



1 **Assessing improvements in global ocean pCO₂ machine learning reconstructions with**
2 **Southern Ocean autonomous sampling**

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9

10 **Abstract**

11 The Southern Ocean plays an important role in the exchange of carbon between the atmosphere
12 and oceans, and is a critical region for the ocean uptake of anthropogenic CO₂. However, estimates
13 of the Southern Ocean air-sea CO₂ flux are highly uncertain due to limited data coverage. Increased
14 sampling in winter and across meridional gradients in the Southern Ocean may improve machine
15 learning (ML) reconstructions of global surface ocean pCO₂. Here, we use a Large Ensemble
16 Testbed (LET) of Earth System Models and the pCO₂-Residual reconstruction method to assess
17 improvements in pCO₂ reconstruction fidelity that could be achieved with additional autonomous
18 sampling in the Southern Ocean added to existing Surface Ocean CO₂ Atlas (SOCAT)
19 observations. The LET allows us to robustly evaluate the skill of pCO₂ reconstructions in space
20 and time through comparison to ‘model truth’. With only SOCAT sampling, Southern Ocean and
21 global pCO₂ are overestimated, and thus the ocean carbon sink is underestimated. Incorporating
22 Uncrewed Surface Vehicle (USV) sampling increases the spatial and seasonal coverage of
23 observations within the Southern Ocean, leading to a decrease in the overestimation of pCO₂. A
24 modest number of additional observations in southern hemisphere winter and across meridional
25 gradients in the Southern Ocean leads to improvement in reconstruction bias and root-mean
26 squared error (RMSE) can be improved by as much as 65 % and 19 %, respectively, as compared
27 to using SOCAT sampling alone. Lastly, the large decadal variability of air-sea CO₂ fluxes shown
28 by SOCAT-only sampling, may be partially attributable to undersampling of the Southern Ocean.

29



30 1. Introduction

31 The ocean plays an important role in mitigating against climate change by sequestering
32 anthropogenic carbon emissions. Since 1850, the oceans have removed a total of 170 ± 35 Gt of
33 carbon (Friedlingstein et al., 2022). In order to fully understand the climate impacts from rising
34 emissions, it is essential to accurately quantify the air-sea CO_2 flux and the global ocean carbon
35 sink in space and time. The Surface Ocean CO_2 Atlas (SOCAT; Bakker et al., 2016) is the largest
36 global database of surface ocean CO_2 . It contains over 33 million high-quality direct shipboard
37 measurements of $f\text{CO}_2$ (uncertainty of $< 5 \mu\text{atm}$), which have been gathered since 1957 (Bakker et
38 al., 2022). However, due to limited resources for ocean observing, limited number of ships/routes,
39 inaccessible regions and unsafe waters, the database covers only about 1% of the global ocean at
40 monthly $1^\circ \times 1^\circ$ spatial resolution over the period of 1982-2023, and is highly biased towards the
41 northern hemisphere.

42 Observation-based data products have been developed to better constrain surface ocean
43 pCO_2 in space and time by extrapolating to global coverage from the sparse SOCAT observations
44 (e.g., Landschützer et al., 2014; Rödenbeck et al., 2015; Gloege et al., 2022; Bennington et al.,
45 2022a,b). These data products utilize machine learning (ML) algorithms to estimate a non-linear
46 function between a suite of driver variables (i.e., sea surface temperature; SST, sea surface salinity;
47 SSS, mixed layer depth; MLD, Chlorophyll; Chl-a, $x\text{CO}_2$; atmospheric CO_2) and ocean pCO_2 (the
48 target variable) where these are co-located. The driver variables are proxies for processes
49 influencing ocean pCO_2 . Full-coverage driver variable datasets are then processed through these
50 ML algorithms to produce estimated global full-coverage surface ocean pCO_2 . Since the data
51 products rely on observations to train the algorithms and thus produce these relationships, data
52 sparsity remains a fundamental limitation to this technique.

53 It has been suggested that targeted sampling from autonomous platforms combined with
54 ships, filling in the state space of pCO_2 , represent a likely path forward to improve surface ocean
55 pCO_2 reconstructions (Bushinsky et al., 2019; Gregor et al., 2019; Gloege et al., 2021;
56 Djeutchouang et al., 2022; Landschützer et al., 2023). One major obstacle, however, is that the
57 indirect pCO_2 estimates from floats have high uncertainties ($\pm 11.4 \mu\text{atm}$) and may be biased by
58 as much as $\sim 4 \mu\text{atm}$ (Bakker et al., 2016; Williams et al., 2017; Fay et al., 2018; Gray et al., 2018;
59 Sutton et al., 2021; Mackay and Watson 2021; Wu et al 2022). Biases and uncertainties can have



60 large impacts on global air-sea CO₂ flux estimates, given that the global mean air-sea
61 disequilibrium is only 5-8 μatm (McKinley et al., 2020). It is therefore critical that bias and
62 uncertainty corrections are well-constrained over different oceanic conditions and over time.

63 Uncrewed Surface Vehicles (USVs), such as those manufactured and maintained by
64 Saildrone Inc., represent a new type of autonomous platform that can obtain direct pCO₂
65 observations with significantly lower uncertainties compared to other autonomous methods, and
66 equivalent to the highest-quality shipboard measurements contained in SOCAT (± 2 μatm; Sabine
67 et al., 2020; Sutton et al., 2021). Such improvements in sampling are critically important in the
68 undersampled Southern Ocean. This region is fundamental in terms of the ocean's ability to
69 remove carbon from the atmosphere, being responsible for ~ 40% of the global ocean uptake of
70 anthropogenic CO₂ (Khatiwala et al., 2009). Improved data coverage in the Southern Ocean
71 represents thus a major opportunity to advance our understanding of the global ocean carbon sink
72 (Lenton et al., 2006, 2013; Takahashi et al., 2009; Monteiro et al., 2015; Gregor et al., 2019; Gray
73 et al., 2018; Mongwe et al., 2018; Bushinsky et al., 2019; Sutton et al., 2021; Long et al., 2021;
74 Mackay et al., 2022; Wu et al., 2022; Landschützer et al., 2023). A combination of SOCAT and
75 Saildrone USV observations would include high accuracy data from both the long record and
76 global coverage of ship tracks, and the expanded finer resolution of spatial and seasonal coverage
77 of the poorly sampled Southern Ocean. Importantly, Saildrone USVs are also able to cover the
78 spatial extent and seasonal cycle of the meridional gradients, which has been shown to be critical
79 in order to reduce errors in reconstructing surface ocean pCO₂ (Djeutchouang et al., 2022). A
80 combined approach, with autonomous samples such as those obtained from Saildrone USVs, in
81 addition to high-quality observations collected from ships, represents thus a promising solution to
82 improve surface ocean pCO₂ ML reconstructions.

83 Here, we assess to what extent surface ocean pCO₂ reconstructions can improve by
84 implementing the pCO₂-Residual machine learning (ML) reconstruction (Bennington et al., 2022a)
85 with the combined inputs of SOCAT and Saildrone USV coverage. However, instead of using
86 actual observations, we sample the target (i.e., surface ocean pCO₂) and driver variables (i.e., SST,
87 SSS, MLD, Chl-a and xCO₂) from our Large Ensemble Testbed (LET) of Earth System Models
88 (ESMs) (e.g., Stamell et al., 2020; Gloege et al., 2021; Bennington et al., 2022a). There are two
89 major benefits of using a testbed compared to actual observations. First, in an ESM, surface ocean



90 pCO₂ is known at all times and locations. Therefore, the pCO₂ reconstructed by the ML algorithm
91 can be robustly evaluated in space and time against a known ‘truth’ (i.e., ‘model truth’). The
92 reconstruction evaluation is thus not limited to the availability of sparse real-world ocean
93 observations. Secondly, a testbed can be used to plan and evaluate the impact of different sampling
94 strategies on the reconstructed pCO₂. It is important to stress that, by using a model testbed, we do
95 not predict real-world surface ocean pCO₂ and air-sea CO₂ fluxes. The goal here is to assess the
96 accuracy with which an ML algorithm can reconstruct the ‘model truth’ given inputs of samples
97 consistent with real-world data coverage from the SOCAT database and Saildrone USVs.

98 By utilizing the observational coverage of SOCAT and Saildrone USV transects, we assess
99 to what extent the pCO₂-Residual method accurately reconstructs model surface ocean pCO₂ in
100 space and time. Additionally, we explore the timing, magnitude, duration and spatial extent of
101 Southern Ocean USV sample additions that most significantly improve the pCO₂ predictions.

102 **2. Methods**

103 *2.1 The Large Ensemble Testbed (LET)*

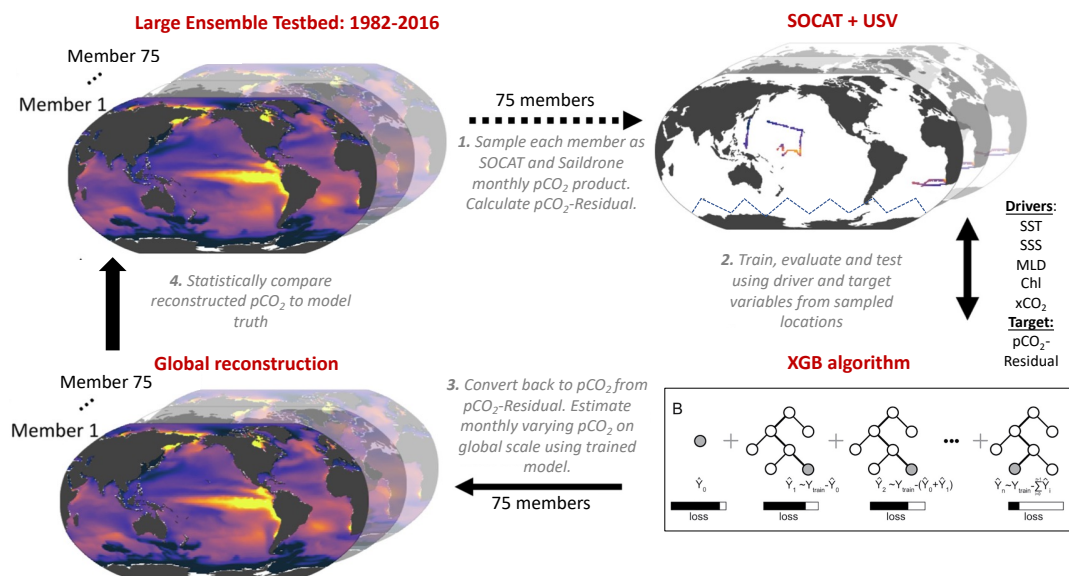
104 In this study, the Large Ensemble Testbed (LET) includes 25 members from three independent
105 initial-condition ensemble models (i.e., CanESM2, CESM-LENS and GFDL-ESM2M; Kay et al.,
106 2015; Rodgers et al., 2015; Fyfe et al., 2017), giving a total of 75 members within the testbed. We
107 do not use the MPI-GE model that was included in the past LET studies because its Southern
108 Ocean pCO₂ seasonality and decadal variability appears to be anomalously large (Gloege et al.,
109 2021; Fay and McKinley, 2021; Bennington et al., 2022a). Each individual Earth System Model
110 (ESM) is an imperfect representation of the actual Earth system, so the multiple Large Ensembles
111 are used to span different model structures and their representation of internal variability. Each
112 ensemble member undergoes the same external forcing (i.e., historical atmospheric CO₂ before
113 2005 and Representative Concentration Pathway 8.5 through 2016, plus solar and volcanic
114 forcing), but the spread across the ensemble members gives a unique trajectory of the ocean-
115 atmosphere state over time, i.e., a different state of internal variability as well as the difference
116 across models.

117 The LET used in this study includes monthly 1°x1° model output from 1982-2016 (Gloege
118 et al., 2021). For each individual ensemble member of the LET, surface ocean pCO₂ and co-located



119 driver variables (i.e., SST, SSS, Chl-a, MLD, xCO₂) were sampled monthly at a 1°x1° resolution,
 120 at times and locations equivalent to SOCAT and Saildrone USV observations (**Fig. 1**; Step 1).
 121 While the SOCAT observations were sampled from the testbed matching the actual years of
 122 sampling, the USV observations were sampled from the testbed starting in year 2007 (for ten-year
 123 sampling) or 2012 (for five-year sampling) (see **Sect. 2.4**). As our focus is on reconstruction for
 124 the open ocean, testbed output for coastal areas, the Arctic Ocean (>79°N) and marginal seas
 125 (Hudson Bay, Caspian Sea, Black Sea, Mediterranean Sea, Baltic Sea, Java Sea, Red Sea and Sea
 126 of Okhotsk) were removed prior to algorithm processing.

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128
 129 **Figure 1:** Schematic of the Large Ensemble Testbed (LET; modified from Gloege et al., 2021). **1:** Surface ocean
 130 pCO₂ from each of the 75 model members is sampled in space and time mimicking real-world SOCAT and Saildrone
 131 USV observations (see **Fig. 2**; **Table 1**; **Section 2.5**). Prior to algorithm processing, pCO₂-Residual is calculated, i.e.,
 132 the direct effect of temperature has been removed from the pCO₂ value (**Section 2.2**). **2:** The pCO₂-Residual (target
 133 variable) and co-located driver variables (i.e., SST, SSS, MLD, Chl, xCO₂) sampled from the testbed are processed
 134 by the XGBoost (XGB) algorithm (**Section 2.3**). **3:** Based on the full-coverage of driver variables, pCO₂-Residual is
 135 reconstructed globally. This process is repeated 75 times, individually for every single testbed model member. The
 136 temperature component (pCO₂-T) is then added back to the pCO₂-Residual for each value. **4:** Since we are using
 137 model testbed and not real-world observations, the globally reconstructed pCO₂ can be evaluated against the ‘model
 138 truth’ at all 1°x1° grid cells, not just where observations are available. SST = sea surface temperature. SSS = sea
 139 surface salinity. MLD = mixed layer depth. Chl = chlorophyll. xCO₂ = atmospheric concentration of CO₂.

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142 2.2 The pCO₂-Residual approach

143 We used the pCO₂-Residual approach following Bennington et al. (2022a), which removes the
144 well-studied direct effect of temperature on pCO₂ from the LET model output prior to algorithm
145 processing. Temperature has both direct and indirect effects on surface ocean pCO₂. The direct
146 effect of temperature, due to solubility and chemical equilibrium, is that an increase in temperature
147 directly causes an increase in pCO₂ (Takahashi et al., 1993). Indirectly, temperature changes are
148 associated with biological production and wintertime vertical mixing; and these processes tend to
149 result in opposing pCO₂ changes. To build reconstruction algorithms through the data-driven
150 training that occurs in ML, the statistics in all other algorithms developed to date must identify a
151 function that disentangles these competing effects of SST on pCO₂. Here, the algorithm is assisted
152 by removing this known temperature effect, and it must therefore only learn the pCO₂ impacts
153 from biogeochemical drivers. The pCO₂-Residual method leads to physically understandable
154 connections between the input data and output (Bennington et al., 2022a), which mitigates to some
155 degree ‘black box’ concerns typically associated with ML algorithms (Toms et al., 2020). Further,
156 this method has been shown to perform better against independent observations than other
157 common observation-based products (Bennington et al., 2022a). A brief description is provided
158 here, but for further details see Bennington et al. (2022a).

159 The temperature-driven component of pCO₂ (pCO₂-T) is calculated using this equation:

$$160 \quad \text{pCO}_2\text{-T} = \text{pCO}_2^{\text{mean}} * \exp[0.0423 * (\text{SST} - \text{SST}^{\text{mean}})]$$

161 where pCO₂^{mean} and SST^{mean} is the long-term mean of surface ocean pCO₂ and temperature,
162 respectively, using all 1°x1° grid cells from the testbed. Once pCO₂-T is determined, pCO₂-
163 Residual is calculated as the difference between pCO₂ and the calculated pCO₂-T:

$$164 \quad \text{pCO}_2\text{-Residual} = \text{pCO}_2 - \text{pCO}_2\text{-T}$$

165 Prior to algorithm processing, pCO₂-Residual values > 250 µatm and < -250 µatm from the
166 testbed were filtered out to target values that are not representative of the real ocean. These pCO₂-
167 Residual values generally correspond to high pCO₂, above the maximum value in SOCAT (816
168 µatm; Stamell et al., 2020). The excluded data points (less than 0.2 % per member) mostly occurred



169 in output from the CanESM2 model, and were restricted geographically, predominantly along the
170 western coastline of South America.

171 The eXtreme Gradient Boosting method (XGB; Chen and Guestrin, 2016) is used to
172 develop an algorithm that allows driver variables (i.e., SST, SSS, Chl-a, MLD, xCO₂) to predict
173 the pCO₂-Residual (**Fig. 1**; Step 2). The pCO₂-Residual and associated feature variables is split
174 into validation, training and testing sets. The test and validation set each account for 20 % of the
175 data, leaving 60 % for training. The validation set is used to optimize the algorithm
176 hyperparameters, which define the architecture of decision trees used in the model. The training
177 set is used to build the decision trees in XGB, while the test set is used to evaluate the performance
178 of the final algorithm. The XGB algorithm for this study used 4,000 decision trees with a maximum
179 depth of 6 levels. For the final reconstruction of surface ocean pCO₂ across all space and time
180 points, the previously calculated pCO₂-T values are added back to the reconstructed pCO₂-
181 Residual (**Fig. 1**; Step 3).

182 The full XGB process, including 1) training/evaluating/testing and 2) reconstructing
183 globally at a monthly resolution, was repeated individually for each LET member. This process
184 provided therefore a total of 75 unique reconstruction vs. ‘model truth’ pairs, which can be
185 statistically compared (**Fig. 1**; Step 4).

186 *2.3 Statistical Analysis in the Testbed*

187 The statistical comparisons between the test set and the reconstructions are equivalent to what
188 would be derived using real-world data (‘seen’ values). Since we are using a testbed, we can also
189 include comparisons on additional independent data, referred to as ‘unseen’ values, which
190 represent the 1°x1° grid cells of the ensemble members that do not correspond to SOCAT or
191 Sairdron USV observations. A suite of statistical metrics can be used to compare the
192 reconstruction to the ‘model truth’ in order to assess how well the algorithm can extrapolate from
193 sparse data to full-field coverage (**Fig. 1**; Step 4). In this study, we focus on bias and root-mean-
194 squared error (RMSE). Bias is calculated as ‘mean prediction – mean observation’ (i.e., pCO₂
195 predicted by XGB subtracted by the pCO₂ ‘model truth’), and is a measure of over- or
196 underestimation in the reconstructions. RMSE measures the magnitude of the predicted error and
197 is calculated as the square root of the mean of the squared errors.



198 2.4 Overview of sampling patterns and model runs

199 First, we sampled target and driver variables from the LET based on sampling distributions
200 equivalent to that of the SOCAT database ('SOCAT baseline'). Then, we combined the 'SOCAT
201 baseline' with testbed output representing additional Saildrone USV coverage in the Southern
202 Ocean. The additional Southern Ocean coverage was based on 1) the Sutton et al. (2021) sampling
203 campaign from 2019 ('one-latitude' track) and 2) potential future meridional USV observations
204 ('zigzag' track) (**Fig. 2**). We performed a total of 10 experimental runs (**Table 1**). These represent
205 different sampling approaches, including: 1) repeating USV sampling over a five- or ten-year
206 period, 2) varying the number of USVs and thus the total number of observations, and 3) restricting
207 all observations to southern hemisphere winter months. By comparing the different runs, we can
208 assess whether or not certain targeted sampling strategies in the Southern Ocean can improve
209 surface ocean pCO₂ ML reconstructions. As discussed above, the LET runs to 2016 only (Gloege
210 et al., 2021). Saildrone USV observations were therefore sampled from the testbed starting in year
211 2006 or 2007 (for the ten-year sampling) or 2012 (for the five-year sampling) until 2016, i.e., the
212 final year of the testbed.

213 2.4.1 'One-latitude' runs

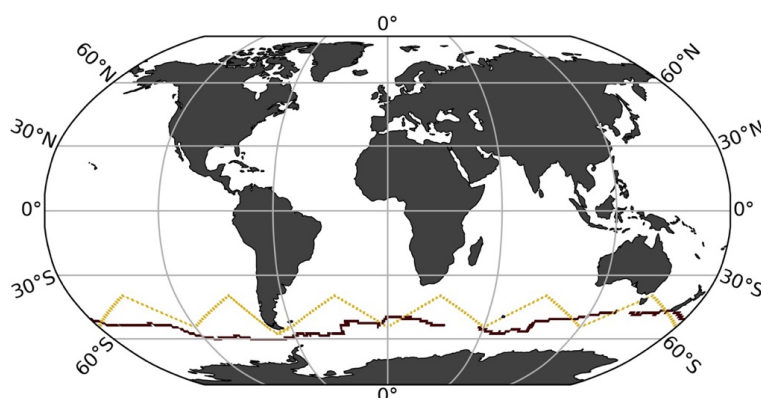
214 Six out of the ten experimental runs include the 'one-latitude' track (**Table 1**). The 2019 Saildrone
215 USV journey (Sutton et al., 2021) covered an 8-month period, from January to August. Since the
216 USV was recovered in early August, it did not cover the entire southern hemisphere winter (**Fig.**
217 **S1**). We repeated this 'one-latitude' eight-month sampling pattern for five years ('5Y_J-A'; 2,075
218 observations) and ten years ('10Y_J-A'; 4,150 observations). In order to evaluate year-round
219 ('YR') coverage, the eight-month sampling period (January-August) was shifted by one month
220 each year for ten years ('10Y_YR'; 4,150 observations). Furthermore, in order to evaluate the
221 impact of increased sampling, the 2019 Saildrone USV track was repeated 12 times with
222 incremental offsets of 1° from the original track, covering an additional 6° north and south (**Fig.**
223 **S2**). This 'high-sampling'-run ('x13_10Y_J-A'; 44,250 observations) represents a total of 13
224 USVs. We also performed an additional 13 USV run, but including observations from southern
225 hemisphere winter ('W') months only ('x13_10Y_W'; 25,395 observations). Finally, considering
226 the cost of deploying 13 USVs, a downscaled 'multiple-USV-winter-only'-run was tested,



227 including five USVs sampling over a period of five years ('x5_5Y_W'; 5,022 observations). This
228 run covers an additional 2° north and south from the original USV track.

229 2.4.2 'Zigzag' runs

230 Four of the ten experimental runs represent potential meridional sampling in the Southern Ocean
231 ('zigzag' tracks; **Table 1**) as suggested by Djeutchouang et al. (2022). Due to limited solar
232 radiation that powers the Saildrone USVs, we let the sampling occur at a maximum latitude of 55°
233 S. This alternative sampling pattern represents USVs sailing west to east in a north/south 'zigzag'
234 pattern covering 40° S and 55° S for every 30° of longitude (**Fig. 2**). We created two scenarios.
235 For the first scenario, every 30° of longitude from 40° S and 55° S is visited every three months
236 within a single year as suggested by Lenton et al. (2006). Considering the average Saildrone USV
237 speed, this scenario represents four platforms equally spaced around the Southern Ocean. This
238 sampling pattern was repeated for 10 years, with year-round coverage ('Zx4_10Y_YR'; 7,600
239 observations), and for southern hemisphere winter months only ('Zx4_10Y_W'; 2,500
240 observations). The second scenario represents a 'high-sampling' strategy, where every 30° of
241 longitude from 40° S and 55° S is visited approximately monthly. This can be achieved by
242 deploying 10 platforms equally spaced around the Southern Ocean. This sampling pattern is
243 repeated for five years, sampling year-round ('Z_x10_5Y_YR'; 11,400 observations) and during
244 southern hemisphere winter months only ('Z_x10_5Y_W'; 3,800 observations).



245
246 **Figure 2:** Saildrone Uncrewed Surface Vehicle (USV) tracks representing the first circumnavigation around
247 Antarctica from 2019 in maroon ('one-latitude' track; Sutton et al., 2021) and an alternative virtual route with
248 meridional coverage ('zigzag' track).



Run name	5Y J-A	10Y J-A	10Y YR	x13 10Y J-A	x13 10Y W	x5 5Y W	Z x4 10Y YR	Z x4 10Y W	Z x10 5Y YR	Z x10 5Y W
Saildrone track	One-lat	One-lat	One-lat	One-lat	One-lat	One-lat	Zigzag	Zigzag	Zigzag	Zigzag
Years of sampling	5	10	10	10	10	5	10	10	5	5
# of Saildrones	1	1	1	13	13	5	4	4	10	10
Duration of sampling	Jan-Aug	Jan-Aug	Year-round	Jan-Aug	SO winter	SO winter	Year-round	SO winter	Year-round	SO winter
Total observations	2,075	4,150	4,150	44,250	25,395	5,022	7,600	2,500	11,400	3,800
Global coverage increase (%)	0.01	0.02	0.02	0.2	0.1	0.02	0.03	0.01	0.04	0.01

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Table 1. Overview of the different Saildrone USV sampling patterns tested in this study using the XGBoost Machine Learning algorithm (Gloege et al., 2021; Bennington et al., 2022a) to estimate surface ocean pCO₂. The ‘one-latitude’ (‘one-lat’) track incorporate the Saildrone USV route from Sutton et al. (2021), while the ‘zigzag’ track represents potential future meridional sampling (see Fig. 2). The total number of USV observations (in bold) represent 1°x1° monthly Saildrone USV observations. J-A= January-August. YR = year-round. W = southern hemisphere winter. x4, x5, x10 and x13 = four, five, ten and 13 USVs. SO winter = Southern Ocean winter months, i.e., June, July, August and also including September. Note that all runs also included SOCAT coverage.

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2.5 Air-sea CO₂ flux

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To assess the global ocean carbon sink associated with our pCO₂ reconstructions, air-sea CO₂ exchange was calculated. Here, we computed air-sea CO₂ fluxes using the bulk formulation with python package Seaflux.1.3.1 (<https://github.com/lukegre/SeaFlux>; Gregor et al. 2021; Fay et al., 2021). We calculated global and Southern Ocean flux in the same manner for 1) the testbed ‘model truth’, 2) the SOCAT baseline and 3) the 10 experimental USV runs.

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The net sea–air CO₂ flux was estimated using:

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$$\text{Flux} = k_w \cdot \text{sol} \cdot (\text{pCO}_2^{\text{ocn}} - \text{pCO}_2^{\text{atm}}) \cdot (1 - \text{ice})$$

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where ‘k_w’ is the gas transfer velocity, ‘sol’ is the solubility of CO₂ in seawater (in units of mol m⁻³ μatm⁻¹), ‘pCO₂^{ocn}’ is the partial pressure of surface ocean carbon (in μatm), either from the ‘model truth’ or from the reconstructions, and pCO₂^{atm} (in μatm) is the partial pressure of atmospheric CO₂ in the marine boundary layer. For GFDL, we used direct model output of pCO₂^{atm}, while for CESM and CanESM2, pCO₂^{atm} was calculated individually, as the product of surface xCO₂ and sea level pressure (pCO₂^{atm} from CESM was corrected for the contribution of water vapor pressure). Finally, to account for the seasonal ice cover in high latitudes, the fluxes were weighted by 1 minus the ice fraction (‘ice’), i.e., the open ocean fraction. Inputs to the calculation include EN4.2.2 salinity (Good et al., 2013), SST and ice fraction from NOAA Optimum Interpolation Sea Surface Temperature V2 (OISSTv2) (Reynolds et al., 2002), and



275 surface winds and associated wind scaling factor from the European Centre for Medium-Range
276 Weather Forecasts (ECMWF ERA5 sea level pressure (Hersbach et al., 2020). Results presented
277 show the global and Southern Ocean (< 35° S) fluxes in units of Pg C yr⁻¹.

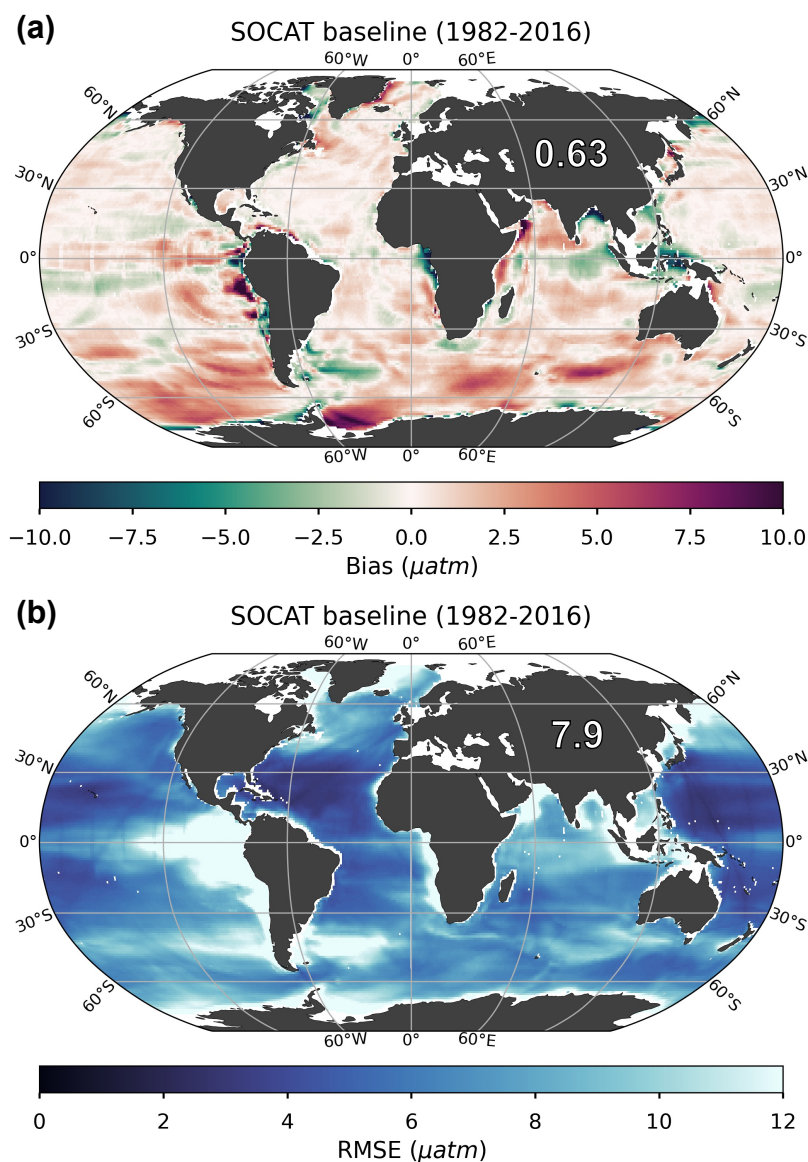
278 Note that, reconstructions of pCO₂ for the SOCAT baseline and the experimental USV runs
279 are limited in their spatial extent to the open ocean (see **Sect. 2.1**; excluding coastal areas, the
280 Arctic Ocean and marginal seas). The same mask was thus also applied when calculating the flux
281 of the ‘model truth’, prior to comparison with the reconstructions.

282 **3. Results**

283 *3.1 Performance metrics for the ‘SOCAT baseline’ reconstruction*

284 The mean bias for the entire testbed period (i.e., 1982-2016) is 0.63 μatm globally (**Fig. 3a**) and
285 1.4 μatm for the Southern Ocean (< 35° S; **Table S1**). Bias is much closer to zero for mid- (between
286 35° S and 35° N; 0.23 μatm) and northern latitudes (> 35° N; 0.11 μatm) (**Fig. 3a**). There is a
287 significant difference in bias considering southern hemisphere winter months (June, July, August)
288 versus summer months (December, January, February), with a global mean bias (for 1982-2016)
289 of 1.3 μatm compared to 0.07 μatm, respectively (**Table S1**), due to the sparseness of SOCAT
290 observations from the southern hemisphere during the harsh winter season (**Fig. S3a**). The mean
291 RMSE for the entire testbed period (i.e., 1982-2016) is 7.9 μatm globally (**Fig. 3b**) and 8.5 μatm
292 for the Southern Ocean (**Table S1**). RMSE is highest in the Eastern Tropical and Southeastern
293 Pacific Ocean and in the Southern Ocean, where the algorithm generally overestimates pCO₂ (i.e.,
294 positive bias; **Fig. 3a**). This is consistent with the areas significantly undersampled by SOCAT
295 (**Fig. S3b**). Except for these areas, RMSE and bias is generally low (close to zero) in the open
296 ocean, but show higher values along coastlines (**Fig. 3b**).

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Figure 3: Bias (a) and root-mean-squared error (RMSE) (b) when comparing the baseline machine learning reconstruction with the testbed ‘model truth’, averaged over the 75 ensemble members for the period of 1982 through 2016. The testbed was sampled based on SOCAT observations only (i.e., no USV). The global mean bias and RMSE is 0.63 μatm and 7.9 μatm , respectively. Red and green areas in a indicate regions where the reconstruction is biased high (i.e., overestimates pCO_2) and low (i.e., underestimates pCO_2), respectively. Generally, RMSE is highest in the East and South Pacific Ocean and in the Southern Ocean, where the algorithm also generally overestimates pCO_2 (positive bias; a). Note that only the open ocean was considered in the reconstruction, so several areas were masked out prior to algorithm processing, such as the Arctic Ocean, coastal areas and marginal seas (no data; white areas in figures).

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309 3.2 Reconstruction improvements with Saildrone USV additions

310 Our presentation of global maps is limited to runs ‘x5_5Y_W’ (5,022 observations) and
311 ‘Z_x4_10Y_YR’ (7,600 observations). These runs were selected as they represent observational
312 schemes that are realistic in the near-term future considering logistics and cost level, both non-
313 meridional and meridional sampling, and different approaches to observing duration and seasonal
314 coverage. For the remaining runs, equivalent maps can be found in the **Supplement**.

315 3.2.1 Bias

316 All Saildrone USV runs show a reduction in bias compared to the global mean 1982-2016 SOCAT
317 baseline (**Figs. 4a, S4**). The improvement in bias is mainly due to lower reconstructed pCO₂ values
318 at southern latitudes, where the baseline reconstruction generally overestimates pCO₂ (**Fig. 3a**).
319 The global mean bias for ‘zigzag’ run ‘Z_x4_10Y_YR’ is 0.51 μatm, a higher improvement (19 %)
320 over the SOCAT baseline compared to the ‘one-latitude’ run ‘x5_5Y_W’ (11 % improvement;
321 mean bias = 0.57 μatm;) (**Fig.4a; Table S1**). Generally, the ‘zigzag’ runs show higher
322 improvements from the SOCAT baseline (19-31 % improvement; mean bias = 0.44-0.51 μatm)
323 compared to the ‘one-latitude’ runs (7-19 % improvement; mean bias = 0.52-0.59 μatm) (**Fig S4;**
324 **Table S1**). However, the ‘one-latitude’-run ‘x13_10Y_W’ that samples southern hemisphere
325 winter months only, stands out with the lowest global mean bias of 0.39 μatm, representing a 39 %
326 improvement from the SOCAT baseline (**Table S1; Fig. S4**). This run, however, has three or five
327 times more observations (25,395) than ‘Z_x4_10Y_YR’ and ‘x5_5Y_W’, respectively.

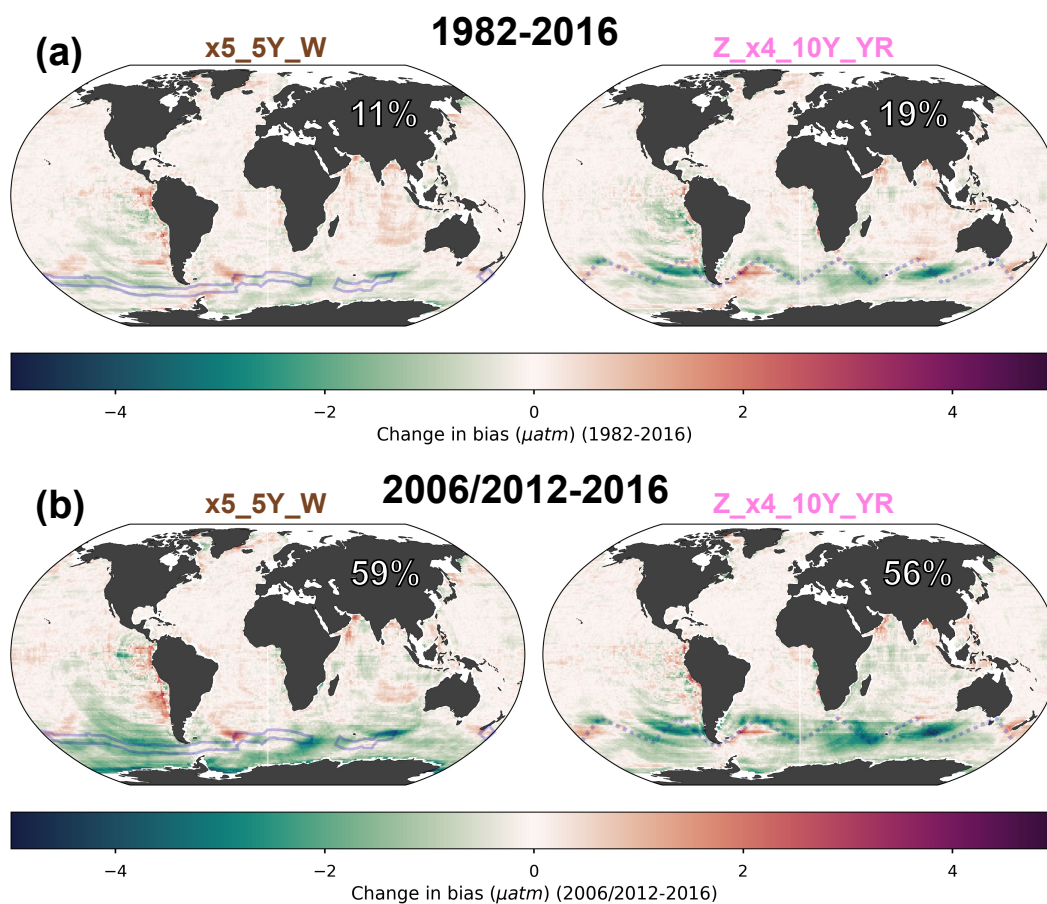
328 Compared to the entire testbed period, even larger improvements in global mean bias are
329 shown for the period of Saildrone USV additions (2006-2016 and 2012-2016; **Figs. 4a vs. 4b,**
330 **Figs. S4 vs. S5**). Compared to the SOCAT baseline, run ‘x13_10Y_W’ results in a bias
331 improvement of 95 %, while the remaining ‘one-latitude’ runs and the ‘zigzag’ runs show
332 improvements up to 63 % and 85 %, respectively (**Fig. S5**).

333 Perhaps surprisingly, there is not a strong connection between the global or Southern Ocean
334 mean bias and the number of added USV observations (**Fig. 5**). The ‘one-latitude’ ‘high-sampling’
335 run ‘x13_10Y_J-A’ (44,250 observations) show similar bias or is outperformed by all ‘zigzag’
336 runs as well as the ‘one-latitude’-runs that restrict sampling to southern hemisphere winter months
337 (i.e., ‘x5_5Y_W’ and ‘x13_10Y_W’).



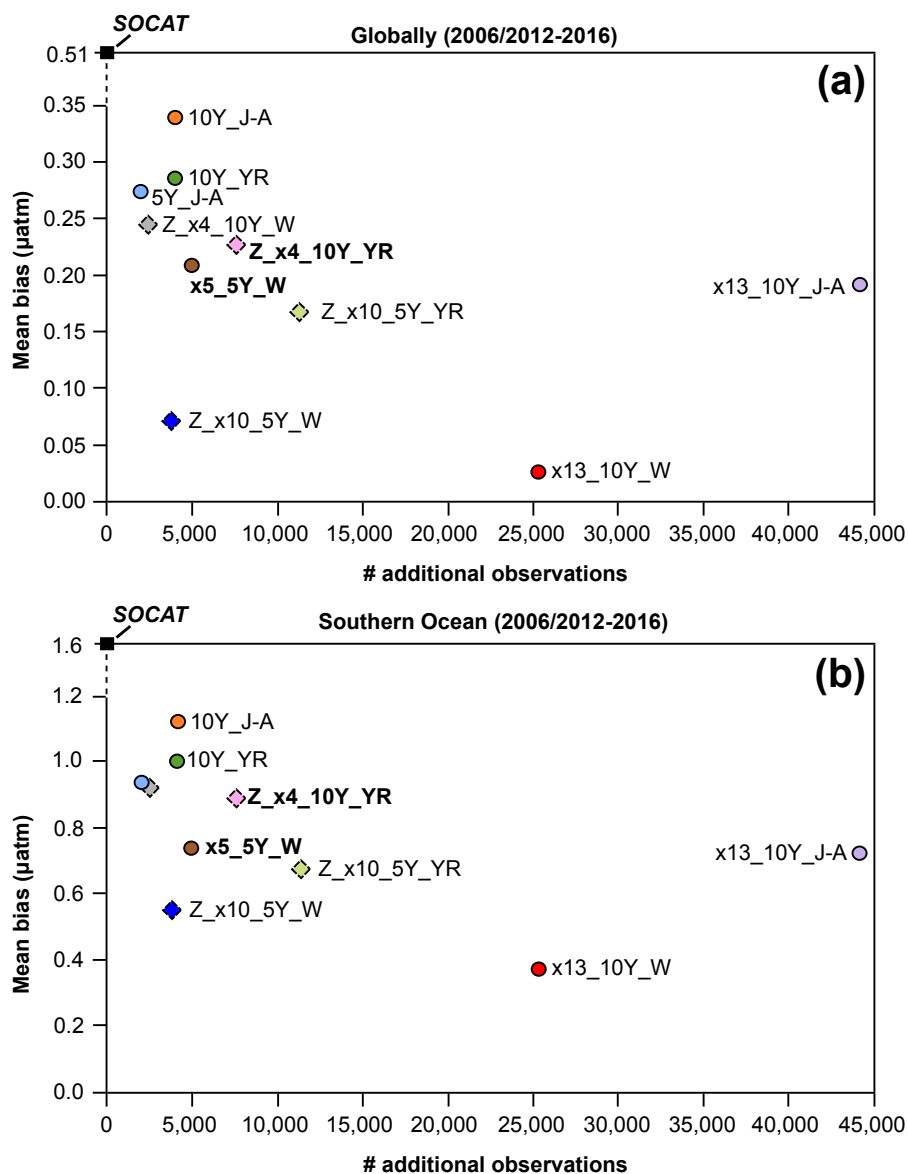
338 Considering the change in bias from year-to-year, the SOCAT baseline shows positive bias
339 at all latitudes in the beginning of the testbed period, before improvement occurs around year 1990
340 (**Fig. 6a**). This is consistent with increasing SOCAT sampling with time for the time period
341 considered here (i.e., up to 2016; **Fig. S3c**). As SOCAT observations are biased towards the
342 northern hemisphere (**Fig. S3a, b**), bias in the Southern Ocean ($< 35^\circ$ S) increases significantly
343 starting in 2000s and remains high until the end of the testbed period (**Fig. 6a**). By adding USV
344 sampling, bias in the Southern Ocean improves over the SOCAT baseline around year 2000 (**Fig.**
345 **6b-d; Fig. S6**), up to 6-12 years prior to the introduction of additional samples in either 2006 or
346 2012. Run ‘Z_x10_5Y_W’, which has the lowest bias out of the ‘zigzag’ runs (**Fig. 5**), shows
347 improvement even further back in time, until the beginning of the testbed period (**Fig. S6**). While
348 the annual mean bias of the ‘zigzag’ runs vary in a similar manner, there is a large spread between
349 the ‘one-latitude’ runs (**Fig. 6d**).

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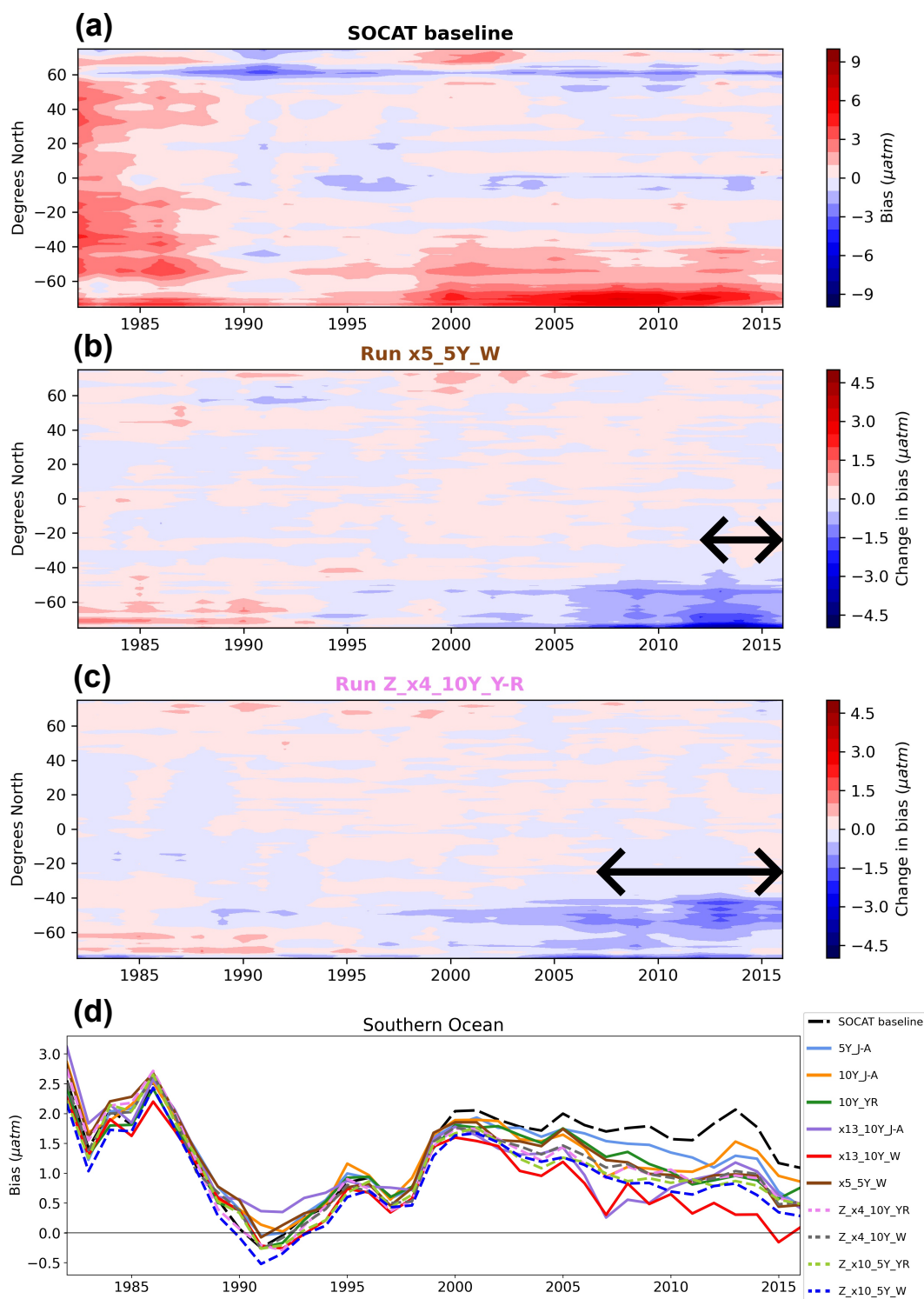


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Figure 4: Change in bias when comparing run 'x5_5Y_W' and 'Z_x4_10Y_YR' to the SOCAT baseline reconstruction, averaged over the duration of the testbed period (**a**; 1982-2016) and the period of USV additions (**b**; 2006-2012 or 2012-2016). Negative change in bias is found across the southern latitudes, indicating an improvement compared to the SOCAT baseline that overestimates pCO₂ (**Figure 3a**). The percent global improvement is shown on each panel. Note that improvement is greater in the period of Sairdrone USV additions compared to the entire testbed period.



359
 360 **Figure 5:** Mean bias globally (a) and for the Southern Ocean (b) for the duration of Saildrone USV sampling (2006-
 361 2016 or 2012-2016) for all runs presented in **Table 1**. Circles represent runs using the ‘one-latitude’ track (Sutton et
 362 al., 2021), while diamonds represent ‘zigzag’ runs. Runs highlighted in bold correspond to the two selected runs
 363 mapped in **Figure 4, 6, 7 and 9**. Global (0.51 µatm) and Southern Ocean (1.6 µatm) bias values shown for the SOCAT
 364 baseline (black squares) represent a mean of values for 2006-2016 (global = 0.52 µatm, S. Ocean = 1.63 µatm) and
 365 2012-2016 (global = 0.51 µatm, S. Ocean = 1.56 µatm). The SOCAT baseline run included 261,733 monthly 1°x1°
 366 observations. Overall, there is not a strong correlation between bias and the number of observations, or duration of
 367 sampling.
 368



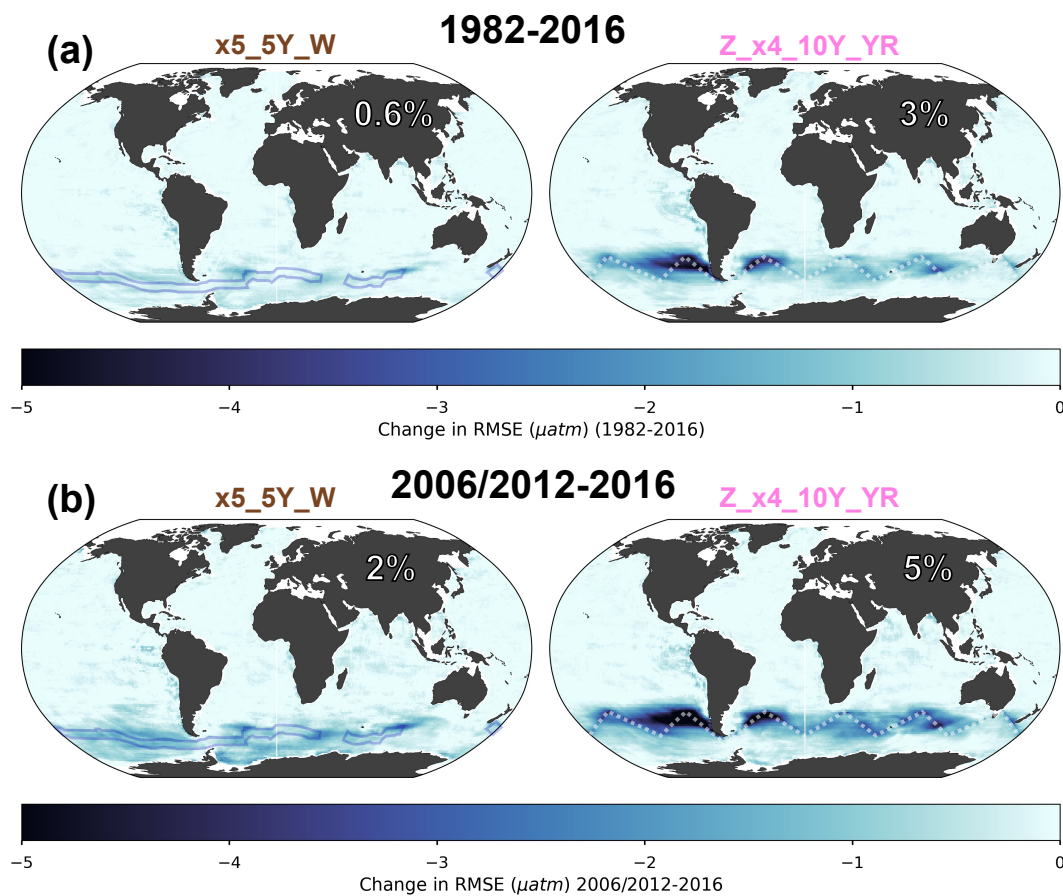


370 **Figure 6:** Zonal mean, annual mean Hovmöller of bias in SOCAT baseline with the testbed ‘model truth’, average of
371 75 ensemble members (a). There is a positive bias at all latitudes from 1982-1995; bias drops to around zero in the
372 late 1980s; and then, particularly in the Southern Ocean, increases at 2000 and remains high through 2016. Change in
373 bias of run ‘x5_5Y_W’ (b) and ‘Z_x4_10Y_YR’ (c) compared to the SOCAT baseline reconstruction shown in (a).
374 Negative changes in the Southern Ocean represents an improvement. The improvement in bias expands back in time
375 well beyond the duration of USV additions for both runs (shown by arrows on each panel). Annual mean bias for the
376 Southern Ocean (> 35° S) for all runs (d). There is a large spread in the impact on bias with ‘one-latitude’ USV
377 sampling (solid lines), while the ‘zigzag’ runs (dashed lines) more consistently reduce bias.

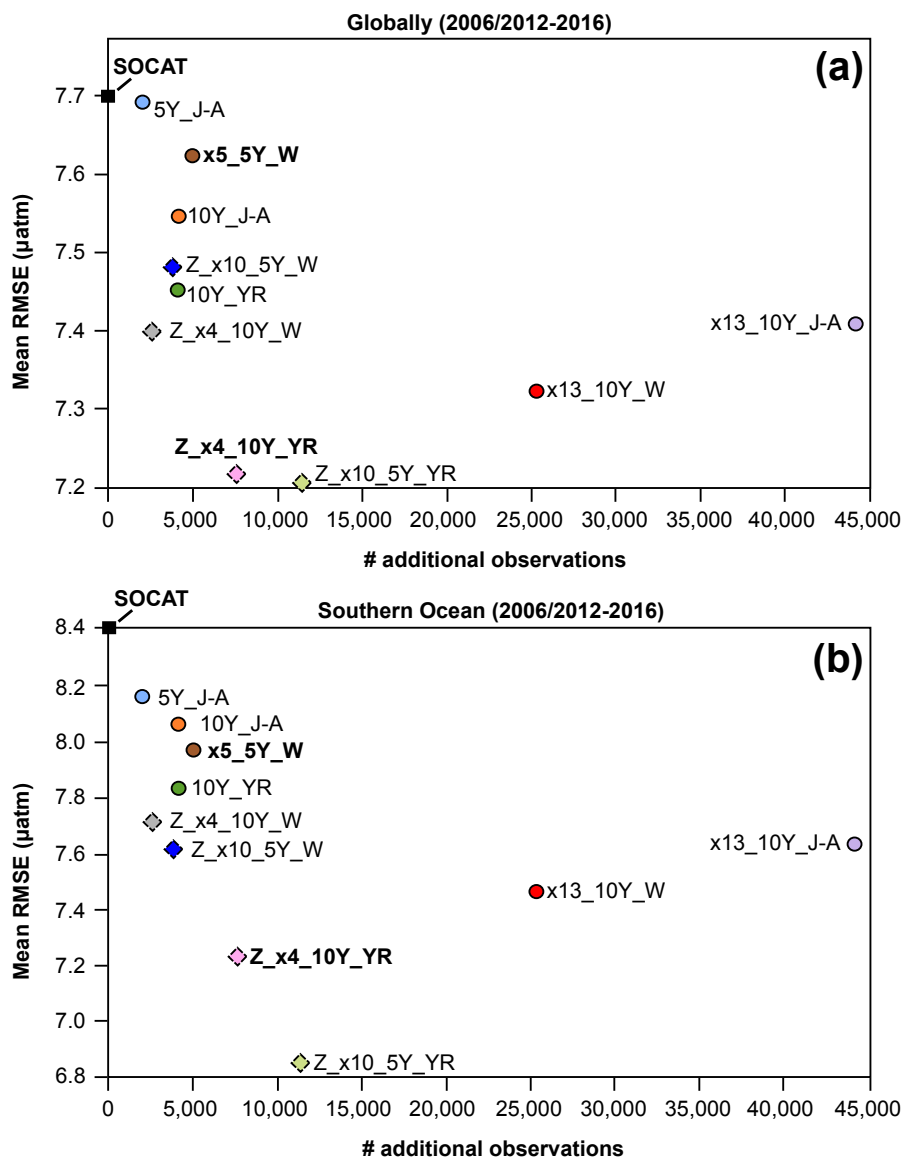
378 3.2.2 Root-mean squared error (RMSE)

379 Similar to bias, improvements in RMSE are most significant during the period of USV additions
380 and within the Southern Ocean (Fig. 7a vs. 7b). For the duration of USV additions, the ‘one-
381 latitude’ runs show improvements in global mean RMSE of 1-4 % (0.3-2 % for 1982-2016), while
382 the ‘zigzag’ runs show higher improvements between 3-8 % (2-3 % for 1982-2016) (Figs. 7, S7,
383 S8). RMSE is further reduced in southern hemisphere winter in the Southern Ocean by up to 26 %
384 (mean RMSE of 6.9 μatm ; Table S1). There is minimal change in RMSE (or bias) during southern
385 hemisphere summer months (DJF; Fig. S9). The two ‘zigzag’ runs sampling year-round
386 (‘Z_x4_10Y_YR’ and ‘Z_x10_5Y_YR’) have the lowest RMSE values both globally and in the
387 Southern Ocean (Fig. 8).

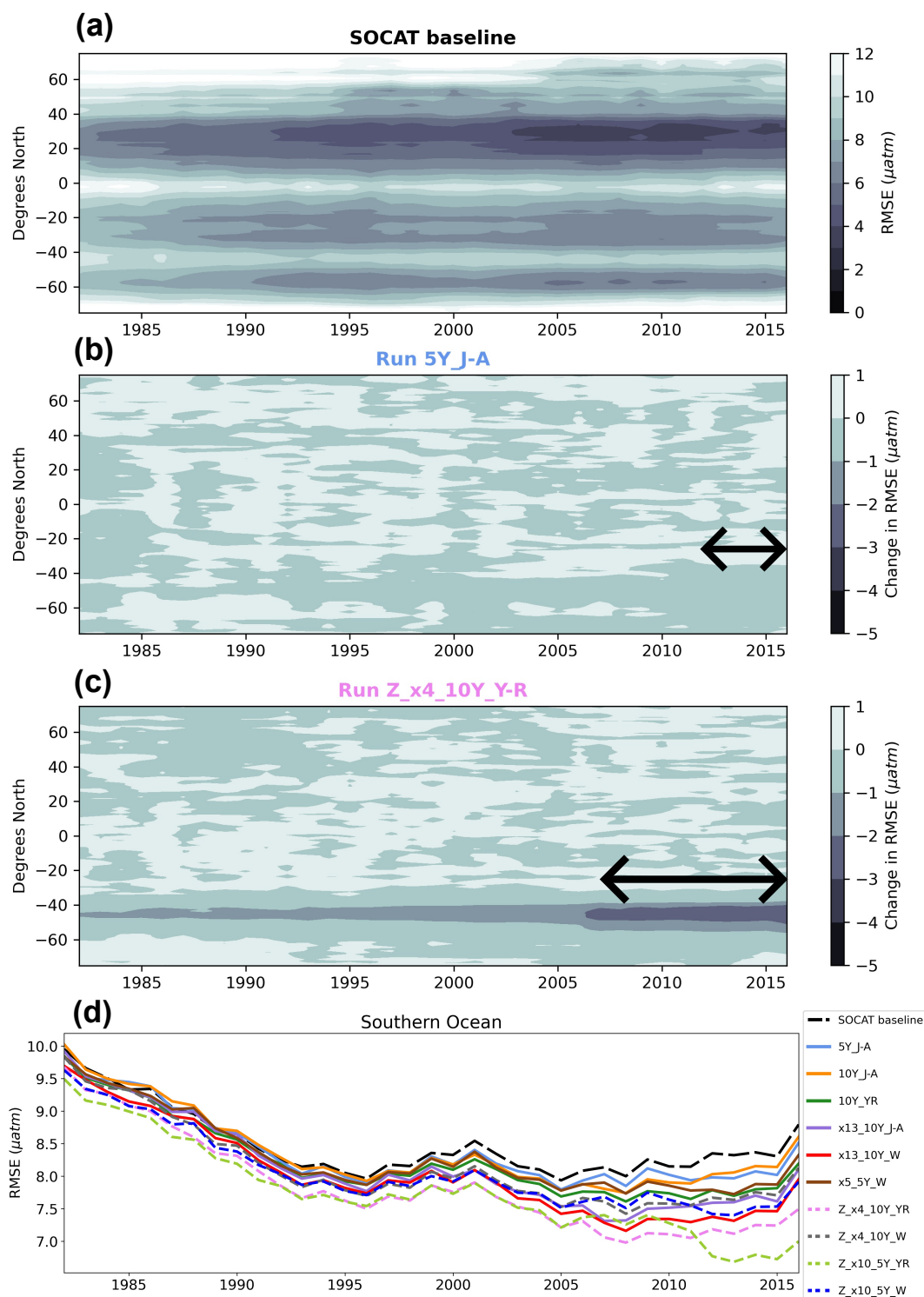
388 The ‘zigzag’ runs, as well as the ‘high-sampling’ ‘one-latitude’-runs (i.e., ‘x13_10Y_J-A’
389 and ‘x13_10Y_W’), show improvements compared to the SOCAT baseline from the initiation of
390 sampling (Figs. 9, S10). The year-round ‘zigzag’ runs, however, show improvement in the
391 Southern Ocean from the beginning of the testbed period (Figs. 9c, d, S10). RMSE improvements
392 back in time are more significant for all runs in the southern hemisphere winter months (Fig. S11).



393
394 **Figure 7:** Change in RMSE when comparing run 'x5_5Y_W' and 'Z_x4_10Y_YR' to the SOCAT baseline
395 reconstruction, averaged over the duration of the testbed period (**a**; 1982-2016) and the period of Sairdrone USV
396 additions (**b**; 2006-2012 or 2012-2016). Improvement in RMSE occurs mainly in southern latitudes ($<35^{\circ}\text{S}$), where
397 the baseline reconstruction shows high RMSEs (**Fig. 3b**). The percent global improvement is shown on each panel.
398 Note the greater improvement for the period of USV additions compared to the entire testbed period.



399
 400 **Fig. 8:** Mean RMSE globally (a) and for the Southern Ocean (< 35° S; b) for the duration of Saildrone USV sampling
 401 (2006-2016 or 2012-2016) for all runs presented in **Table 1**. ‘One-latitude’ runs (circles), ‘zigzag’ runs (diamonds).
 402 Runs highlighted in bold correspond to the two selected runs mapped in **Figure 4, 6, 7 and 9**. Global (7.7 µatm) and
 403 Southern Ocean (8.4 µatm) bias values shown for the SOCAT baseline (black squares) represent a mean of values for
 404 2006-2016 (global = 7.6 µatm, S. Ocean = 8.3 µatm) and 2012-2016 (global = 7.8 µatm, S. Ocean = 8.5 µatm). The
 405 SOCAT baseline run included 261,733 monthly 1°x1° observations. Overall, there is not a strong correlation between
 406 increasing number of observations or duration of sampling and decreasing RMSE.





408 **Figure 9:** Zonal mean, annual mean Hovmöller of RMSE in SOCAT baseline with the testbed ‘model truth’, average
409 of 75 ensemble members (a). Dark and light areas represent regions where RMSE is low and high, respectively. RMSE
410 is highest at latitudes $> 60^\circ$ S, $> 60^\circ$ N and around 40° S and the equator. RMSE is higher at all latitudes in
411 the beginning of the testbed period, before some improvement occurs in the 1990s. Change in RMSE of run ‘x5_5Y_W’
412 (b) and ‘Z_x4_10Y_YR’(c) compared to the SOCAT baseline reconstruction shown in (a). Dark areas represent
413 regions where the change in RMSE is negative, i.e., where the Saildrone USV sampling additions improve the pCO₂
414 reconstruction. Run ‘Z_x4_10Y_YR’ shows improvements in RMSE within the Southern Ocean, which expand well
415 beyond the duration of Saildrone USV additions (shown by arrow on panel). Annual mean RMSE for the Southern
416 Ocean ($> 35^\circ$ S) for all runs (d).

417

418 3.3 Impact on the air-sea CO₂ flux with Saildrone USV additions

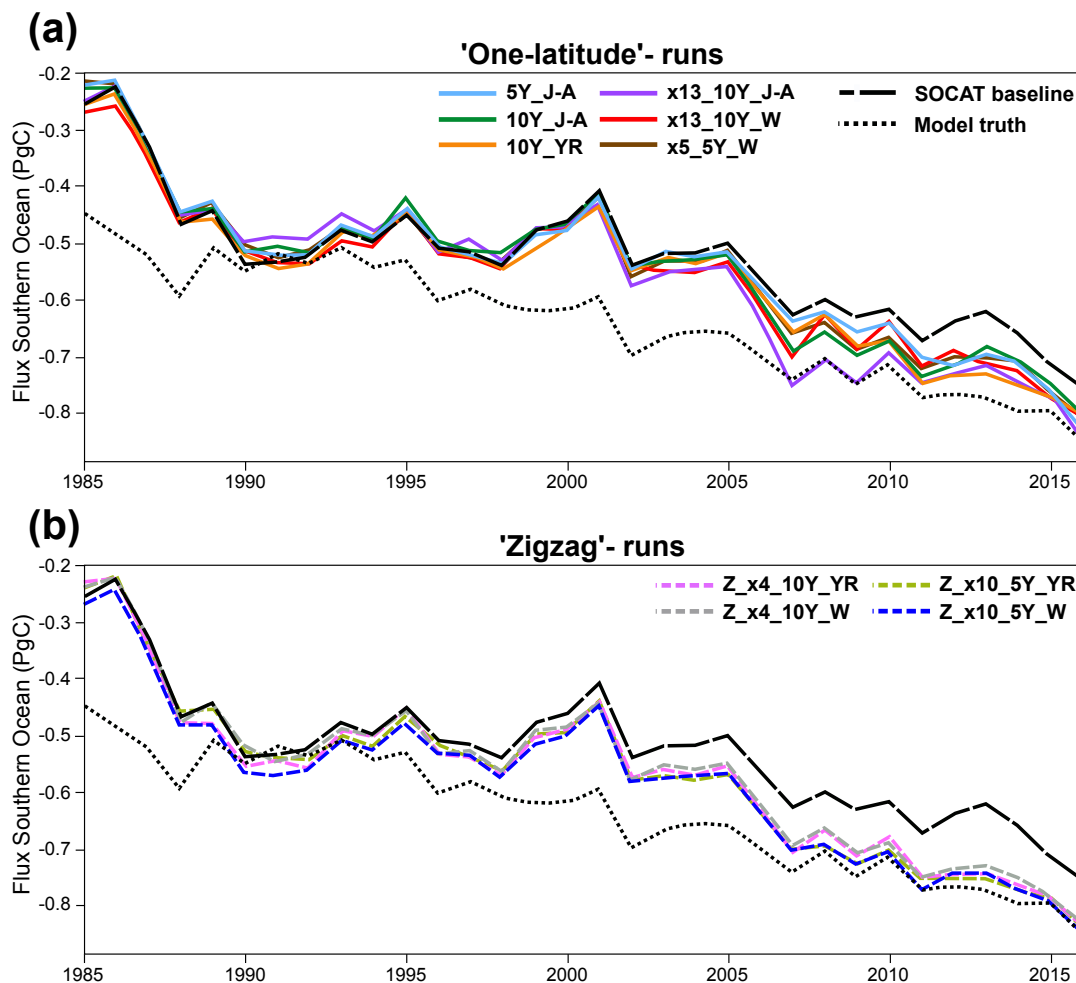
419 Air-sea flux was calculated in the same manner for both the ML reconstructions and the ‘model
420 truth’, which allows for direct comparison of the differences in fluxes (see Sect. 2.5). These flux
421 estimates are made to inform understanding of the errors that may exist in CO₂ flux estimates
422 derived from pCO₂ reconstructions, and how new sampling could address these errors. These
423 fluxes are not estimates of real-world fluxes.

424 Compared to the ‘model truth’, the SOCAT baseline reconstruction underestimates the
425 global and Southern Ocean sink by 0.11-0.13 Pg C yr⁻¹ over 1982-2016 (Fig. 10; Table S2).
426 Regardless of sampling pattern, adding Saildrone USV observations increases both the global and
427 Southern Ocean mean sink compared to the SOCAT baseline (Figs. 10, S12). The ‘one-latitude’
428 runs show an increase of 0.01-0.03 Pg C yr⁻¹ (2-6 % strengthening) of the Southern Ocean sink
429 (1982-2016), while the ‘zigzag’ runs lead to an even stronger sink 0.04-0.06 Pg C yr⁻¹ (7-11 %
430 strengthening) (Table S3). When averaging over the years of Saildrone USV sampling addition
431 (i.e., 2006-2012 and 2012-2016), the Southern Ocean sink increases up to 0.09 Pg C yr⁻¹ (14 %
432 strengthening) for the ‘one-latitude’ runs and up to 0.1 Pg C yr⁻¹ (15 % strengthening) for the
433 ‘zigzag’ runs (Table S3). These same features are found for the global ocean (Fig. S12; Table
434 S3).

435 All of the ‘zigzag’ runs quite closely match both the global and Southern Ocean ‘model
436 truth’ air-sea CO₂ flux for the duration of sample additions (Figs. 10, S12). Except for the first
437 couple of years of sample addition for the ‘high-sampling’-run ‘x13_10Y_J-A’, none of the ‘one-
438 latitude’ runs are able to match the ‘model truth’ air-sea CO₂ flux, as they all underestimate the
439 flux (Figs. 10, S12). The ‘zigzag’ runs have impact on the air-sea flux from an earlier date, starting



440 to pull the results away from the SOCAT baseline and toward the ‘model truth’ already in the late-
441 1990s, while the ‘one-latitude’ runs do the same about a decade later (Figs. 10, S12).



442
443 **Figure 10:** Southern Ocean (< 35° S) annually averaged air-sea CO₂ flux for the SOCAT baseline (black dashed line),
444 ‘model truth’ (black dotted line) ‘one-latitude’ runs (a; solid lines) and ‘zigzag’ runs (b; dashed lines), averaged over
445 the 75 ensemble members. Compared to the SOCAT baseline, regardless of sampling pattern, the Sailability USV
446 additions lead to an increased ocean sink. The ‘zigzag’ runs generate a stronger sink compared to the ‘one-latitude’
447 runs, and closely match the ‘model truth’ for the duration of sample additions.

448

449

450 4. Discussion

451 We have tested the pCO₂-Residual reconstruction method with the Large Ensemble Testbed (LET)
452 to estimate its fidelity and understand how new samples could increase skill. We find that,



453 regardless of the chosen Saildrone USV sampling pattern, the reduction in both bias and RMSE
454 compared to the SOCAT baseline is most prominent within the Southern Ocean ($< 35^\circ$ S) during
455 the period of which Saildrone USV observations were added (**Figs. 4, 6, 7, 9**). However, it is
456 important to mention that additional Southern Ocean sampling also improves pCO₂ reconstructions
457 globally (**Figs. 5a, 8a**). Based on our experiments, a combination of factors seems to be important
458 in order to improve both the global and Southern Ocean pCO₂ reconstructions, and include mainly
459 the type of sampling pattern and seasonality of sampling, but also to some extent the number of
460 additional observations. Importantly, increasing the number of observations or duration of
461 sampling (5 vs. 10 years) is not the sole determining factor for improving the reconstructions (**Figs.**
462 **5, 8**). This is best demonstrated by the ‘high-sampling’-run ‘x13_10Y_J-A’ (44,250 observations),
463 which does not provide significantly better reconstructions, or is even outperformed, by runs with
464 2-18 times less observations, but that cover the full southern hemisphere winter (**Figs. 5, 6d, 8,**
465 **9d**). Run ‘x13_10Y_J-A’ does not include more than a few observations in the month of August,
466 as it follows the temporal pattern of the real-world ‘one-latitude’ Saildrone USV expedition (**Fig.**
467 **S1**; Sutton et al., 2021). The ‘one-latitude’ runs ‘10Y_J-A’ and ‘10Y_YR’ are directly comparable
468 in terms of sample duration, spatial extent and number of observations (**Table 1**), but the latter,
469 which covers all months, always shows lower RMSE and bias (**Figs. 5, 6d, 8, 9d**). These examples
470 attest to the importance of addressing the issue of significant undersampling in the Southern Ocean
471 during the winter season (**Figs. S3a, b**).

472 Another important comparison is the ‘one-latitude’-run ‘x5_5Y_W’ (5,022 observations)
473 and ‘zigzag’-run ‘Z_x10_5Y_W’ (3,800 observations) that both sample during southern
474 hemisphere winter months over a five-year period (**Table 1**), where the ‘zigzag’-run consistently
475 performs better even though it includes fewer observations (**Figs. 5, 8**). Most of the runs that
476 perform similar to, or outperform, the above-mentioned ‘high-sampling’-run ‘x13_10Y_J-A’
477 (44,250 observations), sample in a ‘zigzag’ pattern. Out of all 10 runs, the ‘year-round’ ‘zigzag’
478 runs (‘Z_x4_10Y_YR’ and ‘Z_x10_5Y_YR’) are most able to reduce the magnitude of error as
479 shown by the lowest RMSE values (**Figs. 8, 9d**). A recent study performed similar sampling
480 experiments as shown here, by comparing sampling from different types of autonomous platforms
481 to a SOCAT baseline (Djeutchouang et al., 2022). They emphasized the importance of capturing
482 the significant differences in pCO₂ that exist across meridional gradients during summer and
483 winter months (up to 15 μ atm; Djeutchouang et al., 2022). The meridional coverage provided by



484 the ‘zigzag’ runs could explain why these runs generally outperform the ‘one-latitude’ runs in our
485 study, and show significant reduction in both RMSE and bias, even though the global pCO₂ data
486 density is raised by as little as 0.01-0.04 %.

487 The greatest reduction in bias out of all runs is however shown by run ‘x13_10Y_W’ (**Figs.**
488 **5, 6d**), which represents ‘one-latitude’ ‘high-sampling’ (i.e., 25,395 observations) during southern
489 hemisphere winter months only. This sampling strategy seems thus to have a higher ability to
490 reduce the ML model’s tendency to overestimate pCO₂ in the Southern Ocean compared to any of
491 the meridional (‘zigzag’) runs. However, it should be noted that run ‘x13_10Y_W’ cover areas
492 south of 55° S (**Fig. S2**), and its improvement in bias (and RMSE) is particularly prevalent at such
493 high latitudes (e.g., **Figs. S5, S6, S8, S10**). Whether or not this run is in fact feasible with current
494 or future technology is uncertain as parts of the southernmost tracks cover the Southern Ocean ice
495 zone (**Fig. S13**), and solar radiation for solar-powered platforms and sensors becomes very limited
496 during winter south of 55° S. Furthermore, this particular sampling strategy requires 13 USVs, and
497 thus would be the most costly of the observing scenarios. Although run ‘x13_10Y_W’
498 demonstrates the highest reduction in bias out of all runs, the ‘zigzag’ runs still reduce bias in the
499 Southern Ocean by 44-65 % (vs. 77 % for run ‘x13_10Y_W’).

500 Overall, the ‘zigzag’ runs include significantly fewer observations, require less USVs,
501 collect samples over the same duration, or even half the time as run ‘x13_10Y_W’, cover areas
502 north of 55°S and within the ice-free zone, and show major improvement in the reconstruction of
503 pCO₂, attested to by reductions in both bias and RMSE. The ‘zigzag’ runs also closely match both
504 the global and Southern Ocean ‘model truth’ air-sea CO₂ flux for the duration of sample additions
505 (**Figs. 10, S12**). It also appears that the ‘zigzag’ runs generally have a greater impact on both the
506 pCO₂ reconstruction and the air-sea flux further back in time, starting to deviate from the SOCAT
507 baseline earlier compared to the ‘one-latitude’ runs (**Figs. 6, 9, 10, S6, S10, S11, S12**). Even the
508 ‘zigzag’ scenarios with the least number of USVs (e.g., ‘Z_x4_10Y_YR’) reduces Southern Ocean
509 reconstruction bias and RMSE by up to 46 % and 13 %, respectively, and could provide a basis
510 for realistic future Southern Ocean pCO₂ sampling campaigns.

511 The main motivation for improving surface ocean pCO₂ reconstructions is so that we can
512 more accurately estimate the current and future oceanic uptake of anthropogenic carbon. The
513 Southern Ocean is a significant carbon sink, but estimates of the air-sea CO₂ flux diverge



514 substantially in this region (Takahashi et al., 2009; Landschützer et al., 2014, 2015; Rödenbeck et
515 al., 2015; Williams et al., 2017; Gray et al., 2018; Gruber et al., 2019; Bushinsky et al., 2019; Long
516 et al., 2021; Fay and McKinley, 2021; Wu et al., 2022). Southern Ocean estimates incorporating
517 observations from biogeochemical floats have shown a significantly weaker sink compared to
518 those based only on observations from ships (Williams et al., 2017; Gray et al., 2018; Bushinsky
519 et al., 2019). Bushinsky et al. (2019) performed similar sampling experiments as presented here,
520 by comparing ML surface ocean pCO₂ reconstructions based on SOCAT alone vs. additional
521 Southern Ocean floats. They showed that by adding the floats, the Southern Ocean carbon sink
522 (mean of the period of float additions; 2015-2017) decreased (weakened) by 0.4 Pg C yr⁻¹. In
523 contrast, by using a model testbed, we show that adding USVs increased (strengthened) the
524 Southern Ocean and global ocean sink by up to 0.1 Pg C yr⁻¹ (**Figs. 10, S12; Table S3**), which is
525 a significant fraction of the uncertainty in the global ocean carbon sink (0.4 Pg C yr⁻¹;
526 Friedlingstein et al., 2022). Fed with real-world SOCAT data, the global mean air-sea flux estimate
527 from the pCO₂-Residual method is similar to other available products (Bennington et al., 2022a),
528 suggesting that other products may also underestimate the Southern Ocean carbon sink due to the
529 spatio-temporal distribution of SOCAT data. Our experiments suggest that targeted USV
530 observations could reduce this underestimation of the ocean carbon sink.

531 What else can we learn using the model testbed? The SOCAT baseline demonstrates a
532 weakening of the global and Southern Ocean carbon sink in the 2000s (**Figs. 10, S12**), which is in
533 agreement with various data products using real-world SOCAT data (e.g., Gruber et al., 2019;
534 Landschützer et al., 2015; Bushinsky et al., 2019; Bennington et al., 2022; Gloege et al., 2022).
535 Peaks in bias and RMSE coincide in time with the weakening sink (**Figs. 6d, 9d**). As shown by
536 **Figure 10**, this ‘low sink’ is significantly exaggerated compared to the ‘model truth’. To better
537 understand this discrepancy, we performed an additional experiment based on run
538 ‘Z_x10_5Y_YR’, but assumed sampling every year for the entire testbed period (i.e., 1982-2016).
539 The results from this experiment show a significant reduction in the temporal variability of
540 reconstruction bias; with the additional USV sampling, the reconstructed Southern Ocean air-sea
541 CO₂ flux closely matches the ‘model truth’ for the entire testbed duration (**Fig. S14**). This suggests
542 that the large decadal variability of air-sea CO₂ fluxes since the 1980s, and the weak anomaly in
543 the Southern Ocean carbon sink in the early 2000s (Le Quéré et al., 2007; Landschützer et al.,
544 2015; Gruber et al., 2019; Bennington et al., 2022a,b; Friedlingstein et al., 2022), may be at least



545 partially attributable to undersampling of the Southern Ocean. We will further explore this issue
546 in future work. Still, this preliminary experiment suggests that interpretations of trends and
547 variability of the global and Southern Ocean carbon sink should be considered with caution.

548 **5. Conclusions**

549 By using the Large Ensemble Testbed (LET), we show that targeted meridional and winter
550 sampling in the Southern Ocean can improve global and Southern Ocean ML surface ocean pCO₂
551 reconstructions. Significant improvements are possible by raising the global pCO₂ data density by
552 as little as 0.02-0.04 %. Further, we find that this modest amount of additional Saildrone USV
553 sampling increases the global and Southern Ocean air-sea CO₂ flux by up to 0.1 Pg C yr⁻¹, 25 %
554 of the uncertainty in the ocean carbon sink. Our findings are consistent with previous studies
555 suggesting that additional observations during southern hemisphere winter months and covering
556 meridional gradients can reduce uncertainties and biases in the reconstructions (Lenton et al., 2006;
557 Monteiro et al., 2010; Djeutchouang et al., 2022; Mackay et al., 2022). As opposed to other
558 autonomous platform approaches, Saildrone USVs obtain in situ pCO₂ observations with
559 uncertainties equivalent to the highest-quality observations collected by research ships ($\pm 2 \mu\text{atm}$;
560 Sabine et al., 2020; Sutton et al., 2021), and can operate at a high speed so that the spatial extent
561 and seasonal cycle of meridional gradients can be covered. The approach of combining high-
562 accuracy Saildrone USV and SOCAT observations represents thus a promising solution to improve
563 future surface ocean pCO₂ reconstructions and the accuracy of the ocean carbon sink. Lastly, we
564 show that the large variability in bias, and the weakening of the global and Southern Ocean carbon
565 sink in the 2000s, may be partially an artefact of Southern Ocean undersampling.

566 **Code availability**

567 Data analysis scripts will be made available in a GitHub repository upon publication.

568 **Data availability**

569 The Large Ensemble Testbed is publicly available at
570 https://figshare.com/collections/Large_ensemble_pCO2_testbed/4568555.

571



572 **Author contribution**

573 THH, GAM and AJS designed the experiments, and THH performed the simulations. THH, ARF
574 and LG developed the code. THH and ARF calculated the air-sea fluxes. THH prepared the
575 manuscript with contributions from all co-authors.

576 **Competing interests**

577 The authors declare that they have no conflict of interest.

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583

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