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## S1 Introduction

This supporting information provides details on how the flux between Lake Kuivajärvi and the atmosphere, measured by eddy covariance, was calculated (Sect. S2). It also provides additional figures (Figg. S1-S14). Figures S1 and S2 consist of maps, showing the location of Lake Kuivajärvi in Finland, its bathymetry and the position of the measuring raft. Figure S3 is a schematic representation of the measuring system we built for the CO<sub>2</sub> concentration in the water. Figure S4 displays the time series of isotherms of the lake for the whole summers, while Figg. S5-S14 display the time series of isotherms, of the Schmidt stability and of the CO<sub>2</sub> concentration at 0.2 m for the periods of stable stratification chosen for analysis.

## S2 Calculation of the eddy covariance fluxes

The CO<sub>2</sub> flux between the lake and the atmosphere was measured using the eddy covariance (EC) technique (Aubinet *et al.*, 2012). The fluxes were calculated as in Vesala *et al.* (2006); Mammarella *et al.* (2009, 2015). The chosen averaging time was 30 minutes, and the mean values were obtained by block-averaging. Before calculating the covariances, the data were despiked according to standard methods (Vickers and Mahrt, 1997). Successively, the coordinate system was rotated via a two-step rotation (Kaimal and Finnigan, 1994), so that the  $x$  axis was parallel to the mean wind direction and the mean of the vertical wind velocity was 0. The CO<sub>2</sub> mole fraction values were converted to dry mole fraction values (Burba *et al.*, 2012). The time lag between the measurement of the vertical wind velocity and the measurement of the CO<sub>2</sub> mole fraction was determined for each 30-min interval separately, by maximizing the difference between their cross-correlation function and the line connecting the values of the cross-correlation at the lag window boundaries (Clement, 2004). The fluxes were also corrected for high-frequency and low-frequency losses, according to Foken *et al.* (2012). Finally, the fluxes were quality screened. Data from 30-min intervals when the prevailing wind direction was not along the lake were discarded. Furthermore, data were also discarded when the absolute value of skewness of the CO<sub>2</sub> concentration or of the vertical wind velocity was  $> 2$  and the kurtosis was  $< 1$  or  $> 8$  (Vickers and Mahrt, 1997). The flux steady-state test (FST) was also applied (Foken and Wichura, 1996), and data were rejected when  $FST > 0.3$ . The CO<sub>2</sub> storage flux in the air between the water surface and the height of the measuring system (1.5 m) is negligible.

## S3 Smith and Jassby and Platt model equations and fit results

We checked whether the Smith (1936) or the Jassby and Platt (1976) models were a better fit to the data than the Michaelis-Menten curve. Maintaining the assumption that the daytime respiration rate equals the nighttime respiration rate and that they depend exponentially on temperature (Carignan *et al.*, 2000), we still had:

$$NPP = GPP - R_h = GPP - r_0 Q_{10}^{T/10}, \quad (S1)$$

with  $T$  as the water temperature (in °C),  $Q_{10}$  as a non-dimensional temperature coefficient with a value of 2 for freshwater communities, and  $r_0$  as the parameter representing the basal respiration of phytoplankton ( $\mu\text{mol}(\text{CO}_2) \text{m}^{-2} \text{s}^{-1}$ ).  $GPP$  was

expressed as

$$GPP = \frac{p_{\max} \alpha PAR}{\sqrt{p_{\max}^2 + \alpha^2 PAR^2}} \quad (S2)$$

following Smith (1936), and as

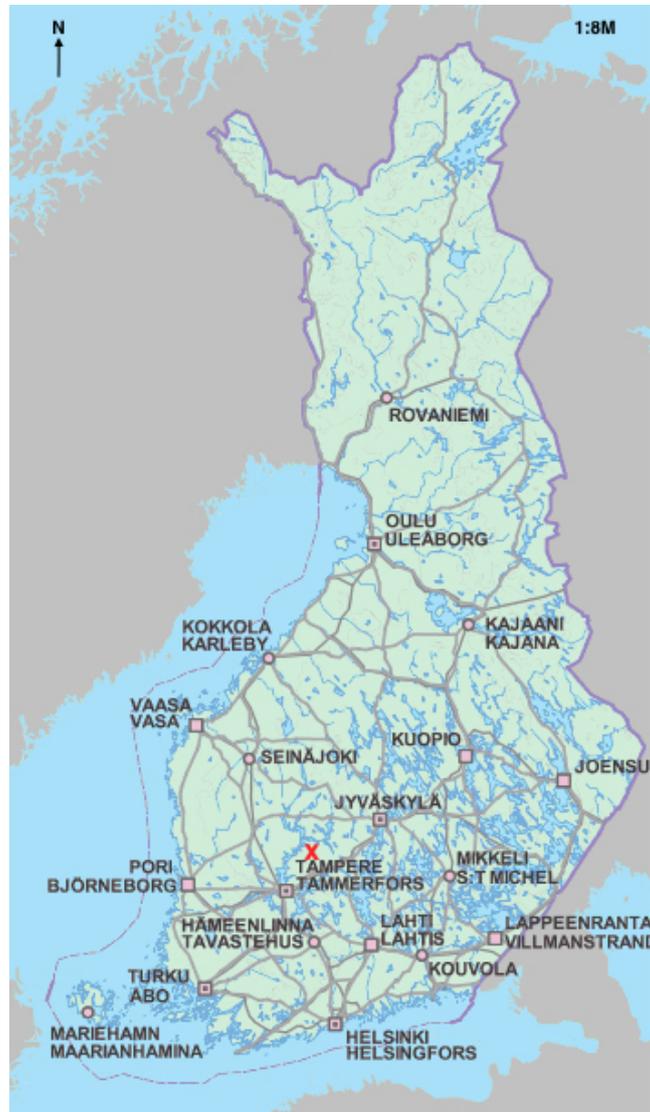
$$GPP = p_{\max} \tanh \frac{\alpha PAR}{p_{\max}} \quad (S3)$$

- 5 following Jassby and Platt (1976), with  $p_{\max}$  as the maximum potential photosynthetic rate ( $\mu\text{mol}(\text{CO}_2) \text{m}^{-2} \text{s}^{-1}$ ) and  $\alpha$  as the curve slope at low light levels ( $\mu\text{mol}(\text{CO}_2) \text{m}^{-2} \text{s}^{-1} (\mu\text{mol}(\text{ph}) \text{m}^{-2} \text{s}^{-1})^{-1}$ ).

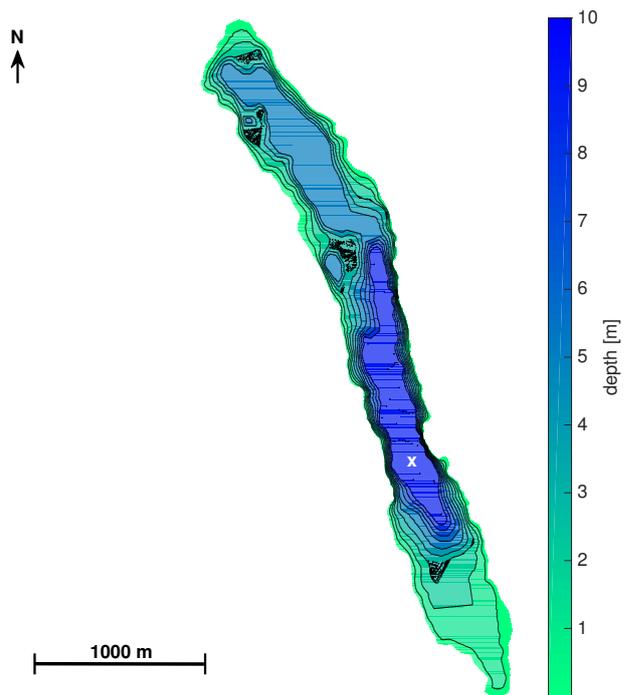
The fit statistics are reported in Table S1 (the Michaelis-Menten fit statistics are also reported, for comparison). They show that there is a good agreement between all the models and the data, and that there is no significant reason to discard the Michaelis-Menten curve.

## References

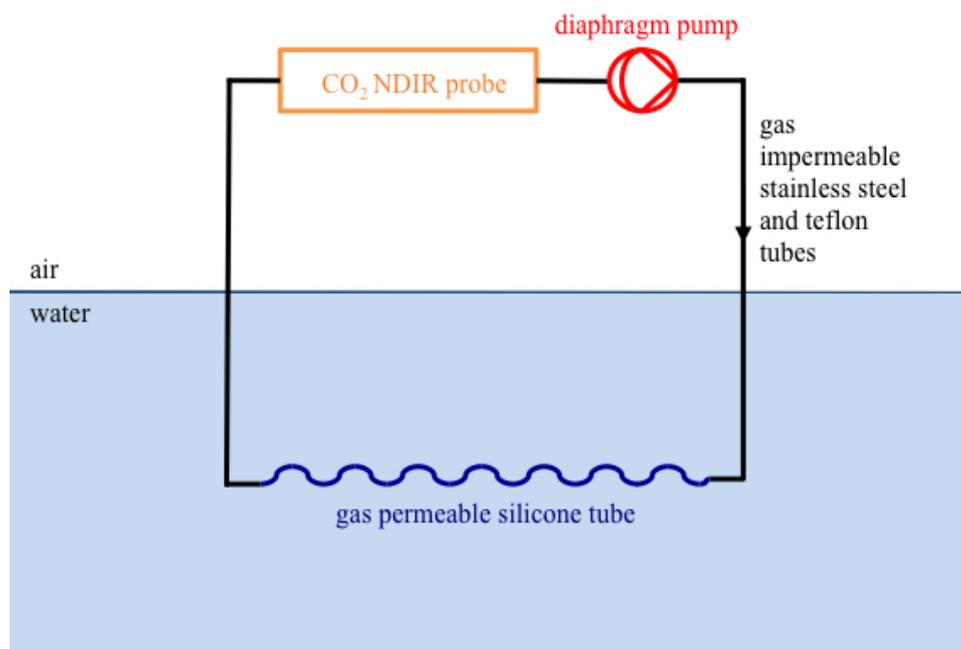
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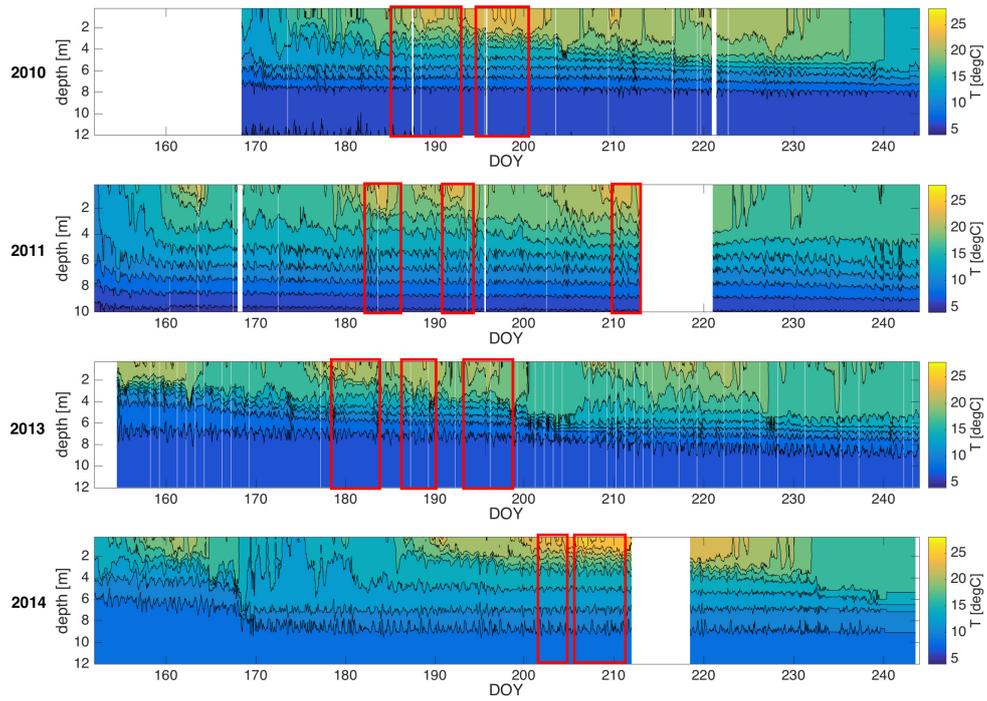
**Figure S1.** The location of Lake Kuivajärvi in Finland, represented by the red “x”. Its coordinates are 61°50.743’ N, 24°17.134’ E. This figure contains data from the National Land Survey of Finland Topographic Database 12/2015.



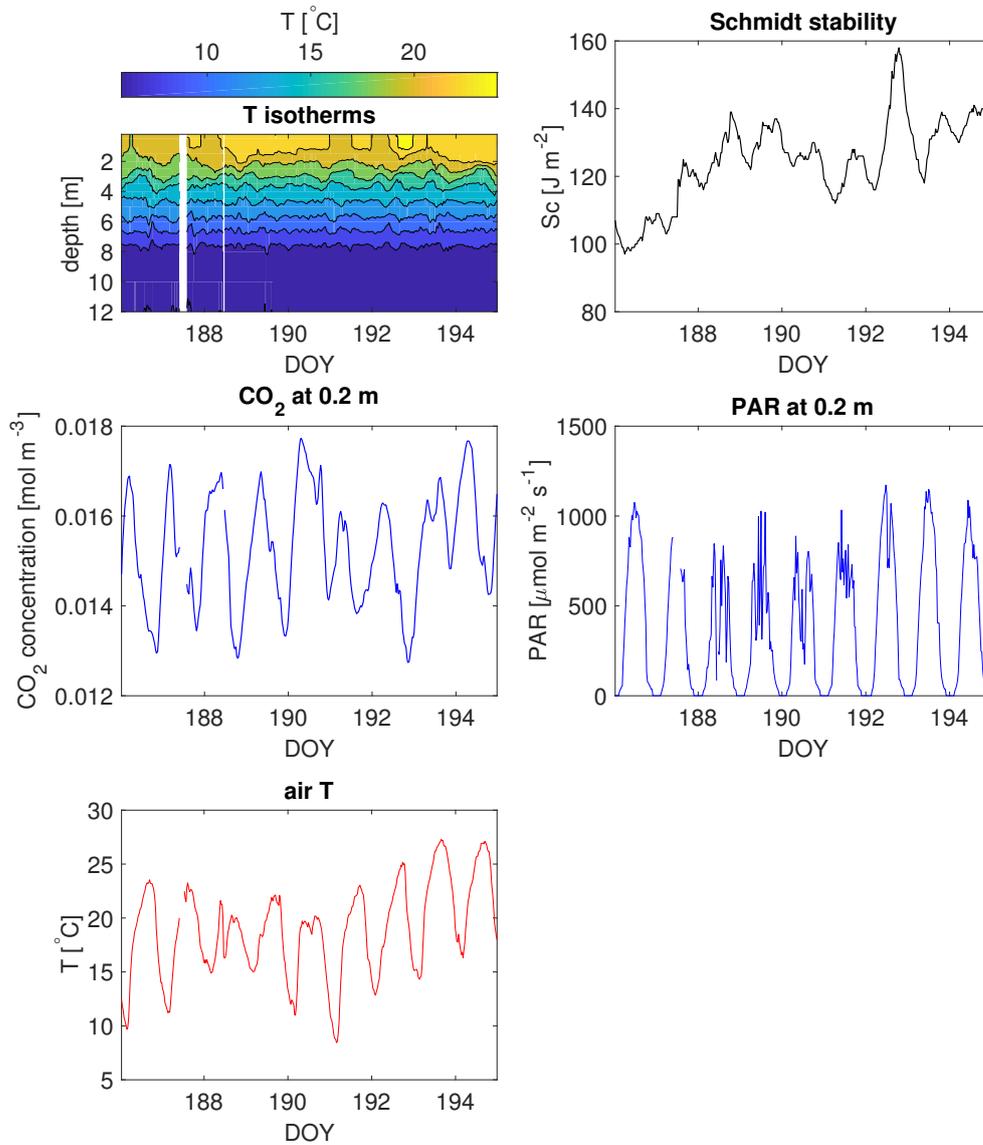
**Figure S2.** The bathymetry of Lake Kuivajärvi. The position of the raft with the measuring instruments is marked in the picture with a white “X”.



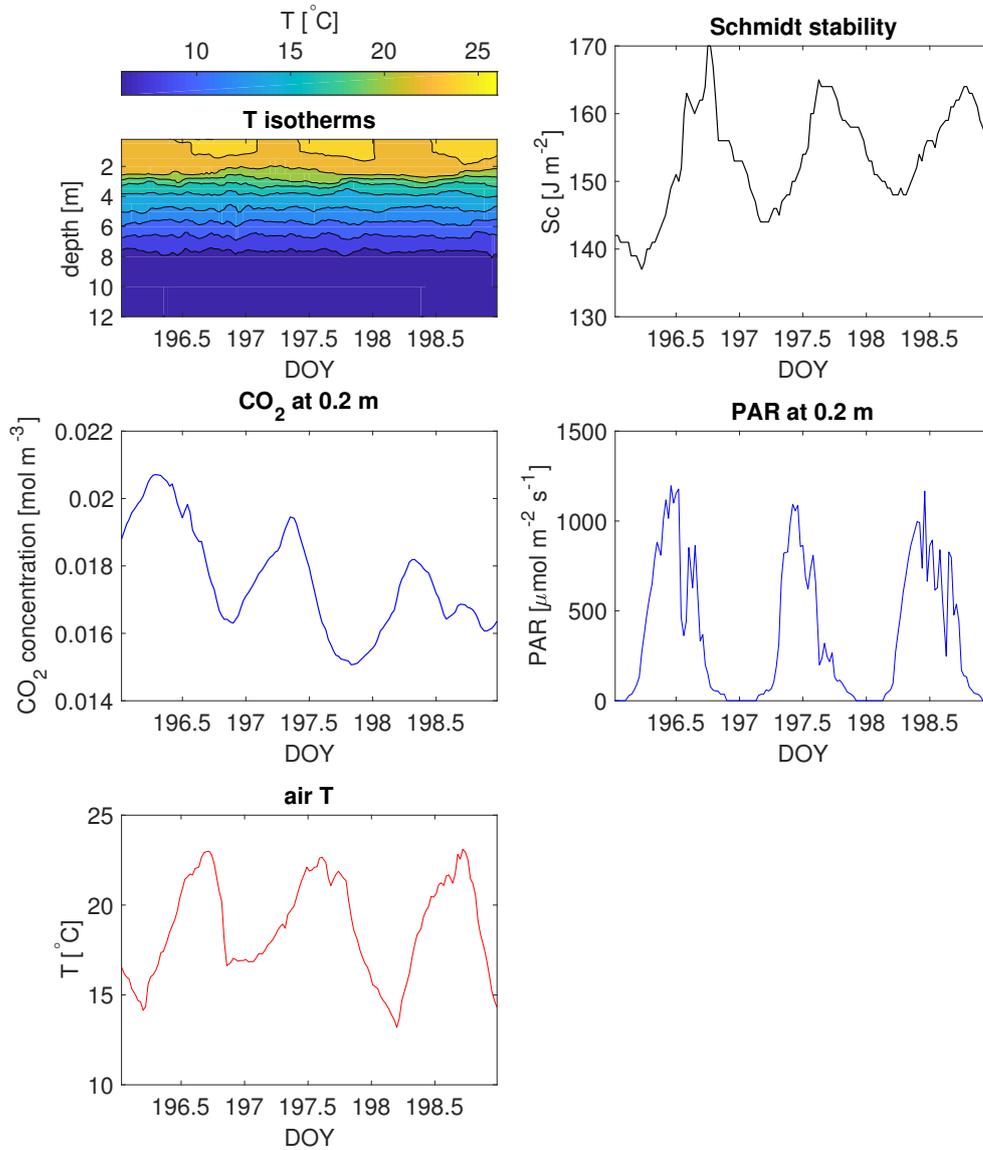
**Figure S3.** The measuring system, consisting in the CO<sub>2</sub> NDIR probe (CARBOCAP® GMP343, Vaisala Oyj, Vantaa, Finland) for the CO<sub>2</sub> concentration in the air, gas impermeable stainless steel and teflon tubes, a submerged silicone gas permeable tube (Rotilabo 9572.1, Carl Roth GmbH and Co. KG, Karlsruhe, Germany) and a diaphragm pump to circulate the air in the system (KNF Neuberger Micro gas pump, KNF Neuberger AB, Stockholm, Sweden).



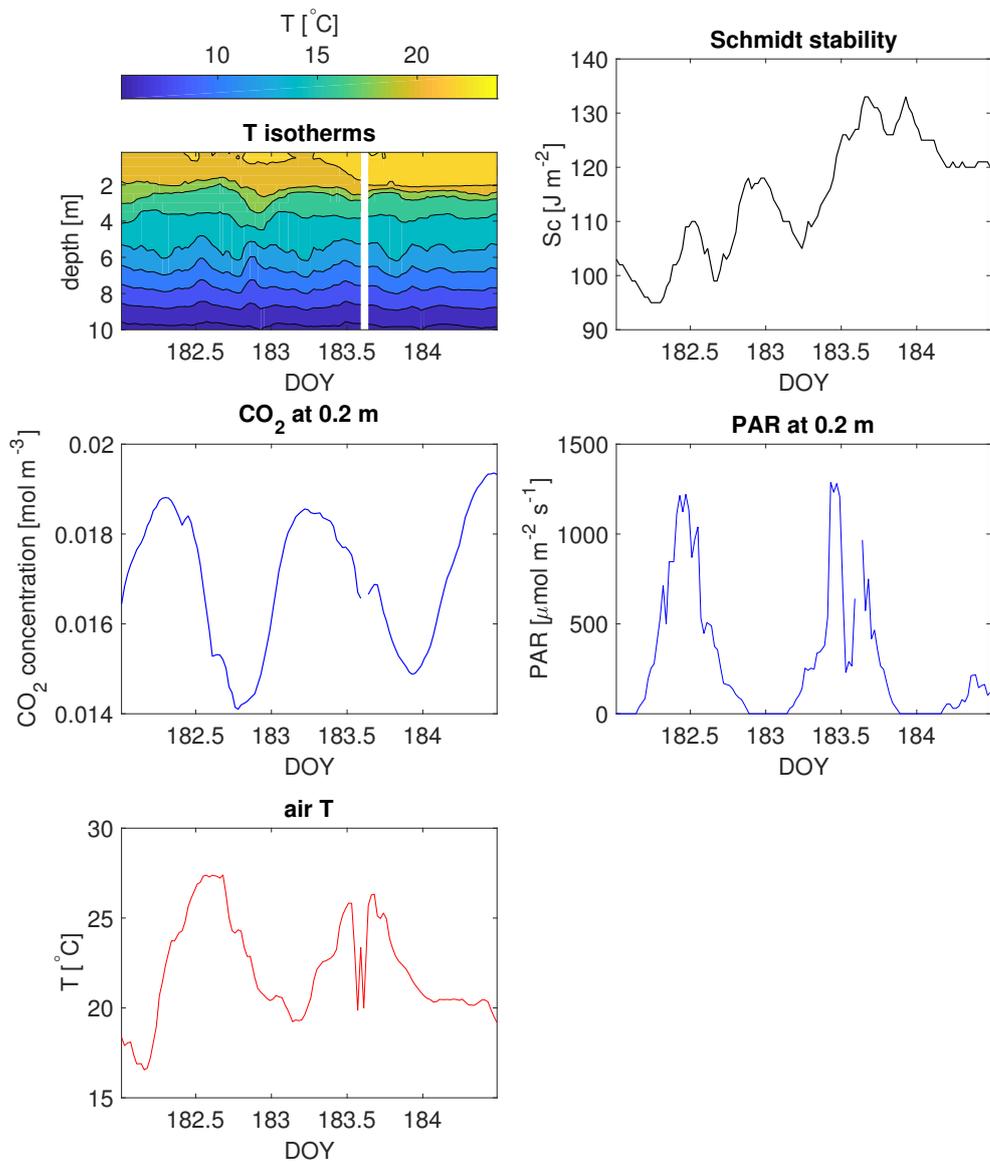
**Figure S4.** The temperature maps of the lake for the studied summers, from 1 June (DOY = 152) to 31 August (DOY = 243). The red rectangles indicate the periods of stable stratification that were chosen for the data analysis. All of them are between mid-June and the end of July.



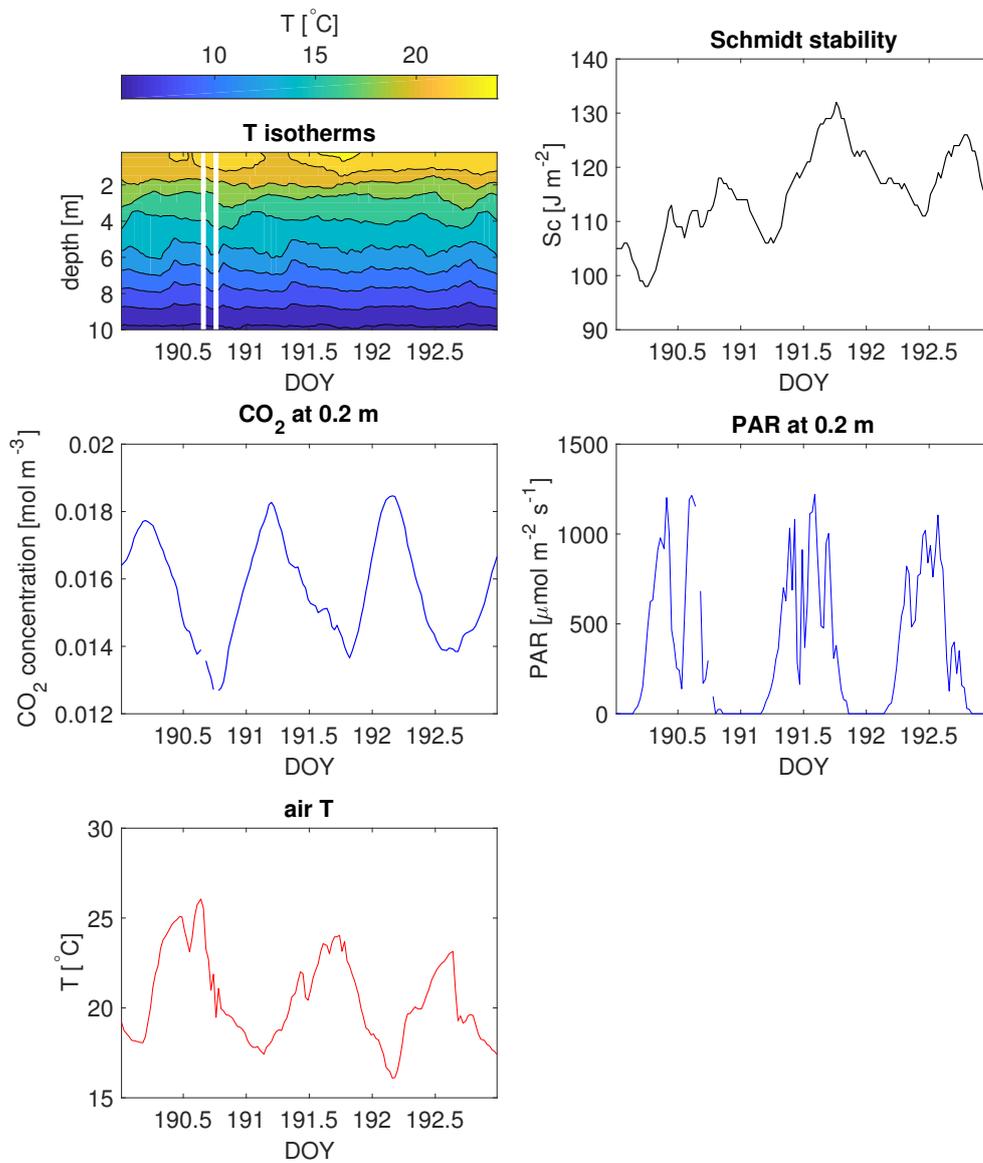
**Figure S5.** Time series of isotherms, Schmidt stability, CO<sub>2</sub> concentration and *PAR* at 0.2 m, and air temperature for the first period of stable stratification studied in 2010 (5 July - 13 July).



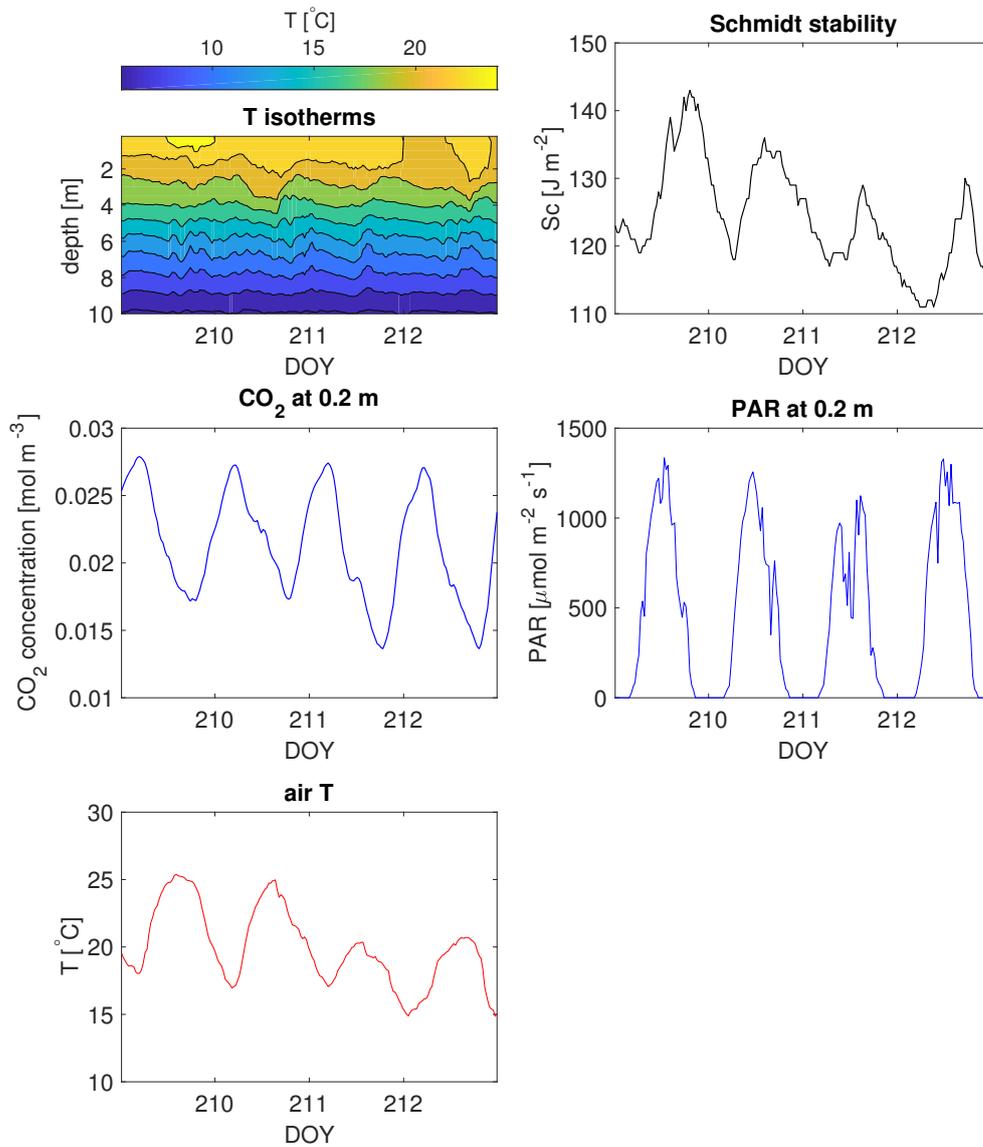
**Figure S6.** Time series of isotherms, Schmidt stability, CO<sub>2</sub> concentration and *PAR* at 0.2 m, and air temperature for the second period of stable stratification studied in 2010 (15 July - 17 July).



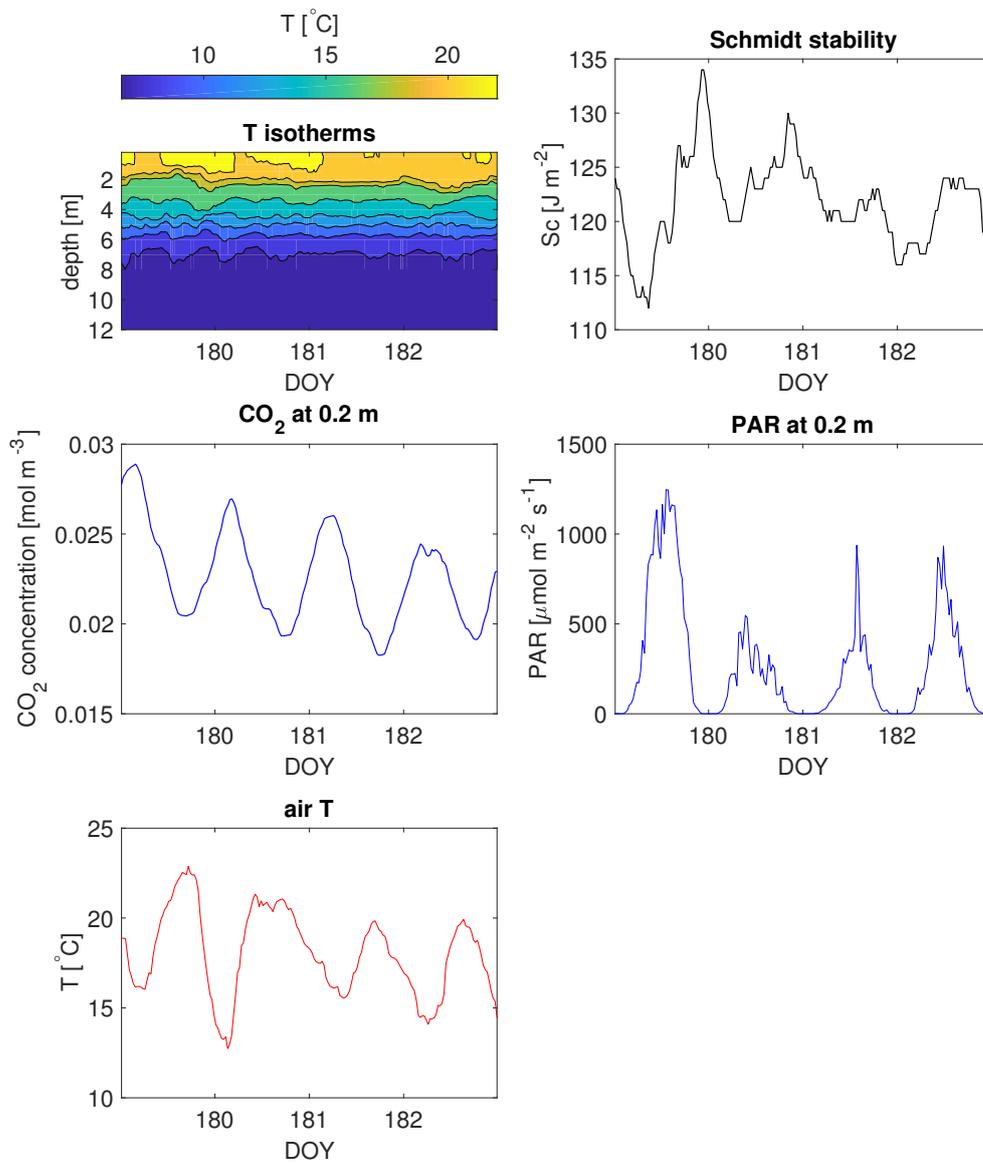
**Figure S7.** Time series of isotherms, Schmidt stability, CO<sub>2</sub> concentration and *PAR* at 0.2 m, and air temperature for the first period of stable stratification studied in 2011 (1 July - 3 July).



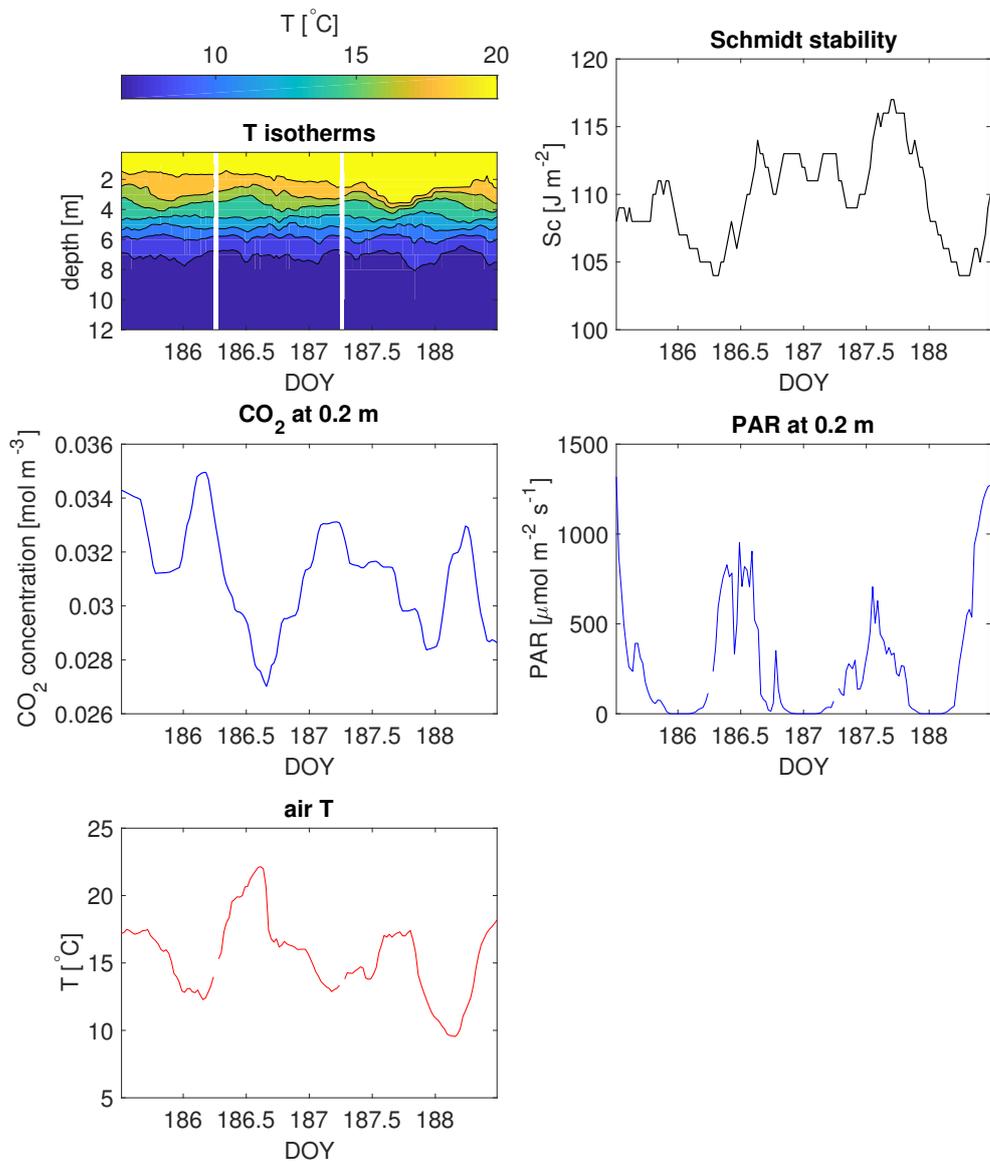
**Figure S8.** Time series of isotherms, Schmidt stability, CO<sub>2</sub> concentration and *PAR* at 0.2 m, and air temperature for the second period of stable stratification studied in 2011 (9 July - 11 July).



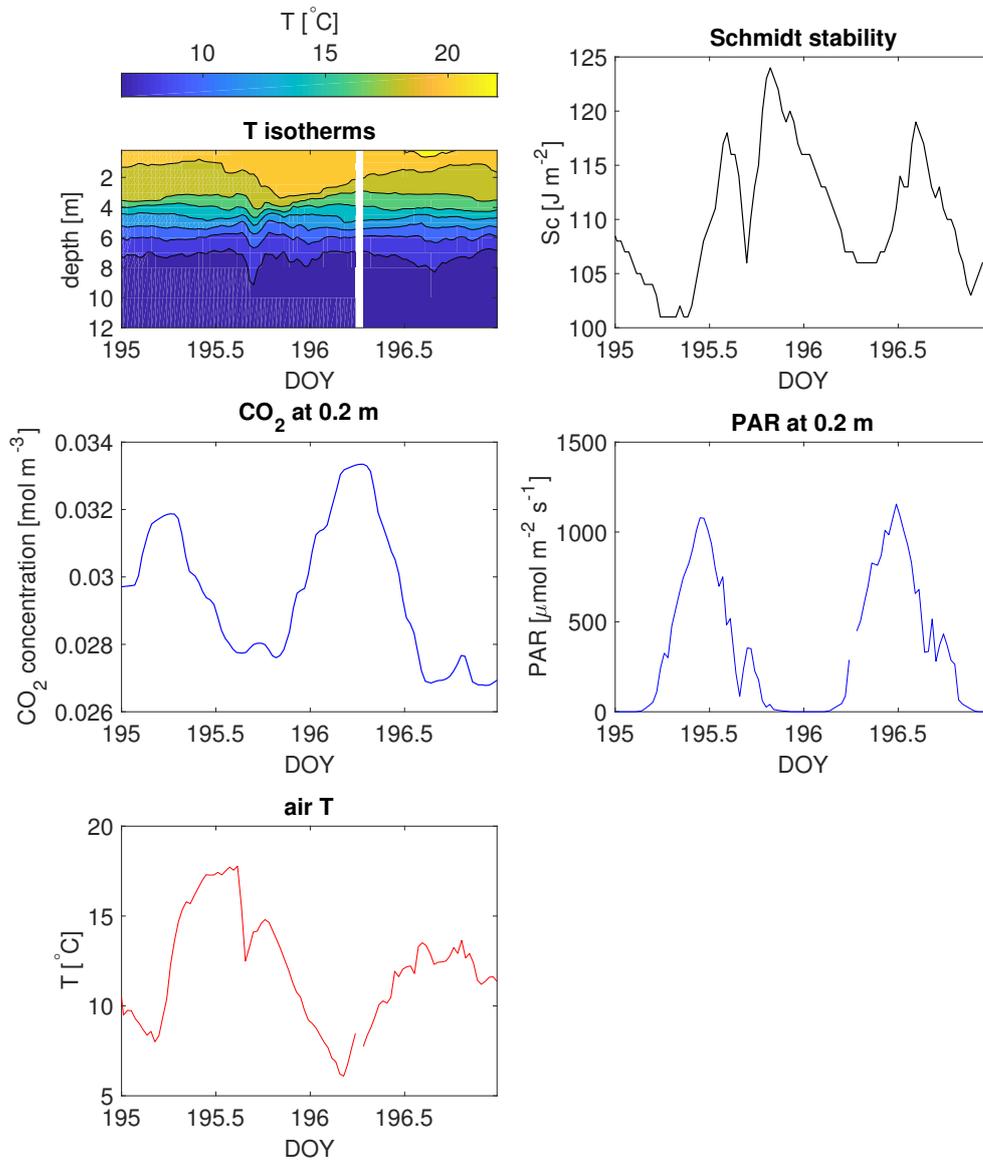
**Figure S9.** Time series of isotherms, Schmidt stability, CO<sub>2</sub> concentration and *PAR* at 0.2 m, and air temperature for the third period of stable stratification studied in 2011 (28 July - 31 July).



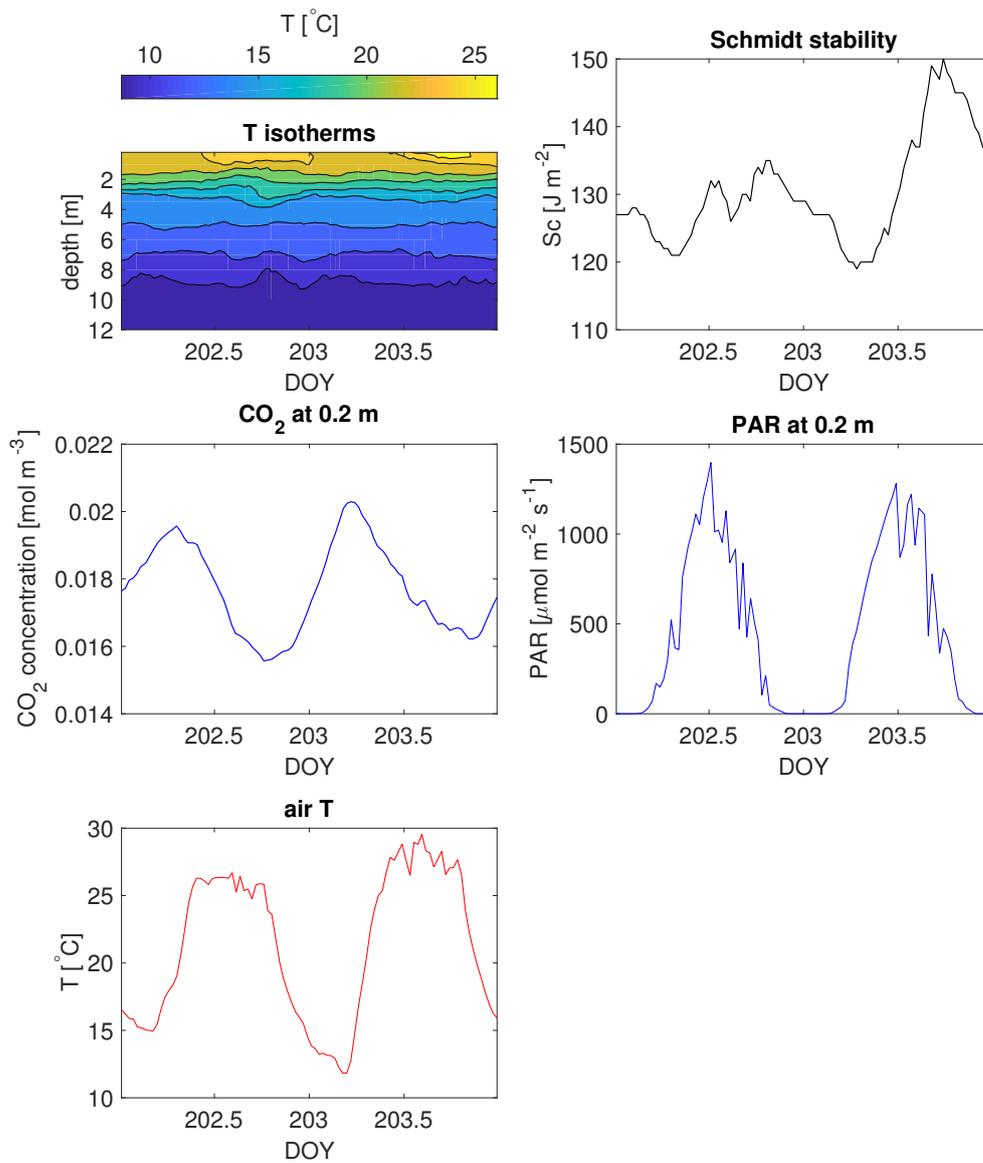
**Figure S10.** Time series of isotherms, Schmidt stability, CO<sub>2</sub> concentration and *PAR* at 0.2 m, and air temperature for the first period of stable stratification studied in 2013 (28 June - 1 July).



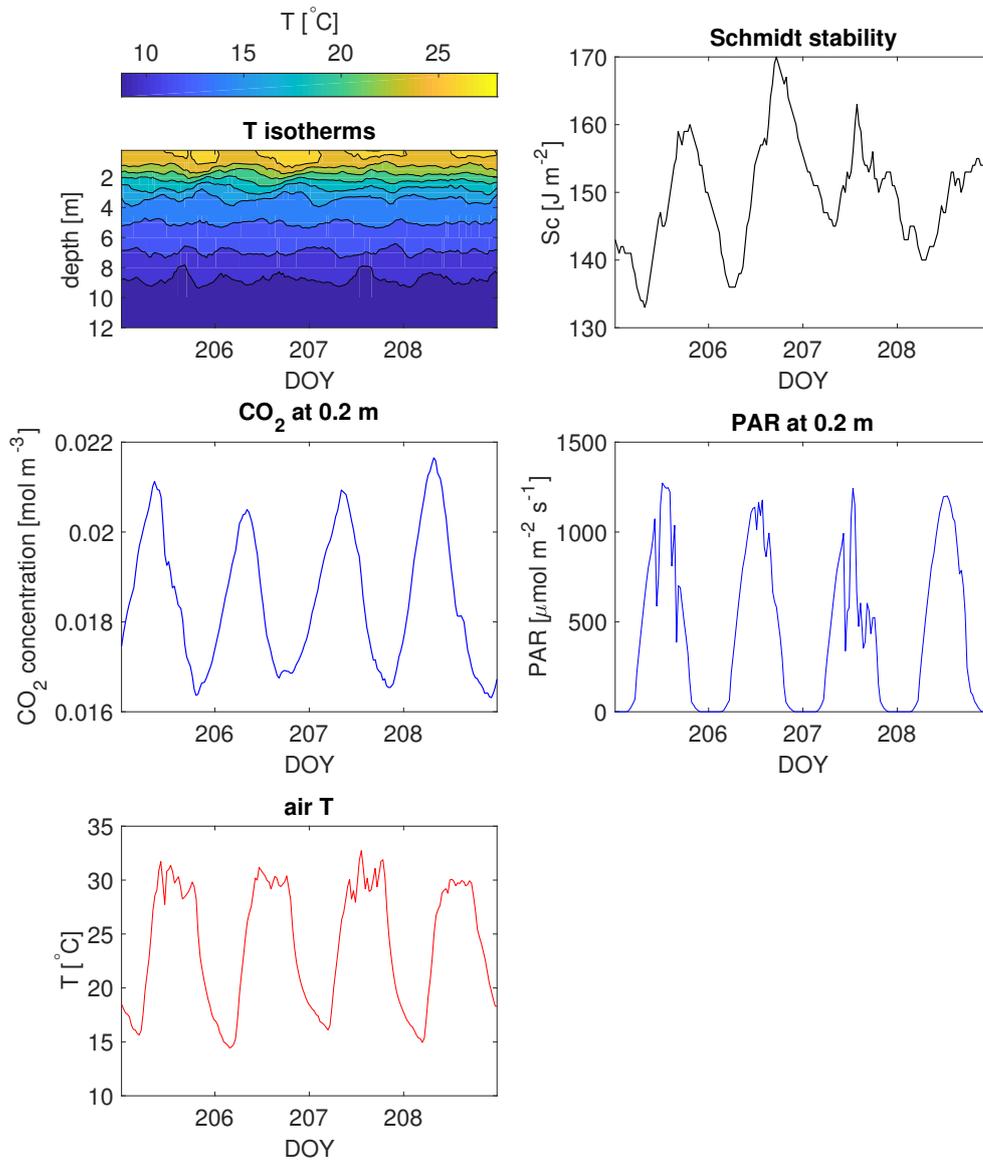
**Figure S11.** Time series of isotherms, Schmidt stability, CO<sub>2</sub> concentration and *PAR* at 0.2 m, and air temperature for the second period of stable stratification studied in 2013 (4 July - 7 July).



**Figure S12.** Time series of isotherms, Schmidt stability, CO<sub>2</sub> concentration and *PAR* at 0.2 m, and air temperature for the third period of stable stratification studied in 2013 (14 July - 15 July).



**Figure S13.** Time series of isotherms, Schmidt stability, CO<sub>2</sub> concentration and *PAR* at 0.2 m, and air temperature for the first period of stable stratification studied in 2014 (21 July - 22 July).



**Figure S14.** Time series of isotherms, Schmidt stability, CO<sub>2</sub> concentration and *PAR* at 0.2 m, and air temperature for the second period of stable stratification studied in 2014 (24 July - 27 July).

**Table S1.** Fit statistics ( $R^2$  and RMSE in  $\mu\text{mol}(\text{CO}_2)\text{m}^{-2}\text{s}^{-1}$ ).

Model	2010 $R^2$	RMSE	2011 $R^2$	RMSE	2013 $R^2$	RMSE	2014 $R^2$	RMSE
Michaelis-Menten	0.73	0.23	0.84	0.25	0.71	0.14	0.74	0.33
Smith	0.76	0.22	0.85	0.25	0.70	0.15	0.74	0.33
Jassby and Platt	0.76	0.22	0.84	0.25	0.70	0.15	0.74	0.33