.40$ (equation (21)) best fit the O_2/Ar-NCP, SST and MLD observations.

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Our results show that NCP^* decreases faster with increasing MLD in warmer waters (Figure 3(B)), because the term $a_3 \times \sqrt{e^{B_t \times T}}$ in equation (21) is negative and negatively correlated to T. This temperature effect contributes to part of the relationship between export production and MLD in Figure 3(A). Interestingly, NCP^* increases with T in colder waters and shallow mixed layers. This is because NCP^* reflects the balance between productivity ($a_4 \times \sqrt{e^{P_t \times T}} \times \sqrt{I_m(0)}$) and heterotrophic respiration ($a_3 \times \sqrt{e^{B_t \times T}} \times \sqrt{MLD}$). In a shallow cold mixed layer, the change in productivity with T ($\frac{d\left(a_4 \times \sqrt{e^{P_t \times T}} \times \sqrt{I_m(0)}\right)}{dT} = \frac{P_t}{2} \times a_4 \times \sqrt{e^{P_t \times T}} \times \sqrt{I_m(0)}$) is greater than that of heterotrophic respiration ($\frac{d\left(a_3 \times \sqrt{e^{B_t \times T}} \times \sqrt{MLD}\right)}{dT} = \frac{B_t}{2} \times a_3 \times \sqrt{e^{B_t \times T}} \times \sqrt{MLD}$). These results could explain part of the variability in the relationship between NCP and SST reported in previous studies [*Li and Cassar*, 2016]. Our NCP^* model does not perform as well in warmer deep mixed layers, where high variability in export ratio maxima have also been reported [*Cael and Follows*, 2016]. This may stem from uncertainties in observations, the differing relationship between T, μ^*, and r_{HR} at high temperature, and/or violations of our assumptions (see caveats and limitations).

Several recent studies have explored the relationship of NCP to oceanic parameters based on various statistical approaches [*Cassar et al.*, 2015; *Chang et al.*, 2014; *Huang et al.*, 2012; *Li and Cassar*, 2016; *Li et al.*, 2016]. Our model can shed some light into the mechanisms driving some of these patterns. To that end, we substitute equation (15) into equation (8):

$$NCP(0, MLD) = C \times MLD \times \left(\frac{1 - e^{-K_I \times MLD}}{K_I \times MLD} \times \mu^* - r_{HR}\right) \qquad (22)$$

Rearranging equation (22):

$$NCP_B = \frac{NCP(0, MLD)}{C \times MLD} = \frac{1}{I_0 + k_m^I} \times N_m \times \mu_{max} \times PAR_{ML} - r_{HR} \qquad (23)$$

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where NCP_B is the biomass-normalized volumetric NCP, PAR_{ML} is the average PAR in the mixed layer ($PAR_{ML} = \frac{1-e^{-K_I \times MLD}}{K_I \times MLD} \times I_0$), and $\frac{1}{I_0 + k_m^I} \times N_m \times \mu_{max}$ and $-r_{HR}$ correspond to the slope and offset, respectively. The scatter in the relationship between chlorophyll-normalized volumetric NCP and PAR_{ML}, as reported in previous studies [*Bender et al.*, 2016], can likely be explained by the effect of temperature and the availability of nutrient and light (among other properties) on the slope and offset of equation (23). Equation (22) can also be reorganized to assess how environmental conditions may impact the export ratio (ef):

$$ef = \frac{NCP(0, MLD)}{NPP(0, MLD)} = 1 - \frac{K_I \times MLD}{1 - e^{-K_I \times MLD}} \times \frac{1}{N_m} \times \frac{1}{I_m(0)} \times \frac{r_{HR}}{\mu_{max}} \qquad (24)$$

where $\frac{r_{HR}}{\mu_{max}}$ is proportional to $e^{(B_t - P_t) \times T}$. Equation (24) is consistent with multiple studies which predict decreasing ef with increasing temperature [*Cael and Follows*, 2016; *Dunne et al.*, 2005; *Henson et al.*, 2011; *Laws et al.*, 2000; *Li and Cassar*, 2016]. In fact, equation (5) of *Cael and Follows* [2016] can easily be derived from equation (24) (see supplementary material). Equation (24) also highlights that a multitude of factors may confound the dependence of ef on temperature (including varying MLD, light attenuation, and availability of nutrient and light). This again may explain some of the conflicting observations recently reported in the literature (e.g., *Maiti et al.* [2013]), where the effect of temperature may be masked by changes in community composition [*Britten et al.*, 2017; *Henson et al.*, 2015]. One therefore needs to account or correct for the multitude of confounding factors when predicting the effect of a given environmental condition (e.g., temperature, mineral ballast, and NPP) on the export ratio.

3. Spatial distribution of the upper bound on carbon export

We estimate the global distribution of the upper bound of carbon export using equation (19) and climatological monthly MLD and PAR. In general, NCP^* is high in low latitudes and low in

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241 the North Atlantic and Antarctic Circumpolar Current (ACC) in the Southern Ocean (Figure
242 4(A)). As expected, this spatial pattern is controlled by MLD (see Figure S1). Satellite-derived
243 estimates of NCP [*Li and Cassar*, 2016] are approximately 10% of global NCP^* , reflecting the
244 high degree of nutrient limitation in the oceans. We also derive a global NCP^* map using
245 equation (21), and find that the global NCP^* estimate is very sensitive to the temperature
246 dependence of r_{HR}. For example, decreasing the B_t in $r_{HR} \propto e^{B_t \times T}$ from 0.11 to 0.08 (as used in
247 *Rivkin and Legendre* [2001] and *Lopez-Urrutia et al.* [2006]) increases the global NCP^* budget
248 from 87 to 322 Pg C yr^{-1}. Large differences in NCP^* in low-latitudes in great part explain this
249 change. In light of the large uncertainties in the relationship between r_{HR} and T [*Cael and*
250 *Follows*, 2016; *Lopez-Urrutia et al.*, 2006], we hereafter only discuss NCP^* estimates derived
251 from equation (19).

252 To estimate how close export production is to its upper bound, we calculate the ratio of
253 export production to NCP^* (f_{pt}). Low f_{pt} regimes represent ecosystems likely regulated by
254 nutrient availability (i.e., ecosystems that have not reached their full export potential based on
255 MLD). As expected, low latitude and subtropical regions have low f_{pt} (Figure 4(B)). High f_{pt}
256 regimes represent ecosystems which have reached their full light potential, and are therefore less
257 likely to respond to nutrient addition because of light limitation (e.g., North Atlantic and ACC
258 (Figure 4(B))). In these regions, especially the subantarctic region, f_{pt} is high in the spring
259 (Figure 4(C)) and decreases in the summer (Figure 4(D)), suggesting that export production is
260 likely co-limited by nutrient and light availability. This may in part explain the lower response to
261 iron fertilization in the subantarctic region where substantial increases in surface chlorophyll
262 were only observed in regions with shallower mixed layers [*Boyd et al.*, 2007; *Boyd et al.*, 2000;
263 *de Baar et al.*, 2005].

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Also shown in Figure 4 are the biological pump efficiency and export ratio ef (panels 4E and 4F, respectively). These various proxies reflect different components of the biological pump. Whereas f_{pt} reflects the export potential based on current MLD and light availability, the biological pump efficiency reflects the potential as derived from nutrient distribution in the oceans, estimated from the extent of nutrient removal from the surface ocean [*Sarmiento and Gruber*, 2006] or the proportion of regenerated nutrients at depth [*Ito and Follows*, 2005]. A revised estimate of the global biological pump efficiency, estimated based on the proportion of regenerated to total nutrients (preformed + regenerated) at depth is around 30-35% [*Duteil et al.*, 2013]. The ef ratio on the other hand describes how much of production is exported as opposed to recycled in the surface [*Dunne et al.*, 2005]. The ultra-oligotrophic subtropical waters have a low export ratio, a strong biological pump efficiency with exhaustion of nutrients at the ocean surface, and therefore have not reached their full light potential (low f_{pt}). The seasonal pattern of f_{pt} in the subantarctic region suggests that the low biological pump efficiency is the result of light limitation in the austral spring and nutrient (likely Fe) and light limitation in the austral summer.

4. Caveats and limitations

A multitude of uncertainties, simplifications, and approximations in our model and field observations may explain some of the discrepancies between the predicted and observed NCP^*. Among others:

- Phytoplankton biomass concentration (C) may vary with depth in the mixed layer, especially for water columns experiencing varying degrees of turbulent mixing. In addition, MLD is not always the best proxy of light availability with mixing layer in

some cases deviating from the mixed layer [*Franks*, 2015; *Huisman et al.*, 1999]. The factors defining the MLD also vary in different oceanic regions.

- For simplicity, we model the dependence of photosynthesis on irradiance assuming Michaelis-Menten kinetics, which does not account for photoinhibition. More accurate models can be found in other studies [*Platt et al.*, 1980]. Due to optional absorption, K_I also varies with depth in the mixed layer. Additionally, the linear relationship between K_I and C is influenced by CDOM, NAP, and other environmental factors (e.g., solar zenith angle) [*Gordon*, 1989].
- μ_{max} and r_{HR} are influenced by environmental factors other than temperature, including community structure.
- NCP may underestimate export production when accompanied by a decrease in the inventory of organic matter in the mixed layer (see introduction and equation (2)).
- Our field observations are limited, mostly focusing on the spring and summer seasons, and harbor significant uncertainties. Descriptions of these uncertainties are presented in other studies [*Bender et al.*, 2011; *Cassar et al.*, 2014; *Jonsson et al.*, 2013].
- Finally, our study is only relevant to the mixed layer. It does not account for productivity below the mixed layer, which can be important in some regions such as the subtropical ocean.

5. Conclusions

In this study, we derived a mechanistic model of an upper bound on carbon export (NCP^*) based on the metabolic balance between photosynthesis and respiration of the plankton community. The upper bound is a positively skewed bell-shaped function of mixed layer depth (MLD). At low temperatures, the upper bound decreases with temperature if mixed layers are deep, but

309 increases with temperature if mixed layers are shallow. We used this model to derive a global
310 distribution of an upper bound on carbon export as a function of MLD, which shows high values
311 in low latitudes and low values in high latitudes due to deep MLD. To examine how current
312 export production compares to this upper bound in the world's oceans, we calculated the ratio of
313 satellite export production estimates to the upper bound derived by our model. High ratios of
314 export production to NCP^* in the North Atlantic and ACC indicate that export production in
315 these regions is likely co-limited by nutrient and light availability. Overall, our results may
316 explain differences in carbon export measured during past iron fertilization experiments (e.g.,
317 subantarctic and polar regions), inform future iron fertilization experiments, and help in the
318 development of remotely-sensed carbon export models.

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454 **Table 1**. Model symbols, abbreviations, and units

Symbol	Description	Units
MLD	Mixed layer depth	m
$MLD_{C^*_{max}}$	Maximum MLD corresponds to maximum achievable autotroph's biomass concentration	m
z	Depth	m
Z_c	Critical depth	m
Z_p	Compensation depth	m
GPP(0,z)	Gross primary production	mmol C m^{-2} d^{-1}
NPP(z)	Net primary production at depth z	mmol C m^{-3} d^{-1}
NPP(0,z)	Net primary production above depth z	mmol C m^{-2} d^{-1}
NCP(z)	Net community production at depth z	mmol C m^{-3} d^{-1}
NCP(0,z)	Net community production above depth z	mmol C m^{-2} d^{-1}
HR(z)	Heterotrophic respiration at depth z	mmol C m^{-3} d^{-1}
HR(0,z)	Heterotrophic respiration above depth z	mmol C m^{-2} d^{-1}
NCP^*	The maximum NCP for a given MLD (upper bound on carbon export)	mmol C m^{-2} d^{-1}
NCP_B	NCP normalized to autotroph's biomass inventory in the mixed layer	d^{-1}
ef	Export ratio	unitless
f_{pt}	Ratio of satellite export production estimates to the upper bound on carbon export	unitless
N	Nutrient concentration	mmol m^{-3}
k_m^N	Half-saturation constant for nutrient concentration	mmol m^{-3}
N_m	Nutrient effect on phytoplankton grow $N_m = \frac{N}{N+k_m^N}$	unitless
PAR	Photosynthetically active radiation	Einstein m^{-2} d^{-1}
I_0	Photosynthetically active radiation just beneath water surface	Einstein m^{-2} d^{-1}
$I(z)$	Photosynthetically active radiation at depth z	Einstein m^{-2} d^{-1}
k_m^I	Half-saturation constant for irradiance	Einstein m^{-2} d^{-1}
$I_m(z)$	Light effect on phytoplankton grow at depth z, $I_m(z) = \frac{I(z)}{I(z)+k_m^I} = \frac{I_0 \times e^{-K_I \times z}}{I_0 \times e^{-K_I \times z}+k_m^I}$	unitless
$I_m(0,z)$	Integrated light effect on phytoplankton grow above depth z, $I_m(0,z) = -\frac{1}{K_I} \times ln\left(\frac{I_0 \times e^{-K_I \times z}+k_m^I}{I_0+k_m^I}\right)$	unitless
PAR_{ML}	Average PAR in the mixed layer ($PAR_{ML} = \frac{1-e^{-K_I \times MLD}}{K_I \times MLD} \times I_0$)	Einstein m^{-2} d^{-1}
μ	Phytoplankton growth rate	d^{-1}
μ_{max}	Maximum phytoplankton growth rate	d^{-1}
r_{HR}	Heterotrophic respiration ratio	d^{-1}
K_I	Diffusion attenuation coefficient ($K_I = K_I^W +$	m^{-1}

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	K_l^{nw})	
K_l^w	Diffusion attenuation coefficient due to water	m^{-1}
K_l^{nw}	Diffusion attenuation coefficient due to optically active components	m^{-1}
k_c	Specific attenuation coefficient for irradiance	m^2 $mmol^{-1}$
C	Phytoplankton biomass concentration	mmol m^{-3}
C^*	Phytoplankton biomass concentration that maximizes NCP	mmol m^{-3}
C_{max}^*	Maximum achievable autotroph's biomass concentration	mmol m^{-3}
POC	Particulate organic carbon	mmol m^{-3}
DOC	Dissolved organic carbon	mmol m^{-3}
CDOM	Colored dissolved organic matter	m^{-1}
NAP	Non-algal particles	mmol m^{-3}
T	Temperature	°C
P_t	Temperature dependence for phytoplankton grow rate	$°C^{-1}$
B_t	Temperature dependence for heterotrophic respiration ratio	$°C^{-1}$
CO_2	Carbon dioxide	ppmv

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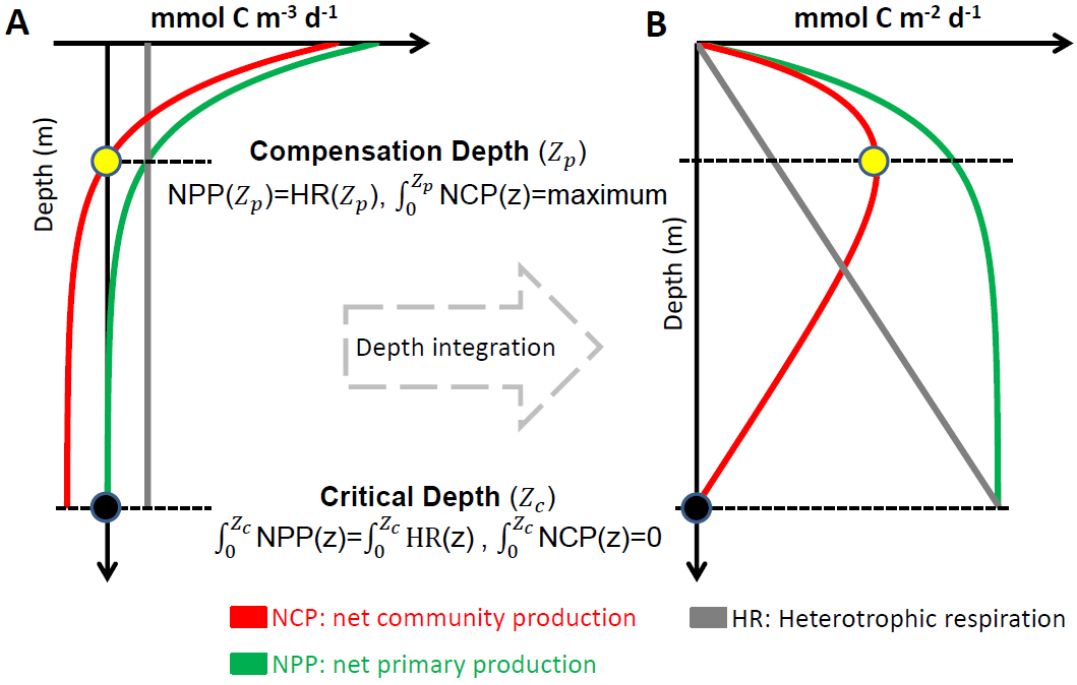

Figure 1. Schematic diagram of depth-profiles of net community production (NCP), net primary production (NPP), and heterotrophic respiration (HR). Yellow and black dots represent the compensation and critical depths, respectively.

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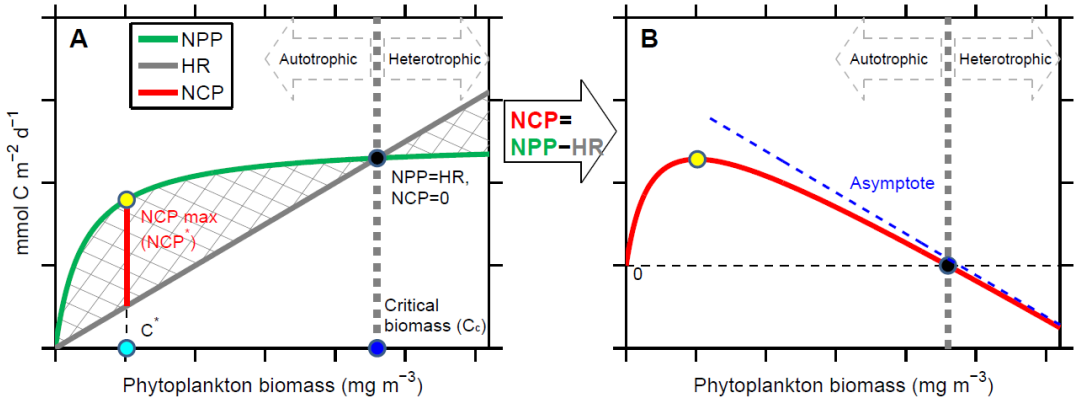

Figure 2. Relationship between net primary production (NPP), heterotrophic respiration (HR), net community production (NCP), and phytoplankton biomass concentration (C) for a given mixed layer depth (MLD). Hatched area in panel A represents NCP. The yellow dot represents the maximal NCP (NCP*) obtainable for a given MLD, with the corresponding phytoplankton biomass concentration (C*) denoted with a cyan dot. NCP on the right of the yellow dot decreases with C due to self-shading. Black dot represents depth-integrated NCP =0 (i.e., NPP=HR), with the corresponding phytoplankton biomass concentration defined as critical biomass (C_c) and denoted with a blue dot. Ecosystems on the left and right of this threshold are net autotrophic and heterotrophic, respectively. The asymptote (dashed blue line) in panel B represents a system dominated by heterotrophic respiration (i.e., NCP ≈ HR >> NPP).

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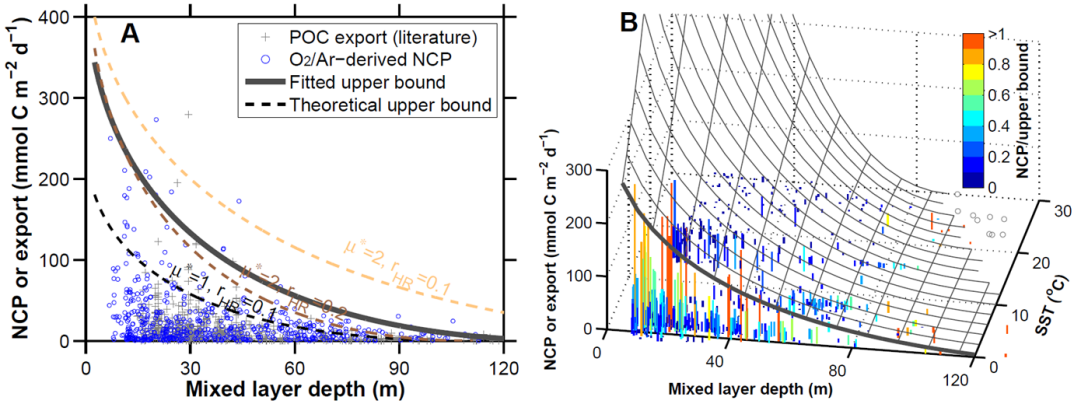

Figure 3. Envelope of the modeled upper bound on carbon export production compared to field observations as a function of mixed layer depth (MLD) and sea surface temperature (SST). Observations are based on ^{234}Th and sediment traps estimates of carbon export production and O_2/Ar-derived net community production. To account for the effect of PAR on export production, both MLD and carbon fluxes are normalized to $I_m(0) = \frac{I_0}{I_0 + k_m^I}$ (see equations (19) and (21)). (A) The thick gray line represents the upper bound fitted to the O_2/Ar-NCP data. Dash-lines represent the upper bounds calculated using parameters available in the literature. (B) Surface representing the envelope of the modeled upper bound of carbon export production as a function of SST and MLD. Bars represent field observations color coded with the ratio of NCP to the upper bound. A stoichiometric ratio of O_2/C=1.4 was used to convert NCP from O_2 to C units [*Laws*, 1991]. The temperature dependence of r_{HR} was modeled as $r_{HR} \propto e^{0.08 \times T}$.

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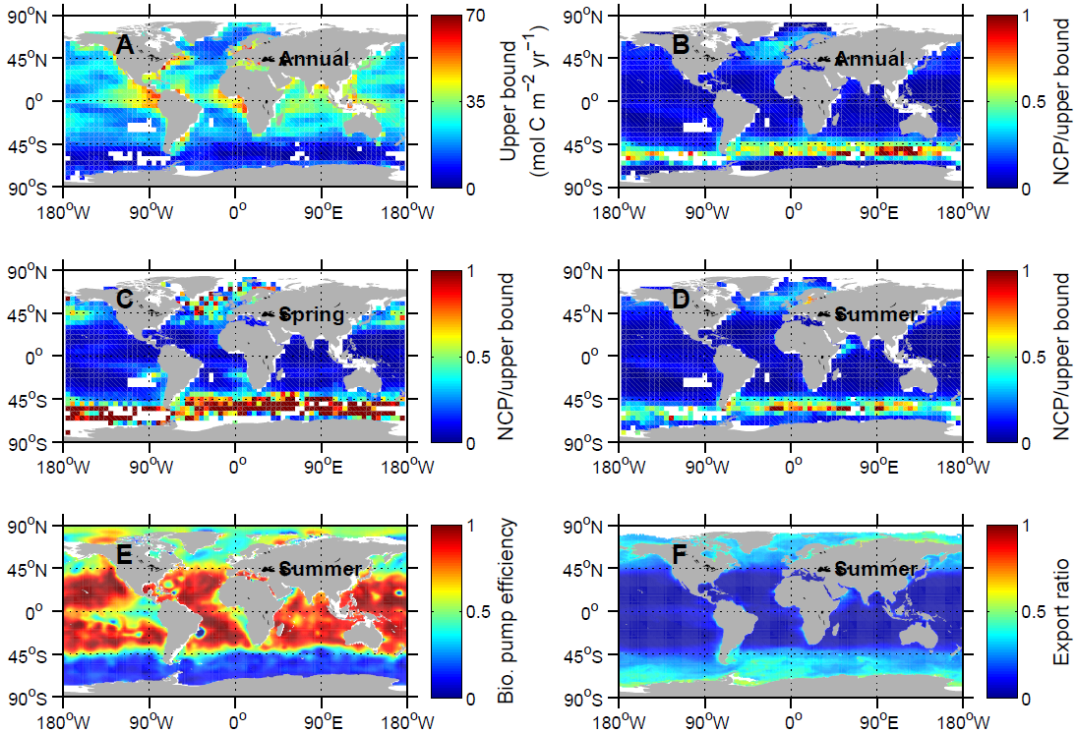

Figure 4. (A) Modeled upper bound on carbon export derived from equation (19), (B-D) ratios of satellite export production estimates to the upper bound on carbon export, (E) biological pump efficiency calculated as the difference in nutrient concentrations between surface and depth, normalized to nutrient concentrations at depth [*Sarmiento and Gruber*, 2006] (nitrate concentration from World Ocean Atlas (https://www.nodc.noaa.gov/OC5/woa13/)), and (F) export ratio derived from Dunne *et al.* [2005]. Annual represents annually-integrated value. Spring and summer represent average value in spring and summer, respectively. In the northern hemisphere, spring and summer seasons are defined as March-May and June-August, respectively. In the southern hemisphere, spring and summer seasons are defined as September-November and December-February, respectively.