Dear handling editor,

Thanks for giving us the opportunity to revise our manuscript following reviewers’ comments. We have taken into account all of reviewers’ comments in revising our manuscript. Among their major comments,

1) we have rearranged the manuscript by moving budget equations to the appendix, and moving the description of all parameterizations to the main text,
2) moved Figure 1, which showed the original structure of the model, from main text to the appendix
3) added additional discussion of various BNF parameterizations, and parameterizations that related leaf N to Vcmax, in the discussion section
4) added equations that describe how the model treats upper limit of C:N ratios of different plant components,
5) included an additional plot (now Figure 10c) which shows zonally-averaged GPP ratios to illustrate how downregulation works differently in the original model and the model version with N cycle, and
6) included a sentence about prioritizing immobilization versus plant N uptake in section 3.3.6 (on page 27 of this document).
7) Reorganized figures such that fertilizer input and N deposition are considered inputs, plotted in a separate figure, and discussed in inputs while BNF is considered a model output, plotted separately than specified N inputs of fertilizer and N deposition, and discussed in the model results section.

In addition, we also took into account all of minor comments that reviewers made as mentioned in our reply to the reviewers in the discussion section.

This document tracks all the changes that we have made since our last version.

Best regards,
Vivek.
Implementation of nitrogen cycle in the CLASSIC land model

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Abstract

A terrestrial nitrogen (N) cycle model is coupled to carbon (C) cycle in the framework of the Canadian Land Surface Scheme including biogeochemical cycles (CLASSIC). CLASSIC currently models physical and biogeochemical processes and simulates fluxes of water, energy, and CO₂ at the land-atmosphere boundary. Similar to most models, gross primary productivity in CLASSIC increases in response to increasing atmospheric CO₂ concentration. In the current model version, a downregulation parameterization emulates the effect of nutrient constraints and scales down potential photosynthesis rates, using a globally constant scalar, as a function of increasing CO₂. In the new model when nitrogen (N) and carbon (C) cycles are coupled, cycling of N through the coupled soil-vegetation system facilitates the simulation of leaf N content and maximum carboxylation capacity (V₅₀) prognostically. An increase in atmospheric CO₂ decreases leaf N content, and therefore V₅₀, allowing the simulation of photosynthesis downregulation as a function of N supply. All primary N cycle processes, that represent the coupled soil-vegetation system, are modelled explicitly. These include biological N fixation, treatment of externally specified N deposition and fertilization application, uptake of N by plants, transfer of N to litter via litterfall, mineralization, immobilization, nitrification, denitrification, ammonia volatilization, and the gaseous fluxes of NO, N₂O, and N₂. The interactions between terrestrial C and N cycles are evaluated by perturbing the coupled soil-vegetation system in CLASSIC with one forcing at a time over the 1850-2017 historical period. These forcings include the increase in atmospheric CO₂, change in climate, increase in N deposition, and increasing crop area and fertilizer input, over the historical period.

Increase in atmospheric CO₂ increases the C:N ratio of vegetation; climate warming over the historical period increases N mineralization and leads to a decrease in vegetation C:N ratio; N deposition also decreases vegetation C:N ratio; and fertilizer input increases leaching, NH₃ volatilization, and gaseous losses of N₂, N₂O, and NO. These model responses are consistent with conceptual understanding of the coupled C and N cycles. The simulated terrestrial carbon sink over the 1959-2017 period, from the simulation with all forcings, is 2.0 Pg C/yr and compares reasonably well with the quasi observation-based estimate from the 2019 Global Carbon Project (2.1 Pg C/yr). The contribution of increasing CO₂, climate change, and N deposition to carbon uptake by land over the historical period (1850-2017) is calculated to be 84%, 2%, and 14%, respectively.
1. Introduction

The uptake of carbon (C) by land and ocean in response to the increase in anthropogenic fossil fuel emissions of CO\textsubscript{2} has served to slow down the growth rate of atmospheric CO\textsubscript{2} since the start of the industrial revolution. At present, about 55% of total carbon emitted into the atmosphere is taken up by land and ocean (Le Quéré et al., 2018; Friedlingstein et al., 2019). It is of great policy, societal, and scientific relevance whether land and ocean will continue to provide this ecosystem service. Over land, as long as photosynthesis is not water limited, the uptake of carbon in response to increasing anthropogenic CO\textsubscript{2} emissions is driven by two primary factors, 1) the CO\textsubscript{2} fertilization of the terrestrial biosphere, and 2) the increase in temperature, both of which are associated with increasing [CO\textsubscript{2}]. The CO\textsubscript{2} fertilization effect increases photosynthesis rates for about 80% of the world’s vegetation that uses the C\textsubscript{3} photosynthetic pathway and is currently limited by [CO\textsubscript{2}] (Still et al., 2003; Zhu et al., 2016). The remaining 20% of vegetation uses the C\textsubscript{4} photosynthetic pathway that is much less sensitive to [CO\textsubscript{2}]. Warming increases carbon uptake by vegetation in mid-high latitude regions where growth is currently limited by low temperatures (Zeng et al., 2011).

Even when atmospheric CO\textsubscript{2} is not limiting for photosynthesis, and near surface air temperature is optimal, vegetation cannot photosynthesize at its maximum possible rate if available water and nutrients (most importantly nitrogen (N) and phosphorus (P)) constrain photosynthesis (Vitousek and Howarth, 1991; Reich et al., 2006b). In the absence of water and nutrients, photosynthesis simply cannot occur. N is a major component of chlorophyll (the compound through which plants photosynthesize) and amino acids (that are the building blocks of proteins). The constraint imposed by available water and nutrients implies that the carbon
uptake by land over the historical period in response to increasing \([\text{CO}_2]\) is lower than what it
would have been if water and nutrients were not limiting. This lower than maximum theoretically
possible rate of increase of photosynthesis in response to increasing atmospheric \([\text{CO}_2]\) is referred
to as downregulation (Faria et al., 1996; Sanz-Sáez et al., 2010). Typically, however, the term
downregulation of photosynthesis is used only in the context of nutrients and not water.

Downregulation is defined as a decrease in photosynthetic capacity of plants grown at elevated
\([\text{CO}_2]\) in comparison to plants grown at baseline \([\text{CO}_2]\) (McGuire et al., 1995). However, despite the
decrease in photosynthetic capacity, the photosynthesis rate for plants grown at elevated \([\text{CO}_2]\)
is still higher than the rate for plants grown and measured at baseline \([\text{CO}_2]\) because of higher
background \([\text{CO}_2]\).

Earth system models (ESMs) that explicitly represent coupling of the global carbon cycle
and physical climate system processes are the only tools available at present that, in a physically
consistent way, are able to project how land and ocean carbon cycles will respond to future
changes in [\text{CO}_2]. Such models are routinely compared to one another under the auspices of the
Coupled Model Intercomparison Project (CMIP) every 6-7 years. The most recent and sixth phase
of CMIP (CMIP6) is currently underway (Eyring et al., 2016). Interactions between carbon cycle
and climate in ESMs have been compared under the umbrella of the Coupled Climate-Carbon
Cycle Model Intercomparison Project (C4MIP) (Jones et al., 2016) which is an approved MIP of
the CMIP. Comparison of land and ocean carbon uptake in C4MIP studies (Friedlingstein et al.,
2006; Arora et al., 2013, 2020) indicate that the inter-model uncertainty in future land carbon
uptake across ESMs is more than three times than the uncertainty for the ocean carbon uptake.
The reason for widely varying estimates of future land carbon uptake across models is that our
understanding of biological processes that determine land carbon uptake is much less advanced than the physical processes which primarily determine carbon uptake over the ocean. In the current generation of terrestrial ecosystem models, other than photosynthesis for which a theoretical framework exists, almost all of the other biological processes are represented on the basis of empirical observations and parameterized in one way or another. In addition, not all models include N and P cycles. In the absence of an explicit representation of nutrient constraints on photosynthesis, land models in ESMs parameterize downregulation of photosynthesis in other ways that reduce the rate of increase of photosynthesis to values below its theoretically maximum possible rate, as [CO$_2$] increases (e.g., Arora et al., 2009). Comparison of models across 5th and 6th phase of CMIP shows that the fraction of models with land N cycle is increasing (Arora et al., 2013, 2020).

The nutrient constraints on photosynthesis are well recognized (Vitousek and Howarth, 1991; Arneth et al., 2010). Terrestrial carbon cycle models neglect of nutrient limitation on photosynthesis has been questioned from an ecological perspective (Reich et al., 2006a) and it has been argued that without nutrient constraints these models will overestimate future land carbon uptake (Hungate et al., 2003). Since in the real world photosynthesis downregulation does indeed occur due to nutrient constraints, it may be argued that more confidence can be placed in future projections of models that explicitly model the interactions between the terrestrial C and N cycles rather than parameterize it in some other way.

Here, we present the implementation of N cycle in the Canadian Land Surface Scheme Including biogeochemical Cycles (CLASSIC) model, which serves as the land component in the family of Canadian Earth System Models (Arora et al., 2009, 2011; Swart et al., 2019). Section 2
briefly describes existing physical and carbon cycle components and processes of the CLASSIC model. The conceptual basis of the new N cycle model and its parameterizations are described in Section 3, Section 4 outlines the methodology and data sets that we have used to perform various simulations over the 1850-2017 historical period to assess the realism of the coupled C and N cycles in CLASSIC in response to various forcings. Results from these simulations over the historical period are presented in Section 5 and finally discussion and conclusions are presented in Section 6.

2. The CLASSIC land model

2.1 The physical and carbon biogeochemical processes

The CLASSIC model is the successor to, and based on, the coupled Canadian Land Surface Scheme (CLASS; Verseghy, 1991; Verseghy et al., 1993) and Canadian Terrestrial Ecosystem Model (CTEM; Arora and Boer, 2005; Melton and Arora, 2016). CLASS and CTEM model physical and biogeochemical processes in CLASSIC, respectively. Both CLASS and CTEM have a long history of development as described in Melton et al. (2019) who also provide an overview of the CLASSIC land model and describe its new technical developments that launched CLASSIC as a community model. CLASSIC simulates land-atmosphere fluxes of water, energy, momentum, CO₂, and CH₄. The CLASSIC model can be run at a point scale, e.g. using meteorological and geophysical data from a FluxNet site, or over a spatial domain, that may be global or regional, using gridded data.

We briefly summarize the primary physical and carbon biogeochemical processes of CLASSIC here that are relevant in the context of implementation of the N cycle in the model.

2.1.1 Physical processes
The physical processes of CLASSIC which simulate fluxes of water, energy and momentum, are calculated over vegetated, snow, and bare fractions at a sub-daily time step of 30 minutes. The vegetation is described in terms of four plant functional types (PFTs): needleleaf trees, broadleaf trees, crops, and grasses. The fractional coverage of these four PFTs is specified in the current study over the historical period. The structural attributes of vegetation are described by leaf area index (LAI), vegetation height, canopy mass, and rooting distribution through the soil layers and these are all simulated dynamically by the biogeochemical module of CLASSIC. In the model version used here, 20 ground layers starting with 10 layers of 0.1 m thickness are used.

The thickness of layers gradually increases to 30 m for a total ground depth of over 61 m. The depth to bedrock varies geographically and is specified based on a soil depth data set. Liquid and frozen soil moisture contents, and soil temperature, are determined prognostically for permeable soil layers. CLASSIC also prognostically models the temperature, mass, albedo, and density of a single layer snow pack (when the climate permits snow to exist), interception and throughfall of rain and snow by the canopy, and the subsequent unloading of snow, are also modelled. The energy and water balance over the land surface, and the transfer of heat and moisture through soil, affect the temperature and soil moisture content of soil layers all of which consequently affect the carbon and nitrogen cycle processes.

### 2.1.2 Biogeochemical processes

The biogeochemical processes in CLASSIC are based on CTEM, and described in detail in the appendix of Melton and Arora (2016). The biogeochemical component of CLASSIC simulates...
the land-atmosphere exchange of CO₂ and while doing so simulates vegetation as a dynamic component. The biogeochemical module of CLASSIC uses information about net radiation, and liquid and frozen soil moisture contents of all the soil layers along with air temperature to simulate photosynthesis and prognostically calculates amount of carbon in the model’s three live (leaves, stem, and root) and two dead (litter and soil) carbon pools for each PFT. The litter and soil carbon pools are not tracked for each soil layer. Litter is assumed to be near surface and an exponential distribution for soil carbon is assumed with values decreasing with soil depth. Photosynthesis in CLASSIC is modelled at the same sub-daily time as the physical processes. The remainder of the biogeochemical processes are modelled at a daily time step. These include: 1) autotrophic and heterotrophic respirations from all the live and dead carbon pools, respectively, 2) allocation of photosynthate from leaves to stem and roots, 3) leaf phenology, 4) turnover of live vegetation components that generates litter, 5) mortality, 6) land use change (LUC), 7) fire (Arora and Melton, 2018), and 8) competition between PFTs for space (not switched on in this study).

Figure A1 in the appendix shows the existing structure of CLASSIC’s carbon pools along with the addition of non-structural carbohydrate pools for each of the model’s live vegetation components. The non-structural pools are not yet represented in the current operational version of CLASSIC (Melton et al., 2019). The addition of non-structural carbohydrate pools is explained in Asaadi et al. (2018) and helps improve leaf phenology for cold deciduous tree PFTs. The N cycle model presented here is built on the research version of CLASSIC that consists of non-structural and structural carbon pools for the leaves (L), stem (S), and root (R) components and the two dead carbon pools in litter or detritus (D) and soil or humus (H) (Figure A1). We briefly describe
these carbon pools and fluxes between them, since N cycle pools and fluxes are closely tied to carbon pools and fluxes. The gross primary productivity (GPP) flux enters the leaves from the atmosphere. This non-structural photosynthate is allocated between leaves, stem, and roots. The non-structural carbon then moves into the structural carbohydrates pool. Once this conversion occurs structural carbon cannot be converted back to non-structural labile carbon. The model attempts to maintain a minimum fraction of non-structural to total carbon in each component of about 0.05 (Asaadi et al., 2018). Non-structural carbon is moved from stem and root components to leaves, at the time of leaf onset for deciduous PFTs, and this is termed reallocation. The movement of non-structural carbon is indicated by red arrows. Maintenance and growth respiration (indicated by subscript m and g in Figure A1), which together constitute autotrophic respiration, occur from the non-structural components of the three live vegetation components. Litterfall from the structural and non-structural components of the vegetation components contributes to the litter pool. Leaf litterfall is generated due to normal turnover of leaves as well as cold and drought stresses, and reduction in day length. Stem and root litter is generated due to their turnover based on their specified life spans. Heterotrophic respiration occurs from the litter and soil carbon pools depending on soil moisture and temperature, and humified litter is moved from litter to the soil carbon pool.

All these terrestrial ecosystem processes and the amount of carbon in the live and dead carbon pools are modelled explicitly for nine PFTs that map directly onto the four base PFTs used in the physics module of CLASSIC. Needleleaf trees are divided into their deciduous and evergreen phenotypes, broadleaf trees are divided into cold deciduous, drought deciduous, and evergreen phenotypes, and crops and grasses are divided based on their photosynthetic
pathways into $C_3$ and $C_4$ versions. The sub-division of PFTs is required for modelling biogeochemical processes. For instance, simulating leaf phenology requires the distinction between evergreen and deciduous phenotypes of needleleaf and broadleaf trees. However, once LAI is known, a physical process (such as the interception of rain and snow by canopy leaves) does not need to know the underlying evergreen or deciduous nature of leaves.

The prognostically determined biomasses in leaves, stem, and roots are used to calculate structural vegetation attributes that are required by the physics module. Leaf biomass is used to calculate LAI using PFT-dependent specific leaf area. Stem biomass is used to calculate vegetation height for tree and crop PFTs, and LAI is used to calculate vegetation height for grasses. Finally, root biomass is used to calculate rooting depth and distribution which determines the fraction of roots in each soil layer. Only total root biomass is tracked; fine and coarse root biomasses are not separately tracked. Fraction of fine roots is calculated as a function of total root biomass, as shown later.

The approach for calculating photosynthesis in CLASSIC is based on the standard Farquhar et al. (1980) model for $C_3$ photosynthetic pathway, and Collatz et al. (1992) for the $C_4$ photosynthetic pathway and presented in detail in Arora (2003). The model calculates gross photosynthesis rate that is co-limited by the photosynthetic enzyme Rubisco, by the amount of available light, and by the capacity to transport photosynthetic products for $C_3$ plants or the $CO_2$-limited capacity for $C_4$ plants. In the real world, the maximum Rubisco limited rate ($V_{Cmax}$) depends on the leaf N content since photosynthetic capacity and leaf N are strongly correlated (Evans, 1989; Field and Mooney, 1986; Garnier et al., 1999). In the current operational version of CLASSIC, the N cycle is not represented and the PFT-dependent values of $V_{Cmax}$ are therefore

Deleted: Other than these structural vegetation attributes the biogeochemical module also calculates canopy resistance (in conjunction with photosynthesis) that is used by the physics module in calculating transpiration.
specified based on Kattge et al. (2009) who compile $V_{\text{cmax}}$ values using observation-based data from more than 700 measurements. Along with available light, and the capacity to transport photosynthetic products, the GPP in the model is determined by specified PFT-dependent values of $V_{\text{cmax}}$.

In the current CLASSIC version a parameterization of photosynthesis downregulation is included which, in the absence of the N cycle, implicitly attempts to simulate the effects of nutrient constraints. This parameterization, based on approaches which express GPP as a logarithmic function of [CO$_2$] (Cao et al., 2001; Alexandrov and Oikawa, 2002), is explained in detail in Arora et al. (2009) and briefly summarized here. To parameterize photosynthesis downregulation with increasing [CO$_2$], the unconstrained or potential GPP (for each time step and each PFT in a grid cell) is multiplied by the global scalar $\xi(c)$

\[ G = \xi(c) \, G_p \]  

\[ \xi(c) = \frac{1+\gamma_d \ln(c/c_0)}{1+\gamma_p \ln(c/c_0)} \]  

where $c$ is [CO$_2$] at time $t$ and its initial value is $c_0$, the parameter $\gamma_p$ indicates the “potential” rate of increase of GPP with [CO$_2$] (indicated by the subscript $p$), the parameter $\gamma_d$ represents the downregulated rate of increase of GPP with [CO$_2$] (indicated by the subscript $d$). When $\gamma_d < \gamma_p$ the modelled gross primary productivity ($G$) increases in response to [CO$_2$] at a rate determined by the value of $\gamma_d$. In the absence of the N cycle, the term $\xi(c)$ thus emulates down-regulation of photosynthesis as CO$_2$ increases. For example, values of $\gamma_d = 0.35$ and $\gamma_p = 0.9$, yield a value of $\xi(c) = 0.87$ (indicating a 13% downregulation) for $c = 390$ ppm (corresponding to year 2010) and $c_0 = 285$ ppm.
Note that while the original model version does not include N cycle, it is capable of simulating realistic geographical distribution of GPP that partly comes from the specification of observation-based $V_{\text{max}}$ values (which implicitly takes into account C and N interactions in a non-dynamic way) but more so the fact that the geographical distribution of GPP (and therefore net primary productivity, NPP), to the first order, depends on climate. The specified $V_{\text{max}}$ values for the 9 PFTs in CLASSIC vary by about 2 times, from about 35 to 75 μmol CO$_2$ m$^{-2}$ s$^{-1}$. The simulated GPP in the model, however, varies from zero in the Sahara desert to about 3000 gC m$^{-2}$ year$^{-1}$ in the Amazonian rainforest indicating the overarching control of climate in determining the geographical distribution of GPP. This is further illustrated by the Miami NPP model, for instance, which is able to simulate the geographical distribution of NPP using only mean annual temperature and precipitation (Leith, 1975) since both the C and N cycles are governed primarily by climate. The current version of CLASSIC is also able to reasonably simulate the terrestrial C sink over the second half of the 20$^{th}$ century and early 21$^{st}$ century. CLASSIC (with its former CLASS-CTEM name) has regularly contributed to the annual Trends in Net Land–Atmosphere Carbon Exchange (TRENDY) model intercomparison since 2016 which contributes results to the Global Carbon Project’s annual assessments — the most recent one being Friedlingstein et al. (2019). What is then the purpose of coupling C and N cycles?

3. Implementation of the N cycle in CLASSIC

The primary objective of implementation of the N cycle is to model $V_{\text{max}}$ as a function of leaf N content so as to make the use of multiplier $\zeta (c)$ obsolete in the model, and allow to project...
future carbon uptake that is constrained by available N. Modelling of leaf N content as a prognostic variable, however, requires modelling the full N cycle over land. N enters the soil in the inorganic mineral form through biological fixation of N, fertilizer application, and atmospheric N deposition in the form of ammonium and nitrate. N cycling through plants implies uptake of inorganic mineral N by plants, its return to soil through litter generation in the organic form, and its conversion back to mineral form during decomposition of organic matter in litter and soil. Finally, N leaves the coupled soil-vegetation system through leaching in runoff and through various gaseous forms to the atmosphere. This section describes how these processes are implemented and parameterized in the CLASSIC modelling framework. While the first order interactions between C and N cycles are described well by the current climate, their temporal dynamics over time require to explicitly model these processes.

Globally, terrestrial N cycle processes are even less constrained than the C cycle processes. As a result, the model structure and parameterizations are based on conceptual understanding and mostly empirical observations of N cycle related biological processes. We attempt to achieve balance between a parsimonious and simple model structure and the ability to represent the primary feedbacks and interactions between different model components.

3.1 Model structure, and N pools and fluxes

N is associated with each of the model’s three live vegetation components and the two dead carbon pools (shown in Figure A1). In addition, separate mineral pools of ammonium (NH₄⁺) and nitrate (NO₃⁻) are considered. Figure 1 shows the C and N pools together in one graphic along with the fluxes of N and C between various pools. The structural and non-structural N pools in
root are written as \(N_{RS}\) and \(N_{RNS}\), respectively, and similarly for stem \((N_S\) and \(N_{SNS}\)) and leaves \((N_L, N_{LS}\) and \(N_{LNS}\)), and together the structural and non-structural pools make up the total N pools in leaf \((N_L = N_{LS} + N_{LNS})\), root \((N_R = N_{RS} + N_{RNS})\), and stem \((N_S = N_{SNS} + N_{SNS})\) components.

The fluxes between the pools in Figure 1 characterize the prognostic nature of the pools as defined by the rate change equations summarized in section A1 in the appendix. The model structure allows the C:N ratio of the live leaves \((C: N_L = C_L/N_L)\), stem \((C: N_S = C_S/N_S)\), and root \((C: N_R = C_R/N_R)\) components, and the dead litter (or debris) pool \((C: N_D = C_D/N_D)\) to evolve prognostically. The C:N ratio of soil organic matter \((C: N_H = C_H/N_H)\), however, is assumed to be constant at 13 following Wania et al. (2012) (see also references therein). The implications of this assumption are discussed later.

The individual terms of the rate change equations of the 10 prognostic N pools (equations A1 through A8, and equations A10 and A11 in the appendix), corresponding to Figure 1, are specified or parameterized as explained in the following sections. These parameterizations are divided into three groups and related to 1) N inputs, 2) N cycling in vegetation and soil, and 3) N cycling in mineral pools and N outputs.

### 3.2 N inputs

#### 3.2.1 Biological N fixation

Biological N fixation (BNF, \(B_{NH_4}\)) is caused by both free living bacteria in the soil and by bacteria symbiotically living within nodules of host plants’ roots. Here, the bacteria convert free nitrogen from the atmosphere to ammonium, which is used by the host plants. Like any other
microbial activity, BNF is limited both by drier soil moisture conditions and cold temperatures.

Cleveland et al. (1999) attempt to capture this by parameterizing BNF as a function of actual evapotranspiration (AET). AET is a function primarily of soil moisture (through precipitation and soil water balance) and available energy. In places where vegetation exists, AET is also affected by vegetation characteristics including LAI and rooting depth. Here, we parameterize BNF (\(B_{NH4}\), gN m\(^{-2}\) day\(^{-1}\)) as a function of modelled soil moisture and temperature to depth of 0.5 m (following the use of similar depth by Xu-Ri and Prentice (2008)) which yields a very similar geographical distribution of BNF as the Cleveland et al. (1999) approach as seen later in Section 4.

\[
B_{NH4} = \left( \sum_c \alpha_c f_c + \sum_n \alpha_n f_n \right) f(T_{0.5}) f(\theta_{0.5}) \\
f(T_{0.5}) = 2^{(T_{0.5} - 25)/10} \\
f(\theta_{0.5}) = \min\left(0, \max\left(1, \frac{\theta_{0.5} - \theta_{fc}}{\theta_{fc} - \theta_{w}}\right)\right) 
\]  

where \(\alpha_c\) and \(\alpha_n\) (gN m\(^{-2}\) day\(^{-1}\)) are BNF coefficients for crop (c) and non-crop or natural (n) PFTs, which are present in a grid cell, \(f(T)\) is the dependence on soil temperature based on a Q\(_{10}\) formulation and \(f(\theta)\) is the dependence on soil moisture which varies between 0 and 1. \(\theta_{fc}\) and \(\theta_{w}\) are the soil moisture at field capacity and wilting points, respectively. \(T_{0.5}\) (°C) and \(\theta_{0.5}\) (m\(^3\) m\(^{-3}\)) in equation (3) are averaged over the 0.5 m soil depth over which BNF is assumed to occur. We do not make the distinction between symbiotic and non-symbiotic BNF since this requires explicit knowledge of geographical distribution of N fixing PFTs which are not represented separately in our base set of nine PFTs. A higher value of \(\alpha_c\) is used compared to \(\alpha_n\) to account for the use of N fixing plants over agricultural areas. Biological nitrogen fixation has been an essential
component of many farming systems for considerable periods, with evidence for the agricultural
use of legumes dating back more than 4,000 years (O’Hara, 1998). A higher \( \alpha_c \) than \( \alpha_n \) is also
consistent with Fowler et al. (2013) who report BNF of 58 and 60 Tg N yr\(^{-1} \) for natural and
agricultural ecosystems for present day. Since the area of natural ecosystems is about five times
the current cropland area, this implies BNF rate per unit land area is higher for crop ecosystems
than for natural ecosystems. Values of \( \alpha_c \) than \( \alpha_n \) and other model parameters are summarized
in Table A1.

Similar to Cleveland et al. (1999), our approach does not lead to a significant change in
BNF with increasing atmospheric CO\(_2\), other than through changes in soil moisture and
temperature. At least two meta-analyses, however, suggest that an increase in atmospheric CO\(_2\)
does lead to an increase in BNF through increased symbiotic activity associated with an increase
in both nodule mass and number (McGuire et al., 1995; Liang et al., 2016). Models have
attempted to capture this by simulating BNF as a function of NPP (Thornton et al., 2007; Wania
et al., 2012). The caveat with this approach and the implications of our BNF approach are
discussed in Section 6.

3.2.2 Atmospheric N deposition

Atmospheric N deposition is externally specified. The model reads in spatially- and
temporally-varying annual deposition rates from a file. Deposition is assumed to occur at the
same rate throughout the year so the same daily rate (g N m\(^{-2} \) day\(^{-1} \)) is used for all days of a given
year. If separate information for ammonium (NH\(_4^+\)) and nitrate (NO\(_3^-\)) deposition rates is available
then it is used otherwise deposition is assumed to be split equally between NH₄⁺ and NO₃⁻ (indicated as $P_{NH4}$ and $P_{NO3}$ in equations A1 and A2).

### 3.2.3 Fertilizer application

Geographically and temporally varying annual fertilizer application rates ($F_{NH4}$) are also specified externally and read in from a file. Fertilizer application occurs over the C₃ and C₄ crop fractions of grid cells. Agricultural management practices are difficult to model since they vary widely between countries and even from farmer to farmer. For simplicity, we assume fertilizer is applied at the same daily fertilizer application rate (gN m⁻² day⁻¹) throughout the year in the tropics (between 30°S and 30°N), given the possibility of multiple crop rotations in a given year. Between the 30° and 90° latitudes in both northern and southern hemispheres, we assume that fertilizer application starts on the spring equinox and ends on the fall equinox. The annual fertilizer application rate is thus distributed over around 180 days. This provides somewhat more realism, than using the same treatment as in tropical regions, since extra-tropical agricultural areas typically do not experience multiple crop rotations in a given year. The prior knowledge of start and end days for fertilizer application makes it easier to figure out how much fertilizer is to be applied each day and helps ensure that the annual amount read from the externally specified file is consistently applied.

### 3.3 N cycling in plants and soil

Plant roots take up mineral N from soil and then allocate it to leaves and stem to maintain an optimal C:N ratio of each component. Both active and passive plant uptakes of N (from both

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Moved down [4]: Litterfall from vegetation contributes to the litter pool and decomposition of litter transfers humified litter to the soil organic matter pool. Decomposition of litter and soil organic matter returns mineralized N back to the NH₄⁺ pool, closing the soil-vegetation N cycle loop.
the NH₄⁺ and NO₃⁻ pools; explained in Sections 3.3.2 and 3.3.3) are explicitly modelled. The active N uptake is modelled as a function of fine root biomass, and passive N uptake depends on the transpiration flux. The modelled plant N uptake also depends on its N demand. Higher N demand leads to higher mineral N uptake from soil as explained below. Litterfall from vegetation contributes to the litter pool and decomposition of litter transfers humified litter to the soil organic matter pool. Decomposition of litter and soil organic matter returns mineralized N back to the NH₄⁺ pool, closing the soil-vegetation N cycle loop.

### 3.3.1 Plant N demand

Plant N demand is calculated based on the fraction of NPP allocated to leaves, stem, and root components and their specified minimum PFT-dependent C:N ratios, similar to other models (Xu-Ri and Prentice, 2008; Jiang et al., 2019). The assumption is that plants always want to achieve their desired minimum C:N ratios if enough N is available.

\[
\Delta_{WP} = \Delta_L + \Delta_R + \Delta_S
\]

\[
\Delta_i = \frac{\text{max}(0, \text{NPP}_{i,C})}{C:N_{i,\text{min}}} \quad i = L, S, R
\]

where the whole plant N demand (Δ_{WP}) is the sum of N demand for the leaves (Δ_L), stem (Δ_R), and root (Δ_S) components, \(a_{i,C}\) is the fraction of NPP (i.e., carbon as indicated by letter C in the subscript \(\mu \text{gC m}^{-2} \text{ day}^{-1}\)) allocated to leaf, stem, and root components, and \(C:N_{i,\text{min}}\) are their specified minimum C:N ratios (see Table A1 for these and all other model parameters). A caveat with this approach when applied at the daily time step, for biogeochemical processes in our model, is that during periods of time when NPP is negative due to adverse climatic conditions (e.g., during winter or drought seasons), the calculated demand
negative. If positive NPP implies there is demand for N, negative NPP cannot be taken to imply that N must be lost from vegetation. As a result, from a plant’s perspective, N demand is assumed to be zero during periods of negative NPP. N demand is also set to zero when all leaves have been shed (i.e., when GPP is zero). At the global scale, this leads to about 15% higher annual N demand than would be the case if negative NPP values were taken into consideration.

3.3.2 Passive N uptake

N demand is weighed against passive and active N uptake. Passive N uptake depends on the concentration of mineral N in the soil and the water taken up by the plants through their roots as a result of transpiration. We assume that plants have no control over N that comes into the plant through this passive uptake. This is consistent with existing empirical evidence that too much N in soil will cause N toxicity (Goyal and Huffaker, 1984), although we do not model N toxicity in our framework. If the N demand for the current time step cannot be met by passive N uptake then a plant compensates for the deficit (i.e., the remaining demand) through active N uptake.

The NH₄⁺ concentration in the soil moisture within the rooting zone, referred to as [NH₄⁺] (gN gH₂O⁻¹), is calculated as

\[
[\text{NH}_4^+] = \frac{N_{\text{NH}_4}}{\theta_i \cdot \mu_i \cdot 10^9 \cdot \rho_i \cdot z_i}
\]  

(5)

where \(N_{\text{NH}_4}\) is ammonium pool size (gN m⁻²), \(\theta_i\) is the volumetric soil moisture content for soil layer \(i\) (m), \(\rho_i\) is the thickness of soil layer \(i\) (m), \(\mu_i\) is the soil layer in which the 99% rooting depth lies as dynamically simulated by the biogeochemical module of CLASSIC following Arora...
and Boer (2003). The $10^6$ term converts units of the denominator term to gH$_2$O m$^{-2}$. NO$_3^-$ concentration ([NO$_3^-$] g N gH$_2$O$^{-1}$) in the rooting zone is found in a similar fashion. The transpiration flux $q_t$ (Kg H$_2$O m$^{-2}$ s$^{-1}$) (calculated in the physics module of CLASSIC) is multiplied by [NH$_4^+$] and [NO$_3^-$] (g N gH$_2$O$^{-1}$) to obtain passive uptake of NH$_4^+$ and NO$_3^-$ (g N m$^{-2}$ day$^{-1}$) as

$$
U_N = 86400 \times 10^3 \beta q_t \left[\text{NH}_4^+\right] \\
U_N = 86400 \times 10^3 \beta q_t \left[\text{NO}_3^-\right]
$$

where the multiplier $86400 \times 10^3$ converts $q_t$ to units of gH$_2$O m$^{-2}$ day$^{-1}$, and $\beta$ (see Table A1) is the dimensionless mineral N distribution coefficient with a value less than 1 that accounts for the fact that NH$_4^+$ and NO$_3^-$ available in the soil are not well mixed in the soil moisture solution, and not completely accessible to roots, to be taken up by plants.

### 3.3.3 Active N uptake

The active plant N uptake is parameterized as a function of fine root biomass and the size of NH$_4^+$ and NO$_3^-$ pools in a manner similar to Gerber et al. (2010) and Wania et al. (2012). The distribution of fine roots across the soil layers is ignored. CLASSIC does not explicitly model fine root biomass. We therefore calculate the fraction of fine root biomass using an empirical relationship that is very similar to the relationship developed by Kurz et al. (1996) (their equation 5) but also works below total root biomass of 0.33 Kg C m$^{-2}$ (the Kurz et al. (1996) relationship yields a fraction of fine root more than 1.0 below this threshold). The fraction of fine root biomass ($f_r$) is given by

$$
f_r = 1 - \frac{C_R}{C_R + 0.6}
$$
where $C_R$ is the root biomass (KgC m$^{-2}$) simulated by the biogeochemical module of CLASSIC.

Equation (7) yields fine root fraction approaching 1.0 as $C_R$ approaches 0, so at very low root biomass values all roots are considered fine roots. For grasses the fraction of fine root biomass is set to 1. The maximum or potential active N uptake for $\text{NH}_4^+$ and $\text{NO}_3^-$ is given by

$$U_{a,pot,\text{NH}_4} = \frac{\epsilon \cdot f_r \cdot C_R \cdot N_{\text{NH}_4}}{k_{p,\text{NH}_4} + N_{\text{NH}_4} + N_{\text{NO}_3}}$$

$$U_{a,pot,\text{NO}_3} = \frac{\epsilon \cdot f_r \cdot C_R \cdot N_{\text{NO}_3}}{k_{p,\text{NO}_3} + N_{\text{NH}_4} + N_{\text{NO}_3}}$$

(8)

where $\epsilon$ (see Table A1) is the efficiency of fine roots to take up N per unit fine root mass per day (gN gC$^{-1}$ day$^{-1}$), $k_{p,\text{NH}_4}$ (see Table A1) is the half saturation constant (gN m$^{-3}$), and $N_{\text{NH}_4}$ and $N_{\text{NO}_3}$ are the ammonium and nitrate pool sizes (gN m$^{-2}$) as mentioned earlier. Depending on the geographical location and the time of the year, if passive uptake alone can satisfy plant N demand the actual active N uptake of $\text{NH}_4^+$ ($U_{a,\text{actual,NH}_4}$) and $\text{NO}_3^-$ ($U_{a,\text{actual,NO}_3}$) is set to zero. Conversely, during other times both passive and potential active N uptakes may not be able to satisfy the demand and in this case actual active N uptake is equal to its potential rate. At times other than these, the actual active uptake is lower than its potential value. This adjustment of actual active uptake is illustrated in equation (9).
if \((\Delta WP \leq U_{p,NH4} + U_{p,NO3})\)
\[
U_{a\text{-actual,NH4}} = 0
\]
\[
U_{a\text{-actual,NO3}} = 0
\]

if \((\Delta WP > U_{p,NH4} + U_{p,NO3}) \land (\Delta WP < U_{p,NH4} + U_{p,NO3} + U_{a,\text{pot,NH4}} + U_{a,\text{pot,NO3}})\)
\[
U_{a\text{-actual,NH4}} = (\Delta WP - U_{p,NH4} - U_{p,NO3}) \cdot \frac{U_{a,\text{pot,NH4}}}{U_{a,\text{pot,NH4}} + U_{a,\text{pot,NO3}}} 
\]
\[
U_{a\text{-actual,NO3}} = (\Delta WP - U_{p,NH4} - U_{p,NO3}) \cdot \frac{U_{a,\text{pot,NO3}}}{U_{a,\text{pot,NH4}} + U_{a,\text{pot,NO3}}} 
\]

if \((\Delta WP \geq U_{p,NH4} + U_{p,NO3} + U_{a,\text{pot,NH4}} + U_{a,\text{pot,NO3}})\)
\[
U_{a\text{-actual,NH4}} = U_{a,\text{pot,NH4}}
\]
\[
U_{a\text{-actual,NO3}} = U_{a,\text{pot,NO3}}
\]

Finally, the total N uptake \((U)\), uptake of NH4\(^+\) \((U_{\text{NH4}})\) and NO3\(^-\) \((U_{\text{NO3}})\), are calculated as

\[
U = U_{p,NH4} + U_{p,NO3} + U_{a\text{-actual,NH4}} + U_{a\text{-actual,NO3}}
\]
\[
U_{\text{NH4}} = U_{p,NH4} + U_{a\text{-actual,NH4}}
\]
\[
U_{\text{NO3}} = U_{p,NO3} + U_{a\text{-actual,NO3}}
\]

3.3.4 Litterfall

Nitrogen litterfall from the vegetation components is directly tied to the carbon litterfall calculated by the phenology module of CLASSIC through their current C:N ratios.

\[
LF_i = \frac{(1-r_L) LF_{i,C}}{C:N_i}, i = L, S, R
\]

where \(LF_{i,C}\) is the carbon litterfall rate (gC day\(^{-1}\)) for component \(i\), calculated by the phenology module of CLASSIC, and division by its current C:N ratio yields the nitrogen litterfall rate, \(r_L\) [see Table A1] is the leaf resorption coefficient that simulates the resorption of N from leaves of deciduous tree PFTs before they are shed and \(r_L = 0, i = R, S\). Litter from each vegetation
component is proportioned between structural and non-structural components according to their pool sizes.

### 3.3.5 Allocation and reallocation

Plant N uptake by roots is allocated to leaves and stem to satisfy their N demand. When plant N demand is greater than zero, total N uptake \((U)\) is divided between leaves, stem, and root components in proportion to their demands such that the allocation fractions for N \((a_i, i = L, S, R)\) are calculated as

\[
a_i = \frac{A_i}{\text{AWP}}, \; i = L, S, R
\]

\[A_{R2L} = a_L (U_{NH4} + U_{NO3})\]

\[A_{R2S} = a_S (U_{NH4} + U_{NO3})\]  \(12\)

where \(A_{R2L}\) and \(A_{R2S}\) are the amounts of N allocated from root to leaves and stem components, respectively, as shown in equations (A5) and (A7). During periods of negative NPP due to adverse climatic conditions (e.g., during winter or drought seasons) the plant N demand is set to zero but passive N uptake, associated with transpiration, may still be occurring if the leaves are still on. Even though there is no N demand, passive N uptake still needs to be partitioned among the vegetation components. During periods of negative NPP allocation fractions for N are, therefore, calculated in proportion to the minimum PFT-dependent C:N ratios of the leaves, stem, and root components as follows.

\[
a_i = \frac{\frac{1}{C:N_{i,\min}}}{\frac{1}{C:N_{L,\min}} + \frac{1}{C:N_{S,\min}} + \frac{1}{C:N_{R,\min}}}, \; i = L, S, R
\]  \(13\)

For grasses, which do not have a stem component, equations (12) and (13) are modified accordingly by removing the terms associated with the stem component.
Three additional rules override these general allocation rule specifically for deciduous tree PFTs (or deciduous PFTs in general). First, no N allocation is made to leaves once leaf fall is initiated for deciduous tree PFTs and plant N uptake is proportioned between stem and root components based on their demands in a manner similar to equation (12). Second, for deciduous tree PFTs, a fraction of leaf N is resorbed from leaves back into stem and root as follows

\[
R_{L2R} = r_L L_F \frac{N_{\text{NS}}}{N_{\text{NS}} + N_{\text{NS}}} \\
R_{L2S} = r_L L_F \frac{N_{\text{NS}}}{N_{\text{NS}} + N_{\text{NS}}}
\]

where \( r_L \) is the leaf resorption coefficient, as mentioned earlier, and \( L_F \) is the leaf litter fall rate.

Third, and similar to resorption, at the time of leaf onset for deciduous tree PFTs, N is reallocated to leaves (in conjunction with reallocated carbon as explained in Asaadi et al. (2018)) from stem and root components.

\[
R_{R2L} = \frac{R_{R2LC}}{C_{NL}} \frac{N_{\text{NS}}}{N_{\text{NS}} + N_{\text{NS}}} \\
R_{S2L} = \frac{R_{S2LC}}{C_{NL}} \frac{N_{\text{NS}}}{N_{\text{NS}} + N_{\text{NS}}}
\]

where \( R_{R2LC} \) and \( R_{S2LC} \) represent reallocation of carbon from non-structural stem and root components to leaves and division by \( C_{NL} \), converts the flux into N units. This reallocated N, at the time of leaf onset, is proportioned between non-structural pools of stem and root according to their sizes.

### 3.3.6 N mineralization, immobilization, and humification
Decomposition of litter \( (R_{L,D}) \) and soil organic matter \( (R_{S,M}) \) releases C to the atmosphere and this flux is calculated by the heterotrophic respiration module of CLASSIC. The litter and soil carbon decomposition rates used here are the same as in the standard model version (Melton and Arora, 2016; their Table A3). The amount of N mineralized is calculated straightforwardly by division with the current C:N ratios of the respective pools and contributes to the NH\(_4^+\) pool.

\[
M_{D,NH4} = \frac{R_{L,D}}{C:N_D} \\
M_{H,NH4} = \frac{R_{S,H}}{C:N_H}
\]  

An implication of mineralization contributing to the NH\(_4^+\) pool, in addition to BNF and fertilizer inputs that also contribute solely to the NH\(_4^+\) pool, is that the simulated NH\(_4^+\) pool is typically larger than the NO\(_3^-\) pool. The exception is the dry and arid regions where the lack of denitrification, as discussed below in Section 3.4.2., leads to a build-up of the NO\(_3^-\) pool.

Immobilization of mineral N from the NH\(_4^+\) and NO\(_3^-\) pools into the soil organic matter pool is meant to keep the soil organic matter C:N ratio \( (C:N_{SO}) \) at its specified value of 13 for all PFTs in a manner similar to Wania et al. (2012) and Zhang et al. (2018). A value of 13 is within the range of observation-based estimates which vary from about 8 to 25 (Zinke et al., 1998; Tipping et al., 2016). Although \( C:N_H \) varies geographically, the driving factors behind this variability remain unclear. It is even more difficult to establish if increasing atmospheric CO\(_2\) is changing \( C:N_H \) given the large heterogeneity in soil organic C and N densities, and the difficulty in measuring small trends for such large global pools. We therefore make the assumption that the \( C:N_H \) does not change with time. An implication of this assumption is that as GPP increases with increasing atmospheric CO\(_2\) rises, and plant litter becomes enriched in C with increasing C:N ratio.
of litter, more and more N is locked up in the soil organic matter pool because its C:N ratio is fixed. As a result, mineral N pools of NH$_4^+$ and NO$_3^-$ decrease in size and plant N content subsequently follows. This is consistent with studies of plants grown in elevated CO$_2$ environment. For example, Cotrufo et al. (1998) summarize results from 75 studies and find an average 14% reduction in N concentration for above-ground tissues. Wang et al. (2019) find increased C concentration by 0.8–1.2% and a reduction in N concentration by 7.4–10.7% for rice and winter wheat crop rotation system under elevated CO$_2$. Another implication of using specified fixed C:N ratio is that it does not matter if plant N uptake or immobilization is given preferred access to the mineral N pool since in the long term, by design, N will accumulate in the soil organic matter in response to atmospheric CO$_2$ increase.

Immobilization from both the NH$_4^+$ and NO$_3^-$ pools (gN m$^{-2}$ day$^{-1}$) is calculated in proportion to their pool sizes, employing the fixed C:N$_H$ ratio as

$$O_{NH} = \max \left( 0, \left( \frac{C_H}{C_{NH}} - N_H \right) \frac{N_{NH}}{N_{NH} + N_{NO3}} \right) k_O$$

$$O_{NO3} = \max \left( 0, \left( \frac{C_H}{C_{NH}} - N_H \right) \frac{N_{NO3}}{N_{NH} + N_{NO3}} \right) k_O$$

(17)

where $k_O$ is rate constant with a value of 1.0 day$^{-1}$. Finally, the carbon flux of humified litter from the litter to the soil organic matter pool ($H_{C,D2H}$) is also associated with a corresponding N flux that depends on the C:N ratio of the litter pool.

$$H_{N,D2H} = \frac{N_{C,D2H}}{C_{N_D}}$$

(18)

3.4 N cycling in mineral pools and N outputs
This section presents the parameterizations of nitrification (which results in transfer of N from the NH$_4^+$ to the NO$_3^-$ pool) and the associated gaseous fluxes of N$_2$O and NO (referred to as nitrifier denitrification), gaseous fluxes of N$_2$O, NO, and N$_2$ associated with denitrification, volatilization of NH$_4^+$ into NH$_3$, and leaching of NO$_3^-$ in runoff.

### 3.4.1 Nitrification

Nitrification, the oxidative process converting ammonium to nitrate, is driven by microbial activity and as such constrained both by high and low soil moisture (Porporato et al., 2003). At high soil moisture content there is little aeration of soil and this constrains aerobic microbial activity, while at low soil moisture content microbial activity is constrained by moisture limitation. In CLASSIC, the heterotrophic respiration from soil carbon is constrained similarly but rather than using soil moisture the parameterization is based on soil matric potential (Arora, 2003; Melton et al., 2015). Here, we use the exact same parameterization. In addition to soil moisture, nitrification (gN m$^{-2}$ day$^{-1}$) is modelled as a function of soil temperature and the size of the NH$_4^+$ pool as follows

$$I_{NO3} = \eta f_1(T_{0.5}) f_2(\psi) N_{NH4}$$

(19)

where $\eta$ is the nitrification coefficient (day$^{-1}$, see Table A1), $f_2(\psi)$ is the dimensionless soil moisture scalar that varies between 0 and 1 and depends on soil matric potential ($\psi$), $f_1(T_{0.5})$ is the dimensionless soil temperature scalar that depends on soil temperature ($T_{0.5}$) averaged over the top 0.5 m soil depth over which nitrification is assumed to occur (following Xu-Ri and Prentice, 2008), and $N_{NH4}$ is the ammonium pool size (gN m$^{-2}$), as mentioned earlier. Both $f_1(T_{0.5})$ and

**Deleted:** average
$f_i(\psi)$ are parameterized following Arora (2003) and Melton et al. (2015). $f_i(T_{0.5})$ is a $Q_{10}$ type function with a temperature dependent $Q_{10}$

$$f_i(T_{0.5}) = Q_{10,i}^{(70_{0.5} - 20)/10}, Q_{10,i} = 1.44 + 0.56 \left( \tanh \left( 0.075(46 - T_{0.5}) \right) \right)$$  \hspace{1cm} (20)

The reference temperature for nitrification is set to 20 °C following Lin et al. (2000). $f_i(\psi)$ is parameterized as a step function of soil matric potential ($\psi$) as

$$f_i(\psi) = \begin{cases} 0.5 & \text{if } \psi \leq \psi_{sat} \\ 1 - 0.5 \frac{\log(0.4) - \log(\psi)}{\log(0.4) - \log(\psi_{sat})} & \text{if } 0.4 > \psi \geq \psi_{sat} \\ 1 & \text{if } 0.6 \geq \psi \geq 0.4 \\ 1 - 0.8 \frac{\log(\psi) - \log(0.6)}{\log(100) - \log(0.6)} & \text{if } 100 > \psi > 0.6 \\ 0.2 & \text{if } \psi > 100 \end{cases}$$  \hspace{1cm} (21)

where the soil matric potential ($\psi$) is found, following Clapp and Hornberger (1978), as a function of soil moisture ($\theta$)

$$\psi(\theta) = \psi_{sat} \left( \frac{\theta}{\theta_{sat}} \right)^{-B}.$$  \hspace{1cm} (22)

Saturated matric potential ($\psi_{sat}$), soil moisture at saturation (i.e., porosity) ($\theta_{sat}$), and the parameter $B$ are calculated as functions of percent sand and clay in soil following Clapp and Hornberger (1978) as shown in Melton et al. (2015). The soil moisture scalar $f_i(\psi)$ is calculated individually for each soil layer and then averaged over the soil depth of 0.5 m over which nitrification is assumed to occur.

Gaseous fluxes of NO ($I_{NO}$) and N$_2$O ($I_{N2O}$) associated with nitrification, and generated through nitrifier denitrification, are assumed to be directly proportional to the nitrification flux ($I_{NO}$) as
where \( \eta_{NO} \) and \( \eta_{N2O} \) are dimensionless fractions (see Table A1) which determine what fractions of nitrification flux are emitted as NO and N\(_2\)O.

### 3.4.2 Denitrification

Denitrification is the stepwise microbiological reduction of nitrate to NO, N\(_2\)O, and ultimately to N\(_2\) in complete denitrification. Unlike nitrification, however, denitrification is primarily an anaerobic process (Tomasek et al., 2017) and therefore occurs when soil is saturated. As a result, we use a different soil moisture scalar than for nitrification. Similar to nitrification, denitrification is modelled as a function of soil moisture, soil temperature and the size of the NO\(_3^-\) pool as follows to calculate the gaseous fluxes of NO, N\(_2\)O, and N\(_2\).

\[
\begin{align*}
E_{NO} &= \mu_{NO} \, f_E(T_{0.5}) \, f_E(\theta) \, N_{NO3} \\
E_{N2O} &= \mu_{N2O} \, f_E(T_{0.5}) \, f_E(\theta) \, N_{NO3} \\
E_{N2} &= \mu_{N2} \, f_E(T_{0.5}) \, f_E(\theta) \, N_{NO3}
\end{align*}
\]  

(24)

where \( \mu_{NO}, \mu_{N2O}, \) and \( \mu_{N2} \) are coefficients (day\(^{-1} \)), see Table A1) that determine daily rates of emissions of NO, N\(_2\)O, and N\(_2\). The temperature scalar \( f_E(T_{0.5}) \) is exactly the same as the one for nitrification \( (f(f(T_{0.5}))) \) since denitrification is also assumed to occur over the same 0.5 m soil depth. The soil moisture scalar \( f_E(\theta) \) is given by

\[
\begin{align*}
f_E(\theta) &= 1 - \tanh \left( 2.5 \left( \frac{1 - w(\theta)}{1 - w_d} \right)^2 \right) \\
w(\theta) &= \max \left( 0, \min \left( \frac{\theta - \theta_m}{\theta_f - \theta_m}, 1 \right) \right)
\end{align*}
\]  

(25)
where \( w \) is the soil wetness that varies between 0 and 1 as soil moisture varies between wilting point \((\theta_w)\) and field capacity \((\theta_f)\), and \( w_d \) [see Table A1] is the threshold soil wetness for denitrification below which very little denitrification occurs. Since arid regions are characterized by low soil wetness values, typically below \( w_d \), this leads to build up of the NO\(_3^-\) pool in arid regions.

### 3.4.3 NO\(_3^-\) leaching

Leaching is the loss of water-soluble ions through runoff. In contrast to positively charged \( \text{NH}_4^+ \) ions (i.e. cations), the NO\(_3^-\) ions do not bond to soil particles because of the limited exchange capacity of soil for negatively charged ions (i.e., anions). As a result, leaching of N in the form of NO\(_3^-\) ions is a common water quality problem, particularly over cropland regions. The leaching flux \( L_{NO3}, \text{gN m}^{-2} \text{ day}^{-1} \) is parameterized to be directly proportional to baseflow \( b_t, \text{Kg m}^{-2} \text{s}^{-1} \) calculated by the physics module of CLASSIC and the size of the NO\(_3^-\) pool \( N_{NO3}, \text{gN m}^{-2} \).

Baseflow is the runoff rate from the bottommost soil layer.

\[
L_{NO3} = 86400 \varphi b_t N_{NO3} \quad (26)
\]

where the multiplier 86400 converts units to per day, and \( \varphi \) is the leaching coefficient \( \text{m}^2 \text{ Kg}^{-1} \) that can be thought of as the soil particle surface area \( \text{m}^2 \) that 1 Kg of water (or about 0.001 m\(^3\)) can effectively wash to leach the nutrients.

### 3.4.4 NH\(_3\) volatilization
NH$_3$ volatilization ($V_{NH_3}$, gN m$^{-2}$ day$^{-1}$) is parametrized as a function of pool size of NH$_4^+$, soil temperature, soil pH, aerodynamic and boundary layer resistances, and atmospheric NH$_3$ concentration in a manner similar to Riddick et al. (2016) as

$$V_{NH_3} = \theta \times 86400 \frac{1}{r_a + r_b}(\chi - [NH_3])$$  \hspace{1cm} (27)$$

where $\theta$ is the dimensionless NH$_3$ volatilization coefficient (see Table A1) which is set to less than 1 to account for the fact that a fraction of ammonia released from the soil is captured by vegetation, $r_a$ (s m$^{-1}$) is the aerodynamic resistance calculated by the physics module of CLASSIC, $\chi$ is the ammonia (NH$_3$) concentration at the interface of the top soil layer and the atmosphere (g m$^{-3}$), $[NH_3]$ is the atmospheric NH$_3$ concentration specified at 0.3 x 10$^{-6}$ g m$^{-3}$ following Riddick et al. (2016), 86400 converts flux units from gN m$^{-2}$ s$^{-1}$ to gN m$^{-2}$ day$^{-1}$, and $r_b$ (s m$^{-1}$) is the boundary layer resistance calculated following Thom (1975) as

$$r_b = 6.2 \times u_*^{0.67}$$  \hspace{1cm} (28)$$

where $u_*$ (m/s) is the friction velocity provided by the physics module of CLASSIC. The ammonia (NH$_3$) concentration at surface ($\chi$), in a manner similar to Riddick et al. (2016), is calculated as

$$\chi = 0.26 \frac{N_{NH_4}}{1 + KH[H^+]/[KH_4]}$$  \hspace{1cm} (29)$$

where the coefficient 0.26 is the fraction of ammonium in the top 10 cm soil layer assuming exponential distribution of ammonium along the soil depth (given by $3e^{-3z}$, where $z$ is the soil depth), $K_H$ (dimensionless) is the Henry’s law constant for NH$_3$, $K_{NH_4}$ (mol L$^{-1}$) is the dissociation equilibrium constant for aqueous NH$_3$, and $H^+$ (mol L$^{-1}$) is the concentration of hydrogen ion.
that depends on the soil pH ($H^+ = 10^{-pH}$). $K_H$ and $K_{NH4}$ are modelled as functions of soil temperature of the top 10 cm soil layer ($T_{0.1}$) following Riddick et al. (2016) as

$$K_H = 4.59 \, T_{0.1} \exp \left( 4092 \left( \frac{1}{T_{0.1}} - \frac{1}{T_{ref,H}} \right) \right)$$

$$K_{NH4} = 5.67 \times 10^{-10} \exp \left( -6286 \left( \frac{1}{T_{0.1}} - \frac{1}{T_{ref,\text{NH4}}} \right) \right)$$

(30)

where $T_{ref,H}$ is the reference temperature of 298.15 K.

3.5 Coupling of C and N cycles

As mentioned earlier, the primary objective of coupling of C and N cycles is to be able to simulate $V_{\text{max}}$ as a function of leaf N content ($N_i$) for each PFT. This coupling is represented through the following relationship

$$V_{\text{max}} = \Lambda \left( \Gamma_1 N_L + \Gamma_2 \right)$$

(21)

where $\Gamma_1$ (13 $\mu$mol CO$_2$ gN$^{-1}$ s$^{-1}$) and $\Gamma_2$ (8.5 $\mu$mol CO$_2$ m$^{-2}$ s$^{-1}$) are global constants, except for the broadleaf evergreen tree PFT for which a lower value of $\Gamma_1$ (5.1 $\mu$mol CO$_2$ gN$^{-1}$ s$^{-1}$) is used as discussed below. $\Lambda$ ($\leq 1$) is a scalar that reduces calculated $V_{\text{max}}$ when C:N ratio of any plant component (C: N$_i$, $i = L, S, R$) exceeds its specified maximum value (C: N$_{i,max}$, $i = L, S, R$) (see Table AA1).

$$\Lambda = \exp \left( -\omega K_\lambda \right)$$

$$\omega = e_1 b_L + e_2 b_S + e_3 b_R$$

(32)

Moved down [2]: The rates of change of N in the NH$_4^+$ and NO$_3^-$ pools (in gN m$^{-2}$ day$^{-1}$), $N_{NH4}$ and $N_{NO3}$, respectively, are given by

$$\frac{dN_{NH4}}{dt} = -V_{NH4} - \left( V_{NH4} + V_{NO3} + V_{NH4} + M_{NH4} \right) \cdot \left( \frac{NH4}{K_{NH4}} \right)$$

(4)$\dagger$

$$\frac{dN_{NO3}}{dt} = -V_{NO3} + \left( V_{NO3} + V_{NO3} + V_{NO3} + M_{NO3} \right) \cdot \left( \frac{NO3}{K_{NO3}} \right) - \left( \Sigma \left( B_{NH4} \cdot \left( B_{NH4} + B_{NO3} + M_{NH4} + M_{NO3} \right) \cdot \left( \frac{NO3}{K_{NO3}} \right) \right) \right)$$

(5)$\dagger$

and all fluxes are represented in units of gN m$^{-2}$ day$^{-1}$. $B_{NH4}$ is the rate of biological N fixation which solely contributes to the NH$_4^+$ pool. $F_{NH4}$ is the fertilizer input which is assumed to contribute only to the NH$_4^+$ pool, and $P_{NH4}$ and $P_{NO3}$ are atmospheric deposition rates that contribute to the NH$_4^+$ and NO$_3^-$ pools, respectively. Biological N fixation, fertilizer input, and atmospheric deposition are the three routes through which N enters the coupled soil-vegetation system. $M_{NH4}$ and $M_{NO3}$ are the mineralization flux from the litter and soil organic matter pools, respectively, associated with their decomposition. We assume mineralization of humus and litter pools only contributes to the NH$_4^+$ pool. $O_{NH4}$ and $O_{NO3}$ indicate immobilization of N from the NH$_4^+$ and NO$_3^-$ pools, respectively, to the humus N pool which implies microbes (that are not represented explicitly) are part of the humus pool. Combined together the terms ($M_{NH4} + N_{NH4} - O_{NH4} - O_{NO3}$) yield the net mineralization rate. $V_{NH3}$ is the rate of ammonia (NH$_3$) volatilization and $L_{NO3}$ is the leaching of N that occurs only from the NO$_3^-$ pool. The positively charged ammonium ions are attracted to the negatively charged soil particles and as a result it is primarily the negatively charged nitrate ions that leach through the soil (Porporato et al., 2003; Xu-Ri and Prentice, 2008). $U_{NH4}$ and $U_{NO3}$ are uptakes of NH$_4^+$ and NO$_3^-$ by plants, respectively. The nitrification flux from NH$_4^+$ to NO$_3^-$ pool is represented by $F_{NH3}$ which also results in the release of the nitrous oxide (N$_2$O), a greenhouse gas, and nitric oxide (NO) through nitrifier denitrification represented by the terms $L_{NO3}$ and $I_{NO}$, respectively. Finally, $E_{NH3}$, $E_{NO2}$, and $E_{NO}$ are the gaseous losses of N$_2$ (nitrogen gas), N$_2$O, and NO from the NO$_3^-$ pool associated with denitrification. N is thus lost through the soil-vegetation system via leaching in runoff and through gaseous losses of $L_{NO3}$, $E_{NH3}$, $E_{NO2}$, $E_{NO}$, and $V_{NH3}$. $\dagger$

The structural and non-structural N pools in root are written as $N_{S,R}$ and $N_{L,R}$, respectively, and similarly for stem ($N_{S,L}$ and $N_{L,L}$) and leaves ($N_{S,L}$ and $N_{L,L}$), and together the structural and non-structural pools make the total N pool in leaf ($N_L = N_{S,L} + N_{L,L}$), root ($N_R = N_{S,R} + N_{L,R}$), and stem ($N_S = N_{S,L} + N_{S,R}$).

Deleted: in Section 2.1.2

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\[ e_i = \max \left( 0, C; N_i - C; N_{i,\max} \right) \]
\[ b_i = \frac{1}{1 / C; N_{i,\max} + 1 / C; N_{i,\max} + 1 / C; N_{i,R,\max}}, \quad i = L, S, R \]

where \( k_A \) is a dimensionless parameter (see Table A1) and \( \omega \) is dimensionless term that represents excess C:N ratios above specified maximum thresholds \((e_i, i = L, S, R)\) weighted by \( b_i, i = L, S, R\). When plant components do not exceed their specified maximum C:N ratio thresholds, \( e_i \) is zero and \( A \) is one. When plants components exceed their specified maximum C:N ratio thresholds, \( A \) starts reducing below one. This decreases \( V_{\text{max}} \) and thus photosynthetic uptake which limits the rate of increase of C:N ratio of plant components, depending on the value of \( k_A \).

The linear relationship between photosynthetic capacity and \( N_i \) (Evans, 1989; Field and Mooney, 1986; Garnier et al., 1999) [used in equation 31] and between photosynthetic capacity and leaf chlorophyll content (Croft et al., 2017) is empirically observed. We have avoided using PFT-dependent values of \( \Gamma_1 \) and \( \Gamma_2 \) for easy optimization of these parameter values but also because such an optimization can potentially hide other model deficiencies. More importantly, using PFT-independent values of \( \Gamma_1 \) and \( \Gamma_2 \) yields a more elegant framework whose successful evaluation will provide confidence in the overall model structure.

As shown later in the results section, using \( \Gamma_1 \) and \( \Gamma_2 \) as global constants yields GPP values that are higher in the tropical region than an observation-based estimate. This is not surprising since tropical and mid-latitude regions are known to be limited by \( P \) (Vitousek, 1984; Aragão et al., 2009; Vitousek et al., 2010; Du et al., 2020) and our framework currently doesn’t model \( P \) cycle explicitly. An implication of productivity that is limited by \( P \) is that changes in \( N_L \) are less...
important. In the absence of explicit treatment of the P cycle, we therefore simply use a lower value of $\Gamma_1$ for the broadleaf evergreen tree PFT which, in our modelling framework, exclusively represents a tropical PFT. Although, a simple way to express P limitation, this approach yields the best comparison with observation-based GPP, as shown later, because the effect of P limitation is most pronounced in the high productivity tropical regions.

The second pathway of coupling between the C and N cycles occurs through mineralization of litter and soil organic matter. During periods of higher temperature, heterotrophic C respiration fluxes increase from the litter and soil organic matter pools and this in turn implies an increased mineralization flux (via equation 16), leading to more mineral N available for plants to uptake.

4.0 Methodology

4.1 Model simulations and input data sets

We perform CLASSIC model simulations with the N cycle for the pre-industrial period followed by several simulations for the historical 1851-2017 period to evaluate the model’s response to different forcings, as summarized below. The simulation for the pre-industrial period uses forcings that correspond to year 1850 and the model is run for thousands of years until its C and N pools come into equilibrium. Global thresholds of net atmosphere-land C flux of 0.05 Pg/yr and net atmosphere-land N flux of 0.5 Tg N/yr are used to ensure the model pools have reached equilibrium. The pre-industrial simulation, therefore, yields the initial conditions from which the historical simulations for the period 1851-2017 are launched. To spin the mineral N pools to their initial values, the plant N uptake and other organic processes were turned off while
the model used specified values of $V_{\text{cmax}}$ and only the inorganic part of N cycle was operative.

Once the inorganic mineral soil N pools reached near equilibrium, the organic processes were turned on. The model also uses an accelerated spin up procedure for the slow pools of soil organic matter and mineral N. The input and output terms are multiplied by a factor greater than one and this magnifies the change in pool size and therefore accelerates the spin up. Once the model pools reach near equilibrium, the factor is set back to one.

To evaluate the model’s response to various forcings over the historical period we perform several simulations turning on one forcing at a time as summarized in Table 1. The objective of these simulations is to see if the model response to individual forcings is consistent with expectations. For example, in the CO2-only simulation only atmospheric CO2 concentration increases over the historical period, while all other forcings stay at their 1850 levels. In the N-DEP-only simulation only N deposition increases over the historical period, and similarly for other runs in Table 1. A “FULL” simulations with all forcings turned on is then also performed which we compare to the original model without a N cycle which uses the photosynthesis downregulation parameterization (termed “ORIGINAL” in Table 1). Finally, a separate pre-industrial simulation is also performed that uses the same $\Gamma_{1}$ and $\Gamma_{2}$ globally (FULL-no-implicit-P-limitation). This simulation is used to illustrate the effect of neglecting P limitation for the broadleaf evergreen tree PFT in the tropics.

For the historical period, the model is driven with time-varying forcings that include CO2 concentration, population density (used by the fire module of the model for calculating anthropogenic fire ignition and suppression), land cover, and meteorological data. In addition, for the N cycle module, the model requires time-varying atmospheric N deposition and fertilizer
The atmospheric CO2 and meteorological data (CRU-JRA) are same as those used for the TRENDY model intercomparison project for terrestrial ecosystem models for year 2018 (Le Quéré et al., 2018). The CRU-JRA meteorological data is based on 6-hourly Japanese Reanalysis (JRA). However, since reanalysis data typically do match observations, they are adjusted for monthly values based on the Climate Research Unit (CRU) data. This yields a blended product with sub-daily temporal resolution that comes from the reanalysis and monthly means/sums that match the CRU data to yield a meteorological product that can be used by models that require sub-daily or daily meteorological forcing. These data are available for the period 1901-2017. Since no meteorological data are available for the 1850-1900 period, we use 1901-1925 meteorological data repeatedly for this duration and also for the pre-industrial spin up. The assumption is that since there is no significant trend in the CRU-JRA data over this period, these data can be reliably used to spin up the model to equilibrium. The land cover data used to force the model are based on a geographical reconstruction of the historical land cover driven by the increase in crop area following Arora and Boer (2010) but using the crop area data prepared for the Global Carbon Project (GCP) 2018 following Hurtt et al. (2006). Since land cover is prescribed, the competition between PFTs for space for the simulations reported here is switched off. The population data for the period 1850-2017 are based on Klein Goldewijk et al. (2017) and obtained from ftp://ftp.pbl.nl/..../hyde/hyde3.2/baseline.zip. The time-independent forcings consist of soil texture and permeable depth data.

Time-varying atmospheric N deposition and fertilizer data used over the historical period are also specified as per the TRENDY protocol. The fertilizer data are based on the N2O model intercomparison project (NMIP) (Tian et al., 2018) and available for the period 1860-2014. For
the period before 1860, 1860 fertilizer application rates are used. For the period after 2014, fertilizer application rates for 2014 are used. Atmospheric N deposition data are from input4MIPs (https://esgf-node.llnl.gov/search/input4mips/) and are the same as used by models participating in CMIP6 for the historical period (1850-2014). For years 2015-2017 the N deposition data corresponding to those from representative concentration pathway (RCP) 8.5 scenario are used. Figure 2 shows the time series of global annual values of externally specified fertilizer input, and deposition of ammonium and nitrate, based on the TRENDY protocol, for the six primary simulations. Geographical distribution of these inputs are also shown for the last 20 years from the FULL simulation corresponding to the 1998-2017 period. In Figure 2 (panels a, c and e) ammonium and nitrate deposition, and fertilizer input stay at their pre-industrial level for simulations in which these forcings do not increase over the historical period. As mentioned earlier, N deposition is split evenly into ammonium and nitrate. The values in parenthesis in Figure 2a legend, and in subsequent time series plots, show average values over the 1850s, the last 20 years (1998-2017) of the simulations, and the change between these two periods. The present day values of fertilizer input and N deposition are consistent with other estimates available in the literature (Table 2). The fertilizer input rate in the simulation with all forcings except land use change (FULL-no-LUC, blue line), that is with no increase in crop area over its 1850 value, is 50 Tg N yr⁻¹ compared to 91 Tg N yr⁻¹ in the FULL simulation, averaged over the 1998-2017 period. The additional 41 Tg N yr⁻¹ of fertilizer input occurs in the FULL simulation due to the increase in crop area but also due to the increasing fertilizer application rates over the historical period. Geographical distribution of the fertilizer application rates in Figure 2b shows that they are concentrated in regions with crop area and with values as high as 16 gN m⁻² yr⁻¹.
especially in eastern China. The N deposition rates (Figure 2d, 2f) are more evenly distributed geographically than the fertilizer applications rates, as would be expected, since emissions are transported downstream from their point sources. Areas with high emissions like the eastern United States, India, eastern China, and Europe, however, still stand out as areas that receive higher N deposition.

4.2 Evaluation data sources

We compare globally-summed annual values of N pools and fluxes with observations and other models, and where available their geographical distribution and seasonality. In general, however, much less observation-based data are available to evaluate simulated terrestrial N cycle components than for C cycle components. As a result, N pools and fluxes are primarily compared to results from both observation-based studies and other modelling studies (Bouwman et al., 2013; Fowler et al., 2013; Galloway et al., 2004; Vitousek et al., 2013; Zaehle, 2013). Since the primary purpose of the N cycle in our framework is to constrain the C cycle, we also compare globally-summed annual values of GPP and net atmosphere-land CO₂ flux, and their zonal distribution with available observation-based and other estimates. The observation-based estimate of GPP is from Beer et al. (2010), who apply diagnostic models to extrapolate ground-based carbon flux tower observations from about 250 stations to the global scale. Observation-based net atmosphere-land CO₂ flux is from Global Carbon Project’s 2019 assessment (Friedlingstein et al., 2019).

5.0 Results

5.1 N inputs
Figure 3 (panels a, c, e) shows the time series of annual values BNF and its natural and anthropogenic components from the six primary simulations summarized in Table 1. BNF stays at its pre-industrial value of around 80 Tg N yr\(^{-1}\) in the CO2-only and N-DEP-only simulations. In the CLIM-only (indicated by magenta coloured line) and the FULL-no-LUC (blue line) simulations the change in climate, associated with increases in temperature and precipitation over the 1901-2017 period (see Figure A2 in the appendix), increases BNF to about 85 Tg N yr\(^{-1}\). In our formulation (equation 1) BNF is positively impacted by increases in temperature and precipitation. In the LUC+FERT-only simulation (dark green line) the increase in crop area contributes to an increase in global BNF with a value around 110 Tg N yr\(^{-1}\) for the present day, since a higher BNF per unit crop area is assumed than for natural vegetation. Finally, in the FULL simulation (red line) the 1998-2017 average value is around 117 Tg N yr\(^{-1}\) due both to changes in climate over the historical period and the increase in crop area. Our present day value of global BNF is broadly consistent with other modelling and data-based studies as summarized in Table 2.

Panels c and e in Figure 3 show the decomposition of the total terrestrial BNF into its natural (over non-crop PFTs) and anthropogenic (over C\(_3\) and C\(_4\) crop PFTs) components. The increase in crop area over the historical period decreases natural BNF from its pre-industrial value of 59 to 54 Tg N yr\(^{-1}\) for the present day as seen for the LUC+FERT-only simulation (green line) in Figure 3c, while anthropogenic BNF over agricultural area increases from 21 to 56 Tg N yr\(^{-1}\) (Figure 3e). Figure 3c and 3e show that the increase in BNF (Figure 3a) in the FULL simulation is caused primarily by an increase in crop area. Our present day values of natural and anthropogenic BNF are also broadly consistent with other modelling and data-based studies as summarized in Table 2.
Figure 3 (panels b, d, and f) shows the geographical distribution of simulated BNF, and its natural and anthropogenic components. The geographical distribution of BNF (Figure 3a) looks very similar to the current distribution of vegetation (not shown) with warm and wet regions showing higher values than cold and dry regions since BNF is parameterized as a function of temperature and soil moisture. Anthropogenic BNF only occurs in regions where crop area exists according to the specified land cover and it exhibits higher values than natural BNF in some regions because of its higher value per unit area (see section 3.2.1).

At the global scale, and for the present day, natural BNF (59 Tg N yr⁻¹) is overwhelmed by anthropogenic sources: anthropogenic BNF (60 Tg N yr⁻¹), fertilizer input (91.7 Tg N yr⁻¹), and atmospheric N deposition increase since the pre-industrial era (~45 Tg N yr⁻¹). Currently humanity fixes more N than the natural processes (Vitousek, 1994).

5.2 C and N pools, fluxes response to historical changes in forcings

To understand the model response to changes in various forcings over the historical period we first look at the evolution of global values of primary C and N pools, and fluxes, shown in Figures 4 through 8. Figure 4a shows the time evolution of global annual GPP values, the primary flux of C into the land surface, for the six primary simulations, the ORIGINAL simulation performed with the model version with no N cycle, and the ORIG-UNCONST simulation with no photosynthesis downregulation (see Table 1). The unconstrained increase in GPP (35.6 Pg C yr⁻¹ over the historical period) in the ORIG-UNCONST simulation (dark cyan line) is governed by the standard photosynthesis model equations following Farquhar et al. (1980) and Collatz et al. (1992) for C₃ and C₄ plants, respectively. Downregulation of photosynthesis in the ORIGINAL...
simulation (purple line) is modelled on the basis of equation (1), while in the FULL simulation (red line) photosynthesis downregulation results from a decrease in $V_{\text{cmax}}$ values (Figure 5d) due to a decrease in leaf N content (Figure 5b). We will compare the FULL and ORIGINAL simulations in more detail later. The simulations with individual forcings, discussed below, provide insight into the combined response of GPP to all forcings in the FULL simulation.

5.2.1 Response to increasing CO$_2$

The response of C and N cycles to increasing CO$_2$ in the CO2-only simulation (orange lines in Figure 4) is the most straightforward to interpret. A CO$_2$ increase causes GPP to increase by 7.5 Pg C yr$^{-1}$ above its pre-industrial value (Figure 4a), which in turn causes vegetation (Figure 4b), leaf (Figure 4c), and soil (Figure 4d) carbon mass to increase as well. The vegetation and leaf N amounts (orange line, Figures 5a and 5b), in contrast, decrease in response to increasing CO$_2$. This is because N gets locked up in the soil organic matter pool (Figure 5c) in response to an increase in the soil C mass (due to the increasing GPP), litter inputs which are now rich in C (due to CO$_2$ fertilization) but poor in N (since N inputs are still at their pre-industrial level), and the fact that the C:N ratio of the soil organic matter is fixed at 13. This response to elevated CO$_2$ which leads to increased C and decreased N in vegetation is consistent with meta-analysis of 75 field experiments of elevated CO$_2$ (Cotrufo et al., 1998). A decrease in N in leaves (orange line, Figure 5b) leads to a concomitant decrease in maximum carboxylation capacity ($V_{\text{cmax}}$) (orange line, Figure 5d) and as a result GPP increases at a much slower rate in the CO2-only simulation than in the ORIG-UNCONST simulation (Figure 4a). Due to the N accumulation in the soil organic matter pool, the NH$_4^+$ and NO$_3^-$ (Figures 5e and 5f) pools also decrease in size in the CO2-only simulation.
Figure 6 shows the time series of N demand, plant N uptake and its split between passive and active N uptakes. The plant N demand in the CO2-only simulation (Figure 6a, orange line) increases from its pre-industrial value of 1512 Tg N/yr to 1639 Tg N/yr for the present day since the increasing C input from increasing GPP requires higher N input to maintain preferred minimum C:N ratio of plant tissues. However, since mineral N pools decrease in size over the historical period in this simulation (Figures 5e and 5f), the total plant N uptake (Figure 6b) reduces. Passive plant N uptake is directly proportional to pool sizes of NH4+ and NO3− and therefore it reduces in response to increasing CO2. Active plant N uptake, which compensates for insufficient passive N uptake compared to the N demand, also eventually starts to decline as it also depends on mineral N pool sizes. The eventual result of increased C supply and reduced N supply is an increase in the C:N ratio of all plant components and litter (Figure 7). The pre-industrial total N uptake of around 960 Tg N/yr (Figure 6b) is lower than the pre-industrial N demand (1512 Tg N/yr, Figure 6a) despite the sum of global NH4 and NO3 pool sizes being around 4000 Tg N (Figures 5e and 5f). This is because of the mismatch between where the pools are high and where the vegetation actually grows and the fact that plant N uptake is limited by its rate. As a result, in our model, even in the preindustrial era vegetation is N limited.

Figure 8 shows the net mineralization flux (the net transfer of mineralized N from litter and humus pools to the mineral N pools as a result of the decomposition of organic matter), nitrification (N flux from NH4+ to the NO3− pool), and the gaseous and leaching losses from the mineral pools. The net mineralization flux reduces in the CO2-only simulation (Figure 8a, orange line) as N gets locked up in the soil organic matter. A reduction in the NH4+ pool size in response to increasing CO2 also yields a reduction in the nitrification flux over the historical period (Figure...
5.2.2 Response to changing climate

The perturbation due to climate change alone over the historical period in the CLIM-only simulation (magenta coloured lines in Figures 4 to 8) is smaller than that due to increasing CO2. In Figure 2a, changes in climate over the historical period increase GPP slightly by 3.60 Pg C yr⁻¹ which in turn slightly increases vegetation (including leaf) C mass (Figure 4b,c). The litter and soil carbon mass (Figure 4d), however, decrease slightly due to increased decomposition rates associated with increasing temperature (see Figure A2b). Both the increase in BNF due to increasing temperature (magenta line in Figure 2a), and the reduction in litter and soil N mass (Figure 5c) due to increasing decomposition and higher net N mineralization (Figure 8a, magenta line), make more N available. This results in a slight increase in vegetation and leaf N mass (Figures 5a and 5b) and the NH₄⁺ (Figure 5e) pool which is the primary mineral pool in soils under vegetated regions. The global NO₃⁻ pool, in contrast, decreases in the CLIM-only simulation (Figure 5f) with the reduction primarily occurring in arid regions where the NO₃⁻ amounts are very large (see Figure 2 that shows the geographical distribution of the primary C and N pools). The geographical distribution of NH₄⁺ (Figure 2a) generally follows the geographical distribution of BNF, but with higher values in areas where cropland exists and where N deposition is high. The geographical distribution of NO₃⁻ (Figure 2b) generally shows lower values than NH₄⁺ except in the desert regions where lack of denitrification leads to a large buildup of the NO₃⁻ pool. As
explained earlier in section 3.4.2). Although Figure 9 shows the geographical distribution of mineral N pools from the FULL simulation, the geographical distribution of pools are broadly similar between different simulations with obvious differences such as lack of hot spots of N deposition and fertilizer input in simulations in which these forcings stay at their pre-industrial levels. Figure 9 also shows the simulated geographical distribution of C and N pools in the vegetation and soil organic matter. The increase in GPP due to changing climate increases the N demand (Figure 6a, magenta line) but unlike the CO2-only simulation, the plant N uptake increases since the NH4+ and NO3− pools increase in size over the vegetated area in response to increased mineralization (Figure 8a, magenta line) and increased BNF (Figure 3a, magenta line).

The increase in plant N uptake comes from the increase in passive plant N uptake (Figure 6c) while the active plant N uptake reduces (Figure 6d). Active and passive plant N uptakes are inversely correlated. This is by design since active plant N uptake increases when passive plant N uptake reduces and vice-versa, although eventually both depend on the size of available mineral N pools. Enhancement of plant N uptake due to changes in climate, despite increases in GPP associated with a small increase in Vcmax (Figure 5d), leads to a small reduction in the C:N ratio of all plant tissues (Figure 7). The litter C:N, in contrast, shows a small increase since not all N makes its way to the litter as a specified fraction of 0.54 (Table A1) leaf N is resorbed from deciduous trees leaves prior to leaf fall (Figure 7e). Although the leaf C:N ratio decreases in the CLIM only simulation, in response to increased BNF and increased mineralization, this decrease is not large enough to overcome the effect of resorption and as a result the C:N litter increases.
Finally, the small increase in pool sizes of NH$_4^+$ and NO$_3^-$ leads to a small increase in leaching, volatilization, and gaseous losses associated with nitrification and denitrification (Figure 8).

**5.2.3 Response to N deposition**

The simulated response of GPP to changes in N deposition (brown line) over the historical period is smaller than that for CO$_2$ and climate (Figure 4a). The small increase in GPP of 2.0 Pg C yr$^{-1}$ leads to commensurately small increases in vegetation (Figure 4b) and litter plus soil (Figure 4d) C mass. Vegetation and leaf N mass (Figure 5a,b) also increase in response to N deposition and so do mineral pools of NH$_4^+$ and NO$_3^-$ (Figure 5e,f). The increase in GPP in the simulation with N deposition results from an increase in $V_{\text{max}}$ rates (Figure 5d) associated with an increase in leaf N content (Figure 5b). N demand increases marginally and so does plant N uptake in response to N deposition (Figure 6). As would be intuitively expected, the C:N ratio of the whole plant, its components of leaves, stem, and root, and litter decreases slightly in response to N deposition (Figure 7). Net N mineralization, nitrification, leaching, volatilization, and gaseous losses associated with nitrification and denitrification all increase in response to N deposition (Figure 8).

**5.2.4 Response to LUC and fertilizer input**

The simulated response to LUC, which reflects an increase in crop area, and increased fertilizer deposition rates over the historical period is shown by dark green lines in Figures 4 through 8. The increase in fertilizer input is a much bigger perturbation to the N cycle system than N deposition. Figure 2 shows that at the global scale the fertilizer inputs increase from 0 to
“92 Tg N/yr over the historical period, while the combined NH₄⁺ and NO₃⁻ N deposition rate increases from around 20 to 65 Tg N/yr. In addition, because of higher per unit area BNF rates over crop area than natural vegetation, the increase in crop area in this simulation leads to an increase in anthropogenic BNF from about 20 to 56 Tg N/yr over the historical period. All together increasing crop area and fertilizer inputs imply an additional ~130 Tg N/yr being input into the terrestrial N cycle at the present day since the pre-industrial period, compared to an increase of only 45 Tg N/yr for the N deposition forcing.

The global increase in fertilizer input over the historical period leads to higher NH₄⁺ and NO₃⁻ pools (Figures 5e and 5f). Although both fertilizer and BNF contribute to the NH₄⁺ pool, the NO₃⁻ pool also increases through the nitrification flux (Figure 8b). An increase in crop area over the historical period results in deforestation of natural vegetation that reduces vegetation biomass (Figure 4b). However, soil carbon mass also decreases (Figure 4d) despite higher litter inputs. This is because a higher soil decomposition rate is assumed over cropland areas to simulate soil carbon loss as empirical measurements of soil carbon show over deforested areas which are converted to croplands (Wei et al., 2014). Fertilizer application only occurs over crop areas which increases the Vcmax rates for crops and, as expected, this yields an increase in globally-averaged Vcmax (Figure 5d). A corresponding large increase in leaf N content (Figure 5b) is, however, not seen because vegetation (and therefore leaf) N (Figure 5a,b) is also lost through deforestation. In addition, Vcmax is essentially a flux (expressed per unit leaf area) that is averaged over the whole year while leaf and vegetation N pools are sampled at the end of each year and all crops in the northern hemisphere above 30° N are harvested before the year end. Vegetation N mass, in fact, decreases in conjunction with vegetation C mass (Figure 4b). Plant N demand
reduces (Figure 6a) and plant N uptake increases (Figure 6b) driven by crop PFTs in response to fertilizer input, as would be intuitively expected. The increase in plant N uptake comes from the increase in passive N uptake, in response to increases in pool sizes of NH₄⁺ and NO₃⁻ over crop areas, while active plant N uptake decreases since passive uptake can more than keep up with the demand over cropland area. While the C:N ratio of vegetation biomass decreases over cropland area, vegetation carbon mass (Figures 4b and 4d) in the FULL simulation are similarly driven by these three factors but, in addition, LUC contributes to decreases in vegetation and soil carbon mass as natural vegetation is deforested to accommodate for increases in crop area.

5.2.5 Response to all forcings

We can now evaluate and understand the simulated response of the FULL simulation to all forcings (red line in Figures 4 through 8). The increase in GPP in the FULL simulation (14.5 Pg C/yr) in Figure 4a over the historical period is driven by GPP increase associated with increase in CO₂ (7.5 Pg C/yr), changing climate (3.6 Pg C/yr), and N deposition (2.0 Pg C/yr). The increases associated with these individual forcings add up to 13.1 Pg C/yr indicating that synergistic effects between forcings contribute to the additional 1.4 Pg C/yr increase in GPP. The changes in vegetation and soil plus litter carbon mass (Figures 4b and 4d) in the FULL simulation are similarly driven by these three factors but, in addition, LUC contributes to decreases in vegetation and soil carbon mass as natural vegetation is deforested to accommodate for increases in crop area.
Vegetation and leaf N mass (Figures 5a and 5b) decrease in the FULL simulation driven primarily by the response to increasing CO₂ (orange line compared to the red line) while changes in litter and soil N mass are affected variably by all forcings (Figure 5c). Changes in \( V_{\text{max}} \) (Figure 5d) are similarly affected by all forcings: increasing CO₂ leads to a decrease in globally-averaged \( V_{\text{max}} \) values while changes in climate, N deposition, and fertilizer inputs lead to increases in \( V_{\text{max}} \) values with the net result being a small decrease over the historical period. The increase in global NH₄⁺ mass in the FULL simulation is driven primarily by the increase in fertilizer input (Figure 5e, red versus green line) while the changes in NO₃⁻ mass are primarily the result of changes in climate (Figure 5f, magenta line) which causes a decrease in NO₃⁻ mass from about 1940 to 1970 and N deposition and fertilizer input (Figure 5f, green and brown lines) which contribute to the increase in NO₃⁻ mass later on in the historical period. The increase in N demand (Figure 6a) over the historical period is also driven primarily by the increase in atmospheric CO₂. Plant N uptake (Figure 6b) decreases in response to increasing CO₂ but increases in response to changes in climate, N deposition, and fertilizer inputs such that the net change over the historical is a small decrease. The increase in the C:N ratio of vegetation and its components (leaves, stem, and root) is driven primarily by an increase in atmospheric CO₂ (Figure 7a, red versus orange line). Litter C:N in the FULL simulation, in contrast, does not change substantially over the historical period in a globally-averaged sense as the increase in the C:N ratio of litter associated with an increase in atmospheric CO₂ is mostly compensated by the decrease associated with an increase in N deposition and fertilizer application. The simulated change in global net N mineralization (Figure 8a) in the FULL simulation, over the historical period, is small since the decrease in net N mineralization due to increasing CO₂ (orange line) is compensated by the increase caused by...
changes in climate, N deposition, and fertilizer inputs (magenta, brown, and green lines respectively). The remaining fluxes of nitrification, NO$_3$ leaching, NH$_3$ volatilization, and gaseous losses associated with nitrification and denitrification in the FULL simulation (Figure 8) are all strongly influenced by fertilizer input (green line compared to red line).

Table 2 compares simulated values of all primary N pools and fluxes from the FULL simulation with other modelling and quasi observation-based studies. Simulated values are averaged over the 1998-2017 period. Where available, time-periods for other modelling and quasi observation-based studies to which estimates correspond are also noted. For the most part simulated pools and fluxes lie within the range of existing studies with the exception of N$_2$ and NO emissions that are somewhat higher.

5.2.6 Response to all forcings except LUC

The FULL-no-LUC simulation includes all forcings except LUC (blue line in Figures 4 through 8) and corroborates several of the points mentioned above. In this simulation crop area stays at its 1850 value. Figure 2b (blue line) shows increasing global fertilizer input in this simulation despite crop area staying at its 1850 value since fertilizer application rates per unit area increase over the historical period. In the absence of the LUC, vegetation C mass (Figure 4b) and soil plus litter C (Figure 4d) and N (Figure 5c) are higher in the FULL-no-LUC compared to the FULL simulation. N demand (Figure 6a) is slightly higher in FULL-no LUC than in FULL simulation because there is more standing vegetation biomass that is responding to increasing CO$_2$. The increase in volatilization, leaching, and gaseous losses associated with nitrification and denitrification (Figures 8c-8f) are all primarily caused by increased fertilizer input over the
specified 1850 crop area. The increase in N losses associated with these processes, over the historical period, is much lower in the FULL-no-LUC simulation than in the FULL simulation since crop area stays at its 1850 values.

5.3 Comparison of FULL and ORIGINAL simulations

We now compare the results from the FULL simulation that includes the N cycle with that from the ORIGINAL simulation that does not include the N cycle. Both simulations are driven with all forcings over the historical period. Figure 4a shows that the global GPP values in the FULL (red line) and ORIGINAL (purple line) simulations are quite similar although the rate of increase of GPP in the FULL simulation is slightly higher than in the ORIGINAL simulation. As a result, simulated global vegetation biomass is somewhat higher in the FULL simulation (Figure 4b). The simulated global litter and soil carbon mass (Figure 4d) is, however, lower in the FULL simulation (1073 Pg C) compared to the ORIGINAL simulation (1142 Pg C) and this decrease mainly comes from a decrease at higher latitudes (not shown) due to a decrease in GPP (Figure 10a). The lower GPP in the FULL simulation, combined with the slow decomposition at cold high latitudes, results in a lower equilibrium for litter and soil carbon compared with the ORIGINAL simulation. Litter mass contributes about 80 Pg C to the total dead carbon mass. Overall both estimates of 1073 Pg C and 1142 Pg C are somewhat lower than the bulk density corrected estimate of 1230 Pg C based on the Harmonized World Soil Database (HWSD) v.1.2 (Köchy et al., 2015). One reason for this is that CLASSIC does not yet represent permafrost related soil C processes.

Figure 10a shows that the zonal distribution of GPP from the FULL and ORIGINAL simulations, for the 1998-2017 period, compares reasonably well to the observation-based
estimate from Beer et al. (2010). The FULL simulation has slightly lower productivity at high-latitudes than the ORIGINAL simulation, as mentioned above. Overall, however, the inclusion of the N cycle does not change the zonal distribution of GPP in the model substantially, which is determined primarily by the geographical distribution of climate. Figure 10b compares the zonal distribution of GPP from the pre-industrial simulation (corresponding to 1850s) from the FULL and FULL-with-no-implicit-P-limitation simulations to illustrate the high GPP in the tropics where P and not N limitation affects GPP and the reason for choosing a lower value of \( \Gamma_1 \) in equation (31) for the broadleaf evergreen tree PFT.

The global GPP in the ORIGINAL and FULL simulations averaged over the period 1998-2017 (120.0 and 120.4 PgC/yr, respectively) are around 15% lower compared to that in the ORIG-UNCONST simulation (142 PgC/yr), as shown in Figure 4a, yielding a global downregulation factor of about 0.85. Figure 10c shows how downregulation works in the ORIGINAL and FULL simulations in a zonally-averaged sense. Ratios of annual GPP averaged over the 1998-2017 period from the ORIGINAL versus ORIG-UNCONST simulations, and FULL versus ORIG-UNCONST simulations were first calculated for each grid cell and then zonally-averaged over the land grid cells. Ratios can be misleading especially for grid cells with low values, for example, in the desert regions. In addition, these ratios also depend on the specified \( V_{\text{max}} \) values in the ORIG-UNCONST simulation. In Figure 10c, the purple line for the ORIGINAL simulation exhibits values around 0.8 consistent with the global downregulation of around 0.85 and the fact that the same scalar downregulation multiplier is used everywhere on the globe (equation 1). The red line for the FULL simulation, however, indicates a pattern of higher downregulation at high-latitudes. The peaks in red line, especially the one around 23°N (Sahara desert), are due to higher values in selected
grid cells in dry and arid regions where the build-up of NO₃ in the soil (due to reduced denitrification) increases V_{max} and thus GPP in the run with N cycle leading to higher ratios although the absolute GPP values still remain low.

Figure 11a compares globally-summed net atmosphere-land CO₂ flux from the FULL, FULL-no-LUC, and ORIGINAL simulations with quasi observation-based estimates from the 2019 Global Carbon Project (Friedlingstein et al., 2019). There are two kinds of estimates in Figure 11a from Friedlingstein et al. (2019): the first is the net atmosphere-land CO₂ flux for the decades spanning the 1960s to the 2000s which are shown as rectangular boxes with their corresponding mean values and ranges, and the second is the terrestrial sink from 1959 to 2018 (dark yellow line). Positive values indicate a sink of carbon over land and negative values a source. The difference between the net atmosphere-land CO₂ flux and the terrestrial sink is that the terrestrial sink minus the LUC emissions yields the net atmosphere-land CO₂ flux. The atmosphere-land CO₂ flux from the FULL-no-LUC simulation (blue line) is directly comparable to the terrestrial sink since 1959, since the FULL-no-LUC simulation includes no LUC, and shows that the simulated terrestrial sink compares fairly well to the estimates from Friedlingstein et al. (2019). Averaged over the period 1959-2017, the modelled and Global Carbon Project values are 2.0 and 2.1 Pg C/yr, respectively. The net atmosphere-land CO₂ flux from the FULL simulation mostly lies within the uncertainty range for the five decades considered, although it is on the higher side compared to estimates from Friedlingstein et al. (2019). The reason for this is that LUC emissions in CLASSIC are much lower than observation-based estimates, as discussed below in context of Figure 11c. CLASSIC simulates LUC emissions only in response to changes in crop area whereas changes in pasture area and wood harvesting also contribute to LUC emissions. The
net-atmosphere land CO$_2$ flux from the ORIGINAL simulation compares better with the estimates from Friedlingstein et al. (2019), than the FULL simulation, because the photosynthesis down-regulation parameter in the ORIGINAL simulation has been adjusted despite discrepancies in simulated LUC processes.

Figure 11b compares the zonal distribution of simulated net atmosphere-land CO$_2$ flux from the FULL and ORIGINAL simulations with the model-mean and range from the terrestrial ecosystem models that participated in the 2019 TRENDY model intercomparison and contributed results to 2019 Global Carbon Project (Friedlingstein et al., 2019). The carbon sink simulated by CLASSIC in the northern hemisphere is broadly comparable to the model-mean estimate from the TRENDY models. However, in the tropics CLASSIC simulates a much stronger sink than the model-mean, likely because of its lower LUC emissions.

### 5.4 Contribution of forcings to land C sink and sources

Figure 11c shows cumulative net atmosphere-land CO$_2$ flux for the 1850-2017 period from the six primary simulations with N cycle. These simulations facilitate the attribution of carbon uptake and release over the historical period to various forcings. The cumulative terrestrial sink in the FULL-no-LUC simulation for the period 1850-2017 is simulated to be ~153 Pg C and this compares reasonably well with the estimate of 185 ± 50 Pg C for the period 1850-2014 from Le Quéré et al. (2018). Increase in CO$_2$ (~115 Pg C), change in climate (~3 Pg C), and N deposition (~19 Pg C) all contribute to this terrestrial sink. These three contributions add up to 137 Pg C so the additional 16 Pg C is contributed by the synergistic effects between the three forcings.

Quantified in this way, the contribution of increasing CO$_2$ (115 out of 137 Pg C), climate change
(3 out of 137 Pg C), and N deposition (19 out of 137 Pg C) to carbon uptake by land over the historical period (1850-2017) is calculated to be 84%, 2%, and 14%, respectively. Cumulative LUC emissions simulated for the period 1850-2017 by CLASSIC can be estimated using a negative cumulative net-atmosphere-land CO2 flux of ~66 Pg C from the LUC+FERT-only simulation or by the differencing the FULL and FULL-no-LUC simulations (~71 Pg C). While LUC emissions are highly uncertain, both of these estimates are much lower than the 195 ± 75 Pg C estimate from Le Quéré et al. (2018).

6.0 Discussion and conclusions

The interactions between terrestrial C and N cycles are complex and our understanding of these interactions, and their representation in models, is based on empirical observations of various terrestrial ecosystem processes. In this paper, we have evaluated the response of these interactions by perturbing the coupled C and N cycle processes in the CLASSIC model with one forcing at a time over the historical period: 1) increase in CO₂, 2) change in climate, 3) increase in N deposition, and 4) LUC with increasing fertilizer input. These simulations are easier to interpret and the model response can be evaluated against both our conceptual knowledge as well as empirical observation-based data. Our assumption is that, if the model response to individual forcings is realistic and consistent with expectations based on empirical observations then the response of the model to all forcings combined will also be realistic and easier to interpret, although we do expect and see synergistic effects between forcings.

The simulated response of coupled C and N cycles in CLASSIC to increasing atmospheric CO₂ is an increase in the C:N ratio of vegetation components due to an increase in their C content.
but also a decrease in their N content. This model response is conceptually consistent with a meta-analysis of 75 field experiments of elevated CO2 as reported in Cotrufo et al. (1998) who find an average reduction in tissue N concentration of 14%. Most studies analyzed in the Cotrufo et al. (1998) meta-analysis used ambient CO2 of around 350 ppm and elevated CO2 of around 650-700 ppm. In comparison, the plant N concentration in CLASSIC reduces by ~26% in response to a gradual increase in atmospheric CO2 from 285 ppm to 407 ppm (an increase of 122 ppm) over the 1850-2017 period [whole plant C:N ratio increases from 142.6 to 194.1 in the CO2-only simulation, Figure 7a]. These two estimates cannot be compared directly - the majority (59%) of Free-Air Carbon dioxide Enrichment (FACE) experiments last less than 3 years (Jones et al., 2014) and the vegetation experiences a large CO2 change of around 300-350 ppm while the duration of our historical simulation is 167 years and the gradual increase in CO2 of 122 ppm over the historical period is much smaller.

The response of our model to CO2 increase over the historical period is also consistent with the meta-analysis of McGuire et al. (1995) who report an average decrease in leaf N concentration of 21% in response to elevated CO2 based on 77 studies, which is the primary reason for downregulation of photosynthetic capacity. The simulated decrease in leaf N concentration in our study for the CO2-only experiment is around 27% (leaf C:N ratio increases from 42.8 to 58.6 in the CO2-only simulation, Figure 7b). Although, the same caveats that apply to the comparison with the Cotrufo et al. (1998) study also apply to this comparison. The decrease in whole plant and leaf N concentrations in our results is conceptually consistent with the meta-analyses of McGuire et al. (1995) and Cotrufo et al. (1998). The decrease in whole plant N concentration in our CO2-only and FULL simulations is the result of an increase in both tissue
C amount and a decrease in N amount. The decrease in tissue N amount is, in fact, necessary in our modelling framework to induce the required downregulation of photosynthesis to simulate the land carbon sink realistically over the historical period.

The meta-analysis of Liang et al. (2016) reports an increase in above and belowground plant N pools in response to elevated CO₂ associated with increase in BNF but since their results are based on pool sizes they cannot be compared directly to the N concentration based results from McGuire et al. (1995) and Cotrufo et al. (1998). Liang et al. (2016) also report results from short-term (≤ 3 years) and long-term (between 3 to 15 years) studies separately (their Figure 3). They show that the increase in total plant and litter N pools become smaller for long-term studies. Regardless, the difference in time scales of empirical studies and the real world is a caveat that will always make it difficult to evaluate model results over long time scales.

The response of C and N cycles to changes in climate in our model (in the CLIM-only simulation) is also conceptually realistic. Globally, GPP increases in response to climate that gradually gets warmer and wetter (see Figure A2) and as a result vegetation biomass increases. Soil carbon mass, however, decreases (despite increase in NPP inputs) since warmer temperatures also increase heterotrophic respiration (not shown). As a result of increased decomposition of soil organic matter, net N mineralization increases and together with increased BNF the overall C:N ratio of vegetation and leaves decreases, which leads to a V_{max} increase. The small increase in V_{max} due to increased mineralization, thus also contributes to an increase in GPP over and above that due to a change in climate alone, and therefore compensates for the amount of carbon lost due to increased soil organic matter decomposition associated with warmer temperatures. This behaviour is consistent with land C cycle models showing a reduction

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in the absolute value of the strength of the carbon-climate feedback when they include coupling of C and N cycles (Arora et al., 2020).

The modelled differences in PFT specific values of $V_{\text{cmax}}$, in our framework, come through differences in simulated values of leaf N content ($N_i$) that depend on BNF (given that BNF is the primary natural source of N input into the coupled soil-vegetation system) but also differences in mineralization that are governed by climate. $N_i$ values, however, also depend on leaf phenology, allocation of carbon and nitrogen, turnover rates, transpiration (which brings in N through passive uptake), and almost every aspect of plant biogeochemistry which affects a PFT’s net primary productivity and therefore N demand. Modelled increases in GPP in response to N deposition come through an increase in leaf N content and therefore $V_{\text{cmax}}$ values.

Finally, changes in land use associated with an increase in crop area, and the associated increase in fertilizer application rates lead to the largest increase in NO$_3^-$ leaching, NH$_3$ volatilization, and gaseous losses associated with nitrification and denitrification among all forcings. Overall, the model response to perturbation by all individual forcings is realistic, conceptually expected, and of the right sign (positive or negative) although it is difficult to evaluate the magnitude of these responses in the absence of directly comparable observation-based estimates.

Despite the model responses to individual forcings that appears consistent with our conceptual understanding of coupled C and N cycles, our modelling framework misses an important feedback process that has been observed in the FACE and other experiments related to changes in natural BNF. FACE sites and other empirical studies report an increase in natural
BNF rates at elevated CO₂ (McGuire et al., 1995; Liang et al., 2016) and a decrease in natural BNF rates when additional N is applied to soils (Salvagiotti et al., 2008; Ochoa-Hueso et al., 2013). On a broad scale this is intuitively expected but the biological processes behind changes in BNF rates remain largely unclear. A response can still be parameterized even if the underlying physical and biological processes are not well understood. For instance, Goll et al. (2012) parameterize BNF as an increasing and saturating function of NPP, \( BNF = 1.8 \left(1.0 - \exp(-0.003NPP)\right) \). This approach, however, does not account for the driver behind the increase in NPP - increasing atmospheric CO₂, change in environmental conditions (e.g., wetter and warmer conditions), or increased N deposition. Clearly, increasing BNF if the NPP increase is due to N deposition is inconsistent with empirical observations. Over the historical period an increase in atmospheric CO₂ has been associated with an increase in N deposition so to some extent changes in BNF due to both forcings will cancel each other. We realize the importance of changes in BNF, given it is the single largest natural flux of N into the coupled soil-vegetation system yet highly uncertain, and aim to address these issues in a future version of the model by exploring existing BNF formulations. Meyerholt et al. (2016), for example, demonstrate the uncertainty arising from the use of five different BNF parameterizations in the context of the O-CN model. They use formulations that parameterize BNF as a function of 1) evapotranspiration, 2) NPP, 3) leaf C:N ratio, that takes into account energy cost for N fixation (Fisher et al., 2010), 4) plant N demand, and 5) an optimality-based approach that follows Rastetter et al. (2001) in which BNF only occurs when the carbon cost of N fixation is lower than the carbon cost of root N uptake. The approach used in our study is closest to the one that is based on evapotranspiration but makes the distinction in BNF rates over natural and agricultural areas.
The reduction of photosynthesis rates in response to N limitation is the most important linkage between C and N cycles and yet it too is parameterized differently across models. Given that leaf N content and photosynthetic capacity are strongly correlated (Evans, 1989; Field and Mooney, 1986; Garnier et al., 1999), photosynthesis downregulation due to N limitation reduces photosynthetic capacity, and thus the GPP flux. Yet models reduce both NPP (Wiltshire et al., 2020) and Vcmax rates, and thus GPP, (Zaehle and Friend, 2010; Wania et al., 2012; von Bloh et al., 2018) in response to N limitation. Vcmax rates may themselves be parameterized as a function leaf N content directly (von Bloh et al., 2018; Zaehle and Friend, 2010) or leaf C:N ratio (Wania et al., 2012). In this study, we have parameterized Vcmax rates as a function of leaf N content (equation 31) since the use of leaf C:N ratio leads to an incorrect seasonal variation of Vcmax. If an increase in leaf C:N ratio, as a result of increase in atmospheric CO2, leads to a decrease in Vcmax rates over the historical period then it implies that Vcmax is inversely related to leaf C:N ratios. Since leaf C:N ratio peak during the growing season (Li et al., 2017) this also implies Vcmax rates are lower during the growing season than at its start and this is in contrast to observations that show an increase in Vcmax during the growing season (e.g., see Fig. 1a of Bauerle et al., 2012).

Our framework assumes a constant C:N ratio of 13 for soil organic matter (C:Nsoil), an assumption also made in other models (e.g., Wania et al., 2012; Zhang et al., 2018). This assumption is also broadly consistent with Zhao et al. (2019) who attempt to model C:N of soil organic matter, among other soil properties, as a function of mean annual temperature and precipitation using machine learning algorithms (their Figure 2h). It is difficult to currently establish if increasing atmospheric CO2 is changing C:Nsoil given the large heterogeneity in soil organic C and N densities, and the difficulty in measuring small trends for such large global pools.
A choice of a somewhat different value for all PFTs or had we chosen specified constant PFT-dependent values of $C : N_H$ is of relatively less importance in this context since the model is spun to equilibrium for 1850 conditions anyway. It is the change in $C : N_H$ over time that is of importance. The assumption of constant $C : N_H$ is the key to yielding a decrease in vegetation N mass, and therefore leaf N mass and $V_{\text{max}}$, as CO$_2$ increases, in our framework. Without a decrease in $V_{\text{max}}$ in our modelling framework, in response to elevated CO$_2$, we cannot achieve the downregulation noted by McGuire et al. (1995) in their meta-analysis, and the simulated carbon sink over the historical period would be greater than observed as noted above. It is possible that we are simulating the reduction in leaf N mass, in response to elevated CO$_2$, for a wrong reason in which case our model processes need to be revisited based on additional empirical data. If our assumption of constant or extremely slowly changing $C : N_H$ is indeed severely unrealistic, this necessitates a point of caution that a realistic land carbon sink can be simulated over the historical period with such an assumption.

Related to this assumption is also the fact that we cannot make decomposition rates of soil organic matter a function of its C:N ratio since it is assumed to be a constant. It is well known that after climate, litter and soil organic matter decomposition rates are controlled by their C:N ratio (Manzoni et al., 2008). Litter decomposition rates can still be made a function of its C:N ratio and we aim to do this for a future model version.

The work presented in this study of coupling C and N cycles in CLASSIC yields a framework that we can build upon to make model processes more realistic, test the effect of various model assumptions, parameterize existing processes in other ways, include additional processes, and evaluate model response at FluxNet sites to constrain model parameters.
Appendix

A1. Budget equations for N pools

The rates of change of N in the NH₄⁺ and NO₃⁻ pools (in gN m⁻²), N₉₅₄ and N₉₅₃₄, respectively, are given by

\[ \frac{d N_{NH₄}}{dt} = B_{NH₄} + F_{NH₄} + P_{NH₄} + M_{D,NH₄} + M_{H,NH₄} \]
\[ - U_{NH₄} - (I_{NO₃} + I_{N₂O} + I_{NO}) - V_{NH₄} - O_{NH₄} \]  \hspace{1cm} (A1)

\[ \frac{d N_{NO₃}}{dt} = P_{NO₃} + I_{NO₃} - L_{NO₃} - U_{NO₃} - (F_{N₂} + F_{N₂O} + F_{NO}) - O_{NO₃} \]  \hspace{1cm} (A2)

and all fluxes are represented in units of gN m⁻² day⁻¹. \( B_{NH₄} \) is the rate of biological N fixation which solely contributes to the NH₄⁺ pool, \( F_{NH₄} \) is the fertilizer input which is assumed to contribute only to the NH₄⁺ pool, and \( P_{NH₄} \) and \( P_{NO₃} \) are atmospheric deposition rates that contribute to the NH₄⁺ and NO₃⁻ pools, respectively. Biological N fixation, fertilizer input, and atmospheric deposition are the three routes through which N enters the coupled soil-vegetation system. \( M_{D,NH₄} \) and \( M_{H,NH₄} \) are the mineralization flux from the litter and soil organic matter pools, respectively, associated with their decomposition. We assume mineralization of humus and litter pools only contributes to the NH₄⁺ pool. \( O_{NH₄} \) and \( O_{NO₃} \) indicate immobilization of N from the NH₄⁺ and NO₃⁻ pools, respectively, to the humus N pool which implies microbes (that are not represented explicitly) are part of the humus pool. Combined together the terms \( \{ M_{D,NH₄} + M_{H,NH₄} - O_{NH₄} - O_{NO₃} \} \) yield the net mineralization rate, \( V_{NH₄} \) is the rate of ammonia (NH₃) volatilization and \( L_{NO₃} \) is the leaching of N that occurs only from the NO₃⁻ pool.
The positively charged ammonium ions are attracted to the negatively charged soil particles and as a result it is primarily the negatively charged nitrate ions that leach through the soil (Porporato et al., 2003; Xu-Ri and Prentice, 2008). $U_{NH4}$ and $U_{NO3}$ are uptakes of $NH_4^+$ and $NO_3^-$ by plants, respectively. The nitrification flux from $NH_4^+$ to $NO_3^-$ pool is represented by $I_{NO3}$, which also results in the release of the nitrous oxide ($N_2O$), a greenhouse gas, and nitric oxide (NO) through nitrifier denitrification represented by the terms $I_{N2O}$ and $I_{NO}$, respectively. Finally, $E_{N2O}$, $E_{NO}$ and $V_{NH3}$ are the gaseous losses of $N_2$ (nitrogen gas), $N_2O$, and NO from the $NO_3^-$ pool associated with denitrification. $N$ is thus lost through the soil-vegetation system via leaching in runoff and through gaseous losses of $I_{N2O}$, $I_{NO}$, $E_{N2O}$, $E_{NO}$, and $V_{NH3}$.

The structural and non-structural $N$ pools in root are written as $N_{R, S}$ and $N_{R, NS}$ respectively, and similarly for stem ($N_{S, S}$ and $N_{S, NS}$) and leaves ($N_{L, S}$ and $N_{L, NS}$), and together the structural and non-structural pools make the total $N$ pool in leaf ($N_L = N_{L, S} + N_{L, NS}$), root ($N_R = N_{R, S} + N_{R, NS}$), and stem ($N_S = N_{S, S} + N_{S, NS}$) components. The rate change equation for structural and non-structural $N$ pools in root are given by

$$\frac{d N_{R, NS}}{dt} = U_{NH4} + U_{NO3} + R_{L2R} - R_{R2L} - A_{R2L} - A_{R2S} - LF_{R, NS} - T_{R, NS2S}$$  \hspace{1cm} (A3)

$$\frac{d N_{R, S}}{dt} = T_{R, NS2S} - LF_{R, S}$$  \hspace{1cm} (A4)

Similar to the uptake of carbon by leaves and its subsequent allocation to root and stem components, $N$ is taken up by roots and then allocated to leaves and stem $A_{R2L}$ and $A_{R2S}$ represent the allocation of $N$ from roots to leaves and stem, respectively. The terms $R_{L2R}$ and $R_{R2L}$ represent the reallocation of $N$ between the non-structural components of root and leaves, $R_{L2R}$ is the $N$ reallocated from leaves to root representing resorption of a fraction of leaf $N$ during

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leaf fall for deciduous tree PFTs, \( R_{R2L} \), indicates reallocation of N from roots to leaves (termed reallocation in Figure 2) at the time of leaf-out for deciduous tree PFTs. At times other than leaf-out and leaf-fall and for other PFTs these two terms are zero. \( T_{R,NS2S} \) is the one way transfer of N from the non-structural to the structural root pool, and similar to the carbon pools, once N is converted to its structural form it cannot be converted back to its non-structural form. Finally, the litterfall due to turnover of roots occurs from both the structural \((LF_{R,S})\) and non-structural \((LF_{R,NS})\) N pools.

The rate change equations for non-structural and structural components of leaves are written as

\[
\frac{dN_{L,NS}}{dt} = A_{R2L} - R_{L2S} - R_{L2S} + R_{R2L} + R_{S2L} - LF_{L,NS} - T_{L,NS2S} \tag{A5}
\]

\[
\frac{dN_{L,S}}{dt} = T_{L,NS2S} - LF_{L,S} \tag{A6}
\]

where \( T_{L,NS2S} \) is the one way transfer of N from the non-structural leaf component to its structural N pool and \( R_{S2L} \) indicates reallocation of N from stem to leaves (similar to \( R_{R2L} \)) at the time of leaf-out for deciduous tree PFTs. Litterfall occurs from both the structural \((LF_{L,S})\) and non-structural \((LF_{L,NS})\) N pools of leaves, and all other terms have been previously defined.

Finally, the rate change equations for non-structural and structural components of stem are written as

\[
\frac{dN_{S,NS}}{dt} = A_{R2S} + R_{L2S} - R_{S2L} - LF_{S,NS} - T_{S,NS2S} \tag{A7}
\]

\[
\frac{dN_{S,S}}{dt} = T_{S,NS2S} - LF_{S,S} \tag{A8}
\]
where \( L_{FS,NS} \) and \( L_{FS,S} \) represent stem litter from the non-structural and structural components. \( T_{S,NS2S} \) is the one way transfer of N from the non-structural stem component to its structural N pool. All other terms have been previously defined.

Adding equations (6) through (11) yields rate of change of N in the entire vegetation pool \( \{N_V\} \) as

\[
\frac{d N_V}{dt} = \frac{d N_{R,NS}}{dt} + \frac{d N_{R,LS}}{dt} + \frac{d N_{S,NS}}{dt} + \frac{d N_{S,LS}}{dt} = \frac{d N_R}{dt} + \frac{d N_L}{dt} + \frac{d N_S}{dt} \tag{A9}
\]

which indicates how the dynamically varying vegetation N pool is governed by mineral N uptake from the \( \text{NH}_4^+ \) and \( \text{NO}_3^- \) pools and litterfall from the structural and non-structural components of the leaves, stem, and root pools. \( L_F \) is the total N litter generation from the root pool and sum of litter generation from its structural and non-structural components \( \{L_F = L_{F,NS} + L_{F,NS}\} \) and similarly for the leaves \( \{L_F\} \) and the stem \( \{L_F\} \) pools.

The rate change equations for the organic N pools in the litter \( \{N_L\} \) and soil \( \{N_H\} \) pools are written as follows.

\[
\frac{d N_L}{dt} = L_F + L_F + L_F - H_{N,D2H} - M_{D,NH4} \tag{A10}
\]

\[
\frac{d N_H}{dt} = H_{N,D2H} + O_{NH4} + O_{NO3} - M_{R,NH4} \tag{A11}
\]

where \( H_{N,D2H} \) is the transfer of humidified organic matter from litter to the soil organic matter pool, and all other terms have been previously defined.
Acknowledgments

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Code/Data availability

Model code for the operational CLASSIC model can be obtained from https://gitlab.com/ccma/classic. Changes made to the operational version to include N cycle and the results shown here can be obtained from the second author.

Author contributions

A.A. implemented the N cycle in the CLASSIC code, put together all the N cycle related input data, and performed all the simulations. V.A. and A.A. wrote the manuscript.

Competing interests

There are no competing interests.

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A1.1 Biological N fixation

Biological N fixation (BNF, $B_{\text{fix}}$) is caused by both free living bacteria in the soil and by bacteria symbiotically living within nodules of host plants' roots. Here, the bacteria convert free nitrogen from the atmosphere to ammonium, which is used by the host plant. Like any other microbial activity, BNF is limited both by drier soil moisture conditions and cold temperatures. Cleveland et al. (1999) attempt to capture this by parameterizing BNF as a function of actual evapotranspiration (AET). AET is a function primarily of soil moisture (through precipitation and soil water balance) and available energy. In places where vegetation exists, AET is also affected by vegetation characteristics including LAI and rooting depth. Here, we parameterize BNF ($B_{\text{fix}}$; gN m$^{-2}$ day$^{-1}$) as a function of modelled soil moisture and temperature to depth of 0.5 m following Xu-Ri and Prentice (2008) which yields a very similar geographical distribution of BNF as the Cleveland et al. (1999) approach as seen in Figure 4c.

\[
B_{\text{fix}} = \left( \sum_m \alpha_m f_m + \sum_n \alpha_n f_n \right) f(T) \left( \theta_x \right)
\]

where $\alpha_m$ and $\alpha_n$ (gN m$^{-2}$ day$^{-1}$) are BNF coefficients for crop (c) and non-crop or natural (n) PFTs, which are area weighted using the fractional coverages $f_m$ and $f_n$ of crop and non-crop PFTs that are present in a grid cell, $f(T)$ is the dependence on soil temperature based on a $Q_10$ formulation and $f(\theta)$ is the dependence on soil moisture which varies between 0 and 1, $\theta_x$ the soil moisture at field capacity and wilting points, respectively. $T_x$ (°C) and $\theta_{x,5}$ (m$^3$ m$^{-2}$) in equation (A1) are averaged over the 0.5 m soil depth over which BNF is assumed to occur. We do not make the distinction between symbiotic and non-symbiotic BNF since this requires explicit knowledge of geographical distribution of N fixing PFTs which are not represented separately in our base set of nine PFTs. A higher value of $\alpha_c$ is used compared to $\alpha_n$ to account for the use of N fixing plants over agriculture areas. Biological nitrogen fixation has been an essential component of many farming systems for considerable periods, with evidence for the agricultural use of legumes dating back more than 4,000 years (O’Hara, 1998). A higher $\alpha_c$ than $\alpha_n$ is also consistent with Fowler et al. (2013) who report BNF of 58 and 60 Tg N yr$^{-1}$ for natural and agricultural ecosystems for present day. Since the area of natural ecosystems is about five times the current cropland area it implies BNF rate per unit land area is higher for crop ecosystems than for natural ecosystems. Values of $\alpha_c$ than $\alpha_n$ and other model parameters are summarized in Table A1.

Similar to Cleveland et al. (1999), our approach does not lead to a significant change in BNF with increasing atmospheric CO$_2$ other than through changes in soil moisture and temperature. At least two meta-analyses, however, suggest that an increase in atmospheric CO$_2$ does lead to an increase in BNF through increased symbiotic activity associated with an increase in both nodule mass and number (McGuire et al., 1995; Liang et al., 2016). Models have attempted to capture this by simulating BNF as a function of NPP (Thornton et al., 2007; Wania et al., 2016).
Figure A1: The structure of CLASSIC model used in this study, upon which the N cycle is implemented, with its carbon pools and fluxes. The fluxes of non-structural carbon are shown in red colour.
Figure A2: Annual values of global precipitation (a) and air temperature (b) over land in the CRU-JRA reanalysis data that are used to drive the model. The data are available for the period 1901-2017. In the absence of meteorological data, the period 1851-1900 uses the data from the period 1901-1925 twice. The thin lines are the annual values and the thick line their 10 year running mean.
Table A1: Model parameters for various model parameterizations. Corresponding equation in which the parameter appears in the main text is also noted. Model parameters may be scalar or an array (if they are PFT dependent) in which case they are written according to the following structure in the table below.

<table>
<thead>
<tr>
<th>Model parameter</th>
<th>Eqn</th>
<th>Description</th>
<th>Units</th>
<th>Value(s)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Biological N fixation</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\alpha_c$</td>
<td>2</td>
<td>BNF rate for crop PFTs</td>
<td>gN m$^{-2}$ day$^{-1}$</td>
<td>0.00217</td>
</tr>
<tr>
<td>$\alpha_n$</td>
<td>2</td>
<td>BNF rate for natural PFTs</td>
<td>gN m$^{-2}$ day$^{-1}$</td>
<td>0.00037</td>
</tr>
<tr>
<td>Plant N demand</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$C_{i, N_{L, min}}$</td>
<td>4</td>
<td>Minimum C:N ratio for leaves</td>
<td>dimensionless</td>
<td>25 22 16 13 30 18 18</td>
</tr>
<tr>
<td>$C_{i, N_{S, min}}$</td>
<td>4</td>
<td>Minimum C:N ratio for stem</td>
<td>dimensionless</td>
<td>450 450 430 430 285 285</td>
</tr>
<tr>
<td>$C_{i, N_{R, min}}$</td>
<td>4</td>
<td>Minimum C:N ratio for root</td>
<td>dimensionless</td>
<td>45 45 35 35 30 30</td>
</tr>
<tr>
<td>Plant uptake</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\beta$</td>
<td>6</td>
<td>Mineral N distribution coefficient</td>
<td>dimensionless</td>
<td>0.5</td>
</tr>
<tr>
<td>$\varepsilon$</td>
<td>8</td>
<td>Fine root efficiency</td>
<td>gN gC$^{-1}$ day$^{-1}$</td>
<td>4.92E-5</td>
</tr>
<tr>
<td>$k_{p,1/2}$</td>
<td>6</td>
<td>Half saturation constant</td>
<td>gN m$^{-2}$</td>
<td>3</td>
</tr>
<tr>
<td>Litterfall</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$r_L$</td>
<td>11</td>
<td>Leaf resorption coefficient</td>
<td>dimensionless</td>
<td>0.54</td>
</tr>
<tr>
<td>Nitrification</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\eta$</td>
<td>18</td>
<td>Nitrification coefficient</td>
<td>day$^{-1}$</td>
<td>7.33E-4</td>
</tr>
<tr>
<td>( \eta_{NO} )</td>
<td>22</td>
<td>Fraction of nitrification flux emitted as NO</td>
<td>dimensionless</td>
<td>7.03E-5</td>
</tr>
<tr>
<td>( \eta_{N2O} )</td>
<td>23</td>
<td>Fraction of nitrification flux emitted as N(_2)O</td>
<td>dimensionless</td>
<td>2.57E-5</td>
</tr>
</tbody>
</table>

**Denitrification**

| \( \mu_{NO} \) | 24 | Fraction of denitrification flux emitted as NO | day\(^{-1} \) | 3.872E-4 |
| \( \mu_{N2O} \) | 25 | Fraction of denitrification flux emitted as N\(_2\)O | day\(^{-1} \) | 1.408E-4 |
| \( \mu_{N2} \) | 26 | Fraction of denitrification flux emitted as N\(_2\) | day\(^{-1} \) | 3.872E-3 |

| \( w_d \) | 27 | Soil wetness threshold below which very little denitrification occurs | dimensionless | 0.3 |

**Leaching**

| \( \phi \) | 28 | Leaching coefficient | m\(^2\) Kg\(^{-1} \) | 1.15E-3 |

**NH\(_3\) volatilization**

| \( \theta \) | 29 | NH\(_3\) volatilization coefficient | dimensionless | 0.54 |

**Coupling of C and N cycles**

| \( I_1 \) | 30 | Parameter for calculating \( V_{max} \) from leaf N content | \( \mu\)mol CO\(_2\) gN\(^{-1} \) s\(^{-1} \) | 13 (all PFTs except broadleaf evergreen tree) 5.1 (for broadleaf evergreen tree) |
| \( I_2 \) | 31 | Parameter for calculating \( V_{max} \) from leaf N content | \( \mu\)mol CO\(_2\) m\(^{-2} \) s\(^{-1} \) | 8.5 |
| \( k_A \) | 32 | Parameter for constraining \( V_{max} \) increase when C:N ratios exceed their maximum limit | dimensionless | 0.05 |

<p>| ( C: N_{L,max} ) | 33 | Maximum C:N ratio for leaves | dimensionless | 60 55 40 40 35 50 |
| ( C: N_{S,max} ) | 34 | Maximum C:N ratio for stem | dimensionless | 800 800 670 670 670 500 500 500 670 |</p>
<table>
<thead>
<tr>
<th>$C:N_{R, \text{max}}$</th>
<th>33</th>
<th>Maximum C/N ratio for root</th>
<th>dimensionless</th>
<th>90</th>
<th>90</th>
<th>70</th>
<th>70</th>
<th>70</th>
</tr>
</thead>
</table>

Deleted: 1
Table 1: Historical simulations performed over the period 1851-2017 to evaluate the model’s response to various forcings. All forcings are time varying. All forcings are also spatially explicit except atmospheric CO2 for which a globally constant value is specified.

<table>
<thead>
<tr>
<th>Simulation name</th>
<th>Forcing that varies over the historical period</th>
<th>N cycle</th>
</tr>
</thead>
<tbody>
<tr>
<td>Primary simulations performed to evaluate N cycle response to various forcings</td>
<td></td>
<td></td>
</tr>
<tr>
<td>1. CO2-only</td>
<td>Atmospheric CO2 concentration</td>
<td>Runs with N cycle</td>
</tr>
<tr>
<td>2. CLIM-only</td>
<td>1901-1925 meteorological data are used twice over the 1850-1900 period. For the 1901-2017 period, meteorological data for the correct year is used.</td>
<td></td>
</tr>
<tr>
<td>3. LUC+FERT-only</td>
<td>Land cover with increasing crop area, and fertilizer application rates over the crop area</td>
<td></td>
</tr>
<tr>
<td>4. N-DEP-only</td>
<td>N deposition of ammonia and nitrate</td>
<td></td>
</tr>
<tr>
<td>5. FULL</td>
<td>All forcings</td>
<td></td>
</tr>
<tr>
<td>6. FULL-no-LUC</td>
<td>All forcings except increasing crop area</td>
<td></td>
</tr>
<tr>
<td>Other simulations</td>
<td></td>
<td></td>
</tr>
<tr>
<td>7. ORIGINAL</td>
<td>All forcings</td>
<td>Runs without N cycle using the original model configuration.</td>
</tr>
<tr>
<td>8. ORIG-UNCONST</td>
<td>All forcings but with downregulation turned off</td>
<td></td>
</tr>
<tr>
<td>9. FULL-no-implicit-P-limitation</td>
<td>All forcings but using same ( \Gamma_1 ) and ( \Gamma_2 ) globally</td>
<td>Run with N cycle</td>
</tr>
</tbody>
</table>
Table 2: Comparison of simulated global N pools and fluxes, from the FULL simulation, with other modelling and quasi observation-based studies (references for which are noted as superscripts and listed below the table). The time-periods to which the other modelling and quasi observation-based estimates correspond are also noted, where available. The estimates are for land. Simulated fluxes and pool corresponds to the period 1997-2018.

<table>
<thead>
<tr>
<th>N pool and fluxes</th>
<th>This study (1998-2017)</th>
<th>Other model and quasi observation-based estimates</th>
</tr>
</thead>
<tbody>
<tr>
<td>N inputs (Tg N yr(^{-1}))</td>
<td></td>
<td></td>
</tr>
<tr>
<td>BNF</td>
<td>119</td>
<td>138(^a) 99(^b) (2001-2010) 138.5(^c) (early 1990s) 128.9(^d) (2000-2009) 104-118(^e) 92(^f) (year 2000)</td>
</tr>
<tr>
<td>Natural BNF</td>
<td>59</td>
<td>58(^g) 107(^h) (early 1990s) 30-130(^i) 39(^j) (year 2000)</td>
</tr>
<tr>
<td>Anthropogenic BNF</td>
<td>60</td>
<td>60(^k) 31.5(^l) (early 1990s) 14-89(^m) 53(^n) (year 2000)</td>
</tr>
<tr>
<td>Fertilizer input</td>
<td>91 [based on TRENDY protocol]</td>
<td>100(^o) 100(^p) (2001-2010) 100(^q) (early 1990s) 88(^r) (year 2000)</td>
</tr>
<tr>
<td>N deposition</td>
<td>66 [based on TRENDY protocol]</td>
<td>70(^s) 56-62(^t) 63.5(^u) (early 1990s) 60(^v) (year 2000)</td>
</tr>
<tr>
<td>N pools (Tg N yr(^{-1}))</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Vegetation</td>
<td>3034</td>
<td>1,780(^w) (2000s) 3,800(^x) (1990s) 5,300(^y) 2,940(^z) (1990s)</td>
</tr>
<tr>
<td>Litter and soil</td>
<td>77161</td>
<td>106,000(^{<strong>}) (2000s) 100,000(^{</strong><em>}) (1990s) 56,800(^{</em>***}) 133,000 (1990s)</td>
</tr>
<tr>
<td>Ammonia</td>
<td>1924</td>
<td>163.7(^{<strong><strong>}) (2000s) 361(^{</strong></strong>}) 1200(^****) (1990s)</td>
</tr>
<tr>
<td>Nitrate</td>
<td>2974</td>
<td>2,778(^{<strong><strong>}) (2000s) 580(^{</strong></strong>}) 14,800 (1990s)</td>
</tr>
<tr>
<td>N fluxes related to N cycling (Tg N yr(^{-1}))</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Plant uptake</td>
<td>940</td>
<td>618(^{<strong><strong>}) (2000s) 1,127(^{</strong></strong>}) (1990s) 1,084(^{****}) 873 (1990s)</td>
</tr>
<tr>
<td>Net mineralization</td>
<td>947</td>
<td></td>
</tr>
<tr>
<td>Mineralization</td>
<td>2045</td>
<td>1,678(^{****}) (2000s)</td>
</tr>
<tr>
<td>Immobilization</td>
<td>1097</td>
<td>1,177(^{****}) (2000s)</td>
</tr>
<tr>
<td>Nitrification</td>
<td>239</td>
<td></td>
</tr>
<tr>
<td>Nitrogen Losses (Tg N yr⁻¹)</td>
<td>2001–2010</td>
<td>2000s</td>
</tr>
<tr>
<td>-----------------------------</td>
<td>-----------</td>
<td>-------</td>
</tr>
<tr>
<td><strong>NO₃⁻ Leaching</strong></td>
<td>53.5</td>
<td>97.1</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td><strong>NH₃ Volatilization</strong></td>
<td>53.9</td>
<td>124.3</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td><strong>N₂ from denitrification</strong></td>
<td>114.2</td>
<td>105.8</td>
</tr>
<tr>
<td><strong>N₂O from denitrification</strong></td>
<td>4.2</td>
<td>12.6</td>
</tr>
<tr>
<td><strong>N₂O from nitrification</strong></td>
<td>8.4</td>
<td>10.9</td>
</tr>
<tr>
<td><strong>NO from denitrification</strong></td>
<td>11.4</td>
<td>34.3</td>
</tr>
<tr>
<td><strong>NO from nitrification</strong></td>
<td>22.9</td>
<td></td>
</tr>
</tbody>
</table>

Figure 1: The structure of CLASSIC model used in this study, upon which the N cycle is implemented, with its carbon pools and fluxes. The fluxes of non-structural carbon are shown in red colour.
Figure 2: Time series and geographical distribution of global annual values of externally specified N inputs. Fertilizer input (a, b), atmospheric deposition of ammonium (c, d) and atmospheric deposition of nitrate (e, f). The values in the parenthesis for legend entries in the time series plots show averages for the 1850s, the 1998-2017 period, and the change between these two periods. The thin lines in the time series plots show the annual values and the thick lines their 10-year moving average. The geographical plots show the average values over the last 20-years of the FULL simulation corresponding to the 1998-2017 period. Note that in the time series plots lines from some simulations are hidden behind lines from other simulations and this can be inferred from the legend entries which shows averages for the 1850s, the 1998-2017 period.
Figure 3: Time series and geographical distribution of annual values biological N fixation (BNF) (a,b) and its natural (c, d) and anthropogenic (e, f) components. The values in the parenthesis for legend entries in the time series plots show averages for the 1850s, the 1998-2017 period, and the change between these two periods. The thin lines in the time series plots show the annual values and the thick lines their 10-year moving average. The geographical plots show the average values over the last 20-years of the FULL simulation corresponding to the 1998-2017 period. Note that in the time series plots lines from some simulations are hidden behind lines from other simulations and this can be inferred from the legend entries which shows averages for the 1850s, the 1998-2017 period.
Figure 4: Global annual values of gross primary productivity (a), vegetation carbon (b), leaf carbon (c), and litter and soil carbon (d) for the primary simulations performed. The values in parenthesis for legend entries show averages for the 1850s, the 1998-2017 period, and the change between 1850s and 1998-2017 periods. The thin lines show the annual values and the thick lines their 10-year moving average.
Figure 5: Global annual values of N in vegetation (a), leaves (b), litter and soil organic matter (c) pools, $V_{\text{max}}$ (d), and ammonium (e), and nitrate (f) pools for the primary simulations performed. The values in the parenthesis for legend entries show averages for the 1850s, the 1998-2017 period, and the change between 1850s and 1998-2017 periods. The thin lines show the annual values and the thick lines their 10-year moving average.
Figure 6: Global annual values of N demand (a), total plant N uptake (b) and its split into passive (c) and active (d) components for the primary simulations performed. The values in the parenthesis for legend entries show averages for the 1850s, the 1998-2017 period, and the change between 1850s and 1998-2017 periods. The thin lines show the annual values and the thick lines their 10-year moving average.
Figure 7: Global annual values of C:N ratios for whole plant (a), leaves (b), root (c), stem (d), litter (e) and soil organic matter (f) pools from the primary six simulations. The values in the parenthesis for legend entries show averages for the 1850s, the 1998-2017 period, and the change between 1850s and 1998-2017 periods. The thin lines show the annual values and the thick lines their 10-year moving average.
Figure 8: Global annual values of net mineralization (a), nitrification (b), NO₃-leaching (c), NH₃ volatilization (d), and gaseous losses associated with nitrification (e) and denitrification (f) from the primary six simulations. The values in the parenthesis for legend entries show averages for the 1850s, the 1998-2017 period, and the change between 1850s and 1998-2017 periods. The thin lines show the annual values and the thick lines their 10-year moving average.
Figure 9: Geographical distribution of primary C and N pools. Ammonium (a), nitrate (b), vegetation C mass (c), litter and soil C mass (d), vegetation N mass (e), and litter and soil N mass (f). The global total values shown are averaged over the 1998-2017 period.
Figure 10: Comparison of zonal distribution of gross primary productivity (GPP) and the effect of GPP downregulation compared to the ORIG-UNCONST simulation. Panel (a) compares zonal distribution of GPP from FULL and ORIGINAL simulations with observation-based estimate from Beer et al. (2010) for the present day. Panel (b) compares the zonal distribution of GPP from the pre-industrial simulation, corresponding to 1850 conditions, from the FULL and FULL-no-implicit-P-limitation simulations to illustrate the effect of not reducing the $\Gamma_3$ parameter for calculating $V_{\text{cmax}}$ for the broadleaf evergreen tree PFT that implicitly accounts for phosphorus limitation. Panel (c) shows the zonally-averaged ratios of GPP from the ORIGINAL and FULL simulations versus those from the ORIG-UNCONST simulations to illustrate how downregulation acts in the ORIGINAL and FULL simulations.
Figure 11: Comparison of simulated net atmosphere-land CO₂ flux from various simulations.

Panel (a) compares globally-summed values of net atmosphere-land CO₂ flux from FULL, FULL-no-LUC simulation, and ORIGINAL simulations with estimate of terrestrial sink (dark yellow line) and net atmosphere-land CO₂ flux (grey bars) from Friedlingstein et al. (2019). The thin lines show the annual values and the thick lines their 10-year moving average. Panel (b) compares zonal distribution of net atmosphere-land CO₂ flux from FULL and ORIGINAL simulations with the range from TRENDY models that contributed to the Friedlingstein et al. (2019) study. Panel (c) shows cumulative values of net atmosphere-land CO₂ flux from the six primary simulations to investigate the contribution of each forcing to the cumulative land carbon sink over the historical period.
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Following earlier simpler approaches (Cao et al., 2001; Alexandrov and Oikawa, 2002), GPP can be expressed as a logarithmic function of [CO₂]

\[ G_p(t) = G_0 \left( 1 + \gamma_p \ln \frac{c(t)}{c_0} \right) \]  

(1)

where the unconstrained or potential GPP at any given time, \( G_p(t) \), is a function of its initial value \( G_0 \), [CO₂] at time \( t \), \( c(t) \), and its initial value \( c_0 \). The rate of increase of GPP is determined by the parameter \( \gamma_p \) (where \( p \) indicates the “potential” rate of increase of GPP with [CO₂]). The parameter \( \gamma_p \) is calculated by fitting equation (1) to simulated GPP over the historical period. In the absence of any nutrient constraints, the rate of increase of carbon uptake per unit area of leaves is determined by the theoretical framework of Farquhar et al. (1980) and Collatz et al. (1992) for C₃ and C₄ photosynthetic pathways, respectively. The rate of increase of global GPP, however, also depends on how the model simulated LAI increases in response to increasing [CO₂], which in turn depends on how photosynthate is allocated between leaves, stem, and root. Arora et al. (2009) compared the unconstrained simulated rate of increase of GPP per unit increase in [CO₂] (their Figure 3) with that based on the theoretical framework to show that the model’s response to increasing [CO₂] over the historical period is consistent with the theoretical framework, given specified time-independent \( V_{\text{cmax}} \) values for different PFTs. To parameterize downregulation of photosynthesis with increasing [CO₂] for emulating nutrient constraints, the unconstrained or potential GPP (for each time step and each PFT in a grid cell) is multiplied by the global scalar \( \xi(c) \)
\[ G = \xi(c) G_p \]  \hspace{1cm} (2)

\[ \xi(c) = \frac{1 + \gamma_d \ln(c/c_0)}{1 + \gamma_p \ln(c/c_0)} \]  \hspace{1cm} (3)

where \( t \) is omitted for clarity and the parameter \( \gamma_d \) represents the downregulated rate of increase of GPP with \([\text{CO}_2]\) (indicated by the subscript \( d \)). When \( \gamma_d < \gamma_p \) the modelled gross primary productivity \( (G) \) increases in response to \([\text{CO}_2]\) at a rate determined by the value of \( \gamma_d \).

In the absence of the N cycle, the term \( \xi(c) \) thus emulates down-regulation of photosynthesis as \( \text{CO}_2 \) increases. For example, values of \( \gamma_d = 0.42 \) and \( \gamma_p = 0.90 \), from Arora et al. (2009), yield a value of \( \xi(c) = 0.94 \) (indicating a 6\% downregulation) for \( c = 390 \text{ ppm} \) (corresponding to year 2010) and \( c_0 = 285 \text{ ppm} \).

\[
\frac{d N_{\text{NH}_4}}{dt} = B_{\text{NH}_4} + F_{\text{NH}_4} + P_{\text{NH}_4} + M_{D,\text{NH}_4} + M_{H,\text{NH}_4} - U_{\text{NH}_4} - (I_{\text{NO}_3} + I_{\text{N}_2\text{O}} + I_{\text{NO}}) - V_{\text{NH}_3} - O_{\text{NH}_4}
\]  \hspace{1cm} (4)

\[
\frac{d N_{\text{NO}_3}}{dt} = P_{\text{NO}_3} + I_{\text{NO}_3} - L_{\text{NO}_3} - U_{\text{NO}_3} - (E_{\text{N}_2} + E_{\text{N}_2\text{O}} + E_{\text{NO}}) - O_{\text{NO}_3}
\]  \hspace{1cm} (5)

and all fluxes are represented in units of gN m\(^{-2}\) day\(^{-1}\). \( B_{\text{NH}_4} \) is the rate of biological N fixation which solely contributes to the \( \text{NH}_4^+ \) pool, \( F_{\text{NH}_4} \) is the fertilizer input which is assumed to contribute only to the \( \text{NH}_4^+ \) pool, and \( P_{\text{NH}_4} \) and \( P_{\text{NO}_3} \) are atmospheric deposition rates that contribute to the \( \text{NH}_4^+ \) and \( \text{NO}_3^- \) pools, respectively. Biological N fixation, fertilizer input, and atmospheric deposition are the three routes through which N enters the coupled soil-vegetation system. \( M_{D,\text{NH}_4} \) and \( M_{H,\text{NH}_4} \) are the mineralization flux from the litter and soil organic matter pools, respectively, associated with their decomposition. We assume mineralization of humus
and litter pools only contributes to the \( \text{NH}_4^+ \) pool. \( O_{\text{NH}_4} \) and \( O_{\text{NO}_3} \) indicate immobilization of N from the \( \text{NH}_4^+ \) and \( \text{NO}_3^- \) pools, respectively, to the humus N pool which implies microbes (that are not represented explicitly) are part of the humus pool. Combined together the terms \((M_D,\text{NH}_4 + M_H,\text{NH}_4 - O_{\text{NH}_4} - O_{\text{NO}_3})\) yield the net mineralization rate. \( V_{\text{NH}_3} \) is the rate of ammonia (\( \text{NH}_3 \)) volatilization and \( L_{\text{NO}_3} \) is the leaching of N that occurs only from the \( \text{NO}_3^- \) pool.

The positively charged ammonium ions are attracted to the negatively charged soil particles and as a result it is primarily the negatively charged nitrate ions that leach through the soil (Porporato et al., 2003; Xu-Ri and Prentice, 2008). \( U_{\text{NH}_4} \) and \( U_{\text{NO}_3} \) are uptakes of \( \text{NH}_4^+ \) and \( \text{NO}_3^- \) by plants, respectively. The nitrification flux from \( \text{NH}_4 \) to \( \text{NO}_3 \) pool is represented by \( I_{\text{NO}_3} \) which also results in the release of the nitrous oxide (\( \text{N}_2\text{O} \)), a greenhouse gas, and nitric oxide (\( \text{NO} \)) through nitrifier denitrification represented by the terms \( I_{\text{N}2\text{O}} \) and \( I_{\text{NO}} \), respectively. Finally, \( E_{\text{N}_2}, E_{\text{N}2\text{O}}, \) and \( E_{\text{NO}} \) are the gaseous losses of \( \text{N}_2 \) (nitrogen gas), \( \text{N}_2\text{O}, \) and NO from the \( \text{NO}_3^- \) pool associated with denitrification. N is thus lost through the soil-vegetation system via leaching in runoff and through gaseous losses of \( I_{\text{N}2\text{O}}, I_{\text{NO}}, E_{\text{N}_2}, E_{\text{N}2\text{O}}, E_{\text{NO}}, \) and \( V_{\text{NH}_3} \).

The structural and non-structural N pools in root are written as \( N_{R,S} \) and \( N_{R,NS}, \) respectively, and similarly for stem (\( N_{S,S} \) and \( N_{S,NS} \)) and leaves (\( N_{L,S} \) and \( N_{L,NS} \)), and together the structural and non-structural pools make the total N pool in leaf (\( N_L = N_{L,S} + N_{L,NS} \)), root (\( N_R = N_{R,S} + N_{R,NS} \)), and stem (\( N_S = N_{S,S} + N_{S,NS} \)) components. The rate change equation for structural and non-structural N pools in root are given by

\[
\frac{dN_{R,NS}}{dt} = U_{\text{NH}_4} + U_{\text{NO}_3} + R_{L2R} - R_{R2L} - A_{R2L} - A_{R2S} - LF_{R,NS} - T_{R,NS2S}
\]

(6)

\[
\frac{dN_{R,S}}{dt} = T_{R,NS2S} - LF_{R,S}
\]

(7)
Similar to the uptake of carbon by leaves and its subsequent allocation to root and stem components, N is taken up by roots and then allocated to leaves and stem. $A_{R2L}$ and $A_{R2S}$ represent the allocation of N from roots to leaves and stem, respectively. The terms $R_{L2R}$ and $R_{R2L}$ represent the reallocation of N between the non-structural components of root and leaves. $R_{L2R}$ is the N reallocated from leaves to root representing resorption of a fraction of leaf N during leaf fall for deciduous tree PFTs. $R_{R2L}$ indicates reallocation of N from roots to leaves (termed reallocation in Figure 2) at the time of leaf-out for deciduous tree PFTs. At times other than leaf-out and leaf-fall and for other PFTs these two terms are zero. $T_{R,NS2S}$ is the one way transfer of N from the non-structural to the structural root pool, and similar to the carbon pools, once N is converted to its structural form it cannot be converted back to its non-structural form. Finally, the litterfall due to turnover of roots occurs from both the structural ($LF_{R,S}$) and non-structural ($LF_{R,NS}$) N pools.

The rate change equations for non-structural and structural components of leaves are written as

$$\frac{dN_{L,NS}}{dt} = A_{R2L} - R_{L2R} - R_{L2S} + R_{R2L} + R_{S2L} - LF_{L,NS} - T_{L,NS2S}$$  \hspace{1cm} (8)

$$\frac{dN_{L,S}}{dt} = T_{L,NS2S} - LF_{L,S}$$  \hspace{1cm} (9)

where $T_{L,NS2S}$ is the one way transfer of N from the non-structural leaf component to its structural N pool and $R_{S2L}$ indicates reallocation of N from stem to leaves (similar to $R_{R2L}$) at the time of leaf out for deciduous tree PFTs. Litterfall occurs from both the structural ($LF_{L,S}$) and non-structural ($LF_{L,NS}$) N pools of leaves, and all other terms have been previously defined.
Finally, the rate change equations for non-structural and structural components of stem are written as

\[
\frac{d N_{SNS}}{dt} = A_{R2S} + R_{L2S} - R_{S2L} - LF_{S,NS} - T_{S,NS2S} \tag{10}
\]

\[
\frac{d N_{SS}}{dt} = T_{S,NS2S} - LF_{S,S} \tag{11}
\]

where \( LF_{S,NS} \) and \( LF_{S,S} \) represent stem litter from the non-structural and structural components, \( T_{S,NS2S} \) is the one way transfer of N from the non-structural stem component to its structural N pool. All other terms have been previously defined.

Adding equations (6) through (11) yields rate of change of N in the entire vegetation pool \((N_V)\) as

\[
\frac{d N_V}{dt} = \frac{d N_{R,NS}}{dt} + \frac{d N_{R,S}}{dt} + \frac{d N_{L,NS}}{dt} + \frac{d N_{L,S}}{dt} + \frac{d N_{SNS}}{dt} + \frac{d N_{SS}}{dt} + \frac{d N_{R}}{dt} + \frac{d N_{L}}{dt} + \frac{d N_{S}}{dt}
\]

\[
\frac{d N_V}{dt} = U_{NH4} + U_{NO3} - LF_{R,NS} - LF_{R,S} - LF_{L,NS} - LF_{L,S} - LF_{S,NS} - LF_{S,S}
\]

\[
= U_{NH4} + U_{NO3} - LF_{R} - LF_{L} - LF_{S}
\tag{12}
\]

which indicates how the dynamically varying vegetation N pool is governed by mineral N uptake from the NH4\(^+\) and NO3\(^-\) pools and litterfall from the structural and non-structural components of the leaves, stem, and root pools. \( LF_R \) is the total N litter generation from the root pool and sum of litter generation from its structural and non-structural components \((LF_R = LF_{R,S} + LF_{R,NS})\), and similarly for the leaves \((LF_L)\) and the stem \((LF_S)\) pools.

The rate change equations for the organic N pools in the litter \((N_D)\) and soil \((N_H)\) pools are written as follows.
\[
\frac{d N_D}{dt} = LF_R + LF_L + LF_S - H_{N,D2H} - M_{D,NH4}
\] (13)

\[
\frac{d N_H}{dt} = H_{N,D2H} + O_{NH4} + O_{NO3} - M_{H,NH4}
\] (14)

where \( H_{N,D2H} \) is the transfer of humidified organic matter from litter to the soil organic matter pool, and all other terms have been previously defined.

Sections A.1, A.2, and A.3 in the appendix describe how the individual terms of the rate change equations of the 10 prognostic N pools (equations 4 through 11, and equations 13 and 14) are specified or parameterized. The treatment of these terms are briefly described here.

Biological N fixation (BNF, \( B_{NH4} \)) is parameterized as a function of soil moisture and temperature with higher fixation rate per unit area for agricultural areas than natural vegetation. If externally specified information for ammonium (\( NH4^+ \)) and nitrate (\( NO3^- \)) deposition rates is available then it is used otherwise deposition is assumed to be split equally between \( NH4^+ \) and \( NO3^- \). Externally specified fertilizer application rates are same throughout the year in the tropics (between 30°S and 30°N), given multiple crop rotations in a given year in tropical regions. Between 30° and 90° latitudes in both northern and southern hemispheres, we assume that fertilizer application starts on the spring equinox and ends on the fall equinox. Plant N demand is calculated on the basis of the fraction of NPP allocated to leaves, stem, and root components and their specified minimum PFT-dependent C:N ratios. Both passive and active root uptakes of N are modelled. Passive uptake depends on transpiration and concentration of \( NH4^+ \) and \( NO3^- \) in the root zone water column. When passive N uptake cannot meet the N demand, active uptake compensates for reduced passive uptake though eventually they both depend on the amount of available N in the mineral pools. Plant N uptake by roots is allocated to stem and leaf components, which allows to
model leaf N content ($N_L$) as a prognostic variable. N contributions to litter through litterfall are based on C:N ratios of the vegetation components and the litterfall rates. Resorption of N before litterfall for deciduous tree species is also modelled. Decomposition of litter and soil organic matter releases C to the atmosphere as CO$_2$ and the mineralized N is moved to the NH$_4^+$ pool. Immobilization of mineral N from NH$_4^+$ and NO$_3^-$ pools into the soil organic matter pool is meant to keep the soil organic matter C:N ratio ($C:N_H$) at its specified constant value of 13 for all PFTs.

Nitrification, the process converting ammonium to nitrate, is driven by microbial activity and depends both on soil temperature and moisture such that it is constrained both at high and low soil moisture contents. Gaseous fluxes of NO ($l_{NO}$) and N$_2$O ($l_{N2O}$) are associated with nitrification and assumed to be directly proportional to the nitrification flux. Denitrification is modelled to reduce NO$_3^-$ to NO, N$_2$O, and ultimately to N$_2$. Unlike nitrification, however, denitrification is primarily an anaerobic process and therefore occurs primarily when soil is saturated. Leaching of NO$_3^-$ ($L_{NO3}$) is parameterized to be directly proportional to baseflow from the bottommost soil layer and the size of the NO$_3^-$ pool. Finally, NH$_3$ volatilization ($V_{NH3}$) is parametrized as a function of NH$_4^+$ pool size, soil temperature, soil pH, and aerodynamic and boundary layer resistances.

### A1. N inputs

#### A1.1 Biological N fixation

Biological N fixation (BNF, $B_{N_H4}$) is caused by both free living bacteria in the soil and by bacteria symbiotically living within nodules of host plants’ roots. Here, the bacteria convert free
nitrogen from the atmosphere to ammonium, which is used by the host plants. Like any other microbial activity, BNF is limited both by drier soil moisture conditions and cold temperatures. Cleveland et al. (1999) attempt to capture this by parameterizing BNF as a function of actual evapotranspiration (AET). AET is a function primarily of soil moisture (through precipitation and soil water balance) and available energy. In places where vegetation exists, AET is also affected by vegetation characteristics including LAI and rooting depth. Here, we parameterize BNF ($B_{NH4}$, gN m$^{-2}$ day$^{-1}$) as a function of modelled soil moisture and temperature to depth of 0.5 m following Xu-Ri and Prentice (2008) which yields a very similar geographical distribution of BNF as the Cleveland et al. (1999) approach as seen in Figure 4c.

\[
B_{NH4} = \left( \sum_c \alpha_c f_c + \sum_n \alpha_n f_n + \right) \left( f(T_{0.5}) f(\theta_{0.5}) \right)
\]

\[
f(T_{0.5}) = 2^{(T_{0.5}-25)/10}
\]

\[
f(\theta_{0.5}) = \min \left( 0, \max \left( 1, \frac{\theta_{0.5}-\theta_w}{\theta_{fc}-\theta_w} \right) \right)
\]

(A1)

where $\alpha_c$ and $\alpha_n$ (gN m$^{-2}$ day$^{-1}$) are BNF coefficients for crop (c) and non-crop or natural (n) PFTs, which are area weighted using the fractional coverages $f_c$ and $f_n$ of crop and non-crop PFTs that are present in a grid cell, $f(T)$ is the dependence on soil temperature based on a Q$_{10}$ formulation and $f(\theta)$ is the dependence on soil moisture which varies between 0 and 1. $\theta_{fc}$ and $\theta_w$ are the soil moisture at field capacity and wilting points, respectively. $T_{0.5}$ ($^\circ$C) and $\theta_{0.5}$ (m$^3$ m$^{-3}$) in equation (A1) are averaged over the 0.5 m soil depth over which BNF is assumed to occur. We do not make the distinction between symbiotic and non-symbiotic BNF since this requires explicit knowledge of geographical distribution of N fixing PFTs which are not represented separately in our base set of nine PFTs. A higher value of $\alpha_c$ is used compared to $\alpha_n$ to account for the use of N fixing plants over agriculture areas. Biological nitrogen fixation has been an essential
component of many farming systems for considerable periods, with evidence for the agricultural use of legumes dating back more than 4,000 years (O’Hara, 1998). A higher $\alpha_c$ than $\alpha_n$ is also consistent with Fowler et al. (2013) who report BNF of 58 and 60 Tg N yr$^{-1}$ for natural and agricultural ecosystems for present day. Since the area of natural ecosystems is about five times the current cropland area it implies BNF rate per unit land area is higher for crop ecosystems than for natural ecosystems. Values of $\alpha_c$ than $\alpha_n$ and other model parameters are summarized in Table A1.

Similar to Cleveland et al. (1999), our approach does not lead to a significant change in BNF with increasing atmospheric CO$_2$, other than through changes in soil moisture and temperature. At least two meta-analyses, however, suggest that an increase in atmospheric CO$_2$ does lead to an increase in BNF through increased symbiotic activity associated with an increase in both nodule mass and number (McGuire et al., 1995; Liang et al., 2016). Models have attempted to capture this by simulating BNF as a function of NPP (Thornton et al., 2007; Wania et al., 2012). The caveat with this approach and the implications of our BNF approach are discussed in Section 6.

A1.2 Atmospheric N deposition

Atmospheric N deposition is externally specified. The model reads in spatially- and temporally-varying annual deposition rates from a file. Deposition is assumed to occur at the same rate throughout the year so the same daily rate (gN m$^{-2}$ day$^{-1}$) is used for all days of a given year. If separate information for ammonium (NH$_4^+$) and nitrate (NO$_3^-$) deposition rates is available
then it is used otherwise deposition is assumed to be split equally between \( \text{NH}_4^+ \) and \( \text{NO}_3^- \) (indicated as \( P_{\text{NH}_4} \) and \( P_{\text{NO}_3} \) in equations 4 and 5).

**A1.3 Fertilizer application**

Geographically and temporally varying annual fertilizer application rates \( (F_{\text{NH}_4}) \) are also specified externally and read in from a file. Fertilizer application occurs over the C3 and C4 crop fractions of grid cells. Agricultural management practices are difficult to model since they vary widely between countries and even from farmer to farmer. For simplicity, we assume fertilizer is applied at the same daily fertilizer application rate \( (\text{gN m}^{-2} \text{ day}^{-1}) \) throughout the year in the tropics (between 30°S and 30°N), given the possibility of multiple crop rotations in a given year. Between the 30° and 90° latitudes in both northern and southern hemispheres, we assume that fertilizer application starts on the spring equinox and ends on the fall equinox. The annual fertilizer application rate is thus distributed over around 180 days. This provides somewhat more realism, than using the same treatment as in tropical regions, since extra-tropical agricultural areas typically do not experience multiple crop rotations in a given year.

**A2. N cycling in plants and soil**

Plant roots take up mineral N from soil and then allocate it to leaves and stem to maintain an optimal C:N ratio of each component. Litterfall from vegetation contributes to the litter pool and decomposition of litter transfers humified litter to the soil organic matter pool. Decomposition of litter and soil organic matter returns mineralized N back to the \( \text{NH}_4^+ \) pool, closing the soil-vegetation N cycle loop. Both active and passive plant uptakes of N (from both
the NH₄⁺ and NO₃⁻ pools) are explicitly modelled. The modelled plant N uptake is a function of its N demand. Higher N demand leads to higher mineral N uptake from soil.

**A2.1 Plant N demand**

Plant N demand is calculated based on the fraction of NPP allocated to leaves, stem, and root components and their specified minimum PFT-dependent C:N ratios, similar to other models (Xu-Ri and Prentice, 2008; Jiang et al., 2019). The assumption is that plants always want to achieve their desired minimum C:N ratios if enough N is available.

\[
\Delta W_P = \Delta_L + \Delta_R + \Delta_S \\
\Delta_i = \max\left(0, \frac{a_{i,C} \cdot a_{i,C}}{C:N_i,\text{min}}\right), \quad i = L, S, R
\]

where the whole plant N demand (\(\Delta W_P\)) is the sum of N demand for the leaves (\(\Delta_L\)), stem (\(\Delta_S\)), and root (\(\Delta_R\)) components, \(a_{i,C}\), \(i = L, S, R\) is the fraction of NPP (i.e. carbon as indicated by letter C in the subscript) allocated to leaf, stem, and root components, and \(C:N_i,\text{min}\), \(i = L, S, R\) are their specified minimum C:N ratios (see Table A1 for these and all other model parameters).

A caveat with this approach when applied at the daily time step, for biogeochemical processes in our model, is that during periods of time when NPP is negative due to adverse climatic conditions (e.g. during winter or drought seasons), the calculated demand is negative. If positive NPP implies there is demand for N, negative NPP cannot be taken to imply that N must be lost from vegetation. As a result, from a plant’s perspective, N demand is assumed to be zero during periods of negative NPP. N demand is also set to zero when all leaves have been shed (i.e., when GPP is zero). At the global scale, this leads to about 15% higher annual N demand than would be the case if negative NPP values were taken into consideration.
A2.2 Passive N uptake

N demand is weighed against passive and active N uptake. Passive N uptake depends on the concentration of mineral N in the soil and the water taken up by the plants through their roots as a result of transpiration. We assume that plants have no control over N that comes into the plant through this passive uptake. This is consistent with existing empirical evidence that too much N in soil will cause N toxicity (Goyal and Huffaker, 1984), although we do not model N toxicity in our framework. If the N demand for the current time step cannot be met by passive N uptake then a plant compensates for the deficit (i.e., the remaining demand) through active N uptake.

The NH$_4^+$ concentration in the soil moisture within the rooting zone, referred to as [NH$_4$] (gN gH$_2$O$^{-1}$), is calculated as

$$[\text{NH}_4] = \frac{N_{\text{NH}_4}}{\sum_{i=1}^{r_d} 10^6 \theta_i z_i}$$

(A3)

where $N_{\text{NH}_4}$ is ammonium pool size (gN m$^{-2}$), $\theta_i$ is the volumetric soil moisture content for soil layer $i$ (m$^3$ m$^{-3}$), $z_i$ is the thickness of soil layer $i$ (m), $r_d$ is the soil layer in which the 99% rooting depth lies as dynamically simulated by the biogeochemical module of CLASSIC following Arora and Boer (2003). The $10^6$ term converts units of the denominator term to gH$_2$O m$^{-2}$. NO$_3^-$ concentration ([NO$_3^-$], gN gH$_2$O$^{-1}$) in the rooting zone is found in a similar fashion. The transpiration flux $q_t$ (kgH$_2$O m$^{-2}$ s$^{-1}$) (calculated in the physics module of CLASSIC) is multiplied by [NH$_4$] and [NO$_3$] (gN gH$_2$O$^{-1}$) to obtain passive uptake of NH$_4^+$ and NO$_3^-$ (gN m$^{-2}$ day$^{-1}$) as
\[
U_{p,NH_4} = 86400 \times 10^3 \beta q_t [NH_4] \\
U_{p,NO_3} = 86400 \times 10^3 \beta q_t [NO_3]
\]  \hspace{1cm} (A4)

where the multiplier $86400 \times 10^3$ converts $q_t$ to units of $gH_2O \text{ m}^{-2} \text{ day}^{-1}$, and $\beta$ (see Table A1) is the dimensionless mineral N distribution coefficient with value less than 1 that accounts for the fact that NH$_4$ and NO$_3$ available in the soil are not well mixed in the soil moisture solution, and not completely accessible to roots, to be taken up by plants.

### A2.3 Active N uptake

The active plant N uptake is parameterized as a function of fine root biomass and the size of NH$_4^+$ and NO$_3^-$ pools in a manner similar to Gerber et al. (2010) and Wania et al (2012). CLASSIC does not explicitly models fine root biomass. We therefore calculate the fraction of fine root biomass using an empirical relationship that is very similar to the relationship developed by Kurz et al. (1996) (their equation 5) but also works below total root biomass of 0.33 Kg C m$^{-2}$ (the Kurz et al. (1996) relationship yields a fraction of fine root more than 1.0 below this threshold). The fraction of fine root biomass ($f_r$) is given by

\[
f_r = 1 - \frac{C_R}{C_R + 0.6}
\]  \hspace{1cm} (A5)

where $C_R$ is the root biomass (KgC m$^{-2}$) simulated by the biogeochemical module of CLASSIC. Equation (A5) yields fine root fraction approaching 1.0 as $C_R$ approaches 0, so at very low root biomass values all roots are considered fine roots. For grasses the fraction of fine root biomass is set to 1. The maximum or potential active N uptake is given by
\[U_{a,\text{pot,NH}_4} = \frac{\varepsilon \, f_r \, c_R \, N_{\text{NH}_4}}{k_{p,\frac{1}{2}} \, r_d + N_{\text{NH}_4} + N_{\text{NO}_3}}\]
\[U_{a,\text{pot,NO}_3} = \frac{\varepsilon \, f_r \, c_R \, N_{\text{NO}_3}}{k_{p,\frac{1}{2}} \, r_d + N_{\text{NH}_4} + N_{\text{NO}_3}}\]

where \(\varepsilon\) is the efficiency of fine roots to take up N per unit fine root mass per day \((\text{gN gC}^{-1} \text{ day}^{-1})\), \(k_{p,\frac{1}{2}}\) is the half saturation constant \((\text{gN m}^{-3})\), and \(N_{\text{NH}_4}\) and \(N_{\text{NO}_3}\) are the ammonium and nitrate pool sizes \((\text{gN m}^{-2})\) as mentioned earlier. Depending on the geographical location and the time of the year, if passive uptake alone can satisfy the plant demand the actual active N uptake of \(\text{NH}_4\) \((U_{a,\text{actual,NH}_4})\) and \(\text{NO}_3\) \((U_{a,\text{actual,NO}_3})\) is set to zero. Conversely, during other times both passive and potential active N uptakes may not be able to satisfy the demand and in this case actual active N uptake is equal to its potential rate. At times other than these, the actual active uptake is lower than its potential value. This adjustment of actual active uptake is illustrated in equation (A7).

If \((\Delta WP \leq U_{p,\text{NH}_4} + U_{p,\text{NO}_3})\)
\[
U_{a,\text{actual,NH}_4} = 0
\]
\[
U_{a,\text{actual,NO}_3} = 0
\]

If \((\Delta WP > U_{p,\text{NH}_4} + U_{p,\text{NO}_3}) \land (\Delta WP < U_{p,\text{NH}_4} + U_{p,\text{NO}_3} + U_{a,\text{pot,NH}_4} + U_{a,\text{pot,NO}_3})\)
\[
U_{a,\text{actual,NH}_4} = (\Delta WP - U_{p,\text{NH}_4} - U_{p,\text{NO}_3}) \frac{U_{a,\text{pot,NH}_4}}{U_{a,\text{pot,NH}_4} + U_{a,\text{pot,NO}_3}}
\]
\[
U_{a,\text{actual,NO}_3} = (\Delta WP - U_{p,\text{NH}_4} - U_{p,\text{NO}_3}) \frac{U_{a,\text{pot,NO}_3}}{U_{a,\text{pot,NH}_4} + U_{a,\text{pot,NO}_3}}
\]

If \((\Delta WP \geq U_{p,\text{NH}_4} + U_{p,\text{NO}_3} + U_{a,\text{pot,NH}_4} + U_{a,\text{pot,NO}_3})\)
\[
U_{a,\text{actual,NH}_4} = U_{a,\text{pot,NH}_4}
\]
\[
U_{a,\text{actual,NO}_3} = U_{a,\text{pot,NO}_3}
\]

Finally, the total N uptake \((U)\), uptake of \(\text{NH}_4^+\) \((U_{\text{NH}_4})\) and \(\text{NO}_3^-\) \((U_{\text{NO}_3})\), are calculated as
\[
U = U_{p,NH4} + U_{p,NO3} + U_{a,actual,NH4} + U_{a,actual,NO3} \\
U_{NH4} = U_{p,NH4} + U_{a,actual,NH4} \\
U_{NO3} = U_{p,NO3} + U_{a,actual,NO3}
\] (A8)

A2.4 Litterfall

Nitrogen litterfall from the vegetation components is directly tied to the carbon litterfall calculated by the phenology module of CLASSIC through their current C:N ratios.

\[
LF_i = \frac{(1-r_L)LF_{i,C}}{C:N_i}, i = L, S, R
\] (A9)

where \(LF_{i,C}\) is the carbon litterfall rate (gC day\(^{-1}\)) for component \(i\), calculated by the phenology module of CLASSIC, and division by its current C:N ratio yields the nitrogen litterfall rate, \(r_L\) is the leaf resorption coefficient that simulates the resorption of N from leaves of deciduous tree PFTs before they are shed and \(r_i = 0, i = R, S\). Litter from each vegetation component is proportioned between structural and non-structural components according to their pool sizes.

A2.5 Allocation and reallocation

Plant N uptake by roots is allocated to leaves and stem to satisfy their N demand. When plant N demand is greater than zero, total N uptake \((U)\) is divided between leaves, stem, and root components in proportion to their demands such that the allocation fractions for N \((a_i, i = L, S, R)\) are calculated as

\[
a_i = \frac{\Delta_i}{\Delta_{WP}} , i = L, S, R \\
A_{R2L} = a_L (U_{NH4} + U_{NO3}) \\
A_{R2S} = a_S (U_{NH4} + U_{NO3})
\] (A10)
where $A_{R2L}$ and $A_{R2S}$ are the amounts of N allocated from root to leaves and stem components, respectively, as mentioned in the main text for equation (8). During periods of negative NPP due to adverse climatic conditions (e.g. during winter or drought seasons) the plant N demand is set to zero but passive N uptake, associated with transpiration, may still be occurring if the leaves are still on. Even though there is no N demand, passive N uptake still needs to be partitioned among the vegetation components. During periods of negative NPP allocation fractions for N are, therefore, calculated in proportion to the minimum PFT-dependent C:N ratios of the leaves, stem, and root components as follows.

$$a_i = \frac{1/C:N_{i\min}}{1/C:N_{L\min} + 1/C:N_{S\min} + 1/C:N_{R\min}}, \ i = L, S, R \quad (A11)$$

For grasses, which do not have a stem component, equations (A10) and (A11) are modified accordingly by removing the terms associated with the stem component.

Three additional rules override these general allocation rule specifically for deciduous tree PFTs (or deciduous PFTs in general). First, no N allocation is made to leaves once leaf fall is initiated for deciduous tree PFTs and plant N uptake is proportioned between stem and root components based on their demands in a manner similar to equation (A10). Second, for deciduous tree PFTs, a fraction of leaf N is resorbed from leaves back into stem and root as follows

$$R_{L2R} = r_L L F_L \frac{N_{R,NS}}{N_{R,NS} + N_{S,NS}}$$

$$R_{L2S} = r_L L F_L \frac{N_{S,NS}}{N_{R,NS} + N_{S,NS}} \quad (A12)$$
where \( r_L \) is the leaf resorption coefficient, as mentioned earlier, and \( LF_L \) is the leaf litter fall rate.

Third, and similar to resorption, at the time of leaf onset for deciduous tree PFTs, N is reallocated to leaves (in conjunction with reallocated carbon as explained in Asaadi et al. (2018)) from stem and root components.

\[
R_{R2L} = \frac{R_{R2L,C}}{C:N_L} \cdot \frac{N_{R,NS}}{N_{R,NS} + N_{S,NS}} \]
\[
R_{S2L} = \frac{R_{S2L,C}}{C:N_L} \cdot \frac{N_{S,NS}}{N_{R,NS} + N_{S,NS}} \]  

(A13)

where \( R_{R2L,C} \) and \( R_{S2L,C} \) represent reallocation of carbon from non-structural stem and root components to leaves and division by \( C:N_L \) converts the flux into N units. The reallocation demand for N, at the time of leaf onset, is proportioned between non-structural pools of stem and root according to their sizes.

**A2.6 N mineralization, immobilization, and humification**

Decomposition of litter \( (R_{R,H}) \) and soil organic matter \( (R_{H,H}) \) releases C to the atmosphere and this flux is calculated by the heterotrophic respiration module of CLASSIC. The amount of N mineralized is calculated straightforwardly by division with the current C:N ratios of the respective pools and contributes to the \( \text{NH}_4^+ \) pool.

\[
M_{D,NH4} = \frac{R_{h,D}}{C:N_D} \]
\[
M_{H,NH4} = \frac{R_{h,H}}{C:N_H} \]  

(A14)

An implication of mineralization contributing to the \( \text{NH}_4^+ \) pool, in addition to BNF and fertilizer inputs that also contribute solely to the \( \text{NH}_4^+ \) pool, is that the simulated \( \text{NH}_4^+ \) pool is typically
larger than the NO$_3^-$ pool. The exception is the dry and arid regions where the lack of
denitrification, as discussed below in Section A.3.2., leads to a build up of the NO$_3^-$ pool.

Immobilization of mineral N from the NH$_4^+$ and NO$_3^-$ pools into the soil organic matter
pool is meant to keep the soil organic matter C:N ratio ($C: N_H$) at its specified value of 13 for all
PFTs in a manner similar to Wania et al. (2012) and Zhang et al. (2018). A value of 13 is within
the range of observation-based estimates which vary from about 8 to 25 (Zinke et al., 1998; Tipping
et al., 2016). Although $C: N_H$ varies geographically, the driving factors behind this variability
remain unclear. It is even more difficult to establish if increasing atmospheric CO$_2$ is changing
$C: N_H$ given the large heterogeneity in soil organic C and N densities, and the difficulty in
measuring small trends for such large global pools. We therefore make the assumption that the
$C: N_H$ does not change with time. An implication of this assumption is that as GPP increases with
increasing atmospheric CO$_2$ rises, and plant litter becomes enriched in C with increasing C:N ratio
of litter, more and more N is locked up in the soil organic matter pool because its C:N ratio is
fixed. As a result, mineral N pools of NH$_4^+$ and NO$_3^-$ decrease in size and plant N content
subsequently follows. This is consistent with studies of plants grown in elevated CO$_2$
environment. For example, Cotrufo et al. (1998) summarize results from 75 studies and find an
average 14% reduction in N concentration for above-ground tissues. Wang et al. (2019) find
increased C concentration by 0.8–1.2% and a reduction in N concentration by 7.4–10.7% for rice
and winter wheat crop rotation system under elevated CO$_2$.

Immobilization from both the NH$_4^+$ and NO$_3^-$ pools is calculated in proportion to their pool
sizes, employing the fixed $C: N_H$ ratio as
Finally, the carbon flux of humified litter from the litter to the soil organic matter pool \(H_{C,D2H}\) is also associated with a corresponding N flux that depends on the C:N ratio of the litter pool.

\[
O_{NH4} = \max\left(0, \left(\frac{C_H}{C:N_H} - N_H\right) \frac{N_{NH4}}{N_{NH4} + N_{NO3}}\right)
\]

\[
O_{NO3} = \max\left(0, \left(\frac{C_H}{C:N_H} - N_H\right) \frac{N_{NO3}}{N_{NH4} + N_{NO3}}\right)
\]

(A15)

\[
H_{N,D2H} = \frac{H_{C,D2H}}{C:N_D}
\]

(A16)

### A3. N cycling in mineral pools and N outputs

This section presents the parameterizations of nitrification (which results in transfer of N from the \(NH_4^+\) to the \(NO_3^-\) pool) and the associated gaseous fluxes of \(N_2O\) and \(NO\) (referred to as nitrifier denitrification), gaseous fluxes of \(N_2O\), \(NO\), and \(N_2\) associated with denitrification, volatilization of \(NH_4\) into \(NH_3\), and leaching of \(NO_3^-\) in runoff.

#### A3.1 Nitrification

Nitrification, the oxidative process converting ammonium to nitrate, is driven by microbial activity and as such constrained both by high and low soil moisture (Porporato et al., 2003). At high soil moisture content there is little aeration of soil and this constrains aerobic microbial activity, while at low soil moisture content microbial activity is constrained by moisture limitation. In CLASSIC, the heterotrophic respiration from soil carbon is constrained similarly but rather than using soil moisture the parameterization is based on soil matric potential (Arora, 2003; Melton et al., 2015). Here, we use the exact same parameterization. In addition to soil moisture, nitrification \((gN \ m^{-2} \ day^{-1})\) is modelled as a function of soil temperature and the size of the \(NH_4^+\) pool as follows
\[
I_{NO3} = \eta f_1(T_{0.5}) f_i(\psi) N_{NH4}
\]  
(A17)

where \(\eta\) is the nitrification coefficient (day\(^{-1}\)), \(f_1(\psi)\) is the dimensionless soil moisture scalar that varies between 0 and 1 and depends on soil matric potential \((\psi)\), \(f_1(T_{0.5})\) is the dimensionless soil temperature scalar that depends on average soil temperature \((T_{0.5})\) over the top 0.5 m soil depth over which nitrification is assumed to occur (following Xu-Ri and Prentice, 2008), and \(N_{NH4}\) is the ammonium pool size (gN m\(^{-2}\)), as mentioned earlier. Both \(f_1(T_{0.5})\) and \(f_1(\psi)\) are parameterized following Arora (2003) and Melton et al. (2015). \(f_1(T_{0.5})\) is a Q\(_{10}\) type function with a temperature dependent \(Q_{10}\)

\[
f_1(T_{0.5}) = Q_{10,i}^{(T_{0.5} - 20)/10}, Q_{10,i} = 1.44 + 0.56 \left( \tanh(0.075(46 - T_{0.5})) \right)
\]  
(A18)

The reference temperature for nitrification is set to 20 °C following Lin et al. (2000). \(f_1(\psi)\) is parameterized as a step function of soil matric potential \((\psi)\) as

\[
f_1(\psi) = \begin{cases} 
0.5 & \text{if } \psi \leq \psi_{sat} \\
1 - 0.5 \frac{\log(0.4) - \log(\psi)}{\log(0.4) - \log(\psi_{sat})} & \text{if } 0.4 > \psi \geq \psi_{sat} \\
1 & \text{if } 0.6 \geq \psi \geq 0.4 \\
1 - 0.8 \frac{\log(\psi) - \log(0.6)}{\log(100) - \log(0.6)} & \text{if } 100 > \psi > 0.6 \\
0.2 & \text{if } \psi > 100
\end{cases}
\]  
(A19)

where the soil matric potential \((\psi)\) is found, following Clapp and Hornberger (1978), as a function of soil moisture \((\theta)\)

\[
\psi(\theta) = \psi_{sat} \left( \frac{\theta}{\theta_{sat}} \right)^B.
\]  
(A20)

Saturated matric potential \((\psi_{sat})\), soil moisture at saturation (i.e. porosity) \((\theta_{sat})\), and the parameter \(B\) are calculated as functions of percent sand and clay in soil following Clapp and
Hornberger (1978) as shown in Melton et al. (2015). The soil moisture scalar $f_i(\psi)$ is calculated individually for each soil layer and then averaged over the soil depth of 0.5 m over which nitrification is assumed to occur.

Gaseous fluxes of NO ($I_{NO}$) and N$_2$O ($I_{N2O}$) associated with nitrification, and generated through nitrifier denitrification, are assumed to be directly proportional to the nitrification flux ($I_{NO3}$) as

$$
I_{NO} = \eta_{NO} I_{NO3} \\
I_{N2O} = \eta_{N2O} I_{NO3}
$$

(A21)

where $\eta_{NO}$ and $\eta_{N2O}$ are dimensionless fractions which determine what fractions of nitrification flux are emitted as NO and N$_2$O.

**A3.2 Denitrification**

Denitrification is the stepwise microbiological reduction of nitrate to NO, N$_2$O, and ultimately to N$_2$ in complete denitrification. Unlike nitrification, however, denitrification is primarily an anaerobic process (Tomasek et al., 2017) and therefore occurs when soil is saturated. As a result, we use a different soil moisture scalar than for nitrification. Similar to nitrification, denitrification is modelled as a function of soil moisture, soil temperature and the size of the NO$_3^-$ pool as follows to calculate the gaseous fluxes of NO, N$_2$O, and N$_2$.

$$
E_{NO} = \mu_{NO} f_E(T_{0.5}) f_E(\theta) N_{NO3} \\
E_{N2O} = \mu_{N2O} f_E(T_{0.5}) f_E(\theta) N_{NO3} \\
E_{N2} = \mu_{N2} f_E(T_{0.5}) f_E(\theta) N_{NO3}
$$

(A22)

where $\mu_{NO}$, $\mu_{N2O}$, and $\mu_{N2}$ are coefficients (day$^{-1}$) that determine daily rates of emissions of NO, N$_2$O, and N$_2$. The temperature scalar $f_E(T_{0.5})$ is exactly the same as the one for nitrification
\( f_1(T_{0.5}) \) since denitrification is also assumed to occur over the same 0.5 soil depth. The soil moisture scalar \( f_E(\theta) \) is given by

\[
\begin{align*}
f_E(\theta) &= 1 - \tanh\left(2.5 \left( \frac{1-w(\theta)}{1-w_d} \right)^2 \right) \\
w(\theta) &= \max\left(0, \min\left(1, \frac{\theta - \theta_w}{\theta_f - \theta_w}\right)\right)
\end{align*}
\]  
(A23)

where \( w \) is the soil wetness that varies between 0 and 1 as soil moisture varies between wilting point \( (\theta_w) \) and field capacity \( (\theta_f) \), and \( w_d \) is the threshold soil wetness for denitrification below which very little denitrification occurs. Since very little denitrification occurs when soil wetness is below \( w_d \) this leads to build up of the \( \text{NO}_3^- \) pool in arid regions.

**A3.3 \( \text{NO}_3^- \) leaching**

Leaching is the loss of water-soluble ions through runoff. In contrast to positively charged \( \text{NH}_4^+ \) ions (i.e. cations), the \( \text{NO}_3^- \) ions do not bond to soil particles because of the limited exchange capacity of soil for negatively charged ions (i.e. anions). As a result, leaching of N in the form of \( \text{NO}_3^- \) ions is a common water quality problem, particularly over cropland regions. The leaching flux \( (L_{\text{NO}_3}, \text{gN m}^{-2} \text{ day}^{-1}) \) is parameterized to be directly proportional to baseflow \( (b_t, \text{Kg m}^{-2} \text{ s}^{-1}) \) calculated by the physics module of CLASSIC and the size of the \( \text{NO}_3 \) pool \( (N_{\text{NO}_3}, \text{gN m}^{-2}) \).

Baseflow is the runoff rate from the bottommost soil layer.

\[
L_{\text{NO}_3} = 86400 \, \varphi \, b_t \, N_{\text{NO}_3}
\]

(A24)

where the multiplier 86400 converts units to per day, and \( \varphi \) is the leaching coefficient \( (\text{m}^2 \text{ Kg}^{-1}) \) that can be thought of as the soil particle surface area \( (\text{m}^2) \) that 1 Kg of water (or about 0.001 m\(^3\)) can effectively wash to leach the nutrients.
A3.4 NH₃ volatilization

NH₃ volatilization \((V_{NH₃}, \text{gN m}^{-2}\text{ day}^{-1})\) is parametrized as a function of pool size of NH₄⁺, soil temperature, soil pH, aerodynamic and boundary layer resistances, and atmospheric NH₃ concentration in a manner similar to Riddick et al. (2016) as

\[
V_{NH₄} = \vartheta \frac{1}{r_a + r_b} \left( \chi - [\text{NH₃,a}] \right)
\]

(A25)

where \(\vartheta\) is the dimensionless NH₃ volatilization coefficient which is set to less than 1 to account for the fact that a fraction of ammonia released from the soil is captured by vegetation, \(r_a\) (s m\(^{-1}\)) is the aerodynamic resistance calculated by the physics module of CLASSIC, \(\chi\) is the ammonia (NH₃) concentration at the interface of the top soil layer and the atmosphere (g m\(^{-3}\)), \([\text{NH₃,a}]\) is the atmospheric NH₃ concentration specified at \(0.3\times10^{-6}\) g m\(^{-3}\) following Riddick et al. (2016), 86400 converts flux units from gN m\(^{-2}\) s\(^{-1}\) to gN m\(^{-2}\) day\(^{-1}\), and \(r_b\) (s m\(^{-1}\)) is the boundary layer resistance calculated following Thom (1975) as

\[
r_b = 6.2 u_*^{0.67}
\]

(A26)

where \(u_*\) (m/s) is the friction velocity provided by the physics module of CLASSIC. The ammonia (NH₃) concentration at surface (\(\chi\)), in a manner similar to Riddick et al. (2016), is calculated as

\[
\chi = 0.26 \frac{N_{NH₄}}{1 + K_H + K_H[H^+] / K_{NH₄}}
\]

(A27)

where the coefficient 0.26 is the fraction of ammonium in the top 10 cm soil layer assuming exponential distribution of ammonium along the soil depth (given by \(3e^{-3z}\), where \(z\) is the soil depth), \(K_H\) (dimensionless) is the Henry’s law constant for NH₃, \(K_{NH₄}\) (mol L\(^{-1}\)) is the dissociation equilibrium constant for aqueous NH₃, and \(H^+\) (mol L\(^{-1}\)) is the concentration of hydrogen ion.
that depends on the soil pH \((H^+ = 10^{-pH})\). \(K_H\) and \(K_{NH4}\) are modelled as functions of soil temperature of the top 10 cm soil layer \((T_{0.1})\) following Riddick et al. (2016) as

\[
K_H = 4.59 \ T_{0.1} \ \exp \left(4092 \ \left( \frac{1}{T_{0.1}} - \frac{1}{T_{ref,v}} \right) \right) \\
K_{NH4} = 5.67 \times 10^{-10} \ \exp \left(-6286 \ \left( \frac{1}{T_{0.1}} - \frac{1}{T_{ref,v}} \right) \right)
\]

(A28)

where \(T_{ref,v}\) is the reference temperature of 298.15 K.