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Dear Prof. Abril,

Thank you for taking into consideration our manuscript for publication in *Biogeosciences*. We are grateful for the granted extension of the submission deadline of our revised manuscript. This has allowed us to improve the depth of the discussion and the scientific significance of the work. We attach our responses to the reviewer’s comments, as well as a revised version of the manuscript and supplementary material in which the edits have been highlighted.

We have made several important changes to the manuscript. Foremost, we have changed the manuscript title and improved the structure of the discussion, as per the suggestions of yourself and Referee #2. We have also increased the relevance of the manuscript to other researchers working on trace gas emissions from lakes by expanding the discussion with a detailed analysis of between-lake differences in the drivers of emissions, which include the effects of atmospheric stability and sheltering on the gas transfer velocity. Contextualizing in this way, we have illustrated which flux-driving mechanisms may be important in different lake types, such as those that are shallow and exposed to wind, deeper and more sheltered, or lakes that are fed by a stream. Minor changes include improved model estimates of lake CH$_4$ emissions by using lake-specific scaling parameters – the analyses for which are provided in the updated supplement.

We hope that these revisions have made our manuscript suitable for publication in *Biogeosciences*. We will be pleased to answer any additional questions or make any further changes that you or the reviewers recommend. Thank you for your kind support.

On behalf of the co-authors,

Joachim Jansen
Response to reviewer 1:

L 33: Statement “A significant portion of sediment-produced CH4 reaches the atmosphere by turbulence-driven diffusion-limited gas exchange” is misleading and term “significant” is conveniently vague. The synthesis of CH4 fluxes from inland waters given by Bastviken et al (2011) and cited by the authors provides a total diffusive flux of CH4 of 9.9 TgCH4/yr that is much smaller than the total flux of 103.3 TgCH4/yr. I suggest that authors be more specific and introduce quantitatively the importance of diffusive CH4 fluxes from inland waters.

Author’s response: we have changed the introductory paragraph to include the estimated contribution of open water diffusive CH4 emissions from three regional and global budget studies. We note that the Bastviken et al. (2011) study separates ‘diffusive’ and ‘storage’ emissions. Because the latter is defined as the ‘flux when CH4 stored in the water column is emitted upon lake overturn’, and occurs via the diffusion-limited pathway, we counted storage fluxes as diffusive fluxes. We thus computed the contribution of diffusion from the pathway specific budgets in Table 1 of Bastviken et al. (2011) as follows: (‘diffusive’ + ‘storage’)/(‘plant flux’ + ‘ebullition’ + ‘diffusive’ + ‘storage’) = 34.8%. This is within the range of values computed from diffusive and ebullitive flux estimates in DelSontro et al. (2018) (21-24%) and Wik et al. (2016b) (46%).

L36: Chambers also “traditionally” capture CH4 ebullition fluxes in addition to diffusive fluxes.

Author’s response: as described in the method section (L. 124-125) our chambers were equipped with plastic shields to prevent bubbles from entering the chamber headspace.

L44: DelSontro et al. (2018) estimated global (and not regional as stated) CH4 emissions based on a statistical (and not “process-based” as stated) approach.

Author’s response: we have removed the reference to DelSontro et al. (2018).

L 52: the formulation of equation (1) was given by Liss and Slater (1974) well before Wanninkhof (1992).

Author’s response: the reference has been changed.

I have the impression that methane oxidation is the main process “that dissociate[s] production from emission rates”, it’s odd this is not mentioned in section L69-83.

Author’s response: we have included oxidation as one of the dissociating factors.

L141-143: Can you please elaborate this section? It’s unclear how the effect of artificial enhancement of turbulence was discarded, and how the citation of the Ribas-Ribas et al. paper is relevant in this context, since this technical paper describes an apparatus to measure fluxes with chambers.

Author’s response: we included a more detailed description of the analysis of the cited paper: “Ribas-Ribas et al. (2018) compared acoustic Doppler velocimeter measurements inside and outside the perimeter of a chamber of similar design, size and flotation depth as those used in this study, and, based on a comparison of measured TKE dissipation rates and computed gas transfer velocities, concluded that the chambers did not cause artificial turbulence.”
L164: It’s strange that only one standard was used to calibrate the GC-FID (a multipoint calibration curve is recommended, Wilson et al. 2018), and the value of standard is so low compared to the sample values, as pCH4 in the headspace was » 2 ppm, as shown in Figure 2. Authors should provide an accuracy and precision of the CH4 measurements and propagate this into an error analysis of the CH4 fluxes, as well as for the computed k600 values.

Author’s response: detector FID’s with N2 carriers are known to be linear over several orders of magnitude (e.g. Colson, 1986). The linearity of the detector is better than the uncertainty in the gas mixtures.

The instrument precision is discussed in Section 2.4 of the paper. 10 standard measurements before and after each run were used to assess instrument precision and drift. The precision – defined as the relative standard deviation of the 10 standard measurements - was generally <0.25%. This converts to negligible deviations in the surface concentration and derived fluxes, and would not affect any of the binned or multi-year mean values or functional relationships discussed in the paper. For example, relative standard deviations of the air-water concentration difference binned by time, temperature and wind speed (Fig. 4e-g) are generally >30%. Thus, uncertainty in this study is dominated by the spatiotemporal variability of the fluxes and surface concentrations rather than uncertainty in the concentration measurements.

L168: Could be useful to explain here how zmix was estimated from the temperature profiles.

Author’s response: the mixing depth was estimated from a density gradient threshold, as described at L. 431. We have now written a few sentences about water density calculations and mixing depth in section 2.5. Here is the revised text:

“Water density was computed from temperature and salinity (Chen and Millero, 1977), using lake-averaged specific conductivity and a salinity factor [mS cm^{-1} / g kg^{-1}] of 0.57. The salinity factor was based on a linear regression of simultaneous measurements of conductivity and dissolved solids (R^2 = 0.99, n = 7) in five lakes in the Torneträsk catchment (Miljödata-MVM, 2017). We defined the diel mixing depth (z_{mix}) at a density gradient threshold (dρ/dz) of 0.03 kg m^{-3} m^{-1} (Rueda et al., 2007).”

L206: This equation assumes that Caq remains unchanged during the 24h chamber deployment which seems unrealistic. Please clarify what does Caq correspond to. Was Caq measured each time Ch was measured?

Author’s response: C_{aq} is defined at L. 51 and corresponds to the measured CH4 concentration in the surface water. When we compute gas transfer velocities from chamber fluxes and the air-water concentration difference (C_{aq}-C_{air,eq}), we only use water samples that were collected simultaneously with, and in close proximity to the floating chamber observations. We took one water sample at each chamber location. Thus when we compute k_{ch} from Eq. 2, we assume that the flux at the time of the concentration measurement was equal to the 24h flux. It is likely that the flux varied over those 24 hours (Fig. 7b,d). However, a quantitative bias assessment would require continuous, 24h observations of the diffusive fluxes and of the surface concentration, which were unavailable for this study.

L207: specify if T is the average during the 24h chamber deployment. In Eq [3] explain how dx/dt was computed. Linear regression over all points? Difference between end and start? Difference between each of the samples?
Author’s response: we have now specified how T and dx/dt were computed. That is, the average over the flux integration time (this is the 24h chamber deployment time for most of our analyses) and OLS linear regression of concentrations onto time, respectively. Here is the revised text:

“\( \frac{\partial x_h}{\partial t} \) is the headspace mole fraction change [mol mol\(^{-1}\) d\(^{-1}\)] computed with an ordinary least squares (OLS) linear regression (Fig. 2), \( M \) is the molar mass of CH\(_4\) (0.016 mg mol\(^{-1}\)), \( P \) is the air pressure [Pa], \( T_{air} \) is the air temperature [K]. Scalar \( c_1 \) corrects for accumulation of CH\(_4\) gas in the chamber headspace and increases over the deployment time. Comparing both chamber flux calculation methods we find \( c_1 = 1.21 \) for 24 hour deployments (OLS, \( R^2 = 0.85, n = 357 \)). Chambers were sampled up to 4 times during deployment (at 10 minutes, 1–5 hours and 24 hours) which allowed us to compute fluxes at time intervals of 1 hour and 24 hours. \( P \) and \( T_{air} \) were averaged over the relevant time interval.”

The use of a single value for scalar \( c_1 \) is surprising because the accumulation of CH\(_4\) in the chamber should depend on the flux intensity itself, so I would expect this value not to be constant.

Author’s response: \( c_1 \) is based on a linear regression of fluxes computed with Eq. 3 (simple linear regression in the time vs chamber headspace concentration plot) and Eq. 2, which corrects for the headspace effect. The good linear fit (\( R^2 = 0.85 \), L. 216) indicates to us that the headspace effect did not change significantly within the range of fluxes observed. If the headspace accumulation effect would increase significantly with the flux, we would expect a highly non-linear correlation.

In equations 2 and 3, the same symbol (\( T \)) is used for water temperature and air temperature, when separate symbols should be used for distinct variables.

Author’s response: we have specified the symbols in the equations.

L 241: It’s odd that both a symbol and an abbreviation are used for turbulent kinetic energy

Author’s response: they refer to different quantities. As stated at L. 241, we use TKE as an abbreviation for ‘turbulent kinetic energy’ and epsilon as the symbol for the dissipation rate of turbulent kinetic energy. Both the abbreviation and the symbol are commonly used in the literature.

L307: Please explain how the residence time of a CH\(_4\) molecule in the lake was estimated.

Author’s response: this computation is described in section 2.7 at L198-199. The sentence reads: “We computed the average residence time of a CH\(_4\) molecule by dividing the amount stored by the lake mean surface flux.”

In Figure 6 the relation between storage time and water T seems significant for I Harrjon and M Harrsjon.

Author’s response: we infer that the reviewer refers to Fig. 6e, which shows an increase of storage with water temperature. We fitted Arrhenius functions, added lines of best fit to the plot and included the following sentence in the figure caption: “Arrhenius-type functions (Eq. 7) adequately described the relation between storage and temperature in each lake (\( R^2 \geq 0.70, p < 0.001 \)).”

L637-639: why would damping of turbulence by near-surface stratification affect particularly your lakes but not those reported by Cole & Caraco (1998) and Wanninkhof and Crusius (2003)?
Author’s response: we moved the discussion of turbulence damping to a separate paragraph, which now reads: “Damping of turbulence results from near-surface stratification and can reduce the gas transfer velocity (MacIntyre et al., 2010, 2018), however, such strong stratification (N > 25 cph) was intermittent in our study (Fig. 5f-h).”

An alternative explanation could be fetch limitation (Wanninkhof 1992) in the very small sampled ponds, and this effect could be more marked at high wind speeds than at low wind speeds.

Author’s response: we thank the reviewer for this suggestion.

Figure 9: abbreviations given in the plot should be defined in the figure legend.

Author’s response: abbreviations of literature references are now included in the figure caption.

In Figure 9, the binned data value at highest wind correspond to a wind speed that is higher than highest wind speeds of individual Kch measurements. How is this possible? The binned value should be below the highest individual wind speeds measurements.

Author’s response: we chose to plot the symbols for binned quantities at the center value of each bin. The center value of the bin may be higher than or lower than the mean value of the datapoints contained in that bin.

L668-670: While I agree with the idea that CH4 is formed in the sediment, as this seems the most likely process in this type of environments, I do not see why the Arrhenius relation proves this. All biological processes follow Arrhenius-type relations, so the occurrence of this relation only shows that CH4 might be biologically produced, but does not allow to pin-point it as sedimentary. Please rephrase. Since it’s not explained in the text how the residence time was computed it is not clear how this proves or disproves a sedimentary CH4 production.

Author’s response: we explain how the residence time was computed at L. 198-199. Sediment production of CH4 is well-known in aquatic systems and we do not mean to prove or disprove it with our observations. We restructured the sentence to put more emphasis on redistribution rather than sediment production: “The Arrhenius-type relation of CH4 fluxes and concentrations (Fig. 4b,f) together with short CH4 residence times (Fig. 6) suggest that efficient redistribution of dissolved CH4 strongly coupled emissions from the Stordalen lakes to sediment production.”

L671: Why do high CH4 in the stream suggest this is of “terrestrial” origin? CH4 is also produced in-stream in sediments. Do you mean that CH4 comes from soils then to streams? Or that the stream CH4 production is fueled by terrestrial organic matter? This statement is very vague and confusing, please clarify.

Author’s response: we have clarified this sentence as follows: “High CH4 concentrations in the stream suggest that external inputs of CH4 — produced in the fens and transported into the stream with surface runoff, or produced in stream sediments — may have elevated emissions in Mellersta Harrsjön (Lundin et al., 2013; Paytan et al., 2015).”

L677-679: or alternatively from dilution with water with low CH4 from surface runoff and rain?
Author’s response: we thank the reviewer for this suggestion.

L723: methane oxidation is also an important removal process that should contribute to imbalances between production and emission.

Author’s response: One could argue that because methane oxidation rates tend to change with concentration and temperature, they would influence the flux on timescales similar to those of production (that is, timescales of a week or more). Changes in storage occur within the short residence times of CH4 gas (1-5 days). This suggests that dissociation occurs on shorter timescales – i.e. those governed by wind speed. However, in this paper we do not present a quantitative assessment of methane oxidation. Following the reviewer’s earlier comment we have mentioned oxidation as a process that dissociates production from emission in the introduction.

L730-740: Wave breaking and bubbles also explain why the relation between the gas transfer velocity and wind speed is non-linear in the ocean (e.g. Wanninkhof 1992), while here you report a linear relation between gas transfer velocity and wind speed.

Author’s response: the processes obtained in large water bodies are not necessarily operative in small lakes. Moreover, it is not clear from our data whether the wind-k relationship is linear or non-linear. At L. 643-645 we state “Due to the large spread of the chamber-derived gas transfer velocities (small rhombuses, Fig. 9) a power-law exponent to U10 (1.0 (0.0-1.8); exponent and 95% CI) and thus the nature of the wind-k relation could not be determined with confidence.”

L763: Is thermocline tilting expected to occur in small ponds?

Yes, wind forcing can cause the thermocline to tilt in small water bodies. The extent of tilt is computed from the Wedderburn number (Imberger and Patterson, 1989). This dimensionless index takes into account stratification, wind speed, and basin dimensions. The lakes in this study are larger than ponds, albeit small, and for the relatively high winds found at these arctic sites, thermocline tilting is expected.

L797-811: Methane oxidation affects CH4 concentrations, so it’s very obscure why methane oxidation should affect the alpha term. This is a scaling between gas transfer velocity that is measured and modelled, and gas transfer velocity depends on physical processes (mainly turbulence)

Author’s response: in this study we infer $k_{ch}$ from measurements of the chamber concentration increase and surface concentrations. The formulations of Eq. 1 and Eq. 2 implicitly assume that all CH4 measured in the water column is emitted to the atmosphere. However, if a fraction of CH4 is removed by oxidation, this would lead to an overestimation of $\Delta[CH_4]$ and an underestimation of $k_{ch}$. This in turn affects the alpha term. So oxidation does not impact gas transfer velocities directly, but may bias the gas transfer velocity high if one uses the two-layer model (Eq. 1), as is common. We have added a few sentences to the paragraph to clarify this point.

References

Chen, C.-T. and Millero, F. J.: The use and misuse of pure water PVT properties for lake waters, Nature,


Response to reviewer 2:

The authors wish to thank the reviewer for their thoughtful comments and detailed suggestions, which helped improve the paper and clarify the narrative.

RC2: This manuscript documents almost a decade of weekly-monthly resolution methane concentration and flux data from 3 sub-Arctic lakes. They found Arrhenius-type temperature relationships with flux and concentration, which has been found before and suggests a strong coupling to methane production rates. They also found that wind shear drove the gas transfer velocity, but on timescales of less than a month while temperature was a driver on timescales longer than a month. They also found that stratification only played a small role in storage/accumulation and emissions in general from their systems. The methods are sound and the results are well-detailed, perhaps a bit on the long side. The dataset is quite unique as it is so long. The authors need to use the length of their dataset to substantiate their results more. They find a temperature relationship that has been shown before in quite a few other datasets, but perhaps ones not as long as theirs. Also, they find that convection does not play as large of a role in surface turbulence as has been found in other lakes. How do those datasets compare to theirs? I also strongly suggest the authors structure the discussion to highlight the main takeaway messages from this work.

Author’s response: The concerns raised in the reviewer’s initial statement have been addressed in our response to individual comments below.

General comments:

RC2: 1. The title seems broad as if you are referring to all lakes, but you actually point out in the manuscript many differences between your findings and those of other lakes, for example, in terms of convection contribution to k. I suggest you narrow down your title slightly. You could even highlight more in the title the amount of data that you have. This multi-year dataset is quite unique.

Author’s response: We have changed the title to “Drivers of diffusive CH₄ emissions from shallow subarctic lakes on daily to multi-year time scales.” However, we chose specify the length of the dataset in the abstract. The basic physics that control diffusion-limited emissions from water surfaces are common to all lakes though, of course, specifics such as depth and geomorphological setting will be unique to each. We feel that this is a contribution that is broadly useful.

RC2: 2. I think the discussion could do with some restructuring and more concisely define the main points of your findings. The subheadings closely follow the results structure, but this doesn’t help the reader easily identify your main points. I like the way you summarized your findings in the first paragraph of the last section (summary and conclusions). I would suggest laying out the discussion with subheadings similar to the structure in that paragraph, at least to start and then edit from there. You also may not need all the information in the discussion if you find it does not highlight one of your main points.

Author’s response: We believe the dataset and the variety of the analyses merits a detailed and thorough discussion. We hope the sections and subheadings as they are currently structured would allow for easy navigation to topical discussions of interest. Noting your point, we added summarizing sentences to some of the paragraphs, restructured Section 4.2 and removed section 4.7 as it does not add to the discussion. Thank you for having us revisit the organization.
Specific comments:

RC2: Line 50- should read ‘, of which the upper boundary.’

Author’s response: We changed the sentence in accordance with the reviewer’s suggestion.

RC2: Line 72 – did you not include Aben et al. 2017 because it is about ebullition? You don’t specifically mention diffusive only in this sentence.

Author’s response: Yes, correct. We considered the Aben et al. paper to not be directly relevant to the diffusion–limited emissions focus of our paper.

RC2: Line 101 – ‘stochastic tools’ sounds too vague here

Author’s response: Thanks for pointing this out. We changed line 101 to ”We then estimate the importance of these and other flux controls on different timescales.”

RC2: Line 129 – I would say ‘During the 24 hr period...’ to avoid confusion. But why 2-4 samplings? What resolution and why?

Author’s response: This information is detailed in section 2.8, where we write: “Chambers were sampled up to 4 times during deployment (at 10 minutes, 1–5 hours and 24 hours) which allowed us to compute fluxes at time intervals of 1 hour and 24 hours.” Also the use of a short and longer time sampling provided information on those manual fluxes that might have been more episodic (i.e. affected by sub-daily changes in the gas transfer velocity) than the more regular increases that we might expect given our assumptions about diffusion-limited emissions.

RC2: Line 135-136 – you need to define Fch,unsh and Fch,sh here in this sentence (i.e., place the variables after ‘shielded’ and ‘unshielded’)

Author’s response: Thanks for noting the confusion. We removed Fch,unsh-Fch,sh from the equation, as we clearly state that we talk about the difference.

RC2: Section 2.2 – Do you flush the chambers between samplings or leave them the entire 24 hrs?

Author’s response: This is clarified in section 2.8. We use the accumulation rate of gas in the chamber headspace to compute the flux, so we don’t flush the chamber within the 24 hour deployment period.

RC2: Section 2.3 – Do you flush or mix the 4m long tube before sampling?

Author’s response: Yes we do and we clarified this point in the text as follows: “the tubes were flushed by extracting a sample volume equal to the tube’s volume at each location and depth.”

RC2: Line 196 – do you mean ‘offshore’ instead of ‘nearshore’ here since you are differentiating between the littoral zone and another zone?

Author’s response: Yes, we consider the shallow littoral zone to be near-shore, and the deeper, pelagic or profundal zone to be offshore.

RC2: Line 198 – make sure the year is correct on the reference

Author’s response: Thanks, we have corrected the year.
RC2: Line 205 – define and give units for ‘kch’

Author’s response: $k_{ch}$ is now defined and units given.

RC2: Line 211-212 – why were there some water measurements not taken and which ones and how many?

Author’s response: The design of the initial water sampling program was not intended to facilitate computation of gas transfer velocities. Simultaneous and co-located sampling was introduced in years 2016 and 2017.

RC2: Line 239 – should be ‘kmod’ specifically in this sentence, no?

Author’s response: In our usage here, $k$ refers to the gas transfer velocity in general.

RC2: Line 245 – why do you need to do this qualitative comparison? Why is it important?

Author’s response: We added a note of explanation with the following sentence: “In this way, we can assess whether the flux relations with wind speed and temperature are reproduced by the model.”

RC2: Line 338 – define ‘oinit’

Author’s response: This term has now been defined in the text as follows: “To allow for comparison between variables we normalized each $\sigma$-series by its initial, smallest-bin value: $\sigma_{\text{norm}} = \sigma/\sigma_{\text{init}}$.”

RC2: Line 420 – include in the caption the panel letters for the histograms in parentheses too

Author’s response: Yes that will help our explanation, panel letters have been added.

RC2: Figure 4 caption – you need to describe the squares, triangles, and diamonds in the caption itself – all the variables that you are presenting here.

Author’s response: Thanks for noting our oversight, symbol descriptions have been added to the figure caption.

RC2: Figure 5 caption – what are the curves you speak of in line 500? Are you sure that e and f are the right panels when you discuss the white lines on line 499? What is the resolution in panels c and d?

Author’s response: Thanks for catching this; the white mixing depth lines are indeed displayed in panel f-h, not e-f. We replaced the word ‘curves’ with ‘lines’ at line 500. The resolution of the chamber flux and water concentration measurements was approximately weekly. We hope this is evident when looking at the monthly tick mark intervals.

RC2: Table 3 title – need to describe N here

Author’s response: The table title has been adjusted to reflect all variables.

RC2: Figure 6 caption – add ‘(a-c)’ after ‘residence time’ and ‘(d-f)’ after ‘storage’. You mention the regressions for residence time but not for storage. Also, it looks as if there could be a trend between temperature and storage (panel e) for at least 2 of the lakes. Was there not?

Author’s response: We have included the panel indicators, and fit storage quantities to Arrhenius-type exponential functions in panel e, which describe the data reasonably well ($R^2 \geq 0.70, p < 0.001$).
RC2: Line 560-561 – the sentence starting with ‘On diel timescales..’ needs rewording. I don’t understand it.

Author’s response: Thanks, we rewrote the sentence as follows: “On diel timescales $\Delta$[CH4] and kmod were out of phase; $\Delta$[CH4] peaked just before noon, when kmod reached its maximum value (Fig. 7b,d).”

RC2: Figure 7 – put a complete legend in panels a and c and state that they apply to panels b and d.

Author’s response: We preferred to keep the legend as is to avoid crowding in the left panels, but we changed the symbol colour of the 1-hour fluxes to improve the clarity of the figure.

RC2: Line 612 – what is ‘Twater/ice’?

Author’s response: Our surface temperature sensors were frozen in the ice in winter. Because we use the whole-year temperature timeseries in our spectral analysis, we specify that this variable reflects both summer and winter variability. In the caption, we now specify “temperature of the surface water and ice”.

RC2: Section 4.1 – The subheading ‘Magnitude’ doesn’t explain much. Magnitude of what?

Author’s response: We have changed the section title to ‘Magnitudes of fluxes and gas transfer velocities’.

RC2: Line 632 – you obtained lower k-values by nearly a factor of 2 compared to what?

Author’s response: This is in comparison to literature models. This has now been specified in the text.

RC2: Line 636 – who had the offset at 0 wind speed? You or the literature? Be specific as this sentence is a bit confusing.

Author’s response: Thanks for pointing out this omission. We meant that several models in the literature have a default offset at 0 wind speed. We have amended the text as follows: “Part of the difference with the models of Vachon and Prairie (2013), Cole and Caraco (1998) and Soumis et al. (2008) was caused by the offset at 0 wind speed.”

RC2: Line 637 – ‘Another explanation’ for what?

Author’s response: Thanks for noting our oversight. This refers to the other explanation for the low k-values found in our study. We changed the sentence to specify this.

RC2: Line 639-640 – how was the atmosphere stable?

Author’s response: We consider a stable atmosphere to be those periods when the tropospheric boundary layer being stably stratified, i.e. when the air temperature exceeds the surface water temperature.

RC2: Line 644-645 – I am confused because you have an equation in Figure 9 caption that has an exponent for u10 with 95% CIs.

Author’s response: The equation in the caption was a linear equation, while we discussed a power-law equation in the text. We’ve now changed the equation in the caption to the power-law equation of Table S1.
RC2: Section 4.2 – delete ‘the’ in the subheading

Author’s response: Thanks for noting this. ‘Drivers of flux’ sounds better.

RC2: Section 4.2 – this is a very important part of the discussion but I feel it needs a little more work to really bring out your main points. It reads a bit like a bunch of ideas thrown into a paragraph but without linking them all together nor highlighting why these ideas matter. For example, the first sentence states that the temperature relationship with flux and concentration suggests a strong coupling to sediment [methane] production (need that word ‘methane’ in there). I agree with this statement and it’s an important one because you did find some nice relationships there. But the next sentence talks about stream inputs (from your own data, correct?) and then the following sentence is back to how sediment methane production could be enhanced. They seem out of order. Then the last thought about the decrease in CH4 after cold rain events is actually still in line with the temperature relationship you saw but you start this sentence off attempting to state that that shouldn’t be the case if there was runoff from fens. This fens part goes more along with the streams sentence from above.

Author’s response: We have revisited the organization and added two introductory sentences to the paragraph to add context to the discussion: “Methane emitted from lakes in wetland environments can be produced in situ, or be transported in from the surrounding landscape (Paytan et al., 2015). The distinction is important because some controls on terrestrial methane production, such as water table depth (Brown et al., 2014), are irrelevant in lakes.” We also replaced “cold and rainy” in the final sentence of the paragraph with “rainy”, to emphasize that were are discussing horizontal transport processes here. We removed the sentence about terrestrial inputs of nutrients.

RC2: I feel the same for the second paragraph of the section. I think you clarify your point about the difference between your results and those of Read et al. I am actually not sure who had lake in the warmer, lower humidity regions – you or them? Also need to put the 50 w/m2 value in context. At the end, I wouldn’t use the word ‘expect’ because I think you showed this. And I believe in this whole section you should already elude to the fact that these drivers work on different timescales.

Author’s response: We have rewritten this section. Read et al. (2012) did not consider Monin-Obukhov similarity scaling in their analysis. When computing dissipation rates with it, wind shear is raised to the 3rd power and divided by depth whereas the contribution from buoyancy flux is only to the first power. With that constraint, buoyancy flux only drives near-surface turbulence when winds have ceased. Figure 4k shows this for our model. Thus, differences in the meteorology between temperate and arctic lakes are not relevant here. On average, the 50 W/m2 represents the value of the net long wave radiation (Lwin - LWout) we’ve computed during the ice-free season in the Toolik area. We normally measured Lwin and computed LWout as a function of the surface water temperature. For reference, in our arctic work at other sites, net long wave radiation applies to periods with cloudy conditions, as often occur in the Stordalen Mire.

RC2: Line 716-728 – The first sentence of this paragraph reads more like a summary sentence. It’s confusing to hear about the feedback before you describe how you got to that point. I would try restructuring this paragraph a bit. I would start with the second sentence and state it like so: ‘Higher temperatures led to elevated CH4 concentrations, which in turn increased emission rates, but high wind speed was correlated with high emission rates and low concentrations. In this way,...’
Author’s response: We agree and we rewrote the paragraph as suggested by the reviewer: “Higher temperatures led to elevated CH$_4$ concentrations (Fig. 4f) which in turn increased emission rates (Eq. 1, Fig. 4b) but high wind speed was correlated with high emission rates and low concentrations (Fig. 4c,g). Degassing prevented an unlimited increase of the emission rate with the gas transfer velocity. In this way, Δ[CH$_4$] acted as a negative feedback that maintained a quasi steady state between CH$_4$ production and removal processes throughout the ice-free season.”

RC2: Line 744 – add the range of binned means in those parentheses of 0 – 10

Author’s response: The ranges have been included.

RC2: Line 784-791 – This is actually one very long sentence. Consider splitting it.

Author’s response: Thank you, the sentence has been split per the reviewer’s suggestion.

RC2: Line 798-799 – missing a word or something here ‘….but can limit surface exchange could be responsible...’

Author’s response: We have split the sentence to clarify its meaning: “The observed variability in α' could be explained by chemical or biological factors that limit surface exchange. Such processes do not affect turbulence in the actively mixed layer, and are thus not accounted for in $k_{mod}$.”

RC2: Line 834-837 – So you don’t completely degas the lake, despite shallowness and frequent mixing, but you also don’t have storage/accumulation of methane. I am finding a hard time reconciling those two results. I feel this needs more explanation here but also in the discussion where you mention it.

Author’s response: Of course there are dynamics in the water column methane concentrations as a result of variability in the loss and input terms. Accumulation is transient – it changes on a timescale of days – and is the result of an imbalance between production and emission rates. Storage increases during long periods of stratification are not due not only due to the reduction in turbulence-driven emissions but also, in the ice-free seasons especially, to higher production rates as a result of elevated water temperatures. We rewrote section 4.3 to provide a more intuitive explanation of these processes.
Drivers of diffusive lake-CH$_4$ emissions from shallow subarctic lakes on daily to multi-year time scales

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Abstract

Lakes and reservoirs are important emitters of climate forcing trace gases. Various environmental drivers of the flux, such as temperature and wind speed, have been identified, but their relative importance remains poorly understood. Here, for improved modelling, we use an extensive field dataset to disentangle physical and biogeochemical controls on the turbulence-driven, diffusion-limited flux of methane (CH$_4$) on daily to multi-year timescales. We compare 8 years of floating chamber fluxes measurements from three small, shallow subarctic lakes (2010–2017, n = 1306) with fluxes computed using to separate the contribution of physical and biogeochemical processes to the turbulence-driven, diffusion-limited flux of methane (CH$_4$) on daily to multi-year timescales. Correlative data include 9 years of surface water concentration measurements (2009–2017, n = 606) and a small eddy surface renewal model informed by in situ meteorological observations. We used the latter to compute near surface turbulence based on similarity scaling and then applied the surface renewal model to compute gas transfer velocities. Chamber fluxes averaged 6.9 ± 0.3 mg m$^{-2}$ d$^{-1}$ and gas transfer velocities ($k_{600}$) from the chamber-calibrated surface renewal model averaged 4.0 ± 0.1 cm h$^{-1}$. We find robust ($R^2 \geq 0.93, p < 0.01$) Arrhenius-type temperature functions of the CH$_4$ flux ($E_a' = 0.90 \pm 0.14$ eV) and of the surface CH$_4$ concentration ($E_w' = 0.88 \pm 0.09$ eV). Chamber derived gas transfer velocities tracked the power-law wind speed relation of the model ($k \propto u^{3/4}$). While the flux increased with wind speed, during storm events ($U_{10} \geq 6.5$ m s$^{-1}$) emissions were reduced by rapid water column degassing. Spectral analysis revealed that on timescales shorter than a month, emissions were driven by wind shear, but whereas on longer timescales variations in water temperature governed the flux, suggesting that chamber derived gas transfer velocities tracked the power-law wind speed relation of the model. Coefficients for the model and dissipation rates depended on shear production of turbulence, atmospheric stability, and exposure to wind. Fluxes increased with wind speed until they exceeded 6.5 m s$^{-1}$, at which point emissions were suppressed due to rapid water column degassing reducing the water–air concentration gradient. Arrhenius-type temperature functions of the CH$_4$ flux ($E_a' = 0.90 \pm 0.14$ eV) were robust ($R^2 \geq 0.93, p < 0.01$) and also applied to the surface CH$_4$ concentration ($E_w' = 0.88 \pm 0.09$ eV). These results indicate that emissions were strongly coupled to production, and supply to the water column. Our findings suggest that accurate short- and long-term projections of lake CH$_4$ emissions can be based on distinct weather- and climate controlled drivers of the flux.
1. Introduction

Inland waters are an important source of the radiatively active trace gas methane (CH$_4$) to the atmosphere (Bastviken et al., 2011; Cole et al., 2007). A significant portion of sediment-produced CH$_4$ reaches the atmosphere by turbulence-driven diffusion-limited gas exchange (Bastviken et al., 2004; Wik et al., 2016b) (hereafter abbreviated to ‘diffusive fluxes’). Traditionally, diffusive fluxes are measured with floating chambers (Bastviken et al., 2004) but gas exchange models are increasingly used, for example to estimate annual emissions on regional scales (Holgerson and Raymond, 2016; Weyhenmeyer et al., 2015). Fluxes computed with modelled gas transfer velocities agree to a certain extent with floating chambers and the eddy covariance technique in short-term intercomparison campaigns (Bartosiewicz et al., 2015; Crill et al., 1988; Erkkilä et al., 2018). However, long-term comparisons are needed to test the validity of flux-driver relations on which models are based across a wider range of meteorological conditions, and to identify weather- and climate-related controls on the flux that are appropriate for seasonal assessments. Considering the increased use of process-based approaches in regional emission estimates (DelSontro et al., 2018; Tan and Zhuang, 2015), understanding the mechanisms that drive the components of the diffusive flux is imperative for improving emission estimates.

1.1 Drivers of diffusive CH$_4$ emissions

Diffusive fluxes at the air-water interface can be modelled as:

\[ F = k(C_{aq} - C_{air,eq}) \]  

The flux $F$ [mg m$^{-2}$ d$^{-1}$] depends on the concentration difference across a thin layer immediately below the air-water interface ($\Delta[\text{CH}_4]$ in mg m$^{-3}$), which upper boundary is in equilibrium with the atmosphere ($C_{air,eq}$) and base represents the bulk liquid ($C_{aq}$), and is limited by the gas transfer velocity $k$ [m d$^{-1}$] (Wanninkhof, 1992). $k$ has been conceptualized as characterizing transfer across the diffusive boundary layer, although other models envision a surface renewal approach in which parcels of water intermittently are in contact with the atmosphere and $k$ depends on the frequency of these renewal events (Csanady, 2001; Lamont and Scott, 1970).
The gas transfer coefficient depends on turbulence caused by wind shear and convection and on the molecular diffusivity of the dissolved gas (see McIntyre et al., 1995 for an overview of the thermodynamic and kinetic drivers of $k$). In a stratified water column, the force of buoyancy counteracts that of wind shear, and gases may accumulate below a shallow upper mixing layer (McIntyre et al., 2010). Conversely, thermal convection as a result of surface cooling can deepen the mixed layer and transfer stored gas to the surface (Crill et al., 1988; Eugster et al., 2003), and enhance emissions at night when the surface cools despite low wind speeds (Heiskanen et al., 2014; Podgrajsek et al., 2014b; Poindexter et al., 2016). While progress has been made in understanding how the components of $k$ vary as a function of turbulence (Tedford et al., 2014) and other factors, such as lake morphology and distance to the shoreline (Read et al., 2012; Schilder et al., 2013; Vachon and Prairie, 2013), the temporal variability and drivers of $\Delta[CH_4]$ remain poorly resolved (Loken et al., 2019; Natchimuthu et al., 2016).

$CH_4$ emissions to the atmosphere also depend on the rates of methane metabolism regulated by substrate availability and temperature-dependent shifts in enzyme activity and microbial community structure (Borrel et al., 2011; McCalley et al., 2014; Tweit et al., 2015). Arrhenius-type relationships of $CH_4$ fluxes have emerged from field studies (DelSontro et al., 2018; Natchimuthu et al., 2016; Wik et al., 2014) and across latitudes and aquatic ecosystem types in synthesis reports (Rasilio et al., 2015; Yvon-Durocher et al., 2014). However, the temperature sensitivity is modulated by biogeochemical factors that differ between lake ecosystems, such as nutrient content (Davidson et al., 2018; Sepulveda-Jauregui et al., 2015), methanotrophic activity (Duc et al., 2010; Lofton et al., 2014), predominant emission pathway (DelSontro et al., 2016; Jansen et al., 2019) and warming history (Yvon-Durocher et al., 2017). In lakes, the air-water concentration difference driving the flux (Eq. 1) is further impacted by abiotic factors that dissociate production from emission rates, such as hydrologic inputs of terrestrially produced $CH_4$ (Miettinen et al., 2015; Murase et al., 2003; Paytan et al., 2015), redistribution of dissolved gas in the water column (DelSontro et al., 2017; Hofmann, 2013) and storage-and-release cycles associated with transient stratification (Czikowsky et al., 2018; Jammet et al., 2017; Vachon et al., 2019). From these interacting functional dependencies emerge complex responses of the flux to biotic and abiotic factors.

Disentangling the physical and biogeochemical drivers of the diffusive $CH_4$ flux remains a challenge. They respond differently to slow and fast changes in meteorological covariates (Baldocchi et al., 2001; Koebseh et al., 2015) such that different mechanisms may explain the diel and seasonal variability of the flux. For example, temperature affects emissions through convective mixing on short timescales and through the rate of sediment methanogenesis on longer timescales; the diurnal cycle of insolation may have a limited effect on production because the heat capacity of the water buffers the temperature signal (Fang and Stefan, 1996). Similar phase lags and amplifications may lead to hysteretic flux patterns, such as cold season emission peaks due to hypolimnetic storage in dimictic lakes (Encinas Fernández et al., 2014; López-Bellido et al., 2009) or thermal inertia of lake sediments (Zimov et al., 1997). Spectral analysis of the flux and its components can improve our understanding of the flux variability by quantifying how much power is associated with key periodicities (Baldocchi et al., 2001).

The flux $F$ [mg m$^{-2}$ d$^{-1}$] depends on the concentration difference across a thin layer immediately below the air-water interface ($\Delta[CH_4]$ in mg m$^{-3}$), of which the upper boundary is in equilibrium with the
atmosphere \( (C_{air, eq}) \) and the base represents the bulk liquid \( (C_{aq}) \), and is limited by the gas transfer velocity \( k \) \( [m \cdot d^{-1}] \). \( k \) has been conceptualized as characterizing transfer across the diffusive boundary layer. Other models envision exchange as driven by parcels of water intermittently in contact with the atmosphere. In these surface renewal models, \( k \) depends on the frequency of the renewal events (Csánydy, 2001; Lamont and Scott, 1970). The resulting calculation for \( k \) is based on the Kolmogorov velocity scale, \( u_{\eta} = (\varepsilon \nu)^{1/4} \) where \( \varepsilon \) is dissipation rate of turbulent kinetic energy (TKE) and \( \nu \) is kinematic viscosity (Tennekes and Lumley, 1972). Progress has been made in understanding how to compute \( \varepsilon \) and gas transfer rates as a function of wind speed and the heating and cooling at the lake’s surface (Tedford et al., 2014). Comparisons between models and other flux estimation methods, such as eddy covariance, illustrate the improved accuracy when computing gas transfer velocities using a turbulence-based approach opposed to wind based models (Czikowsky et al., 2018; Heiskanen et al., 2014; Mammarella et al., 2015).

A key control on emissions is the periodicity at which dissolved gases are brought to the air-water interface. During stratification, the density gradient makes it difficult for wind driven mixing to bring gases to the surface, and they may accumulate in the stratified regions. Conversely, thermal convection associated with surface cooling can deepen the mixed layer and transfer stored gas to the surface (Crill et al. 1988; Eugster et al. 2003). Nighttime emissions can be enhanced when the surface cools despite low wind speeds (Podgrajsek et al., 2015; Poindexter et al., 2016). Temporal patterns of stratification and mixing contribute to variability in diffusive \( \text{CH}_4 \) fluxes (López Bellido et al., 2009; Podgrajsek et al., 2016) and concentrations (Loken et al., 2019; Nachimuthu et al., 2016). Periodic emissions from storage at depth have been particularly difficult to resolve in lake emission budgets (Bastviken et al., 2004; Wik et al., 2016b).

\( \text{CH}_4 \) emissions to the atmosphere also depend on the rates of methane metabolism regulated by substrate availability and temperature-dependent shifts in enzyme activity and microbial community structure (Borrel et al., 2011; McCalley et al., 2014; Tveit et al., 2015). Arrhenius-type relationships of \( \text{CH}_4 \) fluxes have emerged from field studies (DelSontro et al., 2018; Nachimuthu et al., 2016; Wik et al., 2014) and across latitudes and aquatic ecosystem types in synthesis reports (Rasilo et al., 2015; Yvon-Durocher et al., 2014). However, the temperature sensitivity is modulated by biogeochemical factors that differ between lake ecosystems, such as nutrient content (Davidson et al., 2018; Sepulveda-Jauregui et al., 2015), methanotrophic activity (Duc et al., 2010; Lofton et al., 2014), predominant emission pathway (DelSontro et al., 2016; Jansen et al., 2019) and warming history (Yvon-Durocher et al., 2017). In lakes, the air-water concentration difference driving the flux (Eq. 1) is further affected by factors that dissociate production from emission rates. These include biotic factors, such as aerobic and anaerobic methanotrophy, and abiotic factors such as hydrologic inputs of terrestrially produced \( \text{CH}_4 \) (Miettinen et al., 2015; Paytan et al., 2015) and storage-and-release cycles associated with transient stratification (Czikowsky et al., 2018; Jammet et al., 2017; Vachon et al., 2019). Given these interacting functional dependencies, the magnitude of fluxes has complex patterns of temporal variability.

Disentangling the physical and biogeochemical drivers of the diffusive \( \text{CH}_4 \) flux remains a challenge. The component drivers respond differently to slow and fast changes in meteorological covariates (Baldocchi et al., 2001; Koebsch et al., 2015) such that different mechanisms may explain the diel and seasonal...
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Here we present a high-resolution, long-term dataset (2010–2017) of turbulence-driven diffusion-limited diffusion CH₄ fluxes from three subarctic lakes estimated with floating chambers \( n = 1306 \), and a gas exchange model informed fluxes obtained by modelling using in situ meteorological observations and surface water concentrations \( n = 535 \). We use a surface renewal model and is used to compute gas transfer velocities. Arrhenius relationships of \( \Delta[CH₄] \) to disentangle the and fluxes of CH₄ are also calculated. Using spectral analysis of our time series data, we distinguish the temporal dependency of abiotic and biotic controls on the flux. The effects of temperature on the flux. We then use stochastic tools to estimate the importance of these and other flux controls on lake size and wind exposure are illustrated by comparing results from the 3 different timescales lakes.
2. Materials and Methods

2.1 Field site

We monitored CH$_4$ emissions from three subarctic lakes of post-glacial origin (Kokfelt et al., 2010), located on the Stordalen Mire in northern Sweden (68°21′ N, 19°02′ E, Fig. 1), a peatland underlain by discontinuous permafrost (Malmer et al., 2005). The mire (350 m a.s.l.) is part of a catchment that connects Mt. Vuoskoäiveh (920 m a.s.l.) in the south to Lake Torneträsk (341 m a.s.l.) in the north (Lundin et al., 2016; Olefeldt and Roulet, 2012). Villasjön is the largest and shallowest of the lakes (0.17 km$^2$, 1.3 m max. depth) and drains through water-logged fens into a stream feeding Mellersta Harrsjön and Inre Harrsjön, which are 0.011 and 0.022 km$^2$ in size and have maximum depths of 6.7 m and 5.2 m, respectively (Wik et al., 2011). The lakes are normally ice-free from the beginning of May through the end of October. Manual observations were generally conducted between mid-June and the end of September. Diffusion accounts for 17%, 52% and 34% of the ice-free CH$_4$ flux in Villasjön, Inre and Mellersta Harrsjön, respectively, with the remainder being emitted via ebullition (2010–2017; Jansen et al., 2019).

![Figure 1 — Map of the Stordalen Mire field site (left). Chamber and sampling locations are shown as they were in 2015–2017. A schematic of the floating chamber pairs is shown to the right. Lake bathymetry from Wik et al. (2011). Satellite imagery: Google, DigitalGlobe, 2017.](image)
$\text{CH}_4$ emissions were measured from three subarctic lakes of post-glacial origin (Kokfelt et al., 2010), located around the Stordalen Mire in northern Sweden ($68^\circ 21'\text{N, 19}^\circ 02'\text{E}$, Fig. 1), a palsa mire complex underlain by discontinuous permafrost (Malmer et al., 2005). The Mire (350 m a.s.l.) is part of a catchment that connects Mt. Vuoskoäiveh (920 m a.s.l.) in the south to Lake Torneträsk (341 m a.s.l.) in the north (Lundin et al., 2016; Olefeldt and Roulet, 2012). Villasjön is the largest and shallowest of the lakes (0.17 km², 1.3 m max. depth) and drains through fens into a stream feeding Mellersta Harrsjön and Inre Harrsjön, which are 0.011 and 0.022 km² in size and have maximum depths of 6.7 m and 5.2 m, respectively (Wik et al., 2011). The lakes are normally ice-free from the beginning of May through the end of October. Manual observations were generally conducted between mid-June and the end of September. Diffusion accounts for 17%, 52% and 34% of the ice-free $\text{CH}_4$ flux in Villasjön, Inre and Mellersta Harrsjön, respectively, with the remainder emitted via ebullition (2010–2017; Jansen et al., 2019).

**Figure 1** – Map of the Stordalen Mire field site (left). Chamber and sampling locations are shown as they were in 2015–2017. A schematic of the floating chamber pairs is shown to the right. Lake bathymetry from Wik et al. (2011). Satellite imagery: Google, DigitalGlobe, 2017.
2.2 Floating chambers

We used floating chambers to directly measure the turbulence-driven diffusive CH$_4$ flux across the air-water interface (Fig. 1). They consisted of plastic tubs covered with aluminium tape to reflect incoming radiation and were equipped with polyurethane floats and flexible sampling tubes capped at one end with 3-way stopcocks (Bastviken et al., 2004). Depending on flotation depth, each chamber covered an area between 610 and 660 cm$^2$ and contained a headspace of 4 to 5 litres. Chambers were deployed in pairs with a plastic shield mounted underneath 30 cm below one chamber of each pair to deflect methane bubbles rising from the sediment. Every 1–2 weeks during the ice-free seasons of 2010 to 2017, 2–4 chamber pairs were deployed in Villasjön and 4–7 chamber pairs in Inre and Mellersta Harrsjön in different depth zones (Fig. 1). The number of chambers and deployment intervals exceeded the minimum needed to resolve the spatiotemporal variability of the flux (Wik et al., 2016a). Over a 24 hour period, 2–4 60 mL headspace samples were collected from each chamber using polypropylene syringes and the flotation depth and air temperature were noted in order to calculate the headspace volume. The 24-hour deployment period was chosen to compute fluxes over timescales which integrate diel variations in the gas transfer velocity (Bastviken et al., 2004).

The fluxes reported here are from the shielded chambers only. To check that the shields were not reducing fluxes from turbulent processes such as convection, we compared fluxes from shielded and unshielded chambers on days when the lake mean bubble flux was <1% of the lake mean diffusive flux (bubble traps, 2009–2017; Jansen et al., 2019; Wik et al., 2013). Averaged over the three lakes, the difference was statistically significant ($F_{ch,unsh} - F_{ch,sh} = 0.20 \pm 0.16$ mg m$^{-2}$ d$^{-1}$ (n = 58) (mean ± 95% CI)) but only a 6% difference from mean fluxes. Conversely, some types of floating chambers can enhance gas transfer by creating artificial turbulence when dragging through the water (Matthews et al., 2003; Vachon et al., 2010; Wang et al., 2015). The effect appears to be negligible for chambers of the design, size and flotation depth used in this study (acoustic Doppler velocimeter measurements, Ribas-Ribas et al., 2018).

2.3 Water samples
Surface water samples were collected at a depth of 0.2–0.4 m below the surface at 2–3 different locations in each lake (Fig. 1), at one to two-week intervals from June to October (Fig. 1). Samples were collected from shore with a 4 m Tygon tube attached to a floater to avoid disturbing the sediments (2009–2014), and from a rowing boat over the deepest points of Inre and Mellersta Harrsjön (2010–2017) and at shallows (<1 m water depth) on either end of the lakes (2015–2017) using a 1.2 m L x 3.2 mm ID Tygon tube. In addition, water samples were collected at the deepest point of Inre and Mellersta Harrsjön at 1 m intervals down to 0.1 m from the sediment surface with a 7.5 m L x 6.4 mm ID fluorinated ethylene propylene (FEP) tube. Subsequently, 60 mL polypropylene syringes were rinsed thrice with sample water before duplicate bubble-free samples were collected, and were capped with airtight 3-way stopcocks. 30 mL samples were equilibrated with 30 mL headspace and shaken vigorously by hand for 2 minutes (2009–2014) or on a mechanical shaker at 300 rpm for 10 minutes (2015–2017). Prior to 2015, lab outside air – with a predetermined measured CH4 content – was used as headspace. From 2015 on we used an N2 5.0 headspace (Air Liquide). Water sample conductivity was measured over the ice-free season of 2017 (n = 323) (S230, Mettler-Toledo), and converted to specific conductance using a temperature-based approach.
2.4 Concentration measurements
Gas samples were analysed within 24 hours after collection at the Abisko Scientific Research Station, 10 km from the Stordalen Mire. Sample CH$_4$ contents were measured on a Shimadzu GC-2014 gas chromatograph which was equipped with a flame ionization detector (GC-FID) and a 2.0 m long, 3 mm ID stainless steel column packed with 80/100 mesh HayeSep Q and used N$_2$ >5.0 as a carrier gas (Air Liquide). For calibration we used standards of 2.059 ppm CH$_4$ in N$_2$ (Air Liquide). 10 standard measurements were made before and after each run. After removing the highest and lowest values, relative standard deviations of the standard runs were generally less than 0.25%.

2.5 Water temperature and pressure loggers, density and mixed layer depth
Water temperature was measured every 15 minutes from 2009 to 2018 with temperature loggers (HOBO Water Temp Pro v2, Onset Computer) in Villasjön and at the deepest locations within Inre and Mellersta Harrsjön. Sensors monitored the surface water in all lakes were deployed at 0.1, 0.3, 0.5, 1.0 m depth, and further in all lakes, with additional sensors at 3.0, 5.0 m (IH and MH) and at 6.7 m (MH at the deep points.). Sensors were intercalibrated prior to deployment in a well-mixed water tank, and by comparing readouts just before and during ice-on when the water column was isothermal. In this way a precision of <0.05 °C was achieved. The bottom sensors were buried in the surface sediment and were excluded from in situ intercalibration. Water pressure was measured in Mellersta Harrsjön (5.5 m) with a HOBO U20 Water Level logger (Onset Computer). Water density was computed from temperature and salinity (Chen and Millero, 1977), using lake-averaged specific conductivity and a salinity factor [mS cm$^{-1}$/ g kg$^{-1}$] of 0.57. The salinity factor was based on a linear regression of simultaneous measurements of conductivity and dissolved solids ($R^2 = 0.99$, n = 7) in five lakes in the Torneträsk catchment (Miljödata-MVM, 2017). We defined the depth of the surface mixing layer ($z_{mix}$) at a density gradient threshold ($d\rho/dz$) of 0.03 kg m$^{-3}$ m$^{-1}$ (Rueda et al., 2007).

2.6 Meteorology
Meteorological data was collected from four different masts on the Mire (Fig. 1), and collectively covered a period from June 2009 to October 2017 with half-hourly measurements of wind speed, air temperature, relative humidity, air pressure and irradiance (Fig. 1, Table 1). Wind speed was measured with 3D sonic anemometers at the Palsa tower ($z = 2.0$ m), the Villasjön shore tower ($z = 2.9$ m), at the InterAct Lake tower ($z = 2.0$ m) and at the Integrated Carbon Observation System (ICOS) site ($z = 4.0$ m). Air temperature and relative humidity were measured at the Palsa tower, at the Villasjön shore tower (Rotronic MP100a (2012–2015) / Vaisala HMP155 (2015–2017)) and at the InterAct lake tower. Incoming and outgoing shortwave and long wave radiation were monitored with net radiometers at the Palsa tower (Kipp & Zonen CNR1) and at the InterAct lake tower (Kipp & Zonen CNR4). Precipitation data was collected with a WeatherHawk 500 at the ICOS site. Overlapping measurements were cross-validated and averaged to form a single timeseries.
In order to calculate the chamber flux with Eq. 1 we estimated \( k_{ch} \) from the time-dependent equilibrium chamber headspace concentration \( C_{h,eq}(t) \) \( \text{[mg m}^{-2}\text{]} \) (Bastviken et al., 2004):

\[
\frac{C_{aq} - C_{h,eq}(t)}{C_{aq} - C_{h,eq}(t_0)} = e^{\frac{-K_{HRT}A_{ch}ch}{V}}(C_{aq} - C_{h,eq}(t))
\]

where \( K_H \) is Henry’s law constant for CH\(_4\) \( \text{[mg m}^{-3}\text{ Pa}^{-1]} \) (Wiesenburg and Guinasso, 1979) (Wiesenburg and Guinasso, 1979), \( R \) is the universal gas constant \( \text{[m}^3\text{ Pa mg}^{-1}\text{ K}^{-1}\text{]} \), \( T_{water} \) is the surface water temperature \( \text{[K]} \) and \( V \) and \( A \) are the chamber volume \( \text{[m}^3\text{]} \) and area \( \text{[m}^2\text{]} \), respectively. This method accounts for gas accumulation in the chamber headspace, which reduces the concentration gradient and limits the flux (Eq. 1) (Fig. 2). For a subset of chamber measurements where simultaneous water concentration measurements were unavailable \( (n = 949) \) we computed the flux from the headspace concentrations alone:
\[ F = c_1 M \frac{\partial x_h}{\partial t} \frac{PV}{RT_a} \frac{\partial x_h}{\partial t} \frac{RT}{RT_{air} A} \]

where \( \frac{\partial x_h}{\partial t} \) is the headspace \( \text{CH}_4 \) mole fraction change \([10^{-6} \text{ ppm mol}^{-1} \text{ d}^{-1}]\) computed with ordinary least squares (OLS) linear regression (Fig. 2). \( M \) is the molar mass of \( \text{CH}_4 \) (0.016 mg mol\(^{-1}\)), \( P \) is the air pressure [Pa], \( RT_{air} \) is the air temperature [K]. Scalar \( c_1 \) corrects for the accumulation of \( \text{CH}_4 \) gas in the chamber headspace and increases over the deployment time. Comparing both chamber flux calculation methods we find \( c_1 = 1.21 \) for 24 hour deployments (OLS, \( R^2 = 0.85, n = 357 \)). Chambers were sampled up to 4 times during their 24 hour deployment (at 10 minutes, 1–5 hours and 24 hours) which allowed us to compute fluxes at different-time intervals of 1 hour and 24 hours. \( P \) and \( T_{air} \) were averaged over the relevant time interval.

Figure 2 illustrates the importance of shows that the headspace correction is necessary to avoid underestimating fluxes. The headspace-corrected flux (dashed red line) equals the initial slope of Eq. 2 (solid red line) and is about 21% higher than the non-corrected flux (lower dashed black line in Fig. 2).

However, both Eq. 2 (solid red line) and Eq. 3 with \( c_1 = 1 \) (dashed black lines) fit the concentration data \( R^2 \geq 0.98 \) for 94% of 24-hour flux measurements. This similarity results partly because the fluxes were low enough to keep headspace concentrations well below equilibrium with the water column, and because on average, the gas transfer velocity deviated \( \leq 10\% \) from its mean value over its diel cycle (Fig. 7d). Short-term measurements (upper dashed black line) may omit the need for headspace correction but can significantly overestimate the flux if as in our study initial (Bastviken et al., 2004), Because concentration measurements were not available for all chamber observations, we used multi-year mean values of \( \Delta \text{[CH}_4]\) and \( k_{ch} \) to compute \( c_1 \) as a function of chamber deployment takes place during daytime and \( k \) or \( \Delta \text{[CH}_4]\) follow a diurnal pattern (Bastviken et al., 2004). Time. For 24 hour chamber deployments, \( c_1 = 1.21 \).
Figure 2 – Example of chamber headspace CH$_4$ concentrations versus deployment time. Measured concentrations (dots) are averages from 2015–2017 (0.1h) and 2011 (1h–24h); error bars represent the 95% confidence intervals. Linear regressions (dashed black lines) show the rate increase over 1 hour (two measurements) and over 24 hours (five measurements). The solid red line represents chamber concentrations computed with Eq. 2 using multi-year mean values of Δ[CH$_4$] and $k_{ch}$ (uncorrected for headspace accumulation). The rate increase associated with the mean 24h flux corrected for headspace accumulation is shown as a dashed red line (Eq. 1 with $k_{ch}$ from Eq. 2, or Eq. 3 with $c_1 = 1.21$).

Labels denote fluxes calculated from the linear regression slopes (Eq. 3, black) and from Eq. 2 (red).
2.9 Computing gas transfer velocities with the surface renewal model

We used the surface renewal model (Lamont and Scott, 1970) formulated for small eddies at Reynolds numbers >500 (MacIntyre et al., 1995; Theofanous et al., 1976) to estimate $k$:

$$k_{mod} = \alpha (\varepsilon \nu)^{1/4} S_c^{-1/2}$$  \[4\]

where the hydrodynamic and thermodynamic forces driving gas transfer are expressed, respectively, as the dissipation of turbulent kinetic energy ($TKE$, $\varepsilon \ [m^2 s^{-3}]$), and the dimensionless Schmidt number $S_c$, defined as the ratio of the kinematic viscosity $\nu \ [m^2 s^{-1}]$ to the free solution diffusion coefficient $D_0 \ [m^2 s^{-1}]$ (Jähne et al., 1987; Wanninkhof, 2014). The scaling parameter $\alpha$ has a theoretical value of 0.37 (Katul et al., 2018), but is often estimated empirically ($\alpha'$) to calibrate the model (e.g. Wang et al., 2015). To allow for a qualitative comparison between model and chamber fluxes we regressed $k_{ch}$ (floating chambers) onto $(\varepsilon \nu)^{1/4} S_c^{-1/2}$ (surface renewal model, half-hourly values of $k_{mod}$ averaged over each chamber deployment period), and determined $\alpha' = 0.23 \pm 0.02$ (mean ± 95% CI, $n = 334$) (Fig. 3). When comparing $k$-values we normalized to a Schmidt number of 600 (CO$_2$ at 20 °C) (Wanninkhof, 1992):

$$k_{600} = (600/S_c)^{-0.5} k.$$  

To enable comparison with published wind-$k$ relations we calculated the wind speed at 10 m ($U_{10}$) from the anemometer datasets following Smith (1988), assuming a neutral atmosphere.

where the hydrodynamic and thermodynamic forces driving gas transfer are expressed, respectively, as the TKE dissipation rate $\varepsilon \ [m^2 s^{-3}]$, and the dimensionless Schmidt number $S_c$, defined as the ratio of the kinematic viscosity $\nu \ [m^2 s^{-1}]$ to the free solution diffusion coefficient $D_0 \ [m^2 s^{-1}]$ (Jähne et al., 1987; Wanninkhof, 2014). The scaling parameter $\alpha$ has a theoretical value of 0.37 (Katul et al., 2018), but is often estimated empirically ($\alpha'$) to calibrate the model (e.g. Wang et al., 2015). To allow for a qualitative comparison between model and chamber fluxes, we took ratios of $k_{ch}$ (floating chambers) and $(\varepsilon \nu)^{1/4} S_c^{-1/2}$ (surface renewal model, half-hourly values of $k_{mod}$ averaged over each chamber deployment period), and determined $\alpha' = 0.31 \pm 0.06$ ($n = 67$) for Villasjön, $\alpha' = 0.17 \pm 0.02$ ($n = 131$) for Mellersta Harrsjön, and $\alpha' = 0.25 \pm 0.03$ ($n = 136$) for Inre Harrsjön (Supplementary Fig. 1). Calibrating the model in this way allowed us to assess whether chamber flux relationships with wind speed and temperature were reproduced by the model. For similar comparative purposes, $k$-values were normalized to a Schmidt number of 600 (CO$_2$ at 20 °C) (Wanninkhof, 1992):

$$k_{600} = (600/S_c)^{-0.5} k.$$  

The wind speed at 10 m ($U_{10}$) was computed from measured wind speed following Smith (1988), assuming a neutral atmosphere.
Figure 3 – Determination of the model scaling parameter $\alpha'$ via comparison between gas transfer velocities from floating chambers (Eq. 2) and the surface renewal model (Eq. 4 with $\alpha' = 1$ and $Sc = 600$, half-hourly values averaged over each chamber’s 24 hour deployment period). Grey dots are for all three lakes. Dots represent individual chamber deployments (grey) and black dots represent multi-chamber means for each weekly deployment in 2016 and 2017, when concentration measurements were taken simultaneously with, and in close proximity to the chamber measurements. Intercepts (black). Mean ratios, and therefore $\alpha'$, are represented by the slopes of the linear regressions (dotted lines) were fixed at 0. Error bars represent 95% confidence intervals of the means.

We used a parametrization by Tedford et al. (2014) based on Monin-Obukhov similarity theory to estimate the TKE dissipation rate at half-hourly time intervals:

$$\varepsilon = \begin{cases} 0.56 \frac{u_{aw}^3}{\kappa z} + 0.77 \beta \text{ if } \beta > 0 \\ 0.6 \frac{u_{aw}^3}{\kappa z} \text{ if } \beta \leq 0 \end{cases}$$

where $u_{aw}$ is the water friction velocity [m s$^{-1}$], $\kappa$ is the von Kármán constant, $z$ is the depth below the water surface (here set to 0.15 m, the depth for which Eq. 5 was calibrated). We determined $u_{aw}$ from the air friction velocity $u_{aw}$ assuming equal shear stresses ($\tau$) on either side of the air-water interface;

$$\tau = \rho_a u_{aw}^2 = \rho_w u_{aw}^2$$

(MacIntyre and Melack, 1995), and taking into account atmospheric stability (Imberger, 1985; MacIntyre et al., 2014; Tedford et al., 2014). $\beta$ is the buoyancy flux [m$^2$ s$^{-3}$], which accounts for turbulence generated by convective mixing (Imberger, 1985):

where $u_w$ is the water friction velocity [m s$^{-1}$], $\kappa$ is the von Kármán constant, $z$ is depth below the water surface (0.15 m, the depth for which Eq. 5 was calibrated). We determined $u_w$ from the air friction velocity $u_{aw}$ assuming equal shear stresses ($\tau$) on both sides of the air-water interface; $\tau = \rho_a u_{aw}^2 = \rho_w u_{aw}^2$, and taking into account atmospheric stability (MacIntyre et al., 2014; Tedford et al., 2014). $\beta$ is the buoyancy flux [m$^2$ s$^{-3}$], which accounts for turbulence generated by convection (Imberger, 1985):
\[
\beta - \frac{\alpha_T Q_{eff}}{c_{pw} \rho_w} = \alpha_T g Q_{eff} / c_{pw} \rho_w
\]

where \( \alpha_T \) is the thermal expansion coefficient [m³·K⁻¹] (Kell., 1975), \( g \) is the standard gravity [m·s⁻²], \( c_{pw} \) is the water specific heat [J·kg⁻¹·K⁻¹] and \( \rho_w \) is the water density, calculated from the water temperature and corrected for dissolved solids using conductivity measurements and a conversion factor of 0.57 g·kg⁻¹·m⁻²·cm⁻¹. \( Q_{eff} \) [W·m⁻²] represents the net heat flux into the surface mixed layer and is the sum of net shortwave and long-wave radiation and sensible and latent heat fluxes. We used Beer’s Law to compute penetration of radiation into the water column across seven wavelength bands (Jellison and Melack, 1993). Attenuation of the visible portion of the spectrum was computed from the Secchi depth (Karlsson et al., 2010; Wik et al., 2018) with the inverse relationship from Idso and Gilbert (1974). We further computed outgoing component of the net longwave radiation \( (LW_{out}) \) using the Stefan-Boltzmann law: \( LW_{out} = \sigma T^4 \), where \( \sigma \) is the Stefan-Boltzmann constant \( (5.67 \times 10^{-8} \text{ W·m}^{-2}·\text{K}^{-4}) \) and \( T \) is the surface water temperature in K. For periods where we did not have longwave radiation data we assumed \( LW_{out} = -50 \text{ W·m}^{-2} \). Sensible and latent heat fluxes were computed with bulk aerodynamic formula described in MacIntyre et al. (2002). Both \( Q_{eff} \) and \( \beta \) are here defined as positive when the heat flux is directed out of the water, for example when the surface water cools.

Direct measurements of turbulent dissipation rates in a small Arctic lake (1 m depth, 0.005 km²) show that Equation 5 well characterizes near surface turbulence in small, sheltered water bodies similar to the lakes studied here (MacIntyre et al., 2018). Eq. 5 underestimates the dissipation-suppressing effects of stratification of the upper water column at buoyancy frequencies \( (\nu = \sqrt{g/\rho_w \times d \rho_w/\partial z}) \) exceeding 25 cycles per hour (MacIntyre et al., 2018). However, in the current dataset such periods of strong stratification (\( \nu > 25 \text{ cph} \)) were observed <3% of the time.

Here, \( \alpha_T \) is the thermal expansion coefficient [m³·K⁻¹] (Kell., 1975), \( g \) is the standard gravity [m·s⁻²], \( c_{pw} \) is the water specific heat [J·kg⁻¹·K⁻¹] and \( \rho_w \) is the water density. \( Q_{eff} \) [W·m⁻²] represents the net heat flux into the mixing layer and is the sum of net shortwave and long-wave radiation and sensible and latent heat fluxes. Penetration of radiation into the water column was evaluated across seven wavelength bands via Beer’s Law (Jellison and Melack, 1993). An attenuation coefficient of 0.74 was computed for the visible portion of the spectrum from Secchi depth (2.3 m: Karlsson et al., 2010) following Idso and Gilbert (1974). Net longwave radiation \( (LW_{net} = LW_{out} - LW_{in}) \) was computed via measurements of \( LW_{in} \) (Table 1) and \( LW_{out} = \sigma T^4 \), where \( \sigma \) is the Stefan-Boltzmann constant \( (5.67 \times 10^{-8} \text{ W·m}^{-2}·\text{K}^{-4}) \) and \( T \) is the surface water temperature in K. \( LW_{net} \) timeseries were gap-filled with ice-free mean values for each lake. Sensible and latent heat fluxes were computed with bulk aerodynamic formula (MacIntyre et al., 2002). Both \( Q_{eff} \) and \( \beta \) are here defined as positive when the heat flux is directed out of the water, for example when the surface water cools.

Direct measurements of \( \varepsilon \) in an Arctic pond (1 m depth, 0.005 km² surface area) demonstrate that Equation 5 can characterize near-surface turbulence in small, sheltered water bodies similar to the lakes studied here (MacIntyre et al., 2018). When the near surface was strongly stratified at instrument depth (buoyancy frequencies \( (\nu = \sqrt{g/\rho_w \times d \rho_w/\partial z}) > 25 \text{ cycles per hour (cph)} \)), the required assumption of
homogeneous isotropic turbulence was not met and Equation 5 could not be evaluated. We observed cases with $N > 25$ cph <3% of the time.

2.10 Calculation of binned means

We binned data to assess correlations between the flux and environmental covariates. Half-hourly values of water temperature and wind speed were averaged over the deployment period of each chamber (fluxes), and over 24 hours prior to the collection of each water sample (concentrations). The 24-hour averaging period was chosen based on, reflecting the mean residence time of a CH$_4$ molecule in the lake water column. Parameters of interest (fluxes, concentrations and $k$-values) were then binned in 10 day, 1 °C and 0.5 m s$^{-1}$ bins to obtain relationships with time, water temperature and wind speed, respectively. For this calculation, lake-specific variables such as water temperature were normalized by lake to obtain a single timeseries (divided by the lake mean, multiplied by the overall mean).
2.11 Calculation of the empirical activation energy

Chamber and modelled fluxes as well as surface concentrations were fitted to an Arrhenius-type temperature function (e.g. Wik et al., 2014; Yvon-Durocher et al., 2014):

\[
F = e^{-E_a'/k_B T + b}
\]

where \( k_B \) is the Boltzmann constant \((8.62 \times 10^{-5} \text{ eV K}^{-1})\) and \( T \) is the water temperature in K. The empirical activation energy \( (E_a', \text{ in electron volts (eV), 1 eV = 96 kJ mol}^{-1}) \) was computed with a linear regression of natural logarithm of the fluxes and concentrations onto the inverse temperature \((1/K)\), of which \( b \) is the intercept.

2.12 Timescale analysis: power spectra and climacogram

We computed power spectra for near-continuous timeseries of the surface sediment, water- and air temperature and the wind speed according to Welch’s method (pwelch in MATLAB 2018a), which splits the signal into overlapping sections and applies a cosine tapering window to each section (Hamming, 1989). Data gaps were filled by linear interpolation. We removed the linear trend from original timeseries to reduce red noise, and block-averaged spectra (8 segments with 50% overlap) to suppress aliasing at higher frequencies. We normalized the spectral densities by multiplying by the natural frequency and dividing by the variance of the original timeseries (Baldocchi et al., 2001).

We evaluated our discontinuous (fluxes, concentrations) and continuous (meteorology) timeseries with a climacogram, an intuitive way to visualize a continuum of variability (Dimitriadis and Koutsoyiannis, 2015). It displays the change of the standard deviation \( (\sigma) \) with averaging timescale \( (t_{avg}) \) in double-logarithmic space. Variables of interest were normalized by lake to create a single time-series at half-hourly resolution (i.e., 48 entries for each 24-hour chamber flux). To compute each standard deviation \( (\sigma(t_{avg})) \) data were binned according to averaging timescale, which ranged from 30 minutes to 1 year. Because of the discontinuous nature of the datasets, \( n \) bins were distributed randomly across the time series. We chose \( n = 100000 \) to ensure that the 95% confidence interval of the standard deviation at the smallest bin size was less than 1% of the value of \( \sigma \) (Sheskin, 2007). To allow for comparison between variables we normalized each \( \sigma \)-series by its initial, smallest-bin value: \( \sigma_{\text{norm}} = \sigma/\sigma_{\text{init}} \). For timescales < 1 week we used 1-hour chamber observations, noting that sparse, daytime-only observations of concentrations and 1-hour fluxes may underestimate short-term variability \( (\sigma_{\text{init}}) \). We use the climacogram specifically to test whether the variability of the diffusive CH\(_4\) flux is enveloped by hydrometeorological contained within meteorological variability, as for terrestrial ecosystem processes (Pappas et al., 2017).

2.13 Statistics

We used Analysis of Variance (ANOVA) and the t-test to compare means of different groups. The use of means, rather than medians was necessary because annual emissions can be determined by rare, high-
magnitude emission events. Parametric tests were justified because of the large number of samples in each analysis, in accordance with the central limit theorem. Linear regressions were performed with the ordinary least squares method (OLS): reported $p$-values refer to the significance of the regression slope. Non-linear regressions were optimized with the Levenberg-Marquardt algorithm for non-linear least squares with confidence intervals based on bootstrap replicates ($n = 1999$). Computations were done in MATLAB 2018a and in PAST v3.25 (Paleontological Statistics software package) (Hammer et al., 2001).
3. Results

3.1 Measurements and models

Chamber fluxes averaged 6.9 mg m\(^{-2}\) d\(^{-1}\) (range 0.2–32.2, \(n = 1306\)) and closely tracked the temporal evolution of the surface water concentrations (mean 11.9 mg m\(^{-3}\), range 0.3–120.8, \(n = 606\)), with the higher values in each lake measured in the warmest months (July and August, Fig 4a,e). As expected, diffusive fluxes increased with wind speed and water temperature (Fig 4b,c). Reduced emissions were measured in the shoulder months (June and September) and were associated with lower water temperatures. We also observed abrupt reductions of the flux at wind speeds lower than 2 m s\(^{-1}\) and higher than 6.5 m s\(^{-1}\). Surface water concentrations generally increased with temperature and peaked in the summer months, but unlike the chamber fluxes they decreased with increasing wind speed (Fig. 4f,g).

Relationships with wind speed were approximately linear, while relationships with temperature fitted an Arrhenius-type exponential function (Eq. 7). Activation energies were not significantly different between when using either surface water or sediment temperature (\(E_a' = 0.90 \pm 0.14\) eV, \(R^2 = 0.93, E_a' = 1.00 \pm 0.17, R^2 = 0.93\), respectively, mean±95% CI). The fluxes, concentrations, and the wind speed were non-normally distributed (Fig. 4d,h,o). Surface water temperatures (0.1–0.5 m) were normally distributed for around the mean of each individual month of the ice-free season (Fig. 4n), but the composite distribution was bimodal.

Fluxes computed with the surface renewal model (Eq. 1 using \(k_{mod}\)) closely resembled the chamber fluxes (Eq. 3) in terms of temporal evolution (Fig. 4a) and correlation with environmental drivers (Fig. 4b,c). Despite the model’s calibration with a subset of the chamber data, mean model fluxes were slightly higher than the chamber fluxes in all lakes Villasjön and Inre Harrsjön, and slightly lower in Mellersta Harrsjön (Table 2). Model fluxes were significantly different between littoral and pelagic zones in Inre and Mellersta Harrsjön (paired t-tests, \(p \leq 0.02\)), reflecting spatial differences in the surface water concentration (Table 2). Similar to the chamber fluxes, the air-water concentration difference (\(\Delta[CH_4]\)) explained most of the temporal variability of the modelled emissions; both \(k_{mod}\) (Eq. 4) and \(k_{ch}\) (Eq. 2) were functions of \(U_{10}\) (Fig. 4k) and did not display a distinctive seasonal pattern (Fig. 4i). Modelled fluxes were lower when surface concentrations decreased, and displayed a cut-off at daily mean \(U_{10} \geq 6.5\) m s\(^{-1}\), similar to the chamber fluxes, but not at \(U_{10} < 2.0\) m s\(^{-1}\). The temperature sensitivity of the modelled fluxes (\(E_a' = 0.97 \pm 0.12\) eV, mean ± 95% CI, \(R^2 = 0.94\)) did not differ significantly from that of the chamber fluxes.
Table 2 – CH₄ fluxes from floating chambers and the surface renewal model, and surface CH₄ concentrations. Data from 2014 was excluded from the model flux means because of a substantial bias in the timing of sample collection. Model fluxes for each lake were computed with distinct scaling parameter values (Supplementary Fig. 1).

<table>
<thead>
<tr>
<th>Location</th>
<th>Chamber flux (mg m⁻² d⁻¹) mean ± 95% CI</th>
<th>n</th>
<th>Modelled flux (mg m⁻² d⁻¹) mean ± 95% CI</th>
<th>n</th>
<th>Surface concentration (mg m⁻³) mean ± 95% CI</th>
<th>n</th>
</tr>
</thead>
<tbody>
<tr>
<td>Overall</td>
<td>6.9 ± 0.3</td>
<td>1306</td>
<td>7.6 ± 0.5</td>
<td>501</td>
<td>11.9 ± 0.9</td>
<td>606</td>
</tr>
<tr>
<td>Villasjön</td>
<td>5.2 ± 0.5</td>
<td>249</td>
<td>5.3 ± 7.0.7 ± 0.9</td>
<td>149</td>
<td>8.3 ± 1.1</td>
<td>183</td>
</tr>
<tr>
<td>Inre Harrsjön</td>
<td>6.6 ± 0.4</td>
<td>532</td>
<td>7.6 ± 0.67</td>
<td>176</td>
<td>10.2 ± 1.0</td>
<td>211</td>
</tr>
<tr>
<td>Shallow (&lt;2 m)</td>
<td>6.0 ± 0.6</td>
<td>219</td>
<td>7.6 ± 4.8</td>
<td>113</td>
<td>11.1 ± 1.3</td>
<td>133</td>
</tr>
<tr>
<td>Intermediate (2-4 m)</td>
<td>7.1 ± 0.6</td>
<td>212</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Deep (&gt;4 m)</td>
<td>6.6 ± 0.8</td>
<td>101</td>
<td>6.47.0 ± 0.9</td>
<td>63</td>
<td>8.6 ± 1.4</td>
<td>78</td>
</tr>
<tr>
<td>Mellersta Harrsjön</td>
<td>8.0 ± 0.4</td>
<td>525</td>
<td>10.47.7 ± 0.97</td>
<td>176</td>
<td>16.7 ± 2.0</td>
<td>212</td>
</tr>
<tr>
<td>Shallow (&lt;2 m)</td>
<td>8.1 ± 0.6</td>
<td>272</td>
<td>11.1 ± 8.3 ± 0.9</td>
<td>113</td>
<td>18.2 ± 2.7</td>
<td>134</td>
</tr>
<tr>
<td>Intermediate (2-4 m)</td>
<td>7.8 ± 0.7</td>
<td>154</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Deep (&gt;4 m)</td>
<td>8.0 ± 1.0</td>
<td>99</td>
<td>6.8 ± 0.9 ± 1.2</td>
<td>63</td>
<td>14.1 ± 2.7</td>
<td>78</td>
</tr>
</tbody>
</table>
Figure 4 – Scatterplots of the CH₄ flux (a-c), CH₄ air-water concentration difference (e-g) and gas transfer velocity (i-k) versus time, surface water temperature and wind speed, as well as the histograms of the aforementioned variables (d,h,l,m-o). In each scatter plot binned means of the flux (squares, a-c), concentrations (triangles, e-g) and gas transfer velocities (rhombuses, i-k) are represented by large symbols with error bars signifying 95% confidence intervals (error bars). Orange and light blue symbols reflect chamber-derived and model-derived binned values, respectively. Model $k$ was computed with $\alpha' = 0.23$. Bin sizes were 10 days, 1 °C and 0.5 m s⁻¹ for time, surface water temperature and $U_{10}$, respectively. Small green, blue and red dots represent individual measurements in Villasjön, Inre Harrsjön and Mellersta Harrsjön, respectively. Open rhombus symbols in panels i-k represent the buoyancy component of the gas transfer velocity, closed rhombus symbols include both the wind-driven and buoyancy-driven components. Dashed lines in panels b and f represent fitted Arrhenius functions (Eq. 7). Histograms of modelled (light blue) and measured (light orange) quantities (d,h,l) overlap. Histograms of the surface
water temperature (m) and $U_{10}$ (o) are stacked by month, from June (darkest shade) to October (lightest shade).
3.2 Meteorology and mixing regime

The water column of all three lakes was weakly stratified throughout the ice-free season, and the mean diel mixing depths ($d_\rho/dz < 0.03 \text{ kg m}^{-2} \text{m}^{-1}$ (Rueda et al., 2007)) exceeded the lake mean depths (Table 3). Figure 5 shows a timeseries of the mixing depth and water temperature in the deeper lakes, along with wind speed, air temperature and precipitation for the ice-free period of 2017. All lakes were polymictic and mixed to the bottom several times during summer (Fig. 5 f-h). Water temperatures in the surface mixed layer were lowest in Mellersta Harrsjön (9.4 ± 5.0 °C), where the mooring was placed next to the stream outlet (Fig. 1), and were higher in Inre Harrsjön (9.9 ± 5.5 °C) and Villasjön (10.2 ± 5.3 °C) (ice-free seasons of 2009–2017, mean ± SD). In early summer (June, July) deep mixing (Table 3) consisted of two phases. In the first, air and surface water temperatures were higher and the two deeper lakes stratified. Wind speeds increased to mean values approaching 5 m s$^{-1}$ for a few days at a time and then decreased for a day or two. Deep mixing events followed surface cooling and heavy rainfall. Water level maxima and surface temperature minima were observed 2-3 days after rainfall events, for example between 15 and 18 July 2017 (Fig. 5e). In the second phase, wind speeds were persistently higher ($U_0 > 5$ m s$^{-1}$), air and surface water temperatures declined and all lakes mixed to the bottom. Strong nocturnal cooling on 16 August 2017 broke up stratification and the lakes remained well-mixed until ice-on (20 October). Increased wind speeds in September and October may have further enhanced mixing. Overall, throughout the ice-free season from 2009–2018, stratified periods ($z_{\text{mix}} \leq 1$ m) lasted for 7 hours on average and were common (2931% and 4445% of the time in Inre and Mellersta Harrsjön, respectively). but were frequently disrupted by deeper mixing events. Shallow mixing ($z_{\text{mix}} < z_{\text{mean}}$) occurred on diel timescales. Deep mixing occurred at longer intervals (days-weeks), and more frequently toward the end of the ice-free season (Fig. 5g,h) in association with higher wind speeds.

Fluxes and near surface concentrations also varied within these periods, with concentrations and fluxes higher in the warmer, stratified period and lower in the colder, mixed periods. In 2017, the highest concentrations and fluxes occurred earlier in the season, with the initial high values in the two deeper lakes indicative of residual CH$_4$ that had not evaporated immediately after ice-off, around 1 June 2017 (Fig. 5c,d). As residual CH$_4$ was emitted, near surface concentrations declined, and then in the first half of the stratified period (July 2017, Fig. 5d), particularly in Mellersta Harrsjön, increased with increased rainfall and with temperature. During this period, $k_{ch}$ and $k_{mod}$ were similar. Decreases in $k_{ch}$ occurred when air temperatures increased above surface water temperatures in the day leading to a stable atmosphere and when near surface temperatures were warmer, and depending upon the lake, stratified to the surface. Thus, lower fluxes occurred during the second part of the stratified period (August 2017, Fig. 5c) when surface concentrations increased during warming periods when winds were light, the atmosphere was stable during the day, and the upper water column was strongly stratified. Fluxes and concentrations were lower in the autumn mixed periods, by which time the lakes had degassed, and with the colder surface sediment temperatures, rates of production had decreased.

The modelled gas transfer velocity generally followed the temporal pattern of the wind speed (Fig. 4b). Due to model calibration, the chamber-derived modelled gas transfer velocities (Fig. 4b, orange rhombuses) tracked those computed with the surface renewal model (orange rhombuses). Discrepancies pointed to a mismatch between 24-hour integrated chamber fluxes and surface concentrations measured at a single point in time. For example, measuring a low surface concentration in the de-gassed water column after a windy period during which
the surface flux was high led to an overestimated $k_{ch}$ on 21 September 2017. Contrastingly, $k_{ch}$ was lower than $k_{mod}$ on 3 August 2017 due to elevated surface concentrations and a low chamber flux associated with a warm and stratified period preceding water sampling.

The mixed layer water temperature of the surface mixed layer exceeded the air temperature by 1.6 °C on average (Fig. 5a). The bias was a function of temperatures over the lakes was often unstable, particularly at night, dropping below surface water temperatures, which contributed to negative buoyancy fluxes during warm periods as well as during the many cold fronts. We computed an unstable atmosphere over the lakes ($z/L_{MO,a} < 0$, where $z$ is the measurement height and $L_{MO,a}$ is the air-side Monin-Obukhov length; Foken 2006) ~76% of the time during ice-free seasons. Atmospheric instability increases sensible and latent heat fluxes (Brutsaert, 1982), enhancing the cooling rate. Thus, buoyancy fluxes were positive at night and during cold fronts throughout the ice-free season (Fig 5b, Fig. 4i-k). We computed elevated contributions of the buoyancy flux during cooling periods tended to the TKE budget during the night and in the warmest months range from $10^{-8}$ to $10^{-7}$ m$^2$ s$^{-3}$ in the stratified period and decreased as water temperatures cooled in autumn (Fig. 7), but the overall influence of convection on near-surface turbulence was high, with values often between $10^{-6}$ and $10^{-5}$ m$^2$ s$^{-3}$, although values did fall as low as $10^{-8}$ m$^2$ s$^{-3}$ when winds were light. Comparison of these two terms indicated that buoyancy flux during cooling was typically two orders of magnitude less than $\varepsilon$ and was only equal to it during the lightest winds (Fig. 4k). Consequently, its contribution to the gas transfer coefficient was minor. (Fig. 7). Averaged over all ice-free seasons (2009–2017) the buoyancy flux contributed only 8% to the TKE dissipation rate, but up to 90% during rare, very calm periods ($U_{10} \leq 0.5$ m s$^{-1}$, Fig. 4k) and up to 25% on during the warmest days periods ($T_{surf} \geq 18$ °C, Fig. 4j).
Figure 5 – Timeseries of air and surface mixed-layer water temperature (three-lake mean) (a), wind speed, gas transfer velocity from the surface renewal model ($k_{mod}$ and its buoyancy component, $k_{mod,b}$) and from chamber observations ($k_{ch}$) (three-lake mean values, error bars represent 95% confidence intervals) (b), chamber CH$_4$ flux (c), air-water CH$_4$ concentration difference (d), precipitation and changes in water level in Mellersta Harrsjön (e) and the water temperature in Villasjön (f), Inre Harrsjön (g) and Mellersta Harrsjön (h) during the ice-free season of 2017 (1 June to 20 October). The white lines in panels e and f-h represent the depth of the actively mixing surface mixed layer. Thin and thick curves in panels a and b...
represent half-hourly and daily means, respectively. In panel a only the half-hourly timeseries of $T_{\text{water}}$ was plotted.
Table 3 – Lake morphometry, mixing regime, temperature of the surface mixing layer, buoyancy frequency, and CH₄ residence time. Mean values were calculated over the ice-free seasons of 2009–2017.

<table>
<thead>
<tr>
<th>Lake</th>
<th>Area (ha)</th>
<th>Depth (m)</th>
<th>Mixed layer depth (m)</th>
<th>Mixing layer temp. (°C)</th>
<th>N (cycles h⁻¹)</th>
<th>CH₄ residence time (days)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>mean</td>
<td>max</td>
<td>mean ± SD</td>
<td>n</td>
<td>mean ± SD</td>
<td>n</td>
</tr>
<tr>
<td>Villasjön</td>
<td>17.0</td>
<td>0.7</td>
<td>1.3</td>
<td>0.7 ± 0.3</td>
<td>664391</td>
<td>5.7 ± 8.0</td>
</tr>
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<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td>48976</td>
<td></td>
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<tr>
<td>Inre Harrsjön</td>
<td>2.3</td>
<td>2.0</td>
<td>5.2</td>
<td>10.1 ± 5.2</td>
<td>583622</td>
<td>5.2 ± 6.9</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
<td>± 1.6</td>
<td>78752</td>
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</tr>
<tr>
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<td>6.7</td>
<td>3.9 ± 2.4</td>
<td>624722</td>
<td>5.3 ± 9.0</td>
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<tr>
<td></td>
<td></td>
<td></td>
<td></td>
<td>± 4.9</td>
<td>78014</td>
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</tbody>
</table>

3.3 CH₄ storage and residence times
Residence times of stored CH₄ varied between 12 hours and 7 days and were inversely correlated with wind speed in all three lakes (OLS: $R^2 ≥ 0.57$, Fig. 6). The mean residence time was shortest in the shallowest lake, and was not significantly different between the two deeper lakes (paired t-test, $p < 0.01$, Table 3). We did not find a statistically significant linear correlation between the residence time and day of year or the water temperature. CH₄ storage was greatest in the deeper lakes and displayed patterns similar to the surface concentrations, increasing in the warmest months with water temperature and decreasing with wind speed.
Figure 6 – Scatterplots of the CH$_4$ residence time (a-c) and storage (d-f) versus time, surface water temperature and wind speed. Symbol colours represent the different lakes. Large symbols represent binned means, small symbols represent individual estimates. Bin sizes were 10 days, 1 °C and 0.5 m s$^{-1}$ for time, water temperature and $U_{10}$, respectively. Linear relations of binned quantities and the wind speed were statistically significant (residence time: $p \leq 0.002$; each storage: $p \leq 0.04$). Observation was paired with $T$ and $U_{10}$ averaged over the 24h (Villasjön) and 72h (Inre and Mellersta Harrsjön) prior to water sampling, reflecting average conditions during CH$_4$ residence times. The linear regressions of the residence time onto time of measurement (a) and the surface water temperature (b) were not statistically significant ($p = 0.07$–0.10). Linear relations of binned quantities and $U_{10}$ were statistically significant (c: $p \leq 0.002$; f: $p \leq 0.04$). Arrhenius-type functions (Eq. 7) adequately described the storage-temperature relation in each lake (e: $R^2 \geq 0.70$, $p < 0.001$).
3.4 Variability

Chamber fluxes and surface water concentrations differed significantly between lakes (ANOVA, $p < 0.001$, $n = 287, n = 365$) (Table 2). Both quantities were inversely correlated with lake surface area (Table 2). CH$_4$ concentrations in the stream feeding the Mire (22.2 ± 5.1 mg m$^{-3}$, $n = 29$, mean ± 95% CI), were significantly higher than those in the lakes (Table 2) (Lundin et al., 2013). Surface water concentrations over the deep parts of the deeper lakes (≥ 2 m water depth) were lower than those in the shallows (< 2 m) by 21 to 26% for Inre and Mellersta Harrsjön, respectively. However, the diffusive CH$_4$ flux did not differ significantly between depth zones in either Inre Harrsjön (ANOVA, $p = 0.27$, $n = 290$) or Mellersta Harrsjön (ANOVA, $p = 0.90$, $n = 293$), or between zones of high and low CH$_4$ ebullition in Villasjön (paired t-test, $p = 0.27$, $n = 89$). This is a contrast with ebullition, for which the highest fluxes were consistently observed in the shallow lake and littoral areas of the deeper lakes (Jansen et al., 2019; Wik et al., 2013).

Relations between the flux and its drivers — temperature, wind speed and the surface concentration — manifested on different timescales (Fig. 7). Over the ice-free season both the CH$_4$ fluxes and surface water concentrations tracked changes in the water temperature. The wind speed ($U_{10}$) showed less variability over seasonal (CV = 7%, $n = 17$) than over diel timescales (CV = 12%, $n = 24$) and displayed a clear diurnal maximum. The surface water/sediment temperature varied primarily on a seasonal timescale (CV = 52%/45%, $n = 17$), and less on diel timescales (CV = 3%/2%, $n = 24$). Similar to the wind speed the gas transfer velocity varied primarily on diel timescales (Fig. 7), albeit with a lower amplitude. This was in part because $k_{mod} \propto u^{3/4}$ (Eq. 4.4), and because the drag coefficient, used to compute the water-side friction velocity in Equation 5, increases at lower wind speeds and under an unstable atmosphere, which was typically the case. The surface concentration correlated with wind speed and temperature (Fig. 4f,g), and showed both seasonal and diel variability. On diel timescales $\Delta$[CH$_4$] appeared and $k_{mod}$ were out of phase with $k_{mod}$ and $\Delta$[CH$_4$] peaked just before noon, when the gas transfer velocity reached its maximum value (Fig. 7b,d). However, binned means of $\Delta$[CH$_4$the 1-hour chamber fluxes ($F_{ch}(1h)$) were not significantly different at the 95% confidence level (error bars) and the 1-hour chamber fluxes did not show a clear diel pattern (Fig. 7b). Temporal patterns of fluxes and concentrations were very similar between the lakes (Supplementary Fig. 2 and 3).
Figure 7 – Temporal patterns of CH₄ chamber fluxes, concentrations (a,b), gas transfer velocity, air and surface water temperature and wind speed (c,d). Bin sizes are 10 days (a,c) and 1 hour (b,d). Error bars represent 95% confidence intervals of the binned means. Temporal patterns in each individual lake are shown in Supplementary Figures 2 and 3.
3.5 Timescale analysis

The spectral density plot (Fig. 8a) disentangles dominant timescales of variability of the drivers of the flux. The power spectra of wind speed and temperature peaked at periods of 1 day and 1 year, following well-known diel and annual cycles of insolation and seasonal variations in climate (Baldocchi et al., 2001). For $U_{10}$, the overall spectral density maximum between 1 day and 1 week corresponds to synoptic-scale weather variability, such as the passage of fronts (MacIntyre et al., 2009). $U_{10}$ and $T_{air}$ also exhibit spectral density peaks at 1–3 weeks, which could be associated with persistent atmospheric blocking typical of the Scandinavian region (Tyrlis and Hoskins, 2008). While the temperature variability was concentrated at annual timescales, the wind speed varied primarily on timescales shorter than about a month.

The climacogram (Fig. 8b) reveals that the variability of the chamber flux and the gas transfer velocity was enveloped by that of the water temperature and the wind speed, as was the surface concentration difference for timescales < 5 months. The distribution of variability over the different timescales is similar to that shown in the spectral density plot (Fig. 8a). The standard deviation of the water temperature did not change from its initial value ($\sigma/\sigma_{\text{init}} = 1$) until timescales of about 1 month, following the 1 year harmonic. In contrast, most of the variability of the wind speed was concentrated at timescales shorter than 1 month. The variability of the chamber and modelled fluxes first tracked that of the wind speed, but for timescales longer than about 1 month the decrease in variability resembled that of water temperature.

The variability of the modelled fluxes followed that of the surface concentration difference rather than the gas transfer velocity. However, the coarse sampling resolution of the fluxes and concentrations may have led to an underestimation of both the variability at <1-week timescales (Fig. 7b) and the value of $\sigma_{\text{init}}$. Finally, the climacogram shows that $k_{\text{mod}}$ retains about 72% of its variability at 24-hour timescales, which justifies our averaging over chamber deployment periods for comparison with $k_{\text{ch}}$ and the computation of the model scaling parameter $\alpha'$ (Fig. 3).
Figure 8 – Timescale analysis of the diffusive CH$_4$ flux and its drivers. a: Normalized spectral density of whole-year near-continuous timeseries of the air temperature ($T_{air}$), temperature of the surface water temperature and ice (0.1–0.5 m, $T_{water/ice}$), temperature of the surface sediment in Mellersta Harrsjön ($T_{sed}$) and the wind speed ($U_{10}$). b: Climacogram of the measured and modelled CH$_4$ flux ($F_{ch}$, $F_{mod}$), the air and surface water temperature ($T_{air}$, $T_{water}$), water-air concentration difference ($\Delta$[CH$_4$]), modelled gas transfer velocity ($k_{mod}$) and the wind speed ($U_{10}$) during the ice-free seasons of 2009–2017. Dashed, light-grey curves represent (combinations of) trigonometric functions of mean 0 and amplitude 1 with a specified period. 24h and 1yr harmonic functions were continuous over the dataset period while the 24h + 1yr harmonic was limited to periods when chamber flux data were available.
Panel a is based on continuous timeseries that include the ice-cover seasons: Supplementary Figure 4 shows spectral density plots for individual ice-free seasons.
4. Discussion

4.1 Magnitudes of fluxes and gas transfer velocities

Overall, diffusive CH$_4$ emissions from the Stordalen Mire lakes (6.9 ± 0.3 mg m$^{-2}$ d$^{-1}$, mean ± 95% CI) were lower than the average of postglacial lakes north of 50°N, but within the interquartile range (mean 12.5, IQR 3.0–17.9 mg m$^{-2}$ d$^{-1}$, Wik et al., 2016b). Emissions are also at the lower end of the range for northern lakes of similar size (0.01–0.2 km$^2$) (1–100 mg m$^{-2}$ d$^{-1}$, Wik et al., 2016b). As emissions of the Stordalen Mire lakes do not appear to be limited by substrate quality or quantity (Wik et al., 2018), but strongly depend on temperature (Fig. 4b), the difference is likely because a majority of flux measurements from other postglacial lakes were conducted in the warmer, subarctic boreal zone. Boreal lake CH$_4$ emissions are generally higher for lakes of similar size: 20–40 mg m$^{-2}$ d$^{-1}$ (binned means), $n = 91$ (Rasilo et al., 2015); ~12 mg m$^{-2}$ d$^{-1}$, $n = 72$ (Juutinen et al., 2009).

The gas transfer velocity in the Stordalen Mire lakes was similar to that predicted from wind-based models of Cole and Caraco (1998) and Crusius and Wanninkhof (2003) at low wind speeds (Fig. 9). Both were based on tracer experiments with sampling over several days, and thus, like our approach, are integrative measures. The slope of the linear wind-$k_{ch}$ relation (OLS: 0.81 ± 0.21, slope ± 95% CI, $R^2 = 0.20$ and $p < 0.01$ for the individual $k_{ch}$ estimates (small orange rhombuses in Fig. 9)) was similar to that reported by Soumis et al. (2008) (0.78 for a 0.06 km$^2$ lake), who also used a mass balance approach, and Vachon and Prairie (2013) (0.70–1.16 for lakes 0.01–0.15 km$^2$). Part of the difference with the models of Vachon and Prairie (2013), Cole and Caraco (1998) and Soumis et al. (2008) was caused by the offset at 0 wind speed, which may stem from a larger contribution of the buoyancy flux in their lakes than we computed for our lakes with the surface renewal model (Crill et al., 1988; Read et al., 2012) or from remnant wind shear turbulence (MacIntyre et al., 2018). While fetch limitation can reduce gas transfer at high wind speeds in small lakes (Vachon and Prairie, 2013; Wanninkhof, 1992), and the lakes studied here are at the low end of the size spectrum of water bodies in which the gas transfer models in Fig. 9 were developed (Table S1), there are a number of other explanations for the low values we obtained. We further discuss these in section 4.5 after evaluating drivers of fluxes.
Figure 9 – Normalized gas transfer velocities ($k_{600}$) versus the wind speed at 10 m ($U_{10}$). Binned values (large rhombuses, $k_{ch}$, and $k_{mod}$, bin size = 0.5 m s$^{-1}$) and individual observations (small rhombuses, $k_{ch}$) from floating chambers ($k_{ch}$) and the surface renewal model ($k_{mod}$ with $\alpha' = 0.23$). Error bars represent 95% confidence intervals of the binned means. Solid lines represent models from the literature: Cole and Caraco (1998) (CC98), Crusius and Wanninkhof (2003) (bilinear and power law models) (CW03), Soumis et al. (2008) (S08) and Vachon and Prairie (2013) (VP13) for lake surface areas of 0.01 and 0.15 km$^2$. Supplementary Table 1 lists the model equations and calibration ranges. A power-law regression model is shown for the individual $k_{ch}$ datapoints ($n = 334$): $k_{600} = 0.77 \times U_{10}^{1.02} + 0.62$ (dashed yellow line).
4.2 Drivers of flux

Methane emitted from lakes in wetland environments can be produced in situ, or be transported in from the surrounding landscape (Paytan et al., 2015). The distinction is important because some controls on terrestrial methane production, such as water table depth (Brown et al., 2014), are irrelevant in lakes. In the Stordalen Mire lakes, the Arrhenius-type relation of CH₄ fluxes and concentrations (Fig. 4b,f) together with short CH₄ residence times (Fig. 6) suggest that efficient redistribution of dissolved CH₄ strongly coupled emissions to sediment methane production. High CH₄ concentrations in the stream (section 3.4) further suggest that external inputs of CH₄ — produced in the fens and transported into the stream with surface runoff, or produced in stream sediments — may have elevated emissions in Mellersta Harrsjön (Lundin et al., 2013). However, although the Mire exports substantial quantities of DOC and presumably CH₄ from the water-logged fens to the lakes (Olefeldt and Roulet, 2012), after rainy periods we observed either a decrease in Δ[CH₄] (13–19 July 2017, Fig. 5) or no significant change (3–6 July and 21–27 August 2017, Fig. 5). It remains unclear whether such reduced storage resulted from lower methanogenesis rates associated with the temperature drop after rainfall, convection-induced degassing, or lake water displacement or dilution by surface runoff.

Turbulent transfer was dominated by wind shear in the Stordalen Mire lakes, and we computed a minor contribution (~8%) of the buoyancy-controlled fraction of k. Our result differs from that in Read et al. (2012) who found that buoyancy flux dominated turbulence production in temperate lakes 0.1 km² in size and smaller. For the Stordalen lakes we computed higher ice-free season mean values of \( u_{*w} \) as well as lower values of the water-side vertical friction velocity, \( w_{*w} = (\beta z_{mix})^{1/3} \cdot (1.2–1.8 \text{ mm s}^{-1}) \) than they report (2.0–7.5 mm s⁻¹, \( n = 40 \) lakes). The difference here results from high wind speeds and often colder surface waters compared to many temperate lakes. Therefore, values of sensible and latent heat fluxes are lower in our lakes than in lakes in warmer regions. Many small lakes have low wind speeds particularly at night. Consequently, the temperate lakes surveyed in Read et al. (2012), will have a larger contribution of buoyancy flux to the gas transfer coefficient at night (MacIntyre and Melack, 2009). The contribution of convection also depends on the wind-sheltering properties of the landscape surrounding the lake (Kankaala et al., 2013; Markfort et al., 2010). Depending on the turbulence environment, the buoyancy flux is thus weighed differently in parameterizations of \( e \) (Heiskanen et al., 2014; Tedford et al., 2014) and in wind-based models (offsets at \( U_{10} = 0 \) in Fig. 9), contributing to significant differences between model realizations of \( k \) (Dugan et al., 2016; Erkkilä et al., 2018; Schilder et al., 2016).

The distinct spectral peaks of temperature and \( U_{10} \) (Fig. 8) indicate that flux dependencies on these parameters (Fig. 4b,c) acted on different timescales. 4.1 Magnitude

Overall, diffusive emissions were lower than the average of postglacial lakes north of 50°N, but within the interquartile range (12.5, 3.0–17.9 mg m⁻² d⁻¹, Wik et al., 2016b). Emissions are also on the lower end of the range for northern lakes of similar size (0.01–0.2 km²) (1–100 mg m⁻² d⁻¹, Wik et al., 2016b). As emissions of the Stordalen lakes do not appear to be limited by substrate quality or quantity (Wik et al., 2018) this difference has implications for the choice of models or proxies of the flux in predictive analyses. For lakes that mix frequently and a climatology similar to that of the Stordalen Mire (Malmer et al., 2005), temperature-based proxies (e.g. Thornton et al., 2015) would resolve most of the variability of the ice-free diffusive CH₄ flux at timescales longer than a month. Advanced gas transfer models that account for
atmospheric stability and rapid variations in wind shear, such as we have used here, allowed us to resolve variability in flux at timescales shorter than about a month. Our results are representative of small, wind-exposed lakes in cold environments, where, as a result of considerable wind driven mixing, fluxes are lower than would be predicted in lakes where buoyancy fluxes during heating and cooling are higher, but strongly depend on temperature (Fig. 4b). The difference is likely because a majority of flux measurements from other postglacial lakes were conducted in the warmer, subarctic boreal zone. Boreal lake CH₄ emissions are generally higher for lakes of similar size: 20–40 mg m⁻² d⁻¹ (binned means), n = 91 (Rasilo et al., 2015); ~12 mg m⁻² d⁻¹, n = 72 (Juutinen et al., 2009).

The gas transfer velocity in the Stordalen lakes was similar to Cole and Caraco (1998) and Crusius and Wanninkhof (2003) at low wind speeds, both of which were based on tracer experiments with sampling over several days, and thus, like our approach, are integrative measures (Fig. 9). At higher winds we obtain lower k-values by nearly a factor of 2 (Table S1). The slope of the linear wind-kch relation (OLS: 0.81 ± 0.21, slope ± 95% CI, dashed yellow line in Fig. 9) was similar to that reported by Soumis et al. (2008) (0.78 for a 0.06 km² lake), who also used a mass balance approach, and Vachon and Prairie (2013) (0.70–1.16 for lakes 0.01–0.15 km²). Part of the difference with literature models was caused by the offset at 0 wind speed, which may stem from a larger contribution of the buoyancy flux (Crill et al., 1988; Read et al., 2012) or from remnant wind shear turbulence (MacIntyre et al., 2018). Another explanation may be the damping of turbulence by near-surface stratification (MacIntyre et al., 2010, 2018), however, such stratification was intermittent in our study (Fig. 5f–h). It may also result from our typically having a stable atmosphere in the day for much of the summer which reduces momentum transfer to the water surface. While our calculations take atmospheric stability into account, work on modelling momentum flux and related drag coefficients under stable atmospheres is ongoing and may lead to lower dissipation rates than we compute (Grachev et al., 2013). Due to the large spread of the chamber-derived gas transfer velocities (small rhombuses, Fig. 9) a power-law exponent to U₁₀ (1.0±0.18; exponent and 95% CI) and thus the nature of the wind-k relation could not be determined with confidence.
Figure 9—Normalized gas transfer velocities ($k_{\infty}$) versus the wind speed at 10 m ($U_{10}$). Binned values (large rhombuses) and individual observations (small rhombuses) from floating chambers ($k_{ch}$) and the surface renewal model ($k_{mod}$ with $\alpha' = 0.24$). Error bars represent 95% confidence intervals of the binned means. Solid lines represent models from the literature: Cole and Caraco (1998), Crusius and Wanninkhof (2003) (bilinear and power law models), Soumis et al. (2008) and Vachon and Prairie (2013) for lake surface areas of 0.01 and 0.15 km$^2$. Supplementary Table 1 lists the model equations and calibration ranges. A linear regression model is shown for the $k_{ch}$ data (dashed yellow line): $k_{ch} = 0.80^{+0.6}_{-0.5} \times U_{10} + 0.6^{+1.3}_{-0.2}$ (sub- and superscripts denote 95% confidence intervals), with $R^2 = 0.20$ for individual chamber values (small orange rhombuses) and $R^2 = 0.64$ for the binned means (large orange rhombuses).
4.2 Drivers of the flux

The Arrhenius-type relation of CH$_4$ fluxes and concentrations (Fig. 4b,f) together with short CH$_4$ residence times (Fig. 6) suggest that emissions from the Stordalen lakes were strongly coupled to sediment production through efficient redistribution of dissolved CH$_4$. High CH$_4$ concentrations in the stream suggest that terrestrial inputs of CH$_4$ may have elevated emissions in Mellersta Harrsjön (Lundin et al., 2013; Paytan et al., 2015). Similarly, terrestrial inputs of nutrients may have indirectly enhanced emissions in the littoral zones by supporting production of autochthonous organic substrates (Davidson et al., 2018; Rantala et al., 2016). However, although the Mire exports substantial quantities of DOC and presumably CH$_4$ from the waterlogged fens to the lakes (Olefeldt and Roulet, 2012), after cold and rainy periods we observed either a decrease in Δ[CH$_4$] (13–19 July 2017, Fig. 5) or no significant change (3–6 July and 21–27 August 2017, Fig. 5). It remains unclear whether such reduced storage resulted from lower methanogenesis rates, convection-induced degassing or lake water displacement by surface runoff.

Turbulent transfer was dominated by wind shear in the Stordalen lakes. We computed a minor contribution (∼8%) of the buoyancy-controlled fraction of $k$ ($k_{B,0} = 0.3$ cm h$^{-1}$) (ice-free season mean, 2009–2017). Our results differ from that in Read et al. (2012) who expect a dominant role of convection to $k$ in small lakes. The difference here results from low values of sensible and latent heat fluxes due to colder temperatures during summer such that net long wave radiation was often less than 50 W m$^{-2}$.

Lakes in warmer regions with lower humidity and clearer skies and low wind speeds particularly at night will have a larger contribution of buoyancy flux to the gas transfer coefficient (MacIntyre and Melack, 2009). The contribution of convection also depends on the wind-sheltering properties of the landscape surrounding the lake (Kankaala et al., 2013; Markfort et al., 2010). Depending on the turbulence environment the buoyancy flux is thus weighed differently in parameterizations of $k$ (Heiskanen et al., 2014; Tedford et al., 2014) and in wind-based models (offsets at $U_{W} = 0$ in Fig. 9), contributing to significant differences between model realizations of $k$ (Dugan et al., 2016; Erkkilä et al., 2018; Schilder et al., 2016). We expect our results to be representative of small, wind-exposed lakes in cold environments.

4.3 Storage and stability

The robust temperature-sensitivity of lake methane emissions (Fig. 4b,f) (Wik et al., 2014; Yvon-Durocher et al., 2014) is driven by biotic and abiotic mechanisms. Lake mixing regime can modulate flux-temperature relationships by periodically decoupling production from emission rates (e.g., Yvon-Durocher et al., 2014). Enhanced (Engle and Melack, 2000). Here, enhanced CH$_4$ accumulation during periods of stratification may have contributed to concentration and storage maxima in July and August (Fig. 4e, 6d). However, as the CH$_4$ residence time was invariant over the season and with temperature (Fig. 6a,b), the storage-temperature relation (Fig. 6e) likely reflects rate changes in sediment methanogenesis rather than inhibited mixing. For example, the highest CH$_4$ concentrations in our dataset (59.1 ± 26.4 mg m$^{-3}$, $n = 37$) were measured during a period with exceptionally high surface water temperatures ($T_{water} = 18.5 ± 3.6$ °C) that lasted from 23 June to 30 July 2014. Emissions during this period comprised 29%–56% (depending on lake) of the 2014 ice-free diffusive flux, while the peak quantity of accumulated CH$_4$ was comprised <5%.

Two mechanisms may explain the lack of CH$_4$ accumulation. First, stratification was frequently disrupted...
by vertical mixing (Fig. 5g-h) and concurrent hypolimnetic CH₄ concentrations were not significantly different from (Inre Harrsjön, 2010–2017, paired t-test, \( p = 0.12, n = 32 \)) or lower than (Mellersta Harrsjön, 2010–2017, paired t-test, \( p < 0.01, n = 35 \)) those in the surface mixed layer. Second, stratification often was not strong enough to affect gas transfer velocities \( (N > 25 \text{ during } < 17\% \text{ of this period}) \). Even when assuming \( \epsilon \) was suppressed by an order of magnitude for \( N > 25 \) and by two orders of magnitude for \( N > 40 \) \( (\text{MacIntyre et al., 2018}) \) \( k_{\text{mod}} \) was only slightly lower \( (2.8 \text{ cm h}^{-1}) \) than the multi-year mean \( (3.0 \text{ cm h}^{-1}) \). Thus, in weakly stratified, polymictic lakes with strong wind mixing, the temperature sensitivity of diffusive CH₄ emissions may be observed without significant modulation by stratification.

The water-air concentration difference—Degassing (Fig. 4c,g) prevented an unlimited increase of the emission rate with the gas transfer velocity. In this way, \( \Delta \text{[CH}_4\text{]} \) acted as a negative feedback that maintained a quasi-steady state between CH₄ production and removal processes throughout the ice-free season. In other words, higher temperatures led to elevated CH₄ concentrations (Fig. 4f) which in turn increased emission rates \( (\text{Eq. 1, Fig. 4b}) \). However, in contrast to the temperature-binned fluxes, when binned by wind speed high emission rates were associated with low concentrations \( (\text{Fig. 4c,g}) \). In this way the \( \Delta \text{[CH}_4\text{]} \) feedback limited the increase of the emission rate with the gas transfer velocity. In all three lakes CH₄ residence times were inversely proportional to the wind speed \( (\text{Fig. 6c}) \), indicating an imbalance between production and removal processes. We hypothesize that the imbalance exists because the variability of wind speed peaked on shorter timescales than that of the water temperature \( (\text{Fig. 8a}) \).

Changes in wind shear periodically pushed the system out of production-emission equilibrium, allowing for transient degassing and accumulation of dissolved CH₄. The temporal variability of dissolved gas concentrations is likely higher in shallow wind-exposed systems with limited buffer capacity \( (\text{Natchimuthu et al., 2016, 2017}) \) \( (\text{Natchimuthu et al., 2016, 2017}) \), and should be taken into account when applying gas transfer models to small lakes and ponds.

Rapid degassing occurred at \( U_{10} \gg 6.5 \text{ m s}^{-1} \) \( (\text{Fig. 4c, mean wind speed during chamber deployments}) \). Gas fluxes at high wind speeds may have been enhanced by the kinetic action of breaking waves \( (\text{Terry et al., 1996}) \) \( (\text{Terry et al., 1996}) \) or through microbubble-mediated transfer. Wave breaking was observed on the Stordalen lakes at wind speeds \( \geq 7 \text{ m s}^{-1} \). Microbubbles of atmospheric gas \( (\text{diameter } < 1 \text{ mm}) \) can form due to photosynthesis, rain or wave breaking \( (\text{Woolf and Thorpe, 1991}) \) \( (\text{Woolf and Thorpe, 1991}) \) and remain entrained for several days \( (\text{Turner, 1961}) \) \( (\text{Turner, 1961}) \). Due to their relatively large surface area they quickly equilibrate with sparingly soluble gases in the water column, providing an efficient emission pathway to the atmosphere when the bubbles rise to the surface \( (\text{Merlivat and Memery, 1983}) \) \( (\text{Merlivat and Memery, 1983}) \). In inland waters microbubble emissions of CH₄ have only been indirectly inferred from differences in CO₂ and CH₄ gas transfer velocities \( (\text{McGinnis et al., 2015; Prairie and del Giorgio, 2013}) \) \( (\text{McGinnis et al., 2015; Prairie and del Giorgio, 2013}) \), and more work is needed to evaluate their significance in relatively sheltered systems.

4.4 Timescales of variability

Overall, the short-term variability of the flux due to wind speed \( (1.1–13.2 \text{ mg m}^{-2} \text{ d}^{-1}) \) was similar to the long-term variability due to temperature \( (0.7–12.2 \text{ mg m}^{-2} \text{ d}^{-1}) \) \( (\text{ranges of the binned means, Fig. 4b-c}) \).
The diel patterns in the mixed layer depth (Fig. 5) and the gas transfer velocity (Fig. 7d) and daytime variation of the surface concentration (Fig. 7b) were indicative of daily storage-and-release cycles, resulting in a model flux difference of about 5 mg m\(^{-2}\) d\(^{-1}\) between morning and afternoon; about half the mean seasonal range (Fig. 7a). Diel variability of lake methane fluxes has been observed at Villasjön (eddy covariance, Jammet et al., 2017) and elsewhere (Bastviken et al., 2004, 2010; Crill et al., 1988; Erkkilä et al., 2018; Eugster et al., 2011; Hamilton et al., 1994; Podgrajsek et al., 2014). Similarly, diel patterns in the gas transfer velocity have been observed with the eddy covariance technique (Podgrajsek et al., 2015) and in model studies (Erkkilä et al., 2018). Apparent offsets between the diurnal peaks of the flux, surface concentrations and drivers (Fig 7b,d) have been noted previously (Koebsch et al., 2015), but have yet to be explained. Continuous eddy covariance measurements in lakes where the dominant emission pathway is turbulence-driven diffusion could help characterize flux variability on short timescales (e.g. Bartosiewicz et al., 2015).

The CH\(_4\) residence times (1–3 days) were not much longer than the diel timescale of vertical mixing (Fig. 5g,h). As a result, horizontal concentration gradients developed in the deeper lakes (Table 2). The 23 ± 11% concentration difference between depth zones in the deeper lakes (mean ± 95%) fits transport model predictions of DelSontro et al. (2017) for small lakes (< 1 km\(^2\)) that highlight the role of outgassing and oxidation during transport from production zones in the shallow littoral zones or the deeper sediments (Hofmann, 2013). Concentration gradients may also have been caused by physical processes, such as upwelling due to thermocline tilting (Heiskanen et al., 2014). Higher resolution measurements, for example with automated equilibration systems (Erkkilä et al., 2018; Natchimuthu et al., 2016), are needed to assess how much of the spatial and diel patterns of the CH\(_4\) concentration can be explained by physical drivers such as gas transfer and mixed layer deepening (Eugster et al., 2003; Vachon et al., 2019), or by biological processes such as methanogenesis and microbial oxidation (Ford et al., 2002).

Gas transfer models can only deliver accurate fluxes if they are combined with measurements that capture the full spatiotemporal variability of the surface concentration (Erkkilä et al., 2018; Hofmann, 2013; Natchimuthu et al., 2016; Schilder et al., 2016). The short CH\(_4\) residence times and diel pattern of Δ[CH\(_4\)] suggest that weekly sampling did not capture the full temporal variability of the surface concentrations. Especially after episodes of high wind speeds and lake degassing (Fig. 4c,g), concentrations may not have been representative of the 24-hour chamber deployment period.
Overall, the short-term variability of the flux due to wind speed was similar to the long-term variability due to temperature (ranges of the binned means, Fig. 4a-c). The diel patterns in the mixing depth (Fig. 4, 5a) and the gas transfer velocity (Fig. 7d) and daytime variation of the surface concentration (Fig. 7b) were indicative of daily storage and release cycles, resulting in a model flux difference of about 5 mg m$^{-2}$ d$^{-1}$ between morning and afternoon; about half the mean seasonal range (Fig. 7a). Diel variability of lake methane fluxes has been observed at Villäsjön (eddy covariance, Jammet et al., 2017) and elsewhere (Bastviken et al., 2004, 2010; Crill et al., 1988; Erkkilä et al., 2018; Eugster et al., 2011; Hamilton et al., 1994; Podgrajsek et al., 2014b). Similarly, diel patterns in the gas transfer velocity have been observed with the eddy covariance technique (Podgrajsek et al., 2015) and in model studies (Erkkilä et al., 2018). Apparent offsets between the diurnal peaks of the flux, surface concentrations and rivers (Fig 7b, d) have been noted previously (Koebisch et al., 2015), but have yet to be explained. Continuous eddy covariance measurements in lakes where the dominant emission pathway is turbulence-driven diffusion could help characterize flux variability on short timescales (e.g. Bartosiewicz et al., 2015).

The CH$_4$ residence times (1–3 days) were not much longer than the diel timescale of vertical mixing (Fig. 5g, h). As a result, horizontal concentration gradients developed in the deeper lakes (Table 2). The 23 ± 11% concentration difference between depth zones in the deeper lakes (mean ± 95%) fits transport model predictions of DelSontro et al. (2017) for small lakes (< 1 km$^2$) that highlight the role of outgassing and oxidation during transport from production zones in the shallow littoral zones or the deeper sediments (Hofmann, 2013). Concentration gradients may also have been caused by physical processes, such as upwelling due to thermocline tilting (Heiskanen et al., 2014). Higher resolution measurements, for example with automated equilibration systems (Erkkilä et al., 2018; Natchimuthu et al., 2016), are needed to assess how much of the spatial and diel patterns of the CH$_4$ concentration can be explained by physical drivers such as gas transfer and mixed layer deepening (Eugster et al., 2003; Vachon et al., 2019), or by biological processes such as methanogenesis and microbial oxidation (Ford et al., 2002).

The distinct spectral peaks of $U_{10}$ and temperature (Fig. 8) suggest that flux dependencies on these parameters (Fig. 4b, c) acted on different timescales. This has implications for the choice of models or proxies of the flux in predictive analyses. For polymictic lakes and a climatology similar to that of the Stordalen Mire (Malmer et al., 2005), temperature-based proxies (e.g. Thornton et al., 2015) would resolve most of the variability of the near-free diffusive CH$_4$ flux at timescales longer than a month. Advanced gas transfer models that account for atmospheric stability and rapid variations in wind shear are necessary to resolve the flux variability at timescales shorter than about a month. However, gas transfer models can only deliver accurate fluxes if they are combined with measurements that capture the full spatiotemporal variability of the surface concentration (Erkkilä et al., 2018; Hofmann, 2013; Natchimuthu et al., 2016; Schilder et al., 2016). The short CH$_4$ residence times and diel pattern of $\Delta$[CH$_4$] suggest that weekly sampling did not capture the full temporal variability of the surface concentrations. Especially after episodes of high wind speeds and lake degassing (Fig. 4c, g), concentrations may not have been representative of the 24-hour chamber deployment period.
4.6 Model-chamber comparison

It is fundamental to our understanding of controls on fluxes to determine why empirically derived values of the model scaling parameter $\alpha'$ are relatively low in this study (0.17–0.31) compared to the theoretical value of $\sqrt{2/15} \approx 0.37$ (Kurat et al., 2018), and why they were different in the three lakes. Differences in $\alpha'$ resulted from $k_{n}$, with mean (± 95% CI) values estimated at $3.5 \pm 0.7$ ($n = 74$), $3.1 \pm 0.4$ ($n = 131$) and $2.5 \pm 0.6$ ($n = 142$) cm h$^{-1}$ in Villasjön, Inre Harrsjön and Mellersta Harrsjön, respectively, while $k_{mod}$ did not differ significantly between lakes (ANOVA, $p < 0.001$). Synthesis studies show that scaling parameter values can vary between 0.1 and 0.7 over the range of moderate to high dissipation rates computed for the Stordalen Mire lakes (Eq. 5: $\varepsilon = 10^{-7}$–$10^{-5}$ m$^{2}$ s$^{-3}$) (Esters et al., 2017; Wang et al., 2015 and references therein). In such cases $\epsilon$ has been measured directly with acoustic Doppler- or particle image velocimetry and compared with independent estimates of $k$ using chambers (Gálfalk et al., 2013; Tokoro et al., 2008; Vachon et al., 2010; Wang et al., 2015), eddy covariance observations (Heiskanen et al., 2014) or the gradient flux technique (Zappa et al., 2007) and a sparingly soluble tracer, such as CO$_{2}$ or SF$_{6}$. Measured and modelled lake CO$_{2}$ fluxes agree reasonably well if Eq. 4 and Eq. 5 are used with a multi-study mean $\alpha'$ of 0.5 (Bartosiewicz et al., 2015; Czikowsky et al., 2018; Erkkilä et al., 2018; Mammarella et al., 2015), but the agreement is less clear for CH$_{4}$ fluxes (Bartosiewicz et al., 2015). The observed variability in $\alpha'$ could be explained by chemical or biological factors that limit surface exchange, or by the variable contributions of wind sheltering, atmospheric stability, and within lake stratification and mixing. Here, the low $\alpha'$ value may imply an underestimation of $k$ derived from chamber observations or an overestimation of dissipation rates used in the modelling of gas transfer velocities.

An underestimation of chamber-derived gas transfer velocities may have resulted from an overestimation of $C_{an}$ in Equation 1. In most freshwater systems a significant fraction of CH$_{4}$ is removed through microbial oxidation (Bastviken et al., 2002). This additional removal process invalidates the implicit assumption in Eq. 1 and 2 that all dissolved CH$_{4}$ that we measure in the surface water is emitted to the atmosphere. Omitting oxidation would bias $\Delta$[CH$_{4}$] high, and $k_{ch}$ low. The Stordalen Mire lakes remained oxygenated throughout the ice-free season and CH$_{4}$ stable isotopes indicate that between 24% (Villasjön) and 60% (Inre and Mellersta Harrsjön) of CH$_{4}$ in the water column was continually oxidized (Jansen et al., 2019). This may explain not only the low scaling parameter value compared to those found with other tracers, but also why $\alpha'$ was higher in Villasjön ($0.31$, $n = 67$) than in the deeper lakes ($0.17$–$0.25$, $n = 267$) (Supplementary Fig. 1). However, more work is needed to establish how the oxidation effect partitioned between CH$_{4}$ reservoirs in the water column, where it would affect surface emissions, and the sediment.

An increase in surface concentrations which typically occurs at night would not have been manifest (Crill et al., 1988; Czikowsky et al., 2018) because there was, apart from the period just after ice-off in 2017, no significant CH$_{4}$ accumulation below the mixing layer throughout the ice-free seasons. Indeed, CH$_{4}$ concentrations within the 0.1–1 m surface layer of the deeper lakes (Table 2) were not significantly different from those at greater depth (Inre Harrsjön: $12.2 \pm 2.7$ mg m$^{-3}$, $n = 292$; Mellersta Harrsjön: $17.7 \pm 4.9$ mg m$^{-3}$, $n = 405$; means ± 95% CI).

An overestimation of gas transfer velocities computed with the surface renewal model may result if actual dissipation rates are lower than we compute. Such occurs under high wind shear when more of the introduced turbulent kinetic energy is used for mixing the water column and deepening the mixing layer,
and less is dissipated (Ivey and Imberger, 1991; Jonas et al., 2003). When this occurs, the coefficient on $u_w^3$ in Eq. 5 may have a lower value (Tedford et al., 2014), which translates to a reduced estimate of $\varepsilon$ and increased $\alpha'$ values. A similar decrease of $\varepsilon$ can be assumed during heating, when strong stratification ($N > 25 \text{ cph}$) dampens turbulent dissipation (MacIntyre et al., 2010, 2018), however, such stratification was intermittent in our study (Fig. 5f-h). Comparing gas transfer velocities from the floating chambers and the surface renewal model we find a scaling parameter value ($\alpha'$ in Eq. 4) of approximately 0.24 (Fig. 3). Its theoretical value ($\alpha$) is $\sqrt{2}/15 \approx 0.37$ (Katul et al., 2018) but empirically derived values ($\alpha'$) can vary between 0.1 and 0.7 over the range of moderate to high dissipation rates computed for the Stordalen lakes (Eq. 5: $\varepsilon = 10^{-2} - 10^{-5} \text{ m}^2 \text{s}^{-3}$) (Esters et al., 2017; Wang et al., 2015 and references therein), when $\varepsilon$ is measured directly with acoustic Doppler- or particle image velocimetry and compared with independent estimates of $k$ using chambers (Gålfalk et al., 2013; Tokoro et al., 2008; Vachon et al., 2010; Wang et al., 2015), eddy covariance observations (Heiskanen et al., 2014) or the gradient flux technique (Zappa et al., 2007) and a sparingly soluble tracer, such as CO$_2$ or SF$_6$. Recent studies report a reasonable agreement between measured and modeled lake CO$_2$ fluxes if Eq.

Reduced gas transfer velocities and between-lake differences in $k_{eb}$ could also be due to differences in atmospheric forcing. First, the wind speed may have been lower over the lakes than on the Mire due to the slight elevation (<1 m) of the surrounding peatland hummocks (Markfort et al., 2010). The wind-sheltering effect of tall shrubs (Betula nana L., Malmer et al., 2005) on the shores of the deeper lakes (Fig. 1) was readily noticed during sample collection, particularly in Mellersta Harrsjön. Second, atmospheric stability was different over the three lakes. The atmosphere was stable ($z/L_{MO,a} > 0$) over Mellersta Harrsjön, Inre Harrsjön, and Villasjön during 29%, 21% and 22% of the ice free periods (2009–2017), respectively, with drag coefficients ~16% lower than their neutral value during these times. The effect was more pronounced when winds were light during daytime heating, with somewhat higher frequency during autumn. Colder incoming stream water flowing into Mellersta Harrsjön may have contributed to lower surface water temperatures in this lake (Table 3), with the discrepancy more noticeable as lake level rose (Fig. 5e-h). More frequent periods with a stable atmosphere above Mellersta Harrsjön reduced sensible and latent heat fluxes and are a likely cause of the increased stratification of the surface layer: water at 0.1 m was sometimes 0.5 °C to 2 °C warmer than at 0.3 m in Mellersta Harrsjön (5% of the time during ice-free seasons) when temperatures were isothermal in the upper 0.5 m in Villasjön and Inre Harrsjön. Greater near-surface stratification coupled with lower winds than measured on the Mire would have led to the lower values of $k$ and $\alpha'$ obtained in this lake. While this analysis points to the challenges in modelling fluxes when meteorological instrumentation is not situated on the lakes, it also suggests that a solution is to use lower values of $\alpha'$ when modelling $k$ for sheltered water bodies.

In summary, the model scaling parameter $\alpha'$ computed in this study are lower than the theoretical value of 0.37 and the 0.5 recently obtained in eddy covariance studies in which fluxes were measured with CO$_2$ and modelled. The discrepancy may be explained by surface CH$_4$ concentrations decreasing due to microbial oxidation over the same timescale as our chamber measurements. Alternate explanations take into account the magnitude of wind shear and degree of sheltering. Differences in $\alpha'$ between lakes indicate the care required in modelling emissions from sheltered lakes; the overall cooler surface water temperatures in the lake with greater stream inflows points to a new control on emissions. That is, when
stream inflows lead to surface water temperatures cooler than air temperature in sheltered lakes, a stable atmosphere results which leads to a reduced momentum flux, lower emissions, and a longer time over which methane oxidation can occur. The cooling effect may be especially pronounced in northern landscapes underlain by permafrost, where the temperature of meltwater streams and subsurface flow in the active layer remains low throughout the year. Thus, these comparisons of modelled and measured fluxes point to new areas of research.
4 and Eq. 5 are used with a multi-study mean \( \alpha' \) of 0.5 (Bartosiewicz et al., 2015; Czikowsky et al., 2018; Erkkilä et al., 2018; Mammarella et al., 2015). While there is evidence for similar agreement for CH\(_4\) with \( \alpha' = 0.5 \) (Erkkilä et al., 2018), this approach may exceed chamber-derived emissions by a factor of 2 (Bartosiewicz et al., 2015) — i.e. closer to our scaling parameter value of 0.24.

Because the physical drivers of gas exchange have been accounted for in the formulation of \( k_{\text{wind}} \), chemical or biological factors that do not affect turbulence in the actively mixed layer but can limit surface exchange could be responsible for the observed variability in \( \alpha' \). In most freshwater systems a significant fraction of CH\(_4\) is removed through microbial oxidation at the sediment surface and in the water column (Bastviken et al., 2002). The Stordalen lakes remained oxygenated throughout the ice-free season and CH\(_4\) stable isotopes indicate that between 24% (Villasjön) and 60% (Inre and Mellersta Harrsjön) of CH\(_4\) in the water column was oxidized (Jansen et al., 2019). This may explain not only the low scaling parameter value compared to those found with other tracers, but also why \( \alpha' \) was higher in Villasjön (0.31, \( n = 67 \)) than in the deeper lakes (0.17–0.25, \( n = 267 \)). However, more work is needed to establish how the oxidation effect partitioned between CH\(_4\) reservoirs in the water column, where it would affect surface emissions, and the sediment. Other biogenic factors may also have impacted gas transfer, such as organic surface slicks in the 10–100 \( \mu \)m diffusive sublayer (Tokoro et al., 2008).

Additionally, the wind speed may have been lower over the lakes than on the Mire due to the slight elevation (<1 m) of the surrounding peatland hummocks and the wind-sheltering effect of tall shrubs (Betula nana L., Malmer et al., 2005) on the shores of the deeper lakes (Fig. 1) (Markfort et al., 2010).

### 4.7 Omitted fluxes?

We investigated whether our chamber measurements may have missed high-quantity release from storage (Podgrajsek et al., 2014a). In stratified lakes, mixed layer deepening can bring up accumulated gas, resulting in elevated surface fluxes, for example due to night-time convection (Eugster et al., 2003), during autumn overturns (Encinas Fernández et al., 2014; Juutinen et al., 2009; Laurion et al., 2010; López-Bellido et al., 2009) or rain events (Bartosiewicz et al., 2015; Ojala et al., 2011). Here however, >80% of the lakes’ volume mixed on diel timescales and we did not observe substantial CH\(_4\) accumulation over summer. Indeed, CH\(_4\) concentrations within the 0.1–1 m surface layer of the deeper lakes (Table 2) were not significantly different from those at greater depth (Inre Harrsjön: 12.2 ± 2.7 \( \text{mg m}^{-3} \), \( n = 292 \); Mellersta Harrsjön: 17.7 ± 4.9 \( \text{mg m}^{-3} \), \( n = 405 \); means ± 95% CI). It is therefore unlikely that our-chamber fluxes omitted emissions from hypolimnetic storage.

### 5. Summary and conclusions

In this study we combined a unique, multi-year dataset with a modelling approach to better understand environmental controls on turbulence-driven diffusion-limited CH\(_4\) emissions from small, shallow lakes. Floating chambers estimated the seasonal mean flux at 6.9 \( \text{mg m}^{-2} \text{d}^{-1} \) and illustrated how the flux depended on temperature and wind speed. Wind shear controlled the gas transfer velocity while thermal convection and release from storage were minor drivers of the flux. CH\(_4\) fluxes and surface concentrations fitted an Arrhenius-type temperature function \( (E_a' = 0.88–0.97 \text{ eV}) \), suggesting that emissions were strongly coupled to rates of methanogenesis in the sediment. However, temperature was only an accurate proxy of the flux on averaging timescales longer than a month. On shorter timescales wind-induced variability in the gas transfer velocity, \textit{mixed} layer depth, and storage decoupled production from...
emission rates. Transient stratification changes in the lake mixing regime allowed for periodic CH$_4$ accumulation and resulted in an inverse relationship between wind speed and surface concentrations. In this way, the air-water concentration difference acted as a negative feedback to emissions and prevented complete degassing of the lakes, except at high wind speeds ($U_{10} \geq 6.5$ m s$^{-1}$).

Freshwater flux studies are increasingly focused on understanding mechanisms and developing proxies for use in upscaling efforts and process-based models. Our results show that the timescale of driver variability can inform the frequency of field measurements to yield representative datasets. Observations that capture the spatiotemporal variability of dissolved gas concentrations could help realize the potential of advanced gas transfer models to disentangle biogeochemical and physical flux drivers at half-hourly to interannual timescales. Linking model and field measurement approaches could uncover non-linear feedbacks, such as shallow lake degassing at high wind speeds, quantify biases associated with measurement timing and location, and constrain the applicability timescale of novel emission proxies. Simple temperature- or wind-based proxies can yield accurate flux estimates, but model parameters, such as $E_a'$ and $\alpha'$, must be calibrated to local conditions to reflect relevant biotic and abiotic processes at appropriate timescales. Our study highlights the importance of non-linear feedbacks, such as shallow lake degassing at high wind speeds, as well as microbial removal processes and the need to consider the timescale over which fluxes occur relative to the timescale over which CH$_4$ can be oxidized. Such biological removal processes may violate the fundamental assumption of gas transfer models that all gas measured in the surface mixing layer is emitted to the atmosphere. Advanced gas transfer models can only improve the accuracy of flux estimates if they are paired with observations that capture the meteorological conditions over the lake and the spatiotemporal variability of dissolved gas concentrations. Therefore, field measurements remain necessary to inform, calibrate and validate models. Our results indicate that the timescale of driver variability can inform the frequency of field measurements necessary to yield representative datasets for novel proxy development.
6. Data availability
Data are available at www.bolin.su.se/data/. Surface renewal model code is available by contacting SM.

7. Author contributions
JJ, MW and PC designed the study. Fieldwork and laboratory measurements were conducted by JJ, JS and MW. SM and AC developed the surface renewal model code, with contributions from AC. JJ performed the analyses and prepared the manuscript with contributions from BT, PC and SM.

8. Competing interests
The authors declare that they have no conflict of interest.

9. Acknowledgements
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Supplementary material

Supplementary Table 1 – Different relations of \( k \) with the wind speed at 10 m (\( U_{10} \)) and lake surface area (SA). Validity ranges of \( U_{10} \) were based on the data range used to construct each model. For comparison, gas transfer velocities were computed from the multi-year ice-free mean wind speed on the Stordalen Mire and normalized to a Schmidt number of 600 (CO\(_2\) at 20 °C).

<table>
<thead>
<tr>
<th>Model</th>
<th>Method</th>
<th>Lake surface area (km(^2))</th>
<th>( U_{10} ) validity range (m s(^{-1}))</th>
<th>( k_{600} ) at ( U_{10} = 4.3 ) m s(^{-1}) (cm h(^{-1}))</th>
<th>Reference</th>
</tr>
</thead>
<tbody>
<tr>
<td>( k_{600} = 0.77 \times U_{10}^{1.02} + 0.62 )</td>
<td>FC</td>
<td>0.01–0.17</td>
<td>1–9</td>
<td>4.0</td>
<td>This work</td>
</tr>
<tr>
<td>( k_{600} = 0.45 \times U_{10}^{1.6} )</td>
<td>Tracers</td>
<td>0.13–500</td>
<td>1–8</td>
<td>4.6</td>
<td>MacIntyre et al., 1995</td>
</tr>
<tr>
<td>( k_{600} = 0.215 \times U_{10}^{1.7} + 2.07 )</td>
<td>SF(_6)</td>
<td>0.15</td>
<td>0–9</td>
<td>4.6</td>
<td>Cole and Caraco, 1998</td>
</tr>
<tr>
<td>( k_{600} = 4.33 \times U_{10} - 13.3 )</td>
<td>SF(_6)</td>
<td>0.13</td>
<td>1–5.5</td>
<td>5.3</td>
<td>Crusius and Wanninkhof, 2003</td>
</tr>
<tr>
<td>( k_{600} = 0.228 \times U_{10}^{2.2} + 0.168 )</td>
<td>SF(_6)</td>
<td>0.13</td>
<td>1–5.5</td>
<td>5.8</td>
<td>Crusius and Wanninkhof, 2003</td>
</tr>
<tr>
<td>( k_{600} = 0.78 \times U_{10} + 1.31 )</td>
<td>FC</td>
<td>0.06</td>
<td>0–5</td>
<td>4.7</td>
<td>Soumis et al., 2008</td>
</tr>
<tr>
<td>( k_{600} = 1.48 \times U_{10} + 1.48 \times U_{10} \times \log_{10}(SA) + 2.51 )</td>
<td>FC</td>
<td>0.01–0.15</td>
<td>1–6.5</td>
<td>5.5–7.5</td>
<td>Vachon and Prairie, 2013</td>
</tr>
</tbody>
</table>
Supplementary Figure 1 – Based on Figure 3 (main text), but for individual lakes: Villasjön (a), Inre Harrsjön (b) and Mellersta Harrsjön (c). Comparison between gas transfer velocities from floating chambers (Eq. 2, main text) and the surface renewal model (Eq. 4, main text, with $\alpha' = 1$ and $Sc = 600$, half-hourly values averaged over each chamber deployment period). Mean ratios, and therefore $\alpha'$, are represented by the slopes of the dotted lines. Error estimates represent the 95% confidence intervals of the mean ratios.
Supplementary Figure 2 – Based on Figure 7a and 7c (main text), but for individual lakes: Villasjön (a,b), Inre Harrsjön (c,d) and Mellersta Harrsjön (e,f). Temporal variation of the 24-hour chamber fluxes (a,c,e), air-water concentration difference (b,d,f), air and water temperature (g) and modelled gas transfer velocity and measured wind speed (h). In panels a-f, large squares and triangles represent binned means.
with 95% confidence interval error bars, horizontal bars represent binned medians and small symbols show individual measurements. Variables were binned in 10-day bins.
Supplementary Figure 3 – Based on Figure 7b and 7d (main text), but for individual lakes: Villasjön (a,b), Inre Harrsjön (c,d) and Mellersta Harrsjön (e,f). Temporal variation of the 1-hour chamber fluxes (a,c,e), air-water concentration difference (b,d,f), air and water temperature (g) and modelled gas transfer velocity and measured wind speed (h). In panels a-f, large squares and triangles represent binned means.
with 95% confidence interval error bars, horizontal bars represent binned medians and small symbols show individual measurements. Variables were binned in 1-hour bins.
Supplementary Figure 4 – Based on Figure 8a (main text), but for the ice-free seasons of individual measurement years. Normalized spectral densities of wind speed (a), air temperature (c), surface water temperature (e) and surface sediment temperature in Villasjön (b), Inre Harrsjön (d) and Mellersta Harrsjön (f).
Supplementary References


