Ecosystem physio-phenology revealed using circular statistics

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Abstract. Quantifying how vegetation phenology responds to climate variability is a key prerequisite to predict how ecosystem dynamics will shift with climate change. So far, many studies have focused on responses of classical phenological events (e.g. budburst or flowering) to climatic variability for individual species. Comparatively little is known on the dynamics of physio-phenological events such as the timing of maximum gross primary production (DOY GPP max), i.e. quantities that are relevant for understanding terrestrial carbon cycle responses to climate variability and change. In this study, we aim to understand how DOY GPP max depends on climate drivers across 52 eddy-covariance (EC) sites in the FLUXNET network for different regions of the world. Most phenological studies rely on linear methods that cannot be generalized across both hemispheres and therefore do not allow for deriving general rules that can be applied for future predictions. One solution could be a new class of circular-linear (here called circular) regression approaches. Circular regression allows relating circular variables (in our case phenological events) to linear predictor variables as climate conditions. As a proof of concept, we compare the performance of linear and circular regression to recover original coefficients of a predefined circular model on artificial data. We then quantify the sensitivity of DOY GPP max across FLUXNET sites to air temperature, short-wave incoming radiation, precipitation and vapor pressure deficit. Finally, we evaluate the predictive power of the circular regression model for different vegetation types. Our results show that the joint effects of radiation, temperature and vapor pressure deficit is the most relevant controlling factor of DOY GPP max across sites. Woody savannas are an exception where the most important factor is precipitation. Although the sensitivity of the DOY GPP max to climate drivers is site specific, it is possible to generalize the circular regression models across specific vegetation types. From a methodological point of view, our results reveal that circular regression is a robust alternative to conventional phenological analytic frameworks. The analysis of phenological events at global scale can benefit from the use of circular statistics. Such an approach yields substantially more robust results for analyzing phenological dynamics in regions characterized by two growing seasons per year, or when the phenological event under scrutiny occurs between two years (i.e. DOY GPP max in the Southern Hemisphere).
1 Introduction

Phenology is the study of the timing of biological events that can be observed either at the organismic level or at the ecosystem scale (Lieth, 1974). For the latter, phenology is the study of some integral behavior across phenological states of the integrated canopy reflectance captured by remote sensing (Richardson et al., 2009; Zhang et al., 2003), or vegetation-driven ecosystem-atmosphere CO$_2$-exchange fluxes (Richardson et al., 2010). Ecosystem scale physio-phenological processes of this kind are relevant quantities in global biogeochemical cycles and integrates both, the seasonal dynamics of biophysical states (e.g. reflected in the canopy development), and the observed photosynthesis at the stand level (i.e. gross primary production). Here we are particularly interested in the timing when ecosystems reach their maximum CO$_2$-uptake within a growing season.

Ecosystem-physiophenology is influenced by climate conditions but simultaneously contributes to the regulation of different micro and macro meteorological patterns. Physio-phenological cycles determine the temporal dynamics of land-atmosphere water and energy exchange fluxes. Likewise, the terrestrial carbon cycle is affected by phenological controls on CO$_2$ uptake and release (Peñuelas et al., 2009).

The eddy covariance technique (EC) allows to continuously measuring the exchange of energy and matter between ecosystems and atmosphere (Aubinet et al., 2012). The FLUXNET network collects EC data for most ecosystems of the world along with other meteorological variables, i.e. radiation, temperature, precipitation, as well as with atmospheric humidity, and often soil moisture (Baldocchi et al., 2001; Baldocchi, 2020). Particularly relevant to pheneological studies is the seasonal trajectory of gross primary production (GPP) allowing to derive phenological transition dates such as start and end of the growing season (e.g., Luo et al., 2018), as well as the timing of the maximum gross primary production, hereafter as referred to as DOY$_{GPPmax}$ (Zhou et al., 2016; Peichl et al., 2018; Wang and Wu, 2019).

In this study we focus on understanding how climate variability affects the time when ecosystems reach their maximum potential for CO$_2$ absorption. In order to reach this “optimum state” several preconditions must be met during the preceding part of the growing season. So far several studies have focused on studying the variability of maximum GPP during the growing season (GPPmax). For instance, Zhou et al. (2017) studied how the variability of annual GPP is influenced by GPPmax and the start and the end of the growing season. The authors found that GPPmax is a better explanatory parameter for the inter-annual variability of annual GPP than the start and end days of the growing season. Bauerle et al. (2012) studied how photoperiod and temperature influence plants photosynthetic capacity for 23 tree species in temperate deciduous hardwoods, reporting that the photoperiod explains the variability of photosynthetic capacity better than temperature. So far, to the best of our knowledge, only one study has focused on understanding the temporal variability of GPPmax: Wang and Wu (2019) used a combination of satellite remote sensing, and eddy-covariance data to explore how DOY$_{GPPmax}$ is controlled by climatic conditions. The authors reported that higher temperatures advance DOY$_{GPPmax}$, while the influence of precipitation and radiation were biome-dependent. This study had a geographical focus on China; a global approach considering several ecosystems across the whole latitudinal gradient is still lacking.

The challenge of understanding phenology is generally to characterize a discrete event that repeats periodically. Classically, phenological analyses have been performed using linear regression models (Morente-López et al., 2018; Zhou et al., 2016).
Figure 1. Conceptual distribution of GPPmax timing (DOY_{GPPmax}) for two hypothetical ecosystems one in the Northern (Blue), and one in the Southern Hemisphere (Red). The distance between the color line and the circle represent the frequency of the DOY_{GPPmax} observations. The distance between the end and the beginning of the distribution represent the DOY_{GPPmax} inter-annual variability.

Most of these studies analyze ecosystems characterized by one growing season (e.g. temperate or boreal forests), and when the summer is centered around the middle of the calendar year. The existing methods are, however, not sufficiently generic to describe i) ecosystems in the Southern Hemisphere, and ii) ecosystems with multiple growing seasons per year as it is often observed in e.g. semi-arid regions.

Figure 1 illustrates the problem of Northern vs. Southern Hemispheric summers from a conceptual point of view. Assume that some discrete event recurs annually, but the timing varies according to some external drivers. We would then need to find a predictive model explaining the inter-annual variability of phenology i.e. the probability of this recurrent event in the course of the annual cycle. The Fig. 1 shows that linear regression models would be inappropriate to predict the day of the year (DOY) of some phenological event in the Southern Hemisphere, as the actual target values to predict may flip between $\gtrsim \frac{3\pi}{2}$ and $\lesssim \frac{\pi}{2}$.

In recent years, circular statistics have gained some attention as they offer a solution to problems of this kind (Morellato et al., 2010; Beyene et al., 2018). Unlike classical statistics, the predicted variables are expressed in terms of angular directions (degrees or radians) across a circumference (Fisher, 1995) allowing to perform statistical analysis where the data space is not...
Euclidean. In this framework, point events can be described as a von-Mises distribution (Von Mises, 1918), the equivalent to the normal distribution in the circular statistics. The von-Mises distribution is described by two parameters: The mean angular direction ($\mu$) and the concentration parameter ($\kappa$). Circular-linear regressions (in the following simply named circular regression) allow to predict circular responses (e.g. the timing of phenological events) from other linear variables (Morellato et al., 2010). Given that any phenological event can be interpreted as an angular direction, and should be modeled alike, we assume that these circular regressions are well suited in this context. Despite this evident suitability, circular statistics have not yet been extensively applied in the study of phenology and will therefore be presented here as an alternative to conventional linear techniques.

In this paper, we aim to identify the factors controlling the timing of the maximal seasonal GPP (DOY$_{\text{GPPmax}}$). The questions we want to answer are: First, can circular statistics describe and predict DOY$_{\text{GPPmax}}$ per vegetation type? This aspect requires testing the methodological advantages and caveats of circular statistics across hemispheres in comparison with linear methods. Second, can DOY$_{\text{GPPmax}}$ be explained using cumulative climate conditions? This question needs to consider different possibilities for generating temporally integrating features. And third, how is DOY$_{\text{GPPmax}}$ affected by the climatic conditions during the growing season? The last question requires a global cross-site analysis. Based on the findings of these three questions we then discuss the potential of circular regressions beyond this specific application case in related phenological problems and outline future applications.

2 Methods

2.1 Data

We use 52 EC sites (with at least seven years of data) located through the latitudinal gradient of the globe from the FLUXNET-2015 database (Table A1, http://fluxnet.fluxdata.org/ Pastorello et al., 2017). Each FLUXNET site is identified with an abbreviation of the country and the name of the place e.g. the EC tower AU-How, means that it is located in Howard Springs, Australia. From the dataset we use the GPP data that was derived using the nighttime partitioning method and considering the variable $u^*$-threshold to discriminate values of insufficient turbulence (Reichstein et al., 2005). In order to identify maximum daily GPP, we compute the quantile 0.9 for each day based on the half-hourly flux observations. As potential explanatory variables for DOY$_{\text{GPPmax}}$ we use the daily air temperature (Tair), shortwave incoming radiation (SWin), precipitation (Precip), and vapor pressure deficit (VPD).

Given that the past climate conditions affect the CO$_2$ exchange between the atmosphere (ecological memory, Liu et al., 2019; Ryan et al., 2015), we assume that an aggregated form of these climatic variables needs to be considered in the prediction of the phenological responses. We aggregate the original times-series of the Tair, SWin, Precip, and VPD for each DOY$_{\text{GPPmax}}$ using a half-life decay function (eq. 1),

$$\langle x_t \rangle = \frac{\sum_{i=0}^{\tau} x_{t-i} w_i}{\sum_{i=0}^{\tau-1} w_i},$$  \hspace{1cm} (1)
for estimating an exponentially weighted mean of the observation vector, \( \mathbf{x}_t = (x_t, x_{t-1}, \ldots, x_{t-\tau})^T \), at time step \( t \). The symbol \( \langle \ldots \rangle \) denotes the weighted average; \( i \) indicates the number of days before \( t \) going back up to \( \tau = 365 \) days. The weight decay is represented by

\[
w_i = w_0 \exp \left( -i \frac{\ln(2)}{t_{1/2}} \right). \tag{2}
\]

The decay function gives the instantaneous value a weight of 1 \( (w_0 = 1) \) and all preceding values receive an exponentially reduced weight as determined by the half-time-parameter \( t_{1/2} \). Finally, we make these variables comparable via centering standardization to unit variance. We perform a sensitivity analysis evaluating the effect of the half-time parameter and identify the optimum as the value when the variance explained by the circular regression model is maximum. The results are presented in Supplement 1.

Due to the high co-linearity between the exponential weighted variables of Tair, SWin and VPD we perform a principal component analysis (PCA) on the matrix of variables and FLUXNET sites and retain the leading principal component of these variables, and precipitation as input for the circular statistics model (Hastie et al., 2009). The results of the PCA analysis are presented in the Supplement 2.

### 2.2 Circular statistics

Since units of the circular response variable must be in radians or degrees. We transform the days of the year to radians using equation 3. For leap years we remove the last day.

\[
\text{rad} = \text{DOY} \cdot \frac{360 \pi}{365 \cdot 180} \tag{3}
\]

where \( \text{DOY} \) : Day of the year.

A basic circular regression model was proposed by Fisher and Lee (1992) as follows:

\[
y = \mu + 2 \arctan(\beta_i x_i) \tag{4}
\]

where \( y \) is the target variable (i.e. \( \text{DOY}_{\text{GPPmax}} \)) in radians, \( \mu \) is the mean angular direction of the target variable, \( x_i \) are the values for the variable \( i \), and \( \beta_i \) is the regression coefficient. The parameters \( \mu \) and \( \beta \) are fitted via the maximum likelihood method using reweighted least squares algorithm as proposed by Green (1984).

Relevant interpretations of fitted circular regression models are 1) the sign of the \( \beta \)-coefficients, 2) the statistical significance of the coefficients, and 3) the accuracy of the prediction. Regarding the first point: A negative sign of the coefficient would mean that an increasing value of the predictor would lead to an earlier \( \text{DOY}_{\text{GPPmax}} \) compared to the mean angular direction. The inverse would happen when the coefficient is positive. Figure 2 conceptually illustrates how the coefficients affect the predictions. Regarding the second aspect we can state that, if a coefficient is not significant, then its contribution would not be relevant to explain the phenological observation. In our case we define that the coefficient is significant if the median of the
Figure 2. Interpretation of the coefficients in the circular regression. Consider a reference point (Black) generated with a circular-linear model with mean angular direction ($\mu = 0$), two coefficients ($\beta_1, \beta_2$) and two variables ($x_1, x_2$), where one of the coefficients is negative ($\beta_1$) and the other one is positive ($\beta_2$). When the coefficient is negative and the value of the parameter increases (blue) the result is an earlier observation compared with the reference point (The equivalent of -0.413 radians is 6.697 radians. It is shown below the equation). On the other hand, when the coefficient is positive and the variable increase (yellow) the observation is later.

The equation used is:

$$0 = 0 + 2 \tan(-0.3 \times 0.6 + 0.3 \times 0)$$

$$-0.413 = 0 + 2 \tan(-0.3 \times 1.3 + 0.3 \times 0)$$

$$6.697$$

$$0.413 = 0 + 2 \tan(-0.3 \times 0.6 + 0.3 \times 1.3)$$

The distribution of $p$-values is less than 0.05. Finally, we can estimate the accuracy of the prediction using the Jammalamadaka-Sarma (JS) correlation coefficient (Jammalamadaka and Sarma, 1988). As in any other regression framework, this approach helps us to quantify the effect of each climate variable on the inter-annual variability of DOY$_{GPP_{\text{max}}}$.

To estimate the relative sensitivity of DOY$_{GPP_{\text{max}}}$ to the leading principal component representing Tair, SWin, and VPD, as well to Precip we use the implementation of equation 4 in the R package “circular” (Agostinelli and Lund, 2017). To increase the robustness of the method we implemented a block bootstrapping per growing season generating a model parameter average based on 1000 iterations. In each analysis, we estimate the accuracy of the model using the JS correlation coefficient.
To assess the performance of linear versus circular regressions we perform an experiment with simulated data where we evaluate the accuracy and precision of both approaches to recover original regression coefficients in a circular setting (eq. 4). We add noise generated with a random von Mises distribution with parameters: \( n = 100 \) and \( \kappa = 30 \) to the model to ensure that the result follows a normal distribution. We predefined a range of values for two regression coefficients \( \beta_1 = \langle 0.01, \ldots, 3 \rangle, \beta_2 = \langle 0.01, \ldots, 3 \rangle \). We simulate the variables \( x_1 \) and \( x_2 \) as normal distributions with \( n = 100 \), a mean of 10, and 15 respectively, and standard deviations of 1 and 2. We evaluate all possible combinations for the regression coefficients 100 times simulating different \( x_1 \) and \( x_2 \). In each iteration we generate \( y \) using the set-up previously described, and we recover the original regression coefficients using \( y \) as response variable and \( x_1 \) and \( x_2 \) as predictors. Finally, We analyze two scenarios: 1) when the target timing occurs at the beginning of the year (\( \mu = 0 \)), and 2) when the target timing happens at mid-year (\( \mu = \pi \)).

The parameters for the entire set-up generate realistic data where the standard deviation of \( y \) is not higher than 0.3 radians. A standard deviation of 0.5 radians would be equivalent to having phenological observations across half a year which would not be realistic.

To quantify the accuracy of each model per coefficient we estimate the mean absolute error per model and coefficient (eq. 5). To compare the accuracy between models by coefficient we rest the mean absolute errors between models (eq. 6). To generate a single measure that allows to compare both coefficients and models we estimate the mean difference accuracy (eq. 7). The results can be understood as follows: if the difference is higher than 0, the circular model has a higher mean accuracy compared to the linear model and vice versa. To quantify which model has higher precision we estimate the difference between the standard deviation of the mean absolute errors per model for each coefficient (eq. 8). Finally, we estimate the mean differences of precision between the regression coefficients (eq. 9) where again if the value is higher than 0 circular model has a higher mean accuracy than linear model and the inverse sense if the value is lower than 0.

We estimate regression coefficients for the bootstrap sample \( i \in \{1, \ldots, m\} \), \( m = 100 \), for the regression coefficient \( \beta_j \), \( j \in \{1, 2\} \), and the model \( M \in \{l, c\} \) (denoted as \( \hat{\beta}_{M,i}^{j} \)). The model accuracy can then be estimated as the mean absolute error of the estimated regression parameter \( \hat{\beta}_j^M \), \( j \in \{1, 2\} \) for the linear model, \( M = l \), and the circular model, \( M = c \):

\[
a_{M,j} = \frac{1}{m} \sum_{i=1}^{m} |\hat{\beta}_{j,i}^{M} - \beta_j| \tag{5}
\]

The difference in accuracy for the coefficient \( j \) between the circular and the linear model is shown in

\[
\delta_{a,j} = a_{l,j} - a_{c,j} \tag{6}
\]

Finally, the mean difference accuracy between the linear and the circular model is given by

\[
\delta_{a} = \frac{\delta_{a,1} + \delta_{a,2}}{2} \tag{7}
\]
The difference in precision for the coefficient $j$ between the linear ($l$) and the circular model ($c$) is shown in

$$\delta_{p,j} = s_{l,j} - s_{c,j}$$

(8)

The mean difference precision between the linear and the circular model is given by

$$\delta_p = \frac{\delta_{p,1} + \delta_{p,2}}{2}$$

(9)

Where $s_{M,j}$ is the sample standard deviation of the vector $\left( \hat{\beta}_j^M \right)_i$, $M \in \{l, c\}$.

2.4 Analysis setup

The target variable DOY$_{GPP_{\text{max}}}$ is the day of the year when GPP reaches its maximum during the growing season. Given that different ecosystems present more than one growing season per year (e.g. semi-arid ecosystems) it is necessary to identify the number of growing seasons per year. To identify the number of growing seasons we apply a Fast Fourier Transformation (FFT) (Cooley and Tukey, 1965) to the mean seasonal cycle of the GPP time series. The number of growing seasons is equal to the maximum absolute value of the first four FFT coefficients (excluding the first one). For each FLUXNET site, we reconstruct the GPP time series taking the real numbers of the inverse FFT. We use these reconstructed time series to calculate the expected mean timing of DOY$_{GPP_{\text{max}}}$ and use this value as a template. To recover the real DOY$_{GPP_{\text{max}}}$ from the original time series we define a window around the template of length inversely proportional to the number of cycles (180 days / Number of growing seasons). To increase the robustness of the analysis we identify the days with the 10 highest GPP values. These days are used in the block bootstrapping mentioned above. Finally, since most of the sites are located in the Northern Hemisphere we expect that in most cases DOY$_{GPP_{\text{max}}}$ will be reached by middle of the calendar year.

To quantify the contribution of each climate variable, we count the number of sites per vegetation type where the regression coefficient is statistically significant. We perform a leave-one-out cross-validation per vegetation type to evaluate the predictive power of the circular regression using climate conditions. We only consider vegetation types with more than five sites. In this case the standardization of the climate variables is not applied. Finally, we use the mean of the optimum half-time parameter per vegetation type to weigh the climate conditions.

3 Results

Here, we first report results from simulated data to describe the performance of the circular regression approach compared to a linear model. Second, we compare the performance of circular and linear regression using empirical data. Third, we analyze the sensitivity of DOY$_{GPP_{\text{max}}}$ across vegetation types and climate classes. Finally, we show the results of the predictive power of circular regression per vegetation type.
3.1 Circular vs. Linear Regression

Figure 3 (a,c) shows that for $\mu = 0$ (DOY$_{GPP_{max}}$ at the beginning of the year) circular regression has a higher accuracy and precision compared to the linear regression for the entire space of regression coefficient values, with a maximum difference in the order of 0.1 in terms of accuracy, and the order of 1 for precision. For $\mu = \pi$ (DOY$_{GPP_{max}}$ mid-year) the linear model has a higher accuracy in most of the evaluated space with a maximum difference in the order of 0.001 compared with the circular regression. While, circular regression has a higher precision for most of the regression coefficients in the order of 0.001. These results show that circular regression has a higher precision to recover the original regression coefficients than linear regression no matter the moment of the year. On the other hand, circular regression has a higher accuracy than linear model at the beginning of the year. While at mid-year when linear is better the differences are in the order of 0.001.
Two correlation coefficients are used: Jammalamadaka-Sarna (JS) and Pearson product-moment (Pearson). In the circular plot the months and the day of the year (DOY) are also plotted every 75 days. The green arrow indicates the mean angular direction of the original data distribution.

To illustrate the method in practice, we compare the circular and linear models using data from two sites: US-Ha1 (Northern Hemisphere, deciduous broadleaf forest), and AU-How (Southern Hemisphere, woody savanna). We relate the climate variables with \( \text{DOY}_{\text{GPPmax}} \) (See methods) and reconstructed the \( \text{DOY}_{\text{GPPmax}} \) using the linear and circular regression models. We compare observed and predicted \( \text{DOY}_{\text{GPPmax}} \) using JS correlation for circular model and Pearson-Product Moment for linear model. For US-Ha1 both methods shows similar performance predicting \( \text{DOY}_{\text{GPPmax}} \) (Figure 4), while for AU-How, the circular model retrieves the original data better than the linear model explaining 30% more of the variance. In the case when the \( \text{DOY}_{\text{GPPmax}} \) is reached at the beginning of the year, linear methods produce a strong bias that predicts the timing across the entire year (Figure 4,b).
3.2 Sensitivity of DOY$_{\text{GPPmax}}$ to climate variables

From 52 sites analyzed in this study, only one site (ES-LJu) shows a bimodal growing seasons (see Supplement 1.2). As expected in most cases DOY$_{\text{GPPmax}}$ occurs at the middle of the calendar year (Figure S6), reflecting the uneven site distribution in FLUXNET (Schimel et al., 2015). However some ecosystems in the Northern Hemisphere do reach DOY$_{\text{GPPmax}}$ at the beginning of the year, these are Mediterranean sites such as, US-Var and ES-LJu. In general terms, most of the sites have a standard deviation between 10 [days] and 40 [days]. The maximal standard deviation is 46.9 [days] for AU-Tum site. A detailed table with the mean angular direction and standard deviation of DOY$_{\text{GPPmax}}$ of each site is presented in section S1.2.

For half of the sites, the JS correlation coefficients are between 0.70 and 0.97 (Supplement 1, Figure S5) showing that the inter-annual variability of DOY$_{\text{GPPmax}}$ is mainly explained by the cumulative effect of the climate variables. Nineteen sites have a JS coefficient less than 0.7 (DK-Sor, FI-Hyy, US-MMS, DK-ZaH, FR-Pue, US-UMB, AU-Tum, US-Ton, FR-LBr, US-Me2, IT-Lav, AT-Neu, DE-Gri, IT-MBo, IT-Ro2, US-Wkg, BR-Sa1, FR-Fon, CZ-wet). For ES-LJu the JS coefficient for the first growing season is 0.77 and 0.78 for the second one (Table S2).

Across all sites we find that air temperature, shortwave incoming radiation, and vapor pressure deficit appear as the dominant drivers worldwide in 43 sites (84 %, Supplement 3). Precipitation is the main driver for 5 sites (AU-How US-Ton ZA-Kru US-SRM US-Wkg, Supplement 3). Interestingly precipitation was the most important factor for all the woody savanna sites (Supplement 3). For three sites (DE-Gri, IT-Ro2, BRSa1) any climatic variable is significant. In terms of the sign of the coefficients, all the variables are predominantly negative (Table 1). This means that higher values of radiation, air temperature, VPD and precipitation lead to an earlier DOY$_{\text{GPPmax}}$. Individual sensitivities per site are shown in Supplement 3.

**Table 1.** Number of FLUXNET sites where each regression coefficient is statistically significant to explain the physio-phenology of GPPmax (DOY$_{\text{GPPmax}}$). The table is divided by the sign of the coefficient. The first column is coefficient for the dimensionality reduction between: Air temperature (Tair), Shortwave incoming radiation (SWin), and Vapor pressure deficit (VPD), the second column is the coefficient for Precipitation (Precip).

<table>
<thead>
<tr>
<th>Climatic variable</th>
<th>Sign</th>
<th>Tair, SWin, VPD</th>
<th>Precip</th>
</tr>
</thead>
<tbody>
<tr>
<td>(+)</td>
<td>8</td>
<td>2</td>
<td></td>
</tr>
<tr>
<td>(-)</td>
<td>38</td>
<td>14</td>
<td></td>
</tr>
</tbody>
</table>

The PCA between shortwave incoming radiation, air temperature and vapor pressure deficit has the highest frequency of significant correlation coefficients by number of sites for all the vegetation types with exception of Woody Savannas (WSA) where precipitation show to be more important for most sites than the dimensionality reduction between Tair, SWin, and VPD (Figure 5). For Closed Shrublands (CSH), and Savannas (SAV) both drivers have the same number of sites where the coefficients are statistically significant.

A special case to understand the sensitivity of DOY$_{\text{GPPmax}}$ to climate variables is the site: “Llano de los Juanes” an open shrubland ecosystem in Spain (ES-LJu). It is the only clearly bimodal ecosystem in our study (Figure 6). In this case precipita-
Figure 5. Contribution of each climate variable to explain the inter-annual variation of $\text{DOY}_{\text{GPPmax}}$ per vegetation type. CSH: Closed Shrublands ($n = 1$), DBF: Deciduous Broadleaf Forest ($n = 10$), EBF: Evergreen Broadleaf Forest ($n = 5$), ENF: Evergreen Needleleaf Forest ($n = 15$), GRA: Grassland ($n = 8$), MF: Mixed Forest ($n = 5$), OSH: Open Shrublands ($n = 1$), SAV: Savannas ($n = 1$), WET: Permanent wetlands ($n = 2$), WSA: Woody Savannas ($n = 3$). Each bar shows the cumulative number of sites where each climate variables are statistically significant.
Figure 6. DOY$_{GPP_{max}}$ sensitivity to different climate drivers in a Mediterranean ecosystem: "Llano de los Juanes", Spain (ES-Lju) with two growing seasons (green and orange). a) DOY$_{GPP_{max}}$ distribution across the year. The arrows indicate the mean angular direction of the growing season. b) regression coefficients for each growing season and c) the significance values for each variable. The red line in c) represents a p-value of 0.05.

The leave-one-site-out cross-validation for several vegetation types shows that the predictive power of the model for GRA and EBF is -0.3 and -0.31 respectively. For DBF is 0.46 and for ENF is 0.4. While for MF the predictive power of the model is 0.88, respectively (Figure 7).
Figure 7. Cross validation of the circular regression model to predict DOY_{GPPmax} for different vegetation types using air temperature, short-wave incoming radiation, precipitation and vapor pressure deficit (see methods). Deciduous Broadleaf Forest (DBF). Evergreen Broadleaf Forest (EBF). Grassland (GRA). Mixed Forest (MF), and Evergreen Needleleaf Forest (ENF). For each vegetation type the Jammalamadaka-Sarna (JS) correlation coefficient is shown in the title of each plot. The red line represents the perfect fit.
4 Discussion

4.1 Circular vs Linear regression

We explored whether circular regression is a suitable tool to analyze phenological events. Our results suggest that circular regressions can recover predefined coefficients in a set of simulations with higher accuracy and precision than linear regressions. Hence, we would generally suggest that circular regressions may be advantageous when the aim is analyzing the effect of climatic variables on phenological events. We did find, also cases where the classical linear regression may be either more robust or equally suitable e.g. when phenological events are reached close to the mid-year. In the overall view, however, we consider that circular regressions are to be preferred over linear regression for their conceptual capacity to analyze the physio-phenology of ecosystems regardless of the day of the year when an event of interest occurs. This allows us to analyzing phenological studies at global scale regardless of geographic location or the distribution of the observations during the year.

Different phenological models have been developed ranging from empirical approaches (Richardson et al., 2013) to process models (Asse et al., 2020) over the last decades. As we demonstrate here, circular statistics opens new opportunities to increase the robustness of phenological models allowing to analyze ecosystems across hemispheres within the same consistent framework. In fact, the results on phenological sensitivity of DOY$_{GPP_{max}}$ indicate the complexity of ecosystem responses to climate variability. Our approach is a motivation towards integrating circular regressions into more complex statistical techniques like regression trees, Gaussian process, or artificial neural networks, targeting a circular response variable.

4.2 Sensitivity of DOY$_{GPP_{max}}$ to climate variables

The geographical location of the FLUXNET 2015 sites represent an advantage to capture the DOY$_{GPP_{max}}$ variability at global scale (Supplement 1, Figure S6). Most of the analyzed sites (47) are located in the Northern Hemisphere. Two sites (GF-Guy and BR-Sa1) are located in the tropical region and, 3 sites (ZA-Kru, AU-How, AU-Tum) in the Southern Hemisphere. However, because of the low number of sites reported in the tropical and southern region with more than seven years of data, our understanding about the DOY$_{GPP_{max}}$ variability in these regions is still limited. Increasing the number of tropical and Southern Hemisphere sites should be considered a high-priority in the near future to complement our knowledge about the physio-phenological ecosystem state.

The high values of the JS correlation coefficients for most of the sites demonstrate that the inter-annual variability of DOY$_{GPP_{max}}$ can be explained as the cumulative effect of the climate variables during the growing season. Sites where it was not possible to explain the variations of DOY$_{GPP_{max}}$ with enough confidence level (JS correlation < 0.7) might require incorporating biotic variables (e.g. species composition (Peichl et al., 2018)) or soil properties information that can improve the predictive power of the model.

Our results suggest that there is no pattern between the DOY$_{GPP_{max}}$ sensitivity across vegetation type or climate classes (Sect. Figure S1.7). In other words, the DOY$_{GPP_{max}}$ sensitivity is site-specific, probably produced by the unique combination of biotic (e.g. species composition, species phenology, species interaction, and phenotypic plasticity) factors that are not evaluated in
our study. Several studies that focused on ecosystem phenology suggest that species composition play a fundamental role in ecosystem physio-phenology of the CO$_2$ uptake (Gonsamo et al., 2017; Peichl et al., 2018).

While there is no clear relationship between the DOY$_{GPPmax}$ sensitivity and the vegetation type, we find a predominant role of the combined effects of shortwave incoming radiation (SWin), air temperature (Tair) and vapor pressure deficit (VPD) at the global scale on the DOY$_{GPPmax}$ inter-annual variability, where for most of the sites these variables have a negative regression coefficient. This means, that if the SWin, Tair, and VPD increase during the growing season the DOY$_{GPPmax}$ will be reached earlier. This effect can be a consequence of DOY$_{GPPmax}$ being reached at the same time as SWin and Tair are maximum.

On a global scale our analysis shows that the combination of air temperature, short-wave incoming radiation and vapour pressure deficit has a negative sign as well as precipitation. This means that if these variables increase during the growing season, the GPPmax will be reached earlier. Our results are similar to those obtained by Wang and Wu (2019) were the authors conclude that an increase in the temperature produces an earlier DOY$_{GPPmax}$. This phenomenon is likely explained by the leaf-out advancing during spring. Nevertheless, there is still no consensus on whether the increase in temperature will produce an earlier end to the growing season. Several studies demonstrated for different vegetation types that when temperature increases, spring onset is earlier and autumn senescence is later (Christensen et al., 2007; Linkosalo et al., 2009; Migliavacca et al., 2012; Morin et al., 2010; Post and Forchhammer, 2008), increasing the length of the growing season and the amount of CO$_2$ that is uptake by ecosystems (Richardson et al., 2013).

Ecosystems with two growing seasons per year represent a very interesting case of the effect of climate drivers on DOY$_{GPPmax}$ across different growing seasons. In Llano de los Juanes, Spain (ES-LJu, Figure 6) DOY$_{GPPmax}$ is reached in the first growing season when the rainy season is finishing, while in the second growing season DOY$_{GPPmax}$ is reached in the middle of the rainy season (Data not shown). The effect of short-wave incoming radiation, temperature and vapor pressure deficit for both growing seasons is negative suggesting that if we increase these variables during the period before, the DOY$_{GPPmax}$ will happen earlier.

Phenology in Mediterranean ecosystems is mainly controlled by water availability (Kramer et al., 2000; Luo et al., 2018; Peñuelas et al., 2009). However, our results suggest that DOY$_{GPPmax}$ is mainly sensitive to SWin, Tair, and VPD. This result agrees with the analysis performed by Gordo and Sanz (2005) were the authors evaluated the phenological sensitivity of Mediterranean ecosystem to temperature and precipitation, and they concluded that temperature was the most important driver. Although water is a limiting factor in Mediterranean ecosystems, its influence on plant physiology and plant phenology can be completely different. In terms of physiology the GPPmax value can decrease but in terms of phenology DOY$_{GPPmax}$ can be still the same.

Complex interactions between climate variables and phenological response and the interspecificity of the sensitivity at site level explain in part the poor predictive power of the model for grasslands, Evergreen Broadleaf Forest, Evergreen Needleleaf Forest, and Deciduous Broadleaf Forests in the cross validation analysis (Figure 7). However, the predictive power for Mixed Forest is high, also when the distribution of the latitudinal gradient is not the same for all the sites. These results reflect that circular regression model can be extrapolated from different sites, to predict the DOY$_{GPPmax}$ inter-annual variability. This advantage could be a way to solve the common critic that phenological models can not be extrapolated generating only ad-hoc hypothesis (Richardson et al., 2013).
5 Conclusions

In this study we explore the potential of “circular regressions” to explain the physio-phenology of maximal CO$_2$ uptake rates. We conclude that 1) shortwave incoming radiation, temperature and vapor pressure deficit are the main drivers of the timing of maximal CO$_2$ uptake at global scale; precipitation only play a secondary role with the exception of woody savannas where the most important variable is precipitation. 2) Although the sensitivity of the DOY$_{GPP_{max}}$ to the climate drivers is site specific, it is possible to extrapolate the circular regression model for different sites with the same vegetation type and similar latitudes. Finally, we demonstrated using simulated and empirical data, that circular regression produces more accurate results than linear regression, in particular in cases when data needs to be explored across hemispheres.

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Appendix A: FLUXNET Sites

Table A1: FLUXNET sites used in our study. We report the name of the sites, time period used for the analysis, the climate class of each site following the Köppen-Geiger classification: Tropical monsoon climate (Am), Tropical savanna climate (Aw), Cold semi-arid climates (BSk), Humid subtropical climate (Cfa), Oceanic climate (Cfb), Hot-summer mediterranean climate (Csa), Warm-summer mediterranean climate (Csb), Humid subtropical climate (Cwa), humid continental climate (Dfb), Subarctic climate (Dfc, Dsc), and Tundra climate (ET). We also report the Vegetation type of the sites: Closed Shrublands (CSH), Deciduous Broadleaf Forests (DBF), Evergreen Broadleaf Forest (EBF), Evergreen Needleleaf Forests (ENF), Grasslands (GRA), Mixed Forests (MF), Open Shrublands (OSH), Savannas (SAV), Permanent Wetlands (WET), Woody Savannas (WSA).

<table>
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<tr>
<th>Site name</th>
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<th>Vegetation type</th>
<th>Period</th>
<th>N. years analyzed</th>
<th>Citation</th>
<th>Data DOI</th>
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Code availability. Code will be made available under GPL-3 license upon publication

Data availability. FLUXNET database is available in the web page: https://fluxnet.fluxdata.org/

Author contributions. DEPM, TM, MM, and MDM designed the study in collaboration with MR and CR. DEPM conducted the analysis and wrote the manuscript with substantial contributions from all co-authors

Competing interests. The authors declare that they have no conflict of interest