## Text S1.

We construct the full pCO<sub>2</sub> Taylor expansion decomposition starting with the carbonate chemistry definitions of DIC and TA as in Egleston et al. (2010):

$$DIC = [CO_2] + \frac{K_1[CO_2]}{[H^+]} + \frac{K_1K_2[CO_2]}{[H^+]^2}$$
(1)

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$$TA = \frac{K_1[CO_2]}{[H^+]} + 2\frac{K_1K_2[CO_2]}{[H^+]^2} + \frac{B_{tot}K_b}{(K_b + [H^+])} - [H^+] + \frac{K_w}{[H^+]}$$
(2)

Where  $K_1$  and  $K_2$  are defined as *Millero et al.* (2006),  $K_w$  as *Millero* (1995) and  $K_b$  according to *Dickson* (1990). From Eq.(1) we can obtain  $[H^+]$  and from Eq.(2) we get  $[CO_2]$  respectively as:

$$[H^+] = \frac{K_1[CO_2] + \sqrt{K_1^2[CO_2]^2 + 4K_1K_2[CO_2](DIC - [CO_2])}}{2(DIC - [CO_2])}$$
(3)

$$\begin{bmatrix} CO_2 \end{bmatrix} = \frac{[H^+]^2}{K_1[H^+] + 2K_1K_2} \left( TA - \frac{B_{tot}K_b}{(K_b + [H^+])} + [H^+] - \frac{K_w}{[H^+]} \right)$$
(4)

For  $[H^+]$  the positive solution was chosen; the negative root gives a result far from real values. From Eq.(3) and Eq.(4) we can make a Talyor's expansion of  $[H^+]$  and  $[CO_2]$  respectively as:

$$\delta[H^+] = \frac{\partial[H^+]}{\partial DIC} \Big|_{\frac{CO_2, DIC}{T, \overline{S}}} \delta DIC + \frac{\partial[H^+]}{\partial[CO_2]} \Big|_{\frac{CO_2, DIC}{T, \overline{S}}} \delta[CO_2] + \frac{\partial[H^+]}{\partial T} \Big|_{\frac{CO_2, DIC}{T, \overline{S}}} \delta T + \frac{\partial[H^+]}{\partial S} \Big|_{\frac{CO_2, DIC}{T, \overline{S}}} \delta S$$
(5)

 $\delta[CO_2] = \frac{\partial[CO_2]}{\partial TA} \bigg|_{\frac{TA,H}{T,S}} \delta TA + \frac{\partial[CO_2]}{\partial[H^+]} \bigg|_{\frac{TA,H}{T,S}} \delta[H^+] + \frac{\partial[CO_2]}{\partial T} \bigg|_{\frac{TA,H}{T,S}} \delta T + \frac{\partial[CO_2]}{\partial S} \bigg|_{\frac{TA,H}{T,S}} \delta S$ (6)

The over bars indicate the mean values of the variables in which the derivatives are evaluated. Finally, we replace  $\delta[H^+]$  from Eq.(5) into Eq.(6), to get  $[CO_2]$  in terms of DIC, TA, T and S:

$$\delta[CO_{2}] = \left[1 - \frac{\partial[CO_{2}]}{\partial[H^{+}]} \Big|_{\frac{TA,H}{T,S}} \frac{\partial[H^{+}]}{\partial[CO_{2}]} \Big|_{\frac{CO_{2},DIC}{T,S}}\right]^{-1} \cdot \left[\frac{\partial[CO_{2}]}{\partial TA} \Big|_{\frac{TA,H}{T,S}} \delta TA + \frac{\partial[CO_{2}]}{\partial[H^{+}]} \Big|_{\frac{TA,H}{T,S}} \frac{\partial[H^{+}]}{\partial DIC} \Big|_{\frac{CO_{2},DIC}{T,S}} \delta DIC + \left(\frac{\partial[CO_{2}]}{\partial T} \Big|_{\frac{TA,H}{T,S}} + \frac{\partial[CO_{2}]}{\partial[H^{+}]} \Big|_{\frac{TA,H}{T,S}} \frac{\partial[H^{+}]}{\partial T} \Big|_{\frac{CO_{2},DIC}{T,S}} \right) \delta T + \left(\frac{\partial[CO_{2}]}{\partial S} \Big|_{\frac{TA,H}{T,S}} + \frac{\partial[CO_{2}]}{\partial[H^{+}]} \Big|_{\frac{TA,H}{T,S}} \frac{\partial[H^{+}]}{\partial S} \Big|_{\frac{CO_{2},DIC}{T,S}} \right) \delta S \right]$$

$$(7)$$

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Comparing the terms from Eq.(7) to the desired Taylor's expansion:

$$\delta p CO_2 \approx \frac{\partial p CO_2}{\partial DIC} \bigg|_{\frac{TA, DIC}{T, \overline{S}}} \delta DIC + \frac{\partial p CO_2}{\partial TA} \bigg|_{\frac{TA, DIC}{\overline{T}, \overline{S}}} \delta TA + \frac{\partial p CO_2}{\partial T} \bigg|_{\frac{TA, DIC}{\overline{T}, \overline{S}}} \delta T + \frac{\partial p CO_2}{\partial S} \bigg|_{\frac{TA, DIC}{\overline{T}, \overline{S}}} \delta S$$

$$\tag{8}$$

We can identify the derivatives from Eq.(8), as follows:

where  $\Theta = [HCO_3^-] + 4[CO_3^{2-}] + \frac{[B(OH)_4^-][H^+]}{(k_b + [H^+])} + [H^+] + [OH^-]$  and  $\overline{Alk}_c = [HCO_3^-] + 2[CO_3^{2-}]$ . Below are some details of the specific concentrations derivatives.

$$\frac{\partial Alk_c}{\partial T,S} = \frac{[CO_2]}{[H^+]^2} \left( \frac{\partial k_1}{\partial T,S} [H^+] + 2k_1 \frac{\partial k_2}{\partial T,S} + 2k_2 \frac{\partial k_1}{\partial T,S} \right)$$

$$\frac{\partial (DIC - [CO_2])}{\partial T,S} = \frac{[CO_2]}{[H^+]^2} \left( \frac{\partial k_1}{\partial T,S} [H^+] + k_1 \frac{\partial k_2}{\partial T,S} + k_2 \frac{\partial k_1}{\partial T,S} \right)$$

$$\frac{\partial [B(OH)_4^-]}{\partial T} = \frac{B_{tot} [H^+]}{(k_b + [H^+])^2} \frac{\partial k_b}{\partial T}$$

$$\frac{\partial [B(OH)_4^-]}{\partial S} = \frac{B_{tot} [H^+]}{(k_b + [H^+])^2} \frac{\partial k_b}{\partial S} + \frac{k_b}{(kb + [H^+])} \frac{\partial B_{tot}}{\partial S}$$

$$\frac{\partial [OH^-]}{\partial T,S} = \frac{1}{[H^+]} \frac{\partial k_w}{\partial T,S}$$
(10)



**Figure S1.** pCO<sub>2</sub> seasonal cycle amplitude calculated from models outputs compared to its Taylor's expansion reconstruction in a) 2006-2026 and b) 2080-2100. Different colors indicate latitudinal ranges of zonal means, for the Atlantic (triangles), Pacific (circles) and Indian (stars) ocean basins. Large symbols represent the ensemble mean, and small symbols are the result for each model separately.



**Figure S2.** a)  $pCO_2$  seasonal amplitude calculated as summer minus winter for each hemisphere respectively. b)- e) show DIC, T, TA and S contributions to the  $pCO_2$  summer minus winter amplitude. First and second rows represent 2006-2026 and 2080-2100 periods respectively. Third row shows the difference between second and first rows.



Figure S3. a) Ensemble zonal mean  $pCO_2$  climatology and b) DIC contribution in color with overlying black contours of T contribution for 2006-2026 period. c) and d) same as a) and b) but for the 2080-2100 period.



Figure S4. RCP8.5 ensemble zonal mean seasonal cycles: a)  $\delta TA_s$  and b)  $\delta S$ , for different latitudinal bands. Blue lines represent the 2006-2026 period, depicted for comparison with the 2080-2100 period shown by red lines. Different panels represent different latitudinal sections.  $\delta TA_s$  is projected to slightly increase in all the bands, while  $\delta S$  is projected to slightly decrease. The shading represents one standard deviation across the models.

## References

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