A triple tree-ring constraint for tree growth and physiology in a global land surface model

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Abstract. Annually-resolved tree-ring records extending back to pre-industrial conditions have the potential to constrain the responses of global land surface models at interannual to centennial time scales. Here, we demonstrate a framework to simultaneously constrain the representation of tree growth and physiology in the ORCHIDEE global land surface model using the simulated variability of tree-ring width and carbon ($\Delta^{13}C$) and oxygen ($\delta^{18}O$) stable isotopes in six sites in boreal and temperate Europe. We exploit the resulting tree-ring triplet to derive integrative constraints for leaf physiology and growth from well-known mechanistic relationships among the variables. ORCHIDEE simulates $\Delta^{13}C$ ($r = 0.31-0.80$) and $\delta^{18}O$ ($r = 0.36-0.74$) better than tree-ring width ($r < 0.55$), with an overall skill similar to that of a tree-ring model (MAIDENiso) and another isotope-enabled global vegetation model (LPX-Bern). The comparison with tree-ring data showed that growth variability is not well represented in ORCHIDEE, and that the parameterization of leaf-level physiological responses (stomatal control) to drought stress in the temperate region can be constrained using the interannual variability of tree-ring stable isotopes. The representation of carbon storage and remobilization dynamics emerged as a critical process to improve the realism of simulated growth variability, temporal carryover and recovery of forest ecosystems after climate extremes. Simulated forest Gross Primary Productivity (GPP) correlates with simulated tree-ring $\Delta^{13}C$ and $\delta^{18}O$ variability, but the origin of the correlations with tree-ring $\delta^{18}O$ is not entirely physiological. The integration of tree-ring data and land surface models as demonstrated here should guide model improvements and contribute towards reducing current uncertainties in forest carbon and water cycling.

1 Introduction

A major challenge for the Land Surface Model (LSM) component of Earth System models is to accurately simulate the historical and future dynamical coupling between the global biosphere and climate (Friedlingstein et al., 2014). Although LSMs are skillful at reproducing short-term (<20 years) contemporary observations of plant water and carbon cycling, their simulated responses to environmental changes at longer time scales from decades to century are still highly uncertain and contribute to the spread in current climate change projections (Ciais et al., 2013; Friedlingstein et al., 2014). Some of these models project that the terrestrial biosphere will continue behaving as a carbon sink of anthropogenic emissions during the course of the
century, while others simulate that it will turn into an additional carbon source to the atmosphere that will accelerate climate change (Friedlingstein et al., 2006; Jones et al., 2013; Friedlingstein et al., 2014). The uncertainties in simulated long-term trends are also evident for the water cycle and over the historical period (Frank et al., 2015; Phillips et al., 2019). The lack of a general agreement on the historical and future long-term responses of the terrestrial biosphere in land surface models thus limit confidence in future climate projections (Ciais et al., 2013).

The development, parameterization and evaluation of current land surface models have been based on a handful of manipulative experiments (Ainsworth and Long, 2005; Smith et al., 2015; Andresen et al., 2016; Song et al., 2019), a quasi-global network of eddy-covariance observations, Earth observations and forest inventories covering the last few decades. Most of these data streams are not able to reveal the temporal evolution of plant responses to global change factors at multi-decadal and longer time scales, where mechanistic understanding on how trees perish or adapt to environmental change is still limited (McDowell et al., 2008; Cailleret et al., 2018). Tree-ring width and their carbon ($\delta^{13}$C) and oxygen ($\delta^{18}$O) stable isotope data are increasingly being used to address the lack of direct observations on long-term changes in plant physiology and growth with global change (Huang et al., 2007; Frank et al., 2015; Girardin et al., 2016; Babst et al., 2018; de Boer et al., 2019; Lavergne et al., 2020), and could provide the much needed long-term benchmark for land surface models (Zuidema et al., 2018).

In recent decades, some dendrochronological and forest process-based models have successfully integrated the simulation of tree-ring width with stable isotopes in order to interpret measurements and improve simulated tree water status, photosynthesis and growth (Fritts et al., 1999; Hemming et al., 2001; Ogée et al., 2009; Eglin et al., 2010; Danis et al., 2012; Wei et al., 2014; Ulrich et al., 2019). Radial growth is represented with decreasing complexity from tree to stand-level models, considering different degrees of integration of controls from sources (photosynthesis and allocation) and sinks (cell growth) of carbon in the trees (Vaganov et al., 2011; Körner, 2015). The tree-ring community has developed a detailed source-sink representation of radial growth for conifers as the product of daily cambial dynamics and wood formation (i.e., cell division, enlargement, and wall thickening), coupled or not to a full representation of tree-level photosynthesis and carbon allocation (Fritts et al., 1999; Hemming et al., 2001; Vaganov et al., 2011; Drew and Downes, 2015). Stand-level forest models parameterize radial growth of conifers and angiosperms as a direct dependency of photosynthesis, using the allocation of photosynthates and tree allometry (Deleuze et al., 2004; Misson, 2004; Sato et al., 2007; Li et al., 2014). A well-known stand-level tree-ring model using this approach is MAIDENiso (Danis et al., 2012; Lavergne et al., 2017), which has the unique triple capability to simulate radial growth and oxygen and carbon isotopic ratios in tree rings.

The representation of tree biomass growth in global land surface models is still rudimentary and is one of the critical areas where much improvement is needed (Fatichi et al., 2014; Körner, 2015; Jones et al., 2020). Like stand-level models, most global models represent growth using a simple carbon-source approach and consider it as the difference between instantaneous photosynthetic carbon assimilation and respiration. Sink processes of wood formation, emphasized in tree-level models (Vaganov et al., 2011), are neglected (Fatichi et al., 2014). Reserve pools of labile carbon are only recently being considered because of the need to realistically represent continued forest growth when photosynthesis is suppressed by environmental stresses (Naudts et al., 2015; Vuichard et al., 2019; Jones et al., 2020). Currently there is no global land surface model with the capability to explicitly simulate tree-ring width. Nevertheless, tree-ring width data have been used as an indirect benchmark
for the interannual variability of simulated Net Primary Productivity in some global land surface models (Rammig et al., 2015; Churakova et al., 2016). In contrast to ring width, tree-ring δ¹³C or δ¹⁸O stable isotopes have already been incorporated in some global land surface models such as FOREST-BGC (Panek and Waring, 1997), ORCHIDEE (Shi et al., 2011; Churakova et al., 2016; Risi et al., 2016), JULES (Bodin et al., 2013), LPX-Bern (Saurer et al., 2014; Keel et al., 2016; Keller et al., 2017) and CLM4.5 (Raczka et al., 2016; Keller et al., 2017).

An enormous benefit of explicitly modelling tree-ring width and stable isotopes in the global land surface models is the ability to directly compare readily available tree-ring data to modelled data. Thus, the global models can be evaluated and improved with freely available worldwide tree-ring data found, for example, in the ITRDB and tree-ring laboratories around the world. Furthermore, the interpretation of these tree-ring data can be supported by model simulations. The comparison of simulated δ¹³C and derived physiological indicators such as the carbon isotopic discrimination (Δ¹³C) by plants and the intrinsic water use efficiency (iWUE) with direct tree-ring isotopic measurements has helped benchmarking stomatal responses to drought stress and rising atmospheric CO₂ concentrations in the global models (Panek and Waring, 1997; Bodin et al., 2013; Saurer et al., 2014; Keller et al., 2017). Simulated δ¹⁸O has been used to evaluate the representation of hydrological processes along the soil-plant-atmosphere continuum (Risi et al., 2016) and interpret the variability in tree-ring δ¹⁸O data in terms of climatic drivers and source water δ¹⁸O (Shi et al., 2011; Keel et al., 2016; Churakova et al., 2016). The interannual variability of tree-ring δ¹³C and δ¹⁸O has been shown to correlate with local eddy-covariance measurements of forest productivity (Belmecheri et al., 2014; Tei et al., 2019). A recent study showed that the relationship holds at regional scale and is stronger for δ¹⁸O than δ¹³C and tree-ring width (Levesque et al., 2019), suggesting that tree-ring isotopic variability might integrate large-scale physiological signals useful to evaluate global carbon cycle models. Yet, stable isotope-productivity relationships have not been studied in this type of models.

Empirical tree-ring studies frequently combine δ¹⁸O and δ¹³C as a means to mechanistically interpret plant physiological responses (Saurer et al., 1997; Scheidegger et al., 2000; Barnard et al., 2012; Roden and Farquhar, 2012; Szejner et al., 2020). In contrast, most of the studies with land surface models have focused on the simulation and evaluation of a single tree-ring variable (Saurer et al., 2014; Keel et al., 2016; Keller et al., 2017). Key developments in the ORCHIDEE global land surface model now allow to explicitly simulate radial growth (Bellassen et al., 2010; Naudts et al., 2015; Jeong et al., 2020) and carbon and oxygen composition in tree-ring cellulose (Risi et al., 2016) as done in the MAIDENiso tree-ring model (Danis et al., 2012). This offers the opportunity to explore how multiple tree-ring variables can be used to constrain the long-term plant responses simulated by global land surface models and identify processes that need to be better represented or parameterized.

The aims of this study are to (i) integrate key developments and identify the critical processes to concurrently simulate the interannual variability of tree-ring width and its carbon (Δ¹³C) and oxygen stable isotopes in the ORCHIDEE global land surface model, (ii) develop a conceptual triple tree-ring constraint for simulated growth and physiology that exploits the mechanistic relationships among tree-ring variables, and (iii) evaluate the simulated relationships between productivity and tree-ring carbon and oxygen stable isotopes. We first assess and compare the ability of ORCHIDEE and MAIDENiso models to simulate 20th century tree-ring width and isotopic variability, and their inter-relationships in the Fontainebleau forest in France. Then, we run ORCHIDEE in five other sites along a climate gradient from boreal Finland to temperate France, and
compare its ability to simulate $\delta^{18}$O variability in the gradient with that of the LPX-Bern global vegetation model (Keel et al., 2016). The simulated relationships between isotopic variability and productivity in ORCHIDEE are also evaluated along the gradient.

2 Model and evaluation data

2.1 Model description

The global land surface model ORCHIDEE (Krinner et al., 2005) is the terrestrial component of the IPSL (Institut Pierre Simon Laplace) Earth System model (Dufresne et al., 2013; Boucher et al., 2020). ORCHIDEE simulates the half-hourly exchange of energy, carbon and water between the terrestrial biosphere and the atmosphere, either coupled with the LMDz (Laboratoire de Météorologie Dynamique Zoom) general circulation model (Hourdin et al., 2006) or forced by observed meteorology.

The global forests are represented by eight Plant Functional Types (PFTs) described by a common set of governing equations with specific parameter values, with the only exception of some PFT-specific phenology representations (Krinner et al., 2005). Canopy photosynthesis is based on the leaf-level photosynthesis formulation of Farquhar et al. (1980) and together with respiration, the energy balance and hydrological processes are simulated at a half-hourly time step, which is the typical resolution of eddy-covariance measurements of carbon and water fluxes (Baldocchi et al., 2001). Leaf gas exchange is simulated by coupling the photosynthesis model with the stomatal conductance model of Ball et al. (1987). The CO$_2$ demand is determined as the minimum of Rubisco carboxylation and RuBP regeneration, while CO$_2$ supply depends on the difference in CO$_2$ concentration between the air outside the leaf and the carboxylation sites. Carbon allocation to the different vegetation pools, phenology and mortality are calculated at a daily time step.

Soil hydrology is modelled using a surface and a deep reservoir (Choisnel et al., 1995). Water enters the surface layer via throughfall, snow melt, and dew and frost. Water can leave the soil reservoir through transpiration, bare soil evaporation, surface runoff and drainage. Plant water stress is calculated at half-hourly time steps as a function of soil water content (McMurtrie et al., 1990) weighted by root mass. Water stress reduces transpiration through a direct reduction of stomatal conductance as soil moisture depletes.

The key developments used for simulating tree-ring parameters include the addition of a forest management module (Bellassen et al., 2010) and the simulation of oxygen stable isotope ratios along the soil-plant-atmosphere continuum (Risi et al., 2016). The model code used in this study (SVN r898 version) precede the current code that merged the nitrogen cycle and canopy structure in ORCHIDEE r5698 (Naudts et al., 2015; Vuichard et al., 2019), where the tree-ring functionality will also be ported (Jeong et al., 2020).

2.1.1 Tree-ring width

The forest management module explicitly simulates the temporal trajectory of stem growth of trees in a size-structured forest stand. The size structure of the stand is prescribed by defining a starting density of trees per hectare distributed across a number
of stem diameter size classes, typically following an inverted-J distribution. Initial tree height and biomass are obtained by allometric relationships with stem diameter (Bellassen et al., 2010). For each PFT, photosynthesis and NPP are computed at the stand level at half-hourly and daily steps, respectively.

At the end of the year, accumulated woody NPP increment is allocated across the different diameter classes following an empirical competition rule for even-aged stands (Deleuze et al., 2004). A greater NPP share is allocated to larger dominant trees compared to smaller less vigorous trees, emulating the competition for light and resources within the stand. The absolute annual stem growth increment in the allocation rule is determined by a parameter (\( \lambda \)) that defines the slope between the fraction of NPP allocated to each diameter class and the mean diameter of the class. A second parameter (\( \sigma \)) represents a diameter threshold below which less vigorous trees receive only a fixed part of the yearly stand NPP increment. The stem growth of the largest and smallest tree is tracked individually through the entire simulation (Bellassen et al., 2010).

Simulated tree-ring width (i.e., radial growth) for each diameter class was computed from annual increments in stem circumference as follows:

\[
TRW_t = \frac{Circ_t - Circ_{t-1}}{2\pi}
\]

where \( TRW_t \) is the annual tree-ring width in millimetres for year \( t \) and \( Circ_t \) and \( Circ_{t-1} \) are the stem circumferences for the current year and the previous year, respectively. The annual ring-widths simulated in this scheme account for the size-related trend in stem growth increment and PFT-specific tree allometry, providing a mean representation of radial growth for trees across a range of sizes that can be meaningfully compared with measured tree-ring width data. However, in this formulation tree-ring width variability depends only on direct GPP allocation (i.e., it is a carbon-source driven process) and does not consider the dynamics of carbon storage or wood formation processes that can account for a large fraction of observed interannual tree-ring width variation (Misson, 2004).

### 2.1.2 Tree-ring carbon isotopes

To eliminate the effect of \( \delta^{13}C \) of atmospheric CO\(_2\) and preserve only the effects of plant metabolic processes, the \(^{13}C \) enrichment of plant organic material is usually expressed in terms of the carbon isotope discrimination (\( \Delta^{13}C \)). Differences between the \(^{13}C \) enrichment of atmospheric CO\(_2\) and plant material are attributed to discriminatory processes during photosynthesis.

Photosynthetic carbon isotope discrimination was estimated at half-hourly time steps using the simple formulation of Farquhar et al. (1982) for C3 plants:

\[
\Delta^{13}C = a + (b - a) \frac{c_i}{c_a}
\]

where \( a \) (4.4‰) is the kinetic discrimination associated with diffusion between free air and the stomatal cavity, \( b \) (27‰) is the fractionation during CO\(_2\) fixation by the Rubisco enzyme, \( c_i \) is the leaf internal CO\(_2\) concentration simulated by ORCHIDEE and \( c_a \) is the atmospheric CO\(_2\) concentration prescribed from measurements (McCarroll and Loader, 2004). Annual tree-ring carbon discrimination (\( \Delta^{13}C_R \)) was then calculated as the mean of the half-hourly discrimination values in the above-ground
biomass weighted by Gross Primary Productivity (GPP) between the start \((SOS)\) and the end \((EOS)\) of the growing season:

\[
\Delta^{13}C_R = \frac{1}{\sum_{n=SOS}^{EOS} GPP(n)} \sum_{n=SOS}^{EOS} (\Delta^{13}C(n) \times GPP(n))
\]  

(3)

This formulation for carbon discrimination is commonly used as a simple approximation for discrimination derived from measured \(\delta^{13}C\) in tree-ring cellulose (Francey and Farquhar, 1982). For simplicity, it assumes that further post-photosynthetic fractionation during photo- and dark-respiration and carbohydrate remobilization and storage is negligible. Although these processes normally have an important impact on whole-ring cellulose isotopic composition (Gessler et al., 2009; Werner et al., 2012), at least the impact of carbon remobilization is minimal in the latewood component of tree rings (Helle and Schleser, 2004). The \(c_i\) term in Eq. (2) integrates the gas exchange dynamics (i.e., stomatal conductance and photosynthesis) simulated by the model as a complex function of micrometeorological variability, seasonal water stress, and the long-term warming and increase in \(c_o\). Hence, despite its simplicity, simulated carbon discrimination using Eq. (2) has been shown to be valuable to constrain the integrated environmental response of land surface models using carbon discrimination derived from tree-ring \(\delta^{13}C\) measurements (e.g., Bodin et al., 2013; Churakova et al., 2016; Keel et al., 2016).

### 2.1.3 Tree-ring oxygen isotopes

The \(\delta^{18}O\) signature in tree-ring cellulose reflects primarily the isotopic composition of soil water and the evaporative enrichment of leaf water due to transpiration, but other mixing and biochemical fractionation processes during water transport along the soil-plant-atmosphere continuum also contribute to the final \(\delta^{18}O\) signature (Gessler et al., 2014). The \(\delta^{18}O\) isotopic composition of the source water used by plants may originate from rainfall or groundwater, while the \(\delta^{18}O\) isotopic enrichment of leaf water depends strongly on vapour pressure deficit (i.e., the ratio of the vapour pressure in the atmosphere and the intercellular spaces of the leaves) or relative humidity (Farquhar et al., 1998; Scheidegger et al., 2000).

The \(\delta^{18}O\) fractionation and mixing processes in all water pools and fluxes along the soil-plant-atmosphere continuum (Risi et al., 2016) is represented following a similar formulation than in other isotope-enabled global land surface models (Aleinov and Schmidt, 2006; Haese et al., 2012). The isotopic compositions of precipitation and near-surface water vapour have to be prescribed monthly when running the model stand-alone or are simulated by the LMDZ general circulation model in coupled simulations. Precipitation reaching the soil surface or intercepting the canopy fractionates during evaporation according to the Craig and Gordon equation (Craig and Gordon, 1965), which generically describes the preferential evaporation of the lighter isotope of a free water body at steady state.

The resulting isotopic composition of soil water and mixing are parameterized as a vertical profile to overcome the limitation of depth resolution in the two-layer representation of soil in the model. No isotopic fractionation is assumed to occur during absorption of soil water by roots and thus the isotopic signature of xylem water is the same as that of soil water. The isotopic composition of leaf water at the evaporation sites \((\delta^{18}O_e)\) is diagnosed by inverting the Craig and Gordon (1965) equation:

\[
\delta^{18}O_e = \alpha \left( \alpha_k \times (1-h) \times \delta^{18}O_{sw} + h \times \delta^{18}O_v \right)
\]  

(4)
where $\delta^{18}$O$_{sw}$ is the isotopic composition of soil water taken up by the roots integrating older soil water and recent precipitation, $\delta^{18}$O$_{v}$ is the isotopic composition of atmospheric water vapour, $\alpha$ is the equilibrium fractionation due to the phase change from liquid water to vapour, $\alpha_k$ is the kinetic fractionation due to diffusion of vapour into unsaturated air, and $h$ is the relative humidity normalized to surface temperature.

Isotopic enrichment of leaf water in the mesophyll ($\delta^{18}$O$_{lw}$) results from mixing between isotopically enriched leaf water at the evaporative site and depleted xylem water ($\delta^{18}$O$_{xw}$) through the so-called Peclet effect:

$$\delta^{18}O_{lw} = \delta^{18}O_e \times f + \delta^{18}O_{xw} \times (1 - f)$$

(5)

where $f = (1 - e^{-P})/P$ is a coefficient that decreases as the Peclet effect increases, with $P = (E \times L)/(W \times D)$ as the Peclet parameter. $E$ is the transpiration rate per leaf area, $L$ is the effective diffusion length and $W$ is the leaf water content per leaf volume. In order to keep the model as simple as possible, $L$ was set to 8 mm and $W$ was assumed to be 103 kg m$^{-3}$ for all PFTs following Risi et al. (2016). Admittedly, constant $L$ is a major assumption and source of uncertainty for global models (Keel et al., 2016; Risi et al., 2016) since it is highly variable between species and also depends on climate conditions and leaf anatomy, morphology and age (Barnard et al., 2007; Roden et al., 2015). The value used for $L$ was obtained from an optimization of simulated diurnal isotopic cycles against observations at mid-latitude sites (Risi et al., 2016).

Half-hourly tree-ring cellulose isotopic composition ($\delta^{18}$O$_{cell}$) is calculated from the isotopic composition of leaf water ($\delta^{18}$O$_{lw}$) and xylem water ($\delta^{18}$O$_{xw}$) following the formulation of Anderson et al. (2002):

$$\delta^{18}O_{cell} = (f_0 \times \delta^{18}O_{xw} + (1 - f_0) \times \delta^{18}O_{lw}) \times (1 + \epsilon)$$

(6)

Where $f_0$ is the fraction of exchange with xylem water prior to cellulose synthesis, which reduces the imprint of leaf water on cellulose. For $\delta^{18}$O this exchange is estimated to be 0.42 based on the best fit relationship under controlled experiments (Roden et al., 2000). The parameter $\epsilon$ is the biochemical fractionation factor during cellulose formation associated with water carbonyl interactions and is estimated to be 27‰ (DeNiro and Epstein, 1979; Stenberg and DeNiro, 1983).

An estimate of growing season tree-ring isotopic composition ($\delta^{18}$O$_{R}$) is obtained by weighting $\delta^{18}$O$_{cell}$ by GPP as done for $\Delta^{13}$C$_{R}$ in Eq. (3):

$$\delta^{18}O_{R} = \frac{1}{\sum_{n=SOS}^{EOS} GPP(n)} \sum_{n=SOS}^{EOS} (\delta^{18}O_{cell}(n) \times GPP(n))$$

(7)

A model evaluation across a network of 10 sites in Europe and North America shows that this representation is able to reproduce the main features of the seasonal and vertical variations in soil water isotope content, as well as the seasonal isotopic signals in stem and leaf water (Risi et al., 2016). The isotopic variability simulated by ORCHIDEE has been used to interpret local climatic signals in tree-ring $\delta^{18}$O records (Shi et al., 2011; Churakova et al., 2016) and to investigate regional and global isotopic signatures of continental recycling (Risi et al., 2013).
Table 1. Location and characteristics of the six tree-ring sites used for model evaluation. The ORCHIDEE Plant Functional Types (PFTs) corresponding to the sites are Boreal Needleleaf Evergreen (BoNE), Boreal Broadleaf Summergreen (BoBS) and Temperate Broadleaf Summergreen (TeBS).

<table>
<thead>
<tr>
<th>Site</th>
<th>Kessi</th>
<th>Sivakkovaara</th>
<th>Bromarv</th>
<th>Rennes</th>
<th>Fontainebleau</th>
<th>Annecy</th>
</tr>
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<tbody>
<tr>
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<td>Finland</td>
<td>Finland</td>
<td>France</td>
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<td>ORCHIDEE PFT</td>
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<td>BoNE</td>
<td>BoBS</td>
<td>TeBS</td>
<td>TeBS</td>
<td>TeBS</td>
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<tr>
<td>Latitude</td>
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<td>62.5°</td>
<td>60.0°</td>
<td>48.1°</td>
<td>48.4°</td>
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<tr>
<td>Longitude</td>
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<td>31.2°</td>
<td>23.0°</td>
<td>-1.7°</td>
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<td>150</td>
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<td>120</td>
<td>70</td>
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<td>Stand density (trees ha⁻¹)</td>
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<td>-</td>
<td>-</td>
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<td>140</td>
<td>40</td>
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<td>No. trees for tree-ring width</td>
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<td>28</td>
<td>7</td>
<td>28</td>
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<td>13</td>
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<tr>
<td>No. trees for tree-ring isotopes</td>
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<td>4</td>
<td>4</td>
<td>4</td>
<td>4</td>
<td>9</td>
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<tr>
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<td>Sandy loam</td>
<td>Sandy loam</td>
<td>Loam</td>
<td>Calcareous loam</td>
<td>Clay loam</td>
</tr>
<tr>
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<td>&lt;0.5</td>
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<tr>
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2.2 Tree-ring data

Six previously published tree-ring sites in northern and western Europe with simultaneous measurements of ring-width and δ¹³C and δ¹⁸O compositions were used to evaluate the skill of the model along a climate gradient (Table 1). The three northernmost sites are located in the temperature-limited boreal region in Finland, and have chronologies of ring-width and δ¹³C and δ¹⁸O composition for Scotch pine (Kessi and Sivakkovaara; Hilasvuori et al., 2009) and Pedunculate oak (Bromarv; Hilasvuori and Berninger, 2010). The remaining three sites are located in France and represent moisture-sensitive temperate forests of Sessile oak (Fontainebleau; Etien et al., 2009) and Pedunculate oak (Rennes and Annecy; Raffalli-Delerce et al., 2004; Danis et al., 2006). In all sites, except Annecy, the available ring-width and δ¹³C and δ¹⁸O chronologies cover the common period 1960–2000.

The tree-ring width measurement series available for each site were standardized by dividing each series by its mean ring width (Cook et al., 1990). The resulting series of tree-ring width indices were averaged together to produce a mean site chronology composed by seven to twenty-eight trees (Table 1). This simple standardization method allows the computation of
average tree-ring chronologies without the average being dominated by the faster growing trees with wider rings. Depending on the site, 4 to 9 trees were selected to develop carbon ($\delta^{13}C_R$) and oxygen ($\delta^{18}O_R$) stable isotope chronologies by pooling rings from the selected trees (Table 1) and using standard methods for cellulose extraction and measurement of the isotopic ratios (McCarroll and Loader, 2004; Daux et al., 2018). For oaks, earlywood and latewood sections were separated but only latewood was processed. For pine, the carbon and oxygen isotopic compositions were measured for the whole ring.

Tree-ring carbon discrimination was computed by subtracting the stable carbon isotope composition of the atmosphere ($\delta^{13}C_a$) from the measurements using the expression of Farquhar et al. (1982):

$$\Delta^{13}C_R = \frac{\delta^{13}C_a - \delta^{13}C_R}{1 + \frac{\delta^{13}C_R}{1000}}$$  \hspace{1cm} (8)

Data for $\delta^{13}C_a$ were obtained from McCarroll and Loader (2004) for the period 1901–2000.

2.3 Simulations

The model was run at each tree-ring site over the period 1901–2000 using as meteorological forcing the nearest 0.5° grid of the 6-hourly CRU-NCEP dataset (Viovy, 2014). This gridded forcing dataset is a statistical merging of the monthly CRU TS station-based dataset of the Climate Research Unit (New et al., 2000) with the atmospheric reanalysis from the National Center for Environmental Prediction (NCEP). The corresponding soil type and vegetation PFT were prescribed for the sites (Table 1). Monthly $\delta^{18}O$ composition of precipitation ($\delta^{18}O_p$) and water vapour ($\delta^{18}O_v$) were obtained from the nearest grid of a global simulation of the isotope-enabled LMDz general circulation model nudged by an atmospheric reanalysis over the period 1890–2007 (Risi et al., 2010).

Biomass and soil carbon pools were initialized to steady state equilibrium by a 5000-year spinup obtained by cycling over the meteorology for the period 1901–1910. The model was then run over the period 1901–2000 using observed CO$_2$ and an initial tree density of 1000 trees per hectare to approach current forest age and density following tree mortality over time due to self-thinning.

In order to benchmark the triple tree-ring ability of ORCHIDEE, a simulation of the MAIDENiso tree-ring model for the Fontainebleau forest was obtained from an earlier study (Danis et al., 2012). The model simulates tree-ring $\delta^{13}C$ and $\delta^{18}O$ stable isotopes using the formulation of Lloyd and Farquhar (1994) and the Craig-Gordon model (Craig and Gordon, 1965), respectively. Ring width is parameterized as the annual stem growth increment based on daily carbon allocation to leaves, stem, roots and storage as a function of climate, soil water balance and atmospheric CO$_2$. Growth is decoupled from instantaneous photosynthesis by a labile carbon pool, which allows the model to reproduce the temporal autocorrelation in tree rings (Misson, 2004). The simulation was produced using a site-specific calibration and includes tree-ring width, $\delta^{13}C$ and $\delta^{18}O$ over the period 1953–2000 as described in Danis et al. (2012). The daily $\delta^{18}O_p$ and $\delta^{18}O_v$ forcings were obtained by using a linear regression based on daily mean air temperature and precipitation from two nearby stations as predictors, with coefficients obtained from the nearest isotopic observations in Saclay.

In addition, tree-ring $\delta^{18}O$ simulated with the LPX-Bern Dynamic Global Vegetation Model (Keel et al., 2016) was extracted for each site from a published global simulation available for the period 1960–2012 at 3.75°x2.75° (dataset available at: 

[dataset link]
www.climate.unibe.ch). This simulation was obtained by forcing LPX-Bern with monthly soil water $\delta^{18}$O ($\delta^{18}$O$_{sw}$), $\delta^{18}$O$_v$, and relative humidity data from a simulation with the coupled atmosphere-land surface model ECHAM5-JSBACH driven by observed sea surface temperature (Haese et al., 2013; Keel et al., 2016). LPX-Bern uses the Peclet modified Craig-Gordon model to calculate daily $\delta^{18}$O in leaf water together with the formulation of Roden-Lin-Ehleringer (Roden et al., 2000) to determine $\delta^{18}$O in tree-ring cellulose.

2.4 Model-data comparison

The ability of ORCHIDEE to simulate the interannual variability of the three tree-ring parameters over the course of the 20th century was first evaluated in the Fontainebleau forest (Table 1). Fontainebleau is a well-studied tree-ring site in France (Michelot et al., 2011, 2012; Daux et al., 2018) and it has been used to evaluate the MAIDENiso tree-ring model (Danis et al., 2012). We compared our simulation of ring-width, $\Delta^{13}$C and $\delta^{18}$O for this site with the simulation of MAIDENiso over the period 1953–2000. Then, the evaluation was conducted in the rest of the sites over the common period 1960–2000, except in Annecy where a shorter span of the observations limited the model-data comparison to the period 1971–2000.

A simulated tree-ring width chronology was derived for each site by dividing the simulated tree-ring width series of the largest model tree by its mean. Since growth allocation in the model increases almost linearly with stem size, the absolute annual ring-width vary among stem size-classes but its interannual variability remains similar across all size classes, thus the choice of size class does not affect the standardized variability. The standardization removes the effect of stem size-class and conserves the interannual and longer variability but does not remove the juvenile effect in tree-ring width. However, the juvenile trend in simulated and observed ring-width does not affect the evaluation period (1960-2000) because at this time trees were already mature canopy individuals with their radial growth fluctuating around the mean.

Simulated $\delta^{18}$O and $\Delta^{13}$C tree-ring chronologies were obtained by averaging the simulated half-hourly isotopic variability between May and August. Using just the summer season (Jun–August) improves results for $\Delta^{13}$C but degrades substantially results for $\delta^{18}$O, thus May was included as a compromise in order to use a common season for the isotopes and ensure comparability across sites. Late-May and early-June correspond to the seasonal peak in transpiration and photosynthesis of oak in Fontainebleau, which is closely followed by the transition between earlywood and latewood (Michelot et al., 2011). A mean $\delta^{18}$O series was created from the nearest LPX-Bern grid (3.75°x2.75°) and corresponding PFT to each evaluation site for a comparison with the observations and ORCHIDEE over the common period 1960–2000.

Since the focus of our evaluation is on the interannual variability and not on the absolute values, correlation and the normalized standard deviation (i.e., the standard deviation of simulated tree-ring parameters divided by the standard deviation of the observations) were used to quantitatively evaluate the skill of the models to simulate the variability in tree-ring width and stable isotopes. Differences in the temporal persistence (i.e., carryover effect) in the observed and simulated tree-ring parameters were evaluated using the first-order autocorrelation of the time series.

The integrated growth-isotope responses simulated by ORCHIDEE and MAIDENiso models in Fontainebleau were qualitatively compared with observations using a bivariate response surface between tree-ring width variability and the joint variability of the two isotopes. A smoothed response surface was fitted using a data-adaptive bivariate generalized additive model (GAM)
implemented with the *mgcv* package (Wood, 2017) in the R environment (R Core Team, 2020). This visualization device extends the dual isotope conceptual model of Scheidegger et al. (2000) to illustrate the mechanistic information content of the triple tree-ring constraint for models introduced in this study. It neatly reveals the complex association of tree growth with gas exchange inferred from stable isotopes in both observations and models.

To disentangle the relative importance of source water \((\delta^{18}O_{sw})\) and leaf water enrichment above source water \((\Delta^{18}O_{lw} = \delta^{18}O_{lw} - \delta^{18}O_{sw})\) between May and August in determining the variability of \(\delta^{18}O_R\) simulated by ORCHIDEE and LPX-Bern we used the Lindeman-Merenda-Gold (LMG) method (Grömping et al., 2006). This linear decomposition method allows to quantify the contribution of different correlated regressors (here \(\delta^{18}O_{sw}\) and \(\Delta^{18}O_{lw}\)) to the total \(r^2\) of a multiple linear regression model.

## 3 Results

### 3.1 A triple tree-ring constraint for ORCHIDEE and MAIDENiso in Fontainebleau

#### 3.1.1 Interannual and decadal tree-ring variability

ORCHIDEE shows a significant skill in simulating the interannual and multidecadal variability of oak tree-ring width \((r=0.59, p<0.01)\) and latewood \(\Delta^{13}C_R\) \((r=0.41, p<0.01)\) and \(\delta^{18}O_R\) \((r=0.49, p<0.01)\) over the 20th century in Fontainebleau (Fig.1a–c). The magnitude of the interannual variability of \(\delta^{18}O_R\) is well simulated (NSD=1.04) but that of tree-ring width is overestimated by 37\% (NSD=1.37), while that of \(\Delta^{13}C_R\) is underestimated by about a similar magnitude (NSD=0.55). \(\Delta^{13}C_R\) is systematically overestimated since 1980, when the observations show a decrease by about 1\‰ (Fig. 1b). Overall, the model simulates 35\% of the observed tree-ring width variability and 17–24\% of latewood isotopic variability over the 20th century.

The first-order autocorrelation or carryover in observed tree-ring width is significant \((r_{lag1}=0.54, p<0.001)\) and its magnitude indicates that ring width in the previous year explains up to 30\% of current year tree-ring width variability. In contrast, simulated tree-ring width has no first-order autocorrelation \((r_{lag1}=0.02, p>0.1)\) because of the direct coupling of growth with carbon source from photosynthesis in the model. As a result, in years with extreme summer drought conditions like in 1921 and 1976 the model does not simulate any stem growth because photosynthesis is strongly suppressed (Fig. 1a). The simulated growth recovery after these extremes occurs too fast compared with the observations. The first-order autocorrelation in the isotopic observations is significant only for \(\Delta^{13}C_R\) \((r_{lag1}=0.37, p<0.001)\) while in the simulations it is marginally significant for both \(\Delta^{13}C_R\) \((r_{lag1}=0.18, p<0.1)\) and \(\delta^{18}O_R\) \((r_{lag1}=0.27, p<0.01)\).

The skill of ORCHIDEE compares well with that of the MAIDENiso tree-ring model (Fig. 1a–c), specifically calibrated for the site over the period 1953–2000. Over this period, MAIDENiso is able to simulate between 30\% and 46\% of the total variability of the observations of tree-ring width and isotopes, which compares to the 20\% to 44\% of the total observed variance simulated by ORCHIDEE over the same period with standard parameterization. MAIDENiso is considerably better than ORCHIDEE at simulating tree-ring width \((r=0.68 \text{ vs } r=0.51)\) and \(\Delta^{13}C_R\) \((r=0.58 \text{ vs } r=0.45)\) variability, but despite simulating well the amplitude of \(\Delta^{13}C_R\) and \(\delta^{18}O_R\) (NSD=0.91–1.16) it substantially underestimates the amplitude of tree-
ring width (NSD=0.68). Unlike ORCHIDEE, it is able to simulate a significant first-order autocorrelation in tree-ring width ($r_{lag1}=-0.45, p<0.01$) with a magnitude similar to that of the observations ($r_{lag1}=0.50, p<0.01$). This carryover effect accounts for up to 25% of current year tree-ring width variability in the observations (1953–2000) and is thus an important component of the growth variability captured by the carbon remobilization dynamics of the model.

MAIDENiso is able to simulate the observed decrease in $\Delta^{13}C_R$ since 1980 better than ORCHIDEE (Fig. 1b). The amount and amplitude of $\delta^{18}O_R$ variability is slightly better simulated by ORCHIDEE ($r=0.66, p<0.001; \text{NSD}=1.04$) than by MAIDENiso ($r=0.54, p<0.001; \text{NSD}=0.91$; Fig. 1c). The partitioning of the $r^2$ of a multiple linear regression shows that source water ($\delta^{18}O_{sw}$) and leaf water enrichment above source water ($\Delta^{18}O_{lw}$) account for 56% and 37% of the total variability of $\delta^{18}O_R$ simulated by ORCHIDEE over the period 1953–2000, respectively. We could not quantify the contributions of $\delta^{18}O_{sw}$ and $\Delta^{18}O_{lw}$ in MAIDENiso because these simulated data were not available. The two different forcing series of $\delta^{18}O_p$ used to drive MAIDENiso and ORCHIDEE are not significantly correlated over the May-August period ($r=-0.07, p>0.1$). Nevertheless, $\delta^{18}O_R$ simulated by the two models is significantly correlated ($r=0.56, p<0.001$), suggesting a similarity of simulated $\Delta^{18}O_{lw}$ variability.

3.1.2 The growth-isotope tree-ring triplet

So far the evaluation statistics used above only describe the unidimensional skill of the models and do not evaluate their ability to simulate the joint relationships that exist among tree-ring width, $\Delta^{13}C_R$ and $\delta^{18}O_R$. The strength of the correlations between the actual tree-ring width and isotopic chronologies in Fontainebleau indicates that oak radial growth has 10% and 24% of common variance with latewood $\delta^{18}O_R$ and $\Delta^{13}C_R$, respectively (Fig. 1d). In turn, the isotopes have 16% of common variability. The interpretation of these three-way relationships (correlations) can be aided by visualizing the bivariate surface response of tree-ring width as a function of the dual latewood isotope variability (Fig. 1d). The resulting surface provides, at a glance, insights on causal and non-causal (indirect) relationships between environmental variability (temperature and drought stress) and stomatal responses and growth (see axes in Fig. 1d). The main geometry of the surface can be described by three regression slopes: $b1$: tree-ring width in relation to $\delta^{18}O_R$, $b2$: tree-ring width in relation to $\Delta^{13}C_R$ and $b3$: $\Delta^{13}C_R$ in relation to $\delta^{18}O_R$ (Fig. 1d). These slopes can be used to compare the surface of the observations with those simulated by models.

The bivariate surface response in Fontainebleau shows that in the observations, ring-width has a consistent positive and significant linear relationship with latewood $\Delta^{13}C_R$ ($b2=0.16, r=0.48, p<0.01$), whereas its relationship with $\delta^{18}O_R$ is highly non-linear and with an overall negative slope ($b1=-0.11, r=-0.31, p<0.05$; Fig. 1d). The scatter of the observation points across the surface depicts a negative and significant linear relationship between carbon and oxygen isotopic ratios ($b3=-0.45, r=-0.40, p<0.01$; Fig. 1d). The two models simulate qualitatively different growth-isotope surface responses and none is able to capture the observed non-linear relationship between tree-ring width and $\delta^{18}O_R$ (Fig. 1e–f). The surface simulated by ORCHIDEE is more consistent with the observations (Fig. 1e). It captures the sign and significance of the relationships between tree-ring width and $\delta^{18}O_R$ ($r=-0.54, p<0.001$) and $\Delta^{13}C_R$ ($r=0.87, p<0.001$), and also between the isotopic ratios ($r=-0.69, p<0.001$). However, the corresponding slopes $b1$ (-0.22) and $b2$ (0.71) are respectively two and four times higher than in the observations (Fig. 1e). The slope $b3$ (-0.35) is slightly smaller than observed (-0.45), but still the correlation between
\(\delta^{18}O_R\) and \(\Delta^{13}C_R\) is overestimated. Therefore, ORCHIDEE captures important features of the observed tree-ring triplet, but it substantially overestimates the coupling between growth and isotopic variability (29–50% of common variance) and between isotopes (48% of common variance).

The growth-isotope surface response of MAIDENiso is rather flat and considerably different from the surfaces derived from the observations and ORCHIDEE (Fig. 1f). It reveals a decoupling between growth and isotopic variability with slopes \(b_1 (-0.03)\) and \(b_2 (0.04)\) close to zero. Yet, the model simulates a strong coupling between isotopic ratios (\(b_3=-1.31\) and 62% of common variance, \(p<0.001\)), which is three times higher than in the observations and ORCHIDEE. The large slope \(b_3\) in MAIDENiso results from the overestimation of the simulated \(\Delta^{13}C_R\) variability (NSD=1.16) combined with underestimated \(\delta^{18}O_R\) variability (NSD=0.91). This demonstrates that the good performance of the model in simulating individual tree-ring variables (Fig. 1a–c) does not necessarily translate into a realistically simulated tree-ring triplet (Fig. 1f).

### 3.2 Model performance across sites

The performance of ORCHIDEE for tree-ring width, \(\Delta^{13}C_R\) and \(\delta^{18}O_R\) varies substantially across sites (Fig. 2), with no clear pattern along the climate gradient from Finland to France or between species for any parameter. However, it is clear that the isotopic variability is better simulated than tree-ring width and also that \(\delta^{18}O_R\) is the tree-ring variable better simulated. Tree-ring width is well simulated (25–30% of the observed variability) at only two out of six sites. In the remaining sites, the simulations account for less than 10% \((r<0.32)\) of the observed variability, falling mostly in the region of poor performance in Fig. 2.

Although ORCHIDEE is able to simulate about 10–64% \((r=0.31–0.80)\) of the observed \(\Delta^{13}C_R\) variability, it tends to underestimate its amplitude by 30–60%, particularly in the northernmost sites of pine (Kessi and Sivakkovaara) where the isotopic ratios were measured over the whole ring (Fig. 2). With the exception of the northernmost site, the amplitude of \(\delta^{18}O_R\) variability is simulated within \(\pm 20\%\) and the simulations account for 13–55% \((r=0.36–0.74)\) of the variance of the observations, with all the sites falling in the region of moderate to good performance in Fig. 2.

The \(\delta^{18}O_R\) simulations of the LPX-Bern global model are systematically better than the simulations of ORCHIDEE in terms of correlations and amplitude of the interannual variability (Fig. 2). In Fontainebleau LPX-Bern simulates 74% \((r=0.86)\) of the observed \(\delta^{18}O_R\) variability. In this site, ORCHIDEE and MAIDENiso are able to simulate only 40% \((r=0.63)\) and 34% \((r=0.58)\) of the observed variability, respectively. Three sites (Kessi, Sivakkovaara and Fontainebleau) exceed the range of performance of ORCHIDEE (blue shading in Fig. 2), mostly due to the good skill of the LPX-Bern simulation in terms of correlation with the observations.

In order to understand the origin of the differences between ORCHIDE and LPX-Bern, it is necessary to compare their isotopic drivers and the relative contributions of the isotopic composition of source water \(\left(\delta^{18}O_{sw}\right)\) and leaf water enrichment \(\left(\Delta^{18}O_{lw} = \delta^{18}O_{lw} - \delta^{18}O_{sw}\right)\) to simulated \(\delta^{18}O_R\) variability in each model. In contrast to LPX-Bern, ORCHIDEE simulates a much stronger contribution of \(\delta^{18}O_{sw}\) (46–85%) than \(\Delta^{18}O_{lw}\) (14–53%) to \(\delta^{18}O_R\) variability (Fig. 3a). The \(\delta^{18}O_R\) variability simulated by LPX-Bern is dominated by the \(\Delta^{18}O_{lw}\) (42–78%) isotopic signal (Fig. 3b). ORCHIDEE does not simulate any clear latitudinal pattern for the relative importance of \(\delta^{18}O_{sw}\) and \(\Delta^{18}O_{lw}\). In contrast, LPX-Bern simulates an increasing
importance of $\Delta^{18}O_{lw}$ toward the north, except at the coolest northernmost site where $\delta^{18}O_R$ is dominated by the signature of $\delta^{18}O_{sw}$ in the two models.

The isotopic signatures of precipitation ($\delta^{18}O_p$) and vapour ($\delta^{18}O_v$) from the LMDZ atmospheric model used to drive ORCHIDEE are poorly correlated with those produced by the ECHAM5 atmospheric model that underlay $\delta^{18}O_{sw}$ used to force LPX-Bern (Fig. 3c). In spite of this lack of agreement, the soil-integrated $\delta^{18}O_{sw}$ variability simulated by ORCHIDEE and JBACH (coupled with ECHAM5) land surface models are significantly correlated. The strength of the correlations increase for the resulting $\Delta^{18}O_{lw}$ and $\delta^{18}O_R$ variability simulated by ORCHIDEE and LPX-Bern (Fig. 3c). This pattern of correlations indicates that, in models, seasonal differences in the isotopic composition of precipitation are strongly buffered by water mixing in the soil profile, resulting in coherent isotopic variations in source water and thereby contributing to the correlation of the $\delta^{18}O_R$ signals simulated by the models. The significant resemblance of simulated $\Delta^{18}O_{lw}$ between the models points to similarities in the response of leaf evaporative enrichment and meteorological forcings (i.e., VPD). Taken together, the analysis of the isotopic forcings and contributions of source water and leaf enrichment suggests that the better performance of LPX-Bern derives from the higher contribution of leaf enrichment to simulated $\delta^{18}O_R$ variability.

ORCHIDEE overestimates the correlation between $\delta^{18}O_R$ and $\Delta^{13}C_R$ in the temperate sites in France, but it simulates very well the magnitude of the isotopic coupling observed in the boreal oak and pine sites in Finland (Fig. 4a). This means that the simulated stomatal control and responses to atmospheric humidity are overestimated in the temperate deciduous PFT, as is apparent in a stronger correlation between simulated isotopic ratios and VPD in these sites compared with the observations (Fig. 4b–c).

Measured latewood or whole-ring isotopic ratios have no significant first-order autocorrelation in the sites (Fig. 5b–c), with the exception of $\Delta^{13}C_R$ in Fontainebleau. However, ORCHIDEE simulates substantial autocorrelation in $\delta^{18}O_R$ variability in the three temperate sites in France and also in the northernmost boreal site in Finland (Fig. 5c), likely as a result of autocorrelation in the isotopic composition of source water. In contrast, simulated $\Delta^{13}C_R$ has significant autocorrelation only in Rennes, although it is nearly significant as well in Fontainebleau (Fig. 5b).

### 3.3 Simulated relationship between productivity and isotopic variability

Growing season (May-August) GPP is significantly correlated with the simulated isotopic variability across all sites (Fig. 6a). The relationship is more consistent with $\delta^{18}O_R$ ($r$=-0.47 to -0.73) than with $\Delta^{13}C_R$ ($r$=-0.40 to 0.85) along the climate gradient. The strength of the correlations between $\delta^{18}O_R$ and GPP ($r$=-0.47 to -0.73) appears to increase from the boreal to the temperate region. This empirical relationship is driven by a synergistic effect of source water and leaf water enrichment because both variables correlate negatively with GPP (Fig. 6b). Leaf water enrichment tends to correlate with GPP more strongly than source water, though in the northernmost pine site only source water is correlated with GPP. Simulated tree-ring width is highly correlated with simulated GPP because of its direct dependency on it (Fig. 6a).
4 Discussion

4.1 Uncertainties and critical processes for modelling tree-ring width and isotopic ratios in a global model

Our evaluation in Fontainebleau and other five sites across a boreal-to-temperate climate gradient in Europe showed that ORCHIDEE simulates better the interannual variability of tree-ring stable isotopes than ring-width (30-64% and <30% of the observed variability, respectively), with a general performance for the stable isotopes similar to MAIDENiso and slightly lower than LPX-Bern (Figs. 1 and 2). The lower skill for tree-ring width results primarily from the inability of ORCHIDEE to simulate the significant temporal autocorrelation observed in ring-width variability (Fig. 6a). Temporal carryover is characteristic of tree-ring width (Fritts, 1976; Cook, 1985) and varies considerably with species and location, accounting for 20–25% of current year ring-width variability (Breitenmoser et al., 2014). Several developmental and physiological processes involved in tree growth can produce carryover, including primarily remobilization of non-structural carbohydrates from previous years (Kagawa et al., 2006; Keel et al., 2006; Carbone et al., 2013), cambial dynamics (Vaganov et al., 2011), leaf lifespan (LaMarche Jr and Stockton, 1974; Monserud and Marshall, 2001) and environmental cycles or slowly varying crown and root dynamics that affect tree water and carbon balance across several years (Fritts, 1976; Rocha et al., 2006). The carryover of ring-width observations can be removed through statistical prewhitening (Cook, 1985). A data-model comparison using prewhitened observations results in slightly higher correlations with simulated ring-width variability in the three French sites (e.g., increase in $r$ from 0.50 to 0.56 in Fontainebleau) but not in the Finish sites (not shown), where autocorrelation was lower (Fig. 6a).

The ORCHIDEE version used in this study (r898) lacks a labile carbon pool and like most other global land surface models (Fatichi et al., 2014; Jones et al., 2020) is unable to simulate growth carryover. As a result, simulated growth depends directly on instantaneous photosynthesis and thereby it reflects only current year GPP variability (see Fig. 6a). This simplified representation of growth is currently the major limitation of the model to simulate tree-ring width variability (Figs. 1a and 2). Nevertheless, in Fontainebleau ORCHIDEE still simulates 26% of the observed interannual variability but overestimates its amplitude and the speed of recovery from drought extremes like 1976 (Fig. 1a). Legacy effects of reduced growth following drought events can persist for 1 to 4 years in drought-sensitive ecosystems (Anderegg et al., 2015; Cailleret et al., 2018). Such prolonged legacy effects are typically not simulated by global carbon cycle models that lack the representation of the significant dependency of interannual tree growth on carbon remobilization from storage in their carbon allocation schemes (Anderegg et al., 2015). Recent developments to improve the realism of growth variability in land surface models have added a module of labile carbon storage and its utilization to decouple growth from instantaneous photosynthesis (Naudts et al., 2015; Vuichard et al., 2019; Jeong et al., 2020; Jones et al., 2020). This allows reproducing growth carryover and realistically sustain growth from storage during periods of environmental stress that might suppress photosynthesis, such as severe or prolonged drought (Jones et al., 2020). The newest version of ORCHIDEE (r5698) includes a pool of labile carbon that should contribute to a more realistic simulation of tree-ring width variability and ecosystem recovery from climate extremes (Vuichard et al., 2019; Jeong et al., 2020).

MAIDENiso explicitly represents the autocorrelation in tree-ring width through its carbon storage pool and utilization scheme (Missen, 2004; Danis et al., 2012). However, the calibrated model overestimated the magnitude of the observed au-
tocorrelation, which led to muted interannual variability in simulated tree-ring width (NSD=0.68). Because of the simulated carryover, it was able to capture the enduring effect of the extreme drought of 1976 in Fontainebleau (Fig. 1a). In this extreme year, photosynthesis was strongly reduced and carbon expenditure to growth and respiration in the model was sustained by stored carbon at the cost of partially depleting the pool. The carbon pool then took several years to recover, mimicking the observed slow recovery of growth after the drought (Fig. 1a).

ORCHIDEE was able to simulate 30-64% of the observed $\Delta^{13}C_R$ variability along the climate gradient, but the amplitude of the interannual variations was underestimated by 30-60% (Fig. 2) and it failed to capture the decrease in $\Delta^{13}C_R$ since 1980 in Fontainebleau (Fig. 1b). An earlier study with ORCHIDEE found a similar underestimation of the interannual variability of $\Delta^{13}C_R$ for larch in northeastern Yakutia, where the model simulated 26% ($r = 0.51$) of the observed variability (Churakova et al., 2016). The low amplitude of the simulated variability can be related to missing post-photosynthetic fractionation and mixing processes in the simple representation used for $\Delta^{13}C_R$ (Eq. 2). However, the same formulation has been shown to reproduce the observations in earlier studies in Europe with the LPX-Bern and CLM4.5 global land surface models (Keller et al., 2017). The representation of water stress and processes that affect $c_i$ could also explain the lower performance of ORCHIDEE.

A simple parameter sensitivity test in Fontainebleau (not shown) indicated that the amplitude of $\Delta^{13}C_R$ in ORCHIDEE is very sensitive to soil depth and maximum photosynthetic capacity ($V_{c max}$). This suggests that $\Delta^{13}C_R$ simulated by Eq. 2 and the associated drought and stomatal responses can be better parameterized by using tree-ring data as an observational constraint to optimize model parameters. Nevertheless, besides an improved parameterization, using a more complete formulation for carbon discrimination (Lloyd and Farquhar, 1994) combined with a scheme of carbohydrate mixing of isotopic signatures from old stored carbon and new photosynthetic carbon (Hemming et al., 2001; Danis et al., 2012) should contribute to improve the simulation of $\Delta^{13}C_R$ and stomatal responses in the latest version of ORCHIDEE (Jeong et al., 2020).

Modelling the fractionation processes of $\delta^{18}O$ along the soil-plant-atmosphere continuum is complicated by interactions between environmental factors and physiological responses (Gessler et al., 2009; Werner et al., 2012; Gessler et al., 2014). As a result, $\delta^{18}O_R$ is arguably one the tree-ring variables most difficult to interpret (Roden and Siegwolf, 2012; Barbour and Song, 2014) and to simulate in a global model. Our results show that despite this complexity and uncertainties, global models like ORCHIDEE and LPX-Bern can simulate the amplitude of $\delta^{18}O_R$ within $\pm 20\%$ and account for up to 74% of the observed interannual variability (Fig. 2). Disentangling the effect of isotopic signatures from source water and leaf evaporative enrichment revealed that the better performance of LPX-Bern to simulate $\delta^{18}O$ variability was due to its higher sensitivity to leaf evaporative enrichment compared with ORCHIDEE (Fig. 3a), which is predominantly sensitive to source water $\delta^{18}O$ (Fig. 3b). This implies that the observations support a dominant control of leaf evaporative enrichment on $\delta^{18}O_R$ in our study sites. A similar result was found with MAIDENiso for species in Canada and Patagonia (Lavergne et al., 2017). We could not verify if this is also the case in the MAIDENiso simulation used for Fontainebleau (Danis et al., 2012) because simulated $\delta^{18}O_{sw}$ and $\delta^{18}O_{bw}$ were not available. A previous tree-ring study using ORCHIDEE with the same parameterization in the Tibetan Plateau found that $\delta^{18}O_{bw}$ accounted for 66% of the variability of simulated $\delta^{18}O_R$ (Shi et al., 2011), which although dominant still shows the considerable sensitivity of the model to $\delta^{18}O_{sw}$ (i.e., 34% of the variance).
Given the support for a larger relative importance of $\delta^{18}O$ evaporative enrichment of leaf water with transpiration in LPX-Bern and MAIDENiso, uncertainties in the parameterization of leaf physiology and mixing of source (xylem) and leaf water will have a large impact on the overall skill of the models when compared with the observations. LPX-Bern and ORCHIDEE have a similar representation of the Peclet effect (Eq. 5) and isotopic mixing during cellulose production (Eq. 6; Keel et al., 2016), which is reflected in the significant correlation of simulated $\Delta^{18}O_{lw}$ (Fig. 3c). The main difference in the parameterization of the Peclet effect is for the path length $L$. LPX-Bern used a value of 3 mm for all PFTs (Keel et al., 2016), while we used a value of 8 mm obtained from tuning against seasonal observations in a few mid-latitude sites (Risi et al., 2016). Eq. 5 shows that the almost three times higher $L$ in ORCHIDEE should result in a larger Peclet effect, which increases (decreases) the contribution of xylem water (evaporative enrichment) to the $\delta^{18}O$ signature of leaf water. In addition, we assumed the common value 0.42 for the parameter $f_0$ (fraction of exchange with xylem water prior to cellulose synthesis) in Eq. 6, while a value of 0.4 was used in LPX-Bern (Keel et al., 2016). These parameter differences enhanced the imprint of the isotopic signature of xylem water in $\delta^{18}O_R$ simulated by ORCHIDEE. Future studies should evaluate model sensitivity to these parameters and constrain them with tree-ring observations.

The seasonal and interannual variability in the $\delta^{18}O$ composition of precipitation and air vapour at tree-ring sites is a source of uncertainty for modelling tree-ring $\delta^{18}O$ (Evans, 2007; Danis et al., 2012; Lavergne et al., 2017; Keel et al., 2016). However, the dampening effect of soil water mixing reduces considerably the impact of the seasonal variability in $\delta^{18}O$ of precipitation on the more integrated $\delta^{18}O_{sw}$ signal (Danis et al., 2012). Our results showed that even when precipitation $\delta^{18}O$ from two atmospheric models does not correlate, the resulting $\delta^{18}O_{sw}$ variability might be consistent and significantly correlated (Fig. 3c). The current parameterization of the Peclet effect ($L$) and exchange with xylem water ($f_0$) in ORCHIDEE make it more sensitive to uncertainties in precipitation $\delta^{18}O$ forcing data. A dedicated model intercomparison study for tree-ring $\delta^{18}O$ using the same meteorological and isotopic forcing will help to evaluate uncertainties and attribute differences to forcing data, parameters and model structure.

### 4.2 Constraining model processes with the growth-isotope tree-ring triplet

The enhanced information content obtained by combining multiple and complementary tree-ring variables has long been recognized in multi-proxy dendroclimatology (McCarroll et al., 2003; Schollaen et al., 2013; Loader et al., 2015) and dendroecology (Guerrieri et al., 2009; Savard, 2010; Shestakova and Martínez-Sancho, 2020) but its potential remained largely untapped in ecological modelling. The novel simulation of the growth-isotope tree-ring triplet in a global land surface model (Fig. 1e) enables using known mechanistic relationships between isotopes (Scheidegger et al., 2000) and between growth and carbon isotopes in the same ring (Francey and Farquhar, 1982; Cernusak and English, 2015; Shestakova et al., 2017) to benchmark the physiological responses of the model. This brings a new perspective on data-model comparisons beyond the traditional use of the interannual variability or trends (Panek and Waring, 1997; Danis et al., 2012; Bodin et al., 2013; Churakova et al., 2016; Keel et al., 2016; Keller et al., 2017; Ulrich et al., 2019).

The relationship between $\Delta^{13}C_R$ (or $\delta^{13}C_R$) and $\delta^{18}O_R$ is the basis of the well-known dual isotope conceptual model (Saurer et al., 1997; Scheidegger et al., 2000), which is widely used as a physiological constraint of leaf-level plant responses.
to environmental variability (Barnard et al., 2012). $\delta^{18}O_R$ variation is interpreted as a proxy for stomatal conductance ($gs$), assuming that it reflects only changes in leaf water enrichment caused by variation in air relative humidity, whereas changes in $\Delta^{13}C_R$ are interpreted as an integrated measure of photosynthesis ($A$) relative to stomatal conductance, that is the intrinsic water use efficiency (iWUE). A negative relationship between $\delta^{18}O_R$ and $\Delta^{13}C_R$, as seen across the diagonal of the tree-ring triplet in Fontainebleau (slope $b3$ in Fig. 1d), would indicate that plants have a strong stomatal control of gas exchange and stomatal conductance (rather than photosynthetic rate) drives variations in $\Delta^{13}C_R$ and iWUE.

Depending on regional climate, the slope between tree-ring width and $\delta^{18}O_R$ ($b1$ in Fig. 1d) can capture the seasonally integrated response of trees to air temperature and environmental moisture (Rebetez et al., 2003; Liu et al., 2017). However, the shape and nature of the relationship alone might be difficult to interpret without separating the effects of oxygen isotopic fractionation in leaves and source water variability on $\delta^{18}O_R$ (Barnard et al., 2012; Roden and Siegwolf, 2012; Sargeant et al., 2019). But when ring-width variations are simultaneously negatively related to $\delta^{18}O_R$ and positively to $\Delta^{13}C_R$ variations, as observed in Fontainebleau (Fig. 1d), it can be established with confidence that tree growth is modulated by leaf physiology through the stomatal limitation of $CO_2$ supply to photosynthesis as a response to air and soil humidity constraints (see axes in Fig. 1d).

The slope between tree-ring width and $\Delta^{13}C_R$ ($b2$ in Fig. 1d) provides a robust indication of the main climatic and carbon assimilation drivers (i.e., supply of $CO_2$ by stomatal conductance or demand of $CO_2$ by photosynthesis) associated with wood biomass growth variability (Voelker et al., 2014; Shestakova et al., 2017, 2019). In Mediterranean and temperate climates with moisture-limited tree growth, the slope or correlation between ring width and $\Delta^{13}C_R$ is positive (Shestakova et al., 2019), as seen in Fontainebleau (Fig. 1d). This means that tree growth and leaf physiology are both similarly driven by soil moisture constraints through a limitation of $CO_2$ supply to photosynthesis due to reduced stomatal conductance to avoid dehydration. In the boreal region north of the Arctic circle, where tree growth and function are controlled by low temperatures and radiation, the slope and correlation between ring width and $\Delta^{13}C_R$ turn negative (Shestakova et al., 2019). Under these conditions, the main control of $\Delta^{13}C_R$ is assimilation rate and therefore lower $\Delta^{13}C_R$ is associated with increased photosynthesis and growth.

The growth-$\Delta^{13}C_R$ coupling will be stronger when tree-growth variability is driven by concurrent climate and photosynthetic rates. In contrast, it will be weaker when growth relies more on stored carbohydrates and other processes that contribute to growth carryover and isotopic mixing.

The growth-isotope relationships can change over time with increased drought and warming (Shestakova et al., 2017, 2019) and are clearer during climate extremes. For instance, in a temperate location such as Fontainebleau it is expected that dry summer conditions would associate with narrow tree rings, decreased $\Delta^{13}C_R$ and increased oxygen isotope enrichment in leaf water (thus higher $\delta^{18}O_R$) because trees would close their stomata to reduce stomatal conductance and avoid dehydration at the expense of photosynthesis. Precipitation and soil water $\delta^{18}O$ would also be enriched because of higher temperatures, further increasing $\delta^{18}O_R$. Consistent with this expectation, our bivariate response surface shows that years with extremely narrow rings like 1976, 1990 and 1996 are associated with low $\Delta^{13}C_R$ and high $\delta^{18}O_R$ in latewood (Fig. 1d). The opposite occurs during moist years with wider rings, when conditions for stomatal aperture are optimal. Depending on the climatic region, the paleo-
temperature signals carried by δ^{18}O_R could be used to disentangle changes in the climatic forcing of past growth anomalies and physiological responses inferred from the growth-isotope triplet under pre-industrial and current climate conditions.

The growth-isotope triplet of the observations can be directly compared with the simulated triplet to mechanistically constrain the realism of model responses. The geometry of the tree-ring triplet simulated by ORCHIDEE r898 (Fig. 1e) demonstrates that the model is able to simulate more realistic physiological responses to environmental variability than MAIDENiso in Fontainebleau (Fig. 1f). However, the simulated growth–Δ^{13}C_R and Δ^{13}C_R–δ^{18}O_R relationships in ORCHIDEE are much stronger than in the observations. Removing the δ^{18}O_{sw} effect from simulated δ^{18}O_R to highlight the effect of leaf water enrichment in Fontainebleau further increased the strength of the coupling between δ^{18}O_R and Δ^{13}C_R (not shown). The correlation between stable isotopes and their correlations with VPD are also substantially overestimated in the other temperate sites (Rennes and Annecy; Fig. 4a–b). These model-data mismatches indicate that the model overestimates drought stress and the limitation of photosynthetic carbon assimilation by stomatal control in the temperate region, where stomatal regulation strongly drives variability in plant water use efficiency (Frank et al., 2015; Shestakova et al., 2019).

The implication of such a strong stomatal constraint for land-atmosphere interactions in ORCHIDEE r898 is an overestimation of energy partitioning towards sensible heat and an underestimation of transpiration and carbon uptake per unit of leaf area in the temperate region. In the boreal region (Kessi, Sivakkovvara and Bromarv), where stomatal control is not the main driver of Δ^{13}C_R (Shestakova et al., 2019), ORCHIDEE simulated a level of correlation between stable isotopes (Fig. 4b) and sensitivity to VPD (Fig. 4c) in good agreement with the observations, indicating a better gas-exchange parameterization for the boreal Broadleaf Summergreen and Needleleaf Evergreen PFTs (Table 1). The parameterization of the Temperate Broadleaf Summergreen PFT of the model could be improved by assimilating tree-ring data together with other ecosystem observations (e.g., eddy covariance, forest inventories, earth observations) using a data assimilation technique (Peylin et al., 2016; Thum et al., 2017).

The poor realism of the growth-isotope triplet simulated by MAIDENiso (Fig. 1f) is related to the low amplitude of simulated ring-width variability (NSD=0.68) due to excessive carryover from carbon remobilization, which decouples growth from current photosynthesis and leads to small growth-isotope slopes (b1 and b2). Although MAIDENiso was calibrated against the tree-ring observations in Fontainebleau (Danis et al., 2006), it still simulates a stomatal control even stronger than in ORCHIDEE, as indicated by a higher correlation between δ^{18}O_R and Δ^{13}C_R (r=0.79, p<0.001). These issues demonstrate that the statistical calibration of growth and physiological processes separately does not necessarily lead to an improved realism of simulated tree responses to environmental variability. An integrative constraint such as the tree-ring triplet presented here provides a way forward to improve the representation and parameterization of the biology of tree growth and function in models. If only one tree-ring variable is simulated it is easier to tune a model to fit the data. But if the growth-isotope triplet is to be fit, the constraint is stronger and mechanistically informed.

### 4.3 Simulated relationship between isotopic variability and productivity

Our results showed that the simulated interannual variability in δ^{18}O_R was significantly and negatively correlated with GPP across all sites in the climate gradient (r = -0.47 to -0.73, p < 0.01) because both source water (δ^{18}O_{sw}) and leaf water
enrichment ($\Delta^{18}O_{lw}$) related negatively with GPP (Fig. 6). Although $\Delta^{18}O_{lw}$ dominates the correlation in most sites, it is the synergistic effect of $\delta^{18}O_{sw}$ variations that contributes to the apparent spatial consistency of the $\delta^{18}O_{R}$–GPP correlation. The negative sign of the correlations of GPP with both components of $\delta^{18}O_{R}$ points to temperature as their underlying cause. On the one hand, higher temperatures during the growing season result in enriched $\delta^{18}O$ in precipitation and further enrich $\delta^{18}O_{sw}$ through evaporation. On the other hand, higher temperatures also lead to increased VPD, which increases leaf water enrichment and reduces GPP because of stomatal closure (Fig. 1d).

An earlier study attributed the correlation between $\delta^{18}O_{R}$ variability and satellite-based estimates of Net Primary Productivity (NPP) at large spatial scales to the common but opposite effect of VPD on leaf water enrichment and NPP, without considering the possible effect of source water (Levesque et al., 2019). Our finding suggests that $\delta^{18}O_{R}$–productivity correlations should be interpreted with caution because they are not entirely driven by leaf physiology, and source water is often an important driver of $\delta^{18}O_{R}$ (Fig. 3a–b).

The simulated interannual variability in $\Delta^{13}C_{R}$ also correlated with GPP in most sites, but the relationship was less spatially consistent since its significance and sign varied across the boreal-to-temperate climate gradient (Fig. 6a). A positive correlation between simulated $\Delta^{13}C_{R}$ and GPP in all temperate and boreal oak sites ($r = 0.45$ to $0.85$, $p < 0.01$) is coherent with a stomatal limitation of carbon assimilation (Shestakova et al., 2019). In the two boreal pine sites, correlations were weaker and only the northernmost site had a significant negative correlation ($r = -0.40$, $p < 0.01$). In such cool and moist environment, internal leaf CO$_2$ concentration and water use efficiency are controlled by photosynthetic rate, which is limited by temperature and sunshine (McCarroll and Loader, 2004; Hilaire et al., 2009).

This contrast in $\Delta^{13}C_{R}$–GPP correlations between the temperate and boreal region mirrors a shift from a positive to a negative relationship between $\Delta^{13}C_{R}$ and tree-ring width due to a change from water-limited to temperature-limited leaf physiology (Shestakova et al., 2019). These model-based isotope-GPP relationships are consistent with recent findings showing that tree-ring $\delta^{18}O$ correlates with satellite-based NPP over large spatial scales, whereas $\Delta^{13}C$ has a more spatially variable correlation with GPP (Belmecheri et al., 2014; Levesque et al., 2019; Tei et al., 2019) and ring width (Shestakova et al., 2017, 2019).

5 Conclusion

We demonstrated the potential of a tree-ring triplet based on tree-ring width and $\Delta^{13}C$ and $\delta^{18}O$ stable isotopes to constrain the representation of tree growth and physiology in the global land surface model ORCHIDEE (r898), bridging the long-standing gap between the tree-ring and land surface modelling communities. The comparisons with tree-ring data and the MAIDENiso and LPX-Bern models showed that the parameterization of leaf-level physiological responses (stomatal control) of ORCHIDEE can be mechanistically constrained using the simulated tree-ring isotopic variability but the representation of tree growth requires improvement. The lack of carbon remobilization from storage in the model is currently a major limitation for a realistic simulation of the interannual coupling between tree physiology and growth and the enduring legacy effects of
climate extremes on ecosystem dynamics. This calls for an updated representation of the biology of tree growth beyond the simple carbon-source approach, considering the effects of carbon storage and controls from wood tissue formation.

The use of the growth-isotope tree-ring triplet showed that good performance of a model in simulating individual tree-ring variables does not necessarily translate into realistically simulated tree responses to environmental variability. Because the tree-ring triplet integrates the response of the soil-plant-atmosphere system to environmental variability it is a powerful mechanistic constraint for tree growth and physiology in the context of modelling forest-atmosphere interactions. Consistent with recent observational studies, interannual variations in simulated forest productivity (GPP) correlated significantly with simulated variations in tree-ring $\Delta^{13}C$ and $\delta^{18}O$ stable isotopes. However, correlations between tree-ring $\delta^{18}O$ and productivity are not entirely driven by leaf physiology and should be interpreted with caution because of the significant and often large contribution of source water $\delta^{18}O$ to the relationship. These results establish the foundations for improving the simulation of tree rings in ORCHIDEE (Jeong et al., 2020) and a forthcoming optimization of model parameters using tree-ring data together with other short-term ecosystem observations (e.g., remote sensing, eddy-covariance, forest inventories) in a formal data assimilation technique (Peylin et al., 2016). Such advances should contribute to reduce current uncertainties in historical and future changes in forest carbon and water cycling.

Data availability. All the tree-ring data and ORCHIDEE tree-ring simulations used in this study are available at https://github.com/jBarichivich/barichivich2020_biogeosciences

Code and data availability. The model code (SVN r898) is accessible in the ORCHIDEE webpage https://forge.ipsl.jussieu.fr/orchidee/wiki/SourceCode
The code for producing the bivariate surface from the tree-ring triplet is available at https://github.com/jBarichivich/barichivich2020_biogeosciences

Author contributions. JB, PP, TL and VD designed the research. TL conducted the simulations with support of CR. JJ and SL contributed to model development and research design. JB revised the model, analyzed the data and wrote the manuscript. All the authors contributed to data interpretation and commented on the manuscript.

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References


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Figure 1. Comparison of simulated and observed tree-ring width and isotopic variability in Fontainebleau and the triple tree-ring constraint to assess the integrated model responses. **a-c** Comparison of tree-ring width and latewood $\Delta^{13}C_R$ and $\delta^{18}O_R$ variability simulated by ORCHIDEE (red) and MAIDENiso (gray) with observations (black). The normalised standard deviation (NSD) and Pearson correlation ($r$) are indicated in each case. The mean of the simulations was set to that of the observations for each parameter. **d-f** Bivariate response surface of tree-ring width as a function of $\delta^{18}O_R$ and $\Delta^{13}C_R$ variability based on observations and on ORCHIDEE and MAIDENiso simulations over the common period 1953–2000. The individual years are indicated by the black dots and their vertical distance to the surface is represented by the lines. The most extreme years with low growth and high moisture stress are labelled in each panel. The regression slopes between the tree-ring variables are indicated along the edges of each surface: tree-ring width vs $\delta^{18}O_R$ ($b_1$), tree-ring width vs $\Delta^{13}C_R$ ($b_2$) and $\Delta^{13}C_R$ vs $\delta^{18}O_R$ ($b_3$) as predictand vs predictor order. In each case, the linear correlation is indicated in brackets. The asterisks denote the significance levels of the slopes and correlations: *: $p<0.1$, **: $p<0.05$ and ***: $p<0.001$. In panel **d**, the relationship between stomatal aperture and moisture stress is indicated along the isotopic axes together with the expected changes in stomatal conductance ($g_s$) and relative humidity ($rH$) according to the dual isotope model (Scheidegger et al., 2000). The expected enrichment of source water $\delta^{18}O$ with increasing air temperature ($T_{air}$) is also indicated.
Figure 2. Taylor diagram showing the correlation (angular coordinate) and normalized standard deviation (NSD; radial coordinate) of the simulated tree-ring parameters (ORCHIDEE, MAIDENiso and LPX-Bern) with respect to the observations for the six sites used in this study (see Table 1). Tree-ring width is denoted by square symbols and ∆^{13}C_R and δ^{18}O_R by orange and blue circles, respectively. The models are denoted by solid symbols (ORCHIDEE), open symbols (MAIDENiso in Fontainebleau or site 5) and blue crosses (LPX-Bern). The statistics were computed over the common period 1960–2000, except in Annecy (site 6) where data availability limited the comparison to the period 1971–2000. The target point (NSD and correlation equal to 1) is represented by a circle. The gray, blue and orange shading denotes the range of the performance statistics covered by ORCHIDEE for tree-ring width, ∆^{13}C_R and δ^{18}O_R, respectively. Four qualitative areas of performance in terms of the magnitude of correlations or simulated variance are indicated as a visual aid.
Figure 3. Drivers of simulated $\delta^{18}$O$_R$ variability and consistency between isotopic forcings and simulations of ORCHIDEE and LPX-Bern across the climate gradient from boreal Finland (left) to temperate France (right). a) Simulated contributions of source water ($\delta^{18}$O$_{sw}$; turquoise) and leaf water enrichment ($\Delta^{18}$O$_{lw}$; green) signals to $\delta^{18}$O$_R$ variability during 1960–2000. The percentage of explained variance ($r^2$) is indicated in each bar. b) Correlation between the isotopic composition of precipitation ($\delta^{18}$O$_p$; light gray) and air vapour ($\delta^{18}$O$_v$; dark gray) used to force the models and the resulting $\delta^{18}$O$_{sw}$ (turquoise), $\Delta^{18}$O$_{lw}$ (green) and $\delta^{18}$O$_R$ (dark blue) simulated by ORCHIDEE and LPX-Bern during 1960–2000. All variables were averaged over the period May–August. Significance at the 95% confidence level is indicated by the black dots.
Figure 4. Observed and simulated isotopic coupling and response to VPD across the climate gradient during 1960–2000. a Correlation between δ¹⁸O_R and Δ¹³C_R in simulations (gray) and observations (black). b–c Correlations between growing season VPD and simulated (gray) and observed (black) δ¹⁸O_R and Δ¹³C_R variability, respectively. For Annecy the period of analysis is 1971–2000. Significance at the 95% confidence level is indicated by the black dots.
Figure 5. First-order autocorrelation in observed (black) and simulated (gray) tree-ring variables over the period 1960–2000. **a** Tree-ring width. **b** $\Delta^{13}C_R$. **c** $\delta^{18}O_R$. For Annecy the period of analysis is 1971–2000. Significance at the 95% confidence level is indicated by the black dots.
Figure 6. Correlations between the simulated tree-ring variables at each site and simulated May-August Gross Primary Productivity (GPP) over the evaluation period 1960–2000. 

a Correlations of $\delta^{18}$O_R (dark blue), $\Delta^{13}$C_R (light red) and tree-ring width (gray) with GPP. 

b Correlations of soil and leaf water $\delta^{18}$O components of $\delta^{18}$O_R with GPP. For Annecy the period of analysis is 1971–2000. Significance at the 95% confidence level is indicated by the black dots.