



# Quantifying climatic influences on tree-ring width

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## Abstract

Before tree-ring series can be used to quantify climatic influences on growth, ontogenetic and microenvironmental effects must be removed. Existing statistical detrending methods struggle to eliminate bias, caused by the fact that older/larger trees are nearly always more abundantly sampled during the most recent decades – which happens also to have seen the strongest environmental changes. Here we develop a new approach to derive a productivity index ( $P^*$ ) from tree-ring series. The critical stem diameter, when an initial rapid increase in stem radial growth gives way to a gradual decrease, is estimated using a theoretical approximation; previous growth rings are removed from analysis. The subsequent dynamics of stem radial growth are assumed to be determined by: tree diameter and height;  $P^*$  (gross primary production per unit leaf area, discounted by a “tax” due to the respiration and turnover of leaves and fine roots); and a quantity proportional to sapwood specific respiration ( $r_1$ ). The term  $r_1$  depends not only on the growth rate but also on tree height, because a given leaf area requires a greater volume of living sapwood to be maintained in taller trees. Height-diameter relationships were estimated from independent observations.  $P^*$  values were then estimated from tree ring-width measurements on multiple trees, using a non-linear mixed-effects model in which the random effect of individual tree identity accounts for the impact of local environmental variability, due to soil or hydrological conditions, and canopy position (i.e. shading and competition). Year-by-year  $P^*$  at a site should then represent the influence of year-by-year changes in environment, independently of the growth trend in individual trees. This approach was applied to tree-ring records from two genera (*Picea* and *Pinus*) at 492 sites across the Northern Hemisphere extratropics. Using a multiple linear mixed-effects regression with site as a random effect, it was found that estimated annual  $P^*$  values for both genera show consistent, temporally stable positive responses of  $P^*$  to total photosynthetically photon flux density during the growing season (PPFD<sub>5</sub>) and soil moisture availability (indexed by an estimate of the ratio of actual to potential evapotranspiration). The partial effect of mean temperature during the growing season (mGDD<sub>5</sub>) however was shown to follow a unimodal curve, being positive in climates with mGDD<sub>5</sub> < 9 to 11 °C, and negative in warmer climates.

**Keywords:** Tree-ring width, climate reconstruction, stem radial growth, ontogenetic trends, productivity index, mixed-effects model, climate controls on tree growth



## 44 1 Introduction

45 The attribution of recent climate changes to anthropogenic influences (Hegerl et al., 1996; Hegerl and  
46 Zwiers, 2011; Bindoff et al., 2013) requires knowledge of climate changes before the instrumental  
47 period. Annually resolved palaeorecords of temperature change have been constructed for the past  
48 2000 years (e.g. Mann et al., 2009; PAGES 2k Consortium, 2013; Anchukaitis et al., 2017). The most  
49 abundant source of information for such reconstructions comes from time series of tree-ring widths,  
50 because of their chronological accuracy, wide availability, and the sensitivity of tree growth to  
51 environmental factors. To use tree-ring data for palaeoclimate reconstruction, the raw data must be  
52 processed to remove ontogenic effects. In the absence of large environmental effects, radial growth  
53 shows an initial rapid increase but then passes a turning point and slows down gradually as the tree  
54 becomes larger and older. Removal of the ageing effect is called “detrending” in dendroclimatology.  
55 Various statistical methods have been developed for detrending (Cook, 1985; Fritts, 2012). Regional  
56 Curve Standardization (RCS; Briffa et al., 1996) has been widely recognized as a one of the best  
57 techniques for preserving trends due to longer-term environmental changes.

58 There remains however a fundamental, and worldwide, problem in the use of tree-ring data for climate  
59 reconstruction, namely the sampling bias of age distribution. The RCS method is not immune to this.  
60 Inevitably, field sampling focuses on long-lived trees in order to obtain as long a record as possible.  
61 Shorter-lived trees from earlier years have often disappeared by the time of sampling. Therefore there  
62 is a potential bias, such that growth rings from old, more slowly growing trees tend to be over-  
63 represented in the data for more recent years, while growth rings from younger, faster-growing trees  
64 tend to be over-represented in the data for earlier years. One potential consequence is that recent  
65 environmental trends in tree growth, which could be caused (for example) by the recent rapid increase  
66 in atmospheric [CO<sub>2</sub>] and/or global temperature increases, may be removed as an accidental by-  
67 product of detrending. The extent to which environmental effects are thereby missed in tree-ring  
68 reconstructions is controversial. For example, using the traditional method of constructing a ring  
69 width index (RWI), trees from the tropics apparently showed no effect of rising [CO<sub>2</sub>] since the 1950s  
70 despite consistently increasing water use efficiency, as shown by stable carbon isotopes (van der  
71 Sleen et al., 2015). However, Brien et al. (2017) suggested that non-uniform recruitment effects on  
72 sampling could explain this “missing” CO<sub>2</sub> signal. They used a statistical correction accounting for  
73 biases in age at sampling, after which the [CO<sub>2</sub>] signal was significantly positive for both canopy and  
74 understory trees (Brien et al., 2017).

75 There have been a number of suggestions of ways to deal with the problem of temporal bias, including  
76 using fossil trees in the detrending (e.g. Briffa et al., 1996) and (most obviously) more systematic  
77 sampling of both older and younger trees living today. Recognition of the potential bias (Briffa and  
78 Melvin, 2011) has led to several extensions of the RCS detrending method (e.g. cohort RCS: Esper  
79 et al., 2002; adaptive regional growth curves; Nicault et al., 2010; signal-free detrending: Melvin and  
80 Briffa, 2008). However, we argue that even if trees were sampled more systematically, there would  
81 still be sampling bias in the early record, because there is no way to resurrect old trees that are no  
82 longer available for sampling. Moreover, we require a reliable method to process the large volume of  
83 tree-ring data that are already available ([https://www.ncdc.noaa.gov/data-access/paleoclimatology-  
84 data/datasets/tree-ring](https://www.ncdc.noaa.gov/data-access/paleoclimatology-data/datasets/tree-ring)) as a source for climate reconstructions. For example, records covering the  
85 whole period of 1940–2000 for species of *Picea* and *Pinus* from the International Tree Ring Data  
86 Base are widely distributed across the northern extratropics (Fig. 1, left-hand panels). The right-hand  
87 panels of Fig. 1 show age distributions for some example sites. For 184 out of 188 *Picea* sites, the  
88 age of tree rings dated to the years 1970–2000 is greater than that for the years 1940–1969. There is a



difference of 26.4 years on average between the median ages of tree rings dated to the two periods. For *Pinus*, 285 out of 304 sites showed the same phenomenon, with an average difference of 24.4 years (See Supplementary Information).

In this paper, we present a new approach to remove ontogenetic effects. Our approach makes use of a limited amount of readily available independent information, and simple equations for the geometry of tree growth, to infer values of an environmentally influenced productivity index ( $P^*$ ). The use of independent height and diameter data provides a useful biological constraint on the ontogenetic growth trend. The inferred trend is related to size rather than age, reflecting the ergodic nature of tree growth: that is, radial growth depends on tree size rather than directly on age, so – all else equal – trees that start growing more rapidly also show a faster growth decline with age (Hättenschwiler et al., 1997). In addition, we use the power of mixed-effects statistical modelling to separate random effects on individual trees at a site from environmental (fixed) effects, which are presumed to influence the growth of all of the trees at a site.

## 2 Background

### 2.1 A simple diagnostic model for tree growth

We derive a simple, generic model for tree growth in three steps as follows.

1. The annual increment of stem mass ( $dW_s/dt$ ) is assumed to equal carbon export from the canopy ( $X$ ), corrected for growth respiration, minus additional deductions. These are due to foliage turnover and fine-root respiration and turnover, which are proportional to leaf area, and stem respiration, which is proportional to sapwood volume and therefore – according to the pipe model (Shinozaki et al., 1964) – to the product of leaf area and mean foliage height ( $H_f$ ).  $H_f$  is assumed to be  $H/2$  (where  $H$  is tree height) initially, but must increase as the canopy rises. An expression for  $H_f$  can be derived from tree geometry as  $H_f = H(1 - H/2aD)$ , where  $D$  is tree diameter, and  $a$  is the initial slope of the height-diameter relationship (Appendix A). Thus, we can write:

$$dW_s/dt = y A_c (X - qL) [1 - r_1 H (1 - H/2aD)] \quad (1)$$

where  $y$  is the correction factor for growth respiration,  $A_c$  is crown area,  $X$  is carbon export from the canopy,  $q$  is a parameter related to foliage turnover and fine-root respiration and turnover,  $L$  is the leaf area index within the crown, and  $r_1$  is a parameter related to the sapwood respiration rate. Note the assumption here that the absolute respiration rate of sapwood varies in proportion to carbon availability. This is inescapably true, at least to some approximation, as there is neither carbon available nor a physiological need for suppressed trees to respire as much as dominant trees, or for trees in poor growth years to respire as much as the same trees in good growth years.

2. The mass of a parabolic stem is related to its dimensions by  $W_s = (\pi/8) \rho_s D^2 H$ , where  $\rho_s$  is wood density. Hence the increase of stem mass with diameter is  $dW_s/dD = (\pi/8) \rho_s D(2H + DdH/dD)$ . If the height-diameter relationship follows a Mitscherlich curve (Mitscherlich, 1928) then  $dH/dD = a(1 - H/H_m)$  where  $H_m$  is the maximum height (Appendix B). We further assume  $A_c = (\pi c/4a) DH$ , where  $c$  is a constant related to the Huber value (i.e. the ratio of sapwood area to foliage area: Appendix A). Therefore,  $dW_s/dD = (\pi/8) \rho_s DH [2 + aD(1/H - 1/H_m)]$  and, applying the chain rule:

$$dW_s/dt = A_c (dD/dt) (a/c) \rho_s [1 + (aD/2)(1/H - 1/H_m)] \quad (2)$$



133 3. Equating (1) and (2) and solving for  $dD/dt$  yields:

$$134 \quad dD/dt = P^* [1 - r_1 H (1 - H/2aD)] / [1 + (aD/2)(1/H - 1/H_m)] \quad (3)$$

135

136 where  $P^* = (X - qL) (yc/\rho_s)$ .

137

138 The parameters  $a$  and  $H_m$  will be estimated from independent observations. Then  $r_1$  and  $P^*$  will be  
139 estimated from all the tree-ring data for a given species and site. We will assume that  $r_1$  depends only  
140 on the species and site, while year-to-year variations in productivity for any given tree will be  
141 reflected in  $X$  and therefore also in  $P^*$ . We will also assume that there is a random effect on  $P^*$ ,  
142 corresponding to differences (genetic, or due to canopy position or microsite variation) among  
143 individual trees.

144

145 An assumption implicit in the derivation of equation (2) above is that the trees have escaped the  
146 initial, relatively short period of rapidly increasing diameter increment that is commonly observed.  
147 Appendix C details the approximation we have used to estimate the ontogenetic turning point  
148 corresponding to peak radial growth. Earlier rings are discarded.

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### 151 3 Data and methods

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#### 153 3.1. Tree-ring and climate data

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155 We use data from the two most widespread evergreen needleleaf tree genera in the northern  
156 extratropics, *Picea* and *Pinus*, from the International Tree Ring Data Base (ITRDB,  
157 <https://www.ncdc.noaa.gov/data-access/paleoclimatology-data/datasets/tree-ring>). All raw tree-ring  
158 width data covering 1940-2000 CE were included in the analysis.

159

160 Gridded climate data for each site – 3-hourly air temperature ( $t_{as}$ ) and precipitation, downward short-  
161 wave radiation (SWD), specific humidity and air pressure – were obtained from the WFDEI data at  
162  $0.5^\circ$  resolution (Weedon et al., 2014). These data were further used for the calculation of annual total  
163 photosynthetic photon flux density during the period with daily mean  $t_{as} > 5^\circ\text{C}$  (PPFD<sub>5</sub>) and mean  
164 growing-season temperature during the period with daily mean  $t_{as} > 5^\circ\text{C}$  (mGDD<sub>5</sub>). Monthly gridded  
165 air temperature, precipitation, and cloud cover from CRU TS 3.23 (Harris et al., 2014) were used for  
166 the calculation of the annual ratio of potential to actual evapotranspiration ( $\alpha$ ) via the Simple Process-  
167 Led Algorithms for Simulating Habitats (SPLASH) model (Davis et al. 2017). Note that PPFD<sub>5</sub>  
168 includes the effect of changes in growing season length as well as any change in average PPFD.  
169 Annual values of all climate variables were calculated for the “effective carbon accumulation year”,  
170 conventionally defined as the period from 1 July in the year prior to ring formation to 30 June in the  
171 year of ring formation.

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#### 173 3.2 Estimating $a$ and $H_m$

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175 Values of  $a$  and  $H_m$  could in principle be estimated from local (site-level) field observations of the  
176 diameters and heights of individual trees, across the full size range. However, it was not possible to  
177 obtain local sets of paired observations of  $D$  and  $H$  for all the ITRDB sampling sites. Instead, we  
178 estimated generic  $a$  and  $H_m$  ( $H_{m(ICP)}$ ) values for *Picea* and *Pinus* using the available paired  $D$  and  $H$



measurements of each genus in the data set created by the Integrated Co-operative Programme on Assessment and Monitoring of Air Pollution Effects on Forests (ICP Forests, <http://icp-forests.net/>). We used 53,576 paired  $D$  and  $H$  measurements from 340 plots for *Pinus*, and 55,327 paired measurements from 353 plots for *Picea* (Figure 2a, 2b). Maximum tree height tends to be fairly stable within tree genera and species, but sites with especially low productivity (usually in extremely dry and/or cold regions) may have deviating height-diameter curves, with low  $H_m$ . We therefore applied a constraint for  $H_m$  in such regions (Figure 2c). We performed a 99% quantile regression between the satellite-derived observed maximum vegetation height (Simard et al., 2011) and the modelled long-term mean GPP for 1982-2011 (Thomas, 2018), yielding an alternative estimate of maximum height,  $H_{m(sat)}$ . For any given site, we assigned the lower of  $H_{m(ICP)}$  and  $H_{m(sat)}$  as the value of  $H_m$ . Only two out of 269 *Picea* sites ( $< 1\%$ ) were affected by the  $H_{m(sat)}$  constraint, but 83 out of the 151 *Pinus* sites (55%) were affected. We tested the impact of uncertainties in the estimation of  $H_m$  and  $a$  on both individual and site-level estimation of  $P^*$  by running sensitivity tests using a large ( $\pm 50\%$ ) perturbation of both parameters.

### 3.3 Estimation of $P^*$

We fitted a non-linear mixed-effects (NLME) model, based on equation (1), in two steps. The response variable is the (post-peak) annual diameter increments (ring widths  $\times 2$ ) for all trees. In the first step, the parameters to be estimated at each site are the fixed effect of  $P^*$  (site-level mean productivity index during the whole period, a single value for a species and site),  $r_1$  (also constant for a species and site) and random effects corresponding to different  $P^*$  values for individual trees. The contribution (weights) of trees' individual  $P^*$  values to the site mean  $P^*$  value, which accounts for micro-environmental differences on the GPP of individual trees, and the site-level estimate of  $r_1$ , are then used in the second step (a linear regression model) in order to estimate  $P^*$  for each year.

### 3.4 Ring-width index calculation

We also compared reconstructed  $P^*$  values with the standard calculation of the mean raw ring width index (RWI-mean). Raw ring widths were first standardized as the ratio of ring width to the mean ring width of each tree. The year-by-year values of RWI-mean at a site are then calculated as the robust biweight mean of the standardised values of individual trees at that site (Cook and Kairiukstis 1990).

### 3.5 Analysis of the bioclimatic controls on $P^*$

$P^*$  is designed to reflect climate impacts on radial tree growth by removing the effects of sampling biases, ontogeny and within-site variability. Individual bioclimatic parameters should therefore have a consistent impact on growth, independent of sampling period or of genus considered. We used a linear mixed-effects model to analyse the response of  $P^*$  to the bioclimate variables mGDD<sub>5</sub>, PPFD<sub>5</sub>, and  $\alpha$  for both *Pinus* and *Picea* during two intervals 1940-1969 and 1970-2000 CE. Site ID was included as a random intercept. As the influence of  $\alpha$  is strongly non-linear (Wang et al., 2017),  $\alpha$  was transformed to natural logarithms before analysis.

During exploratory analysis, we discovered a strong interaction between the effect of mGDD<sub>5</sub> variability on  $P^*$  and the local mean value of mGDD<sub>5</sub>. That is, the impact of warming on tree growth was positive at low average temperatures, but negative at higher average temperatures. In subsequent



analyses we therefore hypothesized that the effect of mGDD<sub>5</sub> on  $P^*$  should follow a quadratic (unimodal) curve, which can be expressed as:

$$f(T) = \beta_0 + \beta_1 \text{mGDD}_5 + \beta_2 \text{mGDD}_5^2$$

where  $\beta_1$  is positive and  $\beta_2$  negative. The turning point (maximum) of the unimodal response curve occurs when  $f(T) = -\beta_1 / 2\beta_2$ . The uncertainty (standard error) of this derived value is estimated using the variance-covariance matrix for mGDD<sub>5</sub> and mGDD<sub>5</sub><sup>2</sup> from the regression, as follows:

$$\text{standard error of } -\frac{\beta_1}{2\beta_2} = \sqrt{\frac{1}{4} \times \frac{\beta_1^2}{\beta_2^2} \times \left( \frac{\text{Var}(b)}{\beta_2^2} + \frac{\text{Var}(\beta_1)}{\beta_1^2} - 2 \times \frac{\text{Cov}(\beta_1, \beta_2)}{\beta_1 \times \beta_2} \right)}$$

We ran a further analysis to test whether the impact of recent changes in [CO<sub>2</sub>] were discernable in the  $P^*$  reconstructions, by including [CO<sub>2</sub>] in addition to the bioclimatic variables (mGDD<sub>5</sub>, PPFD<sub>5</sub>, and  $\alpha$ ) in the linear mixed-effects model. We considered the two intervals 1940-1069 and 1970-2000 CE separately. The change in [CO<sub>2</sub>] over the first interval was *ca* 13 ppm, and over the second interval *ca* 44 ppm.

## 4 Results

### 4.1 Comparison of $P^*$ and non-detrended ring widths

The reconstructed time series of  $P^*$  at individual sites are comparable to raw ring widths over much of the record. Differences between  $P^*$  and raw ring widths tend to be largest around the beginning and end of each time series (Figure 3; Supplementary Information). Almost all  $P^*$  values are higher than the RWI-mean (89% *Pinus*, 83% *Picea*) in the most recent 30 years, and lower (85% *Pinus*, 77% *Picea*) in the earliest years. The difference between  $P^*$  and RWI-mean is most marked at sites which show the largest sampling biases (e.g. CANA315, CO591, GERM189, TURK036) and least where the sampling of large trees is not confined to the recent past (e.g. MOG039) or where the most recent samples include some smaller trees (e.g. AK113). This comparison suggests that the calculation of  $P^*$  has effectively reduced the effects of sampling biases as well as accounting for ontogeny.

### 4.2 Sensitivity of inferred $P^*$ to the imputed values of $H_m$ and $a$

Year-by-year  $P^*$  estimates are not highly sensitive to the selection of  $H_m$  and  $a$ . Despite the large range (50%) of  $H_m$  and  $a$  values considered (Figure 4), their impact of the final year-by-year variation of  $P^*$  was small. The correlation between alternative reconstructions is always > 0.98.

### 4.3 Sensitivity of inferred $P^*$ to the estimated peak-growth year

Although a number of parameters are required to estimate the peak-growth year (Appendix C), most of these are well constrained by observations (see Supplementary Information). The largest uncertainties are associated with estimates of sapwood-specific respiration rate ( $r_s$ ) and the ratio of fine-root mass to foliage area ( $\zeta$ ). Using a range of estimates for these parameters has a minor effect on the identification of the peak-growth year, with minimum/maximum estimates indicating that peak growth occurs when the diameter of the tree is between 2 and 11 cm for *Pinus* and between 5 and 12 cm for *Picea*. Differences caused by using our theoretical approximation, versus the simple





assumption that the first maximum in ring width corresponds to peak radial growth has little impact on  $P^*$  at most sites. The correlation between  $P^*$  calculated using these two approaches to estimate the peak at site TURK036, for example, is 0.97 (Figure 5; Supplementary Information). However, the theoretical approximation makes it possible to calculate  $P^*$  at sites where identification of peak growth is problematic because the ontogenetic signal is conflated with that of environmental variability.

#### 4.4 Inclusion of within-site variability on $P^*$

The use of a mixed-effects model, including a random effect on productivity (random tree-to-tree  $P^*$ ), is the key to addressing the existence of cohorts of trees differing in productivity. The left-hand panels of Figure 5 also show that the simulated growth trends differ among individuals. The differences are shown for both the level of  $P^*$  (initial productivity or growth rate), and the slope (a combined effect of the growth rate and size-related tree geometry). These differences probably largely reflect microenvironmental differences (including shading and soil depth variations) that are expected to be more stable over time than climate effects during the life of an individual tree, except for occasional gap-creation events. Therefore, the tree-to-tree random  $P^*$  effects are carried over to the second-step linear regression for each specific year's site-level  $P^*$ . This approach ensures that both old and young trees have a similar influence on the final year-by-year time series of  $P^*$  (in contrast to conventional approaches that operate on the mean ring width).

#### 4.5 Global patterns of bioclimatic controls on $P^*$

Consistent and significant patterns of bioclimate control on  $P^*$  are shown for both genera, for different periods, over the whole northern hemisphere (Table 1, Figure 6). Value of the slopes and their ranges are stable within each genus among different periods (Table 1). Overall,  $P^*$  shows a significant positive response  $\alpha$  (all  $p$ -values  $< 0.001$ ), and a significant negative response to mGDD<sub>5</sub> (all  $p$ -values  $< 0.005$ ). The response to PPFD<sub>5</sub> is also positive, and significant in three out of four of the cases. The linear and quadratic terms of the response to temperature (mGDD<sub>5</sub>) are both consistently significant, with all  $p$ -values  $< 0.001$ . The consistency of the response through time, and between genera, demonstrates that  $P^*$  provides a robust estimate of year-to-year climate impacts on radial growth and preserves the signal of long-term climate trends.

The consistently significant positive slopes for mGDD<sub>5</sub> and negative slopes for mGDD<sub>5</sub><sup>2</sup> demonstrate the nonlinear impact of temperature on tree growth (Table 1, Figure 6). In cold climates, higher temperatures in one year lead to increased radial growth but in temperate climates higher temperatures have a detrimental effect on radial growth. The turning point is fairly consistent for genus and period, being between 7 and 11°C for *Pinus* and 8 and 10°C for *Picea*. This consistency again supports the idea that  $P^*$  provides a robust estimate of the climate controls on tree radial growth. However, the non-linear nature of this relationship challenges the conventional assumption of a monotonic relationship that underpins most tree-ring based temperature reconstructions.

The impact of [CO<sub>2</sub>] on  $P^*$  is equivocal (Figure 7, Table 2). There is a significant positive impact during both intervals on *Picea*. There is positive (but not significant) impact on *Pinus* in the interval 1940-1969 CE but a significant negative trend during the interval 1970-2000 CE. All the effects are very small compared to those of climate, and the bioclimatic relationships are stable compared to the model without [CO<sub>2</sub>].



## 304 5 Discussion

305 The method described here removes ontogenetic effects from tree-ring records effectively and also  
306 accounts for microenvironmental differences (including e.g. shading and variability soil depth) on  
307 the productivity of individual trees. Its application is straightforward and requires only a modest  
308 amount of information external to the tree-ring records themselves. The key parameters, maximum  
309 tree height and the initial ratio of height to diameter, could be obtained for individual sites but can  
310 also be derived from regional forestry data. We have shown that the reconstructed  $P^*$  is rather  
311 insensitive to uncertainties in the values used for these externally derived parameters, and to  
312 uncertainties in the estimation of the timing of peak radial growth.

313  
314 However,  $P^*$  does not solve the problem of making reconstructions of individual climate variables.  
315 The climatic control analysis indicates that several bioclimate variables simultaneously influence tree  
316 growth. Classically, reconstructions of past climates based on tree-ring series have focused on sites  
317 showing strong correlations with one particular climate variable. Our results suggest that this criterion  
318 can be, at best, only approximately fulfilled. Most importantly, even if the sensitivity of tree growth  
319 to one climate variable is strong in a certain range of that variable, that range is expected to be narrow.  
320 To take the case of temperature, the response is positive at lower growing-season mean temperatures  
321 but at higher temperatures it becomes flat, and then negative. The multifactorial (and potentially non-  
322 monotonic) nature of tree growth responses to climate is one of the proposed explanations for the  
323 “divergence problem” (D’Arrigo et al., 2008). This interpretation is supported by our results.

324 The  $\text{CO}_2$  effect on tree growth remains enigmatic. A number of studies (Graumlich, 1991; Graybill  
325 and Idso, 1993; Gedalof and Berg, 2010; van der Sleen et al., 2015) have inferred that increasing  
326  $[\text{CO}_2]$  has no impact on stem growth. Our method could, in principle, allow the detection of a  $\text{CO}_2$   
327 effect if present. We looked for such an effect (by including  $[\text{CO}_2]$  as an additional predictor in the  
328 climate response model), but no consistent response emerged. The apparent lack of a  $\text{CO}_2$  effect in  
329 tree-ring records is puzzling, given that several Free Air Carbon dioxide Enrichment (FACE)  
330 experiments have shown  $\text{CO}_2$ -induced enhancement of tree growth (e.g. Oak Ridge FACE: Norby et  
331 al., 2002; DUKEFACE: McCarthy et al., 2010; Swiss FACE: Handa et al., 2006; EUROFACE:  
332 Calfapietra et al., 2003; Arizona FACE: Idso and Kimball, 1993). One possible explanation is  
333 confounding with other variables in the regression model (the fact that  $\text{CO}_2$  has increased steadily  
334 means this is a real possibility when any other variable shows a unidirectional trend). This seems  
335 unlikely, however, given the stability of the bioclimatic relationships between the model with and  
336 without  $\text{CO}_2$  included. Another explanation could be the counteracting effects of other environmental  
337 changes not considered, such as soil acidification. It is also possible that the  $\text{CO}_2$  effect on stem  
338 growth is small because of increased carbon allocation below ground, as might be expected under  
339 nutrient-limited conditions in response to a  $\text{CO}_2$ -induced increase in nutrient demand. Increased  
340 below-ground allocation in response to increased  $\text{CO}_2$  has indeed been observed both in laboratory  
341 experiments (Rogers et al., 1994; Prior et al., 2011) and in several of the FACE experiments (Oak  
342 Ridge FACE: Norby et al., 2004; DUKEFACE: DeLucia et al., 1999; Pritchard et al., 2008;  
343 Rhinelander ASPEN-FACE: King et al., 2001; EUROFACE: Calfapietra et al., 2003; Lukac et al.,  
344 2003; Bangor FACE: Smith et al., 2013).

345 The question of how best to use tree-ring data to reconstruct past climates remains open. One  
346 possibility would be to refrain from reconstructing single climate variables, and instead use  $P^*$  as an  
347 index to compare with net primary production as simulated by ecosystem and Earth System Models  
348 for past climates. Another approach, echoing Fritts (2012), might involve the simultaneous use of





multiple  $P^*$  reconstructions across a region to infer past changes in climate variability modes. The detailed methods for such an analysis remain to be developed.

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## 487 Appendix A

488 We assume that crown area ( $A_c$ ) is related to diameter and height by  $A_c = (\pi c/4a) DH$  where  $D$  is  
 489 diameter,  $H$  is height,  $a$  is the initial rate of increase of height with diameter, and  $c$  is a constant. If  $H$   
 490 follows a “diminishing return” relationship with  $D$ , as is always observed, this formulation ensures  
 491 that the allometric coefficient of  $A_c$  lies between 1 and 2. For small trees (with  $H \approx aD$ ), which lack  
 492 heartwood, the Huber value (ratio of sapwood area to foliage area) is then equal to  $1/Lc$  where  $L$  is  
 493 the leaf area index within the crown (Li *et al.*, 2014). As the tree grows, however, height growth  
 494 slows relative to diameter growth, and the tree’s basal diameter becomes progressively greater than  
 495 is needed to supply the leaves. For a tree of any size, we estimate the current height of the crown base  
 496 ( $z^*$ ) as the height ( $z$ ) at which the ratio of stem area,  $A_s(z)$  to foliage area,  $A_f = L A_c = L (\pi c/4a) DH$   
 497 is equal to the Huber value. Using the unique property of paraboloid stems:

$$498 \quad A_s(z) = A_s(0) (1 - z/H) = (\pi/4) D^2 (1 - z/H) \quad (A1)$$

499 we obtain the solution:

$$500 \quad z^* = H (1 - H/aD). \quad (A2)$$

501 We assume that the mean foliage height  $H_f$  is the midpoint of  $z^*$  and  $H$ :

$$502 \quad H_f = H (1 - H/2aD). \quad (A3)$$

503

## 504 Appendix B

505 The Mitscherlich curve (Mitscherlich, 1928) is a well-established “diminishing return” relationship,  
 506 used in the forestry literature since the early 20<sup>th</sup> century. Applied to tree dimensions, its equation is:

$$507 \quad H = H_m [1 - \exp(-aD/H_m)] \quad (B1)$$

508 where  $H_m$  is the maximum height. This equation has the realistic properties (a) that the tangent at  $D$   
 509  $= 0$  is equal to the constant  $a$ , i.e. the relationship at first is approximately linear with slope  $a$ ; (b) the  
 510 rate of increase of  $H$  with  $D$  declines linearly with  $H$ , so that  $dH/dD = a(1 - H/H_m)$ ; and (c)  $H$   
 511 asymptotically approaches  $H_m$  as  $D \rightarrow \infty$ . Allometric equations, in contrast, have none of these  
 512 properties.

513

## 514 Appendix C

515

516 The equation of the T tree-growth model (Li *et al.*, 2014) is as follows:

$$517 \quad dD/dt = \{y [P - \rho_s(1 - H/2aD)Hr_s/c] - L [1/\sigma\tau_r + \zeta(yr_r + 1/\tau_r)]\} / \{(a/2c) \rho_s [aD(1/H - 1/H_m) + 2] +$$

$$518 \quad (L/D) [aD(1/H - 1/H_m) + 1](1/\sigma + \zeta)\} \quad (C1)$$

519

520 The numerator is the total biomass production (per unit crown area), and the denominator is the  
 521 biomass increment (per unit crown area) that is needed to generate a unit of diameter increment.  $P$  is  
 522 gross primary production (GPP,  $\text{kgC m}^{-2}$ ), net of foliage respiration;  $H$  (m) is tree height;  $D$  (m) is  
 523 stem diameter (with  $H$  and  $D$  linked by equation (2));  $y$  is the “yield factor” accounting for growth  
 524 respiration;  $L$  is the leaf area index within the crown;  $\rho_s$  is sapwood density ( $\text{kgC m}^{-3}$ );  $r_s$  is sapwood-



specific respiration rate ( $\text{year}^{-1}$ );  $c$  is the initial ratio of crown area to stem cross-sectional area;  $\sigma$  is specific leaf area ( $\text{m}^2 \text{kg}^{-1} \text{C}$ );  $\tau_f$  is foliage turnover time (years);  $\zeta$  is ratio of fine-root mass to foliage area ( $\text{kgC m}^{-2}$ );  $r_r$  is the fine-root specific respiration rate ( $\text{year}^{-1}$ ); and  $\tau_r$  is the fine-root turnover time (years).

To simplify equation (A1) we first note that the second term of the denominator quickly vanishes. This term is responsible for the fact that peak diameter increment does not occur in year 1, but a few years later. The division by  $D$  however means that this term is important only near the start of growth than it is later on.

The numerator describes two kinds of “tax” on GPP. The term including  $L$  is a fixed rate (per unit crown area) and corresponds to the allocation of GPP to foliage and fine-root turnover, and to root respiration. The term including  $r_s$  is initially small, but increases in proportion to height. These terms affect tree growth differently. The term including  $L$  represents a constant drain on GPP, while the term including  $r_s$  determines a size-related decline of biomass production.

The first term of the denominator is related to the wood density and the tree geometry. Because of the flattening out of height growth, it initially takes the value  $(3/2)(a/c)\rho_s$  but it declines somewhat, eventually approaching the value  $(a/c)\rho_s$ .

If we disregard the second term of the denominator, it can be seen that root-related parameters ( $\zeta$ ,  $r_r$  and  $\tau_r$ ) all appear together, thus the number of parameters to be estimated is reduced by two. We can therefore write  $Z = \zeta(yr_r + 1/\tau_r)$ .

During early growth we can assume  $H \ll H_m$ , and therefore make the approximation  $H \approx aD$ . Equation (A1) then simplifies to:

$$dD/dt = \{y[P - (\rho_s r_s a/2c)D] - L_0\} / \{3ap_s/2c + 2Lm_A/D\} \quad (\text{C2})$$

where  $L_0 = L[1/\sigma\tau_f + \zeta(yr_r + 1/\tau_r)]$ , the total annual cost of making and maintaining leaves and fine roots; and  $m_A = (1/\sigma + \zeta)$ , the leaf-plus-fine root mass per unit leaf area.

At the turning point, denoting the numerator of equation (A2) by  $A$  and the denominator by  $B$ , we have:

$$B \, dA/dD = A \, dB/dD \quad (\text{C3})$$

where

$$dA/dD = -y\rho_s r_s a/2c \quad (\text{C4})$$

and

$$dB/dD = -(2L/D^2)m_A \quad (\text{C5})$$

By solving the resulting quadratic equation for  $D$ , it can be shown that the turning point occurs when:

$$D = (4/3)(c/ap_s)Lm_A \{ \sqrt{[1 + (3/2)(yP - L_0)/(yr_s Lm_A)]} - 1 \} \quad (\text{C6})$$

This can be rewritten as:



$$D = (4c/3a\rho_s) Lm_A[\sqrt{(1+P_x/u)}-1] \quad (C7)$$

where  $P_x = yP - L_0$  and  $u = 2yr_s/3Lm_A$ . Substituting this value into equation (C7) gives:

$$dD/dt = (2c/3a\rho_s) \{P_x - u[\sqrt{(1+P_x/u)} - 1]\} / \{1 + 1/[\sqrt{(1+P_x/u)} - 1]\} \quad (C8)$$

Simplifying this further, define  $Q = \sqrt{(1+P_x/u)} - 1$ , hence

$$P_x/u = (Q + 1)^2 - 1 = Q(Q + 2) \quad (C9)$$

We can now derive the location of the turning point, which occurs when:

$$D^2/(dD/dt) = 4cLm_A/(a\rho_syr_s) \quad (C10)$$

Thus, given an estimate of the maximum diameter growth rate, we can estimate the critical diameter given suitable values of the parameters  $c$ ,  $a$ ,  $\rho_s$ ,  $L$ ,  $m_A$ ,  $y$  and  $r_s$ .

Note that the ratio of the maximum diameter growth rate to the area at which that growth rate is achieved does *not* depend on the absolute value of the initial biomass growth rate ( $P_x$ ). For high  $P_x$ , this point will simply be reached sooner than for low  $P_x$ . However this ratio is greater for trees that maintain greater initial crown area per unit basal area ( $c$ ) and trees that maintain greater leaf and fine root mass ( $Lm_A$ ). It is less for trees that invest more in height growth (having high initial height-diameter ratio  $a$ ), have denser wood ( $\rho_s$ ), and have intrinsically higher sapwood respiration rates ( $r_s$ ). Although these parameters are not known with precision, the change of the ratio of  $D^2/(dD/dt)$  due to variations in the parameter values is small. The quantity  $D^2/(dD/dt)$  ranges from 0.097 to 2.59 at peak radial growth of *Pinus*, corresponding to a diameter  $D$  of between 2 to 11 cm when the maximum stem growth  $dD/dt$  is 5mm. The value of  $D^2/(dD/dt)$  used in our theoretical approximation is 0.97. Similarly,  $D^2/(dD/dt)$  ranges from 0.49 to 3.11 at peak radial growth of *Picea*, corresponding to a diameter  $D$  of between 5 to 12 cm when the maximum stem growth  $dD/dt$  is 5mm. The value of  $D^2/(dD/dt)$  used in our theoretical approximation is 1.31.





## Figure and Table Captions

Figure 1. (a) Distribution of northern hemisphere *Pinus* and *Picea* tree-ring records covering period 1940-2000 (b) sampling age distribution through time for 3 *Picea* and 3 *Pinus* example sites, showing age sampling biases. These six sites are identified on the map with letters (a-f).

Figure 2. Estimation of asymptotic maximum height ( $H_m$ ) and the initial slope of height to diameter (a). Panel (a) and (b) are the estimations for asymptotic maximum height ( $H_m$ ) and the initial slope of height to diameter (a) using all the measurements for *Picea* and *Pinus* from the Integrated Co-operative Programme on Assessment and Monitoring of Air Pollution Effects on Forests (ICP Forests, <http://icp-forests.net/>). Panel (c) is 99% quantile quadratic regression using the satellite observed maximum vegetation height (from Simard et al., 2011) and long-term mean gross primary productivity (GPP) (from Thomas, 2018).

Figure 3. Comparison of  $P^*$  and the standardised bi-weighted mean of the raw ring width (RWI-mean) for the example sites in Figure 1.

Figure 4. Sensitivity of  $P^*$  to maximum height ( $H_m$ ) and the initial slope of height to diameter (a). Panels a and b show the influence of different values of  $H_m$  and a on the random effects of life-history  $P^*$  for each individual tree in the first step regression. Different coloured points are the measurements for individual trees. Panels c and d show the comparison for the final site-level year-by-year  $P^*$  with different values of  $H_m$  and a.

Figure 5. Effect of peak growth position on final year-by-year  $P^*$ : using the theoretical approach to define peak radial growth (red) and using the first maximum ring width to define peak radial growth (blue).

Figure 6. Observed response of  $P^*$  to bioclimate variables. Partial residual plots, based on the linear mixed model regression analysis, show the response of *Picea* and *Pinus* for the periods 1940-1969 and 1970-2000.

Figure 7. Observed response of  $P^*$  to bioclimate variables and  $[CO_2]$ . Partial residual plots, based on the linear mixed model regression analysis, show the response of *Picea* and *Pinus* for the periods 1940-1969 and 1970-2000.

Table 1. Summary of the linear mixed model for the climate control analysis for the period of 1940-1969, 1970-2000, and 1940-2000 for *Picea* and *Pinus*.

Table 2. Summary of the linear mixed model including  $CO_2$  and climate for the period of 1940-1969, 1970-2000, and 1940-2000 for *Picea* and *Pinus*.



629 Table 1. Summary of the linear mixed model for the climate control analysis for the period of 1940-  
630 1969, 1970-2000, and 1940-2000 for *Picea* and *Pinus*.  
631

species	period	Slope*10000 (except slope of PPFD <sub>5</sub> *e+8)				R <sup>2</sup> <sub>fixed</sub>	R <sup>2</sup> <sub>total</sub>	mGDD <sub>5</sub> at vertex (°C)
		mGDD <sub>5</sub>	mGDD <sub>5</sub> <sup>2</sup>	PPFD <sub>5</sub>	log( $\alpha$ )			
<i>Pinus</i>	1940-1969	2.65±1.32	-0.17±0.05	10.43±3.48	24.76±1.45	0.059	0.882	7.59±1.6
	1970-2000	3.75±1.31	-0.18±0.05	3.36±3.17	24.3±1.52	0.056	0.850	10.62±0.88
	1940-2000	3.18±1.03	-0.18±0.04	1.32±2.63	23.04±1.14	0.071	0.846	8.61±0.99
<i>Picea</i>	1940-1969	5.01±1.71	-0.27±0.08	11.6±4.32	23.09±1.65	0.067	0.880	9.18±0.74
	1970-2000	8.4±1.63	-0.42±0.07	18.26±4.37	24.51±1.72	0.073	0.861	9.99±0.36
	1940-2000	6.81±1.24	-0.36±0.05	7.62±3.27	22.14±1.24	0.070	0.859	9.43±0.38

632  
633  
634 Table 2. Summary of the linear mixed model including CO<sub>2</sub> and climate for the period of 1940-1969,  
635 1970-2000, and 1940-2000 for *Picea* and *Pinus*.  
636

species	period	Slope*10000 (except slope of PPFD <sub>5</sub> *e+8)					R <sup>2</sup> <sub>fixed</sub>	R <sup>2</sup> <sub>total</sub>	mGDD <sub>5</sub> at vertex (°C)
		mGDD <sub>5</sub>	mGDD <sub>5</sub> <sup>2</sup>	PPFD <sub>5</sub>	log( $\alpha$ )	CO <sub>2</sub>			
<i>Pinus</i>	1940-1969	2.67±1.32	-0.17±0.05	10.57±3.51	24.74±1.45	0.01±0.04	0.058	0.882	7.62±1.6
	1970-2000	3.63±1.31	-0.17±0.05	5.94±3.28	25.16±1.55	-0.03±0.01	0.052	0.847	10.77±0.89
	1940-2000	3.23±1.03	-0.18±0.04	3.12±2.66	23.88±1.15	-0.03±0.01	0.067	0.843	8.81±0.96
<i>Picea</i>	1940-1969	4.91±1.71	-0.27±0.08	13.72±4.4	23.13±1.65	0.1±0.04	0.066	0.878	9.22±0.75
	1970-2000	8.29±1.63	-0.42±0.07	13.76±4.57	23.68±1.74	0.04±0.01	0.073	0.865	9.82±0.38
	1940-2000	7.34±1.23	-0.37±0.05	11.58±3.29	23.54±1.25	-0.05±0.01	0.073	0.856	9.8±0.33

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Figure 1. (a) Distribution of northern hemisphere *Pinus* and *Picea* tree-ring records covering period 1940-2000 (b) sampling age distribution through time for 3 *Picea* and 3 *Pinus* example sites, showing age sampling biases. These six sites are identified on the map with letters (a-f).

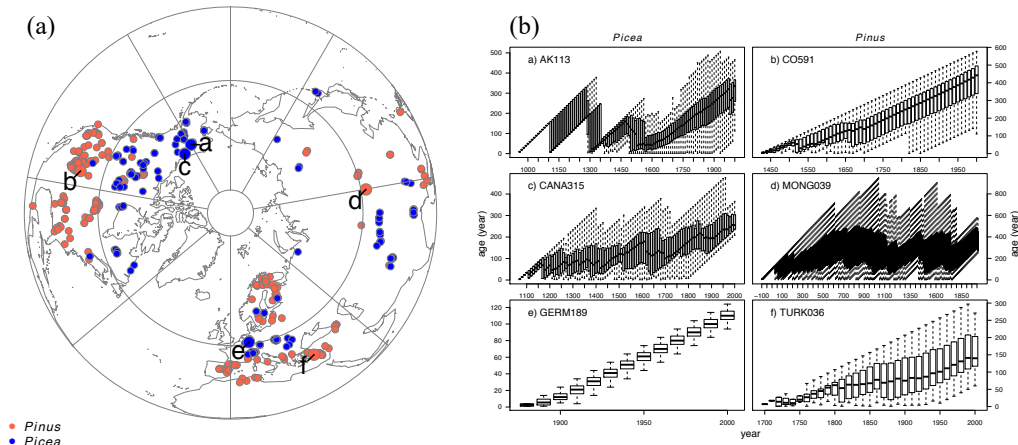


Figure 2. Estimation of asymptotic maximum height ( $H_m$ ) and the initial slope of height to diameter (a). Panel (a) and (b) are the estimations for asymptotic maximum height ( $H_m$ ) and the initial slope of height to diameter (a) using all the measurements for *Picea* and *Pinus* from the Integrated Co-operative Programme on Assessment and Monitoring of Air Pollution Effects on Forests (ICP Forests, <http://icp-forests.net/>). Panel (c) is 99% quantile quadratic regression using the satellite observed maximum vegetation height (from Simard et al., 2011) and long-term mean gross primary productivity (GPP) (from Thomas, 2018).

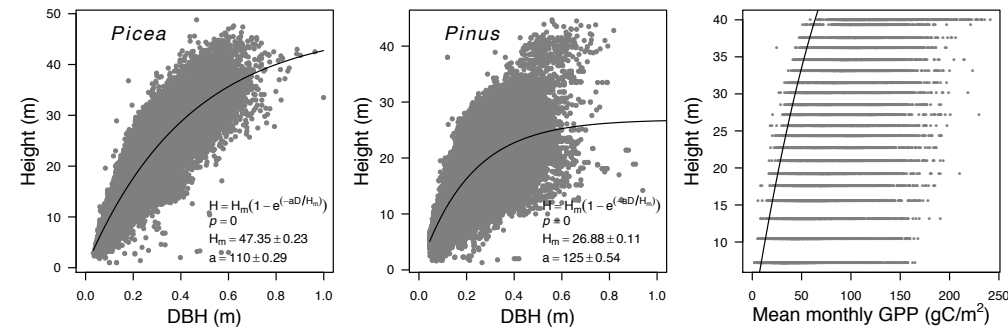




Figure 3. Comparison of  $P^*$  and the standardised bi-weighted mean of the raw ring width (RWI-mean) for the example sites in Figure 1.

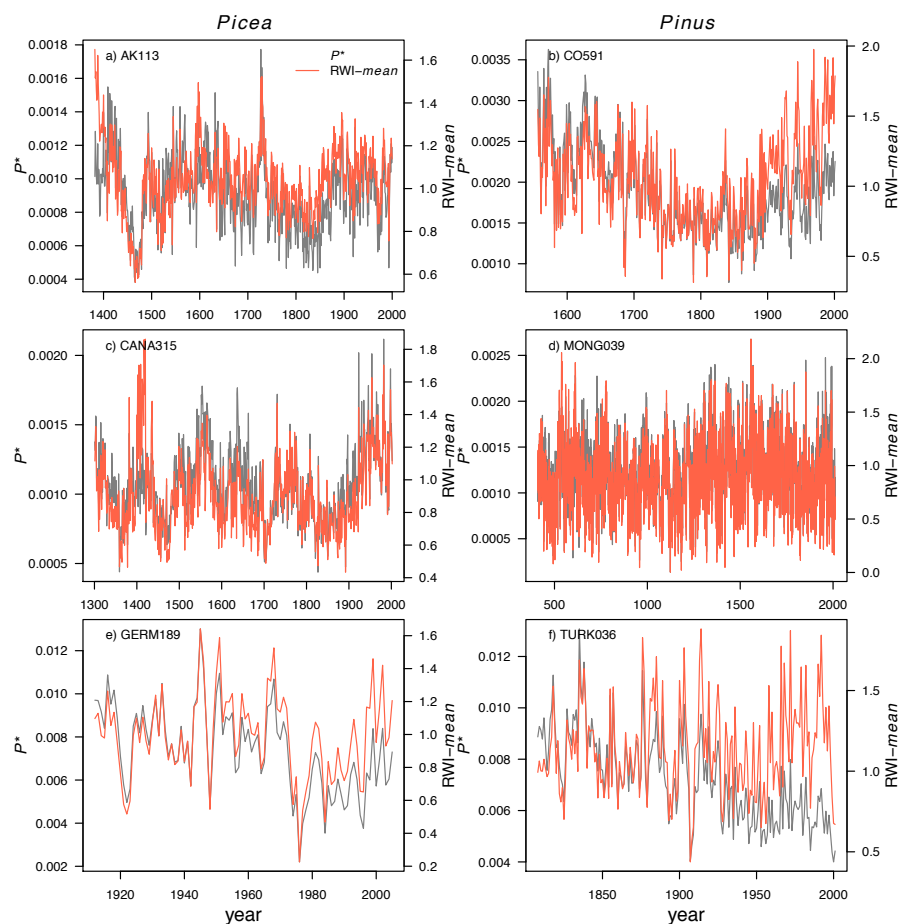
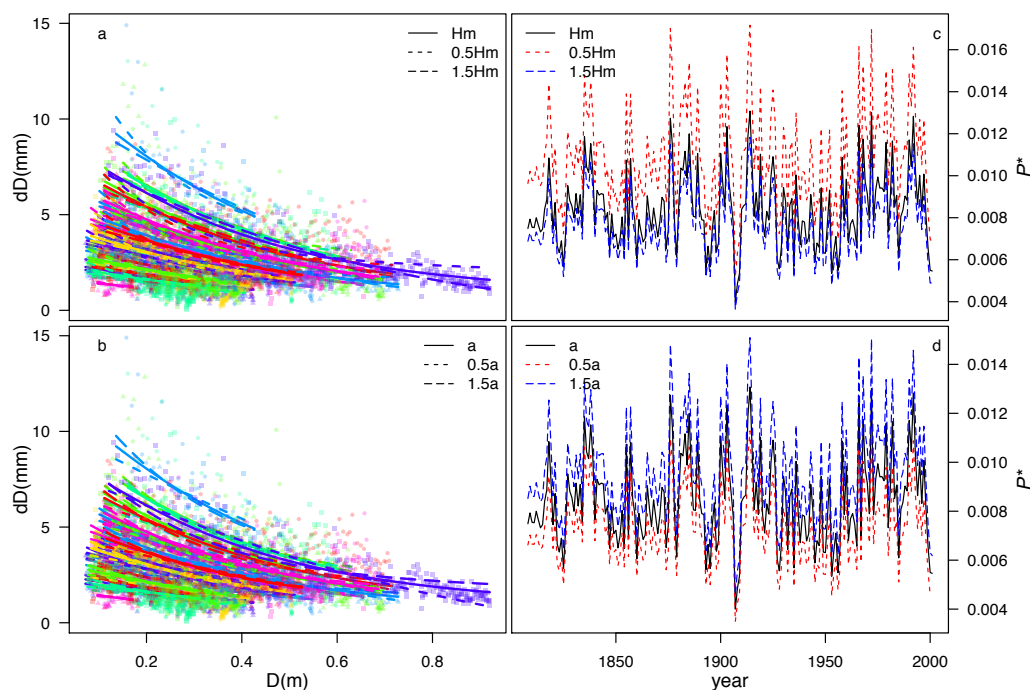


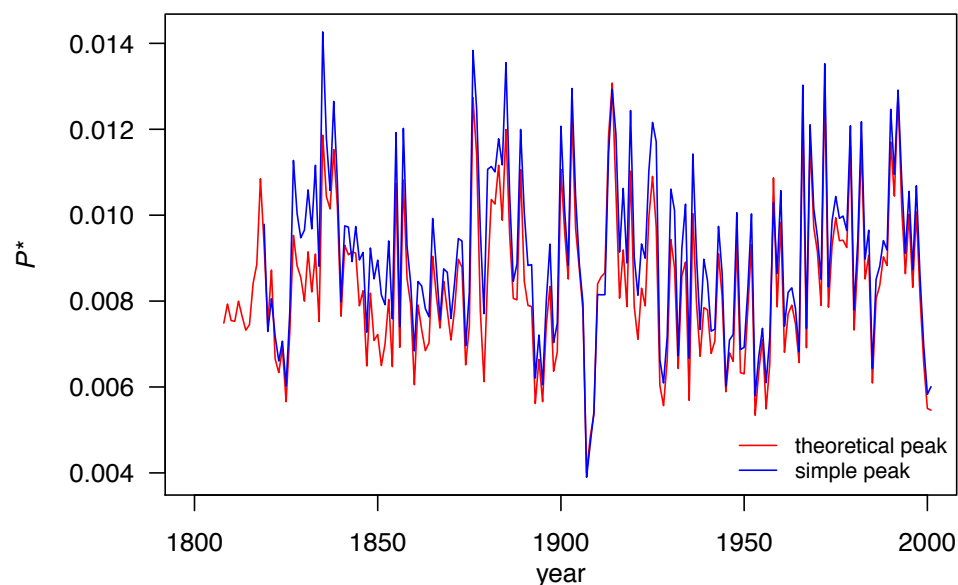


Figure 4. Sensitivity of  $P^*$  to maximum height ( $H_m$ ) and the initial slope of height to diameter ( $a$ ). Panels a and b show the influence of different values of  $H_m$  and  $a$  on the random effects of life-history  $P^*$  for each individual tree in the first step regression. Different coloured points are the measurements for individual trees. Panels c and d show the comparison for the final site-level year-by-year  $P^*$  with different values of  $H_m$  and  $a$ .





666 Figure 5. Effect of peak growth position on final year-by-year  $P^*$ : using the theoretical approach to  
667 define peak radial growth (red) and using the first maximum ring width to define peak radial growth  
668 (blue).  
669



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671  
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Figure 6. Observed response of  $P^*$  to bioclimate variables. Partial residual plots, based on the linear mixed model regression analysis, show the response of *Picea* and *Pinus* for the periods 1940–1969 and 1970–2000.

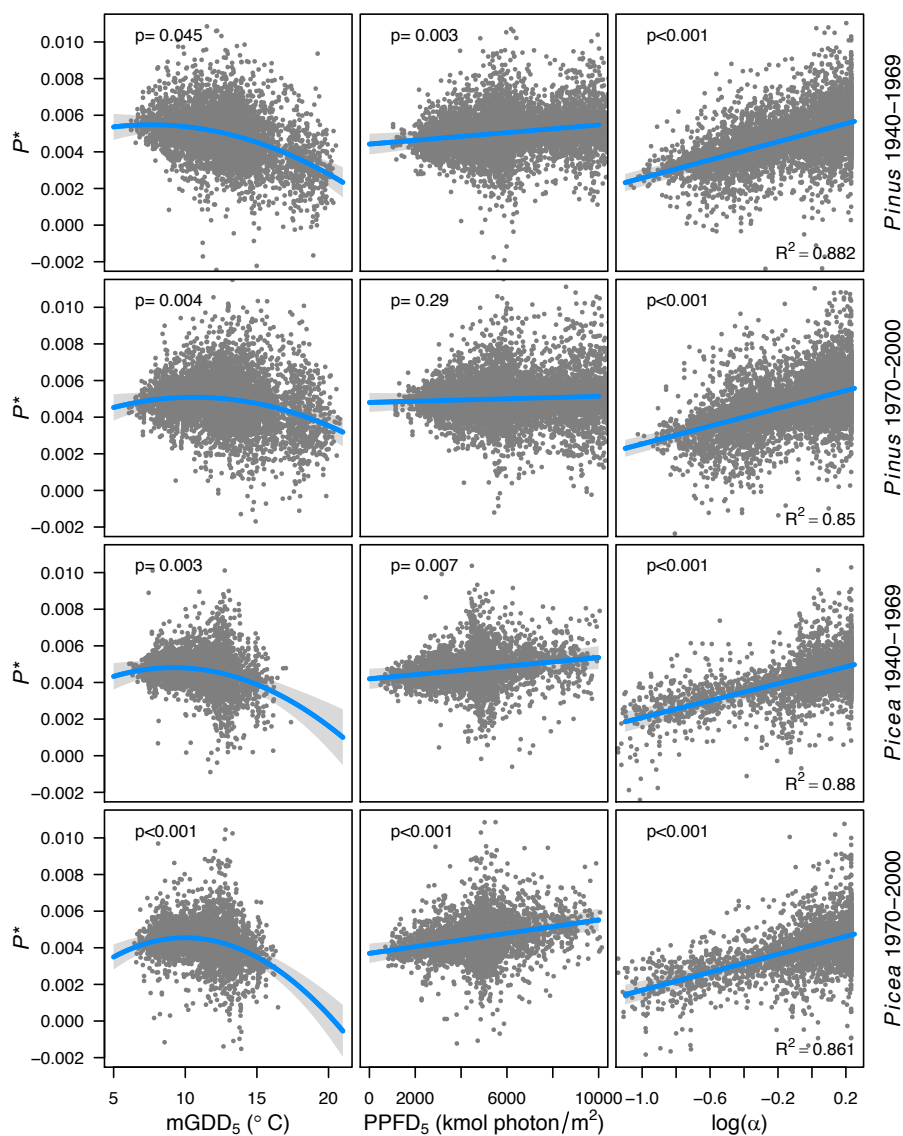




Figure 7. Observed response of  $P^*$  to bioclimate variables and  $[\text{CO}_2]$ . Partial residual plots, based on the linear mixed model regression analysis, show the response of *Picea* and *Pinus* for the periods 1940–1969 and 1970–2000.

