

# Lagrangian-Eulerian statistics of mesoscale ocean chlorophyll from Bio-Argo floats and satellites

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## Author Comments in response to Referee #2

This manuscript presents extensive work evaluating Eulerian and Lagrangian time and length scales of velocity and chlorophyll, as well as discussion about how they correlate. The proper interpretation of drifting phytoplankton observed in a Eulerian fashion is a longstanding paradigm in ocean ecology. However, estimates of Lagrangian phytoplankton statistics and comparisons with Eulerian counterparts are rare. This study represents a significant contribution towards best understanding how to interpret phytoplankton/chlorophyll measured in both Eulerian and Lagrangian platforms. The authors are very thorough in their analysis and description of the results. Nonetheless, I have a few comments to be addressed prior to recommending publication.

[Thank you for your close read and evaluation of our manuscript.](#)

Major comment: There are several data limitations that guide methodological decisions in an analysis of this type (e.g., the broad spatial averaging, chlorophyll averaging in the MLD). While some of the issues arising from these are mentioned briefly throughout the text, I would prefer to see a dedicated discussion section with the limitations and caveats.

[The averaging of scales \(or compositing of ACFs\) over \[5° x 5°\] space bins is meant to enhance the quality of the estimates by averaging over a region that is relatively spatially homogenous. Other authors doing a similar analysis of velocity in this region used \[10° x 10°\] space bins and found this adequate to describe spatial variability in Lagrangian scales \(Lumpkin et al., 2002\). We chose to use the same \[5° x 5°\] space bins as Glover et al. \(2018\), who calculated variograms of satellite ocean color in each bin much like we compute ACFs and found these bins good to resolve spatial variability. We will better motivate this in the text.](#)

[As for the depth reduction of chlorophyll, we had indeed used a simple average over the mixed layer since other authors had done this and demonstrated good agreement with satellite ocean color when describing seasonal variability in the region \(Yang et al., 2020\). At the suggestion of Referee #1, we computed an alternate depth-reduced chlorophyll series from the floats that is](#)

42 meant to better approximate what the satellites see. Please refer to our Author Comment to  
43 Referee #1 for full details, but briefly, we utilize the fact that 90% of the satellite-measured  
44 chlorophyll signal in the open ocean comes from a depth of  $1/Kd_{490}$ , and it is exponentially-  
45 weighted (Gordon and McCluney, 1975). We estimate  $Kd_{490}$  from the floats following Morel et  
46 al. (2007) (their equation 8),

$$47 \quad Kd_{490} = 0.0166 + 0.0773[\text{Chl}]^{0.6715}$$

48 where we take  $[\text{Chl}]$  as the mixed-layer average chlorophyll, and then take a weighted vertical  
49 average at each time step as

$$50 \quad \text{Chl}_{\text{float}}(t) = \frac{\sum_{z=1/Kd_{490}}^{z=\text{surface}} \text{Chl}(z,t) \exp(-2Kd_{490}(t)z)}{\sum_{z=1/Kd_{490}}^{z=\text{surface}} \exp(-2Kd_{490}(t)z)} .$$

51 The series is then log transformed and filtered as before. After rerunning all scales (please refer  
52 to set of figures in Author Comment to Referee #1), the results are not appreciably different. We  
53 will include a description of this comparison in the text.

54 As for the choice of ACF parameters in Table 1, please refer to our response to your comment  
55 below.

56 We plan to consolidate all of the above matters (spatial averaging, depth averaging, ACF  
57 parameters) into a subsection of the Discussions, as you suggest.

58 Specific comments:

59 I find that, while technically correct, talking about Lagrangian-Eulerian “statistics” in the title  
60 and throughout the text can be misleading. Why not refer to the specific statistics that are  
61 included in the analysis? i.e., Lagrangian-Eulerian time and length scales.

62 We felt that use of the word “statistics” made for a more compact title, with the meaning  
63 becoming clear after reading the abstract. But we do not object to changing the title to:  
64 “Lagrangian-Eulerian time and length scales of mesoscale ocean chlorophyll from Bio-Argo  
65 floats and satellites”.

66 The notation of upper case L for both Lagrangian and length-scale can be a bit confusing. I  
67 suggest using upper and lower case or a different notation to improve readability.

68 We agree about the confusion. We thought about using upper and lower case letters but this can  
69 become problematic since a lower case “l” can look like a number 1 or capital “I” or something  
70 else. We propose to maintain “T” and “L” for scales and replace subscripts “L” and “E” with  
71 either “l” and “e” or “LAG” and “EUL” for Lagrangian and Eulerian, respectively, depending on  
72 which of the two looks best.

73 Equation 5. Terminology becomes confusing here too when calling the nominators Lagrangian,  
74 Eulerian and Spatial (chlorophyll) scales. Is there a different name that could be more  
75 appropriate and less confusing? This is essentially a change in chlorophyll, correct?

76 These are effectively standard deviations of chlorophyll computed in different frames: from  
77 Lagrangian time series (subscript “LAG” or “l”) from Eulerian time series (subscript “EUL” or

78 “e”), or from spatial maps (subscript “spatial”). Though less than satisfactory, we cannot think of  
79 a better notation to express this point. However, we could add to the text the literal definition of  
80 each term as supplied here in our Author’s Comment document.

81 Table 1 is also confusing. Why are ACF bins different? Why are time windows for Eulerian and  
82 Lagrangian different? Does that have any effect on the comparison? (I think it would if you were  
83 calculating other statistics). Where does the 27.8km ACF bin for Eulerian length scale come  
84 from? I probably missed it.

85 As indicated in your Major Comment above, we plan to better motivate these choices and  
86 consolidate them into a subsection of Discussions that will cover all methodological choices.  
87 Briefly, we address your specific questions here.

88 Regarding temporal ACF bin sizes: Ideally, one would use a bin size that matches the sampling  
89 interval of the time series because this is the smallest lag that can be resolved. For this reason,  
90 the ACFs based on satellite altimetry, satellite ocean color, or drifters use a bin size of 1 day. The  
91 floats have a variable profiling interval. While they sometimes profile with a frequency of about  
92 1 per day, they generally profile less frequently and we found a bin size of 5 days to be a  
93 reasonable choice (with smaller bin sizes, many segments would offer no pairs). As we state, the  
94 two metbio\* float segments are given special attention because they profile more frequently, and  
95 for that reason we were able to use a finer bin size of 1 day. As a general statement, choosing a  
96 larger bin size for the ACF causes structure (curvature) of the ACF to be poorly resolved at short  
97 lag and biases time scales large. This point is brought up in section 4.2.

98 Regarding temporal segment lengths for ACF analysis: The Lagrangian segments should be kept  
99 as short as possible because as a platform moves it may encounter different environmental  
100 (physical or otherwise) conditions, and we found 120 days was a reasonable length of time. For  
101 Eulerian segments, this is not an issue, and, since seasonal variability is removed, length of the  
102 segment is generally unimportant. Given that, we used 365-366 day segments for chlorophyll out  
103 of convenience since the data were stored as yearly files.

104 Regarding spatial ACF bin size: Related to our point about temporal ACF bin sizes, it would be  
105 best to use a bin size equal to the data spacing. We chose 27.8 km as that approximately  
106 corresponds to the 0.25° resolution of the data in the latitudinal direction. Obviously, pairs  
107 spaced zonally may have a separation less than that distance and would fall into the first bin.

108 Figure 1d. orange profiles: QPI<5km; blue: all others (i.e., not total)

109 You are correct. The total height of the bars represents the total number of profiles, but the blue  
110 region represents only the portion with QPI > 5 km. We will fix this.

111 Line 180. Please specify the convention for flagging. It is my understanding that BGCArgo  
112 flagging may have changed through the years and between institutions. (I’ve used Sprofs where  
113 3 means bad).

114 We will provide a brief description here and include reference to the relevant Argo user manual  
115 for more information.

116 How does the GlobColour product compare to other products? Why is this one selected over  
117 others? (OCCCI, for instance). I suggest including a brief sentence.

118 We did not compare how different satellite products affect the scales that are calculated. We  
119 chose GlobColour because it is blended from all available satellites and is therefore probably a  
120 most complete product in terms of space-time coverage without interpolation. Further, the study  
121 of Zhang et al. (2019) demonstrated that GlobColour data projected onto surface drifter tracks  
122 resolve realistic Lagrangian behavior in terms of (sub)mesoscale dynamics, so we conclude that  
123 their space-time information is biophysically accurate. We plan to include this information in the  
124 manuscript, in the Methods section where we introduce the data. As for why we chose to use a  
125 25 km product, that requires a more nuanced discussion and we refer you to please see our  
126 Author Comment to Referee #1. We propose to include that discussion in a revised Discussions  
127 section.

128 Section 3.3 could be simplified. Two sets of chlorophyll anomalies are estimated: 1. Anomalies  
129 with respect to a 31-day smoothing filter, and 2. Anomalies with respect to the climatology. I  
130 would suggest stating something like that to start, and then continue with the details.

131 This is a reasonable suggestion, and we can modify the opening sentence of section 3.3  
132 accordingly.

133 The climatology is based on the same 31-day filter + a boxcar function? This is not exactly what  
134 comes to my mind when “climatology” or “repeating annual cycle” is mentioned.

135 We apologize for the confusion here. This is an admittedly technical point so we left the details  
136 in the Appendix B, but perhaps we need to clarify the main text. Essentially, the “smoothed”  
137 subtrahend is from a 3-D convolution with a filter kernel that is a 2-D Gaussian in space and a  
138 31-day Hamming window in time. The “climatology” subtrahend comes from first stacking the  
139 arrays by day of year in a 4<sup>th</sup> dimension so that the convolution is with a 4-D kernel that is a 2-D  
140 Gaussian in space, a 31-day Hamming window in day-of-year (like a Julian day, not absolute  
141 calendar date), and a boxcar (equal weights) across years. That way, as we say in the Appendix  
142 B, “[for] example, January 1 of every year is regarded as having the same time coordinate”. The  
143 end result is a set of maps for each day-of-year, hence making it a repeating annual cycle. We  
144 can move the illustrative sentence (reproduced here) to the main text for clarity.

145 I don’t like the use of the satellite-based “subtrahend” to estimate chlorophyll anomalies from the  
146 MLD-averaged chlorophyll from the float. How does the MLD average compare to the satellite?  
147 I think some type of bias correction may be needed. You mention that the subtrahend is  
148 regressed against float data. Do you mean you corrected a bias? That should be included in a  
149 supplement.

150 It is not possible to construct a “climatology” subtrahend from the floats because there is not  
151 enough interannual coverage of floats over the spatial footprint of the horizontal component of  
152 the filter at any given time step. For this reason, we need to turn to climatological fields  
153 constructed from the satellite data. To illustrate how the subtrahends look (and how float and  
154 satellite data compare), we included Figure B1. We think that figure illustrates that the satellite-  
155 constructed “climatology” subtrahend is reasonable to compare with the float data. As you point  
156 out, the regression effectively serves as a bias correction so that the mean and range of the  
157 subtrahend (once it is projected onto the floats) is comparable to the mean and range of the float-  
158 measured chlorophyll. The details of the procedure are described in the existing Appendix B. If it  
159 is helpful, regression coefficients can be included.

160 Line 240. Why aren't Eulerian and Lagrangian segments equal?

161 This is a matter of convenience. The Lagrangian segments should be kept as short as possible  
162 because as a platform moves it may encounter different environmental (physical or otherwise)  
163 conditions, and we found 120 days was a reasonable length of time. However, this is not  
164 important for Eulerian segments, especially since low frequency (such as seasonal) variability  
165 has been removed. Since the Eulerian data are stored in annual files, it was easiest to work with  
166 year-long segments.

167 Section 3.4 could be simplified as well. If I understand correctly, you tested two approaches to  
168 estimate spatially averaged scales. In lines 272-275 you mention you use one or the other. When  
169 and why you use each one should be clearer.

170 This is basically correct. When possible, we apply both methods (e.g., compare Figures 6 and  
171 D1), but only equation 8 is an option for any scales derived from ocean color due to the large  
172 number of gaps. In simplest terms: "All scales are derived by averaging in space (from  
173 integrating Eq. (7) and averaging), except any scales involving satellite ocean color, where large  
174 numbers of gaps require computing scales from space-composited ACFs (from integrating Eq.  
175 (8))." We can open the discussion on lines 272-281 with the preceding simple sentence and then  
176 eliminate much of the redundant (and less clear) text that follows.

177 Line 292. Picks?

178 Sorry: "picks" should read "scales".

179 Lines 319-320: "If we take ..." this sentence is confusing.

180 We apologize for the confusion here. Our intention is to draw some contrast between float  
181 profiles where the QPI is "small" and "large". While the distribution in Figure 2 is continuous  
182 and there is no real threshold, we noted that there is a mode of profiles between zero and 5 km,  
183 so we chose this threshold for display purposes. As we mention in the text, 5 km is a good  
184 compromise between having a large amount of profiles and having a QPI that is small, so it  
185 serves as a reasonable threshold between a "small" and "large" QPI for the purposes of display in  
186 Figures 2-3. Other than for display purposes in those figures, though, QPI is only used for  
187 weighting averaged scales and there is no use of a threshold in Figures 4-9 or their  
188 interpretations. We can update the text with the information supplied in this Author's Comment  
189 document to clarify where the 5 km threshold comes from and when and why it is used.

190 I probably missed this. Are the results in figures 5 to 9 based on all profiles or only QPI<5km?

191 We apologize for the confusion here. Figures 5 to 9 display results based on all float profiles. We  
192 can update the captions to convey this. The filled circles treat all float segments equally in the  
193 averages whereas the crosses weight by segment-median  $QPI^{-2}$  so that segments with smaller  
194 QPI count more.

195

## 196 **References:**

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