

1 Supplements

1.1 Detailed model description

The reactions in the reactive transport model describe organic matter degradation coupled to different electron acceptors. Reactions are divided in primary redox reactions and other biogeochemical reactions (Table S.6). The succession of oxidants during organic matter degradation (Froelich et al., 1979) is described by means of Monod kinetics (Table S.2; Boudreau (1997)). This means that the oxidants with the highest metabolic free energy yield are preferentially used until they become limiting and the oxidant with the next highest energy yield is used (Berg et al., 2003; Boudreau, 1996a; Wang and Van Cappellen, 1996). Respiratory reactions occur where O_2 , NO_3^- , $Mn(OH)_2$, $Fe(OH)_3$ and SO_4^{2-} serve as electron acceptors and finally organic matter is subject to methanogenesis (Reed et al. (2011a, b); Rooze et al. (2016); Table S.2). Organic matter includes carbon (C), nitrogen (N) and P in a C:N:P ratio of 106:16:0.35. In the model, oxidation of CH_4 is possible with O_2 , $Mn(OH)_2$, $Fe(OH)_3$ and SO_4^{2-} . Dissolved inorganic carbon in the model is calculated as the sum of the carbon in CO_2 and HCO_3^{2-} , which is produced or consumed by modeled reactions (Table S.6).

The generic mass conservation equations for solids and solutes are described by Eq. 1 and 2;

$$(1 - \phi) \frac{\partial C_s}{\partial t} = -(1 - \phi)v \frac{\partial C_s}{\partial z} + \sum R_s \quad (1)$$

$$15 \quad \phi \frac{\partial C_{aq}}{\partial t} = \phi D' \frac{\partial^2 C_{aq}}{\partial z^2} - \phi u \frac{\partial C_{aq}}{\partial z} + \sum R_{aq} \quad (2)$$

$$D' = \frac{D_m}{1 - ln\phi^2} \quad (3)$$

where C_s is the concentration of solid species (mol L^{-1}), C_{aq} is the concentration of dissolved species (mol L^{-1}), t is time (yr), ϕ is the sediment porosity, v and u are the advective velocities of solid and dissolved species (cm yr^{-1}), respectively. Variables v and u were described by a depth-dependent function to account for changes in porosity (Meysman et al., 2005).

20 Distance from the sediment-water interface is z (cm), D' the diffusion coefficient of dissolved species ($\text{cm}^2 \text{ yr}^{-1}$), corrected for tortuosity in the porous medium ((Boudreau, 1996b), Eq. 3). $\sum R_s$ and $\sum R_{aq}$ are the net reaction rates from the chemical reaction (Table S.2) for solid and dissolved species.

Porosity (ϕ) is described by Eq. 4 to account for sediment compaction (Meysman et al., 2005; Reed et al., 2011b),

$$\phi(x) = \phi_\infty + (\phi_0 - \phi_\infty) e^{-\frac{x}{y}} \quad (4)$$

25 where ϕ_0 is the porosity at the sediment-water interface, ϕ_∞ is the porosity at depth and y is the porosity attenuation factor/e-folding distance (Fig. S.3A, Table S.3). The model code was written in R with the use of the marelac geochemical dataset package (Soetaert et al., 2010). To calculate the transport in porous media, the R package Reactran was used (Soetaert and Meysman, 2012). The set of ordinary differential equations was solved numerically with the Lsode integrator algorithm (Petzold, 1983).

30 Zero gradient boundary conditions were applied to the base of the model domain for all chemical species. To avoid influence of the boundary conditions at the base of the model domain results, the total depth of the model was set to 90 cm (divided into 900 grid cells of 0.1 cm).

Reaction parameters were mostly taken from literature or obtained within existing parameter ranges (Table S.7). If these were not available, or no fit to the data could be obtained with existing ranges, parameters were constrained by fitting the 35 model to the measured data.

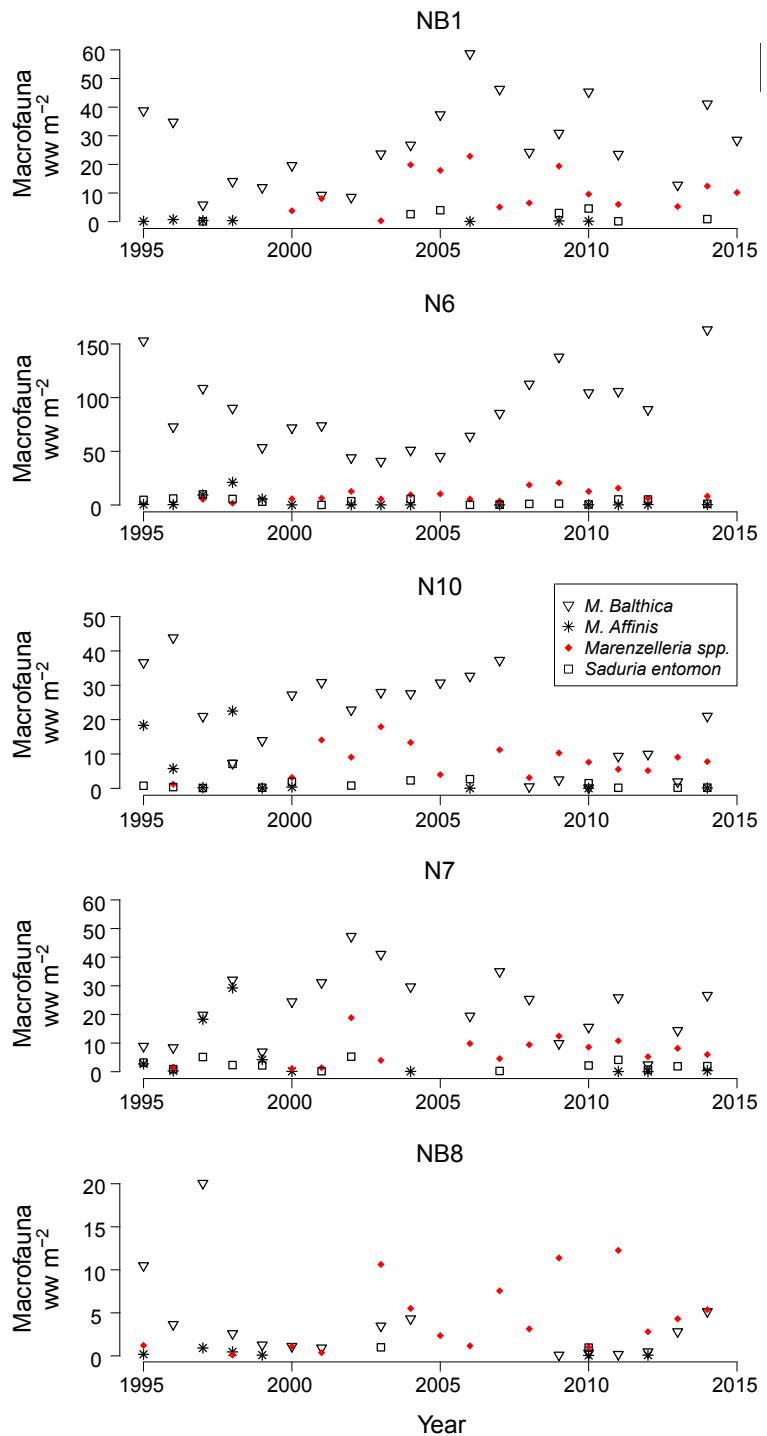


Figure S.1. Wet weight of macrofauna (ww m^{-2} ; in grams) at sites NB1, N6, N10, N7 and NB8 in the Öre Estuary from 1995-2015 (www.SMHI.se).

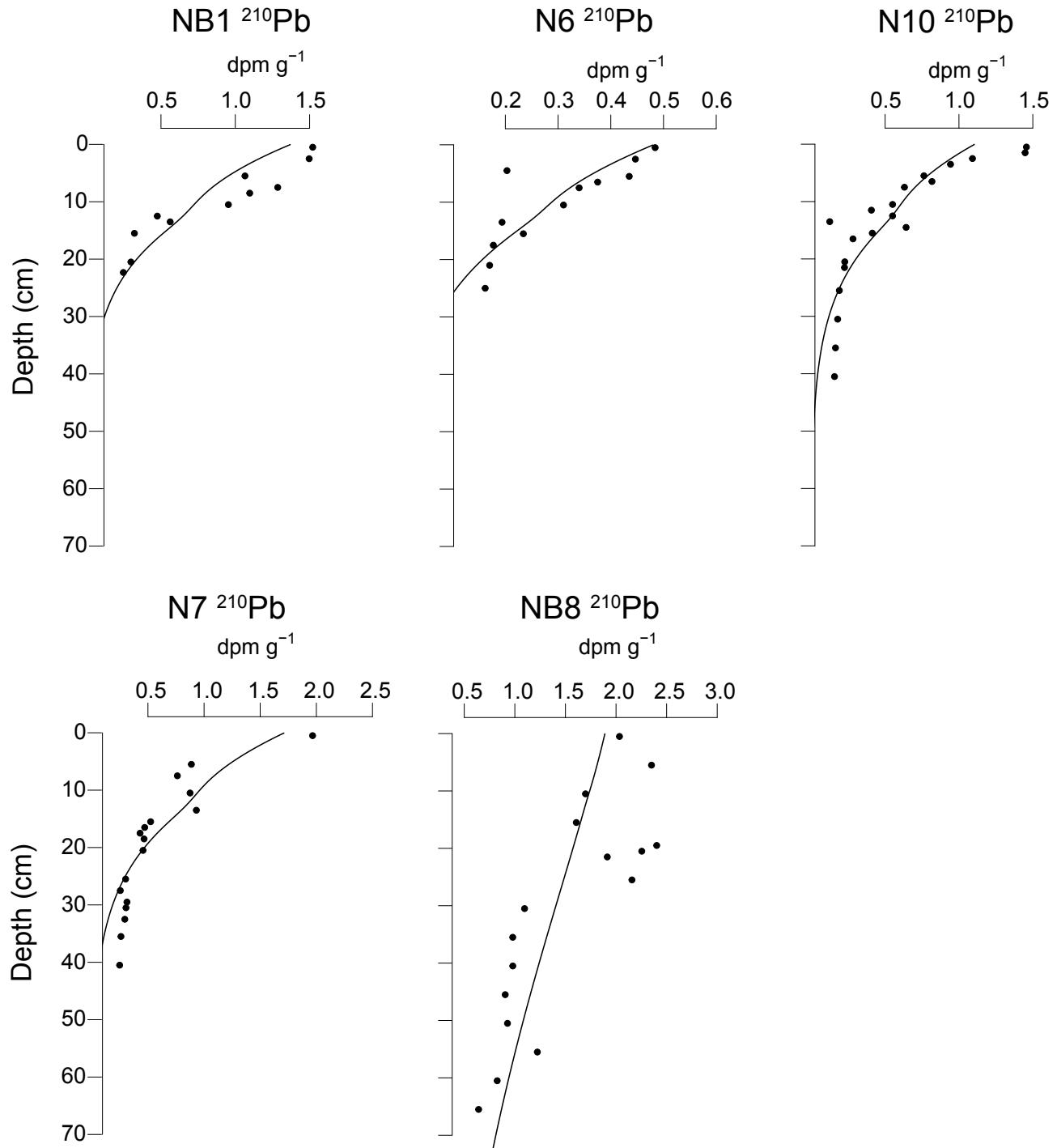


Figure S.2. Solid phase depth profiles of ^{210}Pb at sites NB1, N6, N10, N7 and NB8 and model fits (black lines). Sites NB1, N6, N10 and N7 were sampled in April 2015. Site NB8 was sampled in August 2015.

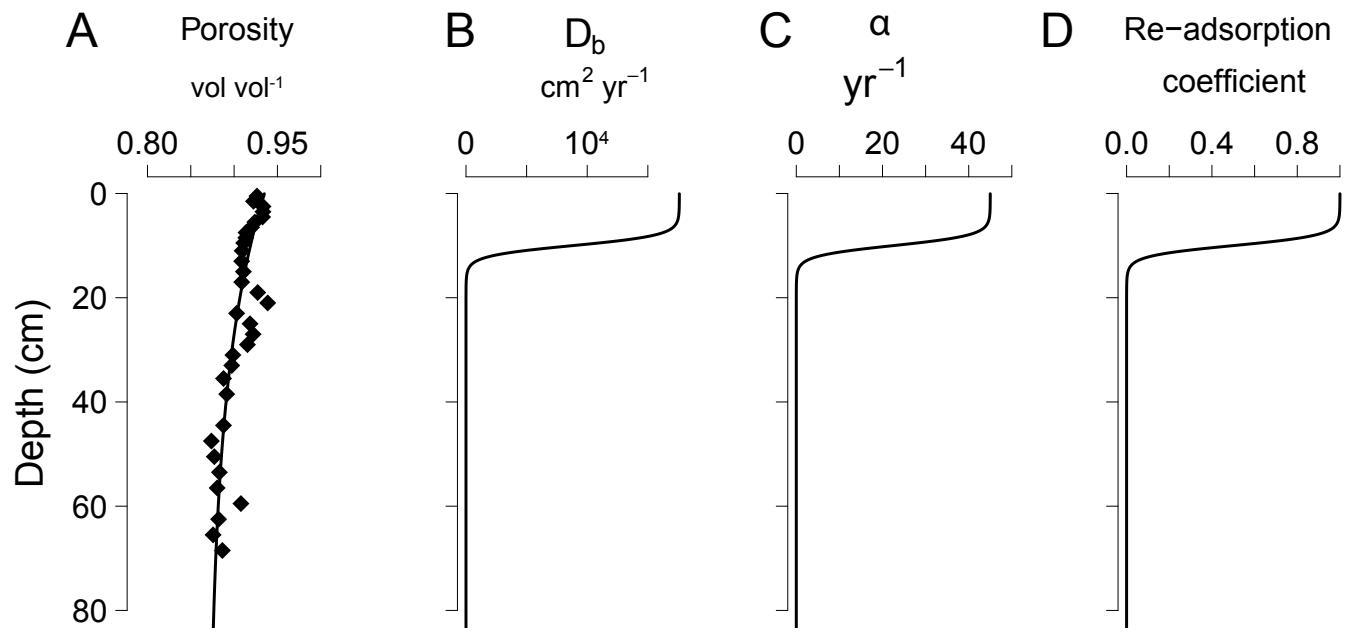


Figure S.3. Depth profiles used in the model A: Measured porosity (vol vol⁻¹) for April 2015 (black circles) and fitted porosity (black line); B: bioturbation coefficient (D_b ; cm yr⁻¹); C: bioirrigation coefficient (α ; yr⁻¹); D: Re-adsorption coefficient for HPO_4^{2-} .

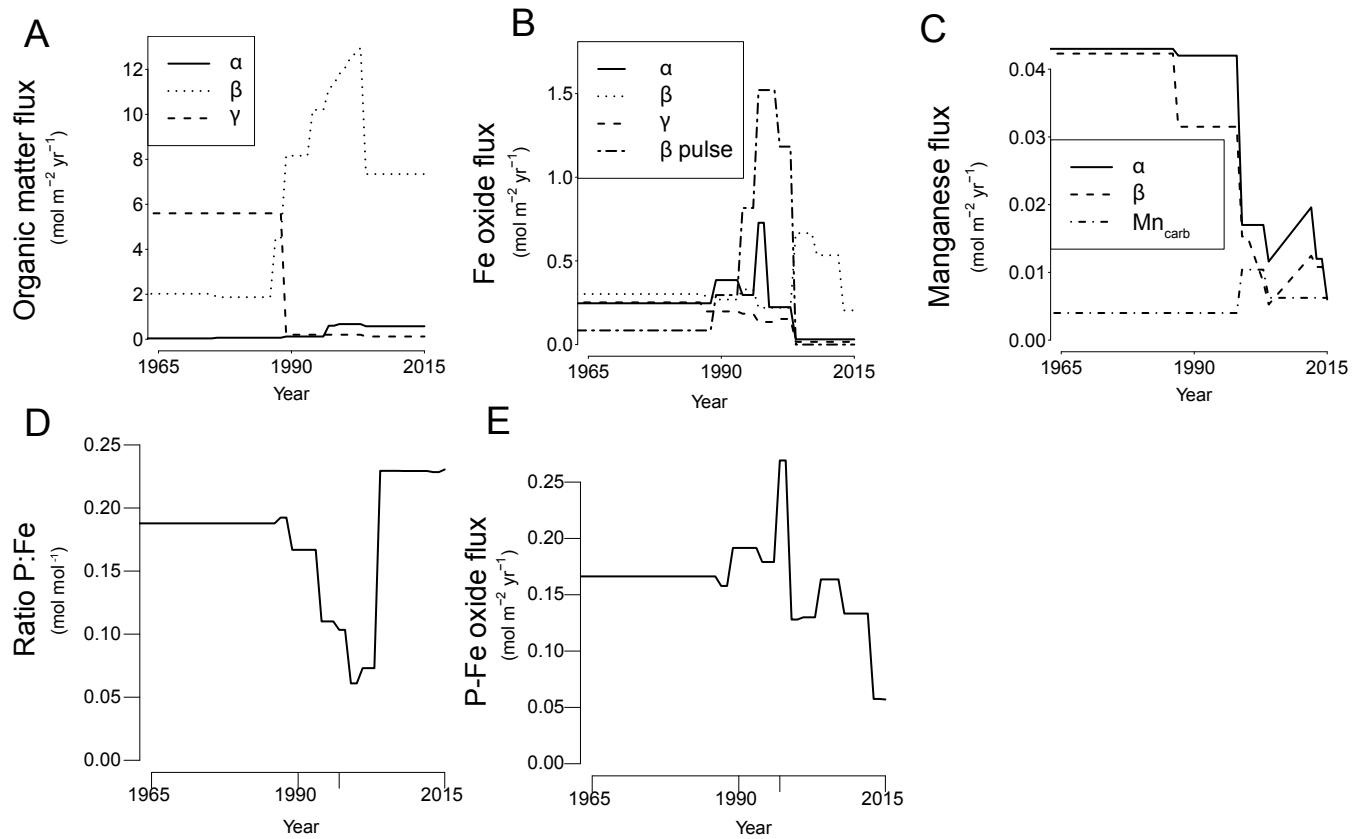


Figure S.4. Transient scenarios used in the reactive transport model between 1965 and 2015; A: different phases of organic matter; B: different phases of Fe oxides; C: different phases of manganese; D: average P:Fe ratio of all Fe oxide fractions combined, E: total P input bound to Fe oxides. The various types of organic matter, Fe oxides and Mn oxides are indicated as α (highly reactive), β (less reactive) and γ (refractory).

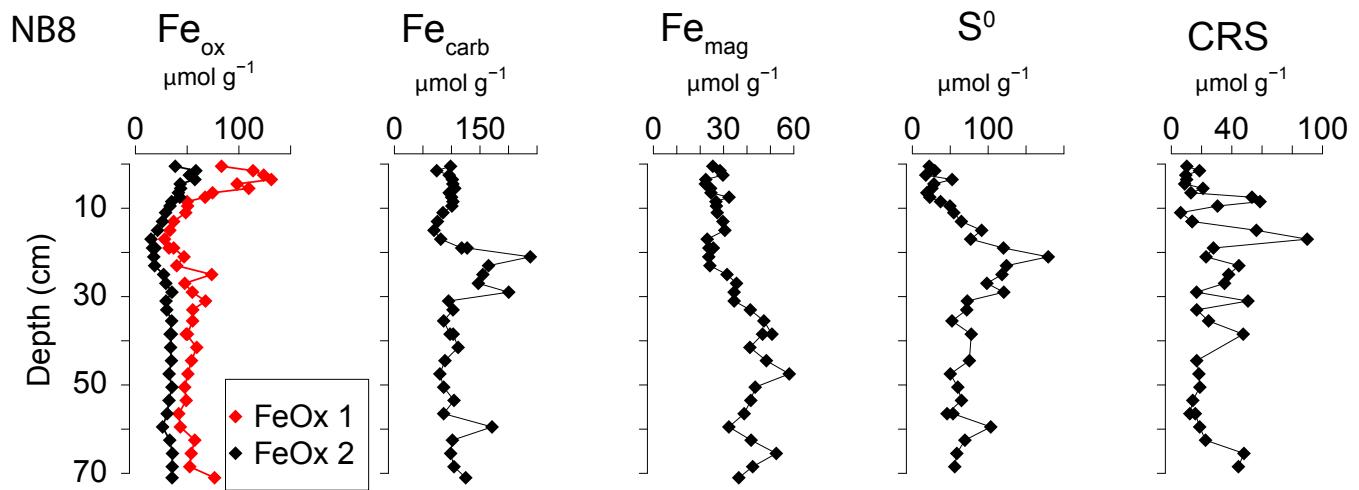


Figure S.5. Solid phase depth profiles of the sum of easily reducible Fe oxides and reducible (crystalline) Fe oxides ($\text{FeOx} = \text{FeOx1} + \text{FeOx2}$), Fe carbonates (Fe_{carb}), magnetite (Fe_{mag}), elemental S (S^0) and S in pyrite (CRS) for site NB8 in April 2015.

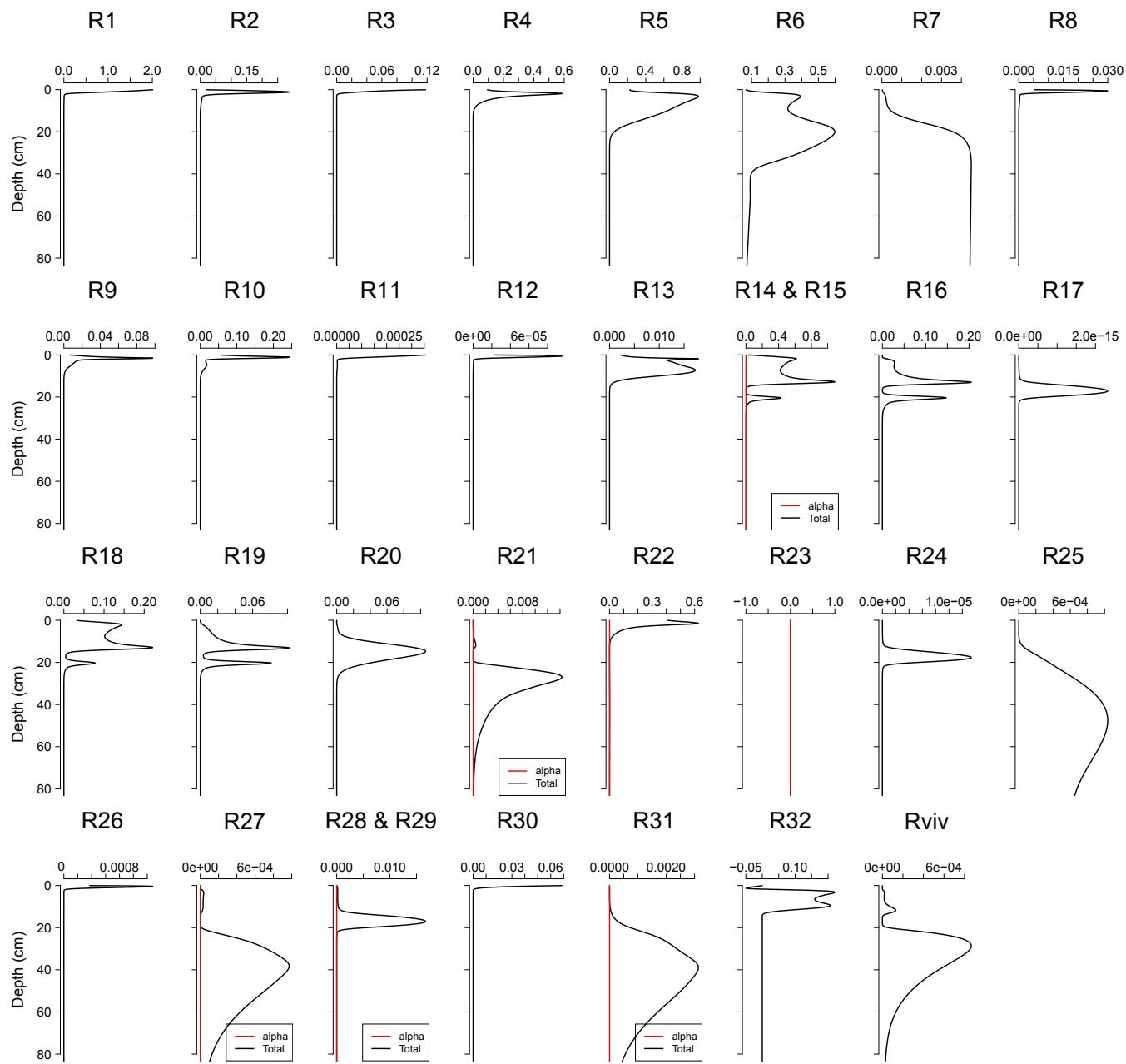


Figure S.6. Depth profiles of reaction rates calculated for the baseline scenario in 2015. Rates are in $\text{mol m}^{-3} \text{ yr}^{-1}$. Reactions are described in Table S.6.

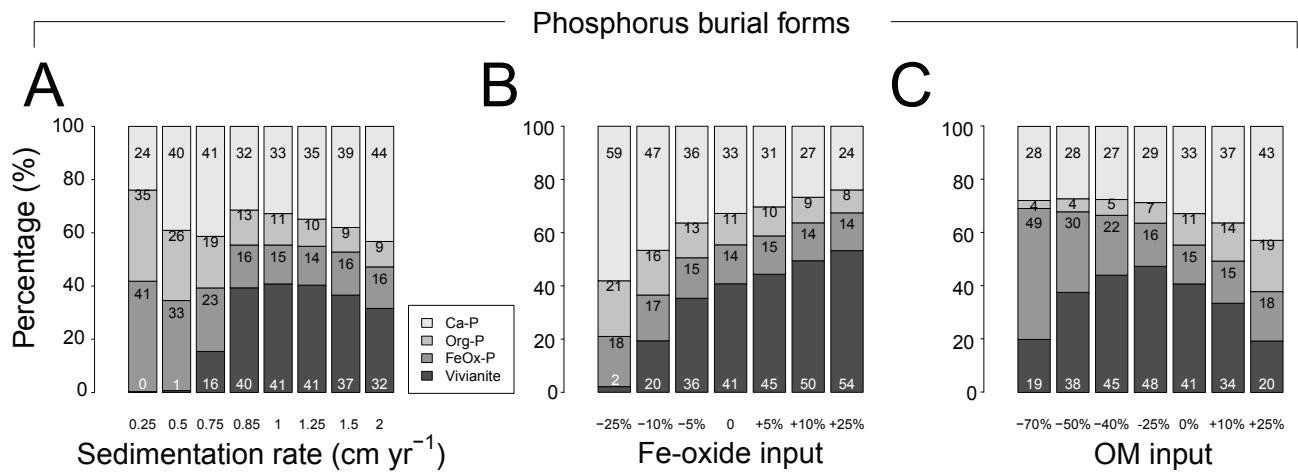


Figure S.7. Modeled burial forms of P as a function of changes in A: sedimentation rates between 0.25 and 2 cm yr^{-1} ; B: organic matter inputs ranging between -70% and +25%; C: inputs of Fe oxides ranging between -25% and 25%. Corresponding P burial rates are shown in figure 9.

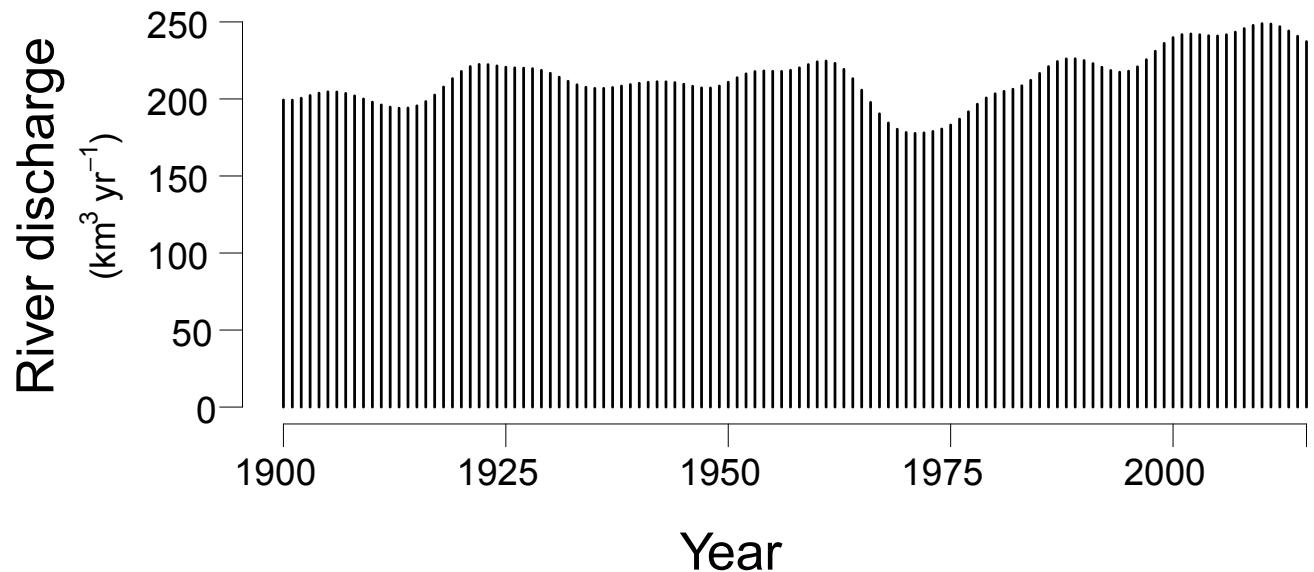


Figure S.8. Averaged summer river discharge for 86 Swedish rivers from 1900-2015 (www.SMHI.se).

Table S.1. Chemical species included in the model.

Species	Notation
Solid	
Organic matter ^a	$\text{OM}^{\alpha,\beta,\gamma}$
Iron oxide ^a	$\text{Fe(OH)}_3{}^{\alpha,\beta}$
Elemental sulfur	S^0
Iron monosulfide	FeS
Pyrite	FeS_2
Iron-bound Phosphorus	$\text{Fe(OH)}_3\text{P}$
Vivianite	$\text{Fe}_3(\text{PO}_4)_2$
Siderite	FeCO_3
Organic phosphorus	P_{org}
Authigenic (Ca) phosphorus	CaP
Detrital phosphorus	DetrP
Manganese oxide ^b	$\text{Mn(OH)}_2{}^{\alpha,\beta}$
Manganese carbonate	MnCO_3
Solute	
Chloride	Cl^-
Oxygen	O_2
Nitrate	NO_3^-
Sulfate	SO_4^{2-}
Methane	CH_4
Iron	Fe^{2+}
Ammonium ^c	$\sum \text{NH}_4^+$
Hydrogen sulfide ^c	$\sum \text{H}_2\text{S}$
Phosphate ^c	$\sum \text{HPO}_4^{2-}$
Dissolved Inorganic Carbon	DIC
Manganese	Mn^{2+}

^a chemical species consist of 3 types: reactive (α), less reactive (β) and refractory (γ). Fe oxide ${}^{\beta(pulse)}$ and Fe oxide ${}^{\beta(max)}$ are not specifically named because they have the same characteristics as Fe oxide ${}^\beta$.

^b chemical species consist of two types: reactive (α) and less reactive (β).

^c \sum denotes that all species of an acid are included.

Table S.2. Reaction pathways and stoichiometries implemented in the model.

Primary redox reactions	
$\text{OM}^{\alpha,\beta} + \text{aO}_2 \rightarrow \text{aCO}_2 + \text{bNH}_4^+ + \text{cH}_3\text{PO}_4 + \text{aH}_2\text{O}$	R1
$\text{OM}^{\alpha,\beta} + 0.8\text{aNO}_3^- + 0.8\text{aH}^+ \rightarrow \text{aCO}_2 + \text{bNH}_4^+ + \text{cH}_3\text{PO}_4 + 0.4\text{aN}_2 + 1.4\text{a H}_2\text{O}$	R2
$\text{OM}^{\alpha,\beta} + 2\text{aMn(OH)}_2^\alpha + 2\text{aH}^+ \rightarrow 2\text{Mn}^{2+} + \text{aCO}_2 + \text{cH}_3\text{PO}_4 + 2\text{aH}_2\text{O}$	R3
$\text{OM}^{\alpha,\beta} + 4\text{a Fe(OH)}_3^\alpha + 4\chi^\alpha\text{Fe}_{\text{ox}}\text{P} + 12\text{aH}^+ \rightarrow \text{aCO}_2 + \text{bNH}_4^+ + (\text{c} + 4\chi^\alpha)\text{H}_3\text{PO}_4 + 13\text{aH}_2\text{O} + 4\text{aFe}_2^+$	R4
$\text{OM}^{\alpha,\beta} + 0.5\text{a SO}_4^{2-} + \text{aH}^+ \rightarrow \text{aCO}_2 + \text{bNH}_4^+ + \text{cH}_3\text{PO}_4 + 0.5\text{aH}_2\text{S} + \text{aH}_2\text{O}$	R5
$\text{OM}^{\alpha,\beta} \rightarrow 0.5\text{aCO}_2 + \text{bNH}_4^+ + \text{cH}_3\text{PO}_4 + 0.5\text{aCH}_4$	R6
$\text{CO}_2 + 4\text{H}_2 \rightarrow \text{CH}_4 + 2\text{H}_2\text{O}$	R7
Secondary and other reactions	
$2\text{O}_2 + \text{NH}_4^+ + 2\text{HCO}_3^- \rightarrow \text{NO}_3^- + 2\text{CO}_2 + 3\text{H}_2\text{O}$	R8
$\text{O}_2 + 4\text{Fe}^{2+} + 8\text{HCO}_3^- + 2\text{H}_2\text{O} + 4\chi^\alpha\text{H}_2\text{PO}_4^- \rightarrow 4\text{Fe(OH)}_3^\alpha + 4\chi^\alpha\text{Fe}_{\text{ox}}\text{P} + 8\text{CO}_2$	R9
$2\text{O}_2 + \text{FeS} \rightarrow \text{SO}_4^{2-} + \text{Fe}^{2+}$	R10
$7\text{O}_2 + 2\text{FeS}_2 + 2\text{H}_2\text{O} \rightarrow 4\text{SO}_4^{2-} + 2\text{Fe}^{2+} + 4\text{H}^+$	R11
$2\text{O}_2 + \text{H}_2\text{S} + 2\text{HCO}_3^- \rightarrow \text{SO}_4^{2-} + 2\text{CO}_2 + 2\text{H}_2\text{O}$	R12
$2\text{O}_2 + \text{CH}_4 \rightarrow \text{CO}_2 + 2\text{H}_2\text{O}$	R13
$2\text{Fe(OH)}_3^\alpha + 2\chi^\alpha\text{Fe}_{\text{ox}}\text{P} + \text{H}_2\text{S} + 4\text{CO}_2 \rightarrow 2\text{Fe}^{2+} + 2\chi^\alpha\text{H}_2\text{PO}_4^- + \text{S}^0 + 4\text{HCO}_3^- + 2\text{H}_2\text{O}$	R14
$2\text{Fe(OH)}_3^{\beta,\beta(\text{max}),\beta(\text{pulse})} + 2\chi^\alpha\text{Fe}_{\text{ox}}\text{P} + \text{H}_2\text{S} + 4\text{CO}_2 \rightarrow 2\text{Fe}^{2+} + 2\chi^\alpha\text{H}_2\text{PO}_4^- + \text{S}^0 + 4\text{HCO}_3^- + 2\text{H}_2\text{O}$	R15
$\text{Fe}^{2+} + \text{H}_2\text{S} \rightarrow \text{FeS} + 2\text{H}^+$	R16
$\text{FeS} + \text{H}_2\text{S} \rightarrow \text{FeS}_2 + \text{H}_2$	R17
$4\text{S}_0 + 4\text{H}_2\text{O} \rightarrow 3\text{H}_2\text{S} + \text{SO}_4^{2-} + 2\text{H}^+$	R18
$\text{FeS} + \text{S}^0 \rightarrow \text{FeS}_2$	R19
$\text{SO}_4^{2-} + \text{CH}_4 + \text{CO}_2 \rightarrow 2\text{HCO}_3^- + \text{H}_2\text{S}$	R20
$\text{CH}_4 + 8\text{Fe(OH)}_3^{\alpha,\beta,\beta(\text{max}),\beta(\text{pulse})} + 8\chi^{\alpha,\beta}\text{Fe}_{\text{ox}}\text{P} + 15\text{H}^+ \rightarrow \text{HCO}_3^- + 8\text{Fe}^{2+} + 8\chi^{\alpha,\beta}\text{H}_2\text{PO}_4^- + 21\text{H}_2\text{O}$	R21
$\text{Fe(OH)}_3^\alpha + (\chi^\alpha - \chi^\beta)\text{Fe}_{\text{ox}}\text{P} \rightarrow \text{Fe(OH)}_3^\beta + (\chi^\alpha - \chi^\beta)\text{H}_2\text{PO}_4^-$	R22
$\text{Fe}^{2+} + \text{CO}_3^{2-} \rightarrow \text{FeCO}_3$	R23
$\text{Fe(PO}_4)_2 + 3\text{H}_2\text{S} \rightarrow 2\text{FeS} + 2\text{HPO}_4^{2-} + 4\text{H}^+$	R24
$\text{Mn}^{2+} + \text{HCO}_3^- + \text{OH}^- \rightarrow \text{MnCO}_3 + \text{H}_2\text{O}$	R25
$2\text{Mn}^{2+} + 2\text{O}_2 + 4\text{H}^+ \rightarrow 2\text{Mn(OH)}_2^\alpha$	R26
$\text{Mn(OH)}_2^{\alpha,\beta} + 2\text{H}_3\text{PO}_4 + 2\text{Fe}^{2+} \rightarrow \text{Mn}^{2+} + 2\chi^\alpha\text{Fe}_{\text{ox}}\text{P}$	R27
$\text{Mn(OH)}_2^\alpha + \text{H}_2\text{S} \rightarrow \text{Mn}^{2+} + \text{S}_0 + 2\text{H}_2\text{O}$	R28
$\text{Mn(OH)}_2^\beta + \text{H}_2\text{S} \rightarrow \text{Mn}^{2+} + \text{S}_0 + 2\text{H}_2\text{O}$	R29
$\text{Mn(OH)}_2^\alpha \rightarrow \text{Mn(OH)}_2^\beta$	R30
$4\text{Mn(OH)}_2^{\alpha,\beta} + \text{CH}_4 + 7\text{H}^+ \rightarrow 4\text{Mn}^{2+} + \text{HCO}_3^- + 5\text{H}_2\text{O}$	R31
$\text{Fe(OH)}_3^{\beta,\beta(\text{pulse})} + (\chi^{\beta(\text{max})} - \chi^{\beta,\beta(\text{pulse})})\text{HPO}_4^{2-} \rightarrow \text{Fe(OH)}_3^{\beta(\text{max})}$	R32

Organic matter is of the form $((\text{CH}_2\text{O})_a(\text{NH}_4^+)_b(\text{H}_3\text{PO}_4)_c$, where $a=1$, $b=1/16$ and $c=300/1$. α , β , & γ describe different fractions (i.e. highly reactive, less reactive and refractory). $\chi^{\alpha,\beta,\gamma}$ describes the different P:Fe ratios of $\text{Fe(OH)}_3^{\alpha,\beta,\gamma}$. Reactions for different Fe(OH)_3^β fractions (β , $\beta(\text{max})$ and $\beta(\text{pulse})$) are the same and are therefore combined as Fe(OH)_3^β .

Table S.3. Environmental parameters used in the model.

Description	Symbol	Value or expression	unit	source
Porosity at the Surface	ϕ_0	0.935	vol vol ⁻¹	a
Porosity at depth	ϕ_∞	0.87	vol vol ⁻¹	a
Porosity e-folding distance	γ	35	cm	b
Sediment density	ρ	2.65	g cm ⁻³	c
Temperature	T	2.77	°C	a
Salinity	S	5.05		a
Advection velocity of solids at depth	v_∞	$\frac{F_{sed}}{\rho(1-\phi_\infty)}$		—
Bioturbation coefficient at sediment-water interface	D_b	1.76	cm ² yr ⁻¹	b
Bioirrigation coefficient at sediment-water interface	α	$45*10^4$	yr ⁻¹	b
Mixed layer depth	ζ	11	cm	b
C:N ratio of organic matter	C/N	6.625	mol mol ⁻¹	d
C:P ratio of organic matter	C/P	300	mol mol ⁻¹	b
P:Fe(OH) ₃ ^α	χ^α	0.28	mol mol ⁻¹	b
P:Fe(OH) ₃ ^β	χ^β	0.23	mol mol ⁻¹	b
P:Fe(OH) ₃ ^γ	χ^γ	0.11	mol mol ⁻¹	b
P:Fe(OH) ₃ ^{β(max)}	$\chi^{\beta(max)}$	0.28	mol mol ⁻¹	b
P:Fe(OH) ₃ ^{β(pulse)}	$\chi^{\beta(pulse)}$	0	mol mol ⁻¹	b

Sources: (a) Measured; (b) Model constrained; (c) Reed et al. (2011b); (d) Redfield (1958).

Table S.4. Boundary conditions of solids and solutes at the sediment-water interface in the model. Time dependent fluxes of OM^{α,β,γ}, Fe(OH)₃^{α,β,γ}, Mn(OH)₂^{α,β}, Mn carbonates and sedimentation rate at the sediment-water interface are shown in figure 3. For all chemical species a zero-gradient boundary condition was specified at the bottom of the model domain.

Solids	Flux at sediment water interface	Unit
F FeS	0	mol m ⁻² yr ⁻¹
F FeS ₂	0	mol m ⁻² yr ⁻¹
F SO	0	mol m ⁻² yr ⁻¹
F FeCO ₃	0.27	mol m ⁻² yr ⁻¹
F Vivianite	0	mol m ⁻² yr ⁻¹
F Detr. P	0.034	mol m ⁻² yr ⁻¹
F Auth. P	0.03	mol m ⁻² yr ⁻¹

Solutes	BW concentration	Unit
C O ₂ ⁻	0.091	mol m ⁻³
C NO ₃ ⁻	0	mol m ⁻³
C SO ₄ ²⁻	4.05	mol m ⁻³
C Fe ²⁺	0	mol m ⁻³
C Mn ²⁺	0	mol m ⁻³
C H ₂ S	0	mol m ⁻³
C NH ₄ ⁺	0	mol m ⁻³
C HPO ₄ ²⁻	0.21	mol m ⁻³
C DIC	1.5	mol m ⁻³

Table S.5. Analyses of vivianite crystals from below the SMTZ at site NB8 with electron microprobe-EDS. Vivianite crystals were collected from 3 different depths. The average value and standard deviation for each element was calculated from 7 EDS point analyses.

Element	mol %
O	37.8 ± 3.4
Na	0.4 ± 0.2
Mg	0.8 ± 0.6
Al	6.3 ± 6.2
Si	2.6 ± 1.5
P	13.5 ± 5.4
Ca	0.3 ± 0.2
Mn	6.9 ± 2.3
Fe	31.4 ± 6.3
mol mol⁻¹	
Fe/P	3.3 ± 2.0
Fe/Mn	4.7 ± 0.8
(Fe+Mn)/P	4.1 ± 2.5
Mn/P	0.8 ± 0.5
(Fe+Mn+Mg)/P	4.3 ± 2.5

Table S.6. Reaction equations implemented in the model.

Primary redox reaction equations	
$R1 = k_{\alpha,\beta} OM^{\alpha,\beta} \left(\frac{[O_2]}{K_{m,O_2} + [O_2]} \right)$	E1
$R2 = k_{\alpha,\beta} OM^{\alpha,\beta} \left(\frac{[NO_3^-]}{K_{m,NO_3} + [NO_3^-]} \right) \left(\frac{K_{m,O_2}}{K_{m,O_2} + [O_2]} \right)$	E2
$R3 = k_{\alpha,\beta} OM^{\alpha,\beta} \left(\frac{[Mn(OH)_2]}{K_{m,Mn(OH)_2} + [Mn(OH)_2]} \right) \left(\frac{K_{m,NO_3^-}}{K_{m,NO_3} + [NO_3^-]} \right) \left(\frac{K_{m,O_2}}{K_{m,O_2} + [O_2]} \right)$	E3
$R4 = k_{\alpha,\beta} OM^{\alpha,\beta} \left(\frac{[Fe(OH)_3]}{K_{m,Fe(OH)_3} + [Fe(OH)_3]} \right) \left(\frac{K_{m,Mn(OH)_2}}{K_{m,Mn(OH)_2} + [Mn(OH)_2]} \right) \left(\frac{K_{m,NO_3^-}}{K_{m,NO_3} + [NO_3^-]} \right) \left(\frac{K_{m,O_2}}{K_{m,O_2} + [O_2]} \right)$	E4
$R5 = k_{\alpha,\beta} OM^{\alpha,\beta} \left(\frac{[SO_4^{2-}]}{K_{m,SO_4^{2-}} + [SO_4^{2-}]} \right) \left(\frac{K_{m,Fe(OH)_3}}{K_{m,Fe(OH)_3} + [Fe(OH)_3]} \right) \left(\frac{K_{m,Mn(OH)_2}}{K_{m,Mn(OH)_2} + [Mn(OH)_2]} \right) \left(\frac{K_{m,NO_3^-}}{K_{m,NO_3} + [NO_3^-]} \right) \left(\frac{K_{m,O_2}}{K_{m,O_2} + [O_2]} \right)$	E5
$R6 = k_{\alpha,\beta} OM^{\alpha,\beta} \left(\frac{K_{m,SO_4^{2-}}}{K_{m,SO_4^{2-}} + [SO_4^{2-}]} \right) \left(\frac{K_{m,Fe(OH)_3}}{K_{m,Fe(OH)_3} + [Fe(OH)_3]} \right) \left(\frac{K_{m,Mn(OH)_2}}{K_{m,Mn(OH)_2} + [Mn(OH)_2]} \right) \left(\frac{K_{m,NO_3^-}}{K_{m,NO_3} + [NO_3^-]} \right) \left(\frac{K_{m,O_2}}{K_{m,O_2} + [O_2]} \right)$	E6
$R7 = k_1 DIC \left(\frac{K_{m,SO_4^{2-}}}{K_{m,SO_4^{2-}} + [SO_4^{2-}]} \right) \left(\frac{K_{m,Fe(OH)_3}}{K_{m,Fe(OH)_3} + [Fe(OH)_3]} \right) \left(\frac{K_{m,Mn(OH)_2}}{K_{m,Mn(OH)_2} + [Mn(OH)_2]} \right) \left(\frac{K_{m,NO_3^-}}{K_{m,NO_3} + [NO_3^-]} \right) \left(\frac{K_{m,O_2}}{K_{m,O_2} + [O_2]} \right)$	E7
Secondary redox and other reaction equations	
$R8 = k_2 [O_2][NH_4^+]$	E8
$R9 = k_3 [O_2][Fe^{2+}]$	E9
$R10 = k_4 [O_2][FeS]$	E10
$R11 = k_5 [O_2][FeS_2]$	E11
$R12 = k_6 [O_2][\sum H_2S]$	E12
$R13 = k_7 [O_2][CH_4]$	E13
$R14 = k_8 [Fe(OH)_3^\alpha][\sum H_2S]$	E14
$R15 = k_9 [Fe(OH)_3^{\beta,\beta(max),\beta(pulse)}][\sum H_2S]$	E15
$R16 = k_{10} [Fe^{2+}][\sum H_2S]$	E16
$R17 = k_{11} [FeS][\sum H_2S]$	E17
$R18 = k_{12} [S^0]$	E18
$R19 = k_{13} [Fe^{2+}][S^0]$	E19
$R20 = k_{14} [SO_4^{2-}][CH_4]$	E20
$R21 = k_{15} [Fe(OH)_3^{\alpha,\beta,max,\beta(pulse)}][CH_4]$	E21
$R22 = k_{16} [Fe(OH)_3^\alpha]$	E22
$R23 = k_{17} [Fe^{2+}][HCO_3^-]$	E23
$R24 = k_{18} [Fe_3(HPO_4^{2-})_2][\sum H_2S]$	E24
$R25 = k_{19} [Mn^{2+}][HCO_3^-]$	E25
$R26 = k_{20} [Mn^{2+}][O_2]$	E26
$R27 = k_{21} [Mn(OH)_2^{\alpha,\beta}][HPO_4^{2-}][Fe^{2+}]$	E27
$R28 = k_{22} [Mn(OH)_2^\alpha][\sum H_2S]$	E28
$R29 = k_{23} [Mn(OH)_2^\beta][\sum H_2S]$	E29
$R30 = k_{24} [Mn(OH)_2^\alpha]$	E30
$R31 = k_{25} [Mn(OH)_2^{\alpha,\beta}][CH_4]$	E31
$R32 = k_{26} [Fe(OH)_3^{\beta,\beta(max),\beta(pulse)}][HPO_4^{2-}]$	E32

Table S.7. Reaction parameters used in the model.

Parameter	Value	Unit	Source	Values in literature
k_α	0.3	yr^{-1}	a,b	0.05-1.62
k_β	0.0086	yr^{-1}	b,h	0.0025-0.0086
K_{O_2}	20	$\mu\text{m L}^{-1}$	c	1-30
$K_{NO_3^-}$	4	$\mu\text{m L}^{-1}$	c	4-80
$K_{Mn(OH)_2}$	4	$\mu\text{m g}^{-1}$	c	4-32
$K_{Fe(OH)_3}$	65	$\mu\text{m g}^{-1}$	c	65-100
$K_{SO_4^{2-}}$	1.6	$\mu\text{m L}^{-1}$	c	1.6
$k1$ (E7)	0.044	yr^{-1}	i	0.0011
$k2$ (E8)	10000	mmol yr^{-1}	c,d	5000-39000
$k3$ (E9)	1.4×10^5	mmol yr^{-1}	c	1.4×10^5
$k4$ (E10)	300	mmol yr^{-1}	c	300
$k5$ (E11)	1	mmol yr^{-1}	c	1
$k6$ (E12)	160	mmol yr^{-1}	c	160
$k7$ (E13)	10^7	mmol yr^{-1}	c	10^7
$k8$ (E14)	55	mmol yr^{-1}	c,g,i	8-100
$k9$ (E15)	44	mmol yr^{-1}	c,j	0.004-100
$k10$ (E16)	9000	mmol yr^{-1}	b,d	100-14800
$k11$ (E17)	10^{-15}	mmol yr^{-1}	e,i	0.0003-3.15
$k12$ (E18)	3	yr^{-1}	f	3
$k13$ (E19)	0.0025	mmol yr^{-1}	f,g	0.001-7
$k14$ (E20)	17	mmol yr^{-1}	c,g	10(c)-120(g)
$k15$ (E21)	0.0021	mmol yr^{-1}	g,i	1.6×10^{-7} - 0.0074
$k17$ (E23)	0	mmol yr^{-1}	i	0.0027
$k18$ (E24)	8×10^{-4}	mmol yr^{-1}	i	8×10^{-4}
$k19$ (E25)	0.265	mmol yr^{-1}		Model constrained
$k20$ (E26)	1200	mmol yr^{-1}	c	800-20.000
$k21$ (E27)	0.002	mmol yr^{-1}	f	2
$k22$ (E28)	0.5	mmol yr^{-1}	c	<100.000 (20)
$k23$ (E29)	0.4	mmol yr^{-1}	c	<100.000 (20)
$k24$ (E30)	1.8	yr^{-1}	f	1.8
$k25$ (E31)	0.0017	mmol yr^{-1}		Model constrained
$k26$ (E32)	3	mmol yr^{-1}		Model constrained
V_{max}	10^{-6}	yr^{-1}		Model constrained
half saturation conc. Fe^{2+}	1000	$\mu\text{mol yr}^{-1}$		Model constrained
half saturation conc. HPO_4^{2-}	1000	$\mu\text{mol yr}^{-1}$		Model constrained

Sources:^a(Moodley et al., 2005); ^b(Reed et al., 2011b); ^c(Wang and Van Cappellen, 1996); ^d(Reed et al., 2011a); ^e(Rickard and Luther, 1997); ^f(Berg et al., 2003); ^g(Rooze et al., 2016); ^h(Reed et al., 2016); ⁱ(Egger et al., 2016a); ^j(Egger et al., 2016b);

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