**RC2**: ['Comment on bg-2023-2'](https://editor.copernicus.org/index.php?_mdl=msover_md&_jrl=11&_lcm=oc158lcm159n&_ms=108842&salt=11357532541578974431#RC2), Anonymous Referee #2, 31 May 2023  [reply](https://editor.copernicus.org/index.php?_mdl=msover_md&_jrl=11&_lcm=oc116lcm117t&_acm=open&_ms=108842&p=245118&salt=50825753296784390)

General comments

This manuscript describes an interesting study of movement of coral rubble under waves. The lab and field measurements of rubble movement seem to have been generally well-executed, the combination of lab and field measurements is informative, the figures show interesting patterns, and the datasets have a lot of potential. While I think the manuscript has potential to ultimately be a nice contribution, I do have serious concerns about aspects of the analysis and the way some of the methods and results are presented in this submission. My major concerns are around the treatment of wave period, which is very different (factor of up to 10) in the lab versus in the field, and the use of orbital velocity as the hydrodynamic parameter against which rubble movement is plotted and assessed.

The physics of rubble motion under waves isn’t fully explained in the manuscript so I provide some background here. The total force on an object under waves is the sum of two components: the inertial force and the drag force. The drag force is proportional to orbital velocity squared and dominates only if the orbital excursion is substantially larger than the size of the object (Keulegan Carpenter number KC>1). From my back-of-the-envelope calculations this seems to be the case in much of the field data presented. However, if the orbital excursion is smaller than the object size (KC<1), the inertial force is the dominant force on the obstacle. The inertial force is proportion to the fluid ACCELERATION, which is the orbital velocity multiplied by the wave frequency (2\*pi /PERIOD). By my calculations the inertial force should be the dominant force for many of the lab flume conditions. The wave period is therefore a critical parameter for this problem, in addition to the orbital velocity.

Because of the very different wave periods between the lab and the field, comparisons between the two datasets need to be done very carefully/cautiously. Additionally, in the lab flume, it seems the period was changed (somewhat arbitrarily when breaking was observed), but the combinations of wave height and period are not reported in the manuscript. A table of the combinations of conditions in the lab flume experiments needs to be reported, along with corresponding bottom orbital excursions, velocities, accelerations. This will allow comparison of orbital excursions with rubble sizes which will inform as to whether drag (proportional to velocity squared) or inertial force (proportional to acceleration) is the relevant force. Ideally, the probability of movement would be plotted against a measure of the total force rather than velocity. There is a nice paper by Viehman et al. (2018) that lays out these forces on rubble. It is cited briefly in the introduction, but I think it could be a useful reference for sorting out this issue of dominant forces.

The figures are generally well-constructed and the manuscript text is well-organized and generally well-written.

I provide a few specific comments below, but I have not provided line-by-line comments at this point because of the critical major issues described above.

Our response:

We thank Reviewer 2 for their review of the manuscript and the time taken to provide comments. We thank the reviewer for their queries in relation to the methodology, which has led to an improved manuscript through inclusion of additional information, though we note that the results do not change substantially. We believe the review comments regarding inertial forces are due to an omission on our part in the original manuscript, where the coral diameter was never stated. Consequently, we believe the reviewer may have anticipated significant inertia forces in the laboratory assuming coral diameters of 0.04-0.2 m, instead of coral diameters of 0.01-0.02 m. The reviewer is correct that coral diameters of the former size range would lead to significant inertia forces. We apologise that the coral diameter was not previously included in the original manuscript, but rather only the lengths were specified.

The actual coral diameters used in the lab do not lead to significant inertia forces for the wave conditions that lead to rubble movement. This is addressed at length in these comments, where we have derived a new relationship for the contribution of the inertia force to the total maximum force as a proportion of the drag force. We have included a table of wave conditions used in the flume (Table A1, Attachment A) and the field (Table B1, Attachment B). These show the average coral rubble diameter, significant wave height, period, water depth, and corresponding velocities, inertia force component and bottom orbital excursions for all wave conditions used in determining the relationship between velocity and movement. These can be included in the Supplementary Material in a revised manuscript.

These tables highlight in which conditions there is potential for the inertia force to be the dominant force as opposed to drag, based on an average coral diameter of 1.64 cm (range ~1-2 cm) in the flume and 1.69 cm (range ~1-3 cm) in the field. The calculations are outlined below.

Assuming the drag and inertia coefficients have the same magnitude, the ratio of the maximum inertia force to the maximum drag force is given by Dean and Dalrymple (1991) as:

*where*  ; *KC = Keulegan-Carpenter number , u = maximum orbital wave velocity, T = wave period ∅ = rubble diameter*

*Hence*

The maximum total force is again given by Dean and Dalrymple (1991), noting that the drag and inertia forces are out of phase,

*FT = maximum total force, FD = drag force, F*I *=inertia force*

*which can be written as*

*or*

The last term (gives the contribution of the inertia force to the total maximum force as a proportion of the drag force. This inertia component is shown in the second- and third-last columns of Tables A1 and B1.

When the inertia component (contributes more than 25% of the drag force to the total force, we consider that to be a potentially significant contribution. For example, when FI=FD, the contribution to the maximum total force from the inertia force is 0.25FD. It should be noted that this relationship is only valid for , and when , the maximum force is pure inertia, meaning it is the dominant force (Dean and Dalrymple, 1991). The maximum force is shown in the last column of Tables A1 and B1.

Table A1 (Attachment A), shows that only 18 out of 71 wave conditions in the flume have the potential for the inertia force to be significant, and of those, only 6 had a ratio >2, meaning that nearly all the wave conditions in the flume led to drag-dominated conditions. Table B1 (in Attachment B), confirms that only 1 out of 90 wave conditions in the field had the potential for inertia to be significant. This condition corresponded to a very low velocity (0.016 m/s), far from the reported transport threshold velocities. Thus, further investigations were made for flume conditions (see below) but not field conditions.

The above calculations were applied to the dataset used to determine the probabilities of rocking, flipping and transport in the flume (for free and interlocked rubble), so that each individual rubble piece’s diameter could be used in place of the average diameter of 1.64 cm. Figure A1 (Attachment A) shows the relationship between bottom orbital velocity and the FI/FD ratio for every individual case in the flume. There is a general trend in which FI/FD decreases as both velocity and the likelihood of movement increases. The dataset includes 7,593 rows and of these, 2,081 had the potential for inertia forces to be significant based on the above calculations. However, in most (90%) of the 2,081 identified cases, there was no movement of the rubble being tested (Figure A1).

In 9.3% of cases (195 of 2,081), rocking movements only were recorded (Figure A1). For these cases, the contribution of inertia force to the total force ranged from 25% to 100% or more of that contributed by the drag force. The highest velocity represented in these cases was 0.2 m/s, though the large majority were much lower. Thus, at velocities <0.2 m/s, there is the potential for inertia forces to contribute to causing rocking motions. But, at a velocity of 0.2 m/s the contribution of inertia is still only 25% of the drag force (not dominant). This can be indicated on the plot of velocity vs probability of rocking (Figure 3a) in a revised manuscript.

In any case, these instances of ‘rocking’ were considered as ‘no movement’ in the analysis determining the probability of transport (see Table 1 of the manuscript) and thus have no bearing on the 50% or 90% thresholds of transport reported.

Only in 0.9% of the cases where inertia forces were potentially significant (18 of 2,081), was transport/flipping recorded (Figures A2-A4, Table A2). For these cases, the average contribution of inertia forces to the total force was 36% of the drag force (Table A2, Figure A3). The highest velocity represented in these cases was 0.16 m/s (Table A2). This indicates that at very low velocities <0.16 m/s, there is the potential for inertia forces to be significant. However, this cut-off is well below the 50% and 90% thresholds of transport that are reported in the paper, and at those velocities, i.e., ≥0.3 m/s, the inertia component contributes as little as 0.1% and at most 4.9% to the total force, and the threshold of motion conditions are thus drag dominated (Figure A5). Furthermore, while inertial forces do have the potential to be dominant at velocities <0.16 m/s in the flume, the field results (drag-dominated conditions), indicate higher probabilities of transport (~30% probability of movement compared to ~10% in the flume) at that velocity of ~0.16 m/s, suggesting that the flume results presented in terms of bottom orbital velocity are conservative estimates.

The reviewer also states that “ideally, the probability of movement would be plotted against a measure of the total force rather than velocity”. We disagree that this is necessary, based on the above calculations and justification, that can be included in Supplementary Material. The total force is also directly dependent on the length of the coral rubble pieces. The threshold of motion is not directly dependent on that length, since, for a given velocity, doubling the length doubles both the force and the resisting force. The observed thresholds are indirectly influenced by length through the greater probability of a longer length piece having a shape that is more stable due to curvature or branches. Furthermore, we feel a plot of movement against velocity is more widely interpretable to a broad coral reef scientist audience, rather than only to those with a knowledge of sediment transport and hydrodynamics, as flow speed is commonly measured on reefs while forces are not. However, we do include tables showing the inertial force component for each velocity in Attachments A and B, and plots of how the inertia force component changes with velocity and movement (like Figure A1 or A5), which can be included in a revised manuscript (Supplementary or main).

Specific comments

Abstract lines 10-15, and corresponding sections of the text. Comparisons rubble motion in lab and field studies with respect to orbital velocities are flawed, due to the reasons outlined above in my general comments. Also, rubble size is an important determinant of when motion occurs, so I didn’t understand why a single probability of motion at a single velocity was reported.

Diagram – the statement that rubble is mobilized for orbital velocities greater than 0.4 m/s is too simplistic since we know (and the results show) there is a strong dependence on rubble size. There will also be a dependence on wave period for some rubble size classes and wave conditions due to inertial force being the dominant force.

We thank the reviewer for these more detailed comments. As described above, the comparisons between flume and field are made with respect to the 50% and 90% thresholds of transport, and at those velocities, i.e., ≥0.3 m/s, the inertia component contributes as little as 0.1% and at most 4.9% to the total force in the flume (Figure A5), and conditions are thus drag dominated. At and above this same velocity threshold in the field, the inertia component contributes on average 0.08% and a maximum of 1% to the total force (Table B1). Thus, comparisons between flume and field are valid despite differences in wave period. With respect to variation in rubble length, the graphical abstract is a summary of the information provided in the paper, and the value given is the 90% threshold averaged across substrates, morphologies and rubble lengths from 4–23 cm (and diameters ~1-3 cm). This has now been highlighted in the footnote of the graphical abstract (Attachment D). The figures and tables in the manuscript provide the detail around rubble movement with respect to varying rubble lengths.

Page 6, line 5-10. A table of wave conditions in the flume (height, period, water depth) is needed. The description of how wave period was increased when waves started to break seems very arbitrary. Changing the wave period for the same wave height will alter the orbital velocity, orbital excursion, and acceleration.

Linear wave theory and the Soulsby model are less accurate once wave breaking occurs. Breaking wave conditions were thus avoided by changing the wave conditions to reduce the wave steepness. This alters the orbital velocity and forces, but has no bearing on the analysis, merely the order in which different conditions are achieved.

We have included a table of wave conditions used in the flume (Table A1, Attachment A). These show the average coral rubble diameter, significant wave height, period, water depth, and corresponding velocities, inertia force component and bottom orbital excursions for all wave conditions used in determining the relationship between velocity and movement. These can be included in the Supplementary Material in a revised manuscript.

P6, Line 17-20. Linear wave theory is generally used to estimate bottom orbital velocities, accelerations, excursions. The approach described here (Soulsby cosine approximation) is non-standard and I didn’t understand why it was used in preference to linear wave theory.

The Soulsby cosine approximation is a one-step method to estimate bottom orbital velocity without solving the dispersion relationship, thus it was simpler to implement. A comparison of bottom orbital velocities estimated from linear wave theory compared to the Soulsby cosine approximation was conducted prior to submission of the original manuscript, for the wave conditions used in the flume. This relationship is shown in Figure C1 of Attachment C and can be included in a revised manuscript.

Velocities were found to be almost identical between methods, with an average change of 0.4 cm/s (55% <0.5 cm/s difference, 90% <1 cm/s difference) and a maximum change of 1.3 cm/s. A table of comparisons of these velocity estimations for each wave condition used in the flume is also included in Table A1 of Attachment A.

Based on the above relationship, we do not deem it necessary to re-run flume analyses using linear wave theory in place of the Soulsby Cosine Approximation.

P6, Line 19-20. The last statement on this page is very concerning: “Wave orbital velocities obtained in the flume were comparable to those measured in the field, hence scaling of the analyses was not required.” As I explained above, the forces on the rubble are the relevant quantity that should be compared in the lab vs the field, and related to rubble motion. The velocities can be the same but if other important parameters are different (e.g., wave period) then direct comparisons of laboratory and field results will not be possible. Careful consideration of scaling is always required when relating lab flume experiments and the field situation.

Our response to the reviewer’s general comment addresses this concern. As pointed out by the reviewer, total force depends on both the inertia force component and drag force component, and while the inertia component is dependent on velocity and wave period, the drag component is only dependant on the velocity (see equations outlined above). Thus, where conditions are determined to be drag dominated, rubble movement only depends on the velocity. As outlined in our response above, our investigation found minor issues with inertia becoming potentially significant at very low velocities in the flume, and some rubble pieces (18 cases) transporting in those conditions, but the contribution of inertia forces to total force in these cases was relatively small. Furthermore, the 50% and 90% thresholds of ≥0.3 m/s represent wave conditions that are drag dominated as in the field. Thus, despite differences in the wave period between the field and flume, meaningful comparisons of these movement thresholds can be made. Since inertial forces are negligible at the 50% and 90% thresholds, the laboratory experiments do not have scale effects, since the coral rubble has the same scale in the laboratory and field and the velocity and Reynolds numbers therefore also have the same magnitudes.

P8. Line 10. Unclear that the shallow water approximation is valid here for computing wavenumber k. There is readily available code available to calculate k from frequency and depth using the general/complete linear wave theory dispersion relation.

We thank the reviewer for this comment and agree that in some circumstances where the wave period is very short, the shallow water approximation should be avoided. We have now solved the dispersion relation to calculate the wave number (k), and the near-bed orbital velocities in the field have been updated using the new k values.

The wave number (*k*) was determined by solving the dispersion relation

where ω is the wave radian frequency (2/T­­p), *h* is water depth, and *g* acceleration due to gravity.

Attachment D includes a plot of the velocity as it appears in the original manuscript against the velocity using the wave number as calculated above (Figure D2), showing that conditions where the shortest wave periods were observed (~4-5 s) result in the greatest change. In a revised manuscript, the results will change only very slightly. The analysis of 50% and 90% thresholds was re-run and found to have reduced slightly from 0.34 and 0.55 m/s, respectively (original manuscript), to 0.3 and 0.47 m/s, respectively, making the new predictions more like those estimated for the flume. Figure D3 depicts Figure 4 as it would appear in a revised manuscript (with corrected u values), next to the original figure.

P8. Iine 32. Unclear what is meant by peak wave orbital velocity here. Do you mean the maximum 30-min significant wave height over the 3-day period? This is not truly the peak wave orbital velocity, which would require going back to the original time series for each burst.

The peak wave orbital velocity in this manuscript is calculated based on the significant wave height and the peak wave period from the wave spectrum, and we have selected the fastest peak wave orbital velocity per day for the regression with rubble movement. We agree that the use of ‘peak’ in the referenced section of the manuscript may be confusing.

We can amend this text for clarity to read:

“From the 30-minute runs across each 3-day period and site (144 each period and site), the fastest wave orbital velocity (calculated from peak wave height and period) was selected for each day, to regress with observed rubble movement on that day. A total of the 90 fastest wave orbital velocities were thus used in the analyses including all days (1 velocity per day for 3 days across 15 sites in two seasons), and 30 in the analyses for day 1 only (1 velocity for each ‘day 1’ across 15 sites in two seasons).”

P9. Results. Wave periods need to be reported and used appropriately in the analysis!

Tables of wave conditions in the flume and field, including average coral rubble diameter, wave height, period and water depth can be provided in the Supplementary Material in a revised manuscript, and are included with this response as Attachment A and B.

A section in the methods has been added to clarify that the dominant forces on rubble under each wave condition in the flume and field has been considered, and the vast majority found to be drag-dominated, meaning that appropriate comparisons can be made across trials despite varying wave periods. This section in a revised manuscript could read:

“Total force depends on the inertia force component and drag force component, and while the inertia component is dependent on velocity and wave period, the drag component is only dependant on the velocity. Thus, where conditions are determined to be drag dominated, rubble movement only depends on the velocity. To determine drag-dominance and ensure that wave orbital velocity was an appropriate predictor for rubble movement, we derived a relationship for the contribution of the inertia force to the total maximum force as a proportion of the drag force for all wave conditions for each case (i.e., movement trial) (see Supplementary Material). Assuming the drag and inertia coefficients have the same magnitude, the ratio of the maximum inertia force to the maximum drag force is given by Dean and Dalrymple (1991) as:

*where*  ; *KC = Keulegan-Carpenter number # , u = maximum orbital wave velocity,*

*T = wave period ∅ = rubble diameter*

Hence

The maximum total force is again given by Dean and Dalrymple (1991), noting that the drag and inertia forces are out of phase,

*FT = maximum total force, FD = drag force, F*I *=inertia force)*

which can be written as

or

The last term gives the contribution of the inertia force to the total maximum force as a proportion of the drag force. When the inertia component (contributes more than 25% of the drag force to the total force, we consider that to be a potentially significant contribution. For example, when FI=FD, the contribution to the maximum total force from the inertia force is 0.25FD. The above relationship is only valid however, for , and when the maximum force is pure inertia (Dean and Dalrymple, 1991).

Inertial forces were found to be negligible at the 50% and 90% thresholds (see Supplementary Material), and thus the flume experiments do not have scale effects. The coral rubble has the same scale in the flume and field and the velocity and Reynolds numbers therefore also have the same magnitudes.”

Fig 4. Bottom orbital excursion and accelerations should be shown also, for the reasons outlined in my General Comments

We have included a table of wave conditions used in the flume (Table A1, Attachment A) and the field (Table B1, Attachment B). These show the average coral rubble diameter, wave height, period, water depth, and corresponding velocities, inertial force component and bottom orbital excursions for all wave conditions used in determining the relationship between velocity and movement. These can be included in the Supplementary Material in a revised manuscript. As one of the key goals of this work is to inform management around reef restoration, we feel that the presentation of the results (figures) as a function of velocity is more broadly comprehendible to managers than are forces.