Supplementary Material



Figure S1. Mean daily air temperature and daily cumulative precipitation during the growing season. Data was retrieved from a weather station approximately 200 m from the field site, operated by the Agenzia Regionale per la Protezione dell'Ambiente-Lomardia (ARPA).



Figure S2. Experimental design and plot layout



Figure S3. Comparison of modeled *r*N₂O, frac_{DEN-gross}, and *DenContribution* under open and closed system dynamics for scenario one (sc1) and scenario two (sc2).



Figure S4. Dissolved and pore air N₂O throughout the experimental period in the three water management treatments (WS-FLD = wet-seeding + conventional flooding; WS-AWD = wet-seeding + alternate wetting and drying; DS-AWD = direct dry seeding + alternate wetting and drying). The dashed vertical line indicates the date of fertilization (60 kg urea-N ha⁻¹). Blue shaded areas represent periods of flooding, shaded areas that last only one day indicate a 'flush irrigation' = flooding for < 6 hrs. The error bars represent the standard error of the mean.



Figure S5. The relationship $\delta^{18}\text{O-N}_2\text{O}$ with $\delta^{15}\text{N-N}_2\text{O}$ in $N_2\text{O}_{\text{emitted}}$ and $N_2\text{O}_{\text{poreair}}.$



Figure S6. The relationship of δ^{18} O-N₂O with δ^{15} N-N₂O in N₂O_{emitted} and N₂O_{poreair}, differentiated by depth. Non-significant relationships are indicated by NS.



Figure S7. The relationship of SP with δ^{18} O-N₂O in N₂O_{emitted} and N₂O_{poreair}, differentiated by depth. Non-significant relationships are indicated by NS.



Figure S8. The relationship of SP relative to δ^{15} N-N₂O in N₂O_{emitted} and N₂O_{poreair}, differentiated by depth. Non-significant relationships are indicated by NS.



Figure S9. δ^{15} N and δ^{18} O of NO₃⁻, NH₄⁺ and the associated isotope effects calculated relative to N₂O_{poreair} at 5, 12.5 and 25 cm in the three water management treatments (WS-FLD = wet-seeding + conventional flooding; WS-AWD = wet-seeding + alternate wetting and drying; DS-AWD = direct dry seeding + alternate wetting and drying). The error bars represent the standard error of the mean.



Figure S10. Graphical two-end member mixing plot shaded by sampling date. Following Lewicka-Szcebak *et al.* (2017), sample values are plotted in SP x δ^{18} O-N₂O space (A) after Toyoda *et al.* (2011) where sample values are plotted in SP x δ^{15} N-N₂O space (B). For further explanation and derivation of endmember values and process boxes the reader is referred to the main text, Fig. 3, Supplementary Table 1.4 and section 2.7.



Figure S11. Graphical two-end member mixing plot shaded by depth. Following Lewicka-Szcebak *et al.* (2017), sample values are plotted in SP x δ^{18} O-N₂O space (A) after Toyoda *et al.* (2011) where sample values are plotted in SP x δ^{15} N-N₂O space (B). For further explanation and derivation of endmember values and process boxes the reader is referred to the main text, Fig. 3, Supplementary Table 1.4 and section 2.7.



Figure S12. Graphical two-end member mixing plot shaded by WFPS. Following Lewicka-Szcebak *et al.* (2017), sample values are plotted in SP x δ^{18} O-N₂O space (A) after Toyoda *et al.* (2011) where sample values are plotted in SP x δ^{15} N-N₂O space (B). For further explanation and derivation of endmember values and process boxes the reader is referred to the main text, Fig. 3, Supplementary Table 1.4 and section 2.7.



Figure S13. Model estimates of net subsurface denitrification/nitrifier-denitrification (a) and gross subsurface denitrification/nitrifier-denitrification N₂O production (b) and N₂ production in the subsurface (c) and N₂ emissions (d). Subsurface values from 25 cm were omitted due to poor data availability. $n \le 4$, as rates could not be estimated for all treatment x depth combinations.

date	N₂O emitted	pore water	pore air	NH ₃	¹⁵ N-NO ₃ ⁻ , NH ₄ ⁺
20-May	Х	•	X		
24-May	Х	Х	Х		х
25-May				Х	
27-May	Х	Х	Х		х
30-May	Х	Х	Х		
31-May				Х	
1-Jun	Х	Х	Х		Х
3-Jun	Х	Х	Х		
7-Jun	Х	Х	Х		Х
9-Jun	Х	Х	Х		
14-Jun	Х	Х			Х
17-Jun	Х	Х	Х		Х
19-Jun	Х	Х			Х
20-Jun	Х	Х	Х	Х	
21-Jun	Х	Х	Х	Х	
22-Jun	Х	Х	Х		Х
23-Jun	х	Х		Х	Х
28-Jun	х	Х		Х	Х
30-Jun	X	Х	Х		

Table S1. Dates of sampling for the various parameters

Table S2. Percent of observations meeting data quality criteria for open and closed mixing models under *scenario one* and *scenario two*. Observations were considered not plausible and were eliminated if the modeled fraction was < 0 or > 1. The open system model was solved by solving a series of equations for the minimal sum of squares (minSS). In this case, an additional criteria of a minSS < 500 was also used. Gross frac_{DEN} is the fraction of N₂O + N₂ attributed to denitrification; gross rN_2O is the fraction of residual N₂O not reduced; DenContribution is the fraction of N₂O attributed to denitrification.

		scenario one		scenario two	
dataset		open	closed	open	closed
N_2O_{poreair}	gross frac _{DEN} > 1	0%	20%	0%	20%
(381 obs)	gross frac _{DEN} < 0	0%	1%	0%	1%
	gross frac _{DEN} = 1	6%	1%	3%	0%
	gross <i>r</i> N ₂ O > 1	0%	0%	0%	0%
	gross <i>r</i> N2O < 0	0%	0%	0%	0%
	DenContribution >1	1%	20%	3%	20%
	DenContribution <0	5%	1%	89%	1%
	minSS > 500	8%	NA	3%	NA
N_2O_{emitted}	gross frac _{DEN} > 1	0%	9%	0%	8%
(128 obs)	gross frac _{DEN} < 0	0%	2%	0%	6%
	gross frac _{DEN} = 1	2%	1%	0%	0%
	gross <i>r</i> N₂O > 1	0%	0%	0%	0%
	gross <i>r</i> N2O < 0	0%	2%	0%	0%
	DenContribution >1	0%	6%	6%	8%
	DenContribution <0	6%	5%	4%	6%
	minSS > 500	5%	NA	4%	NA

Table S3. ANCOVA results of N_2O emissions ($N_2O_{emitted}$), $N_2O_{poreair}$ concentrations, inorganic N, DOC, WFPS and Eh.

	N_2O_{emitted}	N_2O_{poreair}	NO ₃ ⁻	${\sf NH_4}^+$	DOC	WFPS	Eh
treatment	<0.001	0.08	<0.001	<0.001	0.22	0.001	<0.001
date	<0.001	<0.001	<0.001	<0.001	<0.001	<0.001	<0.001
depth		0.43	0.01	0.01	0.15	0.01	0.00
Y position	0.82	0.08	0.86	0.79	0.56	0.92	0.20
treatment x date	<0.001	<0.001	<0.001	<0.001	<0.001	<0.001	<0.001
treatment x depth		0.55	0.02	0.31	0.33	0.42	0.01
date x depth		<0.001	0.05	<0.001	0.61	<0.001	<0.001
treatment x date x depth		<0.001	0.09	<0.001	0.01	<0.001	<0.001

		net denitrification/	gross nitrification/			
		nitrifier-	fungal			
	NumDF	denitrification	denitrification	N_2O reduction		
subsurface						
trmt	2	0.285	0.005	0.431		
day	14	< 0.001	< 0.001	< 0.001		
depth	1	0.378	0.485	0.228		
Yposition	1	0.307	0.467	0.757		
Trmt:day	28	< 0.001	< 0.001	< 0.001		
trmt:depth	2	0.959	0.182	0.773		
day:depth	14	< 0.001	0.476	0.002		
trmt:day:depth	23	< 0.001	< 0.001	0.001		
surface						
trmt	2	< 0.001	0.017	0.858		
day	16	< 0.001	< 0.001	0.008		
Yposition	1	0.650	0.516	0.534		
trmt:day	19	< 0.001	< 0.001	0.005		

Table S4. ANCOVA table of modeled net denitrification/nitrifier-denitrification N_2O , gross nitrification/fungal denitrification N_2O and N_2O reduction. Subsurface data from 25 cm was not included in the analysis due to poor data availability.

Table S5. Mean, minimum and maximum observed $\delta^{15}N-NO_3^-$ and $\delta^{15}N-NH_4^+$ values. The estimated range of $\delta^{15}N-N_2O$ derived from denitrification and nitrification, used in Fig. 3B and Supplementary Fig. 1.9B-1.11B, was calculated using the mean isotope effects for N₂O produced from NO₃⁻ and NH₄⁺, respectively, reported in Denk *et al.*, (2017) plus the minimum and maximum observed $\delta^{15}N-NO_3^-$ and $\delta^{15}N-NH_4^+$.

	DS-AWD	WS-AWD	WS-FLD
		‰	
δ ¹⁵ N-NO₃⁻ (mean)	6.0	9.5	8.5
δ^{15} N-NH4 ⁺ (mean)	4.4	6.8	9.4
δ ¹⁵ N-NO ₃ ⁻ (min)	-7.2	-12.9	2.2
δ^{15} N-NH4 ⁺ (min)	-11.9	-2.0	3.0
δ ¹⁵ N-NO ₃ ⁻ (max)	23.7	45.9	17.2
δ^{15} N-NH4 ⁺ (max)	21.7	26.6	18.8
literature mean ^a $\epsilon^{15}N_{N2O/NO3}$ (denitrification)	-42.9	-42.9	-42.9
literature mean ^a $\epsilon^{15}N_{N2O/NH4}$ (nitrification)	-56.6	-56.6	-56.6
estimated denitrification δ^{15} N-N ₂ O range (min)	-19.2	3.0	-25.7
estimated denitrification δ^{15} N-N ₂ O range (max)	-50.1	-55.8	-40.7
estimated nitrification δ^{15} N-N ₂ O range (min)	-34.9	-30.0	-37.8
estimated nitrification δ^{15} N-N ₂ O range (max)	-68.5	-58.6	-53.6
δ ¹⁵ N-NO ₃ ⁻ (<i>n</i>)	97	58	46
δ ¹⁵ N-NH ₄ ⁺ (<i>n</i>)	19	89	92

^a Denk *et al.,* (2017)

Table S6. Estimated $\epsilon^{15}N_{N2O/NO3}$ considering N₂O reduction effects on measured $\delta^{15}N-N_2O$ values. Values were calculated by using measured 15N-N₂O values and modeled rN_2O values in the Rayleigh equation.

depth	treatment	mean ε ¹⁵ N _{N2O/NO3} (se)
emitted	DS-AWD	-28.6 (1.3)
5	DS-AWD	-25.0 (2.3)
12.5	DS-AWD	-28.9 (2.1)
25	DS-AWD	-36.5 (2.2)
emitted	WS-AWD	-42.3 (3.7)
5	WS-AWD	-39.4 (2.7)
12.5	WS-AWD	-33.1 (5.4)
25	WS-AWD	-32.6 (5.1)
emitted	WS-FLD	-37.6 (3.3)
5	WS-FLD	-51.1 (9.4)
12.5	WS-FLD	-36.8 (3.7)
25	WS-FLD	-29.0 (3.9)