

We are happy that the reviewer found our first revision to be almost satisfactory. Here below you will find a point-by-point response for each of the reviewer's residual comments.

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Reviewer #1:

1. Comment 18: I still think it highly desirable to separate Results (what was found) from Discussion (how the authors interpret the results in support of their argument). At the very least (at the Editor's discretion), please check the structure of each subsection for this clear separation. For example, the first paragraph could clearly be Results and the second paragraph is clearly Discussion of those results. That will clarify these elements for the reader.

Response

We reorganized the paper separating Results and Discussion.

2. For a model validation study such as this, it is also valuable to make testable predictions or forecasts. It would be good to collect these predictions (for instance, of the applicability of the model to predictions of forest growth and allocation dynamics in other boreal forests; for the prediction of the response of the studied boreal forest growth and allocation dynamics under past or future environmental change) into one subsection that is clearly Discussion. This might include the Bayesian estimation of parameters, and here Fig S5, S9 would be useful results to discuss. For example, some parameters appear bimodal with all data but become unimodal with subsets; others show the reverse phenomenon. Why do the authors think this is, and do the uncertainties in the posterior parameter pdfs themselves affect their interpretations? (e.g. Fig S8)

Response

We introduced a new section with some model predictions:

"4.3 Some model predictions

It is possible to use the new optimized MAIDEN version to predict forest growth and allocation dynamics of the studied boreal forests under future environmental change. In the study area, the daily maximum temperature, the daily minimum temperature and the precipitation should increase at the 2050 horizon of about 2.3°C, 4.3°C and 12%, respectively (Guay et al., 2015). If we modify the used climatic data (Section 2.2.3) by these median changes and we fix the CO₂ concentration at the 2010 level, the median increase of the annual GPP and Dstem values simulated by MAIDEN for the studied forests is of 43 and 68%, respectively (Fig. S22). We have to recall that the ring width data used for the optimization of MAIDEN come from lake riparian trees and that these results are too optimistic for more water limited boreal sites."

We also grouped all discussion about parameter interpretation on a new 4.1 section. In this section, we decided to focus on: (1) the shrinking of the parameters' posterior distributions relative to the prior acceptable ranges; (2) the bimodal structures of some parameters; (3) some clear inconsistencies when optimizing on different periods or sites; (4) the impact of parameters' uncertainties on our interpretations; (5) the in depth discussion of some important parameters.

"4.1 Parameter interpretation

The posterior distributions of the parameters were quite sharp (Figs. S4 and S5; Table 1; by sharpness we mean the shrinking of the distribution relative to the prior acceptable range toward a posterior distribution with a well-defined, narrow peak). Sharp distributions with small posterior ranges relative to the prior ones indicate sensitive parameters. This means that the model posterior probability (i.e. model plausibility) increased significantly with the specific values of the selected parameters retained by the MCMC sampling. The slightly bimodal structures of the posterior distributions of *V_{max}*, *V_b* and *V_{ip}* were likely a consequence of their significant cross-correlations (Table S1). However, the posterior distributions of these three parameters were robust and consistent even when the Bayesian optimization was executed on independent periods (Fig. S19). The optimization of some parameters controlling Dstem (the three related to the start of the growing season and *Cbud*) was sensitive to the choice of the period and the site in

the cross-validation exercise (Figs. S20 and S21) likely as a result of the short length of the available observed data (61 yearly R_{WhigF} values) and of some significant cross-correlation coefficients (Table S2). However, in all cases, the uncertainties in the parameters' posterior distributions (Figs. S4 and S5) did not affect our interpretations because the MAIDEN simulations were extremely consistent whatever the selected block of parameters (see Figs. 3 and 5).

The interpretation of some parameters needs special care. For example, those controlling the negative impact of both previous year April precipitation and July-August temperature values on canopy development, which may be explained by the following reasons: warm previous Aprils with infrequent late snowfalls may accelerate snowmelt and the start of the previous growing season, allowing optimal reserve accumulation during the previous year which would influence tree performance the following growing year. This mechanism may be significant especially if we do not observe high temperatures limiting soil water availability and reserve accumulation during the previous summer (Girardin et al., 2016). It has already been shown that shoot elongation of boreal conifers is determined by climate conditions during bud formation (Salminen and Jalkanen, 2005). However, for Scots pine, previous summer temperatures are positively correlated with shoot elongation, while in our case, the opposite process was simulated and the simulations were even more sensitive to the values of the CanopyT temperature dependent parameter than to those of the CanopyP precipitation dependent parameter (Fig. 7b-e). Clearly, we need more data on canopy development and shoot elongation to verify the model results."

3. The discussion of testable predictions would highlight another important element that belongs in the new section 3.4. This is the extent to which the model structure might be overly tuned to the simulation of the target with the multiple fixed parameters described in 2.1.2. This should be discussed in general terms: identify the potential problem and then allow for the possibility of their estimation rather than specification. Of course this would require more tuning and more input data, but this is the price we pay for model complexity.

Response

We added a sentence in section 4.4:

"Second, some fixed parameters are present in the MAIDEN code (see Eqs. 4 and 6). These parameters might be potentially tuned but their specification is justified in Section 2.1.2 and limits additional parameter tuning."

4. Please review the revised/new text, including table and figure captions, for grammar; e.g. "Warmer temperature corresponded to a greater portion of carbon allocated to the stem and less to non-structural carbohydrates (Fig. 8a-b), being the simulations highly sensitive to the st4temp parameter (Fig. 8c-d)." --> "Warmer temperatures corresponded to a greater amount of carbon allocated to the stem and less to non-structural carbohydrates (Fig. 8a-b), because the simulations are highly sensitive to the ..."

Response

We revised the sentence and more carefully checked our text for grammar mistakes.

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In the next pages you will find a marked-up manuscript version where new insertions are in red and moved sections are in green.

Ecophysiological modeling of photosynthesis and carbon allocation to the tree stem in the boreal forest

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Abstract. A better understanding of the coupling between photosynthesis and carbon allocation in the boreal forest, with implicated environmental factors and mechanistic rules, is crucial to accurately predict boreal forest carbon stocks and fluxes, which are significant components of the global carbon budget. Here we adapted the MAIDEN ecophysiological forest model to better consider important processes for boreal tree species, such as non-linear acclimation of photosynthesis to temperature changes, canopy development as a function of previous year climate variables influencing bud formation, and temperature dependence of carbon partition in summer. We tested these modifications in the eastern Canadian taiga using black spruce (*Picea mariana* (Mill.) B.S.P.) gross primary production and ring-width data. MAIDEN explains 90% of the observed daily gross primary production variability, 73% of the annual ring width variability and 20-30% of its high frequency component (i.e. when decadal trends are removed). The positive effect on stem growth due to climate warming in the last decades is well captured by the model. In addition, we illustrate the improvement achieved with each introduced model adaptation and compare the model results with those of linear response functions. This shows that MAIDEN simulates robust relationships with the most important climate variables (those detected by classical response-function analysis), and is a powerful tool for understanding how environmental factors interact with black spruce ecophysiology to influence present-day and future boreal forest carbon fluxes.

25 1 Introduction

Photosynthetic production is the primary motor of growth of trees and other vegetation. However, empirical studies have shown that correlation between photosynthetic production and diameter growth of trees is far from being perfect (Gea-Izquierdo et al., 2014; Rocha et al., 2006; Berninger et al., 2004). This is due to the fact that plant hydraulics (e.g. turgor pressure) and thermal limitations during very short periods of time can be more important than carbon (C) availability for tree secondary growth (Kirdyanov et al., 2003; Rossi et al., 2016; Zweifel et al., 2016; Fatichi et al., 2014; secondary growth is the increase of the girth of the plant roots and stems). These factors influence the proportion of net primary productivity

allocated to stem growth each year, dampening the correlation between gross primary production (GPP) and growth. A better understanding of these factors and of carbon allocation mechanisms is needed when studying forest dynamics, forest carbon balance and the impact of climate change on forests. Indeed, carbon allocated in different tree components (e.g. canopy, stem or roots) has a specific function and is stored for a different length of time (Moorcroft, 2006).

5 The varying roles of allocation and photosynthetic production are integrated in ecophysiological models (Li et al., 2014). Such models are important tools to analyze the direct influence of climate and other environmental factors (e.g. CO₂ concentration) on tree growth and biogeochemical processes in forest ecosystems (Li et al., 2016). Climate-growth relationships have traditionally been assessed using empirical response functions based on linear relationships, thus considering the underlying processes as a black box. In contrast, ecophysiological models are built on mechanistic rules and
10 allow considering non-stationarity and non-linearity in tree responses to environmental variables as well as their interactions (Vaganov et al., 2006). Ecophysiological models may be refined using model-data fusion approaches and optimization techniques (Guiot et al., 2014).

Different models with a different degree of ecophysiological complexity and/or spatio-temporal resolution have already been used to investigate the influence of climate and weather on tree growth in the boreal forest. Some studies focused on the
15 drivers of photosynthetic capacity. For example, Mäkelä et al. (2004) proposed a model to study the influence of temperature on the seasonal variation in photosynthetic production of Scots pine through a delayed dynamic response. Other studies focused on the drivers of carbon allocation. For example, in Manitoba, Canada, a model related GPP and carbon allocation to absorbed photosynthetically active radiation as a function of environmental constraints (Girardin et al., 2008). Another model, called CASSIA (Schiestl-Aalto et al., 2015), was developed to investigate how environmental factors and the
20 ontogenetic stage of tree development influence the annual course of carbon sink–source dynamics in Scots pine stands. However, in spite of recent progress few models have been able to simultaneously simulate the meteorological control on daily photosynthetic production and the meteorological and phenological controls on daily carbon allocation for temperature-limited boreal forest ecosystems. Such models should be able to simulate the following observed phenomena: (i) delayed response of photosynthesis to temperature (Gea-Izquierdo et al., 2010; Mäkelä et al., 2004); (ii) influence of preceding
25 season conditions on current year canopy development (Salminen and Jalkanen, 2005); (iii) strong positive relationship between wood biomass production and temperature (Cuny et al., 2015).

Here we try to fill this gap by adapting the MAIDEN forest ecophysiological model, developed for temperate and Mediterranean environments (Misson, 2004; Gea-Izquierdo et al., 2015), to mimic how weather and climate influence photosynthesis, phenology and carbon allocation in the North American boreal forest on a daily basis. MAIDEN offers an
30 ideal framework to analyze the impact of introducing in the model relevant processes for carbon assimilation and allocation in temperature sensitive boreal trees. Indeed, the model simultaneously simulates the course of photosynthesis and sets different phenological phases to determine the allocation of carbon to different plant compartments in a dynamical manner. In this study, we firstly test and optimize new model features on GPP and growth data from black spruce (*Picea mariana* (Mill.) B.S.P.), the dominant tree species across the North American boreal biome. Secondly, we show the impact of single

processes in the model runs and the improvements achieved with the new model adaptations. Lastly, we compare the simulated GPP and stem growth results with those obtained with conventional empirical linear response functions. This comparison allows to verify that the process-based ecophysiological model satisfactorily reproduces the variability of the observed data and that its simulations keep robust relationships with the most significant climate variables.

5 2 Materials and Methods

2.1 The MAIDEN model

MAIDEN (Misson, 2004; Gea-Izquierdo et al., 2015) is able to consider the influence of several environmental factors on the forest water and carbon cycles. Starting from daily minimum-maximum air temperature, precipitation and CO₂ atmospheric concentration (these are the minimum required input variables which are completed by radiation, relative humidity and wind speed when additional meteorological data are available; Misson, 2004), MAIDEN models the phenological and meteorological controls on GPP and carbon allocation (Fig. 1; see also flowcharts in Misson, 2004 and Gea-Izquierdo et al., 2015). It explicitly allocates carbon to different pools (storage, canopy, roots and stem) on a daily basis using phenology-dependent mechanistic rules. The model has already been successfully optimized for *Quercus petraea* (Matt.) Liebl. and 12 Mediterranean species, including several *Pinus* spp. and *Quercus* spp. (Gaucherel et al., 2008a; Danis et al., 2012; Misson, 2004; Misson et al., 2004; Boucher et al., 2014; Gea-Izquierdo et al., 2015; Gaucherel et al., 2008b; Gea-Izquierdo et al., 2017). Up to now, the model has never been used to simulate forest growth in boreal conditions.

MAIDEN requires the definition of species and site dependent parameters (Misson, 2004; Gea-Izquierdo et al., 2015), such as soil texture and depth and the root to leaf mass fraction in the studied trees. The parameters that could not be set for the studied black spruce sites were analyzed with a sensitivity analysis and the most influential of them were estimated with Bayesian optimization algorithms (Robert, 1996) using observed time series (daily GPP and annual ring width) as a reference. In total, six parameters influencing the GPP for black spruce and 12 parameters controlling the carbon allocation to the stem (Dstem) were optimized (they are described in the following paragraphs and in Table 1). The optimization was based on Markov Chain Monte Carlo (MCMC) sampling which, through its iterations, only retains combinations of parameters satisfying some conditions (Supplement S1; Fig. S1). Among the retained blocks of parameters, one block of six parameters controlling GPP (“Plausible Block GPP”) and one block of 12 parameters controlling Dstem (“Plausible Block Stem”) were selected to illustrate the results with likely parameter values (Supplement S1). The robustness of the parameters’ posterior distributions was tested on a cross-validation exercise (Supplement S1).

2.1.1 Modeling GPP of boreal forests

In MAIDEN, daily stand GPP ($\text{g C m}^{-2} \text{ day}^{-1}$) is derived from the modeling of the coupled photosynthesis-stomatal conductance system. Leaf photosynthesis is calculated following De Pury and Farquhar (De Pury and Farquhar, 1997), while stomatal conductance is estimated using a modified version of the Leuning equation (Leuning, 1995; Gea-Izquierdo et al.,

2015). The photosynthesis-stomatal conductance system is estimated separately for sun and shade leaves based on the photosynthetic photon flux density they receive. The partition of leaf area index (LAI) in its shaded and sunlit fractions and the transmission and absorption of photosynthetically active radiation (PAR) are computed as explained by Misson (Misson, 2004), following De Pury and Farquhar (De Pury and Farquhar, 1997). After a sensitivity analysis, and as stated in the literature for boreal forests (Gea-Izquierdo et al., 2010; Mäkelä et al., 2004; Mäkelä et al., 1996), we found that the modeling of assimilation/photosynthesis for black spruce is very sensitive to the parameters controlling the temperature dependence of maximum carboxylation rate (V_{cmax} ; $\mu\text{mol C m}^{-2}$ of leaves s^{-1}) and the water stress level (θg) influencing the stomatal conductance and consequently the intercellular CO_2 concentration. The computations of V_{cmax} and θg used here are identical to those of the prior formulation of MAIDEN (Gea-Izquierdo et al., 2015). The V_{cmax} is modeled as:

$$10 \quad V_{cmax_i} = \frac{V_{max}}{1 + \exp(Vb \cdot (T_{day_i} - V_{ip}))} \quad (1)$$

V_{cmax} is a logistic function determining how daytime temperature (T_{day} ; °C) controls the maximum carboxylation rate at the day i if Rubisco is saturated. The parameters V_{max} , Vb and V_{ip} are the asymptote, the slope and the inflection point of V_{cmax_i} , respectively. In the model, the temperature dependence when the photosynthesis is instead limited by electron transport (J_{max}) is considered as linearly related to V_{cmax} .

15 The θg influencing stomatal conductance is modeled as:

$$\theta g_i = \frac{1}{1 + \exp(\text{soilb} \cdot (\text{SWC}_i - \text{soilip}))} \quad (2)$$

θg is a logistic function, which varies from 0 (maximum stress) to 1 (no stress) at the day i depending on the soil water content (SWC ; mm). soilb and soilip are the slope and the inflection point of θg_i , respectively.

With its already published MAIDEN configuration (Gea-Izquierdo et al., 2015), the model overestimated black spruce GPP in spring. This is due to the fact that the model has been developed for temperate-Mediterranean trees where it can be assumed no time delay between the recovery of photosynthesis and temperature increase in spring (i.e. no temperature acclimation). However, such a delay is common in boreal trees (Gea-Izquierdo et al., 2010; Mäkelä et al., 2004). For this reason, we modified MAIDEN by including an extra function and an extra parameter (τ) to take into account acclimation of photosynthesis to temperature. Basically, we replaced T_{day} in Eq. (1) by a temperature transformation (S), which responds smoothly with a determined time lag to temperature variations. S of the day i was computed from the following differential equation (Mäkelä et al., 2004), which was solved with the Euler's method:

$$25 \quad \frac{dS_i}{di} = \frac{T_{day_i} - S_i}{\tau} \quad (3)$$

The new parameter τ is a time constant interpretable as the number of days needed by the photosynthetic apparatus to acclimate to changing temperature.

2.1.2 Modeling carbon allocation to the stem (Dstem) in boreal forests

MAIDEN allocates the daily available carbon from photosynthesis and stored non-structural carbohydrates to all plant compartments (stem, roots, canopy and storage) using functional rules specific to each of the five phenological phases characterizing a year (see Fig. 1). Although we maintained the original MAIDEN structure, we modified some previously used functional rules from Gea-Izquierdo et al. (2015) to consider significant processes for the boreal forest. We describe below the functional rules controlling Dstem, according to phenological phases.

During the “winter period 1” (phase 1) few processes are active. However, at the beginning of each year, the model defines the maximum amount of carbon that the canopy can potentially contain that year ($AlloCcanopy_j$; g C m⁻² of stand) as a function of previous year climate variables. Based on previous studies on black spruce forests (Girardin et al., 2016; Ols et al., 2016; Mamet and Kershaw, 2011), we modified the model to consider the effect of the previous year April precipitation and July-August temperature likely influencing the length and the thermal-hydraulic stress of the previous growing season, respectively. Previous year climate conditions of specific months are known to influence shoot extension of boreal trees likely because they control accumulation of resources in the buds (Salminen and Jalkanen, 2005). Here, we calculated the carbon potentially allocated each year to the canopy with the following equations:

$$CanopyMult = \frac{1}{1 + \exp(CanopyT \cdot Temp_{j-1})} \cdot \frac{1}{1 + \exp(CanopyP \cdot Precip_{j-1})} \quad (4)$$

$$AlloCcanopy_j = 0.7 \cdot MaxCcanopy + 0.3 \cdot MaxCcanopy \cdot CanopyMult$$

Where $Temp_{j-1}$ is the previous year mean July-August temperature (detrended and transformed to z-scores), $Precip_{j-1}$ is the previous year April precipitation (detrended and transformed to z-scores), and $MaxCcanopy$ is the absolute maximum canopy carbon reservoir according to forest traits, diameter distributions and previously published allometric equations (Chen, 1996; Bond-Lamberty et al., 2002a; Bond-Lamberty et al., 2002b). $CanopyT$ and $CanopyP$ are two parameters that were optimized and representing the slopes of the relationships between $CanopyMult$ (i.e. the overall climate dependence) and $Temp_{j-1}$ or $Precip_{j-1}$, respectively. In this way, $AlloCcanopy_j$ may vary between the 70% and the 100% of $MaxCcanopy$ as in the previous version of the model (Gea-Izquierdo et al., 2015).

During the “winter period 2” (phase 2), growing degree days (GDD) start to accumulate. We computed accumulation of GDD by summing the mean daily temperature values over 3°C (Nitschke and Innes, 2008; Man and Lu, 2010). MAIDEN simulates budburst (i.e. the transition from the phenological phase 2 to 3) either when the GDD sum threshold is reached (parameter $GDDI$) or when a selected day of the year related to photoperiod is passed (parameter $vegphase23$). With this model configuration, the start of the growing season overreacted to GDD yearly variations. To correct this simulated bias, we modified MAIDEN by adding a mechanism reducing the inter-annual variability of budburst dates. This mechanism simulates the acclimation of the plants to varying GDD sums from year to year. Basically, the yearly time series of days of the year corresponding to budburst (determined by GDD and photoperiod) is smoothed at the beginning of each simulation with a n -year cubic smoothing spline. The integer number n was called $day23_flex$ and optimized like the other parameters.

The “budburst phase” (phase 3) starts with budburst and ends when $AlloCcanopy_j$ is reached or when the carbon in the storage reservoir (i.e. stored non-structural carbohydrates) is lower than a minimum value (Misson, 2004). Here, this phase was set to be shorter than 51 days, based on available spruce budburst and shoot elongation data (Lemieux, 2010). During this phase, the daily available carbon (CT_i) comes from photosynthesis and mobilization of storage carbon. The parameter $Cbud$, which was optimized, is the amount of storage carbon that is used each day by the plant. The total CT_i amount is then allocated to the canopy, the roots or the stem following some functional rules. In the previous version of MAIDEN (Gea-Izquierdo et al., 2015), these rules were functions of daily soil moisture and air temperature. Here these rules did not improve the simulated results and we retained a simpler version independent from climate:

$$Cstem_i = CT_i \cdot (1 - h3) \quad (5)$$

where $Cstem_i$ is the portion of CT_i allocated to stem and $h3$ is a parameter to be defined in the range between 0 and 1. The rest of CT_i is allocated to the canopy or the roots, respecting a prescribed 1.65 root to canopy mass ratio for black spruce (Czapowskyj et al., 1985; Jenkins et al., 2003).

During the “growth and accumulation phase in summer” (phase 4), CT_i comes only from the photosynthesis and is allocated either to stem growth or storage as a function of climate forcing. In the previous version of MAIDEN for water limited sites (Gea-Izquierdo et al., 2015), the allocation rule used a combination of daily soil moisture and air temperature as predictors. Here for temperature limited sites, we only used temperature and set the soil moisture part to be with a null effect (i.e. always equal to 1, note that for more water limited boreal sites this water stress dependence can be used):

$$Cstem_i = CT_i \cdot \left(1 - 0.8 \cdot \exp \left(-0.5 \left(\frac{Tmax_i}{st4temp} \right)^2 \right) \right) \quad (6)$$

where $Tmax_i$ is the daily maximum temperature and $st4temp$ is a parameter that corresponds to the inflection point of the function. The value 0.8 was chosen to force a minimum threshold of C allocation to the stem in this phase (at least 20%) and to guarantee the correspondence between the inflection point and the temperature where roughly 50% of CT_i is allocated to the stem.

The transition from phase 4 to the “fall phase” (phase 5) is determined by either the parameter $photoper$ (threshold of duration of daylight in hours) or by the occurrence of negative minimum daily temperature values after the 1st of September. During the “fall phase”, all photosynthetic products are allocated to the storage reservoir and mortality of fine roots occurs. No specific functional rule influences $Dstem$ during this phase.

The equation controlling partial carbon losses from the canopy (i.e. litterfall) and thus influencing the photosynthetic capacity through modifications of the total leaf area in the studied evergreen species, runs all year round. This equation is inspired from Maseyk et al. (2008):

$$outCcanopy_i = (PercentFall \cdot AlloCcanopy_j) \cdot \exp \left(-0.5 \left(\frac{DOY_i - 1}{OutMax} \right)^{OutLength} \right) - (PercentFall \cdot AlloCcanopy_j) \cdot \exp \left(-0.5 \left(\frac{DOY_i}{OutMax} \right)^{OutLength} \right) \quad (7)$$

where $outCcanopy_i$ is the carbon loss from the canopy at day i and is influenced by parameters *PercentFall*, *OutMax*, and *OutLength* (to be optimized), which determine the yearly canopy turnover rate, the day of the year with maximum losses and the length of the period with losses, respectively.

2.1.3 Model evaluation

- 5 The proportion of the observed variability explained by MAIDEN was evaluated with the coefficient of determination (R^2), which compares the performance of simulated time series relative to that of straight horizontal lines centered on the data:

$$R^2 = 1 - \frac{\sum_i (Obs_i - Sim_i)^2}{\sum_i (Obs_i - \overline{Obs})^2} \quad (8)$$

2.2 Study sites and data

2.2.1 Eddy covariance observations

- 10 We used daily GPP data from one eddy covariance station located in a mature black spruce forest in the northern Quebec taiga (“Quebec Eastern Old Black Spruce” station - EOBS; 49.69N and 74.34W; data from 2003 to 2010; Bergeron et al., 2007; <http://fluxnet.ornl.gov/site/269>; additional information on Supplement S2 and Fig. S2) to optimize the six parameters influencing the stand GPP simulated by MAIDEN for the studied species.

2.2.2 Ring width data from the northern Quebec taiga

- 15 We assumed that the yearly Dstem is proportional to tree-ring growth in order to use ring width data to optimize MAIDEN (12 influential parameters). A regional chronology (hereafter RW) and a detrended regional chronology (hereafter RWhighF) were obtained from 46 black spruce trees sampled in the riparian forests of five lakes in the eastern Canadian taiga (Gennaretti et al., 2014; the coordinates of the central point are 54.26N and 71.34W; see Fig. S3, Dataset S1 and Supplement S2). RWhighF was then used as a reference for the optimization of the MAIDEN parameters, while observed and simulated
20 low frequencies were only compared after the optimization of the model parameters. MAIDEN outputs were simulated for the central point of the source area of ring width data over the 1950-2010 period.

2.2.3 Climate data

- MAIDEN needs daily climate data as inputs. These data were obtained from the gridded interpolated Canadian database of daily minimum–maximum temperature and precipitation for 1950-2015 (Hutchinson et al., 2009;
25 <http://cfs.nrcan.gc.ca/projects/3/4>). CO₂ atmospheric concentration values for the same period were obtained extrapolating the data from the CarbonTracker measurement and modeling system (2000-2015 period; Peters et al., 2007; <http://www.esrl.noaa.gov/gmd/ccgg/carbontracker/>) and the Mauna Loa observatory (1958-2015; Keeling et al., 1976; <http://www.esrl.noaa.gov/gmd/ccgg/trends/>). Additional information can be found in Supplement S2.

2.3 Response function analysis

Linear response functions are regression models used to quantify the proportion of the variability of the observed data (stem growth or GPP in our case) that can be explained by climate variables. These functions do not directly explore the mechanistic rules such as process-based models and are only optimized to achieve the best fit. Thus, comparing the results of linear functions and process-based models can help verify if model performance is satisfactory and if some important climatic factor related to some process is missing in the model. We used linear response functions to analyze the relationships between observed daily GPP at EOBS and daily mean, maximum and minimum temperatures or weekly precipitation (explored time lag from 0 to 30 days before; in the case of precipitation, lag n indicated the sum of the daily precipitation of the week ending in day n). In this analysis we excluded the winter days (days of the year between November 15th and April 1st) where GPP is zero. The 10 predictors most strongly correlated with GPP (and not highly correlated with each other; pairwise $r \in [-0.8, 0.8]$) were retained for the analysis. All linear response functions, resulting from a combination of these 10 predictors, were tested and classed according to their Bayesian information criterion (BIC).

We also used linear response functions to analyze the relationships between RWhighF and climate variables (same methodology than for GPP). We tested as predictors all monthly temperature and precipitation values of the previous and current years. Time windows of 31 days were used to obtain the time series of monthly data (over the 1950-2010 period) for each day (central day), averaging the values of each window and each year. These climate time series were also detrended such as RWhighF.

3. Results

3.1 GPP and tree-ring growth variability explained by MAIDEN

The optimized model (see parameters' posterior distributions on Figs. S4 and S5) explained a large proportion of the observed GPP daily variability (90%; $r=0.95$, $df=2918$, $p<0.001$; Fig. 2a). Although the model was optimized with daily data, the GPP time series also reproduced the annual variability of the observed data quite well (Fig. 3).

As expected, the ring growth variability at our sites was more linked to temperature than to precipitation variables (see Fig. 4a and Gennaretti et al., 2014; Mamet and Kershaw, 2011; Nicault et al., 2014). The model was able to reproduce this correlation pattern (Fig. 4b) and explained about 20-30% of the observed yearly RWhighF variability corresponding to correlations of 0.58-0.66 ($df=59$, $p<0.001$; Figs. 2b and S6). This is a good result because simulated detrended annual GPP values (i.e. photosynthetic assimilation before any carbon allocation) had only negative R^2 with RWhighF (Fig. 2c; meaning performance worse than a straight line centered on RWhighF) and much lower correlations (Figs. S6 and S7). The variance explained by the model increased importantly when the time series of stem growth were analyzed with their trends ($R^2=0.73$ and $r=0.86$, $df=59$, $p<0.001$; Fig. 5b). Indeed, the positive trend in response to the warming of the last few decades was well captured by the model simulations of stem increments, which included some CO_2 fertilization contribution (Fig. S8).

3.2 Mechanistic and regression-based diagnostics

The modeled impact of temperature on the maximum rate of Rubisco-catalyzed carboxylation (V_{cmax}) is shown in Fig. S9. This figure was obtained using Eq. (1) and (3) with the parameters of Plausible Block GPP and using actual temperature data. The obtained V_{cmax} values (up to 30 $\mu\text{mol C m}^{-2}$ of leaves s^{-1} ; Fig. S9c) were comparable to those obtained for another mature black spruce forest in Saskatchewan, Canada (Rayment et al., 2002). Furthermore, the impact of soil water content on the water stress level (θg) influencing the stomatal conductance is shown in Fig. S10. Simulated GPP values were sensitive to all single parameters controlling V_{cmax} or θg , except *soilb* (Fig. S11-S15). The temperature transformation (S) introduced here in MAIDEN also influenced the simulation results (Fig. 6). With no time delay between photosynthesis and temperature increases (i.e. $\tau = 1$ and $S = T_{day}$) MAIDEN overreacted to temperature variations in spring and the GPP annual cycle was antedated (start in spring and highest summer values were too early). In contrast, the use of S with τ values between 10 and 15 days synchronized the GPP annual cycle with observations. This means that black spruce photosynthetic capacity needs about 10-15 days to acclimate to higher daily temperature (e.g. τ equal to 12.43 days was selected for Plausible Block GPP). This time delay is a little longer than that previously found for black spruce but comparable to values found for Scots pine (Mäkelä et al., 2004; Gea-Izquierdo et al., 2010; Gea-Izquierdo et al., 2014).

We modified important processes for carbon allocation in order to adapt MAIDEN to black spruce. For example, previous year precipitation and temperature values influenced the potential maximum amount of carbon that the canopy can contain during the growing season as illustrated in Fig. 7a (see Eq. (4)). Basically, if both previous April precipitation and July-August temperature indexes are negative, the potential amount of carbon simulated by the model would be maximum, otherwise it would be minimum. This was coherent with the correlations shown in Fig. 4.

Another important process is the start of the growing season. According to our simulations, the start could not happen later than June 17th (Figs. S5d and S16; Table 1) and was influenced by the GDD sum and the photoperiod, which are known to be relevant for black spruce budburst along with the tree provenance (Rossi and Bousquet, 2014). However, because we added a mechanism to smooth yearly variations (see the *day23_flex* parameter), more years were needed by the plants to acclimate to more or less fast GDD accumulations in winter-spring. With the selected parameters to simulate stem growth, the median onset of the growing season was June 10th (similar to observations for black spruce in northern Manitoba, Canada; Bronson et al., 2009) with a standard deviation of 7.8 days. If the smoothing term was excluded, the standard deviation increased to 9.4 days (see Fig. S16a). The inclusion of the smoothed mechanism also decreased the correlation between the simulated detrended annual D_{stem} and May average temperature from 0.70 to 0.59 ($df=58$, $p<0.001$). Although this is still a high correlation, it was closer to the correlation between R_{WhighF} and May temperature ($r=0.27$, $df=58$, $p<0.05$; Fig. 4). These results show how the new model configuration decreased the yearly variability of the growth onset and helped achieving more plausible correlations with climate variables. According to the simulations, the onset of the growing season shifted by 7 days from June 14th to June 7th between the 1950-1970 and 1990-2010 periods (Fig. S16b-c). This result is consistent with the study of Bronson et al. (2009) on the effect of warming on black spruce budburst.

In phase 3, corresponding to Budburst, a portion of the available carbon simulated by MAIDEN comes from stored non-structural carbohydrates from the current and previous years (parameter *Cbud*; see Table 1). In our case, *Cbud* was quantified as about $1.69 \text{ g C} \cdot \text{m}^{-2} \text{ day}^{-1}$ (Fig. S5f) and this remobilization improves the correlations between *Dstem* and *RWhighF* (Fig. S17). During phase 3 in our simulations, almost all available carbon was allocated to the canopy and roots ($h3 \approx 0.9905$; Eq. (5); Fig. S5g; Table 1). For this reason, the previously used soil moisture and temperature dependences, determining the portion of carbon allocated to the stem in Mediterranean evergreen woodlands (Gea-Izquierdo et al., 2015), did not improve the results and could be excluded here. The partition of carbon during the growth and accumulation phase in summer (phase 4) was instead modeled as a function of temperature (Eq. (6)). The simulations were highly sensitive to the *st4temp* parameter (Fig. 8c-d) and warmer temperatures corresponded to a greater amount of carbon allocated to the stem and less to non-structural carbohydrates (Fig. 8a-b). These results are in part in line with those of Cuny et al. (2015), who showed that woody biomass production is low in the first part of the growing season for most coniferous tree species because it follows the seasonal course of temperature (highest peak in summer). The simulated accumulation of carbon to the stem ended each year when the photoperiod became shorter than about 13.41 hours (Fig. S5i; Table 1), corresponding to September 2nd. The model performance was very sensitive to this parameter which is known to impact black spruce dormancy induction (D'aoust and Cameron, 1982).

Another important process for carbon allocation is the definition of the carbon losses from the canopy, a process that influences the seasonal course of the photosynthetic capacity. According to the simulations, the canopy mean annual turnover rate was about 13-14% (Fig. S5j; Table 1), which corresponds well to previously published values for boreal spruce species (Tůpek et al., 2015). The simulated annual cycle of canopy losses (Fig. S18) culminated on July 2nd and 80% of litterfall occurred between May 27th and July 19th. This cycle is also similar to published results showing that the majority of litterfall ($\approx 80\%$) occurs in summer during needle growth for conifer species (Maseyk et al., 2008).

The comparison between MAIDEN simulations and classic linear response functions confirmed the quality and plausibility of the simulated results with the process-based model. MAIDEN performed better than response functions in explaining the variability of daily GPP ($R^2=0.90$ vs 0.69 ; Table 2). In the case of annual radial growth, the explained variability with the best response function (50%; Table 3) was greater than with MAIDEN (20-30%; $r \approx 0.65$, $df=59$, $p<0.001$; Fig. 2b). However, the MAIDEN simulated time series were able to respect the relationship with the significant monthly climate variables detected with the response function analysis. Indeed, correlation coefficients of -0.39 , 0.46 and 0.57 ($df=58$, $p<0.01$) were obtained between MAIDEN *Dstem* ($\text{g C} \cdot \text{m}^{-2} \text{ year}^{-1}$) and previous July-August, growing year July and growing year May-June temperature values, respectively (Fig. 4b; these coefficients are to compare with those in Table 3).

4. Discussion

4.1 Parameter interpretation

The posterior distributions of the parameters were quite sharp (Figs. S4 and S5; Table 1; by sharpness we mean the shrinking of the distribution relative to the prior acceptable range toward a posterior distribution with a well-defined, narrow peak). Sharp distributions with small posterior ranges relative to the prior ones indicate sensitive parameters. This means that the model posterior probability (i.e. model plausibility) increased significantly with the specific values of the selected parameters retained by the MCMC sampling. The slightly bimodal structures of the posterior distributions of V_{max} , V_b and V_{ip} were likely a consequence of their significant cross-correlations (Table S1). However, the posterior distributions of these three parameters were robust and consistent even when the Bayesian optimization was executed on independent periods (Fig. S19). The optimization of some parameters controlling D_{stem} (the three related to the start of the growing season and C_{bud}) was sensitive to the choice of the period and the site in the cross-validation exercise (Figs. S20 and S21) likely as a result of the short length of the available observed data (61 yearly R_{WhigF} values) and of some significant cross-correlation coefficients (Table S2). However, in all cases, the uncertainties in the parameters' posterior distributions (Figs. S4 and S5) did not affect our interpretations because the MAIDEN simulations were extremely consistent whatever the selected block of parameters (see Figs. 3 and 5).

The interpretation of some parameters needs special care. For example, those controlling the negative impact of both previous year April precipitation and July-August temperature values on canopy development, which may be explained by the following reasons: warm previous Aprils with infrequent late snowfalls may accelerate snowmelt and the start of the previous growing season, allowing optimal reserve accumulation during the previous year which would influence tree performance the following growing year. This mechanism may be significant especially if we do not observe high temperatures limiting soil water availability and reserve accumulation during the previous summer (Girardin et al., 2016). It has already been shown that shoot elongation of boreal conifers is determined by climate conditions during bud formation (Salminen and Jalkanen, 2005). However, for Scots pine, previous summer temperatures are positively correlated with shoot elongation, while in our case, the opposite process was simulated and the simulations were even more sensitive to the values of the $CanopyT$ temperature dependent parameter than to those of the $CanopyP$ precipitation dependent parameter (Fig. 7b-e). Clearly, we need more data on canopy development and shoot elongation to verify the model results.

4.2 Interpretation of the model performance

The comparisons with the observed data suggest that MAIDEN as revised produces accurate simulations of GPP, of ring width and stem biomass variability and of intra-growing season dynamics. The explained variance ($R^2=0.73$ and $r=0.86$, $df=59$, $p<0.001$; Fig. 5b) is even higher than that explained by MAIDEN for Mediterranean sites (R^2 slightly above 0.5; Gea-Izquierdo et al., 2015). However, the ensembles of daily and annual time series retained by the MCMC sampling were not always centered on the observed time series (Figs. 3 and 5), in particular the simulated annual GPP values often

underestimated the actual GPP especially at low observed GPP. This reflects the fact that the MCMC sampling maximized the model plausibility according to the model structure and, by doing so retained similar blocks of parameters. Thus, the range of simulated values in Figs. 3 and 5, obtained with all retained iterations, should be interpreted as the uncertainty due only to parameter selection while the uncertainty due to the non-perfect fit between observations and simulations was not taken into account.

We were able to draw the following conclusions by the response function analysis (Tables 2 and 3). In the case of daily GPP, first, MAIDEN performed better than response functions, suggesting that it properly simulates climate-driven processes governing photosynthetic assimilation, which are well known to be a result of several non-linear processes. Second, most of the variance explained by the response functions was due to temperature variables, reflecting the greater sensitivity of northern black spruce forests to temperature as compared to drought stress (Gennaretti et al., 2014) and justifying the modeling in MAIDEN of the maximum carboxylation rate as a function of temperature. Third, only temperature variables of preceding days were retained, justifying the inclusion of our acclimation function of photosynthesis to temperature in order to increase the influence of previous days. Fourth, the coefficient estimate for precipitation of lag 0 (i.e. week ending in day 0) was negative, while the one of lag -2 was positive, even though these variables share 5 out of 7 days of data. The reduction of absorbed photosynthetically active radiation associated to cloudiness during raining days could explain this result. In the case of annual stem growth, the explained variability with the best response function was greater than with MAIDEN, suggesting that the process-based modeling can potentially be improved with additional data and including stronger legacy effects of the year preceding ring formation (Girardin et al., 2016). Indeed, most of the variance explained by the response function was due to a negative correlation with the temperature of the previous summer. Contrasting correlations with summer temperature values of the previous and the current growing year are also visible in Fig. 4a and have already been observed for black spruce (Mamet and Kershaw, 2011; Ols et al., 2016).

4.3 Some model predictions

It is possible to use the new optimized MAIDEN version to predict forest growth and allocation dynamics of the studied boreal forests under future environmental change. In the study area, the daily maximum temperature, the daily minimum temperature and the precipitation should increase at the 2050 horizon of about 2.3°C, 4.3°C and 12%, respectively (Guay et al., 2015). If we modify the used climatic data (Section 2.2.3) by these median changes and we fix the CO₂ concentration at the 2010 level, the median increase of the annual GPP and Dstem values simulated by MAIDEN for the studied forests is of 43 and 68%, respectively (Fig. S22). We have to recall that the ring width data used for the optimization of MAIDEN come from lake riparian trees and that these results are too optimistic for more water limited boreal sites.

4.4 Limits and error sources of the study

Although the simulated results with MAIDEN were satisfactory, we have to consider two important limits and error sources of the study. First, for the optimization of carbon allocation, we assumed that stem biomass (or carbon) increments were

proportional to ring growth. This was necessary because data from field plots were not available from all study sites. A recent study showed that the maximum rate of ring width increase during the growing season precedes the maximum rate of increase in wood biomass and that these processes could exhibit differential sensitivities to local environmental conditions (Cuny et al., 2015). However, Cuny et al. (2015) also highlighted that wood biomass production follows the seasonal course of temperature in coniferous forests and this is exactly what we got once MAIDEN was optimized. Indeed, almost all available carbon in spring was allocated to the canopy and roots (Fig. S5g; Table 1), whereas C allocation to the stem (Dstem) in summer increased with temperature (Fig. 8). Furthermore, the used ring width series were highly correlated with July-August temperature as expected for wood biomass production and for climate-growth analysis for the studied species. **Second, some fixed parameters are present in the MAIDEN code (see Eqs. 4 and 6). These parameters might be potentially tuned but their specification is justified in Section 2.1.2 and limits additional parameter tuning.** Third, we modeled GPP and carbon stem increments of a boreal tree species using mechanistic rules which increased the capability of MAIDEN to reproduce observed variations. However, our choice of mechanistic rules was subjective in part and depended on previous physiological knowledge and on model-data comparisons. Such model refining is an important step of all model-data fusion approaches (Guiot et al., 2014) and increases our understanding of ecosystem functioning and responses. Nevertheless, the proposed mechanistic rules should be verified in the future with additional data from a wider boreal area.

5. Conclusion

In this study, we adapted a process-based forest ecophysiological model, developed for temperate and Mediterranean forests, to simulate gross primary production and stem biomass increment for black spruce, the dominant species across the North American boreal forest. The model used, MAIDEN (Misson, 2004; Gea-Izquierdo et al., 2015), has the specificity to simultaneously simulate the course of photosynthesis and phenological phases characterized by specific allocation rules dependent on climatic conditions. The model was able to represent the tree-ring inter-annual variability even though detrended radial growth was poorly explained by the simulated annual GPP (Fig. 2b-c), which suggests that the relationship between GPP and wood production is complex and non-linear (Rocha et al., 2006). Significant simulation improvements were obtained introducing in the model important processes for temperature sensitive boreal forests, such as: (i) the acclimation of photosynthesis to temperature over several days (see Gea-Izquierdo et al., 2010; Mäkelä et al., 2004); (ii) the influence of previous year climatic conditions affecting bud formation on the potential amount of carbon allocated to the canopy each year (see Salminen and Jalkanen, 2005); (iii) the positive relationship between temperature and the carbon allocated to the stem in summer (see Cuny et al., 2015). Although we used black spruce data from the northern Quebec taiga to test and optimize the model, the new model modifications have the potential to work within other boreal regions and tree species. Indeed, the effect of the introduced functions can be amplified, reduced or canceled out in the Bayesian optimization procedure according to the relevance of specific processes in the studied forest.

Boreal ecosystems are crucial carbon stores that must be urgently quantified and preserved (Bradshaw et al., 2009). Their future evolution is extremely important for the global carbon budget. Development of process-based models, such as the one used and improved here, combined with continuous field data acquisition, will help disentangle the role of the different environmental factors and underneath mechanisms on present and future boreal forest carbon fluxes. In this context, we believe that our study helps to understand how boreal forests assimilate and allocate carbon depending on weather/climate conditions.

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References

- 15 Bergeron, O., Margolis, H. A., Black, T. A., Coursolle, C., Dunn, A. L., Barr, A. G., and Wofsy, S. C.: Comparison of carbon dioxide fluxes over three boreal black spruce forests in Canada, *Glob. Change Biol.*, 13, 89-107, doi:10.1111/j.1365-2486.2006.01281.x, 2007.
- Berninger, F., Hari, P., Nikinmaa, E., Lindholm, M., and Meriläinen, J.: Use of modeled photosynthesis and decomposition to describe tree growth at the northern tree line, *Tree Physiol.*, 24, 193-204, doi:https://doi.org/10.1093/treephys/24.2.193, 2004.
- 20 Bond-Lamberty, B., Wang, C., and Gower, S. T.: Aboveground and belowground biomass and sapwood area allometric equations for six boreal tree species of northern Manitoba, *Can. J. Forest Res.*, 32, 1441-1450, doi:10.1139/x02-063, 2002a.
- Bond-Lamberty, B., Wang, C., Gower, S. T., and Norman, J.: Leaf area dynamics of a boreal black spruce fire chronosequence, *Tree Physiol.*, 22, 993-1001, doi:https://doi.org/10.1093/treephys/22.14.993, 2002b.
- 25 Boucher, É., Guiot, J., Hatté, C., Daux, V., Danis, P. A., and Dussouillez, P.: An inverse modeling approach for tree-ring-based climate reconstructions under changing atmospheric CO₂ concentrations, *Biogeosciences*, 11, 3245-3258, doi:10.5194/bg-11-3245-2014, 2014.
- Bradshaw, C. J. A., Warkentin, I. G., and Sodhi, N. S.: Urgent preservation of boreal carbon stocks and biodiversity, *Trends Ecol. Evol.*, 24, 541-548, doi:10.1016/j.tree.2009.03.019, 2009.
- 30

- Bronson, D. R., Gower, S. T., Tanner, M., and Van Herk, I.: Effect of ecosystem warming on boreal black spruce bud burst and shoot growth, *Glob. Change Biol.*, 15, 1534-1543, doi:10.1111/j.1365-2486.2009.01845.x, 2009.
- Chen, J. M.: Optically-based methods for measuring seasonal variation of leaf area index in boreal conifer stands, *Agr. Forest Meteorol.*, 80, 135-163, doi:http://dx.doi.org/10.1016/0168-1923(95)02291-0, 1996.
- 5 Cuny, H. E., Rathgeber, C. B. K., Frank, D., Fonti, P., Makinen, H., Prislan, P., Rossi, S., Del Castillo, E. M., Campelo, F., Vavrci, H., Camarero, J. J., Bryukhanova, M. V., Jyske, T., Gricar, J., Gryc, V., De Luis, M., Vieira, J., Cufar, K., Kirdyanov, A. V., Oberhuber, W., Treml, V., Huang, J. G., Li, X., Swidrak, I., Deslauriers, A., Liang, E., Nojd, P., Gruber, A., Nabais, C., Morin, H., Krause, C., King, G., and Fournier, M.: Woody biomass production lags stem-girth increase by over one month in coniferous forests, *Nature Plants*, 1, 1-6, doi:10.1038/nplants.2015.160, 2015.
- 10 Czapowskyj, M. M., Robinson, D. J., Briggs, R. D., and White, E. H.: Component biomass equations for black spruce in Maine, USDA, Forest Service, Northeastern Forest Experiment Station, Research report NE-564, 1985.
- D'aoust, A. L., and Cameron, S. I.: The effect of dormancy induction, low temperatures and moisture stress on cold hardening of containerized black spruce seedlings, in: *Proceedings of the Canadian Containerized Tree Seedling Symposium*, Toronto, Ontario, 14-16 September 1981, 153-161, 1982.
- 15 Danis, P. A., Hatté, C., Misson, L., and Guiot, J.: MAIDENiso: a multiproxy biophysical model of tree-ring width and oxygen and carbon isotopes, *Can. J. Forest Res.*, 42, 1697-1713, doi:10.1139/x2012-089, 2012.
- De Pury, D. G. G., and Farquhar, G. D.: Simple scaling of photosynthesis from leaves to canopies without the errors of big-leaf models, *Plant Cell Environ.*, 20, 537-557, doi:10.1111/j.1365-3040.1997.00094.x, 1997.
- Fatichi, S., Leuzinger, S., and Körner, C.: Moving beyond photosynthesis: from carbon source to sink-driven vegetation modeling, *New Phytol.*, 201, 1086-1095, doi:10.1111/nph.12614, 2014.
- 20 Gaucherel, C., Campillo, F., Misson, L., Guiot, J., and Boreux, J. J.: Parameterization of a process-based tree-growth model: Comparison of optimization, MCMC and Particle Filtering algorithms, *Environ. Modell. Softw.*, 23, 1280-1288, doi:10.1016/j.envsoft.2008.03.003, 2008a.
- Gaucherel, C., Guiot, J., and Misson, L.: Changes of the potential distribution area of French Mediterranean forests under global warming, *Biogeosciences*, 5, 1493-1504, doi:10.5194/bg-5-1493-2008, 2008b.
- 25 Gea-Izquierdo, G., Mäkelä, A., Margolis, H., Bergeron, Y., Black, T. A., Dunn, A., Hadley, J., Paw U, K. T., Falk, M., Wharton, S., Monson, R., Hollinger, D. Y., Laurila, T., Aurela, M., McCaughey, H., Bourque, C., Vesala, T., and Berninger, F.: Modeling acclimation of photosynthesis to temperature in evergreen conifer forests, *New Phytol.*, 188, 175-186, doi:10.1111/j.1469-8137.2010.03367.x, 2010.
- 30 Gea-Izquierdo, G., Bergeron, Y., Huang, J. G., Lapointe-Garant, M. P., Grace, J., and Berninger, F.: The relationship between productivity and tree-ring growth in boreal coniferous forests, *Boreal Environ. Res.*, 19, 363-378, 2014.
- Gea-Izquierdo, G., Guibal, F., Joffre, R., Ourcival, J. M., Simioni, G., and Guiot, J.: Modelling the climatic drivers determining photosynthesis and carbon allocation in evergreen Mediterranean forests using multiproxy long time series, *Biogeosciences*, 12, 3695-3712, doi:10.5194/bg-12-3695-2015, 2015.

- Gea-Izquierdo, G., Nicault, A., Battipaglia, G., Dorado-Liñán, I., Gutiérrez, E., Ribas, M., and Guiot, J.: Risky future for Mediterranean forests unless they undergo extreme carbon fertilization, *Glob. Change Biol.*, 23, 2915–2927, doi:10.1111/gcb.13597, 2017.
- 5 Gennaretti, F., Arseneault, D., Nicault, A., Perreault, L., and Bégin, Y.: Volcano-induced regime shifts in millennial tree-ring chronologies from northeastern North America, *P. Natl. Acad. Sci. USA*, 111, 10077-10082, doi:10.1073/pnas.1324220111, 2014.
- Girardin, M. P., Raulier, F., Bernier, P. Y., and Tardif, J. C.: Response of tree growth to a changing climate in boreal central Canada: A comparison of empirical, process-based, and hybrid modelling approaches, *Ecol. Model.*, 213, 209-228, doi:http://dx.doi.org/10.1016/j.ecolmodel.2007.12.010, 2008.
- 10 Girardin, M. P., Hogg, E. H., Bernier, P. Y., Kurz, W. A., Guo, X. J., and Cyr, G.: Negative impacts of high temperatures on growth of black spruce forests intensify with the anticipated climate warming, *Glob. Change Biol.*, 22, 627–643 doi:10.1111/gcb.13072, 2016.
- Guay, C., Minville, M., and Braun, M.: A global portrait of hydrological changes at the 2050 horizon for the province of Québec, *Canadian Water Resources Journal / Revue canadienne des ressources hydriques*, 40, 285-302, doi:10.1080/07011784.2015.1043583, 2015.
- 15 Guiot, J., Boucher, E., and Gea Izquierdo, G.: Process models and model-data fusion in dendroecology, *Frontiers in Ecology and Evolution*, 2, Article 52, doi:10.3389/fevo.2014.00052, 2014.
- Hutchinson, M. F., McKenney, D. W., Lawrence, K., Pedlar, J. H., Hopkinson, R. F., Milewska, E., and Papadopol, P.: Development and testing of Canada-wide interpolated spatial models of daily minimum-maximum temperature and precipitation for 1961-2003, *J. Appl. Meteorol. Clim.*, 48, 725-741, doi:10.1175/2008jamc1979.1, 2009.
- 20 Jenkins, J. C., Chojnacky, D. C., Heath, L. S., and Birdsey, R. A.: National-Scale Biomass Estimators for United States Tree Species, *Forest Sci.*, 49, 12-35, 2003.
- Keeling, C. D., Bacastow, R. B., Bainbridge, A. E., Ekdahl, C. A., Guenther, P. R., Waterman, L. S., and Chin, J. F. S.: Atmospheric carbon dioxide variations at Mauna Loa Observatory, Hawaii, *Tellus*, 28, 538-551, doi:10.1111/j.2153-3490.1976.tb00701.x, 1976.
- 25 Kirdyanov, A., Hughes, M., Vaganov, E., Schweingruber, F., and Silkin, P.: The importance of early summer temperature and date of snow melt for tree growth in the Siberian Subarctic, *Trees-Struct. Funct.*, 17, 61-69, doi:10.1007/s00468-002-0209-z, 2003.
- Lemieux, J.: Phénologie de l'épinette noire dans le haut boréal : un patron de la croissance intra-annuelle primaire et secondaire en relation avec la température de l'air journalière, Master of Biology, Université du Québec à Montréal, Montreal, 90 pp., 2010.
- 30 Leuning, R.: A critical appraisal of a combined stomatal-photosynthesis model for C3 plants, *Plant Cell Environ.*, 18, 339-355, doi:10.1111/j.1365-3040.1995.tb00370.x, 1995.

- Li, G., Harrison, S. P., Prentice, I. C., and Falster, D.: Simulation of tree ring-widths with a model for primary production, carbon allocation and growth, *Biogeosciences*, 11, 10451-10485, doi:10.5194/bgd-11-10451-2014, 2014.
- Li, G., Harrison, S. P., and Prentice, I. C.: A model analysis of climate and CO₂ controls on tree growth and carbon allocation in a semi-arid woodland, *Ecol. Model.*, 342, 175-185, doi:http://dx.doi.org/10.1016/j.ecolmodel.2016.10.005, 2016.
- Mäkelä, A., Berninger, F., and Hari, P.: Optimal control of gas exchange during drought: Theoretical analysis, *Ann. Bot.-London*, 77, 461-467, doi:10.1006/anbo.1996.0056, 1996.
- Mäkelä, A., Hari, P., Berninger, F., Hänninen, H., and Nikinmaa, E.: Acclimation of photosynthetic capacity in Scots pine to the annual cycle of temperature, *Tree Physiol.*, 24, 369-376, doi:10.1093/treephys/24.4.369, 2004.
- Mamet, S. D., and Kershaw, G. P.: Radial-Growth Response of Forest-Tundra Trees to Climate in the Western Hudson Bay Lowlands, Arctic, 64, 446-458, 2011.
- Man, R., and Lu, P.: Effects of thermal model and base temperature on estimates of thermal time to bud break in white spruce seedlings, *Can. J. Forest Res.*, 40, 1815-1820, doi:10.1139/X10-129, 2010.
- Maseyk, K. S., Lin, T., Rotenberg, E., Grünzweig, J. M., Schwartz, A., and Yakir, D.: Physiology-phenology interactions in a productive semi-arid pine forest, *New Phytol.*, 178, 603-616, doi:10.1111/j.1469-8137.2008.02391.x, 2008.
- Misson, L.: MAIDEN: a model for analyzing ecosystem processes in dendroecology, *Can. J. Forest Res.*, 34, 874-887, doi:10.1139/x03-252, 2004.
- Misson, L., Rathgeber, C., and Guiot, J.: Dendroecological analysis of climatic effects on *Quercus petraea* and *Pinus halepensis* radial growth using the process-based MAIDEN model, *Can. J. Forest Res.*, 34, 888-898, doi:10.1139/x03-253, 2004.
- Moorcroft, P. R.: How close are we to a predictive science of the biosphere?, *Trends Ecol. Evol.*, 21, 400-407, doi:10.1016/j.tree.2006.04.009, 2006.
- Nicault, A., Boucher, E., Tapsoba, D., Arseneault, D., Berninger, F., Bégin, C., DesGranges, J. L., Guiot, J., Marion, J., Wicha, S., and Bégin, Y.: Spatial analysis of the black spruce (*Picea mariana* [MILL] B.S.P.) radial growth response to climate in northern Québec, Canada, *Can. J. Forest Res.*, 45, 343-352, doi:10.1139/cjfr-2014-0080, 2014.
- Nitschke, C. R., and Innes, J. L.: A tree and climate assessment tool for modelling ecosystem response to climate change, *Ecol. Model.*, 210, 263-277, doi:http://dx.doi.org/10.1016/j.ecolmodel.2007.07.026, 2008.
- Ols, C., Hofgaard, A., Bergeron, Y., and Drobyshev, I.: Previous season climate controls the occurrence of black spruce growth anomalies in boreal forests of Eastern Canada, *Can. J. Forest Res.*, 46, 696-705, doi:10.1139/cjfr-2015-0404, 2016.
- Peters, W., Jacobson, A. R., Sweeney, C., Andrews, A. E., Conway, T. J., Masarie, K., Miller, J. B., Bruhwiler, L. M. P., Pétron, G., Hirsch, A. I., Worthy, D. E. J., van der Werf, G. R., Randerson, J. T., Wennberg, P. O., Krol, M. C., and Tans, P. P.: An atmospheric perspective on North American carbon dioxide exchange: CarbonTracker, *P. Natl. Acad. Sci. USA*, 104, 18925-18930, doi:10.1073/pnas.0708986104, 2007.

- Rayment, M. B., Loustau, D., and Jarvis, P. J.: Photosynthesis and respiration of black spruce at three organizational scales: shoot, branch and canopy, *Tree Physiol.*, 22, 219-229, doi:10.1093/treephys/22.4.219, 2002.
- Robert, C.: Méthodes de Monte Carlo par chaînes de Markov, *Statistique mathématique et Probabilité*, edited by: Deheuvels, P., Economica, Paris, 1996.
- 5 Rocha, A. V., Goulden, M. L., Dunn, A. L., and Wofsy, S. C.: On linking interannual tree ring variability with observations of whole-forest CO₂ flux, *Glob. Change Biol.*, 12, 1378-1389, doi:10.1111/j.1365-2486.2006.01179.x, 2006.
- Rossi, S., and Bousquet, J.: The bud break process and its variation among local populations of boreal black spruce, *Frontiers in Plant Science*, 5, Article 574, doi:10.3389/fpls.2014.00574, 2014.
- Rossi, S., Anfodillo, T., Čufar, K., Cuny, H. E., Deslauriers, A., Fonti, P., Frank, D., Gričar, J., Gruber, A., Huang, J.-G.,
10 Jyske, T., Kašpar, J., King, G., Krause, C., Liang, E., Mäkinen, H., Morin, H., Nöjd, P., Oberhuber, W., Prislan, P., Rathgeber, C. B. K., Saracino, A., Swidrak, I., and Treml, V.: Pattern of xylem phenology in conifers of cold ecosystems at the Northern Hemisphere, *Glob. Change Biol.*, 22, 3804-3813, doi:10.1111/gcb.13317, 2016.
- Salminen, H., and Jalkanen, R.: Modelling the effect of temperature on height increment of Scots pine at high latitudes, *Silva Fenn.*, 39, 497-508, doi:10.14214/sf.362, 2005.
- 15 Schiestl-Aalto, P., Kulmala, L., Mäkinen, H., Nikinmaa, E., and Mäkelä, A.: CASSIA - a dynamic model for predicting intra-annual sink demand and interannual growth variation in Scots pine, *New Phytol.*, 206, 647-659, doi:10.1111/nph.13275, 2015.
- Šupek, B., Mäkipää, R., Heikkinen, J., Peltoniemi, M., Ukonmaanaho, L., Hokkanen, T., Nöjd, P., Nevalainen, S., Lindgren, M., and Lehtonen, A.: Foliar turnover rates in Finland--comparing estimates from needle-cohort and litterfall-biomass
20 methods, *Boreal Environ. Res.*, 20, 283-304, 2015.
- Vaganov, E. A., Hughes, M. K., and Shashkin, A. V.: *Growth Dynamics of Conifer Tree Rings*, *Ecological Studies*, Springer, Berlin and Heidelberg, 354 pp., 2006.
- Zweifel, R., Haeni, M., Buchmann, N., and Eugster, W.: Are trees able to grow in periods of stem shrinkage?, *New Phytol.*, 211, 839-849, doi:10.1111/nph.13995, 2016.

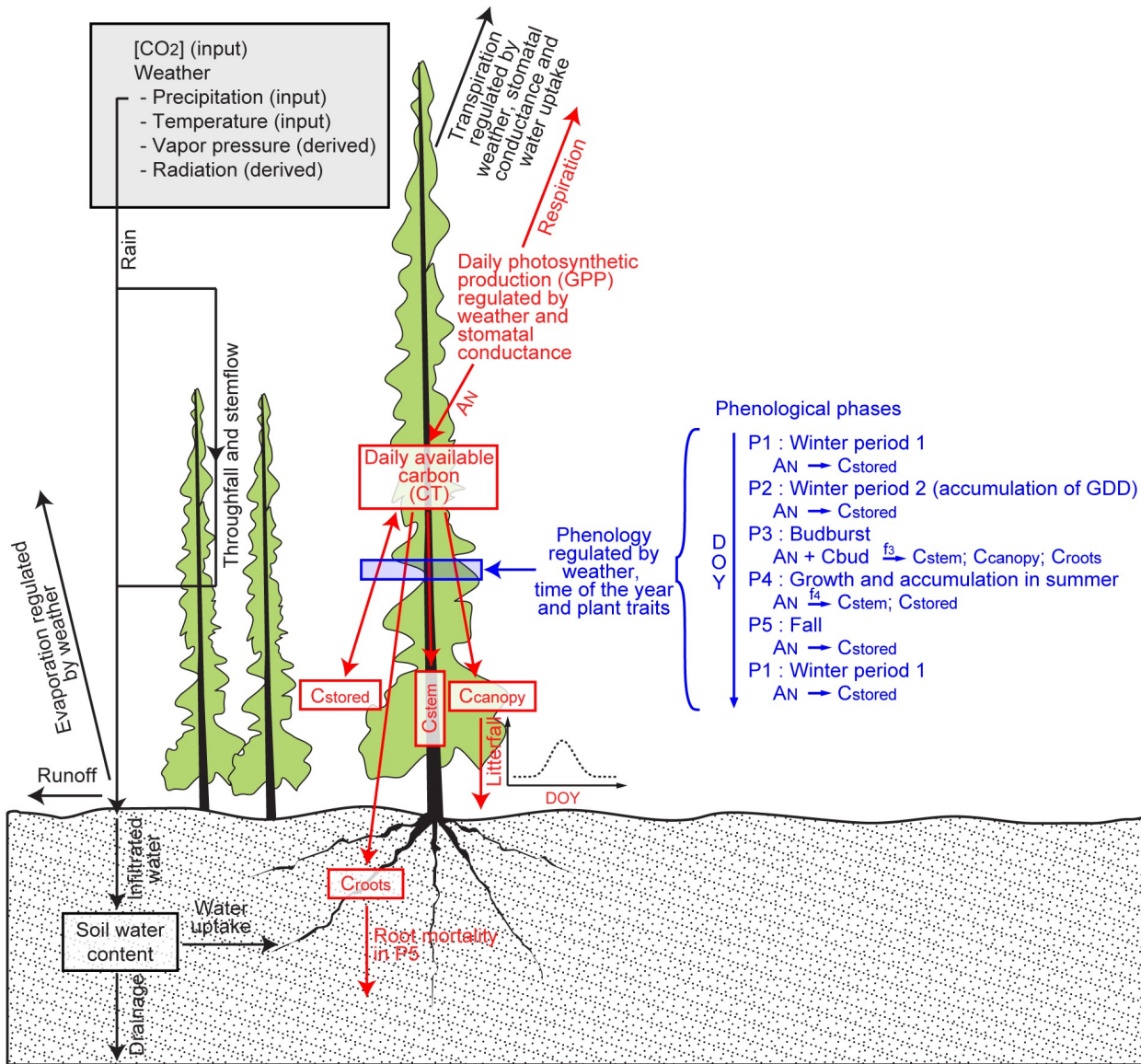


Figure 1: MAIDEN simulated phenology (blue), water (black) and carbon (red) fluxes. AN: net photosynthesis corresponding to net primary production. C_{stored}, C_{stem}, C_{canopy}, C_{roots}: carbon allocated daily to stored non-structural carbohydrates, stem, canopy or roots. DOY: day of the year (1-365). GDD: growing degree days. f₃ and f₄: functions determining carbon allocation in phase 3 and 4. C_{bud}: amount of storage carbon that is used each day by the plant in phase 3.

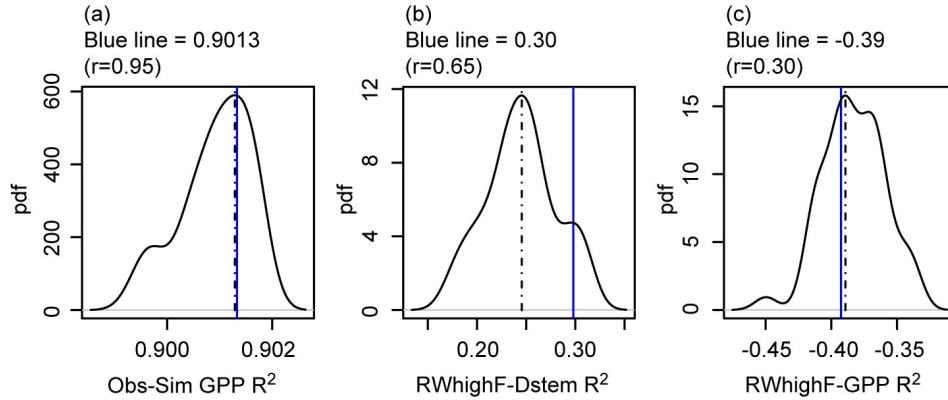


Figure 2: Variance explained by the model. (a) R^2 between observed and simulated GPP daily values. R^2 (computed on data transformed to z-scores) between the mean of the detrended series of black spruce ring growth (RWhighF) and simulated yearly detrended C allocation to the stem (b) or GPP (c). Vertical dashed line is the mode and blue line is the value with Plausible Block GPP (in (a)) or with Plausible Block Stem (in (b) and (c)). All pdfs are based on 50 simulations.

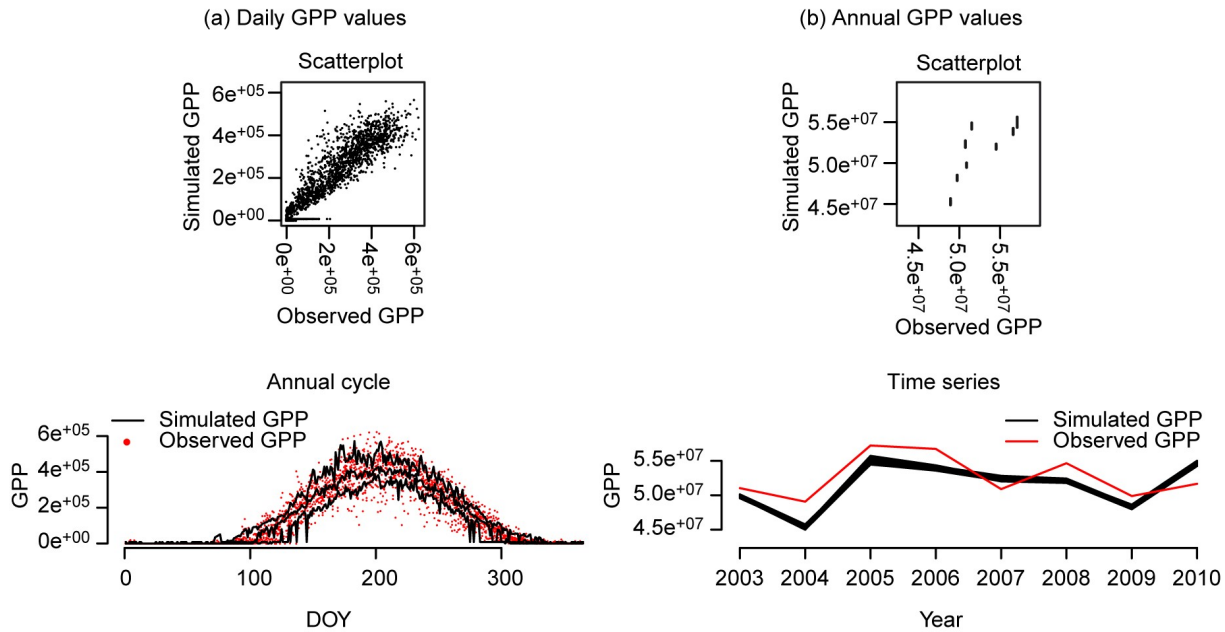


Figure 3: Comparison between observed GPP values and MAIDEN simulated values at the Quebec Eastern Old Black Spruce site. (a) Daily values (units are $\mu\text{mol C m}^{-2} \text{ day}^{-1}$). In the scatterplot ($R^2=0.90$; $r=0.95$, $df=2918$, $p<0.001$), observations are compared with the values obtained with Plausible Block GPP. In the annual cycle plot, black lines are the medians, the 5th and the 95th percentiles of the simulated values from all iterations retained by the MCMC sampling. (b) Annual values (units are $\mu\text{mol C m}^{-2} \text{ year}^{-1}$). In both plots, observations are compared with the values from all iterations retained by the MCMC sampling. In the scatterplot, the R^2 of the data is 0.31 ($r=0.76$, $df=6$, $p<0.05$).

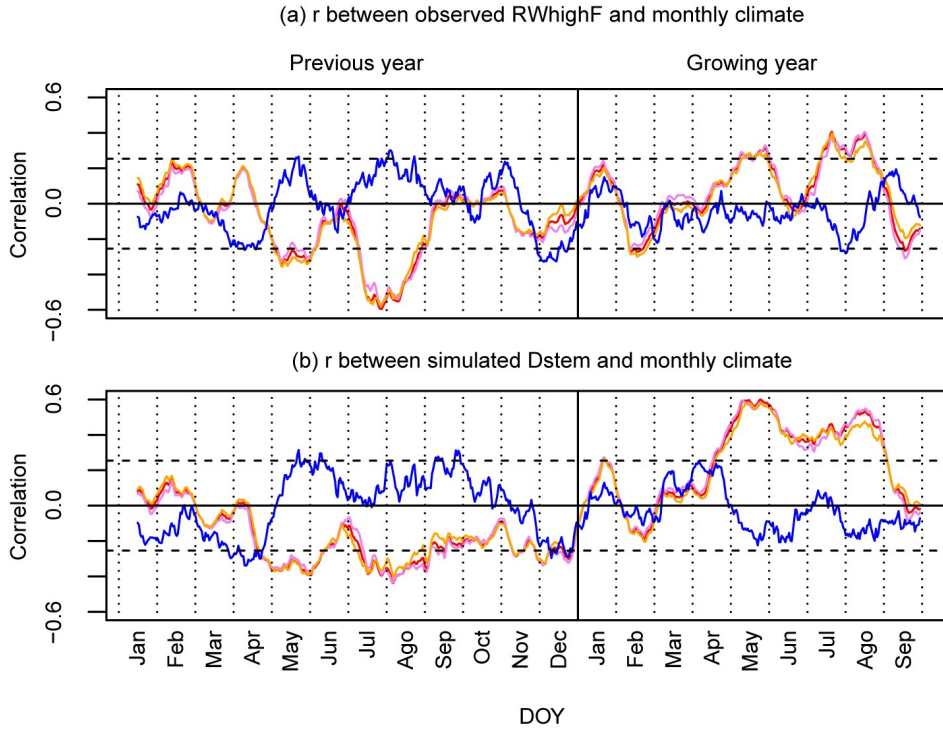


Figure 4: Correlation between monthly climate variables of the study area (precipitation in blue and mean, maximum and minimum temperature in red, violet and orange respectively) and the mean of the detrended series of black spruce ring growth (RWhighF; a) or the simulated detrended annual carbon allocation to the stem (Dstem; b). For the climate variables, time windows of 31 days are used to obtain time series of monthly data (over the 1950-2010 period) for each day (central day), averaging the values of each window and each year. These climate time series are then also detrended. Thresholds of significance ($p < 0.05$) are shown by horizontal dashed lines.

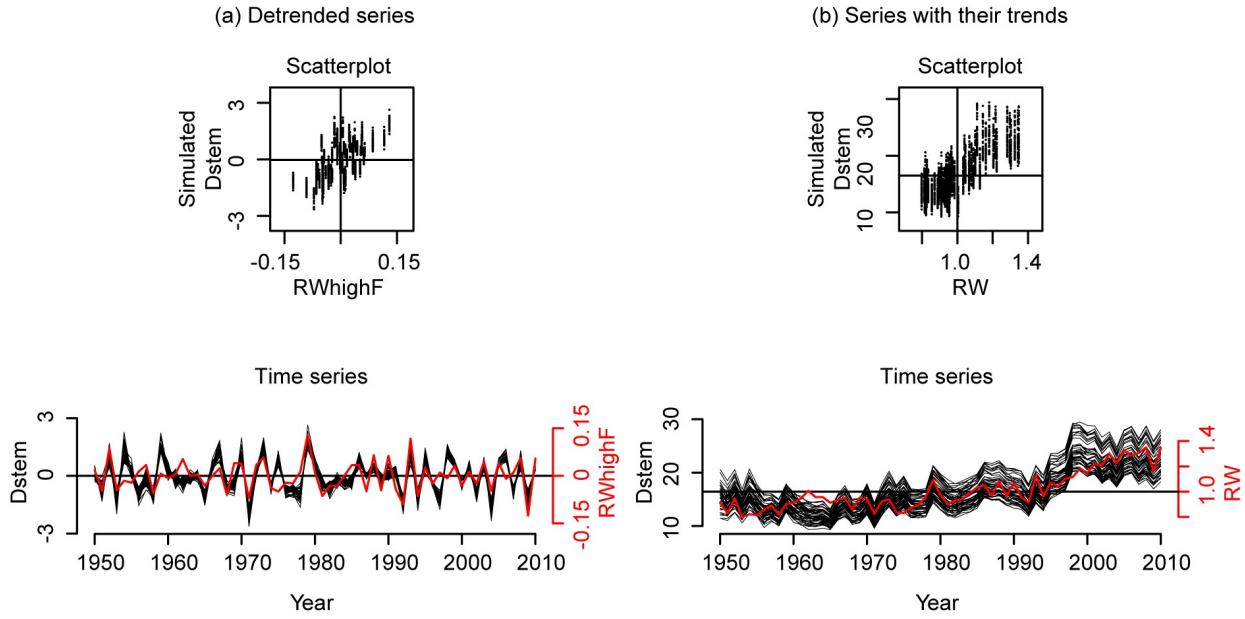


Figure 5: Comparison between the observed mean series of black spruce ring growth (unitless growth indexes) and MAIDEN simulated carbon allocation to stem (Dstem; $\text{g C m}^{-2} \text{ year}^{-1}$). (a) Detrended series (in the scatterplot the R^2 computed on data transformed to z-scores is 0.24; $r=0.62$, $df=59$, $p<0.001$). (b) Series with their trends (in the scatterplot the R^2 is 0.73; $r=0.86$, $df=59$, $p<0.001$). In all plots, observations are compared with the values from all iterations retained by the MCMC sampling.

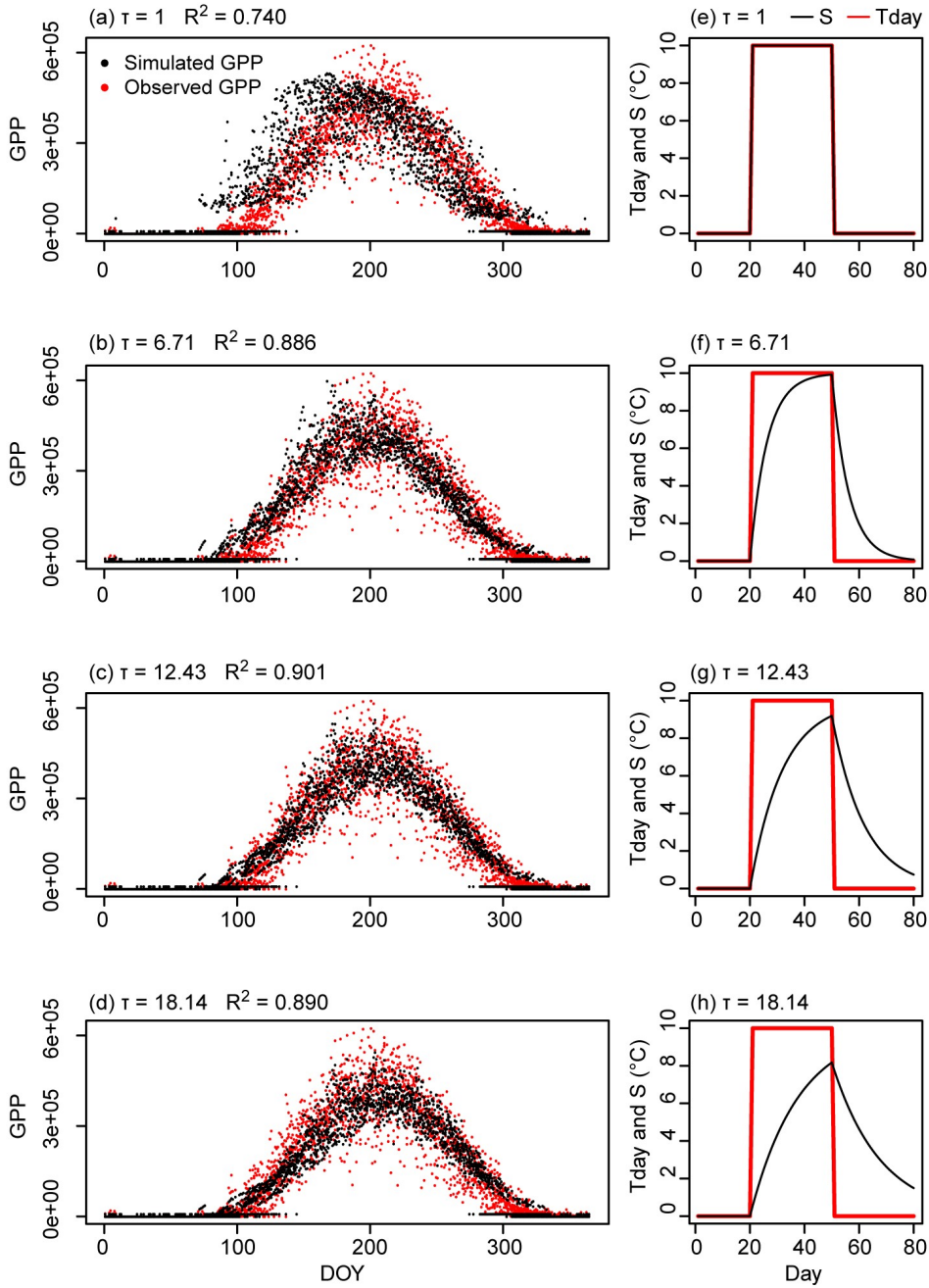


Figure 6: Influence of the temperature transformation (S) on the modeled annual cycle of GPP daily values ($\text{umol C m}^{-2} \text{ day}^{-1}$) at the Quebec Eastern Old Black Spruce site. Only the τ parameter determining the S values was allowed to vary, while the other parameters were fixed to the values of Plausible Block GPP. (a) τ is 1 day (S same as T_{day}). (b) τ is 6.71 days (a middle value between 1 and 12.43). (c) τ is 12.43 days (same τ than in Plausible Block GPP). (d) τ is 18.14 days (a higher value than in Plausible Block GPP). The R^2 between observations and simulations is reported in each plot. Plots e-h show the impact of the respective τ values on S if the daily T_{day} time series corresponds to a single step of 10°C lasting 30 days.

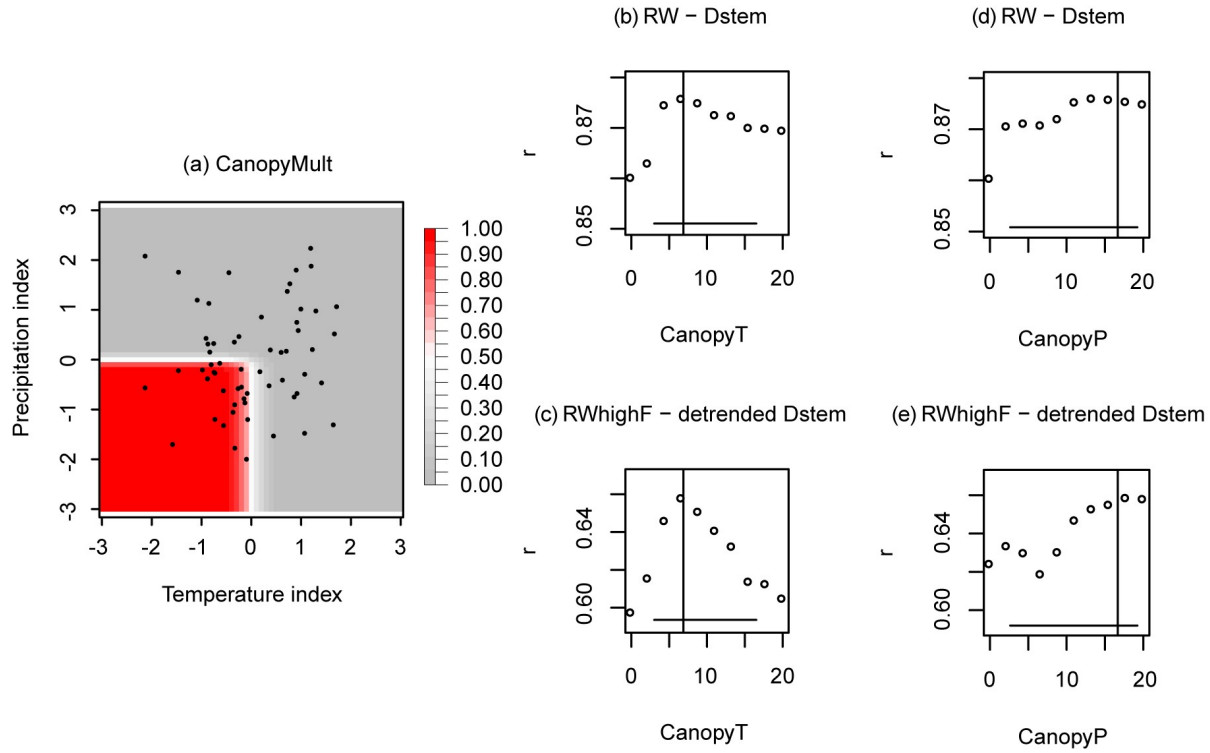


Figure 7: Temperature and precipitation dependence of *CanopyMult* (plot a; unitless multiplier; Eq. (4); *CanopyT* and *CanopyP* are those of Plausible Block Stem), which determines the yearly canopy potential amount of carbon. Previous year mean July-August temperature indexes are on the x-axis and previous year April precipitation indexes are on the y-axis. Black dots are observed values in the central point of the region with ring width data. Plots b-e show how *CanopyT* and *CanopyP* (varying over their prior acceptable ranges) impact the correlations between simulated Dstem ($\text{g C m}^{-2} \text{ year}^{-1}$) and observed ring width data (RW or RWHighF; unitless indexes), when all other parameters are fixed to the values of Plausible Block Stem. The vertical lines are the selected values for Plausible Block Stem and the horizontal lines are the 90% confidence intervals based on the parameters' posterior densities (Fig. S5).

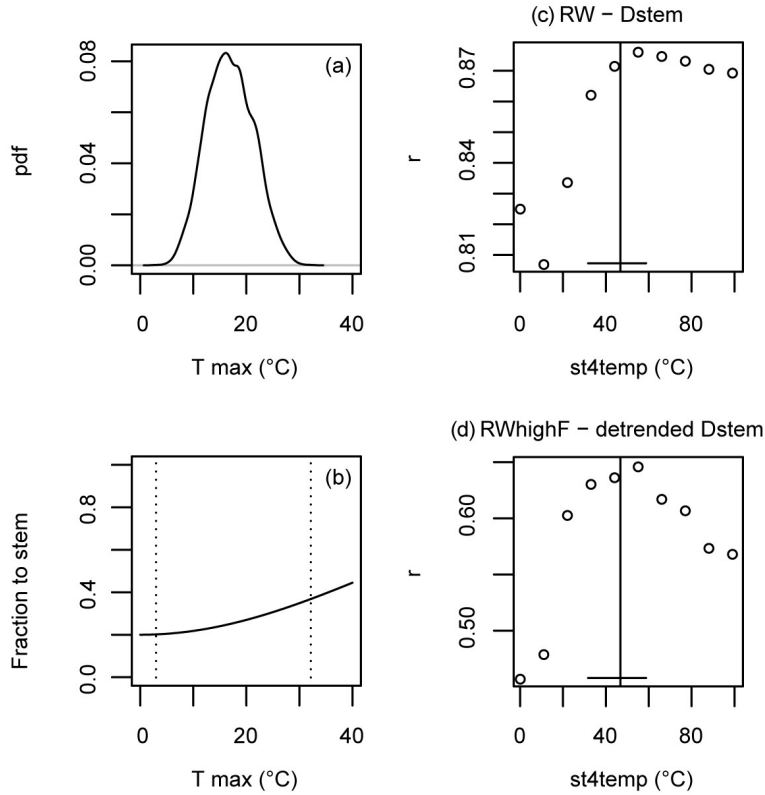


Figure 8: Temperature dependence of the daily partition of carbon in phase 4 (growth and accumulation phase in summer) when MAIDEN is run with the parameters of Plausible Block Stem at the center of the region with ring width data in the northern Quebec taiga. (a) Probability density of daily maximum temperature values in summer. (b) Relationship between maximum temperature values and portion of carbon allocated to the stem (Eq. (6)). The vertical dashed lines show the range of maximum temperature values. Plots c-d show how the parameter *st4temp* influencing this process impacts the correlations between simulated Dstem and observed ring width data (RW or RWhighF), when all other parameters are fixed to the values of Plausible Block Stem and *st4temp* varies over its prior acceptable range. The vertical line is the selected value for Plausible Block Stem and the horizontal line is the 90% confidence interval based on the parameter's posterior density (Fig. S5).

Table 1: Definitions, symbols, prior and posterior ranges of calibrated parameters. Small posterior ranges relative to the prior ones indicate sensitive parameters.

Overall process	Specific Process	Eq.	Parameter	Meaning	Units	Prior Range	Posterior range (value in Plausible Block)
GPP	Temperature dependence of V_{cmax}	1	V_{max}	Asymptote / maximum value	$\mu\text{mol C m}^{-2}$ of leaves s^{-1}	5 / 150	39 / 67 (45)
	Temperature dependence of V_{cmax}	1	V_b	Slope	NA	-0.30 / -0.10	-0.21 / -0.17 (-0.20)
	Temperature dependence of V_{cmax}	1	V_{ip}	Inflection point	$^{\circ}\text{C}$	10 / 30	17.5 / 22.3 (18.8)
	Water stress level influencing the stomatal conductance	2	$soilb$	Slope	NA	-0.025 / -0.005	-0.023 / -0.008 (-0.012)
	Water stress level influencing the stomatal conductance	2	$soilip$	Inflection point	mm	100 / 400	102 / 193 (129)
	Acclimation to temperature of photosynthesis	3	τ	Needed days	days	1 / 20	11.6 / 13.7 (12.4)
C allocation to stem	Definition of canopy maximum amount of C	4	$CanopyT$	Slope of the temperature dependence	NA	0 / 20	0.54 / 19.24 (6.87)
	Definition of canopy maximum amount of C	4	$CanopyP$	Slope of the precipitation dependence	NA	0 / 20	1.70 / 19.85 (16.68)
	Start of growing season (budburst)	NA	$GDD1$	GDD sum threshold	$^{\circ}\text{C}$	10 / 120	56.75 / 87.05 (70.22)
	Start of growing season (budburst)	NA	$vegphase23$	Day before the later start	day of the year	152 / 181	161.5 / 171.0 (167.0)
	Start of growing season (budburst)	NA	$day23_flex$	Acclimation to changing GDD sums	years	1 / 10	1.53 / 3.29 (2.24)
	Daily available C in phase 3	NA	$Cbud$	Storage C used by the plant	g C m^{-2} of stand $\cdot \text{day}^{-1}$	1 / 3	1.59 / 1.86 (1.69)
	Partition of C in phase 3	5	$h3$	Portion allocated to canopy and roots	fraction (0-1)	0 / 1	0.983 / 1.000 (0.991)
	Partition of C in phase 4 (stem versus storage)	6	$st4temp$	Inflection point of the temperature dependence	$^{\circ}\text{C}$	1 / 100	27.53 / 59.11 (46.78)
	Transition from phase 4 to 5	NA	$photoper$	Photoperiod threshold	hours	12 / 14	12.96 / 13.72 (13.41)
	C losses from the canopy	7	$PercentFall$	Yearly canopy turnover rate	fraction (0-1)	0.09 / 0.15	0.093 / 0.149 (0.143)
	C losses from the canopy	7	$OutMax$	Approximate day of the year with maximum losses	day of the year	150 / 200	154.2 / 195.0 (171.7)
	C losses from the canopy	7	$OutLength$	Index proportional to the length of the period with losses	NA	4 / 12	4.80 / 10.80 (9.91)

Table 2: ANOVA table for the best response function (here a combination of 4 out of the 10 tested predictors minimized the BIC) with daily GPP at EOBS as dependent variable (excluding days between November 15th and April 1st). All F values are highly significant ($p < 0.001$). For precipitation, lag n indicates the sum of the daily precipitation of the week ending in day n.

Predictor	Pairwise correlation with GPP	ANOVA table				BIC
		Regression coefficient	d.f.	Variance explained	F value	
Maximum temperature – lag -2 days	0.79	0.149	1	0.630	3716.16	5288.3
Maximum temperature – lag -19 days	0.69	0.057	1	0.049	291.29	
Precipitation – lag -2	0.21	0.019	1	0.005	31.99	
Precipitation – lag -0	0.16	-0.013	1	0.005	29.90	
Total variance explained				0.690		
Residuals	NA	NA	1827	0.310	NA	5315.4
Function with all 10 tested predictors				0.694		

Table 3: ANOVA table for the best response function (here a combination of 3 out of the 10 tested predictors minimized the BIC) with the observed mean detrended ring width series (RWhighF) as dependent variable.

Predictor (monthly data around the indicated day of the year)	Pairwise correlation with RWhighF	ANOVA table				BIC
		Regression coefficient	d.f.	Variance explained	F value	
Mean temperature – Previous July 28 th	-0.60	-0.477	1	0.355	39.88***	
Mean temperature – July 22 th	0.41	0.247	1	0.055	6.14*	
Maximum temperature – May 30 th	0.33	0.146	1	0.093	10.48**	
Total variance explained				0.502		148.7
Residuals	NA	NA	56	0.498	NA	
Function with all 10 tested predictors				0.568		169.0

***($p < 0.001$); **($p < 0.01$); *($p < 0.05$)